The TNG50-SKIRT Atlas: Wavelength dependence of the effective radius

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ABSTRACT

Galaxy sizes correlate with many other important properties of galaxies, and the cosmic evolution of galaxy sizes is an important observational diagnostic for constraining galaxy evolution models. The effective radius is probably the most widely used indicator of galaxy size. We used the TNG50-SKIRT Atlas to investigate the wavelength dependence of the effective radius of galaxies at optical and near-infrared (NIR) wavelengths. We find that, on average, the effective radius in every band exceeds the stellar mass effective radius, and that this excess systematically decreases with increasing wavelength. The optical g-band (NIR K-band) effective radius is on average 58% (13%) larger than the stellar mass effective radius. Effective radii measured from dust-obscured images are systematically larger than those measured from dust-free images, although the effect is limited (8.7% in the g-band, 2.1% in the K-band). We find that stellar population gradients are the dominant factor (about 80%) in driving the wavelength dependence of the effective radius, and that differential dust attenuation is a secondary factor (20%). Comparing our results to recent observational data, we find offsets in the absolute values of the median effective radii, up to 50% for the population of blue galaxies. We find better agreement in the slope of the wavelength dependence of the effective radius, with red galaxies having a slightly steeper slope than green–blue galaxies. Comparing our effective radii with those of galaxies from the Siena Galaxy Atlas in separate bins in z-band absolute magnitude and g − z colour, we find excellent agreement for the reddest galaxies, but again significant offsets for the blue populations: up to 70% for galaxies around Mz = −21.5. This difference in median effective radius for the bluer galaxies is most probably due to intrinsic differences in the morphological structure of observed and TNG50 simulated galaxies. Finally, we find that the median effective radius in any broadband filter increases systematically with decreasing u − r colour and with increasing galaxy stellar mass, total SFR, sSFR, and dust-to-stellar-mass ratio. For the slope of the wavelength dependence of R_e, however, there does not seem to be a systematic, monotonic correlation with any of these global properties.

Key words. dust, extinction – galaxies: fundamental parameters – galaxies: stellar content – galaxies: structure

1. Introduction

Of all the morphological characteristics of a galaxy, size is arguably the most important one. Galaxy sizes correlate with many other important properties of galaxies, such as stellar mass, surface brightness, and stellar density (Kormendy 1977; Roberts & Haynes 1994; Shen et al. 2003; van der Wel et al. 2014). The cosmic evolution of galaxy sizes is an important observational diagnostic for constraining galaxy evolution models (Trujillo et al. 2006, 2007; van der Wel et al. 2008, 2014; Roy et al. 2018; Costantin et al. 2023). Galaxy sizes are also important to define central dark matter fractions, and can be used together with these dark matter fractions to test galaxy evolution models (e.g. Tortora et al. 2018).

There are different ways to characterise the size of a galaxy (Petrosian 1976; Kron 1980; Graham 2019; Trujillo et al. 2020). The effective or half-light radius is probably the most widely used one. One of the main advantages of the effective radius as an indicator of galaxy size is its robustness against many observational issues, such as the depth of images (e.g. Trujillo et al. 2001). On the other hand, the effective radius is an on-sky property and not an intrinsic 3D property of a galaxy, and its value is expected to depend on the orientation and the band in which we observe the galaxy (Möllerhoff et al. 2006; Graham & Werley 2008; Pastrav et al. 2013; Devour & Bell 2017).

Several teams demonstrated observationally that the effective radius is indeed wavelength-dependent. Ko & Im (2005)
and La Barbera et al. (2010) found a 30% decrease in the effective radius of early-type galaxies when moving from the optical $g$- or $V$-bands to the near-infrared (NIR) $K$-band. Kelvin et al. (2012) and Vulcani et al. (2014) extended these studies by including late-type galaxies, and found an overall ~30% decrease in effective radius when moving from $g$- to $K$-band values, with the decrease slightly depending on galaxy colour or Sérsic index. Other studies indicating a similar dependence of effective radius on wavelength include Lange et al. (2015), Kennedy et al. (2015, 2016), Casasola et al. (2017), Dimauro et al. (2018), Psychogios et al. (2020), Baes et al. (2020), and Nersesian et al. (2023). Advanced studies considering multi-wavelength bulge-disc composition of large galaxy samples include Häußler et al. (2022) and Casura et al. (2022).

The systematic wavelength dependence is generally understood to be a combination of two distinct effects: stellar population gradients and differential dust attenuation. Both early-type and late-type galaxies generally show negative metallicity and age gradients (Tortora et al. 2010; Sánchez-Blázquez et al. 2014; Ibarra-Medel et al. 2016; García-Benito et al. 2017; Zheng et al. 2017; López Fernández et al. 2018; Zhuang et al. 2019; Dale et al. 2020; Parikh et al. 2021; Pessa et al. 2023). These stellar population gradients naturally lead to colour gradients, and thus a systematic decrease in the half-light radius for increasing wavelength. On the other hand, dust attenuation primarily obscures the central regions of galaxies, as evidenced from spatially resolved imaging of galaxies at far-infrared wavelengths (Muñoz-Mateos et al. 2009; Pohlen et al. 2010; González Delgado et al. 2015; Casasola et al. 2017; Greener et al. 2020) and studies of overlapping galaxies (Keel & White 2001a,b; Holwerda et al. 2009). This differential dust attenuation leads to a flattening of the surface brightness profile, and hence to an increase in the half-light radius. Dust attenuation, being strongly wavelength-dependent (Mathis 1990; Draine 2003; Burgarella et al. 2005), automatically generates a decrease in half-light radius with increasing wavelength.

These two effects, stellar population gradients and differential dust attenuation, are hard to disentangle for observed galaxies. They can be disentangled, however, for simulated galaxies. In this work we use the TNG50-SKIRT Atlas (TSA, Baes et al. 2024), a large multi-wavelength synthetic image atlas based on simulated galaxies extracted from the TNG50 cosmological hydrodynamics simulation (Pillepich et al. 2019; Nelson et al. 2019b), to investigate the origin of the wavelength dependence of the effective radius in the optical–NIR wavelength domain. Since dust attenuation can artificially be turned on and off, the relative contribution of the two contributors can be determined. Disentangling these two effects is the main goal of this work.

This paper is organised as follows. In Sect. 2 we discuss the data we use and the methods we adopt to determine effective radii (Sect. 2.2) and half-mass radii (Sect. 2.3) for each simulated galaxy.

2.1. The TNG50-SKIRT Atlas

The TSA (Baes et al. 2024) is a synthetic image atlas for a complete stellar-mass selected sample of 1154 galaxies extracted from the TNG50 simulation (Pillepich et al. 2019; Nelson et al. 2019b). TNG50 is the highest-resolution version of the IllustrisTNG suite of cosmological hydrodynamical simulations (Marinacci et al. 2018; Naiman et al. 2018; Nelson et al. 2018; Pillepich et al. 2018a; Springel et al. 2018). The simulation has a baryonic mass resolution of $8.5 \times 10^5 M_\odot$ and a spatial resolution of $70–140$ pc.

We selected all 1154 galaxies with total stellar mass between $10^{9.5}$ and $10^{12} M_\odot$ from the $z = 0$ snapshot of the TNG50 simulation. For each of these simulated galaxies, the TSA contains high-resolution images in 18 broadband filters covering the UV to NIR wavelength range. All images are generated with the SKIRT radiative transfer code (Camps & Baes 2015, 2020) and account for different stellar populations and absorption and scattering by interstellar dust in a realistic 3D setting. The SKIRT post-processing simulations were based on the prescriptions by Camps et al. (2016, 2018, 2022), Kapoor et al. (2021), and Trčka et al. (2022). For each galaxy, the image atlas contains images for five different random observer positions (with observing positions O4 and O5 antipodal). In addition to the dust-obscured images, the atlas contains, for each observer position, synthetic dust-free images in all 18 bands, and stellar mass surface density, mean stellar age, mean stellar metallicity, and dust mass surface density maps. All images and parameter maps contain $1600 \times 1600$ pix with a pixel scale of 100 pc, corresponding to a field of view of 160 kpc.

The TSA sample contains 869 star-forming and 285 quiescent galaxies when the value $sSFR = 10^{-11}$ yr$^{-1}$ is used as the dividing line between the two populations. Figure 1 shows histograms of a number of physical characteristics of the sample. The stellar masses, star formation rates (SFR), and specific star formation rates (ssSFR) are directly taken from the TNG50 public database (Nelson et al. 2019a). The $u-r$ colours are calculated from the SKIRT-generated maps, and take into account the effects of dust attenuation. The dust masses are calculated by integrating the dust mass surface density maps. We note that the TNG50 hydrodynamical simulations do not explicitly contain a prescription for interstellar dust, so dust was added to the galaxies in post-processing using the assumption that the dust density is proportional to the gas metallicity in cold, dense gas (for details, see Trčka et al. 2022; Baes et al. 2024).

The distribution of stellar masses follows the typical Schechter distribution with a strong decline for increasing stellar mass. While our sample consists of all galaxies with stellar masses between $10^{9.5}$ and $10^{12} M_\odot$, the median stellar mass is only $10^{10.3} M_\odot$. The sample contains galaxies with a variety in SFR, ranging from totally quiescent galaxies to actively star-forming galaxies with SFR $> 20 M_\odot$ yr$^{-1}$ and $sSFR > 10^{-9.5}$ yr$^{-1}$. The median values for the sample are $\langle SFR \rangle = 1 M_\odot$ yr$^{-1}$ and $\langle sSFR \rangle = 10^{-10.3}$ yr$^{-1}$, indicating that most of the galaxies in our sample are star-forming. The distribution of $u-r$ colour covers the range between 0.9 and 2.7 and is bimodal, as also noted in observed samples of galaxies in the local Universe.  

1 More specifically, we generated images in the GALEX FUV- and NUV-bands, the Johnson $UBVRi$-bands, the LSST $ugrizy$-bands, the 2MASS $JHK_s$-bands, and the WISE $W1$- and $W2$-bands.
Fig. 1. Histograms of a number of global properties of the galaxies in our sample: stellar mass, star formation rate, specific star formation rate, $u - r$ colour, and dust mass. The dashed lines indicate the median values of the sample. The peaks at low values in the SFR and sSFR histograms correspond to galaxies without ongoing star formation. Similarly, the peak at low dust mass corresponds to galaxies without interstellar dust content.

Fig. 2. Illustration of the curve-of-growth analysis described in Sect. 2.2, here applied to the 2MASS $H$-band image of simulated galaxy TNG000001 in orientation O1. The 2D surface brightness distribution is fitted with a series of concentric ellipses, and the total integrated flux within each ellipse is determined. The effective radius is the semi-major axis of the ellipse that contains half of the total flux. (Strateva et al. 2001; Baldry et al. 2004; Balogh et al. 2004). The median value is 1.72. Finally, the distribution of dust mass is clearly peaked with a long tail towards low dust masses and with a median dust mass of $10^{7.5} M_\odot$. Such a distribution is consistent with the typical dust masses found in nearby galaxies (Auld et al. 2013; Ciesla et al. 2014; Nersesian et al. 2019; Aniano et al. 2020; Galliano et al. 2021).

2.2. Determination of the effective radii

We measured the effective radius in all LSST and 2MASS wavebands using a curve-of-growth analysis, similar to the approach applied to the galaxies from the Siena Galaxy Atlas by Moustakas et al. (2023). Following most observational studies of the wavelength dependence of the effective radius (e.g. Ko & Im 2005; La Barbera et al. 2010; Kelvin et al. 2012; Vulcani et al. 2014; Lange et al. 2015), we focus on the optical and NIR regime, from the $u$- to the $K_s$-band.

As a first step we first convolve each SKIRT post-processed galaxy image with a Gaussian kernel with FWHM of 5 pix. This step was taken to smooth out fine details and Monte Carlo noise in our galaxy images. We experimented with different values of the smoothing lengths and settled on 5 pix as a trade-off between a significant degradation of the resolution and a sufficient noise reduction. The second step consisted of fitting elliptical isophotes to the individual images by means of the standard IRAF STSDAS/ELLIPSE routine (Jedrzejewski 1987), with the galaxy centre fixed. We determined the total integrated flux within each elliptical aperture, and plotting them as a function of increasing semi-major axis yielded the curve-of-growth. This curve was approximated with a cubic spline fit from which the half-light radius was measured. This procedure was independently executed for every single image in our atlas. Figure 2 illustrates our approach.

For a limited number of images this method did not converge, either because the galaxies were extremely asymmetrical, or because there were technical issues (for example, for galaxies located very close to the border of the simulation volume). We discarded all measurements for a given galaxy and observer position if the ellipse fitting routine failed for at least one band. In total, we had to discard 129 sets of images out of a total of $5 \times 1154 = 5770$ sets, corresponding to a 2.2% rejection rate.

To characterise the accuracy of our effective radius measurements, we compared the values obtained independently for the antipodal O4 and O5 observer positions (the images corresponding to observer position O5 were only used as a check for the accuracy of our analysis but were not used in the statistical analysis in the remainder of this work). Figure 3 shows the histograms of the relative error between the two measurements for the $u$, $i$, and $K_s$-bands. The relative difference between the O4 and O5
Fig. 3. Histograms of the relative difference between the effective radius measured from the antipodal O4 and O5 observer positions in the LSST u- and i-bands and the 2MASS Ks-band. The dashed red lines represent the 16% and 86% quantiles of the distribution. Half of the width of this confidence interval can be used as an upper limit for the relative uncertainty on our Re measurements.

Fig. 4. Correlation between the 3D particle half-mass radius rhalf and the half-mass radius Re determined as the semi-major axis of the elliptical iso-density contour that contains half of the total projected stellar mass. Each galaxy is represented by four dots, one for each of the four independent observer’s positions. The solid yellow line is the best-fitting power-law relation.

measurements decreases with increasing wavelength, which can be attributed to the diminishing effect of dust attenuation and the smoother appearance of galaxies at longer wavelengths. For each band, we calculated the 16% and 84% quantiles of the distribution of the relative difference and considered half of the width of this confidence interval as an upper limit for the relative uncertainty on our Re measurements, as the O4 and O5 images are not perfectly mirrored versions due to different levels of dust attenuation. This value decreases from 7.0% in the u-band to 1.3% in the Ks-band.

2.3. Determination of half-mass radii

We determined the effective radius in the stellar mass surface density maps in the same way as for the synthetic images. The corresponding effective radius, denoted as Re, is the semi-major axis of the elliptical iso-density contour that contains half of the total projected stellar mass. In Fig. 4 we compare Re with the half-mass radius rhalf obtained directly from the TNG50 stellar particle data as the radius of the sphere that contains half of the total stellar mass. For completely spherical models with realistic surface density profiles, we expect a relation

\[ R_e^* = \frac{3}{4} rhalf, \]  

as demonstrated by Ciotti (1991) and Wolf et al. (2010).

Figure 4 shows the correlation between rhalf and Re for all galaxies in our image atlas. Every galaxy has, by definition, a single value for rhalf and four different values for Re, corresponding to each different observer position. This figure shows that, for the majority of the galaxies, Eq. (1) underestimates the stellar mass effective radius, particularly for the smaller galaxies. The individual measurements are colour-coded by the inclination of the galaxy for the given observer, defined as the angle between the direction of the stellar angular momentum vector and the direction towards the observer. For a given half-mass radius, galaxies observed nearly edge-on turn out to have, on average, smaller values for Re than galaxies observed nearly face-on. The solid yellow line is a power-law fit to the individual data points and is given by

\[ \frac{R_e^*}{\text{kpc}} = 0.999 \left( \frac{\text{rhalf}}{\text{kpc}} \right)^{0.922}. \]  

Most importantly, we have, for each galaxy and for each observer’s position, a measurement of the half-mass radius determined in the exact same way as the half-light radius in each of the broadband filters.

3. Results

3.1. Wavelength dependence of the effective radius

In Fig. 5 we compare the effective radius Re in each of the nine considered bands with respect to the half-mass radius Re. Focusing first on the blue contours, which correspond to the effective radii obtained from the dust-free images, we see that the dust-free effective radius is larger than the half-mass radius. This excess is largest in the u-band and systematically decreases towards the Ks-band. Looking at the thicker red contours, which correspond to the images with dust attenuation properly accounted for, we note similar but even more outspoken trends. The effective radius as measured from the dust-obscured images systematically exceeds both the half-mass radius and the dust-free effective radius. The excess decreases with increasing wavelength.
Fig. 5. Comparison between the half-mass radius $R^*_e$ and the half-light radius $R_e$ in nine different optical–NIR broadband filters. Thick red contours correspond to measurements of $R_e$ from the dust-obscured images, slightly thinner blue contours to measurements from dust-free images. The contour correspond to the 10, 40, 70 and 90% percentile levels. The dashed lines represent a one-to-one relationship between $R^*_e$ and $R_e$.

Figure 6 shows the same data in an alternative way. The histograms on the left column display a wide range of effective radii in any broadband filter, which just reflects the variety of sizes in the galaxy population. In each individual band, the distribution of effective radii approximates a lognormal distribution, similar to the effective radius distributions at low redshift shown by Vulcani et al. (2014) and at higher redshift by Shibuya et al. (2015). Our distributions tend to be slightly skewed with a long tail towards smaller effective radii, whereas the distributions presented by Vulcani et al. (2014) are rather skewed towards larger effective radii.

More remarkable than the large spread in $R_e$ is that also the range in $R_e/R^*_e$ is relatively broad in all the bands. At short wavelengths, this is not unexpected, as blue light is a poor estimator for the stellar mass. We find that the width of the distribution in $R_e/R^*_e$ decreases when moving from shorter to longer wavelengths. Interestingly, this width is still non-negligible even in the $K_s$-band that is generally considered as a good proxy for stellar mass. The ratio between the $K_s$-band half-light ratio and half-mass ratio can be as small as 0.8 and as large as 2.

Another interesting characteristic of these histograms is the systematic shift with increasing wavelength. Moving from top to bottom, one notes that the histograms of both $R_e$ and $R_e/R^*_e$ slightly but systematically shift towards smaller values. This shift is present for both the dust-obscured and dust-free measurements of the effective radius. The systematic shift with increasing wavelength can be characterised by the median values of the histograms, indicated as dotted vertical lines in Fig. 6. One can immediately note that these median values systematically decrease as a function of increasing wavelength.

In Fig. 7 we show the median values of $R_e$ and $R_e/R^*_e$ explicitly as a function of wavelength. In each panel, the red lines and markers correspond to the dust-obscured images, the blue ones to the dust-free images. These plots confirm the general trends noticeable in Figs. 5 and 6 and allow to make more quantitative observations. It shows that, across the optical–NIR range, the
half-light radius tends to exceed the half-mass radius, and the median effective radius systematically decreases with increasing wavelength. In the optical g-band the median ratio of $R_e/R_\star$ is 1.58, in the $K_s$-band the median ratio is still 1.13. The two panels of Fig. 7 also show that the effective radii measured from dust-obscured images are systematically larger than those measured from dust-free images. The $g$-band half-light radii measured from dust-obscured images are, on average, 8.7% larger than those measured from dust-free images. In the $K_s$-band the median ratio of this excess reduces to 2.1%.

### 3.2. Origin of the wavelength dependence

These findings confirm the common understanding that the decrease in the effective radius of galaxies with increasing wavelength is the combination of two distinct effects: stellar population gradients and dust attenuation. We note that, in the present study, we do not make an explicit distinction between bulge and disc components. The half-light radius we measure is determined using a curve-of-growth analysis and is a nonparametric measure of the galaxy size. Any variation in the relative intrinsic luminosity of bulge and disc components as a function of wavelength is incorporated in our stellar population gradient.

The stellar population gradient contribution is evident from the fact that the effective radius measured from the dust-free images shows this systematic wavelength dependence. It can only be caused by differences in the intrinsic colours of the stellar populations. Differential dust attenuation and the corresponding flattening of the surface brightness profiles is responsible for an additional contribution to the wavelength dependence of the half-light radius.

Contrary to purely observational imaging studies (e.g. Ko & Im 2005; La Barbera et al. 2010; Kelvin et al. 2012; Vulcani et al. 2014), we can try to disentangle the importance of the two effects to the observed wavelength dependence of the half-light radius because we can artificially turn dust attenuation on or off. We fitted power-law fits to the median trends in Fig. 7, shown as the dotted lines in each panel. The parameters

### Table 1. Parameters of power-law fits to the median wavelength dependence of the effective radius, $\log X = \alpha \log(\lambda/\mu\text{m}) + \beta$.

<table>
<thead>
<tr>
<th></th>
<th>$\alpha$</th>
<th>$\beta$</th>
<th>$\alpha_{\text{dust}}$</th>
<th>$\beta_{\text{dust}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_e$/kpc</td>
<td>-0.248</td>
<td>0.767</td>
<td>-0.194</td>
<td>0.739</td>
</tr>
<tr>
<td>$R_e/R_\star$</td>
<td>-0.249</td>
<td>0.125</td>
<td>-0.196</td>
<td>0.099</td>
</tr>
</tbody>
</table>

Notes. The second and third columns correspond to dust-obscured data, the fourth and fifth column to dust-free data.
of the fits are listed in Table 1. While the two contributions (stellar population gradients and differential dust attenuation) do not linearly add up, we can take the slope of the power-law as a qualitative measure of the importance of each contributor. The joint contribution of stellar population gradients and differential dust attenuation results in a slope of almost −0.25 for the two power-law fits. When we consider only stellar population gradients, that is, when we suppress dust attenuation, we find a slope of nearly −0.20 for the two power-law fits. These numbers suggest that the stellar population gradients are the dominant factor in driving the wavelength dependence of the effective radius, and that differential dust attenuation is a minor, but non-negligible, secondary factor. In the concise style of Trujillo et al. (2004) we can summarise the wavelength dependence of galaxy sizes: 80% stellar population, 20% dust attenuation.

4. Discussion

4.1. Comparison to Vulcani et al. (2014)

The results of the previous section are only valid if the TNG50 galaxies in our sample are representative for the galaxies in the local Universe. In this subsection we compare the wavelength dependence of the effective radius of our TNG50 galaxies with the work by Vulcani et al. (2014). These authors presented the wavelength dependence of the effective radius based on a large sample of galaxies with available optical (SDSS $ugriz$) and NIR (UKIDSS $YJHK$) imaging from the Galaxy And Mass Assembly (GAMA, Driver et al. 2011) survey. The authors considered a complete, volume-limited sample with an absolute r-band magnitude limit of $M_r = −21.2$. They split their sample of galaxies into three different populations based on $u−r$ colour: blue ($u−r < 1.6$), green ($1.6 < u−r < 2.1$), and red ($u−r > 2.1$). They simultaneously fitted one wavelength-dependent Sérsic model to the optical and NIR images with the GALFITM code (Häußler et al. 2013). The dashed lines and open squares in Fig. 8 represent the median values for $R_e$ and $R_e/R_e^2$ as a function of wavelength obtained by Vulcani et al. (2014) for their three subpopulations.

We attempted to mimic the sample selection criteria of Vulcani et al. (2014) by excluding from our sample all the galaxies with $M_r > −21.2$ and subsequently subdividing the resulting sample into three subpopulations using the same $u−r$ colour criteria. The resulting median values for $R_e$ and $R_e/R_e^2$ are shown as the solid lines and filled circles in Fig. 8.

The top panel of Fig. 8 shows that there is a significant difference between the absolute values of the effective radii for the different populations. For the red population, there is a reasonable agreement, with our values, averaged over the entire wavelength range, some 9% smaller than the values by Vulcani et al. (2014). For the green and blue populations, however, there is a significant difference: the median effective radii for our green population are about 29% larger than theirs, and for the blue population this increases to almost 50%.

We see three potential reasons that can contribute to these significant differences. The first reason is we used different techniques to determine the effective radii. Vulcani et al. (2014) use single-component Sérsic fits to the images. Such fitting simultaneously determines the total magnitude, effective radius, and Sérsic index as parameters of the parametric model that provides the best description of the surface brightness distribution in a $\chi^2$ fitting. Our half-light radii, on the other hand, are determined using a curve-of-growth analysis (see Sect. 2.2). It is well-known that different measures for the effective radius can differ systematically, as also demonstrated by Vulcani et al. (2014) in their Fig. 1. Moreover, the spatial resolution (i.e. PSF size and pixel size) of the observed imaging data may also have a significant effect on the observed trends.

A second aspect that can at least be partly explain the differences are sample selection affects. While we adopted the same absolute magnitude and colour criteria, the sample considered by Vulcani et al. (2014) contains galaxies with redshifts up to $z = 0.3$, with a peak in the redshift distribution around 0.2. We only have access to simulated galaxies at $z = 0$ as the TSA currently only considers this single TNG50 snapshot. Since galaxy properties, including galaxy sizes, do change as a function of cosmic time (e.g. Conselice 2014), we cannot expect to have a perfect match at this stage.

Finally, we cannot exclude that the TNG50 galaxies have systematically larger sizes than the galaxies considered by Vulcani et al. (2014). Checking this is not straightforward without a detailed matched sample. We come back to this issue in Sect. 4.2.

One would hope that sample selection effects and the differences between the methods used to measure $R_e$ would be less important when considering the systematic wavelength dependence of the effective radius rather than its absolute value. This seems indeed the case, as shown in the bottom panel of Fig. 8. An interesting feature of this plot is the difference between the red population on the one hand, and the green–blue population on the other hand. The wavelength dependence of the former population is steeper than the one of the latter, both for the observed galaxies and for the simulated TNG50 galaxies. The wavelength dependence of $R_e$ is due to a combination of stellar population gradients and differential dust attenuation.

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2 The SDSS $ugriz$ + UKIDSS $YJHK$ filter set is slightly different from the LSST $ugriz$ + 2MASS $HJK_s$ filter set that we used for our SKIRT post-processing, but this does not fundamentally affect the conclusions of the comparison.
but as red, bulge-dominated galaxies are generally less dusty than blue, disc-dominated galaxies (e.g., da Cunha et al. 2010; Cortese et al. 2012; Smith et al. 2012; Nersesian et al. 2019), this difference in slope must be caused by stronger stellar population gradients. This result is in agreement with our conclusion from Sect. 3.1 that stellar population gradients are the dominant factor in driving the wavelength dependence of the effective radius.

4.2. Comparison to the Siena Galaxy Atlas

As indicated in the previous section, we found a significant difference in the absolute values of the effective radii of our TSA galaxies and the observed galaxies considered by Vulcani et al. (2014). To investigate to which degree the sample selection is responsible for these differences, we compare the effective radii of our TSA galaxies to effective radii for galaxies from the 2020 version of the Siena Galaxy Atlas (SGA-2020 or simply SGA) presented by Moustakas et al. (2023). The SGA is an angular-size-selected multi-wavelength atlas of almost 400,000 nearby galaxies (out to $z < 0.5$). The catalogue is based on deep, wide-field $grz$ imaging from the DESI Legacy Imaging Surveys DR9 (Dey et al. 2019).

For the vast majority of the galaxies in the SGA, the effective radius in each of the $grz$-bands is determined using a method that is very similar to the method we applied. Elliptical isophotes are fitted to the images and the curve-of-growth is determined by integrating the flux within the subsequent elliptical apertures. The main difference to our approach is that the curve-of-growth is fitted by an empirical model from which the effective radius is determined, whereas we use a spline interpolation.

Compared to the multi-wavelength study by Vulcani et al. (2014), which showed the wavelength dependence of the effective radius in 8 bands from $u$ to $H$, the SGA only lists effective radii in three optical bands. On the other hand, this sample has the advantages that we can construct galaxy samples that match more closely, and that the methods used to measure the half-light radius are very similar.

We started our selection by picking from the SGA sample all galaxies with distances between 50 and 150 Mpc. By eliminating galaxies with very low redshifts we ensure that the redshifts are dominated by the Hubble expansion and not by peculiar velocities; by eliminating galaxies with high redshifts we avoid a non-negligible effect of K-corrections and small angular sizes that might make the determination of the effective radius from the DESI imaging data more difficult. We further eliminate all galaxies without measurements of the effective radius in all three bands, we converted the model magnitudes to absolute magnitudes, and we calculated the effective radii in physical units.

To generate a matched sample, we subdivided the observed SGA and simulated TSA samples into two-dimensional bins in $z$-band absolute magnitude and $g-z$ colour. We limited the sample to $-23.1 < M_z < -19.9$ and $0.8 < g-z < 1.4$ to ensure sufficient galaxies in each bin. We considered 16 bins in absolute magnitude with width $\Delta M_z = 0.2$ and three bins in $g-z$ colour with $\Delta(g-z) = 0.2$. In each bin we calculated the median effective radii of the two galaxy samples in the $g$-, $r$-, and $z$-bands. The comparison is shown in Fig. 9.

In all 48 bins, we find that the effective radius decreases from the $g$- to the $r$- to the $z$-band. This is in line with the results from our analysis, namely that the effective radius systematically decreases with increasing wavelength. For the reddest galaxies, i.e., with $1.2 < g-z < 1.4$, we find excellent agreement between the effective radii of the SGA-2020 and the TSA galaxies. The median $r$-band effective radius systematically decreases from almost 9 kpc for $M_z = -22$ to 3 kpc for $M_z = -20$. For bluer galaxies with $g-z < 1.2$, we find significant differences (the strong decrease in the effective radius between $r$-band and $z$-band for the most luminous blue galaxies in the SGA seems spurious). For both the SGA and the TSA samples, the median effective radius systematically decreases for decreasing luminosity, but the absolute values differ. For the fainter galaxies with $M_z = -20$ the median effective radii agree fairly well, but for more luminous galaxies the TSA galaxies are systematically larger than the observed SGA galaxies. The largest differences are found for intermediate luminosities ($M_z \approx -21.5$) and for the bluest colours ($0.8 < g-z < 1.0$); in this case the median $r$-band effective radius of simulated TSA galaxies exceeds the corresponding value of the observed SGA galaxies by about 70%.

Having constructed closely matched samples in which the effective radii are measured in very similar ways, we conclude that difference in median effective radius for the bluer galaxies is most probably due to intrinsic differences in the morphological structure of observed and TNG50 simulated galaxies. On the one hand, this seems surprising, as the IllustrisTNG model is by construction designed to match galaxy sizes at low redshift (Pillepich et al. 2018b, Figs. 4 and 8). In their morphological comparison of TNG100 simulated galaxies and Pan-STARRS observed galaxies, Rodriguez-Gomez et al. (2019) measured systematically larger half-light radii at the massive end ($M_\star > 10^{11} M_\odot$), while the apparent sizes of less massive galaxies agree very well with the observations. On the other hand, the IllustrisTNG model is calibrated at the resolution of the TNG100.
Dependence of the effective radius on global physical properties. Each column corresponds to a different global physical property: $u-r$ colour, stellar mass, star formation rate, specific star formation rate, and specific dust mass. The entire sample is split into six subpopulations based on each of these properties. Top row: median effective radius for each subpopulation. Middle row: median ratio of the effective radius and the $g$-band effective radius. Bottom row: scatter plots relating the physical property to the $g$-band effective radius. All TNG50 galaxies without ongoing star-formation are plotted at SFR = $10^{-3}$ M$\odot$ yr$^{-1}$ and sSFR = $10^{-12}$ yr$^{-1}$, and all dust-free galaxies at $M_{\text{dust}}/M_\ast$ = $10^{-5}$. The blue curves represent running medians.

The result of this analysis is shown in Fig. 10. Each column in this figure corresponds to a different global physical property: $u-r$ colour, stellar mass, star formation rate, specific star formation rate, and specific dust mass. The $u-r$ colour was calculated from the SKIRT-generated dust-obscured images, while the other properties were calculated directly from the TNG50 simulation particle data. For each of these five properties, we split the galaxy sample into six bins with the same number of galaxies in each bin. For the median value of the physical property per bin, see the legend in Fig. 10, middle row. For each bin, we calculate the median value of $R_e$ (top row) and $R_e/R_g$ (middle row) in every band.

In future work we will apply different techniques to investigate the morphological structure of the TSA galaxies, including both parametric modelling (one-component Sérsic fitting and bulge-disc decomposition) and nonparametric methods.

4.3. Dependence of the effective radius on global physical properties

In the previous two subsections, we separated our galaxy sample in different subpopulations according to $u-r$ colour (Sect. 4.1) and $z$-band absolute magnitude and $g-z$ colour (Sect. 4.2). In this subsection we want to generalise these results: we investigate how the absolute value of $R_e$ and the wavelength dependence of $R_e$ vary when we split our sample into different subpopulations by means of different global physical properties. We only use the half-light radii derived from the dust-obscured images in this subsection.

The simulation, and is known to generate slightly increased stellar masses and SFRs at the increased resolution of the TNG50 simulation (Pillepich et al. 2018a,b, 2019; Donnari et al. 2019; Trčka et al. 2022). Using intrinsic half-mass radii extracted from the TNG public database, we find that the median half-mass radius of TNG50 galaxies in the stellar mass range we consider ($10^{9.8} M_\odot < M_\ast < 10^{12} M_\odot$) is 20% larger than that of TNG100 galaxies in the stellar same mass range (4.55 kpc versus 3.73 kpc).

In future work we will apply different techniques to investigate the morphological structure of the TSA galaxies, including both parametric modelling (one-component Sérsic fitting and bulge-disc decomposition) and nonparametric methods.
agreement with the findings from Sect. 4.2. A full analysis of the size–mass relation of the galaxies in the TSA, including the dependence on secondary galaxy parameters and the evolution with redshift, is beyond the scope of this paper and will be the topic of future work. For the present paper, the scatter plots at the bottom row of Fig. 10 mainly serve to interpret the results in the top two rows.

The panels in the first column expand upon the results from Fig. 8 by now splitting the sample into six different bins in $u$–$r$ colour. At every wavelength, the median effective radius decreases with increasing $u$–$r$ colour. The reddest galaxies in our sample with $u$–$r > 2.1$ are more compact than bluer galaxies with $u$–$r < 2.1$. This behaviour can be understood by looking at the bottom left panel. The reddest galaxies are very compact: there are virtually no large galaxies with $u$–$r > 2.4$. Concerning the slope of the wavelength dependence of $R_e$, our results are more mixed: there does not seem to be a systematic and consistent change with increasing colour.

In general, we find a similar behaviour with other global physical parameters. Splitting the galaxies in different subpopulations, we find a systematic change of the median half-light radius at every wavelength. More specifically, the median effective radius in every single band increases with galaxy stellar mass, total SFR, sSFR, and dust-to-stellar-mass ratio. In particular for SFR and specific dust mass, the different subpopulations are clearly separated in the panels on the top row, with positive correlations also clearly visible in the panels on the bottom row.

There does not seem to be a systematic correlation with any global property for the slope of the wavelength dependence of $R_e$. There is hardly any difference in the median slope for the different subpopulations in stellar mass, SFR, or sSFR. When we subdivide the sample according to specific dust mass, we do find different median slopes, but they do not increase or decrease systematically or monotonically over the entire parameter range.

We interpret this lack of a monotonic correlation between the slope of the wavelength dependence of galaxy sizes and any physical property as the result of the two different effects that contribute to this wavelength dependence: stellar population gradients and dust attenuation (Sect. 3.1). The mean metallicity and age gradients in both late-type and early-type galaxies vary strongly with galaxy morphology, galaxy stellar mass and environment (e.g. Tortora et al. 2010; Zheng et al. 2017; Zhuang et al. 2019). On the other hand, specific dust masses and the level of attenuation depends strongly on galaxy morphology and stellar mass (Cortese et al. 2012; Smith et al. 2012; Auld et al. 2013; Vlaeene et al. 2016; Bianchi et al. 2018; Nersesian et al. 2019). It is hence not surprising that we find no systematic correlation between the slope of the $R_e(\lambda)$ relation and a single global galaxy parameter.

5. Summary and conclusion

Based on the TSA, a multi-wavelength atlas of high-resolution synthetic images of simulated galaxies extracted from the TNG50 cosmological simulation, we investigated the wavelength dependence of the effective radius of galaxies at optical and NIR wavelengths. We determined the half-light radius in each individual image (and each stellar mass surface density map) using a curve-of-growth analysis. The main results we obtained are the following:

– The effective radius is, in every band, on average larger than the half-mass radius. This excess is largest in the $u$-band and systematically decreases with increasing wavelength. In the optical $g$-band the median ratio of $R_e/R_g^*$ is 1.58, in the $K_s$-band the median ratio is still 1.13.
– Effective radii measured from dust-obscured images are systematically larger than those measured from dust-free images. The $g$-band half-light radii measured from dust-obscured images are, on average, 8.7% larger than those measured from dust-free images. In the $K_s$-band the median ratio is almost negligible at 2.1%.
– The decrease in the effective radius of galaxies with increasing wavelength is due to the combination of two distinct effects: stellar population gradients and dust attenuation. Since we have both dust-obscured and dust-free images, we can disentangle the importance of the two effects. Assuming that our recipe to populate the galaxies with dust is appropriate, we find that stellar population gradients are the dominant factor (about 80%) in driving the wavelength dependence of the effective radius, followed by differential dust attenuation (20%).
– Comparing our results to the observational study by Vulcani et al. (2014), we find significant offsets in the absolute values of the median effective radii. In particular, the median effective radii for our green and blue populations are about 30 to 50% larger than the median values obtained by Vulcani et al. (2014). We also compare the effective radii of our galaxies to those of a carefully matched sample of observed galaxies from the Siena Galaxy Atlas in different bins in $z$-band absolute magnitude and $g$–$z$ colour. We find excellent agreement for the reddest galaxies, but significant differences for the bluer galaxies. The difference in median $r$-band effective radius peaks at about 70%. Since the samples match closely and the approaches used to determine the effective radius are very similar, we interpret these differences as due to intrinsic differences in the morphological structure of observed and TNG50 simulated galaxies.
– Contrary to the absolute values of the effective radii, we find that the slope of the wavelength dependence of the half-light radius of our TSA galaxies agrees more closely with the observational data from Vulcani et al. (2014). We recover the observational result that the mean wavelength dependence for the red galaxy population is steeper than that for the green–blue population. Stronger stellar population gradients are probably the cause of this difference.
– We investigated how the absolute value of $R_e$ and the wavelength dependence of $R_e$ vary when we split our sample into different subpopulations by means of different global physical properties. We find that the median effective radius in every single band increases systematically with decreasing $u$–$r$ colour and with increasing galaxy stellar mass, total SFR, sSFR, and dust-to-stellar-mass ratio. For the slope of the wavelength dependence of $R_e$, there does not seem to be a systematic, monotonic correlation with any global property. We interpret this as the result of the complex dependence of both population gradients and attenuation on galaxy morphology, stellar mass and environment.

As discussed in Baes et al. (2024), the TSA allows for a suite of applications, in particular concerning the link between intrinsic galaxy properties and galaxy morphology. In future papers we plan to use this image atlas to systematically investigate the wavelength dependence and the effects of dust attenuation on other morphological characteristics, derived from single or multiple-component Sérsic fitting or from a non-parametric morphological analysis. We also envision to extend the TSA by adding similar images at different redshifts, which would allow
a direct investigation of the cosmic evolution of galaxy morphology in the TNG50 simulation and direct apples-to-apples comparison to observational data. Specifically focusing on the effective radius discussed in this paper, it would shed light on the nature of the apparent size evolution of galaxies, the origin of which is still under discussion (e.g. Suess et al. 2019; van der Wel et al. 2024).

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References

Emsellem, E., Charlo...