LETTER TO THE EDITOR

The ALMA-ALPINE [CII] survey: Kennicutt-Schmidt relation in four massive main-sequence galaxies at z∼4.5


(Affiliations can be found after the references)

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ABSTRACT

Aims. The Kennicutt-Schmidt (KS) relation between the gas and the star formation rate (SFR) surface density ($\Sigma_{\text{gas}}$−$\Sigma_{\text{SFR}}$) is essential to understand star formation processes in galaxies. To date, it has been measured up to z≈2.5 in main-sequence galaxies. In this letter our aim is to put constraints at z≈4.5 using a sample of four massive main-sequence galaxies observed by ALMA at high resolution.

Methods. We obtained ∼0.3′′-resolution [CII] and continuum maps of our objects, which we then converted into gas and obscured SFR surface density maps. In addition, we produced unobscured SFR surface density maps by convolving Hubble ancillary data in the rest-frame UV. We then derived the average $\Sigma_{\text{SFR}}$ in various $\Sigma_{\text{gas}}$ bins, and estimated the uncertainties using a Monte Carlo sampling.

Results. Our galaxy sample follows the KS relation measured in main-sequence galaxies at lower redshift, and is slightly lower than the predictions from simulations. Our data points probe the high end both in terms of $\Sigma_{\text{gas}}$ and $\Sigma_{\text{SFR}}$, and gas depletion timescales (285-843 Myr) remain similar to z≈2 objects. However, three of our objects are clearly morphologically disturbed, and we could have expected shorter gas depletion timescales (<100 Myr) similar to merger-driven starbursts at lower redshifts. This suggests that the mechanisms triggering starbursts at high redshift may be different than in the low- and intermediate-z Universe.

Key words. Galaxies: high-redshift – Galaxies: ISM – Galaxies: star formation – Submillimeter: galaxies – Submillimeter: ISM

1. Introduction

The Kennicutt-Schmidt (KS) empirical relation (Schmidt 1963; Kennicutt 1998; de los Reyes & Kennicutt 2019) linking the gas and the star formation rate (SFR) surface densities ($\Sigma_{\text{gas}}$−$\Sigma_{\text{SFR}}$) is a key tool for understanding the star formation in galaxies across cosmic times. This relation has been vastly explored in the local Universe including at sub-galactic scales (e.g., Leroy et al. 2013; Pessa et al. 2021; Sun et al. 2023). These studies have also shown that star formation is mainly correlated with the molecular gas (e.g., Bigiel et al. 2008). At higher redshift, these measurements are difficult, since they require resolved maps of the molecular gas, usually using the CO rotational lines, together with reliable star formation maps (e.g., Molina et al. 2019). Since current observing facilities are not sensitive enough to detect the atomic hydrogen at 21 cm in the high-redshift Universe, previous and current studies mainly focused on the molecular KS relation. In the rest of this letter, we only discuss this molecular version. Measurements integrated at the full-galaxy scale up to z≈2.5 showed that most galaxies lie on the local KS relation, but at higher gas surface density (e.g., Tacconi et al. 2013; Freundlich et al. 2019). Most of these high-redshift galaxies also follow a SFR–stellar mass (M*) relation, also known as the main sequence of star-forming galaxies (e.g., Noeske et al. 2007; Elbaz et al. 2007). The normalization of this main sequence increases rapidly with increasing redshift (e.g., Schreiber et al. 2015) together with the gas fraction (e.g., Magdis et al. 2012; Saintonge et al. 2013; Béthermin et al. 2015), suggesting that the larger gas reservoirs are driving the higher specific SFR (sSFR=SFR/M*) observed at high z. However, a small population of starbursts with a SFR excess compared to the KS relation of main-sequence galaxies was found by Genzel et al. (2010) and Daddi et al. (2010), among others. Resolved studies of high-z starbursts confirmed the $\Sigma_{\text{SFR}}$ excess at sub-galactic scale in these systems (e.g., Freundlich et al. 2013; Rawle et al. 2014; Hodge et al. 2015). Another population of starbursts with an SFR excess was also identified above the main sequence (e.g., Rodighiero et al. 2011). The starburst populations observed in both relations are suspected to be driven by mergers (e.g., Sargent et al. 2014; Cibinel et al. 2019). To date, the KS relation in z≈2.5 main-sequence galaxies has remained unexplored. However, the Atacama Large Millimeter Array (ALMA) has opened new perspectives to explore earlier times. In particular, the bright 158 µm rest-frame [CII] line is now easily observable from the ground at z≈4, and can be used as a gas tracer (e.g., Zanella et al. 2018). Recently, Vallini et al. (2024) published a study on the KS relation in five z≈7 bright Lyman break galaxies (LBGs), but the main-sequence nature of these galaxies remains unclear. The ALMA large program to investigate [CII] at early times (ALPINE, Le Fèvre et al. 2020; Article number, page 1 of 9
Béthermin et al. 2020; Faisst et al. 2020) built a sample of 118 main-sequence galaxies at $4<z<6$, observed in [CII] and continuum at low angular resolution ($\sim 1''$, marginally or not resolved). In this sample, Dessauges-Zavadsky et al. (2020) found a flattening of the evolution of the gas fraction with redshift, similar to that observed for the sSFR (Khusanova et al. 2021). In contrast, Jones et al. (2021) and Romano et al. (2021) estimated that a high fraction ($\sim 40$%) of these objects exhibits morpho-kinematical signatures of mergers despite being on the main sequence, suggesting that the mechanisms driving star formation in the $z=4$ Universe may differ from lower redshifts.

In this letter we explore the KS relation at $z\sim 4.5$ using a sample of four ALPINE galaxies followed up at higher resolution ($\sim 0.3$ arcsec, 2 kpc) by ALMA. In Sect. 2 we describe our observations and the data analysis. We then present our new results on the KS relation in Sect. 3. Finally, we discuss them and conclude in Sect. 4. We assume a flat ACDM cosmology ($h_0=0.7$, $\Omega_m=0.3$) and a Chabrier initial mass function (IMF).

2. Observations and data analysis

We observed the three brightest ALPINE objects (for a full discussion of the selection, see Devereaux et al. 2023) in [CII] (DEIMOS_COSMOS_818760, DEIMOS_COSMOS_873756, vuds_cosmos_5101218326), using the C43-3 (~0.4'', 73 min) and C43-5 (~0.2'', 189 min) configurations (2019.1.00226.S). This is only a small fraction (17%) of the 30 h initially planned to study the dynamics, but it is sufficient for the goal of this letter. In addition, we observed a massive and bright ALPINE rotator candidate VC5110377875 (2022.1.01118.S) in C43-4 (~0.3'') configuration during 286 min. These observations were supposed to be followed by higher-resolution observations (C43-7, ~0.07''), which were not completed.

The data were calibrated by the standard observatory pipeline, and imaged using the common astronomy software applications for radio astronomy (CASA; CASA Team et al. 2022). We produced continuum maps after excluding the [CII]-contaminated channels and the [CII] momentum-0 maps (i.e., velocity-integrated line flux maps) after subtracting the continuum in Fourier space. For DC818760, DC873756, and VC5101218326 we also included the compact-configuration visibilities from the initial ALPINE observations to recover the large-scale components. This was not necessary for VC5110377875 since the full ALPINE integrated flux is already recovered by the new high-resolution observations alone. The data reduction is described in detail in a companion paper focusing on the morpho-kinematical analysis of these objects (Devereaux et al. 2023). The source properties and the achieved ALMA performance are listed in Table 1.

The [CII] flux is then used to derive the gas mass, while the rest-frame far-infrared continuum provides the dust obscured SFR. While initially considered to be an SFR tracer (e.g., De Looze et al. 2014; Capak et al. 2015), recent theoretical and observational studies pointed out that [CII] is more tightly connected to the molecular gas mass (e.g., Zanella et al. 2018; Madden et al. 2020; Vizgan et al. 2021; D’Eugenio et al. 2023; Ramambason et al. 2023), and correlates with SFR through the KS relation (e.g., Ferrara et al. 2019). The [CII] line also comes from the neutral and ionized medium, but their contribution is expected to be small in massive high-redshift galaxies (e.g., Vizgan et al. 2022). In addition, starbursting systems with short depletion timescales ($\text{M}_{\text{gas}}$/SFR~100 Myr) tend to have low [CII]-to-IR luminosity ratios (Díaz-Santos et al. 2013; Gallberg et al. 2015), which should not be the case for an SFR tracer. A theoretical discussion about this [CII] deficit in starbursts can be found in Vallini et al. (2021). Finally, integrated [CII]-based gas masses of the ALPINE sample agree with dust-based measurements and dynamical estimates after subtracting the stellar masses (Dessauges-Zavadsky et al. 2020). A systematic comparison of the various tracers (CO, [CII], [CII], and dust) in high-z lensed dusty star-forming galaxies, with higher SFRs than our targets by a factor of 2–50, also found a good agreement between them (Gururajan et al. 2023). Contrary to CO, the [CII] line luminosity has a weak dependence on metallicity and is sensitive to CO-dark gas as shown by studies in nearby low-metallicity dwarfs (Madden et al. 2020; Ramambason et al. 2023).

The surface density ($\Sigma_{\text{gas}}$) is derived from the [CII] moment-0 map $m_{\text{[CII]}}$ in Jy km s$^{-1}$ beam$^{-1}$ using

$$\Sigma_{\text{gas}} = \frac{\alpha_{\text{[CII]}}}{D_{\Lambda}^2 A_{\text{beam}}} \left( \frac{1.04 \times 10^{-3}}{L_{\odot} \text{ s}} \right) \frac{L_{\odot}}{\text{ GHz Mpc}^3 \text{ Jy km}} \frac{D_{\Lambda}^2 A_{\text{beam}} m_{\text{[CII]}}}{100 \text{ Myr}}$$

where $\alpha_{\text{[CII]}}$ is the [CII]-to-gas conversion factor (31 M$_{\odot}$/L$_{\odot}$, Zanella et al. 2018). This conversion factor has been cross-calibrated using CO up to $z=2$ to measure the molecular gas mass. If the small expected fractional contribution from other phases to the [CII] luminosity in their sample and in our objects are similar, we should thus obtain directly a molecular gas mass corrected from the contribution of the rest of the interstellar medium. The parameter $D_{\Lambda}$ is the angular diameter distance and $A_{\text{beam}}$ the solid angle of the synthesized beam defined as the integral of a beam after normalizing its peak to unity, $D_{\Lambda}^2 A_{\text{beam}}$ being the physical area associated with the synthesized beam. The following factors in Eq. 1 correspond to the conversion from line flux to luminosity (Solomon et al. 1992) with $D_{\Lambda}$ being the luminosity distance and $v_{\text{phys}}$ the observed frequency.

The SFR surface density ($\Sigma_{\text{SFR}}$) is the second quantity involved in the KS relation. In galaxies with a non-negligible dust content as ALPINE galaxies (Fudamoto et al. 2020), we can estimate the total SFR by combining the obscured SFR probed by the far-infrared ($S_{\text{SFR}}$) and unobscured SFR seen in the UV ($S_{\text{SFR}}$). The total SFR is the sum of these two values, and can be derived using (Madau & Dickinson 2014)

$$S_{\text{FIR}} = S_{\text{FIR}} + S_{\text{FIR}} = \frac{k_{\text{IR}}}{k_{\text{UV}}} L_{\text{UV}} + k_{\text{IR}} L_{\text{IR}}$$

$$S_{\text{FIR}} = S_{\text{FIR}} + S_{\text{FIR}}$$

where $S_{\text{FIR}}$ is the rest-frame $1500 \text{ Å}$ luminosity and $L_{\text{IR}}$ the total $8-1000 \text{ μm}$ IR luminosity; $k_{\text{IR}}$ and $k_{\text{UV}}$ are the conversion factors with a value of $1.02 \times 10^{-10} \text{ M}_\odot L_{\odot}$ and $1.47 \times 10^{-10} \text{ M}_\odot L_{\odot}$ after converting to the Chabrier IMF.

The $158 \text{ μm}$ rest-frame continuum map ($m_{158}$) is converted into obscured SFR surface density ($\Sigma_{\text{SFR}}$) using

$$\Sigma_{\text{SFR}} = k_{\text{IR}} \frac{D_{\Lambda}^2 A_{\text{beam}}}{4 \pi D_{\text{cont}}^2} L_{\text{cont}} n_{\text{cont}} m_{158}$$

where $n_{\text{cont}}$ is the rest-frame continuum frequency, and $D_{\text{cont}}$ is the ratio of the total luminosity to the $158 \text{ μm}$ rest-frame monochromatic luminosity. We use the value of 1/0.113 computed by Béthermin et al. (2020) based on Herschel stacking. This constant conversion factor assumes implicitly a constant dust temperature in our objects, and variations could lead to systematic effects on $\Sigma_{\text{SFR}}$ estimates (Cochrane et al. 2022). Unfortunately, high-resolution observations at higher frequency to constrain the
Table 1. Summary of the observations and achieved performance. The $\sigma_{\text{cont}}$ and $\sigma_{\text{CII}}$ Column are the noise of the continuum map and the [CII] moment-0 map, respectively. The $5\sigma$ $\Sigma_{\text{gas}}$ limit is derived from the gas surface density map obtained after applying the conversion from Eq. 1.

<table>
<thead>
<tr>
<th>Source</th>
<th>RA</th>
<th>Dec</th>
<th>$z_{\text{CII}}$</th>
<th>beam size</th>
<th>$\sigma_{\text{cont}}$</th>
<th>$\sigma_{\text{CII}}$</th>
<th>$5\sigma$ $\Sigma_{\text{gas}}$ limit</th>
</tr>
</thead>
<tbody>
<tr>
<td>DC818760</td>
<td>10:01:54.86</td>
<td>+2:32:31.54</td>
<td>4.5613</td>
<td>0.30x0.23</td>
<td>31</td>
<td>0.068</td>
<td>2000</td>
</tr>
<tr>
<td>DC873756</td>
<td>10:00:07.21</td>
<td>+2:37:40.20</td>
<td>4.5457</td>
<td>0.31x0.25</td>
<td>26</td>
<td>0.077</td>
<td>1940</td>
</tr>
<tr>
<td>VC5101218326</td>
<td>10:01:12.50</td>
<td>+2:18:52.72</td>
<td>4.5739</td>
<td>0.29x0.23</td>
<td>31</td>
<td>0.074</td>
<td>1920</td>
</tr>
<tr>
<td>VC5110377875</td>
<td>10:01:32.33</td>
<td>+2:24:30.41</td>
<td>4.5505</td>
<td>0.40x0.35</td>
<td>17</td>
<td>0.037</td>
<td>420</td>
</tr>
</tbody>
</table>

Table 2. Average gas ($\langle \Sigma_{\text{gas}} \rangle$) and SFR ($\langle \Sigma_{\text{SFR}} \rangle$) surface density measured in two $\Sigma_{\text{gas}}$ bins for our four objects. The uncertainties are determined using the Monte Carlo simulations described in Sect. 3. The uncertainties are based only on the instrumental noise.

<table>
<thead>
<tr>
<th>Name</th>
<th>$\Sigma_{\text{gas}}$ range</th>
<th>$\langle \Sigma_{\text{gas}} \rangle$</th>
<th>$\langle \Sigma_{\text{SFR}} \rangle$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$M_{\odot}/\text{pc}^2$</td>
<td>$M_{\odot}/\text{pc}^2$</td>
<td>$M_{\odot}/\text{yr}^{-1}\text{pc}^{-2}$</td>
</tr>
<tr>
<td>DC818760</td>
<td>2005-3232</td>
<td>2468±101</td>
<td>2.9±0.4</td>
</tr>
<tr>
<td>DC818760</td>
<td>3232-5208</td>
<td>4068±219</td>
<td>7.1±0.9</td>
</tr>
<tr>
<td>DC873756</td>
<td>1945-3291</td>
<td>2500±151</td>
<td>5.0±0.4</td>
</tr>
<tr>
<td>DC873756</td>
<td>3291-5570</td>
<td>4062±215</td>
<td>14.2±0.6</td>
</tr>
<tr>
<td>VC5101218326</td>
<td>1926-2590</td>
<td>2203±182</td>
<td>3.3±0.7</td>
</tr>
<tr>
<td>VC5101218326</td>
<td>2590-3481</td>
<td>3003±295</td>
<td>5.4±1.2</td>
</tr>
<tr>
<td>VC5110377875</td>
<td>424-862</td>
<td>613±37</td>
<td>0.8±0.2</td>
</tr>
<tr>
<td>VC5110377875</td>
<td>862-1755</td>
<td>1210±50</td>
<td>2.3±0.3</td>
</tr>
</tbody>
</table>

For each source, we defined two different regions based on their $\Sigma_{\text{gas}}$. We cut the range between the $5\sigma$ limit and the maximum in two bins of the same logarithmic size, building two different regions with a lower and a higher $\Sigma_{\text{gas}}$. The high-density region tends to be in the center, while the lower-density region forms a ring around it (see Fig. 1). However, the disturbed morphologies of our systems lead to rather complex shapes, which justifies a posteriori not using radial profiles in this object type. Finally, we computed the mean $\Sigma_{\text{gas}}$ and $\Sigma_{\text{SFR}}$ in each region of each object. In Appendix C we describe a simulation validating our method. This simulation shows that we can recover without bias the intrinsic relation in the presence of noise. However, this simulation does not include the potential complex systematic effects from spatial variations of the conversion factors used in Eqs. 1, 2, and 3.

To derive uncertainties on these quantities, we moved randomly the two regions in a noisy area of the map using the same offset for both regions, and measured our observables using the same method as previously. This process was repeated 10000 times, and the standard deviation of the results provides the uncertainty. The results are summarized in Table 2. We also computed the typical correlation between the noise realizations in the two regions and found a Pearson correlation coefficient of 0.5±0.1. This is expected since the two regions have a common origin, and the interferometric noise is correlated at the scale of the synthesized beam. In Fig. 2 these average values are located at the middle of the cloud of points when most of the pixels are detected (DC873756 and high-density bin of DC818760), but lie significantly below otherwise. This is not surprising since in the regime of average S/N the detections are biased toward positive outliers of the KS relation and the instrumental noise.

In Fig. 3 we present a synthesis of our results together with a compilation of previous works. All our data points but one are consistent with a 0.5-1 Gyr depletion timescale expected for massive main-sequence galaxies at $z\sim4.5$ (Scoville et al. 2017; Dessauges-Zavadsky et al. 2020). The only outlier...
Fig. 1. Surface density maps of DC873756: Gas (left, traced by [CII]), obscured FIR SFR (center, traced by the 158 μm rest-frame continuum), and unobscured UV SFR (right, traced by the F814W observer-frame continuum). The black contours are the (3+2k)σ levels (k≥0) of the gas surface density. The thicker solid and dashed lines, respectively, are used to highlight the 5σ Σgas limit and the border between the low- and high-density regions used in our analysis (see Sect. 3). The ALMA synthesized beam size is shown in the lower left corner. The unobscured SFR surface density map based on HST data is convolved by a Gaussian kernel to match the ALMA resolution.

Fig. 2. Pixel-by-pixel KS relation between the SFR and gas surface density. Each panel corresponds to a source (upper left: DC818760, upper right: DC873756, lower left: VCS101218326, lower right: VCS110377875). The small black filled circles correspond to lines of sight with a >3σ signal on the SFR surface density, and the small red downward triangles to 3σ upper limits. The large filled symbols (same as in Fig. 3) correspond to the average value for all the pixels in a given gas surface density bin (see Sect. 3 and Table 2).

(285±20 Myr) is the central high-density region of DC873756, which has the highest obscured SFR fraction (SFR_{IR}/SFR_{tot} = 98.7±0.3%) of the sample, and could thus hide a mild but heavily obscured starburst.

We compared our results with CO measurements of the global KS relation from the nearby COLD GASS sample (Saintonge et al. 2012) and the z≤2.5 PHIBBS and PHIBBS2 samples (Tacconi et al. 2013; Freundlich et al. 2019). We find that our objects are located in the scatter of these previous studies (~0.3 dex corresponding to a factor of 2), but with a higher gas surface density than most of the nearby sample by almost two orders of magnitude. Similarly, our sources are within a factor of 2 of the global KS relation fits by de los Reyes & Kennicutt (2019) at low redshift and by Wang et al. (2022) at high redshift, and the resolved low-z KS fit by Pessa et al. (2021). In contrast, most of the measurements of Nagy et al. (2023) at the scale of 1.6 kpc (compared to ~2 kpc in our analysis) in two strongly lensed z~1 galaxies have significantly lower ΣSFR at a given Σgas than other analyses; this is discussed in their paper without converging on a final explanation. Since their Cosmic Snake measurements agree with those of Pessa et al. (2021) and with our results, but not their measurements in the A521 galaxy, it could suggest that the the A521 galaxy is an outlier. In contrast, our sample of main-sequence galaxies have significantly lower ΣSFR at a given Σgas than typical high-redshift starbursts, which have an average depletion timescale of 100 Myr (Sharon et al. 2013; Rawle et al. 2014; Hodge et al. 2015). The z~7 LBGs studied by Vallini et al. (2024) exhibit a similar behavior, suggesting that they could also be starbursting systems. Finally, we compared our results with the KS relation of Kraljic et al. (2023, fit for z=4 and 10^9 < M_*/M_0 < 10^{10}) from the hydrodynamical simulation NewHorizon (Dubois et al. 2021). Their results suggest a slightly higher normalization (by a factor of ~1.5) than our measurements. However, objects as massive as our targets are not found in the limited volume of their simulated box, and low- and high-mass high-z galaxies could exhibit different behaviors.

4. Discussion and conclusion

Our study suggests that main-sequence galaxies follow the same KS relation from z=0 to z=4.5, but exhibit a strong increase in their gas density with increasing redshift driving a rise in their SFR density. This universality of the KS relation for main-sequence galaxies might seem surprising considering how different local and z~4 galaxies are, for example in term of gas fraction or sSFR. Since a significant fraction of our sample (Devereaux et al. 2023), and more globally of z~5 massive main-sequence galaxies (e.g., Romano et al. 2021), are identified as possible mergers by morpho-kinematical analyses, this opens the question of a possible decoupling of the merging and starburst events in high-redshift galaxies, but also of the timescale of the SFR enhancement and the associated merger stage. Theoretical works suggest that high-z mergers could often be inefficient in increasing star formation (e.g., Fensch et al. 2017) because their turbulence-dominated medium is incapable of producing high-density regions, decreasing dramatically the gas depletion timescale (Segovia Otero et al. 2022). However, since extremely star-forming major starbursts are routinely observed in the sub-millimeter domain (e.g., Hodge & da Cunha 2020, for a review), we need to better understand the mechanism at play in the high-
test whether the KS relation breaks at smaller scales in main-sequence galaxies, as discussed in Nagy et al. (2023) at z~1.

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Fig. 3. Kennicutt-Schmidt relation between the SFR and gas surface density. The averaged data points from DC818760, DC873756, VCS101218326, and VCS110377875 are shown as violet squares, blue filled circles, yellow hexagons, and green diamonds, respectively. Our results are compared with the CO measurements of the global KS relation from the low-z COLD GASS sample (Saintonge et al. 2012, crosses) and at redshifts up to z~2.5 from the PHIBBS (Tacconi et al. 2013, plus signs) and PHIBBS2 (Freundlich et al. 2019, three-branch stars) programs, together with the resolved KS relation in z~1 lensed main-sequence galaxies (Nagy et al. 2023, five-branch stars). Also shown are the global (de los Reyes & Kennicutt 2019, dashed line) and resolved (Pessa et al. 2021, two-dot-dashed line) KS relations measured in the local Universe, the high-redshift global KS relation obtained by ALMA CO stacking (Wang et al. 2022, dotted line), and the global KS relation from simulations at z~4 (Kraljic et al. 2023, three-dot-dashed line). The thin gray lines indicate the various depletion timescales. The red points are resolved measurements in high-z starbursts by Hodge et al. (2015). The brown six-branch stars are the measurements in z~7 LBGs by Vallini et al. (2024). The error bars include only the uncertainties from the instrumental noise, but not from the calibration (~10 % for ALMA) or from the conversion factors used in Sect. 2. They are often smaller than the symbols.

Our analysis is a very first step. We need to confirm these results on larger samples and with other SFR (e.g., Hz with JWST) and gas tracers, since [CII] has not been tested at sub-galactic scale in the high-redshift Universe yet. Ideally, we should also push toward lower masses with potentially less mature systems and lower metallicities. Deeper ALMA observations would also allow us to detect the dust continuum in most lines of sight providing a local estimate of Σsfr, and measure the scatter on the KS relation. Finally, higher-resolution observations will
Appendix A: Gas and SFR maps of the other sources

Figures A.1 and A.2 show the gas and SFR density maps of DC818760, VC5101218326, and VC5110377875, which are not discussed in the main text. Similarly to DC873756, we note that DC818760 and VC5101218326 have very different obscured and unobscured SFR density maps, confirming the need to have access to both. For instance, both the central and western components of DC818760 host an important obscured star formation activity, but only the central one is detected in the unobscured SFR density map. The morphology and the kinematics of these two objects is discussed in a companion paper (Devereux et al. 2023; see also Jones et al. 2020 about the initial ALPINE data of DC818760). They are both identified as solid merger candidates. VC5110377875 will be studied in greater detail when the high-resolution data reaches a sufficient depth. So far it looks like a well-behaved rotator. However, we note a small displacement of the unobscured SFR toward the east compared to the gas.

Appendix B: Depletion timescales measured inside apertures with various radii

Since our targets have complex morphologies, we decided to measure the average $\Sigma_{\text{SFR}}$ in regions selected to be in a specific range of $\Sigma_{\text{gas}}$. This type of measurement is easy to reproduce in simulations. This method is particularly well suited for $z>4$ observations since the [CII] line used as a gas tracer usually has a better S/N (by a factor of $\sim 3$) than the dust continuum tracing the obscured SFR. It is not the case at lower redshift, where the gas tracers are often shallower than SFR estimators. Usually, the gas and SFR surface densities are measured in an aperture corresponding to the source size. This leads to multiple questions about the choice of wavelength or line to measure the source size, but also the exact definition of the source radius.

To compare the two approaches, we measured the gas depletion timescale in apertures centered on the maximum of the [CII] emission with various radii. This choice may appear arbitrary, but the UV center is often not representative of the mass distribution of the system because of the dust attenuation, and to date we have no access to high-resolution rest-frame near-infrared data probing the old stars. The uncertainties are determined using the same Monte Carlo resampling method that we used for $\Sigma_{\text{gas}}$ regions in Sect. 3. The comparison of the two approaches is shown in Fig. B.1 (solid lines). We note that two sources have a significantly longer gas depletion timescale for large aperture radii (DC818760, DC873756), while the two others do not exhibit any significant trend (VC5101218326, VC5110377875). DC818760 is a multi-component system and the large radii include the two neighbors, while the small radii only include the central component. It is not surprising to find slightly different timescales in the various components. As discussed in Sect. 3, DC873756 probably hosts an obscured starbursting core with a short depletion timescale, while it is longer in the outskirts.

In Fig. B.1 we also show the gas depletion timescales found in our low- and high-$\Sigma_{\text{gas}}$ regions. The x-axis position of these datapoints corresponds to the average angular radial distance to the maximum of the [CII] emission. The error bars represent the full range of distances. Since the morphologies are not centro-symmetrical, there is an overlap between the two regions in terms of radial distance. The high-density regions correspond to smaller radii and agree with aperture measurements at the 1$\sigma$ level. This is not the case of the low-density regions at larger...
Depletion timescale [Myr]

Fig. B.1. Gas depletion timescale measured in an aperture centered on the maximum of the [CII] emission as a function of its radius (solid lines, see Appendix B). The colored areas correspond to the 1σ uncertainties determined using the Monte Carlo sampling described in Sect. 3. For comparison, we represent the depletion timescales measured in our two \( \Sigma \) regions using the same symbols as in Fig. 3. The horizontal error bars correspond to the full range of angular radial distances to the [CII] maximum in the region. The high-density region systematically corresponds to the smaller radius.

To study this dependence, we built a simulation to test the accuracy of our method to determine the gas depletion timescale measured in an aperture centered on the maximum of the [CII] emission. We produced cases based on DC873756 (hereafter case 1), for which most of the pixels in both the low and high gas density regions are detected in the combined \( \Sigma_{\text{gas}} \) map; and VC5110377875 (case 2), for which most of the pixels in the low-density region are undetected. The first source is modeled by a symmetrical Gaussian with a FWHM of 0.5\textdegree, and the second by a 1.5\textdegree × 0.5\textdegree elliptical Gaussian. We convolved these models by the associated synthesized beams in the real observations and rescaled the peak of the convolved maps to match the observed values. We thus obtained three noiseless maps (\( \Sigma_{\text{gas}}, \Sigma_{\text{SFR}, \text{gas}} \), and \( \Sigma_{\text{SFR}, \text{gas}} \)) for each source. Since we applied a simple rescaling to our models, the local depletion timescale is constant across the simulated objects by construction. Finally, we added interferometric noise to the \( \Sigma_{\text{gas}} \) and \( \Sigma_{\text{SFR}, \text{gas}} \) maps after rescaling it to the observed values, and white noise smoothed by our convolution kernel to the \( \Sigma_{\text{SFR}, \text{gas}} \) map after matching its level to the observed value.

We then applied the same measurement process as described in Sect. 3 on both noiseless and noisy maps. The results are presented in Fig. C.1. The KS relation in the noiseless case is our reference (light blue small squares). Since there is no noise associated with these maps, we used the noise level of the \( \Sigma_{\text{gas}} \) noisy map to define the region above the 5σ density limit in which we analyzed individual pixels. The low and high gas density regions are defined in a similar way, and we derived the mean \( \Sigma_{\text{gas}} \) and \( \Sigma_{\text{SFR}} \) in each of them (dark blue large squares). As expected, there is a near perfect agreement between the individual pixels and the mean measurements in the two simulated objects.

We also analyzed the noisy maps. The various regions used in our analysis can slightly change compared to the noiseless case, since some pixels can pass above or below a threshold because of the noise. The individual detected pixels (small black filled circles) agree with the noiseless relation in case 1 where the S/N is high. In case 2 the detections agree only at the high-\( \Sigma_{\text{gas}} \) end, but are systematically higher than the noiseless case at the low-\( \Sigma_{\text{gas}} \) end. Since only pixels with \( \Sigma_{\text{SFR}} \) above 2.5 \( M_\odot \) yr\(^{-1} \) kpc\(^{-2} \) are detected, only the positive noise outliers are detected in the low-\( \Sigma_{\text{gas}} \) regime for which the average \( \Sigma_{\text{SFR}} \) lies above this limit. In contrast, the mean values measured in the low and high gas density regions (dark green pentagons) agree at 5σ with the noiseless relation. To check for a possible bias, we computed their average positions over 1000 noise realizations (light green hexagons), and they agree at better than 3% with the noiseless case.

Our simulation confirms that mean measurements over several well-selected regions are more effective at recovering mean \( \Sigma_{\text{SFR}} \) than individual pixel measurements, which are strongly biased in the low S/N regime. It is not surprising, since these regions encompass several synthesized beams and averaging them improves the S/N by approximately a factor of \( \sqrt{N_{\text{sh}}} \), where \( N_{\text{sh}} \) is the number of synthesized beams in the region.\(^2\) However, this method works only because we benefit from deep \( \Sigma_{\text{gas}} \) maps to select these regions.

\(^2\) This is an approximation since the shape of the regions and the spatially correlated interferometric noise are both complex, but it works with a 20% accuracy in our simulations.
Fig. C.1. Kennicutt-Schmidt relation between the SFR and gas surface density in our simulation described in Appendix C. The panels correspond to two different simulated objects based on DC873756 (upper panel) and VC5110377875 (lower panel), illustrating different S/N regimes. The small blue squares show the pixels of the noiseless map, and the large dark blue squares are the mean computed in the low and high gas density regions (see Sect. 3). The small black filled circles are the 5σ SFR detections in the noisy maps, and the small red downward-facing triangles are the 3σ upper limits of non-detections. The dark green filled pentagons are the mean values measures in the two gas density regions. The small light green hexagons are the averages of these mean measurements over 1000 noise realizations.