Understanding the radio emission from \( \epsilon \) Eridani

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ABSTRACT

Some solar-type stars are known to present faint, time-variable radio continuum emission whose nature is not clearly established. We report on Jansky Very Large Array observations of the nearby star \( \epsilon \) Eridani at 10.0 and 33.0 GHz. We find that this star has flux density variations on scales down to days, hours, and minutes. On 2020 April 15 it exhibited a radio pulse at 10.0 GHz with a total duration of about 20 min and a peak four times larger than the plateau of 40 Jy present in that epoch. We were able to model the time behavior of this radio pulse in terms of the radiation from shocks ramming into the stellar wind. Such shocks can be produced by the wind interaction of violently expanding gas heated suddenly by energetic electrons from a stellar flare, similar to the observed solar flares. Because of the large temperature needed in the working surface to produce the observed emission, this has to be nonthermal. It could be gyrosynchrotron or synchrotron emission. Unfortunately, the spectral index or polarization measurements from the radio pulse do not have a high enough signal-to-noise ratio to allow us to determine its nature.

Key words. radiation mechanisms: general – stars: individual: \( \epsilon \) Eridani – radio continuum: stars

1. Introduction

Located at 3.22 pc, \( \epsilon \) Eridani (HD 22049) is a young Sun-like star close to our Solar System. Its spectral type is K2V, and its estimated age is 0.8 Gyr (Di Folco et al. 2004). It has a circumstellar debris disk with a physical extension of \( \sim \)64 AU and a radial width of \( \sim \)20 AU, possibly the residual of the process of formation of a young planetary system (Greaves et al. 1998). Backman et al. (2009) and Reidemeister et al. (2011) have suggested that this disk consists of different components: two warm inner belts, a cold outer belt, and an extended halo of small grains. Observations by Chavez-Dagostino et al. (2016) and Bastian et al. (2018) show continuum emission from the central star at millimeter and centimeter wavelengths.

Like our Sun, \( \epsilon \) Eridani exhibits an active chromosphere (e.g., Baliunas et al. 1981), as well as an active X-ray corona (e.g., Johnson 1981). In addition, it shows a magnetic activity cycle, which was originally reported by Hatzes et al. (2000). Metcalfe et al. (2013) report the simultaneous operation of two magnetic activity cycles, where the amplitude of the shorter cycle of 2.95 yr (see, also, Jeffers et al. 2017) is modulated by a longer, 12.7-year cycle. This resembles the interaction of the 11-year solar cycle with the quasi-biennial (2-year) variations of the Sun (Fletcher et al. 2010).

Bastian et al. (2018) observed radio-continuum emission associated with \( \epsilon \) Eridani with the Jansky Very Large Array (VLA) at four frequency bands: 2–4 GHz, 4–8 GHz, 8–12 GHz, and 12–18 GHz. They report quasi-steady unpolarized emission in the three high-frequency bands, and point out that this quiescent emission is consistent with optically thick emission from the star at coronal temperatures. In the coronal regions of \( \epsilon \) Eridani, the opacity at frequencies higher than 2–4 GHz is dominated by gyrosynresonance absorption, suggesting magnetic fields between 475 G and 2700 G in the low corona and the production of gyrosynresonance emission between 4–8 GHz and 8–12 GHz.

In addition, Bastian et al. (2018) detected a radio pulse from \( \epsilon \) Eridani in the 2–4 GHz band. The detected radio pulse (a sudden brief increase in emission) had a degree of circular polarization of up to 50% and lasted a few minutes. They proposed that the origin of the radio pulse may be nonthermal gyrosynchrotron emission from mildly relativistic electrons interacting with the coronal magnetic fields (\( \sim \)100 G) of the star. Alternatively, coherent cyclotron maser instability emission in the bandwidth 2–4 GHz is also a possible mechanism for the stellar conditions, with magnetic fields of 700–1400 kG. Nevertheless, the problem for cyclotron maser instability emission in coronal conditions is the escape of the radiation, since it is absorbed by gyrosynresonance processes. Alternatively, Bastian et al. (2018) discuss the possibility that the radio pulse could come from an as yet undetected nearby planet with a kG magnetic field, from the interaction with space weather events driven by stellar flares and/or coronal mass ejections from \( \epsilon \) Eridani.

Bastian et al. (1998) pointed out that radio observations were fundamental in establishing that particle acceleration in solar flares is a two-phase process (Wild et al. 1963). There is a first phase of particle acceleration in which electrons reach energies of \( \sim \)100 keV, producing hard X-ray emission, microwave emission, and type III radio bursts. A second phase occurs \( \sim \)10 min after the first phase, in which shock waves are produced by the initial energy released. These shocks then propagate into the corona. During the latter stage, electrons and ions are further accelerated by the Fermi mechanism to energies as high as 100 MeV and 1 GeV, respectively, and type II and type IV radio bursts occur. These bursts are thought to be responsible for geomagnetic effects. In addition, since their discovery, coronal mass ejections have been recognized as the primary drivers of interplanetary and geomagnetic perturbations (see Gosling et al. 1991; Gosling 1993). Consequently, an accepted point of view nowadays is that interplanetary and geomagnetic disturbances are produced by two types of solar energetic phenomena, flares...
and coronal mass ejections, whose relationship is still poorly understood.

Recently, Burton et al. (2022) reported the detection of three flares from $\epsilon$ Eridani using the Atacama Large Millimeter Array (ALMA) at 1.3 mm. They characterized the temporal, spectral, and polarization of these flare events and suggested that their properties are similar to those of the Sun at similar wavelengths. Also, Loyd et al. (2022) conducted a coronal dimming analysis at far-ultraviolet spectral lines in archival observations of $\epsilon$ Eridani and found a prominent flare in the 2015 data.

In another work, Rodríguez et al. (2019, hereafter RLL19) reported VLA observations of $\epsilon$ Eridani at 33 GHz. These observations had high enough angular resolution to demonstrate the stellar origin of the radio emission since the detected emission has an angular size of $\sim0^\circ07$ (which corresponds to a physical extension of 0.2 au from the star), which is smaller than the semimajor axis ($\sim3.4$ au) of the exoplanet $\epsilon$ Eridani b. In addition, RLL19 showed that the observed centimeter emission of $\epsilon$ Eridani from 5 to 50 GHz is remarkably flat and could be due to optically thin free–free emission from a steady stellar wind with a mass-loss rate of $\sim6.6 \times 10^{-14} M_\odot$ yr$^{-1}$, which is 3300 times larger than the solar value, $M_\odot = 2 \times 10^{-14} M_\odot$ yr$^{-1}$ (Feldman et al. 1977). Nonetheless, other mechanisms such as coronal free–free and gyrosesonance emission could not be ruled out. The high mass-loss rate inferred by RLL19 is at odds with the mass-loss rate 30 times the solar value estimated by Wood et al. (2002) from the interstellar hot HI that surrounds the star and is observed in absorption in the Ly$\alpha$ spectrum. The Ly$\alpha$ absorption comes from the interstellar medium gas that is heated by the interaction with the stellar wind. Wood et al. (2002) used hydrodynamic models of atmospheres to infer the mass-loss rates from the HI absorption. Furthermore, Cranmer & Saar (2011) modeled the steady mass-loss rates of cool main-sequence stars and evolved giants. They studied magnetohydrodynamic turbulence motions from subsurface convection zones and their dissipation and escape through the stellar wind. They estimated an even smaller value for the mass-loss rate of $\epsilon$ Eridani, of only 2.4 times the solar value. On the other hand, Johnstone et al. (2015) investigated the evolution of stellar rotation and wind properties of low-mass main-sequence stars. They note that there is a large uncertainty regarding the evolution of the stellar winds of these stars, the major problems being the lack of observational constraints on the wind properties and the large spread in rotation rates at young ages. Thus, disagreement between the mass-loss rates obtained from observations and theoretical models of $\epsilon$ Eridani is still an open problem.

One way to determine if the observed radio emission from $\epsilon$ Eridani is thermal or nonthermal is to study the variability and/or polarization characteristics of the emission. Extremely fast variability would imply that the source is small, and very high brightness temperatures, not achievable with thermal mechanisms, would be required. The presence of linear or circular polarization is indicative of synchrotron or gyrosynchrotron emission, respectively (Güdel 2002). In addition, the spectral index could help in determining the nature of the radio emission, since negative indices ($<-0.1$) cannot be obtained with free–free emission (Rodriguez et al. 1993). For this reason, we monitored the source at 10 GHz and 33 GHz, notably finding a radio pulse at 10 GHz. We investigated the possibility that the pulse could be produced by shocks in the $\epsilon$ Eridani stellar wind. As discussed above, such shocks could be produced in the second phase of stellar flares, after the magnetic energy is released.

The rest of this paper is organized as follows. In Sects. 2 and 3 we discuss the observations. In Sect. 4 we present the model of the flare–wind interaction used to interpret the radio pulse observed at 10 GHz. In Sect. 5 we present our conclusions.

2. Observations

The observations were part of our VLA project 20A-020, made with the Karl G. Jansky VLA of NRAO in its C configuration during eight epochs in 2020 February–May. We used the X band (8–12 GHz) at six epochs and the Ka band (29–37 GHz) at two epochs. The flux and bandpass calibrator was J0137+3309 or J0542+4951, and the phase calibrator was always J0339–0146. In the X band, the digital correlator of the VLA was configured in 32 spectral windows of 128 MHz width, covering the range 8–12 GHz. In the Ka band, the digital correlator of the VLA was configured in 64 spectral windows of 128 MHz width, covering the range 29–37 GHz. In both bands, each spectral window is divided into 64 channels with an individual spectral resolution of 2 MHz. The data were calibrated in the standard manner using the Common Astronomy Software Applications (CASA) package of NRAO and the pipeline provided for VLA observations (McMullin et al. 2007).

We created an image concatenating the six epochs observed at 10.0 GHz (the center of the X band) to search for sources in the field. A robust weighting of 2 (Briggs 1995) was used to optimize sensitivity in all the images discussed here. A total of 13 sources were detected (see Table 1). One of the radio sources corresponds to $\epsilon$ Eridani and of the remaining 12 sources, 10 had been previously detected by RLL19. With the exception of RLL2019 3, which shows an increase of a factor of 2 between the observations reported in RLL19 (taken in 2013) and those presented here, the other sources show flux densities consistent within $\pm25\%$ between the two epochs.

The region was observed at 10.0 GHz at six epochs and at 33.0 GHz (the center of the Ka band) at two epochs, as listed in Table 2. In this table we also give the flux densities of $\epsilon$ Eridani and of the steady source RLL2019 7 for each individual epoch. RLL2019 7 was used as a comparison source to check that the variability was not due to some systematic effect. While RLL2019 7 shows 10.0 GHz flux densities that, within the noise, are consistent with no variability, $\epsilon$ Eridani exhibits important time variability. Two observations made on 2020 April 05 at 10.0 GHz with a time difference of 3.6 h show a flux density increase of about 2.2. On 2020 April 15, $\epsilon$ Eridani appeared unusually bright. A 10 GHz image of the emission at that epoch is shown in Fig. 1. An analysis of the flux density within the time interval of the observations (approximately one hour) shows that most of the increase comes from a flare. This flare had a duration of only about 20 min and shows the characteristic rapid rise and slower fall of flares (see Fig. 2). We tried to estimate the spectral index of the emission during the flare by making images at 9.0 and 11.0 GHz. The flux densities obtained, 155$\pm$17 and 175$\pm$24 mJy respectively, imply a spectral index of 0.6$\pm$0.9, which, unfortunately, does not have a high enough signal-to-noise ratio to discriminate between possible emission mechanisms. The poor signal-to-noise ratio comes from the fact that the two frequencies used are close to each other.

1 The National Radio Astronomy Observatory is a facility of the National Science Foundation operated under cooperative agreement by Associated Universities, Inc.

2 https://science.nrao.edu/facilities/vla/data-processing/pipeline

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Table 1. 10 GHz sources in the field of $\epsilon$ Eridani.

<table>
<thead>
<tr>
<th>Number</th>
<th>RA(J2000) 03$^b$</th>
<th>Dec (J2000) $^c$</th>
<th>Flux density (µJy)</th>
<th>Counterparts</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>32$^{m}$ 44$^{s}$343</td>
<td>29$^{d}$ 21$^{m}$14</td>
<td>180±29</td>
<td>–</td>
</tr>
<tr>
<td>2</td>
<td>32$^{m}$ 47$^{h}$004</td>
<td>28$^{d}$ 23$^{m}$59</td>
<td>127±12</td>
<td>[RLL2019] 3</td>
</tr>
<tr>
<td>3</td>
<td>32$^{m}$ 47$^{h}$783</td>
<td>25$^{d}$ 43$^{m}$28</td>
<td>70±15</td>
<td>–</td>
</tr>
<tr>
<td>4</td>
<td>32$^{m}$ 48$^{h}$852</td>
<td>27$^{d}$ 10$^{m}$53</td>
<td>41±7</td>
<td>[RLL2019] 4</td>
</tr>
<tr>
<td>5</td>
<td>32$^{m}$ 49$^{h}$53</td>
<td>28$^{d}$ 16$^{m}$49</td>
<td>250±9</td>
<td>[RLL2019] 5</td>
</tr>
<tr>
<td>6</td>
<td>32$^{m}$ 54$^{h}$498</td>
<td>27$^{d}$ 29$^{m}$37</td>
<td>46±5</td>
<td>$\epsilon$ Eridani</td>
</tr>
<tr>
<td>7</td>
<td>32$^{m}$ 55$^{h}$149</td>
<td>28$^{d}$ 23$^{m}$02</td>
<td>178±7</td>
<td>[RLL2019] 7</td>
</tr>
<tr>
<td>8</td>
<td>32$^{m}$ 56$^{h}$148</td>
<td>25$^{d}$ 29$^{m}$96</td>
<td>63±6</td>
<td>[RLL2019] 8</td>
</tr>
<tr>
<td>9</td>
<td>32$^{m}$ 58$^{h}$011</td>
<td>24$^{d}$ 13$^{m}$62</td>
<td>352±33</td>
<td>[RLL2019] 9</td>
</tr>
<tr>
<td>10</td>
<td>32$^{m}$ 58$^{h}$144</td>
<td>25$^{d}$ 05$^{m}$95</td>
<td>1127±25</td>
<td>[RLL2019] 10</td>
</tr>
<tr>
<td>11</td>
<td>32$^{m}$ 59$^{h}$068</td>
<td>28$^{d}$ 29$^{m}$40</td>
<td>72±11</td>
<td>[RLL2019] 11</td>
</tr>
<tr>
<td>12</td>
<td>32$^{m}$ 59$^{h}$899</td>
<td>27$^{d}$ 52$^{m}$38</td>
<td>40±5</td>
<td>[RLL2019] 13</td>
</tr>
<tr>
<td>13</td>
<td>33$^{m}$ 08$^{h}$730</td>
<td>28$^{d}$ 10$^{m}$61</td>
<td>359±53</td>
<td>[RLL2019] 14</td>
</tr>
</tbody>
</table>

Notes. The positions and flux densities are from an image made concatenating the data from the six epochs observed at 10.0 GHz. The flux densities are corrected for the primary beam response.

Table 2. Flux density of $\epsilon$ Eridani and [RLL2019] 7 as a function of time (averaged over each epoch of observation).

<table>
<thead>
<tr>
<th>Epoch</th>
<th>Frequency (GHz)</th>
<th>Flux density (µJy) $\epsilon$ Eridani</th>
<th>[RLL2019] 7</th>
<th>Circular polarization</th>
</tr>
</thead>
<tbody>
<tr>
<td>2020 Feb. 11</td>
<td>10.0</td>
<td>37.5±5.1</td>
<td>216±12</td>
<td>≤44%</td>
</tr>
<tr>
<td>2020 Feb. 19</td>
<td>10.0</td>
<td>46.8±3.3</td>
<td>193±9</td>
<td>≤26%</td>
</tr>
<tr>
<td>2020 Apr. 05</td>
<td>10.0</td>
<td>17.3±3.4</td>
<td>170±12</td>
<td>≤86%</td>
</tr>
<tr>
<td>2020 Apr. 05</td>
<td>10.0</td>
<td>37.5±3.1</td>
<td>193±11</td>
<td>≤40%</td>
</tr>
<tr>
<td>2020 Apr. 15</td>
<td>10.0</td>
<td>79.6±3.1</td>
<td>191±9</td>
<td>≤19%</td>
</tr>
<tr>
<td>2020 Apr. 17</td>
<td>10.0</td>
<td>29.9±3.9</td>
<td>162±13</td>
<td>≤65%</td>
</tr>
<tr>
<td>2020 May 08</td>
<td>33.0</td>
<td>62±12</td>
<td>–</td>
<td>≤58%</td>
</tr>
<tr>
<td>2020 May 18</td>
<td>33.0</td>
<td>≤32</td>
<td>–</td>
<td>–</td>
</tr>
</tbody>
</table>

Notes. The last column is the 4σ upper limit to the circular polarization of $\epsilon$ Eridani. The two observations from 2020 April 05 were made with a time difference of 3.6 h. The values given for all epochs are from average images made using all the data from that day. During the flare of 2020 April 15, the 10.0 GHz flux density reached a value of 165±12 µJy and the upper limit for the circular polarization was ≤17%. The value of the 33.0 GHz flux density quoted for 2020 May 18 is a 4σ upper limit.

At 33 GHz, $\epsilon$ Eridani was detected only in the observations of 2020 May 08. Given the small primary beam and lower sensitivity at this frequency, this was the only source detected. Between the two epochs observed at 33 GHz, with a separation of 10 days, the flux density decreased by a factor of at least ~2. Again, we tried to estimate the spectral index of the emission on 2020 May 08 by making images at 31.0 and 35.0 GHz. The flux densities obtained, 62±15 and 61±20 µJy respectively, imply a spectral index of ~0.1±3.4, which, again, does not have a high enough signal-to-noise ratio to discriminate between possible emission mechanisms. Finally, the last column of Table 2 gives the 4σ upper limit to the circular polarization of $\epsilon$ Eridani. No circular polarization was detected at any epoch.

3. Individual sources

3.1. Sources 2 and 13

As noted by RLL19, source 11 of Table 1 is associated with a millimeter source detected by Chavez-Dagostino et al. (2016). In the 7′68 × 7′68 region we imaged at 10.0 GHz, a total of 13 radio sources were detected (Table 1). We wanted to include optical counterparts other than $\epsilon$ Eri and thus added the Gaia Data Release 3 sources from the same region of the sky to our sample (Gaia Collaboration 2016, 2023), for a total of 64 sources. Remarkably, radio sources 2 and 13 coincide within 2σ with the sources Gaia DR3 5164707626664526592 and 5164696081792414464, respectively. We speculate that these two Gaia sources could be background galaxies. According to the NASA/IPAC Extragalactic Database (NED), only source 2 is an infrared source. However, there are no other data, and the nature of the source (galactic or extragalactic) is not determined in the NED.

3.2. Source 11

This source was detected as a single source in the 2013 observations presented by RLL19, which had an angular resolution of ~6″. The higher-angular-resolution observations presented here (Fig. 3) show it actually a double source, probably a radio galaxy.

4. The radio behavior of $\epsilon$ Eridani

4.1. Comparison with the Sun

At 10.0 GHz, the quiet Sun (at sunspot minimum) has a flux density of ≈2.8 × 10⁶ Jy as measured from the Earth
The total peak flux density of $190 \times 10^{-6}$ Jy to the flux densities of [RLL2019] 7 (hollow squares) during the observations of 2020 April 15. Con- tours are $-4, -3, 3, 4, 5, 6, 8, 10, 12, \text{and} 15$ times $4.0 \mu$Jy beam$^{-1}$, the rms noise in this region of the image. The synthesized beam $(3.548\times2.2\text{arcsec}; \text{PA}=6.7^\circ)$ is shown in the bottom-left corner. The cross marks the peak position of the optical star from Gaia Early Data Release 3, corrected for the proper motions of the source (Gaia Collaboration 2020).

Fig. 2. 10.0 GHz flux densities for $\epsilon$ Eridani (solid circles) and [RLL2019] 7 (hollow squares) during the observations of 2020 April 15. The hour is given in Coordinated Universal Time (UTC). The horizontal bars indicate the duration of the scan, while the vertical bars indicate the noise of the measurement. The dashed line joins the data points for $\epsilon$ Eridani. We have added $80 \mu$Jy to the flux densities of [RLL2019] 7 to better separate the data points of the two sources.

With respect to flare activity, Nita et al. (2002) investigated the peak flux distribution of 40 years of solar radio burst data. They find that in the 8.4–11.8 GHz band during solar maximum, one can expect one flare above $8 \times 10^7$ Jy about every 30 days. The total peak flux density of $190 \mu$Jy of the $\epsilon$ Eridani flare reported here would become $8.4 \times 10^7$ Jy at 1 au, comparable to the brightest solar flares. On the other hand, Wang et al. (2020) studied 86 solar events at 9.4 GHz between 2000 and 2010. They find that the peak flux densities are distributed along two orders of magnitude, from about $2 \times 10^7$ to about $2 \times 10^9$ Jy, but the relatively small number of flares observed limits their statistics.

4.2. Interpretation of the observed radio pulse at 10 GHz

Unfortunately, it was not possible to determine the spectral index of the emission during the radio pulse at 10 GHz accurately enough to determine if the origin of the emission is thermal or nonthermal. As discussed in Sect. 4.2, the derived value of the spectral index is 0.6±0.9.

The observed pulse at 10 GHz could be produced by shocks in the ionized stellar wind of $\epsilon$ Eridani (see RLL19). As mentioned above, shocks can occur from the interaction of gas heated by energetic electrons from a stellar flare with the steady stellar wind of the star. When the heated gas collides with the stellar wind, a working surface (WS), bounded by two shock fronts, will be formed as a fast flow overtakes the previously ejected slow wind. In this section we model the observed radio pulse at 10 GHz of $\epsilon$ Eridani as produced by shocks in the stellar wind inside a cone with solid angle $\Omega$.

We assumed that there is an increase in the flow velocity at the base of the wind, that is, during the violent expansion event the ejection velocity drastically increases with respect to the stellar wind value. We also allowed the expanding gas to have a mass-loss rate different from that of the stellar wind. This type of variability in the flow parameters has previously been studied by Montes-Doria et al. (2022) in the case of the Sun. They used the general model of the WS dynamics from Cantó et al. (2000) for highly supersonic flows, which is based on mass and momentum conservation.

The Montes-Doria et al. (2022) model gives a analytic solution for the dynamical evolution of the WS. In this model, the wind is ejected with a constant velocity $v_1 = v_w$ and an isotropic...
mass-loss rate $M_w$. At an injection time $\tau = 0$, one considers mass injection within a solid angle $\Omega$, with an increased velocity $v_i = a v_1$, with $a > 1$, during an interval of time $\Delta \tau$, and a change in the mass-loss rate per unit solid angle from the wind mass-loss rate $m_1 = M_w/4\pi$ to $m_2 = bm_1$. In this case, the WS forms instantaneously and has an initial phase where it moves at a constant speed, $v_{\text{WS}} = \sigma v_w$, where $\sigma = a^{1/2}(1 + a^{1/2}b^{1/2})/(a^{1/2} + b^{1/2})$. Consequently, the position of the WS during this initial phase is given by $r_{\text{WS}} = R_i + \sigma v_w t$, where $R_i$ is the injection radius. Once all the heated gas has entered the WS, the inner shock disappears, giving rise to a decelerating phase. This occurs at a critical time $t_c = \Delta \tau(\sigma - a)$. For later times, the WS decelerates with a velocity and position given by Eqs. (2) and (3) of Montes-Doria et al. (2022). The WS moves away from the source and decelerates, asymptotically approaching the wind velocity, $v_w$. During its evolution, the WS will lose energy via radiation. From Eqs. (4), (5), and (19) of Cantó et al. (2000), the bolometric luminosity of the WS (within the solid angle $\Omega$) can be written as

$$L_{\text{WS}}(t) = \left( \frac{\Omega}{4\pi} \right) \frac{1}{2} M_w v_w^2 \left( \frac{b}{a} \left( a - \frac{v_{\text{WS}}}{v_w} \right)^3 + \left( \frac{v_{\text{WS}}}{v_w} - 1 \right)^3 \right), \quad (1)$$

for $t \leq t_c$, when the WS is bounded by two shocks, and

$$L_{\text{WS}}(t) = \left( \frac{\Omega}{4\pi} \right) \frac{1}{2} M_w v_w^2 \left( \frac{v_{\text{WS}}}{v_w} - 1 \right)^3, \quad (2)$$

for $t > t_c$, when the internal shock disappears and the WS decelerates.

For simplicity, we assumed that a constant fraction, $\epsilon$, of the WS bolometric luminosity is radiated at 10 GHz. Thus, the 10 GHz flux is given by

$$F_{10\text{GHz}}(t) = \epsilon F_{\text{WS}} \equiv \epsilon \frac{L_{\text{WS}}(t)}{4\pi D^2}, \quad (3)$$

where $F_{\text{WS}}$ is the bolometric flux, and $D = 3.22$ pc is the distance to $\epsilon$ Eridani.

To correct the ten data points of the 2020 April 15 observations, we fitted and subtracted the slope of a baseline in time obtained from a linear fit to the first four points. The resulting flux densities are given in Table 3. In Fig. 4 we show these data points as well as a model, as a solid red line. This model gives the flux from a WS produced in a wind with mass-loss rate $M_w = 6.6 \times 10^{-11} M_\odot \text{yr}^{-1}$ and velocity $v_w = 650 \text{km s}^{-1}$ (taken from the model of RLL2019 for the steady wind of $\epsilon$ Eridani), a velocity increase $a = 3.3$, a mass-loss rate parameter $b = 2.6$, a time interval of injection of high velocity gas $\Delta \tau = 3.0$ min, and a solid angle $\Omega = 9.5 \times 10^{-2}$ str (corresponding to a half opening angle $\theta = 10^\circ$). The emission of the WS is superimposed on a steady wind emission of $40 \mu$Jy. The WS has initial velocity $v_{\text{WS}} = 1300 \text{km s}^{-1}$. The inner shock disappears at the critical time $t_c = 8.2$ min, and then the WS starts to decelerate and eventually reaches the wind velocity. The deceleration starts at a distance $R_i = 1.7 R_\odot$ from the center of the star. We note that the duration of the observed radio pulse is longer than the model time interval of ejection of fast material ($\Delta \tau$).

The observed maximum flux of the radio pulse is $150 \mu$Jy, emitted on top of a steady wind emission of $40 \mu$Jy. For the shock model discussed above, the maximum of the total bolometric flux is $F_{\text{max}} = 1.4 \times 10^{13}$ Jy obtained by substituting $v_{\text{WS}}/v_w = \sigma$ in Eqs. (1) and (3)). To observe $150 \mu$Jy at the peak of the 10 GHz pulse, one needs a fraction, $\epsilon$, of the total energy emitted at this frequency to be $\epsilon = 150 \mu$Jy/$F_{\text{max}} = 1.0 \times 10^{-17}$. On the other hand, as discussed in the Introduction, Wood et al. (2002) estimated a mass-loss rate for $\epsilon$ Eridani of 30 times the solar value, that is to say, 110 times smaller than the value of RLL19. Assuming the same wind speed (which is the escape speed from the surface of the star), the shock would have a maximum flux, $F_{\text{max}}$, 110 times smaller because the shock luminosity is proportional to $M_w$ (Eq. (1)). In this case, the fraction of the total energy emitted at 10 GHz would be 110 times higher, namely $\epsilon = 1.2 \times 10^{-15}$.

In this simple model, we do not solve for the shock microphysics. Nevertheless, it can be used to obtain further insights into the origin of the emission. First, the estimated size, $l$, of the emitting region at the distance $R_i = 1.7 R_\odot$ with opening angle $\theta = 10^\circ$ is $l \sim 2.1 \times 10^{10}$ cm. Thus, at the distance of $\epsilon$ Eridani, the WS would need to have a brightness temperature $T_b \sim 3.6 \times 10^6$ K to produce the observed peak flux of $150 \mu$Jy at 10 GHz.

If the emission is thermal, one can calculate the fraction of energy emitted by a black body (BB) in the range 8–12 GHz. The

### Table 3. Flux density of $\epsilon$ Eridani at 10 GHz on 2020 April 15.

<table>
<thead>
<tr>
<th>Hour (UTC)</th>
<th>Flux density (µJy)</th>
</tr>
</thead>
<tbody>
<tr>
<td>21.369</td>
<td>44.8±8.4</td>
</tr>
<tr>
<td>21.431</td>
<td>33.4±7.4</td>
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<td>21.513</td>
<td>39.3±9.5</td>
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<td>21.576</td>
<td>42.5±6.0</td>
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<td>21.657</td>
<td>150.1±8.6</td>
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<td>21.720</td>
<td>190.2±11.0</td>
</tr>
<tr>
<td>21.801</td>
<td>107.7±9.0</td>
</tr>
<tr>
<td>21.864</td>
<td>64.2±9.0</td>
</tr>
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<td>21.946</td>
<td>69.2±8.6</td>
</tr>
<tr>
<td>22.009</td>
<td>62.5±7.9</td>
</tr>
</tbody>
</table>

Notes. The flux densities have been corrected by removing the slope of a linear baseline in time.

![Fig. 4. Model of the radio pulse as the emission of a WS formed in the stellar wind (solid red line) superimposed on a steady emission of 40µJy. The data points are those given in Table 3.](https://example.com/fig4.png)
integral over the whole spectrum, \( B_\nu(T) \), is \( I_{\text{total}} = \int_0^\infty B_\nu d\nu = \sigma_B T^4 / \pi \text{erg s}^{-1} \text{cm}^{-2} \text{str}^{-1} \), where \( \sigma_B \) is the Stefan-Boltzmann constant. In the Rayleigh-Jeans approximation, the integral over the VLA bandwidth at 10 GHz is \( I_{10\text{GHz}} = \frac{I_{12\text{GHz}}}{B_{12\text{GHz}}} B_{\nu} d\nu \sim \left( \frac{T}{B_{12\text{GHz}}} \right) (12^{8} - 8^{8}) \times 10^{27} \times \text{erg s}^{-1} \text{cm}^{-2} \text{str}^{-1} \). Then, the fraction of the BB energy that is radiated in the 10 GHz band is \( \epsilon_{\text{BB}} = \frac{I_{10\text{GHz}}}{I_{\text{total}}} = 1.4 \times 10^{-22} \left( T / 3.6 \times 10^{6} \text{K} \right)^{-3} \). The fraction of thermal BB energy emitted at 10 GHz is thus too small compared to the values calculated above and so the emission of the WS cannot be thermal emission. Therefore, the emission produced by the WS needs to be nonthermal, for example synchrotron emission by relativistic electrons accelerated in the shocks via the Fermi mechanism. In the Sun after a solar flare, electrons are Fermi-accelerated in shocks up to energies of 100 MeV (e.g., Bastian et al. 1998).

In summary, internal shocks produced in the wind, expected from gas heated by stellar flares, can produce the temporal variation in the observed 10 GHz pulse in \( \epsilon \) Eridani. The emission of the WS has to be nonthermal. Further monitoring of this source is needed to obtain the spectral index or polarization measurements of the radio emission and thus further constrain the emission mechanism. The nonthermal emission could be due to gyrosynchrotron from a flare due to magnetic reconnection in the low corona (Nita et al. 2002) or to synchrotron emission from relativistic electrons accelerated in shocks, as in the scenario discussed above. Further observations are required to determine the polarization state and spectral index of the emission. A positive spectral index would indicate gyrosynchrotron or optically thick synchrotron emission. In addition, synchrotron would produce circularly polarized emission, while one expects linear polarization in the case of synchrotron emission (Güdel 2002).

In particular, the observed radiation is entirely consistent with nonthermal gyrosynchrotron emission from a solar-like flare in the low corona. For example, for a source radius of 5% of the stellar radius, the brightness temperature would be a few times \( 10^{5} \) K, consistent with nonthermal gyrosynchrotron emission. This interpretation is also supported by the fact that at lower frequencies Bastian et al. (2018) doubtlessly detected a gyrosynchrotron pulse.

5. Conclusions

Our main conclusions can be summarized as follows:

We present sensitive, high-angular-resolution VLA observations of the nearby (3.22 pc) Sun-like star epsilon Eridani at 10.0 (six epochs) and 33.0 GHz (two epochs). While the other radio sources in the field are steady, \( \epsilon \) Eridani shows flux density variations down to scales of days, hours, and even minutes. The emission at 10 GHz, excluding the radio pulse observed on 2020 April 15, varied by a factor of \( \sim 3 \) during the observation campaign.

The 2020 April 15 radio pulse of \( \epsilon \) Eridani lasted for about 20 min. At the peak of the pulse, the flux density was \( \sim 150 \mu \text{Jy} \), a factor of \( \sim 4 \) above the plateau of \( \sim 40 \mu \text{Jy} \) present at that epoch.

We successfully modeled the energy and temporal variation in the 10 GHz radio pulse in terms of the emission from shocks in the wind of \( \epsilon \) Eridani. These shocks have enough energy to produce the observed flux. The model does not solve for the microphysics of the shock emission. Nevertheless, the brightness temperature required to produce the observed flux implies that the emission has to be nonthermal.

Unfortunately, neither the spectral index nor the polarization measurements of the radio flare emission are stringent enough to determine the nature of the nonthermal radio emission, either gyrosynchrotron from stellar flares or synchrotron emission from relativistic electrons accelerated in shocks. However, the observed flare radiation is consistent with nonthermal gyrosynchrotron emission from a solar-like flare in the low corona. Ultra-sensitive observations such as those that will be provided by the Square Kilometer Array and the Next Generation VLA may be required to firmly establish the nature of the radio emission of \( \epsilon \) Eridani and similar stars.

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References

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