Distributions of gas and small and large grains in the LkHα 330 disk trace a young planetary system

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ABSTRACT

Planets that are forming around young stars are expected to leave clear imprints in the distribution of the gas and dust of their parental protoplanetary disks. In this paper, we present new scattered light and millimeter observations of the protoplanetary disk around LkHα 330, using SPHERE/VLT and ALMA, respectively. The scattered-light SPHERE observations reveal an asymmetric ring at around 45 au from the star, in addition to two spiral arms with similar radial launching points at around 90 au. The millimeter observations from ALMA (resolution of 0.06''×0.04'') mainly show an asymmetric ring located at 110 au from the star. In addition to this asymmetry, there are two faint symmetric rings at 60 au and 200 au. The \(^{12}\text{CO},^{13}\text{CO},\) and \(^{18}\text{O}\) lines seem to be less abundant in the inner disk (these observations have a resolution of 0.16''×0.11''). The \(^{13}\text{CO}\) peaks at a location similar to the inner ring observed with SPHERE, suggesting that this line is optically thick and traces variations of disk temperature instead of gas surface-density variations, while the \(^{18}\text{O}\) peaks slightly further away at around 60 au. We compare our observations with hydrodynamical simulations that include gas and dust evolution, and conclude that a 10 M\(_{\odot}\) mass planet at 60 au and in an eccentric orbit (\(e = 0.1\)) can qualitatively explain most of the observed structures. A planet in a circular orbit leads to a much narrower concentration in the millimeter emission, while a planet in a more eccentric orbit leads to a very eccentric cavity as well. In addition, the outer spiral arm launched by the planet changes its pitch angle along the spiral due to the eccentricity and when it interacts with the vortex, potentially appearing in observations as two distinct spirals. Our observations and models show that LkHα 330 is an interesting target to search for (eccentric-) planets while they are still embedded in their parental disk, making it an excellent candidate for studies on planet-disk interaction.

Key words. accretion, accretion disk – circumstellar matter –stars: pre-main-sequence–protoplanetary disk–planet formation

1. Introduction

Most of the information that we have about planets forming in protoplanetary disks comes from observations of the dust scattering and emission. We can access the distribution of the micron-sized particles at the surface layers of the disks using optical and near-infrared scattered light observations, while the distribution of the larger particles, that is, the pebbles (millimeter- and centimeter-sized particles), is obtained from (sub-) millimeter observations. From the combination of these two techniques, it is possible to understand if the distribution of small and large particles is different in disks, which can give hints about the main mechanisms that rule the gas evolution (e.g., Pinilla & Youdin 2017). This is because small dust grains are well coupled to the gas and follow the gas distribution, while large particles that are partly decoupled from the gas settle to the midplane and migrate quickly inwards toward the central star, unless they are trapped in a pressure bump (Whipple 1972).

One of the first discoveries with the Atacama Large Millimeter/submillimeter Array (ALMA) in the field of planet formation was the confirmation of highly asymmetric disks; for example, the disks around HD 142527, Oph IRS 48, and HD 135344B (Casassus et al. 2013; van der Marel et al. 2013; Pérez et al. 2014). HD 142527 and HD 135344B also show spiral arms in high angular resolution observations of their scattered light with SPHERE (Avenhaus et al. 2014; Stolker et al. 2016). Other examples are V1247 Ori and MWC 758 (Kraus et al. 2017; Dong et al. 2018, respectively). Only a few disks show spirals at both near-infrared and submillimeter wavelengths (e.g., HD 100453 and WaOph 6, Rosotti et al. 2020; Brown-Sevilla et al. 2021; Huang et al. 2018). Interestingly, spiral arms in scattered light are found mainly around stars toward the end of their pre-main-sequence evolution (Garufi et al. 2018), suggesting that the observed spiral arms are unlikely to originate from gravitational instability, which is expected in young massive disks (e.g., Kratter & Lodato 2016).

Potential origins of the observed asymmetries in the millimeter emission are vortices and disk eccentricity (Ataiee et al. 2013; Zhu et al. 2014; Price et al. 2018; Ragusa et al. 2020). In the case of vortices, they can originate due to embedded planets in the disk perturbing the gas density and/or velocity field and triggering the Rossby-wave instability (RWI; Lovelace et al. 1999; Li et al. 2000; Lyra et al. 2009). Similarly, the RWI can also be triggered at the edges of dead zones that are forming vortices (Regály et al. 2012; Flock et al. 2015). In addition, the baroclinic instability (Klahr & Bodenheimer 2003; Barge et al. 2016) can also be the origin of vortices in a disk. Another potential explanation of asymmetries is dust trapping in the trailing Lagrange point of a planet that is interacting with the disk (Rodénkirch et al. 2021).

Even though planets may naturally explain both spiral arms and vortices, numerical simulations have shown that the first mode of planet-driven spiral arms are usually very tight (small pitch angles) compared to the observed spiral arms in the infrared images (e.g., Juhász et al. 2015; Bae & Zhu 2018a). For this reason, massive planets orbiting outside the spirals have been used in models to explain some of the observed spirals in scattered light (e.g., Dong et al. 2015; Muley et al. 2021).
In this paper, we present new observations from SPHERE and ALMA of the disk around LkHα 330, which is an F7 star with a stellar mass of $\sim 2.5 \, M_\odot$, a luminosity of $\sim 15 \, L_\odot$ (Herčeg & Hillenbrand 2014, assuming a distance of 315 pc), and an estimated age of $\sim 2.5 \, \text{Myr}$ (Uyama et al. 2018). It is located in the Perseus molecular cloud at a distance of $\sim 318$ pc (Gaia Collaboration et al. 2016, 2021). It was identified as a transition disk from observations with the Spitzer Space Telescope due to the lack of the emission in its near-infrared spectra. Observations with the Submillimeter Array (SMA) confirmed the existence of a cavity in this disk (Brown et al. 2009; Andrews et al. 2011). Isella et al. (2013) combined SMA and the Combined Array for Research in Millimeter-wave Astronomy (CARMA) data at 1.3 mm and found an asymmetric structure that potentially originated from a vortex in the disk. Recent scattered light observations of LkHα 330’s disk suggested the presence of two spiral arms (Akiyama et al. 2016; Uyama et al. 2018), which have been proposed to have originated from planet-disk interaction.

This paper is organized as follows. Section 2 summarizes the new SPHERE and ALMA observations of the disk around LkHα 330. Section 3 describes the morphology observed with SPHERE and ALMA. Section 4 compares the observations with hydrodynamical simulations of gas and dust evolution in the context of planet-disk interaction, in addition to radiative transfer models being compared with observations. Section 5 presents the discussion about the observed structures, their origin, and the limitations of our current models to explain the observational results. Finally, Sect. 6 summarizes the main conclusions of this paper.

2. Observations

2.1. SPHERE Observations

We obtained observations of LkHα 330 at the Very Large Telescope located at Cerro Paranal, Chile, using the SPHERE instrument (Beuzit et al. 2008), a high-contrast imager with an extreme adaptive optics system (Sauvage et al. 2014) under program IDs 098.C-0760(B) and 100.C-0452(A) (PI: M. Benisty). In this paper, we report new polarimetric observations taken on 2017-10-05 and 2017-10-11 and obtained in the near-infrared ($J-(1.2 \, \mu m)$ and $H-(1.65 \, \mu m)$, respectively) with the IRDIS instrument (Dohlen et al. 2008). For all the IRDIS observations presented in this paper, we use a 185 mas diameter coronagraph (N_ALC_YJH_S) to enhance the signal-to-noise ratio in the outer disk regions. The plate scale is 12.26 mas and 12.25 mas per pixel, for the $J$- and $H$-band data, respectively.

To reduce the data, we use the public IRDAP pipeline (IRDAS Data reduction for Accurate Polarimetry) by van Holstein et al. (2020a,b). In polarimetric differential imaging, the stellar light is split into two orthogonal polarization states, and a half-wave plate (HWP) is set to four positions shifted by 22.5° to construct a set of linear Stokes images. The data are then reduced following the double-difference method, from which one can derive the Stokes parameters $Q$ and $U$. If we assume single scattering events on the protoplanetary disk surface, the scattered light is...
linearly polarized in the azimuthal direction; therefore, we describe the polarization vector field in polar coordinates with the $Q_\phi$, $U_\phi$ Stokes images (Schmid et al. 2006). In this framework, the $Q_\phi$ image contains all disk signals, while the $U_\phi$ image does not contain any.

2.2. ALMA Observations

This work includes ALMA observations at 1.3 mm (Band 6) of LkHα 330, which was observed on a single execution as part of the ALMA project 2018.1.01302.S (PI: M. Benisty) on 11-Jul-2019. The correlator was configured to observe four spectral windows: two covered dust-continuum emissions were centered at 217.015 GHz and 233.016 GHz, and the two remaining ones were centered at 230.716 GHz to observe the molecular line $^{12}$CO ($J = 2 \rightarrow 1$), and at 219.660 GHz to observe the transitions $^{13}$CO ($J = 2 \rightarrow 1$) and C$^{18}$O ($J = 2 \rightarrow 1$). The channels’ frequency spacing is $15.625$ MHz for continuum and $976.562$ kHz for the CO isotopologues lines (approximately $21$ km s$^{-1}$ and $1.3$ km s$^{-1}$, respectively). The total time on source is $36.79$ min, observed with $46$ antennas spanning baselines from $111.2$ m to $12644.7$ m.

Using CASA 5.6.2, we extract the dust-continuum emission from all the windows by flagging the channels located at $\pm 25$ km s$^{-1}$ from each targeted spectral line. The remaining channels from all spectral windows are averaged into $125$ MHz channels. We applied the task statwt to recalculate the visibilities’ weight according to their observed scatter. To enhance the signal-to-noise ratio, self-calibration is applied to the data. We use a Briggs robust parameter of 0.6 for the imaging of the self-calibration process. We apply two phase calibrations and one amplitude calibration using the whole integration time as the solution interval. The overall improvement on the signal-to-noise ratio in the continuum images is approximately $21$ km s$^{-1}$.

To enhance the signal-to-noise ratio in the continuum images, we apply a $uv$-tapering with a full width at half maximum (FWHM) of a 2D Gaussian of $0.03'' \times 0.01''$ with position angle of $110^\circ$. The dust continuum emission image is generated using a robust parameter of 0.7, which provides us the best compromise between resolution and sensitivity. The CO lines are imaged with a robust parameter of 1.2, and a channel width of $1.5$ km s$^{-1}$, and an $uv$-tapering of $0.08'' \times 0.08''$. We find that increasing the robust value farther than 1.2 does not improve the sensitivity of the CO images, as the poor $uv$-coverage of our observations results in stronger side lobes of the point spread function (PSF), which are not balanced by a small increase in the beam size when going from 1.2 to 2.0 (natural weighting). The velocity width of $1.5$ km s$^{-1}$ is chosen to increase the sensitivity of individual channels, which were imaged with manual masking. As a final step, we apply the JvM correction to our images, which accounts for the volume ratio $\epsilon$ between the PSF of the images and the restored Gaussian of the CLEAN beam, as described in Jorsater & van Moorsel (1995) and Czekala et al. (2021). We find $\epsilon_c = 0.39$ and $\epsilon_l = 0.62$ for the continuum and line images, respectively. Finally, the bettermoments package (Teague & Foreman-Mackey 2018) is used to create the moment maps.

In order to reduce the data volume for the visibility analysis, we average the continuum emission into $500$ MHz width channels and $30$s of time binning. We use each binned channel central frequency to convert the $uv$-coordinates into wavelength units.

3. Results

3.1. Structures observed with SPHERE

Figure 1 shows the SPHERE ($Q_\phi$ and $U_\phi$) observations of LkHα 330 in the $J$–band (1.2 $\mu$m, top panels) and $H$–band (1.6 $\mu$m, bottom panels). The $U_\phi$ images are almost free of any scattered light signal from the disk, and it only shows some emission in the inner ring of the H-band image. Figure 1 also shows the $Q_\phi \times r^2$ in linear scale to compensate for stellar illumination and better enhance the outer structures. These observations mainly reveal two types of clear structures: (a) a non-uniform brightness ring and (b) two spiral arms.
First, the non-uniform ring is located between 0.11″ and 0.22″ from the star and the variation of its brightness is shown in Fig. 2. The peak brightness of this ring (from the $Q_a$ image) is located at 0.15″. The left panel of this figure shows the polar mapping from 0.1″ to 0.5″ of the $Q_a\times r^2$ of the H-band image after deprojection. For the deprojection, we use the inclination and position angle obtained from the visibility fitting to the millimeter dust-continuum emission as shown in Sect. 3.2 (incl=27.5° and PA=49.2°). The ring shows a sinusoidal pattern in polar coordinates, and it is possible that the deprojection may not fully restore the “face-on” view of the disk due to the flaring of the disk surface (Dong et al. 2016). The right panel of Fig. 2 shows the azimuthal profile of the ring calculated from 0.11″ to 0.22″, demonstrating variations of the ring brightness of ~50%. The ring has three local brightness maxima: the main peak located at a position angle of around ~130°, and two surrounding peaks, a very wide one located at ~70° and a narrower one at ~200°, both of them being ~15% less bright than the main peak. The rest of the ring from ~250° to 360° has an almost uniform brightness, which is 50% lower than the mean peak.

The second clear set of structures are the spiral arms. To quantify the shape of the two spiral arms, we first deprojected the $Q_a$ of the H-band image (which has better signal-to-noise ratio than the J-band image) after multiplying by $r^2$ and took the difference between the original image and a smoother version which is obtained by convolving it with a circular Gaussian kernel ($\sigma = 50$ mas). This process is known as a high-pass filter (or unsharp masking) and it helps to sharpen the image and highlight potential small-scale structures (see Fig. 3). From this sharper image, we select the peak of emission along the radial direction every 4° along the spiral arm (e.g., Pérez et al. 2016; Kurtovic et al. 2018).

With the selected points, we calculate the pitch angle of the features by fitting an Archimedean spiral, following

$$ r = r_0 + b\theta, $$

where $\theta$ is the azimuthal angle, $r_0$ is the spiral position for $\theta = 0$, and $b$ is a constant that relates to the pitch angle by $r_\text{pitch} = b/r$. We assume that both spirals share the same polar coordinate system, centered at the stellar position. We fit ($r_0, b$) for each spiral with an MCMC routine based on emcee (Foreman-Mackey et al. 2013a); each run has two free parameters, 128 walkers, and 1000 steps, of which the first 200 are considered burn-in steps. We minimize the $\chi^2$ between the model spiral and the measured points in the image using 1 pix as the error for each measurement and a flat prior for both parameters.

We find that the points on the edges of the south-west feature start moving in the reversed radial direction compared to the rest of the spiral. This effect is most likely produced by de-projection effects of the flared surface layer and would require a correction with the flaring angle to be fixed (Dong et al. 2016). In addition, it is possible that the inclination and position angle obtained from ALMA is not exactly the same for the scattered light image since they trace different disk vertical regions. Therefore, those points that move in the reversed radial direction were not considered for the fit.

In the right panel of Fig. 3, we show the best fit and the 3σ confidence region for each spiral, and Table 1 summarizes the best parameters from this fitting. This table includes the inner and outer radii and the pitch angle, referring to the side of each spiral that is closer or farther from the disk center. The launching point of the north-east spiral arm is 294 mas (~94 au), with a pitch angle of 11.3°. The launching point of the south-west spiral arm is very similar at 283 mas (~90 au), with a pitch angle of 9.0°. The farthest point of this spiral arm is at 352 mas (~111 au), which is similar to the location of the main asymmetry of the dust-continuum emission from ALMA (Sect. 3.2).

| Table 1. Best parameters from spiral fitting following Equation 1. Inner and outer refer to the side of each spiral that is closer or farther from the disk center, respectively, “mas” stands for milliarcsecond. NE refers to the north-east, whereas SW refers to the south-west spiral. |
|---|---|---|
| Spiral NE | Spiral SW |
| $r_0$ | 314.5±3.7 | 419.1±12.5 |
| $b$ | 1.01±0.12 | 0.78±0.10 |
| $\mu_{inner}$ | 294.4±5.5 | 283.3±5.1 |
| $\mu_{outer}$ | 378.2±5.5 | 352.0±19.0 |
| $\mu_{inner}$ | 11.3±1.3 | 9.0±1.3 |
| $\mu_{outer}$ | 8.8±0.9 | 7.3±0.8 |

Fig. 3. SPHERE observations of LkHα 330. Left panel: $Q_a$ of the H-band observations after multiplying by $r^2$ and deprojection. Center panel: High pass filtered image. Right panel: Polar mapping from 0.1″ to 0.5″ of the sharper image in the center panel. The white lines show the spiral fit described in the text, and the shaded areas show the 1σ uncertainty of the fit. In this case, the axis of the position angle is shifted in comparison with Fig. 2 for a better visualization of the fit.
We calculate the optical depth of the peak of the continuum ring, 3.2.1. Optical depth and dust disk mass
the maximum (see top left panel in Fig. 10), the flux within this
the visibility fitting described later in this section of 56.1 mJy.

\[ \tau = -\ln \left( 1 - \frac{I(r_{\text{peak}})}{B(T_d(r_{\text{peak}}))} \right), \]  

(2)

with \( T_d \) being the dust temperature at the peak location \( r_{\text{peak}} \).
Equation 2 is only valid when neglecting dust scattering. In this
scenario and using a dust temperature of 20 K, we find that the
optical depth at the peak (which is at the location of the
 asymmetry) is \( \tau_{\text{peak,B6}} = 0.37 \), similar to the values found in the
DSHARP sample (Huang et al. 2018; Dullemont et al. 2018).
From the radiative transfer models in Sect. 4 that assume the
results of the hydrodynamical simulations after 0.15 Myr, the
temperature at the midplane at the location of the asymmetry
\( \sim 110 \) au is 36 K. Using this temperature for the calculation of
the optical depth, we obtain \( \tau_{\text{peak,B6}} = 0.16 \). However, the
emission may still be optically thick for two potential reasons.
First, because the outer disk may be as cold as the interstellar medium
\( \sim 10 \) K, in which case \( \tau_{\text{peak,B6}} = 1.8 \). Second, dust scattering
may not be negligible (which happens when dust grains have a
radius comparable to the wavelength of the observations), in
which case an optically thick region can be misidentified as optically
thin (Zhu et al. 2019).
Assuming that the emission is optically thin, we calculate the
dust disk mass as \( M_{\text{dust}} \sim \frac{d^2 F_s}{\kappa_e T_s}, \) where \( d \) is the distance to the
source, \( F_s \) is the total flux at 1.3 mm, and \( B_s \) is the black-body
surface brightness at a given temperature (Hildebrand 1983).
Taking a mass absorption coefficient \( (\kappa_e) \) at a given frequency
as \( \kappa_e = 2.3 \text{ cm}^2 \text{ g}^{-1} \times (\nu/230 \text{ GHz})^{0.4} \) (Beckwith et al. 1990; Andrews et al. 2013), we obtain 168.5 \( M_{\oplus} \), and inside the asymmetry the dust mass is 37 \( M_{\oplus} \) \( \sim 2.2 M_{\text{Neptune}} \).
Using the canonical dust-to-gas mass ratio of 0.01 (Mathis et al. 1977), the disk mass is
0.05 \( M_{\text{sun}} \), and inside the asymmetry it is \( \sim 12 M_{\text{Neptune}} \). However, assuming a dust-to-gas mass ratio of 0.01 inside the asymmetry
may be unrealistic if this asymmetry is a vortex where particles are trapped. Based on the hydro-dynamical simulations of
Sect. 4, the dust-to-gas mass ratio at the location of the peak of the
dust concentration is around 0.2, which leads to a mass of
\( \sim 2.3 M_{\text{Neptune}} \) inside the asymmetry.

3.2.2. Visibility fitting of the dust morphology
We describe the dust-continuum emission observed with ALMA
with a parametric model. Motivated by the radial profile from the
CLEAN model image (see Fig. 8), we describe LkH\( \alpha \) 330 with
three Gaussian rings and a Gaussian asymmetry in radius and azimuth
direction as shown in Fig. 6.
For each model, the visibilities were obtained by optimizing the
model profile with a spatial offset \( \delta_{\text{RA}}, \delta_{\text{Dec}} \), an inclination (inc), and position angle (PA), which are used to deproject the

![Fig. 4. Observations versus model images from our best fit with galarrio (before and after convolution) and the residuals. The contours of the residual map are [−10\( r \), −5\( r \), 5\( r \), 10\( r \)], where negative values are dashed contours and positive values solid contours. The green contour in the residual map shows the area that encloses 80% of the peak of the emission from the observations as a reference.](image-url)
Table 2. Best parameters from the $uv$-modeling. $R_{68}$ and $R_{90}$ denote the radius that encloses either 68% or 90% of the total flux ($F_i$). Index 1 corresponds to Ring 1, indices 2 and 4 describe Ring 2, which is the main asymmetric ring, and index 3 corresponds to Ring 3 (see schematic in Fig 6 for reference). Pixel size is 5 mas.

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<tr>
<th>Model</th>
<th>$\delta_{\text{RA}}$</th>
<th>$\delta_{\text{Dec}}$</th>
<th>inc</th>
<th>PA</th>
<th>$f_1$</th>
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<td>-3.6$^{+0.4}_{-0.3}$</td>
<td>-7.2$^{+0.4}_{-0.2}$</td>
<td>27.5$^{+0.3}_{-0.2}$</td>
<td>49.2$^{+0.8}_{-0.2}$</td>
<td>1.01$^{+0.07}_{-0.07}$</td>
<td>202.7$^{+1.3}_{-1.3}$</td>
<td>26.8$^{+1.7}_{-2.2}$</td>
<td>3.52$^{+0.03}_{-0.02}$</td>
<td>368.0$^{+2.0}_{-2.0}$</td>
<td>61.8$^{+2.5}_{-2.5}$</td>
<td>53.3$^{+1.8}_{-1.5}$</td>
<td>0.20$^{+0.02}_{-0.02}$</td>
<td>631.8$^{+1.6}_{-5.3}$</td>
<td>62.3$^{+2.2}_{-6.9}$</td>
<td>8.29$^{+0.06}_{-0.15}$</td>
<td>349.8$^{+0.1}_{-0.1}$</td>
<td>-126.9$^{+0.4}_{-0.7}$</td>
<td>31.5$^{+0.1}_{-0.1}$</td>
<td>21.8$^{+0.1}_{-0.2}$</td>
<td>397.0$^{±0.6}_{\pm}$</td>
<td>472.8$^{±2.8}_{\pm}$</td>
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The width of this inner ring remains unresolved (the resolution of our observations in au is 19 au×12 au). The main ring is described by two Gaussian profiles, one is a ring centered at 117.0$^{+0.7}_{-0.6}$ au and is radially asymmetric, with the inner radial width slightly higher than the other width ($\sigma_{2i}=19.4^{+0.7}_{-0.8}$ au vs. $\sigma_{2o}=16.9^{+0.5}_{-0.5}$ au). The second Gaussian is an asymmetry that peaks at 111.2$^{+0.1}_{-0.1}$ au, with an azimuthal width of 21.8$^{+0.3}_{-0.3}$ deg. Finally, there is a faint ring at 200.9$^{+0.7}_{-0.5}$ au with a width of 19.8$^{+0.3}_{-0.3}$ au.

Figure 4 shows the comparison of the observations with the obtained $uv$-model, and the model after being imaged with the same procedure as the data. The right panel shows the residual image after subtracting the model from the observations; this is also imaged using CLEAN. The residuals map shows that the model describes the observations well, leaving residuals of a level of 10σ, mainly at the location of the asymmetry. It is interesting that the negative residuals line up with respect to the scattered light spiral arm in the south-west. However, this shape in the residuals may appear because we assume circular Gaussians in our model and the rings may be slightly eccentric. As a test, we also run a simulation with a Gaussian asymmetry that has different width in the azimuth direction (e.g., Pérez et al. 2014; Cazzoletti et al. 2018), but such a model does not significantly improve the residuals map. The model in Fig. 4 gives an azimuthal contrast of the asymmetry of $\sim 4$. Figure A.1 shows the fit of this model of the binned data of the real and imaginary part of the depolarized visibilities.

observational data. Therefore, each model has four extra free parameters in addition to those that describe the intensity profile. The Fourier transforms to obtain the model visibilities and the $\chi^2$ calculation are computed with the galario python package (Tazzari et al. 2018) using a pixel size of 5 mas.

We sampled the posterior probability distribution with a Markov chain Monte Carlo (MCMC) routine based on the emcee python package (Foreman-Mackey et al. 2013b). We use a flat prior probability distribution over a wide parameter range, such that the walkers would only be initially restricted by geometric considerations (inc $\in$ [0, 90], PA $\in$ [0, 180], $\sigma \geq 0$). We ran more than 250000 steps after convergence to find the most likely parameter set for each model, as well as taking the 16th and 84th percentiles for the error bars. Our results are shown in Table 2.

Based on the best parameters of this model, the faint inner ring is very narrow ($\sigma_1=8.3^{+0.5}_{-0.3}$ au) and centered at 63.6$^{+0.4}_{-0.4}$ au.

Fig. 5. ALMA dust continuum observations in a color scale that highlights the faint structures.

Fig. 6. Schematic of components used for $uv$ fitting of the dust-continuum emission from ALMA.
3.2.3. Emission of $^{12}$CO, $^{13}$CO, and C$^{18}$O

Figure 7 shows the moment 0 maps of $^{12}$CO, $^{13}$CO, and C$^{18}$O. The emission from $^{12}$CO is mainly between the channel maps from 4 to 13.0 km s$^{-1}$ (7 channels, see Fig. B.1). The $^{12}$CO does not show an emission in the south-west that is as extended as it is in the north-east, and it is possible that this is because of cloud contamination, and/or low signal-to-noise ratio due to the lack of short baseline observations that cover large scales. Thus, we cannot conclude that this asymmetry is real. For $^{13}$CO and $^{18}$CO, the emission mainly comes from five channels from 5.5 to 11.5 km s$^{-1}$ (Fig. B.1), and both look more azimuthally symmetric than the $^{12}$CO, although with a poor signal-to-noise ratio (for all three maps, the ratio between the peak and r.m.s. noise on the corresponding map is 5-6).

Figure 8 shows the azimuthally averaged radial intensity profiles of the deprojected images of the continuum, and from the moment 0 maps of the $^{12}$CO, $^{13}$CO, and C$^{18}$O. Each profile is normalized to the peak. All 3 molecular lines peak inside the main peak of the continuum millimeter emission. In the moment 0 map of $^{12}$CO, it seems that there is an emission drop near the center, which could have been washed out by the noise and the azimuthally averaging in Fig 8. The radial profile of the $^{12}$CO bends in the inner disk. Such a bending may be the combined effect of a reduced $^{12}$CO surface density and beam smearing (e.g., Bruderer et al. 2014; Fedele et al. 2017; Ubera Gabellini et al. 2019). The radial profile of the $^{13}$CO and C$^{18}$O show an inner drop of emission, where the $^{13}$CO peaks at a location similar to the inner ring observed with SPHERE ($R_{\text{inner}}$ = 45-50 au), whereas the C$^{18}$O peaks at ~60 au, which is very close to the peak of the inner faint ring observed with ALMA. Figure B.2 shows the moment 8 map (peak value of the spectrum) of the $^{12}$CO, $^{13}$CO, and C$^{18}$O lines of LkH$\alpha$ 330. The moment 8 has been used to identify gas substructures (e.g., Favre et al. 2019), and in this case the three lines show a clear cavity in the moment 8 map.

4. Comparison with planet-disk interaction models

4.1. Estimation of planet mass and position

We investigate the origin of the cavity and the structures of LkH$\alpha$ 330 in the context of planet-disk interaction. Based on the different radial extent of the cavity in scattered-light, CO molecular lines, and the dust continuum emission, it is possible to give an estimate of the mass of the potential planet carving this cavity, when assuming that the planet is in a circular orbit. As discussed in Sect. 5.4, planet eccentricity can affect different aspects of the disk, such as spiral shape, vortex survival, and gap size.

There are two different approaches to obtaining such an estimation. First, by comparing the location of the cavity wall in scattered light versus the peak of the millimeter emission (de Juan Ovelar et al. 2013). The wall of the emission in scattered light is defined as the location where the intensity value is halfway between the intensity at the bottom of the gap and top of the ring. However, from our observations it is not possible to obtain the location of the minimum inside the cavity due to the coronagraph, and therefore we take the location of the peak (45 au) as the wall of the cavity in scattered light. This provides us a lower limit of the planet mass. The peak of the millimeter emission is at 110; hence, $R_{\text{wall}}/R_{\text{mm,peak}}$ is 0.41, which will indicate a planetary mass higher than investigated in de Juan Ovelar et al. (2013) (15 $M_{\text{Jup}}$ for a 1 $M_{\odot}$ star), suggesting a brown dwarf-type companion.

Another possibility is to take the gap size as observed from $^{13}$CO and compare it with the location of the peak from the continuum millimeter emission (Rosotti et al. 2016; Facchini et al. 2018). We note, however, that this approach is valid when the $^{13}$CO is optically thin. It is also difficult to obtain the location of the minimum flux inside the cavity from our $^{13}$CO due to the large uncertainties and poor resolution. Hence, we take the location where $^{13}$CO peaks (~50 au) and provide a lower limit for the planet mass, using $(R_{\text{mm}} - R_{\text{Hill}})/R_{\text{CO}} = 1.2$. Comparing with Fig. 11 from Facchini et al. (2018), this gives a planet-to-star mass ratio ($q$) between $4 \times 10^{-3}$ and $7 \times 10^{-3}$ (depending if the output from the simulations is taken at 1000 or 3000 planetary orbits, with a lower q for longer times of evolution).

Taking a planet-to-star mass ratio of $4 \times 10^{-3}$ and assuming the peak of the millimeter emission is radially located at around $R_{\text{Hill}}$ from the planet position (where $R_{\text{Hill}}$ is the planet’s Hill radius: Pinilla et al. 2012), we obtain that the planet location is around 58 to 62 au. We use 60 au to perform hydrodynamical simulations of the gas and dust evolution and check if such a planet can create some of the observed structures: in particular, the large cavity and the asymmetric structure seen in the millimeter emission. Uyama et al. (2018) showed the Subaru/HiCIAO companion limits from a separation of 60 au. The mass limits at 60 au are well above (70-80 $M_{\text{Jup}}$) the values considered in our models.

4.2. Hydrodynamical simulations with FARGO3D

We perform hydrodynamical simulations using the publicly available code FARGO3D (Benítez-Llambay & Masset 2016) and use the 2D version of the code (radial and azimuthal). We assume a locally isothermal disk and a power-law radial density profile: $\Sigma = \Sigma_0 r^{-\alpha}$.

We use normalized units such that $G = M_\star + M_P = 1$ and the location of the planet is at $r_P = 1$. The simulations are performed from $r_{\text{in}} = 0.1$ to $r_{\text{out}} = 5.0$. We assume that the planet’s orbital semi-major axis is 60 au; thus, the radial grid spans from 6 to 300 au, and it is logarithmically spaced with 512 cells. The azimuth grid (from 0 to 2$\pi$) is linear with 1024 cells. The outer dust disk radius obtained from the visibility fit of the dust continuum emission is ~ 140 au, and most of the observed disks are two to three times larger in gas (Ansdell et al. 2018), which supports our choice for the outer disk radius.

The initial gas surface density $\Sigma_0$ at the position of the planet is such that the disk mass is ~0.05 $M_\odot$ (or 0.02 $M_\star$, assuming the mass of the LkH$\alpha$ 330 star is 2.5 $M_\star$). This mass is consistent with the calculations from the dust-continuum emission (Sect. 2). We assume a flared disk with a flaring index of 0.25 and a disk aspect ratio of 0.06 at the planet location (60 au). This aspect ratio is obtained assuming that the temperature profile is (Kenyon & Hartmann 1987)

$$T(r) = T_\star \left(\frac{R_\star}{r}\right)^{1/2} \phi_{\text{inc}}^{1/4},$$

where $R_\star = 2 R_\odot$, and $T_\star = 5800 \text{ K}$ as in Andrews et al. (2011). The incident angle $\phi_{\text{inc}}$ is taken to be 0.05. The values of the aspect ratio and flaring index of our models agree with the best values of the models for fitting the spectral energy distribution (SED) of LkH$\alpha$ 330 by Andrews et al. (2011). In these radiative transfer models, the scale height is 6.5 au at 100 au (i.e., an aspect ratio of 0.065), with a flaring index of 0.2.

The planet-to-star mass ratio is $4 \times 10^{-3}$ (10 $M_{\text{Jup}}$ around a 2.5 $M_\star$ star). We consider three values of planet eccentricity ($e = 0.0, 0.1$, and 0.2). This choice is motivated by recent models that demonstrate that spiral arms launched by eccentric plan-
ets can change their pitch angle along the spiral (e.g., Zhu & Zhang 2022), potentially appearing as two distinct spiral arms as in our SPHERE observations. Such planet mass is introduced in the first 100 orbits into the smooth disk. Planetary accretion and planet migration are not considered in these simulations. Depending on the planetary gas accretion rate, the gap shape (width and depth) can vary, and hence it can affect the potential formation of vortices at the edges of the carved gap when planet accretion is considered (Bergerz-Casalou et al. 2020). For massive planets such as those assumed in this work, 3D hydrodynamical simulations including planet migration have shown that a vortex can form at the outer edge of the planetary gap, diffusing material into the gap and migrating inwards with the planet (Lega et al. 2021). Therefore, these two limitations can affect the interpretation of our models. The gravitational effect of the planet is smoothed out, such that the gravitational potential \( \phi \) is softened over distances comparable to the disk scale height:

\[
\phi = -\frac{Gm_p}{(r^2 + \epsilon^2)^{\frac{1}{2}}},
\]

where \( m_p \) is the planet mass and \( \epsilon \) is taken to be 0.6\( h \) (where \( h \) is the disk scale height defined as \( h = c_s/\Omega \), with \( c_s \) the sound speed and \( \Omega \) the Keplerian frequency).

Besides the gas evolution, we include the evolution of four dust species as in the FARGO3D version of Benítez-Llambay et al. (2019), with the dust diffusion implementation from Weber et al. (2019). These grains have sizes of 1, 10, 100, and 1000 \( \mu \)m. These particles are initially distributed as gas with a dust-to-gas ratio of 0.01. We assume a power-law for the dust grain size distribution, such that \( n(a) \propto a^{-3.5} \). The intrinsic volume density of the particles is assumed to be \( \rho_s = 1.6 \text{ g cm}^{-3} \). Finally, we take an \( \alpha \) viscosity (Shakura & Sunyaev 1973) of 10\(^{-4}\), in agreement with recent suggestions of low viscosity in disks (e.g., Flaherty et al. 2015, 2017; Teague et al. 2016). This value of disk viscosity is also taken for the dust turbulent diffusion.

A summary of the results of our simulations is given in Fig. 9, which shows the gas surface density and the dust surface density for each grain size. All panels are normalized to the initial gas or dust surface density. We show the results for each eccentricity value after around 500 orbits (~0.15 Myr). The exact output that is selected for this figure is such that the vortex is opposite the planet location. Fig. C.1 shows the same as Fig. 9, but after 3000 orbits (~0.88 Myr).

The planet triggers the RWI that leads to the formation of a vortex at the outer edge of its gap at around 105-120 au (the exact location depends on the planet eccentricity, being further away for higher planet eccentricity). This vortex appears in the gas and the small particles (1 and 10 \( \mu \)m) with an azimuthal contrast of \( 3 - 3.5 \). This contrast is much higher in the density of 100 \( \mu \)m (contrast of 20) and 1000 \( \mu \)m (contrast > 600) dust particles due to particle trapping in the vortex (e.g., Ataiee et al. 2013).

For the case of the planet with zero eccentricity, the vortex starts to dissipate after the first 700 orbits because of the disk’s
Fig. 9. Results from hydrodynamical simulations performed with FARGO3D assuming a planet-to-star mass ratio of $4 \times 10^{-3}$ ($10 M_{\text{Jup}}$ around a 2.5 $M_{\odot}$ star) at 60 au and $\sim0.15$ Myr of evolution ($\sim500$ orbits, where the exact output is taken when the vortex is opposite the planet). Each set of panels assumes a different planet eccentricity: $e = 0.0, 0.1, 0.2$ from the top to the bottom. The simulation assumes an $\alpha$ viscosity of $10^{-4}$. For each eccentricity, the top left panel shows the gas surface density, the panels from the top middle to the bottom right show the dust surface density of 1, 10, 100, and 1000 $\mu$m-sized particles, respectively.
Fig. 10. Comparison of models and observations. Upper left panel: Overlap of ALMA and SPHERE observations, both images are deprojected, and a distance of 318 pc is used to change the units to au. The colors are SPHERE data of LkHα 330 in the H-band ($Q\phi \times r^2$) in linear scale, and the contours are ALMA data of LkHα 330 in Band 6 (1.3mm) every 20%, 40%, 60%, and 80% of the peak of the emission. Other panels: Zoomed-in view of the dust density distribution of 1 $\mu$m-sized dust particles from the hydrodynamical simulations shown in Fig. 9 for the three values of the eccentricity. The same coronograph as the SPHERE observations covers the inner disk. The arrows aim to qualitatively compare the observed structures (especially from SPHERE) with the models.

For the case where the planet eccentricity is 0.1, the vortex lives for $\sim$500 orbits in the gas and hence in the distribution of the small-sized particles (1 and 10$\mu$m); but, as in the case of zero eccentricity, the concentration of the large sized particles takes longer to dissipate. In the case of $e = 0.1$, the asymmetry in the large particles (100 and 1000$\mu$m) lives until around 700 orbits, and then the concentration becomes a ring-like structure that merges with the outer ring, as is shown in Fig. C.1, where a clear ring-like structure is formed in the density of the 100 and 1000$\mu$m-sized particles at $\sim$ 140 au.

For the case of $e = 0.2$ a similar situation occurs. The vortex in the gas density and the concentration of the small-sized parti-
cles (1 and 10 µm) survives until around ~ 400 orbits, and in the large grains it remains until ~ 600 orbits. The ring-like structure that remains is initially very eccentric, but it circularizes with time, as seen when comparing Fig. 9 and Fig. C.1. Based on these results, we hypothesize that if the planet is in an eccentric orbit, it must be very young to explain the azimuthal asymmetry observed with ALMA.

Planets are a natural explanation for the formation of spiral arms and the structures observed in near-infrared scattered light (e.g., Bae & Zhu 2018a). However, it has been shown that to reproduce the contrast of these spiral arms as observed, 3D simulations are required because 2D simulations usually underestimate their brightness (Juhász et al. 2015; Dong & Fung 2017).

Because of the limitations in comparing our 2D simulations with the observations in scattered light, we only performed a visual inspection of the spiral arms launched by the proposed planet and qualitatively compared it with the scattered-light observations. Fig. 10 shows the overlap of ALMA and SPHERE observations. Both images are deprojected, and we use a distance to the source of 318 pc to show the scale in au. We compare the observations with the results from the hydrodynamical simulations and show a zoomed-in view of the dust density distribution of 1 µm-sized dust particles for the three values of the eccentricity.

The planet launches three spiral arms, two inner spiral arms, and one outer spiral arm, in agreement with the results from Bae & Zhu (2018b). In the models where the planet has some eccentricity, the spiral arms are distorted, in particular the outer spiral arm, which shows that the pitch angle suddenly changes values in different locations, as shown by Zhu & Zhang (2022). In this comparison, part of the inner ring observed with SPHERE is part of the inner spiral, which could explain the non-uniform brightness distribution of this ring. The outer spiral could be the one observed with SPHERE in the north-east, which passes through the vortex, making it very prominent again in the (south-) west. As we explain in Sect. 2, the pitch angle of the two spiral arms is similar, which may indicate that the origin is the same and the difference may originate from the distortion expected when the planet is in an eccentric orbit and/or when it passes through the vortex. The launching points of our two spiral arms inferred from the SPHERE observations are further away from the planet position (~90 au), and a possible explanation is that the inner ring at ~45 au is hot and puffed up, blocking the starlight near the planet.

4.3. Radiative transfer and comparison with the dust-continuum emission from ALMA

In order to compare the results from the hydrodynamical simulations to the ALMA observations, we perform radiative transfer calculations with RADMC3D (Dullemond et al. 2012). We calculate the opacity of each grain size from the FARGO simulations considering the DSHARP opacities (Birnstiel et al. 2018) and using optool (Dominik et al. 2021). We assume a black-body radiation field from the central star as the radiation source and use $1 \times 10^7$ photons and $5 \times 10^6$ scattering photons for our calculations.

To calculate the total volume dust density, we follow

$$\rho_d(R, \varphi, z, St) = \frac{\Sigma_d(R, St)}{2 \pi R h_d(R, St)} \exp \left( \frac{z^2}{2 h_d^2(R, St)} \right),$$

(5)

where $z = r \cos(\theta)$ and $R = r \sin(\theta)$, with $\theta$ being a polar angle. We keep the same radial and azimuthal resolutions as for the hydrodynamical simulations. For the vertical grid, we use 128 cells. The particle scale height $h_d$ is given by (Youdin & Lithwick 2007; Birnstiel et al. 2010)

$$h_d(St) = h \times \min \left( 1, \sqrt{\frac{\alpha}{\min(St, 1/2)(1 + St^2)}} \right),$$

(6)

where $St$ is the Stokes number of the dust particles calculated at the midplane, that is $St = \frac{2 \pi d^2 \rho_d}{\sigma}$. Under the assumptions of our model, a 1 mm particle at ~110 au has $St$~0.1, implying that the scale height of the 1 mm grains is around 3% of the disk scale height. Thus, millimeter-sized particles are well confined in the midplane, whereas the micron-sized particles have $St$~ $10^{-4}$ in
the outer region, and therefore their scale height is almost the same as the gas.

We obtain the temperature profile for each grain size and calculated images at 1.3 mm. We assumed the distance, PA, and disk inclination of LkH$\alpha$ 330. To create realistic ALMA images with the same $uv$ coverage as the actual observations, we use the SIMO package \(^1\), which replaces the observed visibilities with the radiative transfer model visibilities. Before the radiative transfer modelling, we remove the emission from the inner disk (<50 au), which is not detected with ALMA. In simulations that include the growth and fragmentation of dust particles, the inner disk is expected to be depleted of dust in around one million years, when the gap carved by the planet efficiently filtered dust particles from the outer disk, while the dust initially located inwards of the planet grows and efficiently drifts toward the star (e.g., Pinilla et al. 2016b).

Figure 11 shows the comparison between the model and observations when taking the outputs from the hydrodynamical simulations after 500 orbits (Fig. 9), for different planet eccentricities. For $e = 0.0$, the dust is highly concentrated in the center of the vortex, creating a more compact asymmetry compared to observations; this is the case even after 3000 orbits (Fig. C.1). For the case of $e = 0.2$, the asymmetry is similar to that observed with ALMA; however, the cavity is very eccentric in contrast to the ALMA observations. In the case of $e = 0.1$, the main asymmetry is surrounded by a ring, and after convolution with the beam, the two (the asymmetry and the ring) almost merge. A point-like structure is obtained at the location of the planet, which remains in the simulations due to the lack of proper planet accretion (Bergez-Casalou et al. 2020).

5. Discussion

5.1. Different radial distribution of the scattered light, millimeter emission, and CO lines

The disk around LkH$\alpha$ 330 shows a large segregation (radial and azimuthal) of the distribution of small grains traced with scattered light, the large grains traced with the dust-continuum emission from ALMA, and the gas distribution potentially traced with the emission from CO isotopologues. The radial difference in these distributions can be seen in Fig. 8. In the top left panel of Fig. 10, we overlap the ALMA and SPHERE observations to highlight the different structures at the two wavelengths, in particular in the azimuthal direction, where the location of the end of the south-west spiral in scattered light coincides with the location of the asymmetry observed with ALMA. The potential connection between these structures is discussed in Sect. 5.2.

The radial difference in the distribution of gas and small/large dust particles is typical in observations of transition disks (e.g., Dong et al. 2012; van der Marel et al. 2016; Villenave et al. 2019), and it is expected from planet-disk interaction models as shown in Sect. 4. In the assumption of our models, the planet is located at 60 au in order to have the asymmetric ring at a similar location to the observations (~110 au). This simulation succeeds in explaining the asymmetry and potentially the formation of a faint outer ring as observed, although at a different location, ~140 au in the models versus 200 au in the observations. Therefore, after convolution with the ALMA beam, the asymmetry and the outer ring obtained in the models almost merge.

This model is roughly consistent with the distribution of the small dust particles and the gas. In the observations, $^{12}$CO, which is usually optically thick, blends in the inner disk, while the $^{13}$CO and the scattered light peak at the same location at around 45-50 au (Fig. 8). The fact that these two peaks coincide supports the idea that $^{13}$CO is also optically thick and traces variations in disk temperature (as the scattered light) instead of gas-surface-density variations. The hydrodynamical models presented in Sect. 4 do predict a faint ring (in gas and in small dust species) inside the planet gap (see zoomed-in images in the panels in Fig. 10). The inner edge of the gap is located at 45 au. This ring is not fully symmetric due to the launched spiral arms inside the planet’s orbit, and it could potentially explain the ring and its brightness variations observed in scattered light. However, when we perform radiative transfer models and create images at 1.6 μm to compare with observations, the ring from the synthetic images looks mostly symmetric (Fig. D.1), but this is likely due to the fact that our simulations are 2D and cannot produce the high contrast of the spirals obtained from more realistic 3D simulations. Similarly, in the 1.6 μm synthetic images the outer spiral arm is also very faint, and the vortex dominates the emission (Fig. D.1). A possible way to mitigate this inconsistency is to use another equation of state. We use vertically isothermal disks, while with an adiabatic equation and long cooling times the contrast of the spirals is expected to increase, making possible to detect them even with ALMA observations with high levels of sensitivity and high resolutions (Speedie et al. 2022).

As we mention in Sect. 4.3, in simulations where dust growth is also included, it is expected that this inner disk is not long-lived because particles grow and quickly drift inwards. One possible solution is that fragmentation of particles is efficient in these regions, making it possible to continuously keep small (micron-sized) particles in the inner disk that are well coupled to the gas, which remain invisible at millimeter emission.

The $^{12}$CO, $^{13}$CO, and C$^{18}$O lines seem to be less abundant in the inner disk. These molecular line observations have a very low signal-to-noise ratio, and they lack short baselines, so the nature of these emission lines in the inner disk is poorly constrained from observations. The $^{13}$CO and C$^{18}$O peak close to the location where the planet is assumed in the models (60 au). In our simulations, there is very little material in the co-rotation region of the planet, and it is insignificant compared to the material inside and outside the planet’s orbit. In fact, this co-rotation material is only expected to be observable for low-mass planets that do not open a deep gap (e.g., Pérez et al. 2019; Weber et al. 2019), creating at least three observable rings. A possible explanation is that the peak of $^{13}$CO and C$^{18}$O is tracing the location where the gas surface density starts to increase (instead of the actual peak of the gas density), possibly because both of these lines may not be fully optically thin. In the simulations, the gas surface density starts to increase at around 65 au reaching its maximum at the location of the vortex. Nonetheless, to test this idea, thermochemical simulations are needed, which are not included in our models. Higher sensitivity observations are needed to better constrain the shape of the CO emission and its isotopologues and see if their emission agrees with the existence of a real gas cavity or an actual gap in the gas surface density.

Planets are not the only possible explanation for the radial segregation seen between the gas and small/large dust particles. The presence of a dead zone interplaying with a magneto-hydrodynamical wind (Pinilla et al. 2016a) or a photoevaporative wind (Gárate et al. 2021) can also explain such differences. In addition, at the outer edge of a dead zone, vortices can be formed due to the RWI as well (Flock et al. 2015). Furthermore, variations of the disk viscosity can also trigger spiral arms (Lyra et al. 2015), but in this case numerous spiral arms would be expected.

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\(^1\) https://www.nicolaskurtovic.com/simio/

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while only two are detected in current observations. However, the extension of a dead zone for a star such as LkHα 330 is expected to be around 20 au (Delage et al. 2022), which is much smaller than the observed cavity. A clear way to distinguish this scenario from the planet scenario is to actually detect potential planet(s) or their circumplanetary disks inside the cavity, as in the case of PDS 70 (Kepler et al. 2018; Benisty et al. 2021).

5.2. Origin of the spiral arms and millimeter asymmetry

The pitch angles of observed spiral arms are larger compared to the ones obtained from models of planet-disk interaction, in particular when comparing with the spirals expected outside the planet’s orbit. The pitch angle of the spiral arms is directly connected to the local scale height of the disk, that is the disk temperature. Typically, to obtain the large observed pitch angles, the disk temperatures need to be unrealistically high (Benisty et al. 2015). In our hydrodynamical simulations we have a similar problem and the spiral arms look tighter in the simulations when compared to the SPHERE observations. In addition, the disk temperature is vertically stratified such that the surface is hotter than the midplane. Spirals in 3D simulations adopting vertical temperature stratification have larger pitch angles in the surface than the midplane (e.g., Juhász & Rosotti 2018).

One way to reconcile this discrepancy is to assume that the planet is located sufficiently far outside the observed spirals, and the primary and secondary arms inside the planet’s orbit are the ones that we observe (as suggested in the case of MWC 758, HD 135344B and HD 100453 Dong et al. 2015; Fung & Dong 2015). Applying this idea to LkHα 330, a possible solution is that a planet is located between the rings observed with ALMA at 110 and 200 au, creating the spiral arms inside its orbit, while the asymmetry may be explained by a vortex at the inner edge of this hypothetical planet, and where dust particles are accumulated in a faint, ring-shaped emission at the outer edge of this gap. Such a scenario cannot explain the formation of the cavity itself (and the observed radial segregation of the gas and dust particles), as we aim to do with the hydrodynamical simulations presented in this paper. Therefore, a potential scenario is the combination of two planets, as investigated by Baruteau et al. (2019) for the case of MWC 758.

Another possibility for the formation of the spiral arms is that the disk is massive and cold enough to be gravitationally unstable, forming several spiral arms in the disk (Lodato & Rice 2004). Such spiral arms could be observed in scattered light, as well in the millimeter emission (e.g., Dipierro et al. 2015), and the observed pitch angles for LkHα 330 can also be explained by gravitational instability (Bae & Zhu 2021). The disk mass obtained from the dust continuum emission is such that the disk-to-stellar mass ratio is 0.02, and the Toomre parameter (Toomre 1964) is well above unity in the disk (assuming the temperature profile of Eq.3). However, the calculation of the disk mass is highly uncertain when using the millimeter flux, due to the assumptions of the optical depth, dust opacities, dust temperature, and dust-to-gas mass ratio. A potential diagnostic to determine if LkHα 330 may be gravitationally unstable is to detect signatures in the disk kinematics, where, unlike in the planet-disk interaction case, the gravitational-instability spirals perturb the velocity in the entire disk, creating wiggles that are visible at all disk radii and all azimuthal angles (Hall et al. 2020).

For the origin of the asymmetry, we explored the possibility of a vortex triggered by the RWI in the context of planet-disk interaction. As mentioned in the previous section, another possibility is a vortex formed by the same instability at the edge of a dead zone. Besides these possibilities, disk eccentricity can create azimuthal overdensity features, as in the cases where there is a binary companion (e.g. Calcino et al. 2019; Ragusa et al. 2020). For LkHα 330, there are no observational signatures of a binary companion (Uyama et al. 2018).

Finally, the vortex itself may trigger the spiral arms (Paardekooper et al. 2010; Chametla & Chrenko 2022). From the millimeter fluxes, we inferred that the mass inside the asymmetry could be a few Jupiter masses (Sect. 2). This is a tentative alternative because of the overlap of the south-west spiral arm with the location of the asymmetry. However, the spirals triggered by a vortex are expected to be weak density waves and impossible to detect in scattered-light observations (Huang et al. 2019).

5.3. Origin of the faint rings around the main asymmetric structure

Recent high angular resolution observations of transition disks have unveiled that the ring-shaped accumulation of dust particles around the cavity of these disks is a composite of more complex substructures. Some examples are the cases of the transition disks around LkCa 15, 2MASS J16100501-2132318 (Facchini et al. 2020), HD 135344B (Cazzoletti et al. 2018), SR 21 (Muro-Arena et al. 2020), and PDS 70 (Kepler et al. 2019; Benisty et al. 2021). In addition, in some of these observations a very faint ring has also been detected in the outer regions far away from the main structures, as in the cases of HD 100546 (Walsh et al. 2014; Fedele et al. 2021; Pyerin et al. 2021), AA Tau (Loomis et al. 2017), HD 97048 (van der Plas et al. 2017), and DM Tau (Kudo et al. 2018).

Facchini et al. (2020) suggested that the equation of state considered in the simulations can lead to the production of one or multiple rings around the main cavity. In a vertically isothermal disk, the interaction with a planet can lead to multiple rings, while in an adiabatic disk with large cooling factors and the same disk and planet parameters can lead to a single ring. In that paper, where the authors present ALMA observations of LkCa 15 and 2MASS J16100501-2132318, the main ring is composed of two rings, where the inner ring is brighter than the outer ring, which contradicts what we see in our observations of LkHα 330; hence, it is unclear if adiabatic simulations of planet-disk interaction can produce the right brightness distribution for LkHα 330.

Another degeneracy concerning the number of rings that a single planet can create comes from the assumed planet mass. For a low-mass planet, the material in the co-rotation region can be observable, creating at least three rings (one inside, one at the co-rotation region, and one outside the planet; e.g., Bae et al. 2017; Dong et al. 2017; Pérez et al. 2019). As we discuss in Sect. 5.1, a low-mass planet cannot explain the formation of the cavity itself, but it is still possible that there is a low-mass planet between 60 and 110 au and/or between 110 and 200 au.

An additional degeneracy about the number of rings is the inclusion of dust growth and fragmentation (e.g., Bae et al. 2018; Bergez-Casalou et al. 2022). In this case in particular, the dust turbulent parameter plays a key role because if dust is highly diffused in a disk, even when a pressure trap is present, dust particles may not accumulate in the pressure bump (de Juan Ovelar et al. 2016). In addition, faint rings around the main accumulation of the large grains can be formed due to the ring’s self-evolution effect on the disk’s thermal structure (Zhang et al. 2021).

Finally, for the formation of a very faint ring in the outer disk, a possible scenario is that there is an outer planet trapping the
particles, but such a planet must form late in the evolution, such that most of the dust has drifted inwards and little dust is outside to be trapped (Pinilla et al. 2015). Alternatively, if the initial disk gas surface-density distribution is a power law tapered with an exponential function, then any planet that is located outside the cutoff radius can trap only the little amount of dust that is outside (Pyerin et al. 2021). In our models, we do reproduce an outer ring without the need for an extra planet, but this is closer in than observed.

5.4. Effect of planet eccentricity

Planet eccentricity adds another degeneracy to planet-disk interaction models as investigated by Chen et al. (2021), where a lower mass planet in an eccentric orbit can create a similar gap shape as a more massive planet. Planet eccentricity can affect the vortex by smoothing the outer gap edge, breaking the RWI condition for its formation. D’Angelo et al. (2006) and Hosseinibor et al. (2007) investigated how the disk-planet interaction can affect the gap and planet eccentricities. They found that an eccentric planet carves a shallower and broader gap, implying that the density profile at the gap edge is less steep than the ones of a gap created by a Jovian planet. Therefore, it is harder to open a gap by a planet on a circular orbit. Consequently, the planet eccentricity can also affect the vortex’s survival and the dust concentration. In our simulations, the vortex lives over shorter timescales, and therefore the dust concentration is more azimuthally extended and has lower contrast once the vortex starts to dissipate. In addition, the planet eccentricity can also affect the shape of the launched spiral arms as we discuss earlier in the paper, whereby the spiral pitch angle can change along the spiral.

Finally, Duffell & Dong (2015) showed that the depth of the gaseous gap created by a Jovian planet can be reduced by one order of magnitude when the planet is in an eccentric orbit with values of $e > 0.1$. This can have direct consequences on the emission of CO and isotopologues observed inside the cavity, but thermochemical models coupled with hydrodynamical simulations are required to properly quantify this effect.

6. Conclusions

In this paper, we present new scattered light SPHERE observations at $J$–Band (1.2$\mu$m) and $H$–Band (1.6$\mu$m), in addition to new ALMA observations in Band 6 (1.3 mm) of the transition disk around LkHa 330. These observations are compared to hydrodynamical simulations that include gas and dust evolution with the goal of explaining the observed structures with a single planet, which does neither migrates nor accretes material. The main conclusions are the following.

- The SPHERE observations reveal two types of clear structures. First, a non-uniform ring in brightness at around 45 au from the star, with brightness variations along the ring of $\sim$50%. Second, two spiral arms, one in the north-east and the other in the south-west with similar pitch angles ($\sim$9–11$^\circ$) and radial launching points ($\sim$90 au). However, there is a high uncertainty on the pitch angles of the spirals in particular of the south-west due to the unknown geometry of the scattered light (the inclination and position angle is assumed from the dust continuum emission).
- The ALMA observations of the dust-continuum emission reveal three main structures: a large cavity surrounded by a faint inner ring at around 60 au; a bright asymmetric ring at around 110 au, and this asymmetry has an azimuthal width of around 20$^\circ$; in addition to a faint ring at around 200 au.
- The $^{12}$CO, $^{13}$CO, and $^{18}$O lines seem to be less abundant in the inner disk. All of these lines peak inside the main ring observed in the dust-continuum emission (at 110 au). The $^{13}$CO peaks at a similar location to the inner ring observed with SPHERE ($\sim$45 au), while the $^{18}$O peaks around 60 au, which is very close to the faint inner ring observed in the dust continuum with ALMA. Any conclusions about the gas distribution from these CO observations must be taken with caution because they have poor signal-to-noise ratios due to the lack of short baseline observations and short integration times.
- The radial segregation in the distribution of the gas and small and large dust particles can be reproduced when assuming a 10 $M_{Jup}$ planet located at 60 au. Such planet mass is well below the current observational limits for planetary companions at such distances (Uyama et al. 2018).
- Our qualitative comparison of the observations with hydrodynamical simulations suggests that to explain the asymmetry seen with ALMA, the planet should be in an eccentric orbit with $e = 0.1$. A planet in a circular orbit leads to a very narrow azimuthal concentration of the particles compared to observations, whereas a planet in a more eccentric orbit leads to a very eccentric cavity during the timescales when the asymmetry is still present. At longer times, the cavity circularizes, but the asymmetry also decays. The results from these models suggest that the planet is young.
- According to our comparison with hydrodynamical simulations, it is possible that the two spiral arms observed with SPHERE originate from the outer spiral launched by the proposed eccentric planet, which corresponds to the spiral in the north-east. When the spiral passes through the vortex, it becomes very prominent again in the (south-) west. In this scenario of the eccentric planet, the pitch angle changes along the spiral in addition to the distortion when it overlaps with the vortex, explaining why in the observations one single spiral may appear as two.

Our results show that LkHa 330 is an exciting target to search for (eccentric) planets while they are still embedded in their parental disk, making it an excellent candidate for planet-disk interaction studies.

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Appendix A: Visibility fit

Figure A.1 shows the fit to the real and imaginary part of the visibilities to the model with the best-fitting parameters from galario.

Fig. A.1. Real (upper panel) and imaginary (lower panel) part of the binned and deprojected visibilities versus the model with the best-fitting parameters from galario (red solid line). The error bars correspond to the standard error in each bin.

Appendix B: Channel maps and moment 8 maps

Figure B.1 shows the channel maps of the $^{12}$CO, $^{13}$CO, and C$^{18}$O of LkH$\alpha$ 330 from our ALMA observations. Figure B.2 shows the moment 8 maps (peak value of the spectrum) of the $^{12}$CO, $^{13}$CO, and C$^{18}$O lines of LkH$\alpha$ 330.
Fig. B.1. Channel maps of $^{12}$CO, $^{13}$CO, and C$^{18}$O of LkH$\alpha$ 330. The contours are at the $5 \times \sigma$ level of the continuum emission. The scale bar in the left panel represents a scale of 50 au.
Fig. B.2. Moment 8 map (peak value of the spectrum) of the $^{12}$CO, $^{13}$CO, and C$^{18}$O lines of LkH$\alpha$ 330.
Appendix C: Hydrodynamical simulations at longer times of evolution

Figure C.1 shows the results from hydrodynamical simulations as in Fig. 9, but at 0.88 Myr of evolution (~3000 orbits).
Fig. C.1. Results from hydrodynamical simulations as in Fig. 9, but at 0.88 Myr of evolution (∼3000 orbits).
Appendix D: Synthetic image in H-band

Figure D.1 shows the synthetic image (already deprojected) in the H-band from our radiative transfer calculations, after convolving with a 0.04” Gaussian beam and multiplying by $r^2$. For this image, we use the model of a planet at 60 au and an eccentricity of 0.1 after 500 orbits.

Fig. D.1. Synthetic image in H-band after convolving with a 0.04” Gaussian beam and multiplying by $r^2$ using the model of a planet at 60 au and an eccentricity of 0.1.