Improving Earth-like planet detection in radial velocity using deep learning

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ABSTRACT

Context. Many novel methods have been proposed to mitigate stellar activity for exoplanet detection. Unlike traditional methods that model stellar activity in the RV domain, more methods are moving in the direction of disentangling stellar activity at the spectral level. As deep neural networks have already been proven to be one of the most effective tools in data mining, in this work, we explore their potential in the context of Earth-like planet detection in RV measurements.

Aims. The goal of this paper is to present a novel convolutional neural network-based algorithm that efficiently models stellar activity signals at the spectral level, enhancing the detection of Earth-like planets.

Methods. Based on the idea that the presence of planets can only produce a Doppler shift at the spectral level while the presence of stellar activity can introduce a variation in the profile of spectral lines (asymmetry and depth change), we trained a convolutional neural network to build the correlation between the change in the spectral line profile and the corresponding RV, full width at half maximum (FWHM) and bisector span (BIS) values derived from the classical cross-correlation function.

Results. This algorithm has been tested on three intensively observed stars: Alpha Centauri B (HD 128641), Tau Ceti (HD 10700), and the Sun. By injecting simulated planetary signals at the spectral level, we demonstrate that our machine learning algorithm can achieve, for HD 128621 and HD 10700, a detection threshold of 0.5 m s\(^{-1}\) and the Sun. By injecting simulated planetary signals at the spectral level, we demonstrate that our machine learning algorithm can achieve, for HD 128621 and HD 10700, a detection threshold of 0.5 m s\(^{-1}\) in semi-amplitude for planets with periods ranging from 10 to 300 days. This threshold would correspond to the detection of a \(\sim 5 M_E\) planet in the habitable zone of those stars. On the HARPS-N solar dataset, thanks to significantly more data, our algorithm is even more efficient at mitigating stellar activity signals and can reach a threshold of 0.2 m s\(^{-1}\), which would correspond to a 2.2 \(M_E\) planet on the orbit of the Earth.

Conclusions. To the best of our knowledge, it is the first time that such low detection thresholds are reported for the Sun, but also for other stars, and therefore this highlights the efficiency of our convolutional neural network-based algorithm at mitigating stellar activity in RV measurements.

Key words. methods: data analysis – techniques: radial velocities – techniques: spectroscopic – planets and satellites: detection – stars: activity

1. Introduction

The detection of low-mass planets using the radial-velocity (RV) technique remains extremely challenging in the presence of stellar activity. Stellar activity is the result of complex underlying physical processes happening at different timescales (e.g., Meunier et al. 2010, 2017). For example, granulation and supergranulation contribute to stellar activity most on timescales of hours to a few days (e.g., Del Moro et al. 2004; Del Moro 2004; Dumusque et al. 2011), while dark spots and bright faculae regions contribute to photometric and RV variations on the timescale of the host star’s rotational period (e.g., Saar & Donahue 1997; Dumusque et al. 2014; Zhao & Dumusque 2023). On the timescale of years, the magnetic cycle of the host stars contributes to stellar activity the most (Lovis et al. 2011; Haywood et al. 2016, 2022).

Machine learning is one of the most efficient and successful tools to handle large amounts of data in the scientific field. Many algorithms based on machine learning have been proposed to mitigate stellar activity to better detect low-mass and/or long-period planets. These algorithms can be classified into two categories: supervised learning and unsupervised learning. The advantage of supervised learning is that the proposed model contains a large set of variables and has the ability to produce relatively accurate predictions based on the training data. The Gaussian process (GP), as a supervised learning algorithm, is widely used to mitigate stellar activity using photometric or spectroscopic data. By carefully selecting the parametric kernels and priors, GP can efficiently model stellar activity (Perger et al. 2021; Nicholson & Aigrain 2022; Aigrain & Foreman-Mackey 2023). The potential drawback of GP is data overfitting when the hyperparameters or priors of GP are not chosen wisely. This
may lead to erroneous parameter estimates for the detected planets (e.g., Blunt et al. 2023) or to the difficulty of resolving weak planetary signals as they might be absorbed by the fitted GP (e.g., Langelier et al. 2021). Some previous work has already demonstrated the power of the convolutional neural network (CNN) in detecting transiting exoplanet signals (Shallue & Vanderburg 2018; Dattilo et al. 2019), and also in mitigating stellar activity in RVs. In de Beurs et al. (2022), the authors explain how they used a CNN to efficiently model stellar activity at the level of the cross-correlation functions (CCF Baranne et al. 1996) derived from the HARPS-N solar observations (Dumusque et al. 2015, 2021; Phillips et al. 2016; Collier Cameron et al. 2019). The results show that solar activity is significantly reduced and it was possible to use this framework to detect a planetary signal with a period of 365 days and an amplitude of 0.4 m s\(^{-1}\). Perger et al. (2023) used several stellar activity indices as inputs to train a CNN and predict the corresponding stellar activity affecting the RVs. The CNN application on \(\epsilon\) Eridani and AU Microscopii showed that the stellar activity signal of the two stars can be greatly reduced. Nieto & Díaz (2023) trained a convolutional neural network in the periodogram domain to classify whether the planetary signals can be detected or not in RV time series affected by correlated noise. The performance on the simulated RV data shows an improvement of 28% fewer false positives. These successful applications demonstrate that CNNs are powerful tools to model stellar activity and enhance the detectability of planetary signals embedded into astrophysical noise; however, they also reveal the disadvantages of CNNs. Indeed, the major drawbacks of CNNs are the hyperparameter tuning and the generalization from the training set. There are many hyperparameters that need to be tuned during the training process. This part usually involves human interference and may not be optimal for different stellar types. Even when the tuning is done properly, the fact that a CNN model contains a large number of free variables makes it difficult to generalize the target features from the training data, which can lead to bad predictions.

Many methods based on unsupervised learning have also been proposed to mitigate stellar activity at either the CCF level or the spectral level. Davis et al. (2017) developed a principle component analysis (PCA) algorithm for simulated stellar activity affected spectral time series. This algorithm showed that eigenvectors of PCA are greatly affected by spectral line shape variation. Cretignier et al. (2020a, 2022) further explored this idea and converted stellar spectra into flux-flux gradient space and implemented PCA to mitigate stellar activities in HD10700 (\(\tau\) Ceti) and HD 12861 (\(\alpha\) Cen B) RV datasets. On 5 yr of HD 12861 data, the authors show that stellar activity at the rotational period was significantly removed and the RV root mean square was significantly reduced from 2.44 m s\(^{-1}\) down to 1.73 m s\(^{-1}\). Collier Cameron et al. (2021) applied PCA to the autocorrelation function (ACF) of HARPS-N solar data CCF and were able to disentangle stellar activity from a planet signal of semi-amplitude \(-0.4\) m s\(^{-1}\). Compared to supervised learning algorithms, unsupervised learning algorithms have few hyperparameters to be tuned and may avoid overfitting; however, they strongly suffer from the quality of the input data. For example, some low-rank eigenvectors derived from PCA may be very sensitive to the noise level or outliers in the input data (e.g., Ould-Elhkim et al. 2023). This may lead to a challenge in selecting proper sets of latent features for stellar activity removal. Furthermore, the limitation of employing PCA lies in its linear decomposition of inputs. Given that stellar activity represents a complex physical process, important features or proxies may be embedded in spectral time series in a nonlinear manner, which may not be captured due to the linearity of inputs. CNN, in contrast, is known for its ability to capture nonlinear features in input data.

In this paper, we propose a CNN-based algorithm that has the ability to efficiently remove stellar activity and improve the detection efficiency of low-mass, long-period exoplanet signals. The CNN architecture and hyperparameters can be automatically optimized for different stellar types. We describe the preprocessing of the spectral data and the strategy to generate training data in Sect. 2. The architecture of the neural network and methods for automatic hyperparameter tuning are described in Sect. 3. In Sect. 4, we explain how we applied the CNN to three stars: the Sun, HD 128612, and HD 10700, and we derived the detection limits of low-mass exoplanets for these stars. Finally, we draw our conclusion in Sect. 4. The code of this algorithm is publicly available on GitHub\(^1\).

2. Spectra preprocessing and dataset preparation

Two recent studies have shown that a CNN framework can be applied to mitigate stellar activity in RV measurements. Perger et al. (2023) uses as input of a CNN several time series (CCF FWHM, BIS and contrast, multiband photometry) to model as output the RV measured as the mean of a Gaussian fit to the CCF. Although the CCF, FWHM, BIS and contrast contain some information about the CCF asymmetry, they do not necessarily capture all the information for optimal stellar activity modeling. De Beurs et al. (2022) chose to use as input the full CCF to model stellar activity on the HARPS-N solar data. However, as demonstrated in Dumusque (2018), stellar activity can be significantly reduced by carefully selecting certain absorption lines in the spectra. Therefore, there is clearly some information about stellar activity at the spectral level that a CCF might not be sensitive to, as by construction, the CCF is an average of most of the lines in a spectrum. If spectral lines are affected differently by stellar activity, which should be the case as lines are formed at different depths in the stellar photosphere and are therefore affected differently by the magnetic field, a CCF will wipe out those differential effects and thus it might be more difficult to probe and model stellar activity at the CCF level than at the spectral level. Some pioneering works described in Cretignier et al. (2020a), Wise et al. (2022) and Al Moulla et al. (2022) demonstrate how spectral lines are differently affected by stellar activity, and explain the observed behavior based on the physics of stellar atmospheres.

The above discussion strongly motivates the development of methods to model stellar activity at the spectral level and there are already a few frameworks that show promising results (e.g., Binnenfeld et al. 2020, 2022; Shahaf & Zackay 2023). However, a HARPS-N spectrum has hundreds of thousands of data points. This is three orders of magnitude larger than the input data used in the CNN frameworks described in the preceding paragraph, and using spectra as input of a CNN will very significantly increase the complexity of the CNN architecture, with a risk of overfitting at the end, without speaking about the time needed to train the network. Our approach is therefore to use a dimensional space which is in-between the stellar spectrum and a CCF in terms of input dimension and in terms of capturing differential effects due to stellar activity between spectral lines. The chosen space is the normalized flux-flux gradient space (hereafter shell spectral representation) described in Cretignier et al. (2022).

\(^1\) Code available here https://github.com/YinanZhao21/DeepLearningShell
This space has been specifically designed to reduce the dimension of a spectrum while maximizing the information induced by the inhibition of the convective blueshift, the main contributor of stellar activity on solar-type stars. A detailed description of the transformation from spectrum to shell is presented in Sect. 2.1.

The bottleneck in training a neural network to mitigate stellar activity is the limited number of observed spectra. Stars significantly observed have at most a few thousand observations, and it is expected that stellar activity behavior changes for different spectral types, therefore it is dangerous to merge the data of different stars together. It is tempting to rely on simulated data for different stars together. It is tempting to rely on simulated data to train a CNN, however, due to the complexity of the physics behind stellar activity, good performance on simulated data usually leads to a moderate performance on the real observed stellar spectra. In order to solve the limitation of the training sample size, de Beurs et al. (2022) first introduced the cross-validation technique to increase the sample size during the training process. In this work, we adopt this technique to train our neural network for different stars. We describe this in Sect. 2.2.

2.1. Definition and motivation of the shell spectral representation

The shell spectral representation was first defined in Cretignier et al. (2022) and in this section, we revisit its definition to be more sensitive to stellar activity. From the physics of stellar atmospheres, all photospheric spectral lines share the same bisector, which traces the velocity of stellar convection as a function of depth into the photosphere (e.g. Dravins 2008; Gray 2009). The cores of shallow spectral lines, probing deep regions into the photosphere, are strongly blueshifted compared to the laboratory wavelength of the line transitions, which is not the case for the cores of strong lines, which are formed toward the top of the photosphere (e.g. Reiners et al. 2016; Al Moulla et al. 2022). Therefore, convection is strong deep inside the photosphere, with values of a few hundred of m s\(^{-2}\) for the solar case, and nearly zero close to the chromosphere. The strong magnetic fields present inside active regions tend to inhibit stellar convection (e.g. Cavallini et al. 1985), and therefore the cores of shallow lines, but also the wings of strong lines close to the continuum will be strongly affected by this inhibition of convective blueshift, while the core of strong lines should not be affected as there is no convection to inhibit. In summary, the bisector of spectral lines encodes a lot of information regarding stellar activity. By cross-correlating a stellar spectrum with a mask that has different weights for each spectral line, as it is generally done to optimize RV precision (Pepe et al. 2002), the cross-correlation technique destroys the original line bisector and some information about stellar activity is lost in the process. To be more sensitive to stellar activity, we should consider a CCF without line weighting, or the “shell” spectral representation, described in Cretignier et al. (2022) and revisited below.

Let us consider two spectra \(f(\lambda)\) and \(f_0(\lambda)\) that are defined on the same grid in wavelength \(\lambda\) but that are Doppler-shifted by an amount that is small compared to the sampling\(^{2}\). The observed flux variation at pixel \(i\) can be expressed as (see also Bouchy et al. 2001):

\[
f(\lambda_i) - f_0(\lambda_i) = \frac{df_0(\lambda_i)}{d\lambda_i} \cdot \delta \lambda_i = \frac{df(\lambda_i)}{d\lambda_i} \cdot \frac{\delta V}{c} \cdot \lambda_i,
\]

\(^{2}\) Typical sampling for a high-resolution \(R = 100’000\) spectrograph is several hundreds of m s\(^{-1}\), so this assumption is most of the time valid when working with high-precision RVs.

Considering that the Doppler shift formula is \(\delta V/c = \delta \lambda/\lambda, \delta V\) being the Doppler shift and \(c\) the speed of light. We can therefore rewrite:

\[
\delta V_i = \frac{c}{\lambda_i} \cdot (f(\lambda_i) - f_0(\lambda_i)) \cdot \left(\frac{df_0(\lambda_i)}{d\lambda_i}\right)^{-1} = \frac{c}{\lambda_i} \cdot \delta f_i \cdot \left(\frac{df(\lambda_i)}{d\lambda_i}\right)^{-1},
\]

Following this equation, Cretignier et al. (2022) define the shell spectral representation as being normalised flux as a function of flux derivative with respect to wavelength, \((f_0, \frac{df}{d\lambda})\). With this convention, two similar spectral lines in the blue and red parts of the spectrum will follow different loops in the shell spectral representation due to dispersion (see left panel of Fig. 1). The way line bisector, or velocity of convection as a function of depth, is therefore chromatic in this definition of the shell spectral representation, which will alter the signal induced by stellar activity similarly to a weighted CCF. To prevent that and optimize the extraction of stellar activity, we propose in this paper to define the shell spectral representation as being normalised flux as a function of flux derivative with respect to velocity, \((f_0, \frac{df}{d\lambda})\). In this new shell spectral representation, rewriting Eq. (2):

\[
\delta V_i = \delta f_i \cdot \left(\frac{df(\lambda_i)}{d\lambda_i}\right)^{-1},
\]

we easily see that a pure Doppler shift is simply a gradient in \(\lambda\) direction (see middle panel of Fig. 2). From now on, the term spectral shell will be used to describe the shell spectral representation in velocity space, \((f_0, \frac{df}{d\lambda})\).

Another difference with the spectral shell we use in this paper compared to what is published in Cretignier et al. (2022) is the part of the spectrum that is used to build the spectral shell. In this previous work, the authors were using the full spectrum, which can be a disadvantage as other effects than stellar activity and planetary signals might contaminate the spectral shell. While in a weighted CCF, the weight, which is generally proportional to the contrast of spectral lines, strongly down weight very shallow spectral lines that contain little information, this is not the case in a spectral shell as no weight is applied. To
We must therefore remove from the spectral shell any component that corresponds to a Doppler shift in order to obtain what we refer to as a shape shell. This can be done by first estimating the Doppler shell $S_{\text{Doppler}}$, which can be derived by injecting an arbitrary Doppler shift into the template spectrum $f_0$. Once this is done, the shape shell at time $t$, $S_{\text{shape}}(t)$, can be obtained from the spectral shell at the same time $S(t)$ using the formula:

$$S_{\text{shape}}(t) = S(t) - \langle S(t) \cdot S_{\text{Doppler}} \rangle S_{\text{Doppler}}.$$  

(4)

An example of shape shell (Doppler free spectral shell) is shown in the right panel of Fig. 2.

### 2.2. Spectral data as cross-validation dataset

In the application of deep learning, the preparation of training data and test data is important for the success of solving any task. In the context of this work, the main challenge lies in the amount of data that can be used for different types of stars. In the 6-yr HARPS-N solar observations, there are $\sim$30 000 hourly binned spectral data. In order to minimize the effect of granulation and supergranulation, and other short-term effects, we daily binned the spectra (e.g. Dumusque et al. 2011). As a result, only $\sim$1800 daily binned spectra can be used to train and test different deep learning architectures. Speaking of stars other than the Sun, there are $\sim$400 daily binned spectra for HD 10700 (τ Ceti) and $\sim$300 daily binned spectra for HD 128621 (α CenB) in the HARPS archive dataset. The limitation of the available data for different stars is therefore the main obstacle. One possible solution would be to use simulated spectra as the training sets for different stellar types and apply the trained neural network to the observed spectra. Although the recently released SOAP-GPU is able to simulate stellar activity at spectral level for stellar type from F9 to K2 (Zhao & Dumusque 2023), stellar activity is a complex process and although most of the main physical processes are included in the code, the amplitude and covariance of those processes are based on either solar observations or numerical simulations. In addition, instrumental systematics and telluric contamination are not included in SOAP-GPU, and the presence of those in real observations likely makes it more difficult for a neural network to converge to what we want, modeling only the stellar activity component. Preliminary tests showed that the difference between SOAP-GPU simulated spectra and observed spectra is significant and although SOAP-GPU data were used at the start to develop and test different neural network architectures in an idealistic case, we quickly moved to real data as a trained neural network on the simulated data was not delivering good results when applied to real observations.

To augment the dataset based on real observations, we can use cross-validation as a resampling method. In general, cross-validation splits the data into training and test sets for different realization. For each realization, the training and test sets are used to train a machine learning model. The final result is the ensemble of the trained models for $k$ iterations. de Beurs et al. (2022) first used this method to handle the limited solar spectra of HARPS-N observation when training the neural network to model solar activity at CCF level. Here we also use this method to train neural network for different stars. Throughout this paper we use $k = 10$, which is the number of realization in which the input data are split into. In details, the spectral shells are randomly divided into 10 groups. For each iteration, one group is designated as the test set, while the remaining groups are used to train a model. The final results is the summary of the evaluations conducted on the test sets across all iterations. The
The weights in each filter is optimized by the back propagation neural network architecture, each convolutional layer contains (hereafter Conv layer), pooling layers and fully connected data rather than low S/N input data with more complexity. Considering that most of the stars have components: an input layer, hidden layers and an output layer. In this study, we need to tailor is the optimizer algorithms used during the training. The possible options are Adam (Kingma & Ba 2014), RMSprop and Stochastic Gradient Descent (SGD). The number of trials for a given star is set to 50. The search space of all the hyperparameters is summarized in Table 1.

Since shape shells are two-dimensional data, we use a convolutional neural network to achieve this regression task. The deep learning model is implemented using PyTorch (Paszke et al. 2017). Regarding the challenging task of hyperparameter tuning, which is generally done manually, it is unrealistic here, when considering several stars, to each time go through this manual process. We therefore implemented an automatic hyperparameter tuning algorithm to choose the best neural network architecture for different input stars. We describe the automatic neural network initialization in Sect. 3.1 and the deep learning algorithm to model stellar activity from shape shell in Sect. 3.2.

### 3.1. Neural network initialization for different stars

The deep neural network used in this study has three basic components: an input layer, hidden layers and an output layer. In this case, the input layer is the input shape shell with a dimension of $10 \times 10$. Although a higher resolution of the input shell includes more complex features, it also leads to a S/N decrease, mainly at the edges of the shell. Considering that most of the stars have only limited data, it is recommended to privilege high S/N input data rather than low S/N input data with more complexity.

Three blocks are used in the hidden layer: convolutional layers (hereafter Conv layer), pooling layers and fully connected layers (hereafter FC layer). As the key element in convolutional neural network architecture, each convolutional layer contains number of length-fixed nodes called filters. Each filter convolves the input shell with a set of weights (Krizhevsky et al. 2012). The weights in each filter is optimized by the back propagation algorithm using cost function (Rumelhart et al. 1986). The convolved image in each node is called a feature map. We denote the feature map from the $k$th node as $F^k$, whose filters are determined by the weights $W^k$ and bias $b^k$. The feature map can be obtained by:

$$F^k = (W^k \times S_{\text{shape}}, b^k).$$

### 3. Deep neural network model

We aim to build a neural network that can predict the RV induced by stellar activity from spectral shape shells in the $(f_0, S_{\text{shape}})$ space. If this works, and if our network is insensitive to planetary signals, then simply removing the predicted RVs from the raw RVs should enhance the significance of planet signals embedded into stellar signals. To prevent absorbing planetary signals, we first work with the shape shells, which are free from any Doppler component, as the input of our neural network. In addition, rather than predicting only the RVs, which are derived from the CCF technique and therefore contain tiny planet signals that the neural network could tend to model, we also predict simultaneously to the RVs, the FWHM and BIS derived from the CCF, similarly to what is done in multidimensional GP regression to prevent planetary signal overfitting (e.g. Rajpaul et al. 2015; Barragán et al. 2022; Delisle et al. 2022). For stars where planetary signals have already been detected, we remove the known planetary signals before feeding the spectral time series and the corresponding RV time series into the deep learning framework.

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Important features in the input shell is maximized by this process and will be passed to the next layer.

A pooling layer is used to reduce the spatial size of the feature maps from previous convolutional layers while important features in feature maps are preserved by calculating the average or max value when the filters of pooling layer convolve with feature maps. In this work, we use the adaptive average pooling layer after the convolutional blocks and before passing the flattened vectors into FC layers. The advantage of adaptive pooling is to have better spatial adaptability than the traditional average or max pooling which has a fixed window size (Stergiou & Poppe 2021).

Once the feature map after the pooling layer is flattened, it is connected to FC layers. Each element in the flattened feature map is connected to neurons in the FC layers, which perform a linear transformation by using a weight matrix. After each FC layer, we implement a dropout layer which will randomly drop out neurons with a specified ratio, as a measure to alleviate overfitting during the training process (Hinton et al. 2012).

Since we want to use the neural network to predict radial velocity corresponding to stellar activity from shape shell, the Mean Squared Error (MSE) function is used as the cost function. During the training process, we minimize the cost function:

$$C = \frac{1}{N} \sum_{i=1}^{N} \left( \text{RV}_{\text{pred}} - \text{RV}_{\text{CCF}} \right)^2,$$

where $N$ is the number of input shape shell during the training, $\text{RV}_{\text{CCF}}$ is the ground truth RVs measured from spectral CCF and $\text{RV}_{\text{pred}}$ is the predicted RV based on the input shape shell.

In order to find the best neural network architecture that is appropriate given the input data of a given star, we use the automatic hyperparameter optimization framework Optuna (Akiba et al. 2019) to search for the most appropriate hyperparameters of the neural network. Since the input shape shell only has a dimension of $10 \times 10$, a very deep neural network may lead to data overfitting. Therefore, the maximum numbers of both convolutional and FC layers are set to three. We set the maximum filter size of the first convolutional layer to five, in order to have a large receptive field, while the maximum filter size of the remaining layers is set to three. The last hyperparameter that we need to tailor is the optimizer algorithms used during the training. The possible options are Adam (Kingma & Ba 2014), RMSprop and Stochastic Gradient Descent (SGD). The number of trials for a given star is set to 50. The search space of all the hyperparameters is summarized in Table 1.

Since the idea of this work is to use the neural network to predict RVs corresponding to stellar activity from spectral shape shell, the main obstacle we have to handle during optimizing the neural network architecture is the presence of planetary signals in the RV time series. For most of the stars other than the Sun, we have no prior information about the presence of planetary signals. If we optimize the neural network architecture by minimizing the MSE equation (see Eq. (6)), the neural network is very likely to fit not only the RV component of stellar activity but also absorb the RV component of possible planetary signals.
### Table 1. Hyperparameters to be optimized by Optuna.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value: min, max</th>
<th>Step size</th>
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<tbody>
<tr>
<td>No. convolutional layers</td>
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<td>No. convolutional filter in each layer</td>
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<td>No. FC layer</td>
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</tr>
<tr>
<td>No. FC neurons in each layer</td>
<td>32, 512</td>
<td>32</td>
</tr>
<tr>
<td>Dropout ratio in each FC layer</td>
<td>0.2, 0.5</td>
<td>0.1</td>
</tr>
</tbody>
</table>

| Optimizer                | Adam, RMSprop, SGD |

In order to avoid this issue when finding the best neural network architecture, we use a measured activity index as the output of our neural network. This optimizes its architecture and loosely constrains the neural network to prevent it from fitting potential planetary signals in the RV spectral time series. Specifically, we use the calcium activity index \( \log(R'_{\text{HK}}) \) for optimization as this indicator is derived from the \( S \)-index, primarily containing information about solar plage (Cretignier et al. 2024) and does not contain any planetary information. Given that we want the trained CNN to predict the RVs, FWHM and BIS simultaneously, it is wise to use activity indicators other than FWHM or BIS to optimize the neural network hyperparameters. Relying on the optimization by FWHM and BIS for CNN hyperparameters could result in an overweighting of FWHM and BIS, potentially leading to an imbalance in the multi-task predictions, with reduced emphasis on RVs.

If the architecture is chosen without considering any planetary signal, it is likely to absorb less planetary signal when trained on RV data. Therefore, instead of considering Eq. (6) to optimize our neural network, we use as cost function:

\[
C_{\text{Optuna}} = \frac{1}{N} \sum_{i=1}^{N} \left[ \log(R'_{\text{HK, pred}}) - \log(R'_{\text{HK, obs}}) \right]^2. \tag{7}
\]

The basic architecture to be optimized by \textit{Optuna} is shown in Fig. 3.

\textit{Optuna} monitors Eq. (7) for each trial of hyperparameters and selects the optimal set with minimum \( C_{\text{Optuna}} \). Throughout optimization, we maintained a fixed training epoch of 300 steps per trial. To prevent overfitting during the optimization, the algorithm outputs the minimum \( C_{\text{Optuna}} \) value, rather than the \( C_{\text{Optuna}} \) value at the final epoch, for each trial. To ensure convergence within the fixed training epochs, we employed input shell data derived by injecting the YARARA stellar activity correction component back into the YARARA-cleaned spectra (for detailed spectrum processing descriptions, see Sect. 4). An example of the neural network, featuring the best hyperparameters derived from \textit{Optuna}, applied on the activity indicator time series is illustrated in Fig. 4.

#### 3.2. Neural network application in stellar activity mitigation

Once the hyperparameters of the neural network architecture has been optimized to the given data, we start training our neural network. To further prevent our neural network to fit potential planetary signals in the RV time series, we ask our neural network to predict simultaneously the RVs, FWHM and BIS time series. The ground truth of those values are derived from the CCFs which is obtained by using the specific line mask mentioned in Sect. 2.1. Since we have three outputs from the neural network, the cost function we want to minimize is:

\[
C_{\text{total}} = W_{\text{RV}}C_{\text{RV}} + W_{\text{FWHM}}C_{\text{FWHM}} + W_{\text{BIS}}C_{\text{BIS}}, \tag{8}
\]

where

\[
C_{\text{RV}} = \frac{1}{N} \sum_{i=1}^{N} \left[ \text{RV}_{\text{pred}} - \text{RV}_{\text{CCF}} \right]^2, \tag{9}
\]

\[
C_{\text{FWHM}} = \frac{1}{N} \sum_{i=1}^{N} \left[ \text{FWHM}_{\text{pred}} - \text{FWHM}_{\text{CCF}} \right]^2, \tag{10}
\]

\textit{Fig. 3.} Demonstration of a neural network architecture to be optimized by \textit{Optuna}. Shape shell with dimension of \( 10 \times 10 \) is feed into the neural network. The neural network consists of convolutional blocks, an adaptive layer and fully connected layers. In order to avoid overfitting planetary signals in RV time series, the calcium activity indicator \( \log(R'_{\text{HK}}) \) is used as output of the neural network to search for its best architecture.

\textit{Fig. 4.} Results of stellar activity modeling on the calcium activity index derived from the HARPS-N solar data with our trained neural network. \textit{Top:} the calcium activity index time series derived from HARPS-N solar spectra is labeled in red, while the predicted calcium activity index time series, obtained using the neural network optimized by \textit{Optuna}, is labeled in black. \textit{Bottom:} the residual time series of the calcium activity index.
and where \( W \) is the corresponding weight for the cost function of each output. Generally it is possible to derive the weight \( W \) for each output during training (Kendall et al. 2017). However, considering the limited data for each star, such an approach might not give good results. For simplicity, and to prevent planetary signal overfitting, we assign an equal weight of one for each output.

Following some tests, we found it was difficult for the neural network to predict three outputs by only changing the output layer from 1 to 3. We therefore modified the neural network so that each output is connected to its own FC block. The three FC blocks have the same hyperparameters derived from the Optuna optimization. The three individual FC blocks share the same feature maps derived from the convolutional blocks. The architecture of the used neural network to predict stellar activity is shown in Fig. 5.

The strategy outlined in Sects. 3.1 and 3.2 serves only as a streamlined approach to avoid of fitting potential planetary signals in the RV time series. Directly performing optimization and training the neural network using RVs, FWHM and BIS is rather challenging. Attempting optimization on the multi-task neural network by monitoring \( C_{\text{total}} \) from Eq. (8) may result in underfitting some outputs. For instance, although the optimal set may yield the minimum \( C_{\text{total}} \) with a fixed training epoch, its corresponding \( C_{\text{RV}}, C_{\text{FWHM}}, \) and \( C_{\text{BIS}} \) may not exhibit a monotonically decreasing trend. When applying the neural network to stars with little stellar activities, underfitting of RV time series often occurs due to the dominance of instrumental signals in the input spectral shell.

\[
C_{\text{BIS}} = \frac{1}{N} \sum_{i=1}^{N} [\text{BIS}_{\text{pred}} - \text{BIS}_{\text{CCF}}]^2, \tag{11}
\]

and where \( W \) is the corresponding weight for the cost function of each output. Generally it is possible to derive the weight \( W \) for each output during training (Kendall et al. 2017). However, considering the limited data for each star, such an approach might not give good results. For simplicity, and to prevent planetary signal overfitting, we assign an equal weight of one for each output.

Following some tests, we found it was difficult for the neural network to predict three outputs by only changing the output layer from 1 to 3. We therefore modified the neural network so that each output is connected to its own FC block. The three FC blocks have the same hyperparameters derived from the Optuna optimization. The three individual FC blocks share the same feature maps derived from the convolutional blocks. The architecture of the used neural network to predict stellar activity is shown in Fig. 5.

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4. Model performance and application

In order to test our deep learning framework for different regimes of stellar activity, we trained and tested our neural network on three stars: the Sun, HD 128621 (Alpha Centauri B) and HD 10700 (Tau ceti). These stars are intensively observed by HARPS-N or HARPS and have enough spectra to train our neural network. The Sun serves as the golden target to test the performance of a deep learning framework on solar-like stellar activity with a nearly perfect sampling. HD 128621 is more active and can be used to evaluate the performance of our framework when stellar activity is stronger. HD 10700 seems extremely quiet in RV, likely due to its pole-on configuration (Korolik et al. 2023), and therefore can test our framework when no or very little stellar activity is observed. Results on this star can also show the influence of instrumental and other sources of noise on the performance of the neural network. All the spectra of these stars are preprocessed by the YARARA data pipeline (Cretignier et al. 2021) to remove systemic errors such as induced by tellurics, detector stitching, ghosts and interference patterns. Another YARARA processing corrects for stellar activity seen at the spectral flux level and should mitigate the flux effect induced by active regions.

In the initial version of the pipeline, stellar activity was corrected on the residual spectra time-series by a linear decorrelation with the \( S \)-index. This is justified since the \( S \)-index is largely dominated by the contribution of plages at least on the Sun (Cretignier et al. 2024). This recipe was then slightly improved afterward. The stellar activity correction is now performed in the rest frame of the active regions at the stellar surface (Cretignier, in prep.) by following the recommendations of Thompson et al. (2017). A similar philosophy was also recently presented by Shahaf & Zuckay (2023) where the authors assumed that the spectra of active regions were “known,” while in our case we used the \( S \)-index as an empirical proxy for them.

Our deep learning framework is applied on the shape shells derived after all those YARARA corrections. We note that we will also investigate, in the subsections relative to each star, the effect of the different YARARA corrections on the performance of our neural network. For reader clarity, we adhere to the naming conventions for spectral products established in Cretignier et al. (2023). These include:

- YARARA products corrected of all spectral-level corrections, denoted as YV1.
- YV1 with reinjected activity, labeled as YVA.
- YARARA products not corrected but continuum normalized, referred to as YV0.

4.1. The Sun

We used the solar spectra observed by the HARPS-N solar telescope ranging from 2015 July 19th to 2024 January 8th (Dumusque et al. 2021, and in prep.). There are 2040 daily binned spectra in total. The hyperparameters of the neural network architecture are derived by optimizing training our neural network to predict the log(\( R'_{\text{HK}} \)) index of the Sun with Optuna. The best neural network architecture for the Sun is summarized in Table 2. We trained the neural network with those 2040 spectra by using Algorithm 1 for 100 training epochs. The predicted RV, FWHM, and BIS span time series from the trained neural network are illustrated in Fig. A.1.

In the RV space, we found that the neural network produces a good fit of the RV time series. In the periodogram, we also found that the neural network can well capture the activity signal at half the solar rotational, which was difficult to model when using principal component analysis decomposition of spectral shell (at least on HD 128621, see Cretignier et al. 2022). However, there is still some signal at the solar rotation that is not fully modeled. The root mean square (RMS) of the RV time series is reduced from 0.822 m s\(^{-1}\) to 0.663 m s\(^{-1}\). There are still some features in
Finally, we tested the performance of the deep learning framework on the solar spectra in the case with no YARARA correction. Before training our neural network, we injected all the YARARA correction components back into the solar spectra. The obtained dataset is therefore similar to the raw spectra extracted from the HARPS-N ESPRESSO pipeline with the exception that they have been normalized using RASSINE (Cretignier et al. 2020b). The results of our trained neural network can be seen in Fig. A.3. Compared with the two other cases presented above, we find that the RMS of the RV, and BIS residual increase only slightly and signals associated with stellar activity can still be well modelled by the neural network. This is not surprising since the major YARARA correction besides the correction of stellar activity that improves the RVs is the correction of telluric lines. Given that we only use strong stellar lines that are not blended and affected by strong systematics to build our shape shells but also to compute the CCFs that are used to derive the RV time series series, we do not expect strong contamination from telluric features. For the FWHM though, the RMS of the residuals is however much larger, mainly induced by strong signals at 1 yr and a half of it, due to the variation in the viewing angle of the Sun along the Earth orbit, but also a sudden jump in the FWHM time series around 59500 induced by the change of the HARPS-N cryostat.

In order to test our neural network performance at recovering planetary signals, we injected simulated planets into the solar spectra. For the sake of simplicity, all the simulated planets have a circular orbit with amplitudes evenly sampled from 0.1 to 0.5 m s⁻¹ with a step size of 0.033 m s⁻¹. The periods of the simulated planet signals are evenly sampled in logarithmic scale from 10 to 550 days, for a total of 180 planetary signals modeled. We inject each planetary signal into the solar spectral time series and train our neural network on that dataset. Since the log(RHK) of the Sun does not change for each planet injection, there is no need to optimize again the neural network architecture. We derive the RV residuals for each injection by subtracting the RVs predicted by the trained neural network from the RV time series which contains the planetary signal. We compute the periodogram of the RV residuals, with a corresponding numerically estimated >0.1% false alarm probability (FAP) level. A planet is detected if the power of its corresponding peaks is higher than the >0.1% FAP threshold, in which case we fit the observed signal with a sinus to recover the injected planet amplitude and phase. The results of this injection recovery test is illustrated in Fig. 6.

The trained neural network can reach a detection limit in planetary signal semi-amplitude as small as 0.18 m s⁻¹ for period ranging from 10 to 550 days. For periods not close to the half period of the solar rotation and the 1 yr observation window, the neural network can even reach a limit of 0.15 m s⁻¹. Some of the successful detection at 0.1 m s⁻¹ is very likely due to noise since their recovered amplitude and/or phase are significantly off from the injected values. The amplitude differences for most of the recovered planetary signals are less than 20% and the phase differences less than 0.04. We also test the effect of different YARARA corrections on the detection map. We also injected the simulated planet signals into the YVA solar spectra and the YVO solar spectra. The detection maps corresponding to those different datasets are shown in Figs. 7 and 8, respectively. We found that the detection maps derived from those two different spectral datasets are similar to the one derived from the YV1 solar spectra except that the detection limits around half the solar rotation period and 1 yr are higher than before. This is not surprising since we already found the YARARA

<table>
<thead>
<tr>
<th>Table 2.</th>
<th>Best neural network architecture for the Sun.</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Input layer</strong></td>
<td><strong>Adaptive average pooling(3,3)</strong></td>
</tr>
<tr>
<td>Conv1 (128, 3)</td>
<td>FC1 (352)</td>
</tr>
<tr>
<td>Conv2 (32, 1)</td>
<td>FC1 (352)</td>
</tr>
<tr>
<td>Conv3 (48, 1)</td>
<td>FC1 (352)</td>
</tr>
<tr>
<td>Dropout1 (0.2)</td>
<td>Dropout1 (0.2)</td>
</tr>
<tr>
<td>Dropout1 (0.2)</td>
<td>Dropout1 (0.2)</td>
</tr>
<tr>
<td>FC1 (416)</td>
<td>FC1 (416)</td>
</tr>
<tr>
<td>FWHM</td>
<td>FC1 (416)</td>
</tr>
<tr>
<td>RV</td>
<td>FC1 (416)</td>
</tr>
<tr>
<td>BIS</td>
<td>FC1 (416)</td>
</tr>
</tbody>
</table>

**Notes.** Adam algorithm is employed as the optimizer.
Fig. 6. Exoplanet detection limits from our neural network framework in the case of HARPS-N solar spectra. We derived the detection limit map by injecting simulated circular planetary signals covering periods ranging from 10 to 550 days and semi-amplitude ranging from 0.1 to 0.5 m s$^{-1}$ into the solar data. Left: detection limit map in the period-amplitude domain. The red dots indicate the successful detection by the trained neural network with FAP > 0.1%. Middle: amplitude comparison between the injected and recovered signals in the period-amplitude domain. The amplitude difference for most of the recovered signals are <20%. The large difference at low amplitude (0.1 m s$^{-1}$) is likely due to noise in the data. Right: phase comparison between the injected and recovered signals in the period-amplitude domain. The phase difference for most of the recovered planets is <0.04. The large differences at long periods is likely due to a poorer sampling of the phase for long-period planetary signals.

Fig. 7. Same as Fig. 6 but with the YVA solar spectra.

correction does not improve a lot on the results when we applied the neural network to the solar spectra at different YARARA correction stages. While achieving a detection limit of 0.18 m s$^{-1}$ for periods ranging from 10 to 550 days is indeed impressive, it represents an optimal scenario. This is because most stars do not have as frequent observations as the solar case. To further evaluate the performance of the deep learning framework regarding sampling effect. We selected segments of the HARPS-N spectral time series sampled at the observation timestamps of HD 10700, as illustrated in Fig. 9. We examined the detection thresholds of the neural network using the YV1 spectra with this sampling rate. The neural network demonstrates the capability to achieve a detection threshold of ~0.35 m s$^{-1}$ for planetary signals across periods spanning from 10 to 550 days, as illustrated in Fig. 10.

4.2. HD 128621

We used the HARPS spectra of HD 128621 collected between 2008 February 28th and 2015 May 21st, which corresponds to 288 daily binned spectra with S/N of ~600. The best neural network architecture of HD 128621 is summarized in Table 3. The given neural network is trained with the cross-validation algorithm mentioned in Algorithm 1 using the 288 spectral shape shell available. After 150 epochs of training, we derived the predicted RV, FHWM and BIS time series from the neural network outputs. The results are illustrated in Fig. A.4.

Table 3. Neural network architecture for HD 128621.

<table>
<thead>
<tr>
<th>Input layer</th>
<th>Conv1 (112, 1)</th>
<th>Conv2 (32, 3)</th>
<th>Conv3 (80, 1)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Adaptive average pooling(3,3)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>FCI (256)</td>
<td>FCI (256)</td>
<td>FCI (256)</td>
<td></td>
</tr>
<tr>
<td>Dropout1 (0.2)</td>
<td>Dropout1 (0.2)</td>
<td>Dropout1 (0.2)</td>
<td></td>
</tr>
<tr>
<td>FCI (480)</td>
<td>FCI (480)</td>
<td>FCI (480)</td>
<td></td>
</tr>
<tr>
<td>Dropout1 (0.2)</td>
<td>Dropout1 (0.2)</td>
<td>Dropout1 (0.2)</td>
<td></td>
</tr>
<tr>
<td>FCI (224)</td>
<td>FCI (224)</td>
<td>FCI (224)</td>
<td></td>
</tr>
</tbody>
</table>

FWHM | RV | BIS |

Notes. Adam algorithm is employed as the optimizer.

We found that the RV time series of CCFs is significantly reduced from 2.166 m s$^{-1}$ to 0.970 m s$^{-1}$. The stellar activity signal at the rotation period of the star is well modeled, as shown in the RV periodogram. We see no significant signals left at the periodogram of the RV residuals. In the FHWM space, the trained neural network also generated a good fit to the FHWM time series derived from CCFs. In the BIS domain, the stellar activity feature in the periodogram can be captured by the neural
network but there are still signals associated with stellar rotation left in the periodogram of the BIS residuals. For HD 128621, we performed the same test as we did for the Sun. We checked how the results of the neural network change with different YARARA corrections. We trained the neural network on the YVA spectra of HD 128621. The result is shown in Fig. A.5. Although the signals associated with stellar activity seem well modelled by the neural network in the periodogram of the RVs, FWHM and BIS, the RMS of the RV residual did increase a lot, from 0.970 m s$^{-1}$ to 1.582 m s$^{-1}$. Compared with the solar case, for which RV residual RMS only increases from 0.663 m s$^{-1}$ to 0.872 m s$^{-1}$, the trained neural network failed to model most of the components coming from the YARARA stellar activity correction. One possible explanation is that HD 128621, which is a K-type star, has less stellar activity due to the inhibition of the convective blueshift than the solar case and strong flux effect (Liebing et al. 2021, e.g.). In order to further validate that the flux effect is the dominant component in the stellar activity of HD 128621, we employed SOAP-GPU to evaluate the strength of different stellar activity components. We used the best-fit parameters of HD 128621 from Dumusque (2014). As shown in Fig. B.1, the flux effect of HD 128621 has an amplitude of 3.592 m s$^{-1}$, which is larger than the amplitude of the convective blueshift inhibition. Details of the SOAP-GPU simulation on HD 128621 can be found in Appendix B. Given that our neural network framework is designed to model the effect induced by the convective blueshift inhibition, it is less effective at mitigating the flux effect component of stellar activity compared to the YARARA correction. We further tested the performance of the deep learning framework on the flux effect and the inhibition of the convective blueshift using SOAP-GPU simulated spectra. These spectra were generated based on the intensity continuum and magnetogram images obtained from the Helioseismic and Magnetic Imager (HMI/SDO; Schou et al. 2012). For further details regarding the results, please refer to Appendix C.
Fig. 11. Exoplanet detection limits on HD 128621 HARPS spectra. We derived the detection limit maps by injecting simulated planetary signals covering periods ranging from 10 to 300 days and semi amplitude ranging from 0.4 to 1.1 m s\(^{-1}\), into the spectra. Left: detection limit map in the period-amplitude domain. The red dots indicate the successful detection by the trained neural network of a signal with a FAP >0.1%. Middle: amplitude comparison between the injected and recovered signals in the period-amplitude domain. The amplitude difference for most of the detected signals is <30%. Right: phase difference between the injected and recovered signals in the period-amplitude domain. The phase difference for most of the detected signals is <0.06.

Fig. 12. Same as Fig. 11 but with the YV A spectra of HD 128621. Given that the neural network does not perform well on the YV A spectra, the semi amplitude of simulated planet signals is from 0.7 to 2.0 m s\(^{-1}\).

We further test the neural network performance when an exoplanet signal is present in the spectral time series of HD 128621. As in the solar case, a set of simulated circular planetary signals are created with the amplitude evenly sampled from 0.4 m s\(^{-1}\) to 1.1 m s\(^{-1}\) and periods evenly sampled in logarithmic scale from 10 days to 300 days, for a total of 180 simulated planetary signals. We trained our neural network on the datasets with the planetary signals injected at the spectral level. The derived detection limit map is shown in Fig. 11. We find that the detection limit in RV semi-amplitude of the trained neural network is \(\sim 0.7\) m s\(^{-1}\) for planetary signals with period ranging from 10 to 300 days. For signals with periods far from the stellar rotation period and half of it, the neural network can even reach a limit of 0.5 m s\(^{-1}\). The low detection limits around the stellar rotation period and half of it is due to the presence of remaining stellar activity at the RV residual level. We also test the effect of the YARARA stellar activity correction on the detection map by training the neural network on the YV A spectra (see Fig. 12). We find that the detection limit largely increases from \(\sim 0.7\) m s\(^{-1}\) to \(\sim 1.7\) m s\(^{-1}\). This is likely due to the flux effect component of active regions which is not well modeled in the spectral shell representation.

4.3. HD 10700

We used the HARPS spectra of HD 10700 collected between 2005 August 1st to 2014 December 18th, which corresponds to 380 daily binned spectra with S/N of \(\sim 500\). The best neural network architecture for HD 10700 is summarized in Table 4. Given the fact that HD 10700 is a stellar quiet star and stellar activity may not be the dominant component, we trained the neural network on the 380 corresponding shape shells for 1000 training epochs. The predicted RV, FWHM and BIS time series from the neural network are shown in Fig. A.6.

Table 4. Neural network architecture for HD 10700.

<table>
<thead>
<tr>
<th>Input layer</th>
<th>Conv1 (96, 5)</th>
<th>Conv2 (48, 2)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>FC1 (224)</td>
<td>FC1 (224)</td>
</tr>
<tr>
<td></td>
<td>Dropout1 (0.3)</td>
<td>Dropout1 (0.3)</td>
</tr>
<tr>
<td></td>
<td>FC1 (192)</td>
<td>FC1 (192)</td>
</tr>
<tr>
<td></td>
<td>Dropout1 (0.3)</td>
<td>Dropout1 (0.3)</td>
</tr>
<tr>
<td></td>
<td>FC1 (128)</td>
<td>FC1 (128)</td>
</tr>
</tbody>
</table>

Notes. Adam algorithm is employed as the optimizer.
Table 5. Summary of neural network performance on different stars at different YARARA corrections.

<table>
<thead>
<tr>
<th></th>
<th>The Sun</th>
<th>HD 128621</th>
<th>HD 10700</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>RV</td>
<td>FWHM</td>
<td>BIS</td>
</tr>
<tr>
<td>YV1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>σraw (m s(^{-1}))</td>
<td>0.822</td>
<td>0.682</td>
<td>0.480</td>
</tr>
<tr>
<td>σresidual (m s(^{-1}))</td>
<td>0.663</td>
<td>0.553</td>
<td>0.314</td>
</tr>
<tr>
<td>YVA</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>σraw (m s(^{-1}))</td>
<td>2.206</td>
<td>3.592</td>
<td>1.028</td>
</tr>
<tr>
<td>σresidual (m s(^{-1}))</td>
<td>0.872</td>
<td>0.584</td>
<td>0.339</td>
</tr>
<tr>
<td>YV0</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>σraw (m s(^{-1}))</td>
<td>2.446</td>
<td>4.516</td>
<td>1.084</td>
</tr>
<tr>
<td>σresidual (m s(^{-1}))</td>
<td>0.898</td>
<td>0.908</td>
<td>0.363</td>
</tr>
</tbody>
</table>

Notes. σresidual is the residual after after extracting the neural network’s prediction from the original time series.

Fig. 13. Exoplanet detection limits on HD 10700 HARPS spectra. We derived the detection limit maps by injecting simulated planetary signals covering periods ranging from 10 to 350 days and semi amplitude ranging from 0.3 to 1.1 m s\(^{-1}\), into the spectra. Left: detection limit map in the period-amplitude domain. The red dots indicate the successful detection by the trained neural network of a signal with a FAP >0.1%. Middle: amplitude comparison between the injected and recovered signals in the period-amplitude domain. The amplitude difference for most of the detected signals is <20%. Right: phase difference between the injected and recovered signals in the period-amplitude domain. The phase difference for most of the detected signals is <0.04.

series either. A summary of the neural network performance on HD 10700, as well as on the Sun and HD 128621, is provided in Table 5. Given the fact that instrumental systematic uncertainty is the dominant factor in the spectra of HD 10700, it is difficult for the neural network to extract information of it at the level of the shape shells. We also tested the ability of our neural network to recover injected planetary signals in the spectra of HD 10700. We simulated a set of circular planetary signals with the amplitude evenly sampled from 0.3 m s\(^{-1}\) to 1.1 m s\(^{-1}\) and periods evenly sampled in logarithmic scale from 10 days to 350 days, for a total of 180 simulated planetary signals. These planetary signals are injected into the spectra which are further used for the neural network training. The detection map of the trained neural network on the spectra of HD 10700 can be found in Fig. 13. This analysis shows a detection threshold of ~0.5 m s\(^{-1}\) for planetary signals with periods ranging from 10 to 350 days. The detections at long periods are likely to be false positives as the recovered amplitudes and phases are significantly different from the injected values.

5. Conclusions

In this paper, we developed a neural network framework to efficiently mitigate stellar activity at the spectral level, to enhance the detection of low-mass planets on periods from a few days up to a few hundred days, corresponding to the habitable zone of solar-type stars. The framework is flexible and can be adapted to any solar-like star, by optimizing the neural network architecture in a data-driven way, by using the Optuna software and predicting the log($R''$HK) index of a given star, an index that is not affected by planetary signals. The neural network takes spectral shape shell as the input to predict the corresponding RV, FWHM, and BIS.

We tested this framework on three stars that have been intensively observed by HARPS and HARPS-N: the Sun, HD 128621 and HD 10700. In the solar case, the neural network is able to detect planet signals with semi amplitude as low as 0.2 m s\(^{-1}\) and periods ranging from 10 to 550 days. When applying the framework to the more active star HD 128621, the neural network can
reach a detection limit of 0.7 m s\(^{-1}\) for planet signals with periods from 10 to 300 days. In the case of the quiet star HD 10700, the neural network does not help much in decreasing the RMS of the RV residuals, however, we can still reach a very low detection limit of 0.5 m s\(^{-1}\) in planetary semi-amplitude, for planets with periods ranging from 10 to 350 days.

We further tested how the different stages of YARARA corrections affect our neural network performances. We find that the YARARA stellar activity correction is important when likely the flux component of stellar activity is more important, like it should be the case for later spectral-type stars where the velocity of convection diminishes, like for the K-dwarfs HD 128621. However, on a star like the Sun that is dominated by the stellar activity effect induced by the inhibition of the convective blueshift, for which shell have been designed to be sensitive for, our neural network framework seems to model efficiently stellar activity signals.

To improve further the performance of our neural network framework, we should consider adding as input some information about the flux effect induced by stellar activity. This could be done either by injecting at the convolution layer input a spectral representation, similar to the shell, but which is optimized to extract the flux effect, or injecting at the level of the fully connect layer, time series that are sensitive to the flux effect, like photometry. We could further enhance our deep learning framework’s performance by training an autoencoder to model shape shells for specific spectral types, rather than individual stars. Once the model is well-trained, we can use transfer learning to connect the pretrained encoder to new fully connected layers. This enables us to effectively train the neural network to model RV time series due to stellar activity.

The obtained results with our neural network approach for the Sun are quite impressive and to the best of our knowledge, it is possible that we could be sensitive to other Earths.

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References

Appendix A: Results of the deep learning framework on different stars

We summarize the results of the trained neural network on the Sun, HD 128621 and HD 10700. The predicted RV, FWHM and BIS time series of each case are derived by training the corresponding neural networks using the cross validation technique described in Algorithm 1. For each iteration in Algorithm 1, we randomly select 90% of the spectra as the training set and the rest 10% of the spectra as the test set. After the neural network is trained, the trained model is applied to remaining 10% of the spectra to get the predicted values. For the next iteration, 10% of the spectra, which are different from the last iteration, are selected as the test set and the remaining 90% are used for training. By repeating this process 10 times, all the spectra can be predicted by the same neural network architecture but with 10 sets of parameters.

Fig. A.1: Results of stellar activity modeling on the HARPS-N solar data with our trained neural network. The results of our neural network modeling on RVs, FWHM and BIS are shown in the left, middle and right columns, respectively. The first panels of each column shows the physical parameter derived from the specific solar cross-correlation mask and the one predicted by the neural network. Their corresponding periodograms are shown in the second panels of each column. The residuals of each physical parameter are shown in the third panels of each column. The last panels of each column shows the periodogram of the corresponding residuals. The FAP level of 0.1% is present in red dashed line.
Fig. A.2: Same as Fig A.1 but with the YVA solar spectra.

Fig. A.3: Same as Fig A.1 but with the YV0 solar spectra.
Fig. A.4: Same as Fig A.1 but for the HARPS data of HD128621.

Fig. A.5: Same as Fig A.4 but with the YVA spectra of HD128621.
Appendix B: Stellar activity contributions of HD128621

We employed SOAP-GPU to evaluate the importance of flux effect and the inhibition of convective blueshift in HD128621. We adopted the best-fit parameters of HD128621 from Dumusque (2014): A single faculae region with a size of 2.4% at latitude of 44 degrees, and the host star has a rotation period of 36.65 days with an inclination of 22 degrees. Using these parameters, we found that the amplitude of the flux effect is 3.592 m s\(^{-1}\) and the amplitude of the convective blueshift inhibition is 3.053 m s\(^{-1}\), which is smaller than the flux effect. The simulation further validates that the flux effect is the dominant component in the stellar activity of HD128621.

Appendix C: Results of the deep learning framework on different stellar activity effects

The two primary effects of stellar activity are the flux effect and the inhibition of the convective blueshift. We employed the deep learning framework on simulated spectra generated by SOAP-GPU to evaluate the neural network’s performance on each effect. These simulated spectra were derived from SDO/HMI images, which effectively model solar activity (Zhao et al. in prep). The neural network’s results for each effect are illustrated in Fig C.1 and Fig C.2, respectively. Our findings reveal that the RMS of the RV time series can be reduced by 62 % for the flux effect, and by 76 % for the inhibition of the convective blueshift. This suggests that the deep learning framework is particularly effective in correcting the inhibition of the convective blueshift in shell space.
Fig. C.1: Same as Fig A.1 but for the SOAP-GPU simulated spectra of the flux effect.

Fig. C.2: Same as Fig A.1 but for the SOAP-GPU simulated spectra of the inhibition of the convective blueshift effect.