Peculiar hydrogen-deficient carbon stars: strontium-rich stars and the s-process*

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ABSTRACT

Context. R Coronae Borealis (RCB) variables and their non-variable counterparts, the dustless Hydrogen-deficient Carbon (dLHdC) stars have been known to exhibit enhanced s-processed material on their surfaces, especially Sr, Y, and Ba. No comprehensive work has been done to explore the s-process in these types of stars, however one particular RCB star, U Aqr, has been under scrutiny for its extraordinary Sr enhancement.

Aims. We aim to identify RCB and dLHdC stars that have significantly enhanced Sr abundances, such as U Aqr, and use stellar evolution models to begin to estimate the type of neutron exposure that occurs in a typical HdC star.

Methods. We compared the strength of the Sr II 4077 Å spectral line to Ca II H to identify the new subclass of Sr-rich HdCs. We additionally used the structural and abundance information from existing RCB MESA models to calculate the neutron exposure parameter, τ.

Results. We identified six stars in the Sr-rich class. Two are RCBs, and four are dLHdCs. We additionally found that the preferred RCB MESA model has a neutron exposure τ ≃ 0.1 mb−1, which is lower than the estimated τ between 0.15 and 0.6 mb−1 for the Sr-rich star U Aqr found in the literature. We found trends in the neutron exposure corresponding to He-burning shell temperature, metallicity, and assumed s-processing site.

Conclusions. We have found a sub-class of six HdCs known as the Sr-rich class, which tend to lie in the halo, outside the typical distribution of RCBs and dLHdCs. We found that dLHdC stars are more likely to be Sr-rich than RCBs, with an occurrence rate of ~13% for dLHdCs and ~2% for RCBs. This is one of the first potential spectroscopic differences between RCBs and dLHdCs, along with dLHdCs having stronger surface abundances of 15O. We additionally found neutron exposure trends in our RCB models that will aid in understanding the interplay between model parameters and surface s-process elements.

Key words. stars: abundances – methods: observational – stars: carbon – stars: chemically peculiar – stars: evolution – supergiants

1. Introduction

The rare supergiant class of variables known as the R Coronae Borealis (RCB) stars and their non-variable counterparts, the dustless Hydrogen-deficient Carbon (dLHdC) stars, provide a wealth of information on their unique stellar evolution. These two subsets of stars form the overarching class of Hydrogen-deficient Carbon (HdC) stars1. While spanning a higher temperature range (5000–6000 K, Keenan 1993), these stars are spectroscopically similar to other carbon stars, except with very weak or undetectable H lines and CH bands, a severe depletion in 12C, and strong 13C16O bands in the infrared (Clayton 1996, 2012; Clayton et al. 2007). These stars also show enhanced s-process elements, for which the primary neutron source is the 13C(a,n)16O reaction (Asplund et al. 2000). The origin of RCB stars was originally theorized with two possible paths: a post-AGB star undergoing a very late thermal pulse (often called a final He-shell flash or the FF model), and the merger of a carbon/oxygen (CO) and a helium (He) white dwarf (WD) (Fujimoto 1977; Webbink 1984). Recently, the former evolutionary path has fallen out of favor for multiple reasons. Namely, there are three stars known to have undergone a very late thermal pulse: Sakurai’s Object, V605 Aql, and FG Sge, and while these stars do spectroscopically resemble RCB stars, they do not reflect important aspects of the RCB spectrum such as enhanced 18O abundance and weak 13C (Clayton 2012). Additionally, their lifetimes are too short to explain the population size of known RCB stars. Recent RCB models originating from WD mergers have been successful at replicating the 16O/18O and 12C/13C ratios of RCB stars, as well as the average radius, mass and temperatures for these stars (Longland et al. 2011; Menon et al. 2013, 2018; Zhang et al. 2014; Schwab 2019; Lauer et al. 2019; Crawford et al. 2020; Munson et al. 2021).

The s-process abundances in HdC stars are often compared to the “strong” and “weak” components of the Solar System s-process abundances. The former component, which makes up the majority of these abundances, is understood as enrichment from AGB stars which have undergone several thermal pulses and therefore a series of decaying neutron exposures, the sum of...
which can be modeled as a weighted exponential neutron exposure (Beer & Macklin 1989). The latter component, on the other hand, can be understood as a weaker single neutron exposure, the source of which is not well understood (Beer & Macklin 1989). Utilizing the models created by Crawford et al. (2020), in Sect. 4 we estimate a probable neutron exposure for a typical HdC star and compare to those that create the Solar System s-process abundances.

One particularly unusual RCB star, U Aqr, has been recognized for its unique s-process element distribution. In particular, the light s-process elements such as Sr, Y, and Zr are greatly enhanced in comparison to heavier s-process elements such as Ba (see Fig. 1) (Bond et al. 1979; Malaney 1985; Vanture et al. 1999). Bond referred to U Aqr as “the star with the strongest known Strontium lines”, as the blue Sr II lines at 4077 and 4215Å are comparable in strength to Ca H and K. Vanture et al. (1999) suggest that U Aqr’s abundances most resemble the weak single neutron exposure component. Goswami & Aoki (2013) also point out that the dLHdC star HE 1015-2050 has similarly strong Sr II lines in the blue region of the spectrum. Goswami & Aoki (2013) also note that HE 1015-2050 has been observed to have emission lines consistent with those seen in RCB declines and the star has also noted that HE 1015-2050 has been observed to have emission lines in the blue region of the spectrum. Goswami & Aoki (2013) also noted that HE 1015-2050 has been observed to have emission lines consistent with those seen in RCB declines and the star has also

![Fig. 1. The blue region of the spectrum for U Aqr and HE 1015-2050 with a non-Sr-rich comparison star of similar temperature, HD 182040. Ca II H and K are denoted by vertical red lines, Sr II 4077 and 4215 by vertical black lines, and Ba II 4554 by a vertical green line.](image)

Table 1. Observations of Sr-rich stars.

<table>
<thead>
<tr>
<th>Name</th>
<th>Observation date</th>
</tr>
</thead>
<tbody>
<tr>
<td>U Aqr</td>
<td>15 July 2010</td>
</tr>
<tr>
<td>HE 1015-2050</td>
<td>7 June 2012</td>
</tr>
<tr>
<td>EROS2-LMC-RCB-3</td>
<td>18 April 2008</td>
</tr>
<tr>
<td>A249</td>
<td>14 April 2021</td>
</tr>
<tr>
<td>A166</td>
<td>21 May 2021</td>
</tr>
<tr>
<td>C539</td>
<td>24 September 2021</td>
</tr>
</tbody>
</table>

Table 2. Spectral lines relevant to this study.

<table>
<thead>
<tr>
<th>Element</th>
<th>Wavelength (Å)</th>
<th>Light/heavy?</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sr II</td>
<td>4077</td>
<td>Light</td>
<td>Near C₂ bandhead</td>
</tr>
<tr>
<td>Sr II</td>
<td>4215</td>
<td>Light</td>
<td>Ca II H &amp; K</td>
</tr>
<tr>
<td>Ca II</td>
<td>3933, 3968</td>
<td>Light</td>
<td>in between H &amp; K</td>
</tr>
<tr>
<td>Y II</td>
<td>3950</td>
<td>Light</td>
<td></td>
</tr>
<tr>
<td>Ba II</td>
<td>4554</td>
<td>Heavy</td>
<td></td>
</tr>
</tbody>
</table>

3. Spectral line analysis

We measured equivalent widths (EWs) for the available s-process lines. The spectra of HdC stars are full of weak atomic lines and, for the cooler stars, molecular bands. Therefore, the spectral continuum is not directly observable at intermediate resolution and we must rely instead on pseudo-continua and, by extension, pseudo-equivalent widths (hereafter pseudo-EW) of the measured lines. We examine all the lines listed in Table 2. Many of the spectral lines, observed at this intermediate resolution, especially those for weak-lined elements such as Fe, are blended with other lines. Therefore, we were unable to estimate the intrinsic abundances of HdCs, opting only to measure the pseudo-EW of the stronger lines in the spectrum. High resolution abundance analyses have been done for a few individual HdC stars (e.g., Asplund et al. 2000).

For each HdC star, we compared the pseudo-EWs of the Ca II H & K lines to those of the nearby Sr II lines (4077 and 4215 Å). We calculated the ratio of Sr II 4077 to Ca II H, as the Sr II 4215 line is blended with a CN band head, and the Ca II K line is close to the CN bandhead at ~3890 Å. The stars where the Ca II H/Sr II 4077 ratio is less than 1.5, i.e., where the Sr II pseudo-EW is comparable or larger than that of the Ca II H lines, are a special class of HdC star we denote as “Sr-rich”. By comparison, the average value of this ratio for HdC stars that are not rich in Sr is ~5.5. Comparing the pseudo-EWs of Sr II 4077 and Ca II H for all HdC stars allows for clear identification of the six Sr-rich stars (see Fig. 2): U Aqr, EROS2-LMC-RCB-3, HE 1015-2050, A249, A166, and C539. U Aqr and EROS2-LMC-RCB-3
Ca II H and K strength is affecting our selection of Sr-rich stars. Narrow range of temperatures at the cooler end of the RCBs and warmer temperature regime, and most of the Sr-rich stars lie in this. In fact, we find no stars in the Sr-rich class that lie in this regime. If our analysis was biased to include stars with weak Ca II H and K lines. According to Tisserand et al. (2020, 2022), or Ca abundance within the HdC sample, however, we do not see a relationship between luminosity and the Ca II H and K strength. Within our sample, intrinsically brighter stars exhibit weaker Ca II H and K lines. According to Tisserand et al. (2020, 2022), brighter RCB stars tend to be in the warmer temperature regime. If our analysis was biased to include stars with weak Ca II H and K, we would expect most of our Sr-rich class to consist of brighter, and therefore warmer, stars, however we do not see this. In fact, we find no stars in the Sr-rich class that lie in this warmer temperature regime, and most of the Sr-rich stars lie in a narrow range of temperatures at the cooler end of the RCBs and dHdCs. Thus, we do not suspect that some systematic trend in Ca II H and K strength is affecting our selection of Sr-rich stars.

Two other important s-process elements, although less prominent, are observed in the Y II and the Ba II lines. Yttrium is another light s-process element, and therefore should be enhanced to a similar extent as the Sr lines are. This line is clearly visible in the spectra of most HdCs, but since it lies in between the Ca II H & K lines, it is difficult to get an accurate pseudo-EW measurement. Therefore, we inspected this line visually to confirm that the Sr-rich stars are also enhanced in Y II, but otherwise it is not considered. As seen in Fig. 3, all Sr-rich stars have clearly identifiable Y II lines except for A166, whose blue features are nearly undetectable. This star is discussed further in Sect. 5. Barium on the other hand, is a heavy s-process element. The strengths of the lines of Sr, Y, and Ba give us an idea on the neutron exposure during nucleosynthesis, as a strong neutron exposure will enhance Ba as well as Sr and Y, whereas a weak exposure will only enhance the lighter elements (see Sect. 4). We observed a large range in the measured ratios of Y/Ba and Sr/Ba pseudo-EWs, see Fig. 4. The intrinsic spread of Y and Ba abundances has been noted in Asplund et al. (2000) (see Fig. 13). They comment that this indicates a large range in the amount of s-processing that happens within HdC stars. We note that the star A166 has clearly enhanced Ba, which would signify that its neutron exposure is larger than for U Aqr and the rest of the Sr-rich stars.

HdC stars are generally enhanced in s-process elements, as the majority class of RCB stars have average abundances of [Y/Fe] ≈ 0.8 and [Ba/Fe] ≈ 0.4 (Asplund et al. 2000). Notice that this implies the light s-process elements are overabundant compared to heavy elements, however not to the same extent as U Aqr which has [Y/Fe] = 3.3 and [Ba/Fe] = 2.1. This result explains why most of our HdC stars exhibit non-zero pseudo-EWs for the persistent Sr II and Ba II lines, as shown in Fig. 4, but we do not consider all stars as extraordinarily enhanced in these elements.

4. The s-process in HdC stars

Elements heavier than Fe are predominantly synthesized via neutron capture chains in either the slow (s-) or rapid (r-) processes, the relative contributions of which have been modeled in works such as Seeger et al. (1965). Describing the s-process is possible by defining a neutron exposure parameter

\[ \tau [\text{mb}^{-1}] = \int_0^{\tau_{\text{exp}}} n_\nu(t) v_\tau \, dt \]

where \( n_\nu(t) \) is the number density of free neutrons, \( v_\tau \) is the thermal velocity, and \( \tau_{\text{exp}} \) is the duration of the neutron exposure. There are two types of neutron exposure considered. The first case is a single neutron exposure event and the second is a series of decaying neutron exposure events. The second case corresponds to physical situations such as the thermal pulses in AGB stars where between each pulse the population of neutrons decays. This can be represented mathematically as a weighted exponential function \( C e^{-\tau/\tau_0} \) where \( C \) is a weighting constant and \( \tau_0 \) represents how fast the neutron exposure decays between pulses. When describing a neutron exposure event, \( \tau \) is used to describe single neutron exposures and \( \tau_0 \) is used to describe exponential exposures. A thorough explanation of this theory can be found in works such as Clayton et al. (1961) and Clayton (1968, ch. 7), and an exact solution of the exponential case is found in Clayton & Ward (1974).

The measured s-process solar system abundances of heavy elements require two components to get a good model fit: the
“strong” and the “weak” components (Beer & Macklin 1989). The strong component, also referred to as the “main” component, can be replicated by an exponential neutron exposure with \( \tau_0 = (0.30 \pm 0.01)(kT/30 \text{ eV})^{1/2} \text{ [mb}^{-1}] \) (Beer 1986). The weak component, however, is more correctly modeled by a single neutron exposure with \( \tau = (0.23 \pm 0.03)(kT/30 \text{ eV})^{1/2} \text{ [mb}^{-1}] \) (Beer & Macklin 1989). The strong component enhances all \( s \)-process abundances, whereas the weak component mainly enhances the light \( s \)-process elements (i.e., elements with mass number \( \leq 90 \)). This is because \(^{88}\text{Sr}, ^{89}\text{Y}, \) and \(^{90}\text{Zr} \) all have closed neutron shells and, by extension, small neutron capture cross sections. The weaker neutron exposure associated with the weak component does not provide enough neutron flux for significant neutron capture onto these closed shells, therefore causing a buildup of the lighter elements.

Previous studies on U Aqr attempted to characterize its neutron exposure event. Bond et al. (1979) noted that an enhancement of the light \( s \)-process elements such as \( \text{Sr} \) and \( \text{Y} \) is only possible with weak neutron exposures, and is less likely to occur in an exponential exposure. This is corroborated by Malaney (1987) which notes that in single neutron exposures, the \( \text{Sr}/\text{Ba} \) ratio peaks near \( \tau = 0.5 \text{ mb}^{-1} \), with higher exposures having larger amounts of \( \text{Ba} \). Bond et al. (1979) estimates the best fit for U Aqr as a single neutron exposure with \( \tau = 0.6 \text{ mb}^{-1} \), assuming dilution of the processed material by a factor, \( f \approx 10 \). Malaney (1985) assumes a post-AGB origin of U Aqr and therefore fits the star’s abundances using an exponential neutron exposure with \( \tau_0 = 0.1 \text{ mb}^{-1} \). Vanture et al. (1999) point out that qualitatively, the \( s \)-process abundances in U Aqr are similar to those of the solar weak component. They compare their abundance calculations to the general \( s \)-process models presented in Malaney (1987) and find that it requires a large fraction of processed material in the outer atmosphere to match model abundances. They find the best fit to be a single neutron exposure with \( \tau = 0.15–0.4 \text{ mb}^{-1} \), but do not exclude the possibility of an exponential irradiation.

Recently, advances have been made in narrowing down the more likely origin of RCB stars to a double WD merger, and therefore an AGB-like neutron irradiation is unlikely in these kinds of stars. In fact, recent stellar evolution models from Crawford et al. (2020) and Munson et al. (2021) show that RCB surface abundances are set within the first \( \sim 10–50 \) yr of evolution after the WD merger, hundreds of years before reaching the RCB phase, and the surface abundances do not change for the remainder of the star’s evolution. This happens because as the star expands due to energy generation at the He-burning shell, the convective region in the outer envelope splits into two regions and the processed material can no longer be transported from
the burning region to the surface of the star. Therefore, these models imply that the neutron exposure creating the $s$-process abundances on the surface of RCB stars would resemble a single neutron exposure.

Further, using the models from Crawford et al. (2020) we can estimate the neutron exposure for a typical RCB star. We calculated the neutron exposure for five RCB models: SOL8.39, SOL8.69, SUB8.39, SUB8.48, and SUB8.69. An important aspect of calculating $\tau$ is to define the site where the $s$-process will occur. For this work we defined this region in two ways, first where the temperature of the zone is greater than $10^8$ K (where the triple-$\alpha$ process occurs) and the second where the zone’s temperature is greater than $2 \times 10^8$ K (for exploratory purposes). The number density of neutrons and the thermal velocity for each time step was taken as an average over this region. The result values for the neutron irradiation parameter $\tau$ are listed in Table 3 and plotted in Fig. 5.

Three trends can be gleaned from these models. First, models with hotter burning regions such as SOL8.69 and SUB8.69 have significantly weaker neutron irradiations than cooler models. The warmer temperature of these models is such that while there is now a second activated neutron source due to the reaction $^{22}_{\text{Ne}}(\alpha,n)^{26}_{\text{Mg}}$, the neutron poison reaction $^{14}_{\text{N}}(n,p)^{16}_{\text{O}}$ which converts protons into neutrons. Note that this difference in $H$ abundances between the two types of models is not physically motivated, and is instead a result of the process of creating the models. In future models, the $H$ abundance in the envelope will be standardized between different metallicities.

It is clear that the neutron exposures calculated for these models are lower than those estimated for U Aqr, which is understood to have a weaker neutron exposure than normal RCB stars. The lowest irradiation calculated for U Aqr is $\tau = 0.15 \text{ mb}^{-1}$, whereas the largest irradiation calculated for the preferred RCB Model (SUB8.48) is $\tau = 0.1 \text{ mb}^{-1}$. Using the $^{56}_{\text{Fe}}$ neutron capture cross section from Liou et al. (1979) of $\sigma = 7.5 \pm 4.2 \text{ mb}$ at 24.37 keV, a neutron exposure of 0.1 mb$^{-1}$ translates to approximately 0.75 neutrons captured per $^{56}_{\text{Fe}}$ nucleus. This low level of exposure cannot explain the $s$-process abundances in the majority of RCB stars. Most RCB stars have $s$-process enhancements indicative of stronger neutron exposures than that of U Aqr (i.e. they have smaller Sr/Ba ratios), and our models cannot currently explain this discrepancy. Using a separate test set of unpublished RCB models where the initial envelope mass fraction of $N$ was decreased from $10^{-2}$ to $10^{-3}$, we calculated an increase in the neutron irradiation $\tau$ from 0.04 to 8.48. Therefore it is clear that the initial abundance of $N$ plays a large role in the resulting neutron exposure, as it would also govern the presence of the neutron poison, $^{14}_{\text{N}}$. More work must be done on interplay of initial $N$ abundance and available neutrons in RCB models.

While the aforementioned models were created to understand RCB evolution, they additionally inform us about dLHdC star evolution. As the dLHdCs bear a strong resemblance to RCBs, we believe that the formation process of all these stars should be similar. Karambelkar et al. (2022) and Tisserand et al. (2022) suggest that the differences in these stars could be a result of them forming from different WD-binary populations. In this case, the models used for RCBs should be a good approximation to the dLHdCs as well, since the RCB models are not finely tuned to parameters such as mass ratio and total mass. Future modeling will focus more on these parameters and explore whether different initial binary parameters produce results matching either the RCB or dLHdC class of stars. See Sect. 5 for more discussion on the differences between RCBs and dLHdCs.

5. Discussion

Previously, RCB stars and dLHdC stars have been indistinguishable in their abundances derived from optical spectra (Warner 1967). The only known difference between the two classes is whether or not they form dust. $K$-band spectra of CO absorption bands has revealed that dLHdC stars generally have

<table>
<thead>
<tr>
<th>RCB Model</th>
<th>$10^8$ K</th>
<th>$2 \times 10^8$ K</th>
</tr>
</thead>
<tbody>
<tr>
<td>SOL8.39</td>
<td>1.1 mb$^{-1}$</td>
<td>4.7 mb$^{-1}$</td>
</tr>
<tr>
<td>SOL8.69</td>
<td>0.1 mb$^{-1}$</td>
<td>0.3 mb$^{-1}$</td>
</tr>
<tr>
<td>SUB8.39</td>
<td>0.04 mb$^{-1}$</td>
<td>0.9 mb$^{-1}$</td>
</tr>
<tr>
<td>SUB8.48</td>
<td>0.05 mb$^{-1}$</td>
<td>0.1 mb$^{-1}$</td>
</tr>
<tr>
<td>SUB8.69</td>
<td>0.001 mb$^{-1}$</td>
<td>0.003 mb$^{-1}$</td>
</tr>
</tbody>
</table>
larger surface abundance enhancements of $^{18}$O than RCB stars (Clayton et al. 2007; García-Hernández et al. 2009; Karambelkar et al. 2022). It is unknown whether or not the dLHdC class is simply a dustless phase of RCB evolution. There were previously only five known dLHdC stars, however Tisserand et al. (2022) has discovered 27 more dLHdC stars, increasing the sample to 32 total stars. Therefore, we can now begin to discern any further differences between the RCBs and dLHdCs.

Using the spectra of all known RCBs and dLHdCs (Crawford et al. 2022, in prep.), we were able to identify a small sub-class of these stars with extraordinarily enhanced Sr lines, which we denote as Sr-rich stars. The six stars which belong to this sub-class are U Aqr, EROS2-LMC-RCB-3, HE 1015-2050, A249, A166, and C539. The latter four are dLHdCs, the final three of which were recently discovered by Tisserand et al. (2022). These stars are easily differentiated from other HdC stars when comparing their Sr II and Ca II H pseudo-EWs (Fig. 2). There is no clear reason why these six stars have a nearly linear relationship between Sr II and Ca II H pseudo-EWs. These six stars are all in the cooler regime of HdCs (5000–6500 K), which clearly show enrichments of Sr in these stars. The six stars which belong to this sub-class are U Aqr, EROS2-LMC-RCB-3, HE 1015-2050, A249, A166, and C539. The latter four are dLHdCs, the final three of which were recently discovered by Tisserand et al. (2022).

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We additionally explored the Galactic distribution of the Sr-rich stars, which can be seen in Fig. 6. Four out of the five Galactic Sr-rich stars lie clearly in the halo, which is known to have very low metallicity. The star that lies in the bulge is C539. We found one Sr-rich RCB in the LMC: EROS2-LMC-RCB-3. We note as well that this star lies away from the majority of the LMC RCBs which lie in the LMC Bar. It seems, then, that this star also lies in the LMC analog to the halo population. There are four other RCBs that lie within the halo population: AO Her, Z Umi, and NSV 11154 in the Northern Galactic Hemisphere, and ASAS-RCB-6 in the Southern Galactic Hemisphere. We do not currently have the spectra necessary to comment on the strength of Sr in these stars. There is one additional star that appears to be in the Northern halo region. This star is the eponymous R CrB, which only lies 1.3 kpc away from us and is therefore not a true member of the halo. The distribution of Sr-rich stars is significantly different from other HdC stars and thus may indicate a correlation between metallicity and the strength of the neutron exposure.

Recent RCB models such as Crawford et al. (2020) and Munson et al. (2021) have shown convincing evidence for the origin of the surface abundance of $^{18}$O, a trait unique to the HdC stars. This isotope is created during the reaction chain $^{14}$N($\alpha$,γ)$^{18}$O($\beta^+$)$^{18}$O($\alpha$,γ)$^{22}$Ne, which flows to completion in a typical star, causing an enhancement of $^{22}$Ne. However, in these stars, this reaction chain must be halted before completion. These two sets of models show that due to their unusual convective system and its evolution, material is mixed out of the He-burning shell to the surface only within the first ~10–50 yr of post-merger evolution, after which the surface abundances are set and do not change throughout the remainder of the star’s life. Therefore, this short triple-α burning is integral to the existence of surface $^{18}$O. A comparison can easily be drawn between the this short triple-α burning and the requirement of a weak neutron exposure in RCB stars. This possibly parallel relationship could be further explored using IR spectra of the Sr-rich stars to observe the $^{12}$C+$^{16}$O bands. Of the Sr-rich stars, only U Aqr has been observed in the near IR, which confirms it has enhanced $^{18}$O, similar to other RCB stars (Karambelkar et al. 2022). However, dLHdC stars are known to have larger $^{18}$O enhancements than RCB stars (Clayton et al. 2007; García-Hernández et al. 2009), which could
explain the larger occurrence rate of Sr-richness in dLHdC stars. More observations are needed to draw any further conclusions on the relationship between surface $^{18}\text{O}$ and Sr abundances.

The neutron exposure for the Sr-rich class of stars is best understood as a weak, single event. Weaker exposure events can mean either a short time scale, a low neutron density, or a low temperature. As the neutron irradiation $\tau$ relies on the temperature to only the first order, the differences in the He-burning shell temperature from 2.45 to 4.4 $\times 10^8$ K are negligible compared to the other factors that influence the neutron exposure. However, we have no evidence to suggest whether the Sr-rich phenomenon is due to short exposure timescales or lower neutron densities. Weak neutron exposure events deposit neutrons onto seed nuclei up until the lowest mass set of closed neutron shells at $^{88}\text{Sr}$, $^{88}\text{Y}$, and $^{90}\text{Zr}$. These nuclei have significantly smaller neutron capture sections than the nuclei around them in mass, and therefore the $s$-process slows around these nuclei. This is why Sr-rich stars are associated with weaker neutron exposures, as this buildup of lighter $s$-process elements indicates that neutrons are not captured across closed neutron shells. Upon having stronger exposures, neutron capture across these closed shells becomes more likely, and therefore the $s$-process can progress to create higher mass nuclei such as Ba by capturing neutrons onto the lighter nuclei, decreasing their abundance. Thus, as the Ba abundance builds, the lighter elements such as Sr, Y, Zr will decrease in abundance.

The unique Sr-rich star A166 does not show the typically expected range of Sr and Ba abundances. While this star’s Ca II H, K, Sr II, and Y II lines are extremely weak, the ratio of Sr II 4077 vs. Ca II H is still less than 1.5, thus the Sr II 4077 is still enhanced compared to Ca II H. However, it also shows an enhanced Ba II 4554 line. In Fig. 4, we can see that this star has a larger pseudo-EW of Ba II 4554 than any of the other HdCs measured. We note that this star is the reddest known dLHdC, and therefore has quite weak Ca II H & K, so perhaps the comparison is not straightforward. The enhancement of both Sr II (when compared to Ca II H & K) and Ba II is not something we can easily explain using a single neutron exposure. A166 is unique in almost every way compared to normal dLHdCs (Tisserand et al. 2022; Karambelkar et al. 2022). The continuum of the spectrum for this star appears different from all other RCBs and dLHdCs except the similarly unique RCB ASAS-RCB-6. The shape of this star’s continuum resembles that of a late K star, making it appear extremely red and cold. It also displays an IR excess at 22 $\mu$m indicating the presence of cold dust. This redness of the spectrum could influence the perceived strength of the lines in the blue – making the relevant lines nearly undetectable, as they currently appear in the spectrum, and therefore A166 needs to be studied more closely before any conclusions can be drawn regarding its neutron exposure. For now, we include A166 in the Sr-rich class, although it appears to belong to its own, separate class.

There is currently no comprehensive study of $s$-processing in HdCs, so in addition to exploring the sub-class of HdCs with extraordinary Sr enhancement, we also attempted to categorize the neutron exposure in normal HdCs. From the existing estimates of $\tau$ for U Aqr between 0.15 and 0.6 mb$^{-1}$, we estimated that a typical RCB neutron exposure should be greater than 0.6 mb$^{-1}$, however, our calculation using the preferred RCB model from Crawford et al. (2020) gave $\tau = 0.05$, assuming the $s$-process occurs at a temperature of $10^8$ K. We are unsure exactly what causes our models to have very small neutron exposures, but we note that increasing the assumed $s$-process temperature to $2 \times 10^8$ increases $\tau$ to 0.1. By investigating the neutron exposure in other RCB models, we found that our subsolar metallicity models have smaller neutron exposures, likely due to the initial abundance of H. Additionally, warmer models have lower neutron exposures due to the larger activation of the $^{14}\text{N}$ neutron poison. We also found from unpublished models that the initial $^{14}\text{N}$ abundance plays a large role in the neutron exposure – a lower initial $^{14}\text{N}$ leads to an increase in the neutron exposure. Further exploration of the neutron exposures in observed HdCs and RCB models is necessary. Note also that our neutron exposure calculations assumed a single exposure event rather than pulsed exponential exposures, as the latter of these two options is not reconcilable with our current understanding of RCB formation, especially as our RCB models are of WD merger origin.

In summary, we have found a small sub-class of six RCBs and dLHdCs that are extraordinarily Sr-rich. These stars tend to be in the cooler regime of HdCs, clearly showing both C and CN bands, and additionally lie outside of the typical distribution of HdCs in the bulge and old disk regions. One of these stars, A166, is unique even within the class of Sr-rich stars, as it shows strongly enhanced Ba II as well. The expansion of this small class of Sr-rich RCBs and dLHdCs, in tandem with the large increase of known dLHdC stars has allowed us to begin a more detailed exploration into not only the amount of $s$-processing in HdCs, but also the differences and similarities between the two component classes of stars. While dLHdC stars do not exhibit IR dust signatures or the dust declines unique to RCB stars, they do have stronger surface $^{18}\text{O}$ than RCB stars (Karambelkar et al. 2022) and are more likely to be Sr-rich. Tisserand et al. (2022) finds that the dLHdCs have stronger H abundances and weaker CN compared to RCBs, as well as occupying a slightly less luminous space of the color-magnitude diagram. These are the only known differences between dLHdCs and RCBs. Previously, dLHdCs were believed to be RCBs that were in an “off” period, or in other words were simply a dustless phase of RCB evolution. This idea cannot yet be fully discredited, as there are RCB stars with dLHdC-like abundances, and dLHdCs with cold dust shells (Karambelkar et al. 2022). However, there is strong evidence that these stars could be formed from different WD-binary populations (Tisserand et al. 2022; Karambelkar et al. 2022). We are working towards obtaining more data to further explore the differences between the two types of HdC stars and discern whether or not they share an evolutionary history.

6. Conclusions
While HdC stars, especially RCBs, have been known to exhibit $s$-processed material such as Sr and Ba on their surfaces, we have found that there is a small sub-class of HdC stars that have particularly strong Sr features in their optical spectra. All of these stars except for A166 clearly show Sr II 4077 Å features and weak Ba II 4554 Å lines by comparison. The enhancement of Sr but not Ba is indicative of a weak single neutron exposure in the He-burning shell, as a weak exposure would not create the neutron density necessary to capture significantly over the closed shells in the light $s$-process elements. We additionally used existing RCB models from Crawford et al. (2020) to estimate a probable neutron exposure parameter $\tau \sim 0.1$ mb$^{-1}$ in a typical HdC. This neutron exposure is not large enough to explain the $s$-process composition of a typical HdC star, however we are able to begin to explore the trends in this exposure including an assumed $s$-processing site, metallicity, and He-burning region temperature. This is the first analysis of its kind on RCB star models, and our future models will take the induced neutron exposure into consideration.
Our analysis further cements the suggestion that dLHdCs and RCBs must be related in some way. We cannot differentiate whether dLHdCs represent a phase of RCB evolution or are a separate population using the analysis contained in this work alone, however our companion works, Tisserand et al. (2022) and Karambelkar et al. (2022), present convincing evidence that dLHdCs are formed due to differences in mass ratio, composition, and total mass of the progenitor WD-binary system that creates these stars. Discovering new dLHdCs has allowed us to begin noting the first spectroscopic differences between these two sub-classes of HdC stars.

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