

Observed abundance of X-ray low surface brightness clusters in optical, X-ray, and SZ selected samples

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ABSTRACT

The comparison of the properties of galaxy cluster samples selected using observations in different wavebands may shed light on potential biases of the way in which the samples are assembled. For this comparison, we introduce a new observable that does not require previous knowledge of the cluster mass: the X-ray mean surface brightness within the central 300 kpc. We found that clusters with low surface brightness, defined as those with a mean surface brightness below $43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$, are about one quarter of the whole cluster population in a sample of 32 clusters in the nearby Universe, selected independently of the intracluster medium properties. Almost no example of a low central surface brightness cluster exists instead in two X-ray selected samples, one sample based on *XMM-Newton* XXL-100 survey data and the other on full-depth eROSITA eFEDS data, although these clusters are known to exist in the range of redshift and mass as probed by these two surveys. Furthermore, the Sunayev–Zeldovich Atacama Cosmology Telescope cluster survey is even more selective than the previous two samples because it does not even include clusters with intermediate surface brightness, which are instead present in X-ray selected samples that explore the same volume of the Universe. Finally, a measure of the mean surface brightness, which is obtained without knowledge of the mass, proves to be effective in narrowing the number of clusters to be followed-up because it recognizes those with a low gas fraction or with a low X-ray luminosity for their mass. Identifying these would otherwise require knowledge of the mass for all clusters.

Key words. galaxies: clusters: general – galaxies: clusters: intracluster medium – X-rays: galaxies – X-rays: galaxies: clusters

1. Introduction

Our current knowledge of the properties of the intracluster medium of galaxy clusters comes primarily from detailed studies of clusters selected through the intracluster medium, either in emission (in X-ray) or via the effect the intracluster medium has on photons of the cosmic microwave background (Sunayev–Zeldovich effect; SZ hereafter, Sunyaev & Zeldovich 1972). It is now generally appreciated that clusters selected in X-ray surveys offer a biased view of the cluster population, although considerable effort has been made to take into account and correct for the inherent biases (Pacaud et al. 2007; Stanek et al. 2006; Andreon et al. 2011, 2016; Andreon & Moretti 2011; Eckert et al. 2011; Planck Collaboration IX 2011; Planck Collaboration I 2012; Maughan et al. 2012; Anderson et al. 2015). The bias occurs because at a given mass, brighter-than-average clusters are easier to select and be made part of a sample, while fainter-than-average clusters are easily missed. It is difficult to correct for the bias because the correction depends on assumptions about the unseen population, namely the clusters that are faint for their mass (Vikhlinin et al. 2009a; Andreon et al. 2011, 2016, 2017a). Andreon et al. (2022) showed that the covariance between detectability and location of a cluster in the mass-temperature diagram is strong, whereas the luminosity-temperature plane is largely unaffected by the missed population. This emphasizes that the missing population behaves differently in the various scaling relations. Using an X-ray unbiased sample (XUCS hereafter) selected from velocity dispersion measurements, we unveiled an even larger variety of clusters at a given mass (Andreon et al. 2016, 2017a, hereafter Paper I and

Paper II) that was lost in previous surveys because their surface brightness is low. Paper II showed these differences to be related to the gas fraction: Clusters with a low surface brightness also have a low gas fraction. Some of these low surface brightness clusters, with some new additions, are being rediscovered by other authors from independent data (Lietzen et al. 2024). Low surface objects of lower mass are also being discovered (O’Sullivan et al. 2017; Pearson et al. 2017; Xu et al. 2018, 2022; Capasso et al. 2020; Crossett et al. 2022).

Cluster samples selected using the SZ effect are said to offer a less biased view because the SZ signal in simulations is tightly correlated to the mass (e.g., Motl et al. 2005; Nagai 2006; Angulo et al. 2012). They show a larger variety in X-ray luminosity at a fixed mass than X-ray selected samples (e.g., Planck Collaboration IX 2011; Planck Collaboration I 2012), but as shown by recent analyses (e.g., Andreon et al. 2016, 2017a; Xu et al. 2018, 2022; Orłowski-Scherer et al. 2021) and in this work, even the SZ-selection fails to sample the full range. While much of the literature identified integrated pressure with mass, the existence of massive clusters that are undetectable in current SZ surveys, that is, which have a low brightness in their SZ signal, is slowly starting to be allowed in collective analyses of SZ samples (Orłowski-Scherer et al. 2021; Grandis et al. 2021).

We extensively studied one cluster with a low surface brightness, CL2015 (Andreon et al. 2019, hereafter Paper IV). Its core-excised X-ray luminosity is low for its mass M_{500} , 12σ below the mean relation derived from the X-ray selected sample of Pratt et al. (2009), but only 1σ below that derived for the X-ray unbiased sample. CL2015 differs from X-ray selected clusters in two aspects: First, the total mass profile has a very low

concentration. This feature is shared by weak-lensing selected clusters, which have lower concentrations than X-ray selected clusters on average (Miyazaki et al. 2018). Second, the gas pressure profile and integrated pressure (measured by the total Y_{SZ}) are greatly depressed (by a factor of three). Similar objects were recently reported at $z = 1.75$ (Andreon et al. 2021) and at $z = 1.80$ (Andreon et al. 2022), as well as several other less clear examples at $z \approx 1$ (Dicker et al. 2020; Di Mascolo et al. 2020). The existence of several clusters with depressed pressure profiles has profound cosmological and astrophysical consequences because an overestimate by 15% of the average pressure profile is enough to resolve the tension between cosmological parameters derived from CMB anisotropies and cluster abundances (Ruppin et al. 2019). We currently observe only one-third of the clusters expected from CMB cosmology (e.g., Planck Collaboration XX 2014); if a larger number of clusters with a low X-ray surface brightness exist, the tension could be attenuated or resolved.

The comparison of the properties of galaxy cluster samples selected using observations in different wavebands may shed light on potential biases of the way in which samples are assembled. Several works analyzed the overlap between cluster samples selected at different wavelengths. Donahue et al. (2002), Gilbank et al. (2004), Rykoff et al. (2008), Sadibekova et al. (2014), Willis et al. (2021), and Upsdell et al. (2023), among others, studied the overlap between optical and X-ray selected cluster samples. However, the X-ray data were shallow, and this led to poorly constrained results because objects were undetected, regardless of whether the two populations overlapped or were widely different (see Andreon & Moretti 2011 for a discussion). Sadibekova et al. (2014) and Upsdell et al. (2023) reported that the richest optically selected clusters are X-ray detected when they are in a redshift range in which the considered X-ray data are informative. Donahue et al. (2020) and Willis et al. (2021) instead emphasized that the X-ray selection misses some bona fide optically selected and X-ray bright clusters. Andreon & Moretti (2011) used deeper X-ray data for the considered clusters and concluded that the optical and X-ray selected populations largely overlap, although with a large (0.51 dex) scatter in X-ray luminosity at a fixed richness, which makes their X-ray detection hard and poorly predictable. Andreon et al. (2016) confirmed the above large variety using targeted X-ray observations of a velocity-dispersion-selected cluster sample, XUCS. In this work, we intend to proceed in a similar way to what was adopted for galaxies, that is, we create histograms of the number of objects per unit central surface brightness and learn selection effects from the observed differences in the histograms (e.g., McGaugh 1996; O’Neil et al. 2003). For this comparison, we introduce in Sect. 2 four samples that were selected differently, and a new observable, the X-ray mean surface brightness within the central 300 kpc. In Sect. 3 we compare the samples to understand how many clusters with a low surface brightness are present. In Sect. 4 we discuss whether low surface brightness clusters are absent in these samples because they are missed or because they do not exist in the redshift and mass ranges sampled by these surveys. Section 4 summarizes the results. Throughout this paper, we assume $\Omega_M = 0.3$, $\Omega_\Lambda = 0.7$, and $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$.

2. Samples

To explore the sensitivity of optical, X-ray, and SZ-selected samples to clusters with a low X-ray surface brightness, we considered four samples:

1. First of all, we considered the XUCS sample. It was selected from the Sloan digital spectroscopic survey and consists of 34 clusters in the very nearby Universe ($0.050 < z < 0.135$), characterized by more than 50 concordant galaxy redshifts within 1 Mpc, a velocity dispersion of the members $\sigma_v > 500 \text{ km s}^{-1}$ (see Paper I and Paper II), and low line-of-sight Galactic absorption. The probability of a cluster to be part of the sample is independent of its X-ray luminosity or any X-ray property. The X-ray properties were obtained later with targeted observations with the *Neil Gehrels Swift* Observatory, except for a handful of clusters that had adequate archival *XMM-Newton* or *Chandra* data. In the current paper we use the core radii derived in Paper I. Briefly, we fit a modified beta model with $\beta = 2/3$ to individual photons in the [0.5–2] keV band, accounting for excised regions, gaps, and variation in the exposure time and background. The modified beta model has a power-law-type cusp at the center to allow for a cool core. Weak priors were taken for all parameters. Two examples of fit of the radial profiles are shown in Fig. 4 in Paper I. The median core radius error is 12%. To offer a glimpse of the spread of the quality of the determinations, the error interquartile range is (7,15)%, the worst determination has an error of 31%. The values of the core radii of the three clusters measured from observations with different telescopes are consistent with each other (they differ by 2.5, 1.3, and 0.2σ). Using the same radial fitting model as adopted for computing X-ray luminosities, we measured the mean [0.5–2] keV X-ray surface brightness within an aperture radius of 300 kpc, μ_{300} . The aperture radius was chosen to be equal to other literature determinations (e.g., Giles et al. 2016; Liu et al. 2022). The median μ_{300} error is 0.03 dex, the error interquartile range is (0.01,0.04) dex, and the worst determination has an error of 0.09 dex. Table A.1 lists derived core radii and μ_{300} brightnesses. As in Andreon et al. (2022), we excluded two clusters from the further analysis: CL1022 because it is bimodal (two X-ray peaks), and CL2081 because it is too faint to derive a robust estimate of the temperature.
2. As a first X-ray selected sample, we considered the XXL-100 sample (Pierre et al. 2016), which is formed by the 100 brightest (in an aperture of 2 arcmin) clusters in the 50 deg^2 of the XXL survey (with ≥ 10 ks observations with *XMM-Newton*). The luminosities were taken from Giles et al. (2016), whereas the core radii come from the XXL database¹, where they are listed without errors. These core radii were used by the XXL collaboration, for example, in a XXL-100 detectability study (Pacaud et al. 2016), and the luminosities were used in several papers, including by Giles et al. (2016).
3. As a second X-ray selected sample, we considered the eROSITA² Final Equatorial Depth Survey (eFEDS: Brunner et al. 2022), which covers about 140 square degrees and has a sensitivity that exceeds what is expected from the final eROSITA full survey in the equatorial region. The authors of the eFEDS sample (Liu et al. 2022; Klein et al. 2022) quoted core radii and X-ray luminosities within 300 kpc. We only considered $F_{\text{cont}} < 0.2$ clusters to reduce false detections, as suggested by the authors, and a minimum of 200 counts to have reliable estimates of the brightness and core radius. This sample consists of 85 clusters.

¹ <http://cosmosdb.iasf-milano.inaf.it/XXL/>

² Extended ROentgen Survey with an Imaging Telescope Array.

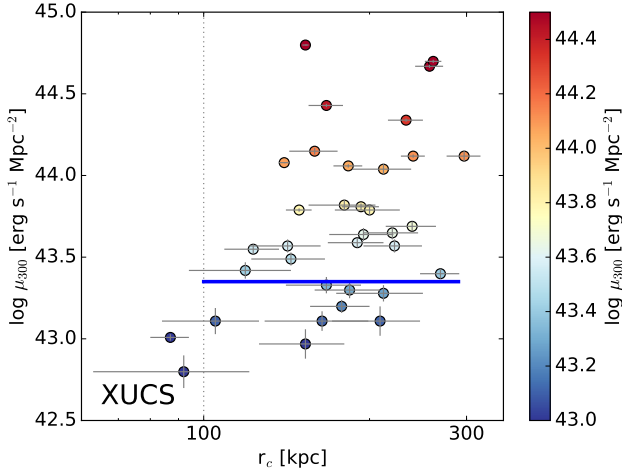


Fig. 1. Mean surface brightness vs. core radius. The mean surface brightness of about one quarter of the clusters with $r_c > 100$ kpc is below $43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ (blue line) in the $[0.5\text{--}2]$ keV band within a radius of 300 kpc. The vertical dotted line marks the minimum core radius considered for computing the fraction of low surface brightness clusters. Three clusters (observed by two telescopes) appear twice in the figure, but were counted only once in the accounting of the low surface brightness fraction. The individual values can be found in Table A.1. The points are color-coded by μ_{300} to facilitate the comparison with Fig. 7.

- To test the SZ selection, which has been claimed to be a better choice in the selection of cluster samples (e.g., Motl et al. 2005; Nagai 2006; Angulo et al. 2012; Planck Collaboration XX 2014), we considered the sample of clusters detected in the survey of the Atacama Cosmology Telescope (ACT; Hilton et al. 2021). We matched it to the above eFEDS sample, and only 3 out of 30 clusters did not match in the eFEDS footprint. These clusters are detected with an $S/N < 5$, which suggests that the probability of a false detection is 30% (Hilton et al. 2021). Moreover, they are not optically identified in the deep multiband Hyper Suprime-Cam Subaru survey (Aihara et al. 2022), nor in the Sloan digital sky survey (Ahumada et al. 2020). Our own visual inspection of the field confirms that there is no galaxy overdensity at the position of the SZ detection, again indicating false detections. Therefore, these three objects are likely false detections, and the sample is SZ-selected only.

The four samples are considered by the authors above not to be overly affected by cosmic variance. The three ICM-selected surveys were used to compute luminosities or mass functions based on these data. When limited to $z < 0.4$, the comoving volumes sampled by XUCS, ACT, XXL-100, and eFEDS are comparable (the XXL-100 volume is 50% smaller than that of XUCS, whereas the other surveys cover a volume larger by 50%). Therefore, comparable numbers of clusters (of any brightness) are expected in these surveys, unless strong selection or evolution effects are in place.

3. Numerical abundance of clusters with a low surface brightness in optical, X-ray, and SZ-selected samples

Figure 1 shows the observed distribution of the optically selected sample in the plane core radius versus mean surface brightness within a radius of 300 kpc. The paucity of $r_c \lesssim 150$ kpc at all

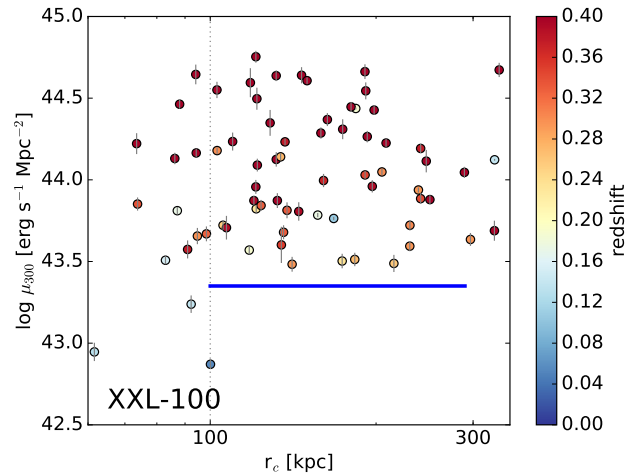


Fig. 2. Mean surface brightness within 300 kpc vs. core radius for the XXL-100 sample, color-coded by redshift (useful for a comparison with Fig. 3 and for the discussion). Only about 1% of the clusters has $r_c > 100$ kpc and a mean surface brightness below $43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ (blue line) vs. one quarter in the XUCS sample. The vertical dotted line marks the minimum core radius we considered to compute the fraction of clusters with a low surface brightness. Correcting luminosities for evolution would only alter the points in the top part of the figure, which is of no interest here.

brightnesses is a planned feature of the XUCS sample, which selects objects with a velocity dispersion larger than 500 km s^{-1} to focus on clusters. In the XUCS sample, about one-third of the sample have a surface brightness below $43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$, which is marked in the figure by a blue line. This percentage is robust to the precise choice of the minimum core radius for 150 kpc or 100 kpc, for example. We assumed 100 kpc from now on: above this radius, about one quarter of the clusters have a low surface brightness. Their core radius is large, typical of clusters, their richness (Puddu & Andreon 2022) is typical of clusters, but their core-excised luminosity, ($\log L_{500,ce} < 43 \text{ erg s}^{-1}$), is typical of cores.

Figure 2 shows the observed distribution of the XXL-100 sample in the $\mu_{300} - r_c$ plane, color-coded by redshift. One object at $\mu_{300} < 43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ among the 56 clusters has $100 < r_c < 300$ kpc (i.e., $\sim 2\%$)³. Even when we only count objects with $z < 0.4$ (and $100 < r_c < 300$ kpc as before), the percentage remains at about 3%. The only low surface brightness cluster in XXL-100 has the lowest redshift in the survey ($z = 0.054$, about twice the distance of the Coma cluster). This suggests that with the current analysis, the XXL-100 survey is sensitive enough to reliably detect clusters with a low surface brightness exclusively in the local Universe. Pacaud et al. (2007) demonstrated that if the clusters had a core radius twice larger than measured, they would largely not be detected in the XXL-100 survey. This agrees with our finding that almost no cluster is found. An observer willing to study a low X-ray surface brightness with $z > 0.054$ in detail would find no cluster in the XXL-100 sample (Fig. 2).

The percentage of clusters with a low surface brightness in XXL-100 (between 1% and 3%) is significantly lower than the percentage obtained in the XUCS sample, where about

³ There is one object of low surface brightness outside the range shown in the Figure, at $r_c > 350$ kpc, a region unprobed by XUCS. Visual inspection of the X-ray data suggest that it is a bimodal cluster. Even including it, the overall percentage would only be 3%.

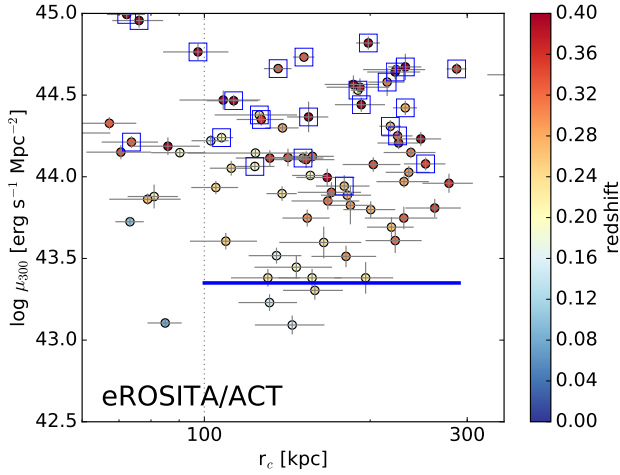


Fig. 3. Mean surface brightness within 300 kpc vs. core radius, color-coded by redshift (useful for the comparison with Fig. 2 and for the discussion) for clusters in eFEDS. Clusters that are also detected in the ACT survey are marked with a square. About 5% of the eFEDS clusters have a mean surface brightness below $43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ vs. about one quarter in the XUCS sample. The ACT survey only detects the clusters with a higher surface brightness. The vertical dotted line marks the minimum core radius we considered to compute the fraction of clusters with a low surface brightness. As for the XXL-100 sample, correcting luminosities for evolution would not significantly alter the results.

one quarter of the clusters has $r_c > 100 \text{ kpc}$ and $\mu_{300} < 43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$. At the opposite end, the XXL-100 sample has a higher percentage of bright and compact ($r_c \lesssim 150 \text{ kpc}$) clusters, which are easy to detect in X-ray selected samples and span a larger volume, as can be seen in the comparison between Figs. 2 and 1 at $\mu_{300} \sim 44.5 \text{ erg s}^{-1} \text{ Mpc}^{-2}$.

Figure 3 shows the observed distribution of the eFEDS sample in the μ_{300} - r_c plane, color-coded by redshift. Only three clusters lie below the blue line and have $100 < r_c < 300 \text{ kpc}$. This is 5% of the sample. The comparison with the 25% present in the XUCS sample indicates that eROSITA also poorly samples clusters with a low surface brightness. As in the case of the XXL-100 sample, eFEDS clusters with a low surface brightness are at low redshift (see the color-coding). The rarity of clusters with a low X-ray surface brightness agrees with the eFEDS detectability study (Liu et al. 2022) and with Bulbul et al. (2022).

In Fig. 3 ACT clusters are identified with a square. It is evident from the figure that ACT only detects the high surface brightness clusters and does not detect even clusters of intermediate brightness, $\mu_{300} \sim 43.5\text{--}44 \text{ erg s}^{-1} \text{ Mpc}^{-2}$, which are abundant in X-ray selected samples. We expect that the South Pole Telescope (SPT) cluster survey (Bleem et al. 2015) has the same limitation since SPT and ACT data share many similarities, such as telescope size and data reduction (Bleem et al. 2022).

So far, we have limited our analysis to the comparison of the fractions of objects below the arbitrary threshold value of $43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$. We now compare the whole observed surface brightness distributions of the samples (with $100 < r_c < 300 \text{ kpc}$ as before), although this requires that we assume a value for the surface brightness at which the distributions are normalized. We assumed $\mu_{300} = 44.5 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ because ACT includes only a few objects at fainter brightnesses, and XUCS poorly samples brighter brightnesses. Figure 4 shows the observed distribution in brightness for the four samples, both using top-hat 0.5 dex bins and a running average with a Gaussian with $\sigma = 0.2 \text{ dex}$. The ACT (SZ) sample is shallow-

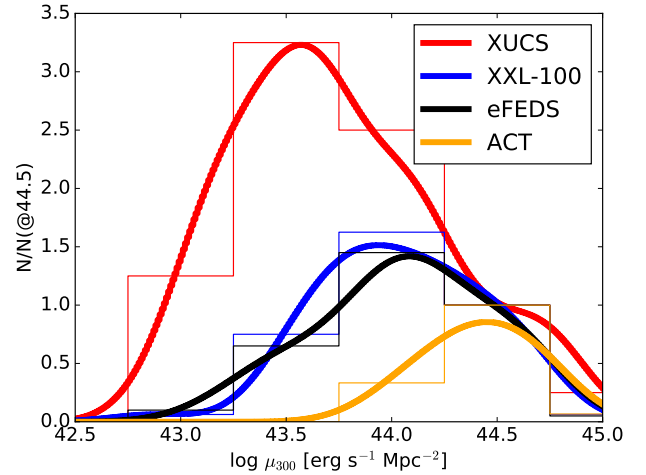


Fig. 4. Observed brightness distribution of the various samples normalized at the $\mu_{300} = 44.5 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ bin. The histogram uses top-hat bins, and the curves are running averages using a Gaussian with $\sigma = 0.2 \text{ dex}$. ACT lacks clusters with a normal brightness ($\mu_{300} \approx 44.0 \text{ erg s}^{-1} \text{ Mpc}^{-2}$), whereas X-ray selected samples lack most clusters with $\mu_{300} \lesssim 43.7 \text{ erg s}^{-1} \text{ Mpc}^{-2}$.

est: its brightness distribution only shows rare examples of clusters with an intermediate brightness of $\mu_{300} \approx 44.0 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ and has no examples with $\mu_{300} \approx 43.5 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ or fainter. The two X-ray selected sets sample a wider range than the SZ-selected sample, but they only include a few examples of clusters with $\mu_{300} \sim 43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$, which are much more abundant in XUCS. As mentioned, the normalization is arbitrary and can therefore be changed. However, a normalization change does not displace the location of the peaks of the three distributions horizontally, with XUCS and ACT remaining at the two extremes. To summarize, the XUCS sample alone of those considered here provides examples of low surface brightness that are useful for follow-up studies: About one quarter of the sample belongs to this group, as opposed to only a few percent (or none) in the comparison samples.

It might be wondered whether the differences observed in the samples are simply due to differences in the size of sampled volumes. As mentioned, XXL-100, eFEDS, and ACT, when bounded to $z < 0.4$, sample a comparable comoving volume and should therefore contain a similar number of clusters with $\mu_{300} \sim 43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ as XUCS. This is clearly not the case (compare the numbers of points below the blue line in Figs. 1–3), which implies that strong selection effects are at play, given that evolution effects are minor, as discussed in Sect. 4.1. Selection and evolution effects also cause the well-known overabundance of high surface brightness clusters, which are visible over even larger volumes in ICM-selected samples.

The rarity of clusters with a low surface brightness in X-ray and SZ samples, based on just photometric data (radius and brightness), is derived on purpose without knowledge of the cluster mass or temperature for greater applicability. Visual inspection of the few objects with a mean surface brightness below $43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ in the two X-ray selected samples shows that some of them may be groups in which the core radius is temporally inflated by interactions with a companion (e.g., O’Sullivan et al. 2018), and are not more massive objects in a nearly steady state as seen in XUCS. A comparison at fixed mass and using a mass-informed aperture, such as r_{500} , would be

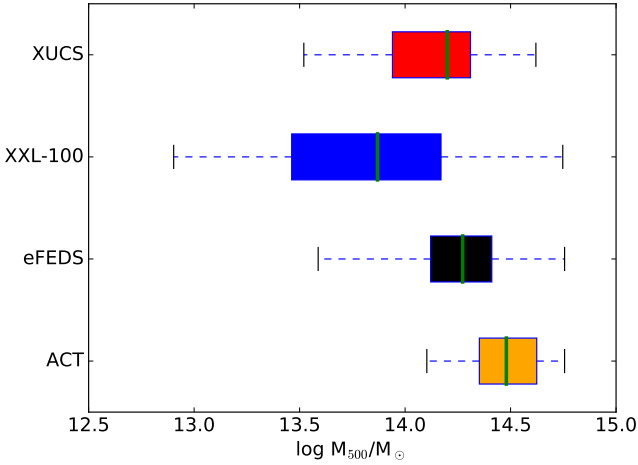


Fig. 5. Mass ranges explored by the different cluster samples as a whisker plot. The boxes extend from the lower to the upper quartiles, with a line at the median. The whiskers show the full range. Mass ranges largely overlap across the samples.

preferable, but this would preclude the applicability of our work to common cluster samples, which usually lack a mass estimate.

4. Discussion

In this section, we present our considerations about the results we illustrated above. We note however that they are not exhaustive nor they represent the final word on the subject.

4.1. Whether clusters of low surface brightness are rare because they are missed, or because they do not exist in the sampled ranges of mass and redshift

As illustrated above, clusters with a low surface brightness are present in the optically selected sample, but are extremely rare in the ICM-selected samples we considered. The question now is whether this arises because we sample a disjoint mass or redshift ranges. This is probably not the explanation, as detailed below: the mass and redshift ranges overlap or are very close to each other.

Figure 5 shows the mass ranges of the different samples as a whisker plot. Only clusters with $100 < r_c < 300$ kpc and available masses are considered. The XUCS sample has caustic masses (Diaferio & Geller 1997 and later works) with $\log M/M_\odot$ values in the range 13.5–14.6 (ends of whiskers), and the first, second, and third quartiles (extremes of the box and line inside it) are $\log M/M_\odot = 13.90, 14.15,$ and 14.30 (see Papers I–IV for details). Andreon et al. (2017b) found that the caustic masses used in XUCS are consistent with hydrostatic masses. The eFEDS sample includes clusters with mass quartiles similar to those of XUCS (individual mass values are taken from Chiu et al. 2022, which are based on count rates that were converted in mass using weak lensing observations). XXL-100 samples the same mass ranges as XUCS and eFEDS and also includes clusters that are less massive than these samples because it includes clusters with an estimated weak-lensing mass as low as $\log M/M_\odot = 12.7$ (Umetsu et al. 2020). The ACT sample is expected to have typical masses higher than $\log M_{500}/M_\odot = 14.5$ (Hilton et al. 2021). Their mass range overlaps that of the other samples based on six out of eight clusters with weak-lensing masses in Miyatake et al. (2019). According to

the values tabulated in Chiu et al. (2022) and shown in Fig. 5, most of the sample is in the top three quartiles for XUCS and eFEDS.

With XUCS, we have shown that the Universe at $0.050 < z < 0.135$, which is included in the redshift range probed by both XXL-100 and eFEDS, contains clusters with a low surface brightness whose masses are sampled by both XXL-100 and eFEDS (see also other detections by Lietzen et al. 2024; O’Sullivan et al. 2017; Pearson et al. 2017; Xu et al. 2018). Therefore, clusters with a low surface brightness are known to exist in the same range of redshift and mass as is probed by these two surveys, but they are rare at best in these catalogs. XXL-100 reaches lower masses than XUCS (Fig. 5).

Since the redshift ranges of the above samples overlap, it is unlikely that evolution plays a large role in explaining the different faint ends of the brightness distribution. Furthermore, according to the determinations of Giles et al. (2016) and Chiu et al. (2022) for the XXL-100 and eFEDS samples, the evolution is minimum at low redshift, so that we expect that they are present in the whole wider redshift range probed by these surveys. To match the peaks of X-ray selected and XUCS samples, a 0.5 dex evolution is needed on average (Fig. 4) in the 0.5 Gyr just before $z = 0.08$, which is huge and unlikely to have been so badly mistaken by these authors. Finally, the faint end of the brightness distribution of these two surveys cannot change because in their samples the objects with a lower surface brightness are at low redshift and therefore have negligible evolutionary corrections. Therefore, low surface brightness clusters exist in the redshift and mass ranges explored by these X-ray surveys, and their rarity is intrinsic in these catalogs.

The case for the ACT survey is less clear. The survey is mostly sensitive to clusters with expected masses $\log M_{500} > 14.5$, according to Hilton et al. (2021). However, according to Miyatake et al. (2019) and Chiu et al. (2022), the ACT mass range largely overlaps the range explored by the other samples (Fig. 5). The ACT clusters considered in this work have $z > 0.19$, which is outside the range probed by XUCS. The difference in redshift probed is not enough to invoke evolution to explain the difference unless (a) an extreme evolution is assumed, and (b) both Giles et al. (2016) and Chiu et al. (2022) are in error. Therefore, we currently cannot firmly conclude that ACT does not contain examples of clusters with a low surface brightness because they do not exist at the mass/ z of the survey. However, at intermediate brightness (e.g., $43.5\text{--}44.3 \text{ erg s}^{-1} \text{ Mpc}^{-2}$), eFEDS contains clusters at $z \sim 0.3$ with large r_c , but only some of them are detected by ACT (the orange-red points in the center right panel of Fig. 3). This indicates that intermediate-brightness clusters in the region of the Universe that is covered by ACT exist, but they are not detected. Further support for the existence of massive clusters that are undetected by ACT comes from a) the Orłowski-Scherer et al. (2021) analysis, which required half of the richest clusters to be missed by ACT; b) the very rich but SZ-faint clusters in Dicker et al. (2020) and in Di Mascolo et al. (2020); and c) the low SZ strength signal for its mass of JKCS 041, a $z = 1.803$ cluster (Andreon et al. 2023). The redshift of all these clusters is much higher than probed in this work, but they indicate that massive clusters with a low SZ signal also exist outside of the very local Universe.

To summarize, the two X-ray surveys do not include existing low surface brightness clusters, and the ACT survey does not include existing intermediate surface brightness clusters. This suggests that the paucity of low to intermediate surface brightness clusters in the X-ray and SZ catalogs is not due to the fact that these clusters do not exist in the mass/ z range explored by

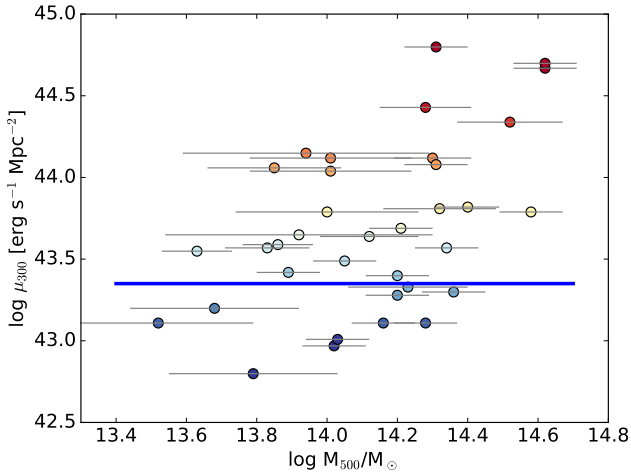


Fig. 6. Mean surface brightness μ_{300} in the [0.5–2] keV band vs. M_{500} for the XUCS sample. Clusters with a low surface brightness are spread over three out of the four mass quartiles. The large scatter between these two quantities strongly reduces the impact of the differences in mass on the brightness distribution. We plot the measurements of μ_{300} from two different telescopes for three clusters.

these catalogs, but that they have been missed at the current sensitivity of the surveys.

The authors of X-ray and SZ surveys are aware that clusters with a low brightness are difficult to detect in X-ray surveys (Vikhlinin et al. 1998, 2009b; Moretti et al. 2004; Pacaud et al. 2007, 2016, see Andreon et al. 2019 and Andreon et al. 2022 for a detailed listing). Figures 2 and 3 in Andreon et al. (2022) showed that it is challenging to account for low surface brightness clusters for the L_X – M and T – M scaling relations because a smaller scatter around the mean relation is derived, even when the X-ray selection is said to be accounted for, compared to the mean relation observed in samples that include the low surface brightness population. As detailed in Andreon et al. (2019) and as was at least known since Vikhlinin et al. (2009b), the determination of the scaling relation parameters is conditional on assumptions on the unseen population, namely being able to estimate how many low surface brightness clusters are missed, and how these objects populate the plane of the scaling relation in question. These determinations are extremely hard to make when the collected sample of low surface brightness objects is a few clusters or none. Our work shows that low surface brightness clusters exist. Their impact on the scaling relations may range from negligible (for the L_X – T scaling relation; Andreon et al. 2022) to major (for the T – M and L_X – M relations; Andreon et al. 2016, 2022) and depends on survey characteristics.

4.2. Whether the comparison between samples is influenced by a tight brightness–mass correlation and by large mass biases

If very hypothetically the masses of XUCS clusters were strongly overestimated and if there were a tight and steep brightness–mass relation, then the XUCS brightness distribution would include clusters with a low brightness that would be rightfully absent in the X-ray selected samples. We now show that neither of these two hypotheses, which are both needed to bias our results, is true. The XUCS masses are not systematically overestimated (Papers I, III, and IV), and a huge mass overes-

timate is needed to make them less massive than eFEDS and XXL-100 clusters with which we compare them. For example, the most massive low surface brightness cluster, CL2015, has a caustic mass of $\log M_{500} = 14.39 \pm 0.09$ (Paper I) and a hydrostatic mass of $\log M_{500} = 14.23 \pm 0.22$ (Paper IV). A mass bias of 0.6 dex by both the caustic and hydrostatic method, which is unheard of before, is needed to bring the CL2015 mass below the range sampled by XXL-100. Second, the relation between brightness and mass is neither tight nor steep: Fig. 6 shows the distribution of the XUCS sample in the mean surface brightness μ_{300} versus mass M_{500} plane, with mass errors including those induced by triaxiality and projection effects. Because of the large scatter, a hypothetical over- or underestimate of the mass has a negligible effect on the XUCS brightness distribution (the effect would be exactly zero in absence of a relation) and on the results of our comparison of the samples.

4.3. Robustness analysis

Although the details of the radial profile fit are not the same, the core radii in XUCS, XXL-100, and eFEDS are all derived from a fit to the X-ray photons with a circular beta model (possibly with a cusp in the case of XUCS) with the same fixed beta parameter and allowing for a background. We only used the core radii to remove very compact objects with sizes typical of groups (smaller than 100 kpc) from the sample. Moreover, the fraction of low surface brightness clusters does not depend strongly on the core radius (see Figs. 1–3), and therefore, we do not expect that the slightly different methods for deriving the core radius have any significant effect on the final results.

As in Andreon et al. (2022), 2 out of 34 clusters were excluded from the XUCS sample. Returning them (at whatever surface brightness) in XUCS would not cause low surface brightness clusters to appear in other samples, such as eFEDS, XXL-100, or ACT samples. Independently of whether these two clusters have a low or high surface brightness, the fraction of low surface brightness clusters of XUCS continues to be about one quarter, and our conclusions about the rarity of clusters of low surface brightness in X-ray and SZ-selected samples are not altered. Regardless of the surface brightness of the two missing XUCS clusters, the ACT sample lacks intermediate-brightness clusters compared to the X-ray selected samples.

4.4. A first look at the ICM properties of clusters that are rare in ICM-selected samples

Figure 7 shows the XUCS L_X – M and f_{gas} – M relations that were presented in previous papers, but with the points color-coded by surface brightness. Clusters with $\mu_{300} < 43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$, which we have shown to be rare in ICM-selected samples, are indicated by squares in the figure. Clusters with a low X-ray luminosity for their mass and with a low gas fraction lie well below the mean line (near or below the lower dashed line). All of them have a low surface brightness. However, the low surface brightness clusters (i.e., squares) include clusters near the solid line that are faint because they have a low mass and a common gas fraction. To identify clusters with a low luminosity for their mass (and with low gas fraction) among those with a low surface brightness, a mass determination is needed. Because of the large scatter in the M – T relation (Andreon et al. 2022), the mass cannot be inferred from T following the common practice of estimating r_{500} from T . Similarly, f_{gas} , M_{gas} , or Y_X cannot be used for this purpose (see Andreon et al. 2022 for details). To obtain

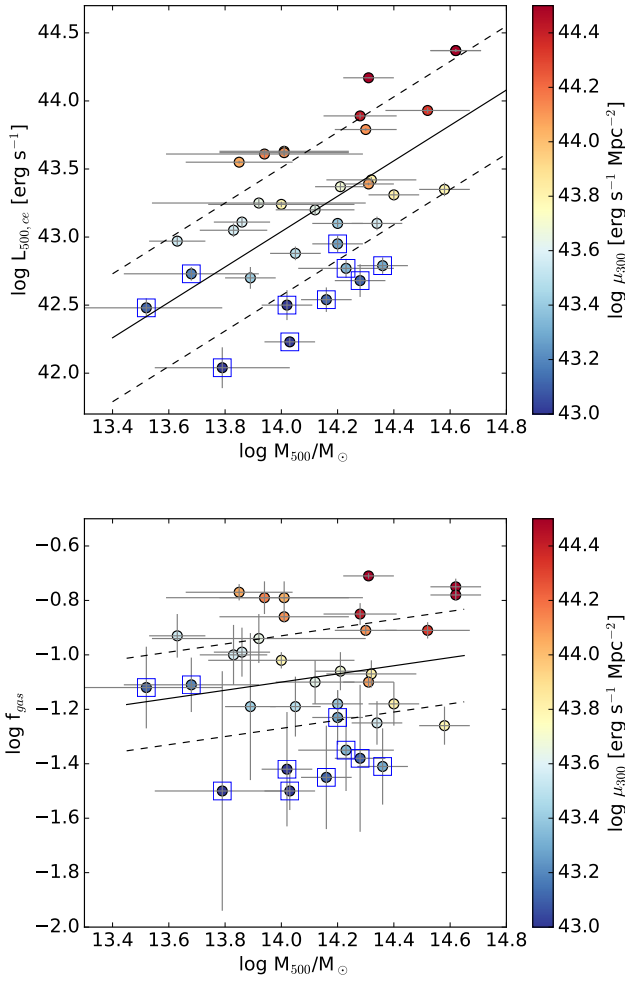


Fig. 7. Core-excised [0.5–2] keV luminosity (upper panel) and gas fraction (bottom panel) within r_{500} vs. M_{500} color-coded by brightness within 300 kpc for the XUCS sample. The solid black line and the dashed corridor indicate the mean relation and the $\pm 1\sigma_{\text{intr}}$ regions derived in Papers I and II. Low surface brightness clusters (with $\mu_{300} < 43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$) are indicated by squares and are mostly clusters that are X-ray faint for their mass and have a low gas fraction (near or below the lower dashed line) with some contamination by objects with an average gas fraction that are faint because the mass is low (near the solid line). We plot the measurements from two different telescopes for three telescopes, although it can be challenging to identify these duplicates in the plot.

a reliable estimate of the total mass, we would need a measure that samples the regions that contain most of the mass, such as a hydrostatic estimate with a precisely measured temperature gradient near r_{500} , or weak-lensing or caustic masses, which all are costly observationally. A preselection on μ_{300} would therefore significantly reduce the number of targets to be followed-up for mass determination.

5. Conclusions

The comparison of the properties of galaxy cluster samples selected using observations in different wavebands may shed light on potential biases of the way in which the samples are assembled. For this comparison, we introduced a new observable that does not require previous knowledge of the cluster mass: The X-ray mean surface brightness within the central 300 kpc.

We found that clusters with a low surface brightness, defined as those with a mean surface brightness below $43.35 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ within 300 kpc in the [0.5–2] keV band, are about one quarter of the whole cluster population in a sample of 32 clusters in the nearby Universe selected independently of the intracluster medium properties. On the other hand, almost no example of a low central surface brightness cluster exists in two X-ray selected samples, one based on *XMM-Newton* XXL-100 survey data and one using full-depth eROSITA eFEDS data, even though they are known to exist in the same range of redshift and mass as probed by these two surveys.

Furthermore, the Sunayev–Zeldovich Atacama Cosmology Telescope cluster survey is even more selective than the previous two samples because it does not even include clusters with an intermediate surface brightness, which are instead present in X-ray selected samples that explore the same volume of the Universe.

Finally, a measure of the mean surface brightness, which is obtained without knowledge of the mass, proves to be effective in narrowing the number of clusters to be followed-up to recognize those with a low gas fraction or with a low X-ray luminosity for their mass, whose identification would otherwise require knowledge of the mass for all clusters.

Since the introduced observable does not require previous knowledge of the cluster mass, it is possible and useful to repeat the work performed here using other cluster samples and to extend it considering a sample with tighter redshift overlaps, for example.

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Appendix A: List of core radii and brightnesses

Table A.1. Results of the analysis.

Id	RA (J2000)	Dec	z	r_c kpc	err	$\log \mu_{300}$ erg s ⁻¹ Mpc ⁻²	err dex
CL1001	208.2560	5.1340	0.079	240	12	44.12	0.01
CL1009	198.0567	-0.9744	0.085	149	8	43.79	0.01
CL1011	227.1073	-0.2663	0.091	167	26	43.33	0.04
CL1014	175.2992	5.7350	0.098	180	25	43.82	0.02
CL1015	182.5701	5.3860	0.077	183	11	44.06	0.01
CL1018	214.3980	2.0530	0.054	178	22	43.20	0.04
CL1020	176.0284	5.7980	0.103	159	16	44.15	0.02
CL1030	206.1648	2.8600	0.078	164	35	43.11	0.05
CL1033	167.7473	1.1280	0.097	142	21	43.57	0.04
CL1038	179.3788	5.0980	0.076	239	25	43.69	0.03
CL1039	228.8088	4.3860	0.098	193	15	43.81	0.01
CL1041	194.6729	-1.7610	0.084	153	2	44.80	0.01
CL1047	229.1838	-0.9693	0.118	212	26	44.04	0.03
				297	21	44.12	0.01
CL1052	195.7191	-2.5160	0.083	140	3	44.08	0.01
CL1067	212.0220	5.4180	0.088	220	25	43.65	0.03
CL1073	170.7265	1.1140	0.074	269	22	43.40	0.02
				212	38	43.28	0.04
CL1120	188.6107	4.0560	0.085	153	27	42.97	0.08
CL1132	195.1427	-2.1340	0.085	92	29	42.80	0.09
CL1209	149.1609	-0.3580	0.087	87	7	43.01	0.02
CL2007	46.5723	-0.1400	0.109	209	38	43.11	0.09
CL2010	29.0706	1.0510	0.080	222	27	43.57	0.03
CL2015	13.9663	-9.9860	0.055	184	25	43.30	0.03
CL2045	22.8872	0.5560	0.079	190	22	43.59	0.03
CL3000	163.4024	54.8700	0.072	200	27	43.79	0.02
CL3009	136.9768	52.7900	0.099	119	25	43.42	0.05
CL3013	173.3113	66.3800	0.115	167	12	44.43	0.01
CL3020	232.3110	52.8600	0.073	195	26	43.64	0.03
CL3023	122.5355	35.2800	0.084	144	22	43.49	0.04
CL3030	126.3710	47.1300	0.127	233	17	44.34	0.01
CL3046	164.5986	56.7900	0.135	257	15	44.67	0.01
				261	9	44.70	0.01
CL3049	203.2638	60.1200	0.072	123	14	43.55	0.02
CL3053	160.2543	58.2900	0.073	105	21	43.11	0.09

Three clusters were observed by two telescopes and therefore are listed twice. Id, RA, Dec, and z are from Paper I.