VALES

VII. Molecular and ionized gas properties in the pressure balanced interstellar medium of starburst galaxies at \( z \approx 0.15 \)

Juan Molina\(^1,2\), Edo Ibar\(^3\), Nicolás Godoy\(^3,4\), Andrés Escala\(^2\), Tomonari Michiyama\(^1\), Cheng Cheng\(^5,6,3\), Thomas M. Hughes\(^3,5,7,8\), Maarten Baes\(^9\), Yongquan Xue\(^7\), Michal J. Michalowski\(^10\), Paul van der Werf\(^11\), and Xue-Jian Jiang\(^12\)

\(^1\) Kavli Institute for Astronomy and Astrophysics, Peking University, 5 Yiheyuan Road, Haidian District, Beijing 100871, PR China  
\(^2\) Département de Astronomie (DAS), Universidad de Chile, Casilla 36, Santiago, Chile  
\(^3\) Instituto de Física y Astronomía, Universidad de Valparaíso, Avda. Gran Bretaña 1111, Valparaíso, Chile  
\(^4\) Núcleo Milenio de Formación Planetaria – NPF, Universidad de Valparaíso, Av. Gran Bretaña 1111, Valparaíso, Chile  
\(^5\) Chinese Academy of Sciences South America Center for Astronomy, National Astronomical Observatories, CAS, Beijing 100101, PR China  
\(^6\) CAS Key Laboratory of Optical Astronomy, National Astronomical Observatories, CAS, Beijing 100101, PR China  
\(^7\) CAS Key Laboratory for Research in Galaxies and Cosmology, Department of Astronomy, University of Science and Technology of China, Hefei 230026, PR China  
\(^8\) School of Astronomy and Space Science, University of Science and Technology of China, Hefei 230026, PR China  
\(^9\) Sterrenkundig Observatorium, Universiteit Gent, Krijgslaan 281 S9, 9000 Gent, Belgium  
\(^10\) Astronomical Observatory Institute, Faculty of Physics, Adam Mickiewicz University, ul. Śloneczna 36, 60-286 Poznań, Poland  
\(^11\) Leiden Observatory, Leiden University, PO Box 9513, 2300 RA Leiden, The Netherlands  
\(^12\) East Asian Observatory, 660 North A’ohoku Place, Hilo, Hawaii 96720, USA

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ABSTRACT

Context. Spatially resolved observations of the ionized and molecular gas are critical for understanding the physical processes that govern the interstellar medium (ISM) in galaxies. The observation of starburst systems is also important as they present extreme gas conditions that may help to test different ISM models. However, matched resolution imaging at \( \sim \) kpc scales for both ISM gas phases are usually scarce, and the ISM properties of starbursts still remain poorly understood.

Aims. We aim to study the morpho-kinematic properties of the ionized and molecular gas in three dusty starburst galaxies at \( z = 0.12 \)–0.17 to explore the relation between molecular ISM gas phase dynamics and the star-formation activity.

Methods. We employ two-dimensional dynamical modelling to analyse Atacama Large Millimeter/submillimeter Array CO(1–0) and seeing-limited Spectrograph for INtegral Field Observations in the Near Infrared Paschen-\( \alpha \) (Pa\( \alpha \)) observations, tracing the molecular and ionized gas morpho-kinematics at \( \sim \) kpc-scales. We use a dynamical mass model, which accounts for beam-smearing effects, to constrain the CO-to-H\(_2\) conversion factor and estimate the molecular gas mass content.

Results. One starburst galaxy shows irregular morphology, which may indicate a major merger, while the other two systems show disc-like morpho-kinematics. The two disc-like starbursts show molecular gas velocity dispersion values comparable with those seen in local luminous and ultra luminous infrared galaxies but in an ISM with molecular gas fraction and surface density values in the range of the estimates reported for local star-forming galaxies. We find that these molecular gas velocity dispersion values can be explained by assuming vertical pressure equilibrium. We also find that the star-formation activity, traced by the Pa\( \alpha \) emission line, is well correlated with the molecular gas content, suggesting an enhanced star-formation efficiency and depletion times of the order of \( \sim 0.1 \)–1 Gyr. We find that the star-formation rate surface density (\( \Sigma_{\text{SFR}} \)) correlates with the ISM pressure set by self-gravity (\( P_{\text{gas}} \)) following a power law with an exponent close to 0.8.

Conclusions. In dusty disc-like starburst galaxies, our data support the scenario in which the molecular gas velocity dispersion values are driven by the ISM pressure set by self-gravity and are responsible for maintaining the vertical pressure balance. The correlation between \( \Sigma_{\text{SFR}} \) and \( P_{\text{gas}} \) suggests that, in these dusty starbursts galaxies, the star-formation activity arises as a consequence of the ISM pressure balance.

Key words. galaxies: starburst – ISM: kinematics and dynamics – galaxies: star formation

1. Introduction

Understanding how galaxies build up their stellar mass content within dark matter haloes is a key goal in modern extragalactic astrophysics. One of the best constraints comes from studying the evolution of the star-formation rate density (SFRD) across cosmic time (Madau et al. 1996; Madau & Dickinson 2014). The overall decline in the SFRD in the last \( \sim 10 \) Gyr coincides with the decrease in the average fraction of molecular gas mass in galaxies (Tacconi et al. 2010; Geach et al. 2012; Carilli & Walter 2013). A straightforward interpretation is that the molecular gas is the fuel that maintains the star-formation activity (Bigiel et al. 2008; Leroy et al. 2008). If the gas supply into galaxies is continuously smooth, then the formation of stars may be driven by internal dynamical processes within the interstellar medium (ISM; Kereš et al. 2005; Bournaud et al. 2007;
Dekel et al. 2009; Spring & Michałowski 2017). It is therefore essential to identify the physical processes that govern the ISM properties to tackle galaxy evolution.

A complete characterization of the ISM involves the understanding of many complex processes that are driven and evolve on different spatial and time scales. The ISM models often assume a dynamic equilibrium (e.g. Thompson et al. 2005; Ostriker et al. 2010; Faucher-Giguère et al. 2013; Krumholz et al. 2018). In this “quasi-steady state”, the ISM gas pressure is set to maintain the vertical pull from galaxy self-gravity. The star-formation activity, parameterized by the Kennicutt-Schmidt law (Kennicutt 1998a), arises as a result of the pressure balance (e.g. Ostriker & Shetty 2011; Hayward & Hopkins 2017).

It is still unclear which mechanism is predominately responsible for setting the pressure support to stabilize the ISM gas against self-gravity. One possibility is stellar feedback (e.g. Ostriker & Shetty 2011; Kim et al. 2011). Another possibility comes from the energy released by gravitational instabilities and mass transport within galactic discs (Krumholz & Burkert 2016; Krumholz et al. 2018). Local galaxy spatially resolved observations show trends in favour of the stellar-feedback regulated model (Sun et al. 2020). Unresolved observations for starbursts also agree with this model (Fisher et al. 2019). However, there is also evidence that additional sources of energy beyond stellar feedback may help support system self-gravity (Zhou et al. 2017; Molina et al. 2019a), especially for systems with high star-formation rates (SFRs; e.g. Varidel et al. 2020). Luminous and ultra luminous infrared galaxies (LIRGs; ULIRGs) seem also to be in vertical pressure equilibrium set by the release of gravitational energy (Wilson et al. 2019). In any case, to test the pressure balance-based ISM models, galaxy spatially resolved observations that trace the ISM gas phases, star-formation activity, and the stellar component are needed.

Obtaining such a dataset for large galaxy samples is generally time-consuming. While integral field unit (IFU) observations targeting the star-formation activity in galaxies are common (e.g. Sánchez et al. 2012; Bryant et al. 2015), molecular gas spatially resolved observations are relatively scarce. Observing the spatial distribution of the molecular gas content in star-forming galaxies (SFGs) is still, relative to the optical and near infrared (IR) observations, highly time-consuming. This is true even for the present times of Atacama Large Millimeter/submillimeter Array (ALMA) and the NOrthern Extended Millimetre Array (NOEMA). The hydrogen molecule (H$_2$) is not easily detectable at low temperatures in the range of a few hundred Kelvin (e.g. Papadopoulos & Seaquist 1999; Bothwell et al. 2013), and the use of molecular gas tracers, such as the carbon monoxide molecule ($^{12}$C$^{16}$O, hereafter CO) seem of rotational low-J transitions (e.g. $J < 10$), is strictly necessary to indirectly observe this cold gaseous ISM phase (Solomon & Vanden Bout 2005; Bolatto et al. 2013).

In this work, we introduce new detailed ~kpc-scale morphokinematics observations towards three starburst galaxies taken from the Valparaiso ALMA/APEx Emission Line Survey (VALE; Villanueva et al. 2017; Cheng et al. 2018) at $z \sim 0.12-0.18$. The VALE survey is designed to target low-J CO emission line transitions in dusty galaxies extracted from the Herschel Astrophysical Terahertz Large Area Survey (H-ATLAS; Eales et al. 2010). VALE extracts sources from the equatorial Galaxy And Mass Assembly (GAMA) fields (Driver et al. 2016), which present wide broad-band imaging and photometry in multiple bands sampling the galaxy spectral energy distribution (SED) from far-ultraviolet (far-UV) to IR. The VALE survey covers the redshift range of $0.02 < z < 0.35$, stellar masses ($M_\star$) from $\approx 6$ to $11 \times 10^{10} M_\odot$, and the IR-luminosity range of $L_\text{IR} = 10^{10}-10^{12} L_\odot$ (see Villanueva et al. 2017 for more details).

We characterize the molecular gas morpho-kinematics by observing the CO($J = 1-0$, $\nu = 115.271$ GHz) molecule via ALMA. These sub-mm observations are complemented by spatially resolved seeing-limited ionized gas phase measurements taken by the Spectrograph for INtegral Field Observations in the Near Infrared (SINFONI) IFU located at the European Southern Observatory Very Large Telescope (ESO-VLT). The ionized gas ISM phase is traced by observing the nebular Paschen alpha (Pa$\alpha$) emission line ($\lambda_{\text{Pa}} = 1.8751$ $\mu$m). Our observations are one of the few that use the CO and Pa$\alpha$ emission lines to study the ISM dynamics in dusty starbursts.

We assume a Lambda cold dark matter (LCDM) cosmology with $\Omega_M = 0.73$, $\Omega_{\Lambda} = 0.27$, and $H_0 = 70$ km s$^{-1}$ Mpc$^{-1}$. Thus, at a redshift range of $z = 0.1-0.2$, a spatial resolution of 0.06 corresponds to a physical scale between 1.0 and 1.8 kpc.

2. Observations and data reduction

2.1. The three targeted galaxies

We selected three galaxies taken from the VALES survey at $z \approx 0.12-0.18$. These systems were selected based on their likelihood to be molecular gas-rich systems, that is, with expected molecular gas fractions $f_{\text{H}_2} \equiv M_{\text{H}_2}/(M_{\text{H}_2} + M_\star) > 0.3$ assuming a Milky Way-like CO-to-H$_2$ conversion factor $\alpha_{\text{CO, MW}} = 4.6 M_\odot$ (K km s$^{-1}$ pc$^2$)$^{-1}$ (Bolatto et al. 2013). Our “gas-rich” criterion takes into account two observational facts: (1) the negligible cosmic evolution of $f_{\text{H}_2}$ in the redshift range $z = 0-0.2$ (Villanueva et al. 2017; Tacconi et al. 2018); and (2) local galaxies have average molecular gas fractions of $\approx 0.1$ (Leroy et al. 2009; Saintonge et al. 2017) with only a few of these presenting $f_{\text{H}_2} > 0.3$ ($\approx 1\%$ based on XCOLDGASS survey $M_{\text{H}_2}$ measurements re-scaled by assuming $\alpha_{\text{CO, MW}}$; Saintonge et al. 2017).

In Fig. 1, we present the global properties for these three galaxies compared to full VALES and GAMA surveys. We adopt the SFG “main-sequence” parametrization suggested by Whitaker et al. (2012). The main sequence corresponds to the tight correlation between the galaxy stellar masses and SFRs. Our three targets are representative of the starburst galaxy population.

Using the Baldwin-Phillips-Terlevich (BPT) diagram (Baldwin et al. 1981), we show that two systems lie just below the limit of the pure star-forming region (Kauffmann et al. 2003). The remaining target (HATLAS14625–014511) is located in the low ionization nuclear emission line region (LINER). The H$\beta$, [OIII], H$\alpha$, and [NI] flux measurements are presented in Appendix A. By using the Wide-field Infrared Survey Explorer (WISE; Wright et al. 2010) mid-IR colour diagram (right-hand panel in Fig. 1; Stern et al. 2012; Mateos et al. 2012). HATLAS114625–014511 would be classified as an active galactic nucleus (AGN) host galaxy, while the other two targets are classified as SFGs in agreement with the BPT-diagram analysis.

2.2. ALMA observations

In this work, we describe an ALMA follow-up campaign (taken from project 2015.1.01012.S; P.I.: E. Ibar) for imaging three VALES galaxies for which we obtained the previous bright CO(1–0) detections presented in Villanueva et al. (2017).
was interactively cleaned down to 2−σ in spectral channels. The solid and dashed lines represent the main-sequence (MS) parametrization suggested by Whitaker et al. (2012) and the 4×SFR(MS) starburst threshold, respectively. Middle: BPT-diagram (Baldwin et al. 1981). The dashed curve shows the empirical star-forming threshold (Kauffmann et al. 2003), whereas the solid curve corresponds to the theoretical maximum starburst model (Kewley et al. 2001). These two lines encompass the SFGs-AGN “composite” zone. The dotted-dashed line indicates the division between AGNs and LINERs (Schawinski et al. 2007). Right: WISE mid-IR colour-colour diagram. The solid lines delimit the AGN-zone suggested by Mateos et al. (2012), whereas the dashed line represents the AGN threshold adopted by Stern et al. (2012). The WISE data 1−σ errorbars are smaller than the plotted symbol sizes. The GAMA data are taken from their data-release 3 (GAMA-DR3; Baldry et al. 2018), encompassing galaxies at z < 0.35 (the upper redshift limit for the VALES survey) and with 5−σ or higher flux estimates. These three panels indicate that the three galaxies presented in this work can be classified as starbursts, with one target (HATLAS114625−014511) likely to be classified as an obscured AGN host galaxy.

Observations were taken on Band-3 with the extended 12 m array to obtain higher spatial and spectral resolution imaging than previous observations. The spectral setup was designed to target the redshifted CO(1−0) emission line (between 97 GHz and 103 GHz, depending on the source) using a spectral window in frequency division mode to cover 1.875 GHz of bandwidth at a native 3906.250 kHz resolution. The other three spectral windows were used in time division mode and were positioned to measure the continuum emission around the redshifted line. Observations were taken under relatively good weather conditions with precipitable water vapour (P.W.V.) ranging from 0.6 mm to 0.8 mm, and using 36 to 38 antennas with a maximum baseline of 1.5 km. The phase, bandpass, and flux calibrations are listed in Table 1.

Data reduction was carried out using the Common Astronomy Software Applications (CASA) and using the provided ALMA pipeline up to calibrated 1µv products. Data taken on different days were concatenated together after running the pipeline and before imaging. After exploring different imaging approaches using task TCLEAN, and guided by our scientific objectives, we decided to use a Briggs weighting (ROBUST = 0.4) to reach a major axis full width half maximum (FWHM) for the synthesized beam (θ_{maj}) in a range between 0′.45−0′.52. For each source, we applied a slight convolution (within TCLEAN) to obtain a circular beam. The pixel size was set to 0′.1. All three sources were clearly detected at high significance, and the signal was interactively cleaned down to 2−3−σ in spectral channels with confident source emission.

Final images reach rms noises of ~400−500 µJy beam−1 at ≈12 km s−1 channel width. The channel width was set to minimize spectral resolution effects (Molina et al. 2019a). The continuum emission image, obtained over 6 GHz bandwidth, reaches noise levels of 13 µJy beam−1. Two targets are detected as point sources with peak flux densities of ~110 µJy beam−1, while HATLAS121446.4−011155 remains undetected.

### 2.3. SINFONI observations

We observed the Paα emission line by using the SINFONI IFU (Eisenhauer et al. 2003) on the ESO-VLT in its seeing-limited mode (Project 099.B-0479(A); P.I. J. Molina). The SINFONI field-of-view (FOV) is 8′×8′ with a pixel angular size of 0′.125. The spectral resolution is λ/∆λ ~ 3800, and OH sky lines have ~5 Å FWHM (~30 km s−1 at 2.1 µm). The observations were carried out in service mode between 2017 March 15 and 2017 December 11 in seeing and photometric conditions (point spread function – PSF FWHM ∼ 0′.4−0′.8 in K-band). In addition, two different jittering patterns were used during the observing runs in order to boost the observation signal-to-noise ratio (S/N) in one galaxy.

#### 2.3.1. “OSSO” jittering

To observe the HATLASJ114625−014511 and HATLASJ121446.4−011155 galaxies (hereafter, HATLAS114625 and HATLAS121446, respectively), we used the traditional “ABBA”
chop sequences, nodding 16′’0 across the IFU. That means that the traditional jittering OBJECT-SKY-SKY-OBJECT (“OSSO”) pattern was implemented. We used one observing block (OB) per target, implying a total observing time of ≈3.2 ks per source. The raw datasets for these two sources were reduced by using the standard SINFONI ESOREX\textsuperscript{1} data reduction pipeline.

2.3.2. OOOO Jittering

We perform an on-source experimental jittering pattern to increase the S/N of the Paα emission line in one galaxy. In this experimental observation, the pointing was kept fixed at the galaxy location. Thus, an OBJECT-OBJECT-OBJECT-OBJECT (“OOOO”) jitter sequence was used. Based on previous analyses by Godoy et al. (in prep.), this observing approach provides reliable results for emission lines with $S/N \gtrsim 15$.

To reduce the data, we first used the SINFONI ESOREFLEX and ESOREX pipelines. Then, sky emission lines were subtracted using SKYCOR (Noll et al. 2014), while MOLECFIT (Kausch et al. 2015) was implemented to remove telluric absorption band-pass lines (Godoy et al., in prep.). This was necessary as we did not have “sky” observations.

To test this experimental jitter pattern, we chose the brightest galaxy in our small sample, HATLASJ090750.0+010114 (hereafter, HATLAS090750). By using this method, the observed emission line S/N is expected to increase by $\sim \sqrt{2}$ compared to the use of an OSSO jitter pattern due to the extra on-source time. For this observation, the exposure time was also set to ≈3.2 ks. More details about this experimental observation are reported in Appendix B.

2.3.3. Flux calibration

The standard star observation was used to perform the flux calibration. First, the galaxy spectrum was corrected in each pixel by atmospheric telluric absorptions and by the SINFONI $K$-band transmission curve. We did this by collapsing the standard star datacube in the spectral axis using a wavelength range free from significant telluric absorptions. A two-dimensional Gaussian function was fitted to this spectrally collapsed image.

To determine the PSF FWHM ($\theta_{\text{PSF}}$) for each $K$-band observation, we fitted a two-dimensional Gaussian function, we determined $\theta_{\text{PSF}} \approx 0\farcs62$, $0\farcs39$, and $0\farcs81$ for HATLAS090750, HATLAS114625, and HATLAS121446, respectively.

2.4. Stellar mass and IR-based SFR estimates

The stellar masses for the three galaxies were estimated in Villanueva et al. (2017) by using the photometry provided by the GAMA survey (extending from the far-UV to far-IR (FIR) – $\sim 0.1–500 \mu$m) and by using the Bayesian SED fitting code MAGPHYS (Da Cunha et al. 2008). We assumed a Chabrier (2003) initial mass function (IMF). The $M_*$ values are presented in Table 2.

The IR-based SFRs (SFR\textsubscript{IR}) were estimated by using the rest-frame far-IR 8–1000 μm luminosity ($L_{\text{IR}}$) estimates taken from Ibar et al. (2015). By assuming a Chabrier (2003) IMF, the SFR\textsubscript{IR} values were calculated following SFR\textsubscript{IR} ($M_\odot$ yr$^{-1}$) = $10^{10} \times L_{\text{IR}}$ (L$_\odot$; Kennicutt 1998b) and correspond to the obscured star-formation activity. The IR-based SFRs are consistent with the SFR estimates suggested by MAGPHYS but tend to be offset by a factor of $\sim 2$ towards higher values (see Villanueva et al. 2017 for more details).

2.5. CO(1–0) luminosities

The total galaxy CO(1–0) velocity-integrated flux densities ($S_{\text{CO}(1-0)} \Delta v$) were taken from Villanueva et al. (2017). Briefly, these were estimated by implementing a two-step procedure. First, the CO(1–0) line was spectrally fitted by a Gaussian profile to determine its FWHM and to spectrally collapse the datacube within $\pm 1 \times$ FWHM. Then, $S_{\text{CO}(1-0)} \Delta v$ values were estimated by fitting a two-dimensional Gaussian function to the spectrally integrated datacube (moment 0) using the task GAUSSFIT within CASA. Finally, the CO(1–0) luminosities ($L'_{\text{CO}(1-0)}$) were calculated by following Solomon & Vanden Bout (2005):

\[
L'_{\text{CO}(1-0)} = 3.25 \times 10^7 S_{\text{CO}(1-0)} \Delta v \nu_{\text{obs}}^2 D_L^2 (1+z)^{-3} \text{[K km s}^{-1}\text{pc}^2],
\]

where $S_{\text{CO}(1-0)} \Delta v$ is in Jy km s$^{-1}$, $\nu_{\text{obs}}$ is the observed frequency of the emission line in GHz, $D_L$ is the luminosity distance in Mpc, and $z$ is the redshift. Both estimates are presented in Table 2.

3. Analysis and results

3.1. Average ISM properties

To analyse the spatially integrated emission line fluxes for our three galaxies, we first collapsed the new ALMA and SINFONI datacubes into one-dimensional spectra (Fig. 2). These spectra were built by stacking the spectra seen in the individual pixels from which we detected an emission line (see Sect. 3.2). Before stacking, we manually shifted the individual emission lines to rest-frame accounting for redshift and the respective pixel line-of-sight (LOS) velocity value (see Fig. 3). Thus, we tried to

\textsuperscript{1}http://www.eso.org/sci/software/pipelines/
Table 2. Spatially integrated measurements for the three starbursts.

<table>
<thead>
<tr>
<th></th>
<th>HATLASJ090750.0+010141</th>
<th>HATLASJ114625.4−014511</th>
<th>HATLASJ121446.0−011155</th>
</tr>
</thead>
<tbody>
<tr>
<td>RA (J2000)</td>
<td>09:07:50.07</td>
<td>11:46:25.01</td>
<td>12:14:46.47</td>
</tr>
<tr>
<td>Dec (J2000)</td>
<td>+01:01:41.47</td>
<td>−01:45:12.81</td>
<td>−01:11:55.55</td>
</tr>
<tr>
<td>(z_{\text{spec}})</td>
<td>0.12834</td>
<td>0.16553</td>
<td>0.17981</td>
</tr>
<tr>
<td>(M_\star \times 10^{10} M_\odot)</td>
<td>1.4 ± 0.4</td>
<td>5.1 ± 1.2</td>
<td>6.6 ± 1.7</td>
</tr>
<tr>
<td>(L_{\text{IR}} \times 10^{10} L_\odot)</td>
<td>50 ± 1</td>
<td>53 ± 1</td>
<td>35 ± 1</td>
</tr>
<tr>
<td>SFR(\text{IR})</td>
<td>50 ± 1</td>
<td>53 ± 1</td>
<td>35 ± 1</td>
</tr>
<tr>
<td>(f_{\text{Pa}} \times 10^{-17} \text{erg s}^{-1} \text{cm}^{-2})</td>
<td>–</td>
<td>1069 ± 111</td>
<td>644 ± 96</td>
</tr>
<tr>
<td>(E(B−V)_{\text{Neb}})</td>
<td>–</td>
<td>1.35 ± 0.05</td>
<td>0.91 ± 0.06</td>
</tr>
<tr>
<td>SFR(\text{Pa})</td>
<td>–</td>
<td>32 ± 4</td>
<td>25 ± 4</td>
</tr>
<tr>
<td>SFR(\text{Pa,corr})</td>
<td>–</td>
<td>67 ± 8</td>
<td>40 ± 6</td>
</tr>
<tr>
<td>(S_{\text{CO}}\Delta v \text{ (Jy km s}^{-1})</td>
<td>6.8 ± 0.6</td>
<td>6.6 ± 0.6</td>
<td>4.6 ± 0.6</td>
</tr>
<tr>
<td>(L_{\text{CO}}' \times 10^9 \text{K km s}^{-1} \text{pc}^2)</td>
<td>5.4 ± 0.5</td>
<td>8.6 ± 0.8</td>
<td>7.3 ± 0.9</td>
</tr>
</tbody>
</table>

Notes. The far-IR luminosities are calculated across the rest-frame 8−1000 \(\mu\)m wavelength range. \(E(B−V)_{\text{Neb}}\) is the colour excess estimated by using the observed \(Hα\)-to-\(Pa\alpha\) flux ratio. SFR\(\text{Pa}\) and SFR\(\text{Pa,corr}\) correspond to the observed and attenuation-corrected \(Pa\alpha\)-based SFR estimates, respectively. \(S_{\text{CO}}\Delta v\) is the velocity-integrated flux density. \(L_{\text{CO}}'\) is the \(CO\)(1–0) line luminosity taken from Villanueva et al. (2017).

minimize any line broadening produced by rotational motions, and we focused on intrinsic individual emission line widths.

In all three starbursts, the spatially integrated \(Pa\alpha\) emission line seems broader than the \(CO\)(1–0) emission line. By convolving the ALMA spatially integrated spectrum by the SINFONI line spread function (LSF; green curves in Fig. 2), we find that the spectral resolution difference is not producing this trend. The difference between the spatially integrated \(Pa\alpha\) and \(CO\)(1–0) line widths seems to be caused by broader nuclear \(Pa\alpha\) emission lines in the individual pixels in each galaxy (see Sect. 3.2.2). The broad nuclear emission lines indicate that the ionized gas ISM phase is more affected by turbulent supersonic motions than the molecular gas. We do not detect any broad-line component (\(>500 \text{ km s}^{-1}\)) in the spatially collapsed SINFONI spectra, suggesting the absence of signatures from a broad-line region produced by an AGN.

We used the \(Pa\alpha\) emission line shapes to derive SFR estimates (less affected by attenuation compared to \(H\alpha\)) using the Kennicutt (1998b) conversion for the Chabrier (2003) IMF. By assuming an intrinsic \(H\alpha\)-to-\(Pa\alpha\) ratio equal to 0.116 (Case B recombination, Osterbrock & Ferland 2006), the Paα-based SFRs (SFR\(\text{Pa}\)) were calculated following SFR\(\text{Pa} = 4.0 \times 10^{-41} \times L_{\text{Pa}} \text{ (erg s}^{-1}\)\). The SFR\(\text{Pa}\) values are presented in Table 2. We do not present an SFR\(\text{Pa,corr}\) estimate for the HATLASJ090750 galaxy as we were unable to obtain a reliable flux calibration for its SINFONI observation.

We computed the nebular \(E(B−V)\) colour excess (\(E(B−V)_{\text{Neb}}\)) by using the observed \(H\alpha\)-to-\(Pa\alpha\) flux ratio\(^3\) and a Calzetti et al. (2000) attenuation law. We list the \(E(B−V)_{\text{Neb}}\) values in Table 2. We note that these \(E(B−V)_{\text{Neb}}\) values are \(\sim 4.7\) and \(\sim 2.3\) times higher than the colour excess estimates given by MAGPHYS for the stellar component (\(E(B−V)\) \(\approx 0.29\) and \(\approx 0.39\) for HATLAS114625 and HATLAS121446, respectively). This is expected from local galaxy studies, where the higher \(E(B−V)_{\text{Neb}}\) values suggest a differential attenuation model in which stars experience attenuation from a diffuse ISM dust component, but the massive young stars experience an additional attenuation as they are embedded in their dusty birth clouds (Calzetti et al. 2000). However, we note that the HATLAS114625 nebular-to-stellar colour excess ratio is twice than the average value found in local galaxies (\(-2.3\), Calzetti et al. 2000), indicating its highly dusty nature, and more in line with the findings of an extreme obscured starburst galaxy population at \(z \sim 0.5−0.9\) (Calabrò et al. 2018).

By considering the derived \(E(B−V)_{\text{Neb}}\) values, we estimated attenuation-corrected SFR\(\text{Pa}(\text{SFR}\text{Pa,corr})\) values of \(67±8\) and \(40±6\) \(M_\odot\text{ yr}^{-1}\) for HATLAS114625 and HATLAS121446, respectively. These estimates are slightly higher than the SFR\(\text{IR}\) values (Table 2) but still consistent with the 2-\(\sigma\) uncertainties for both starbursts.

3.2. Galaxy dynamics

We constructed the two-dimensional moment maps by following Swinbank et al. (2012). Briefly, the spectrum associated with each pixel corresponds to the average spectrum calculated from the pixels inside a square area that contains the spatial resolution element – the synthesized beam or PSF. The noise per spectral channel was estimated from a region that does not contain any source emission. We used the LMFIT PYTHON package (Newville et al. 2014) to fit a Gaussian profile to the emission lines. In the case of the SINFONI observations, we masked the spectrum at the wavelength ranges where OH sky-line features are present, and the \(Pa\alpha\) line widths were corrected by spectral resolution effects. We applied an \(S/N = 5\) threshold to determine whether we have detected an emission line or not. If this criterion was not achieved, then we increased the square binned area by one pixel per side and repeated the Gaussian fit. We iterated up to two more times in order to avoid large binned regions. After the third iteration, if the \(S/N\) criterion was not achieved, we masked that pixel and skipped to the next one.

The pixel-by-pixel intensity, velocity, and velocity dispersion 1-\(\sigma\) uncertainties were estimated by re-sampling via Monte Carlo simulations the flux density uncertainties in the data. The maps from both emission lines are presented in Fig. 3.
The CO(1–0) and Paα intensity maps present smooth distributions with no clear level of clumpiness, at ~kpc-scales, in the three starbursts. These also agree with the stellar morphology seen in the K-band image. However, we note that OH sky-line features present in the SINFONI observations may add noise to the Paα two-dimensional maps, and this may partly explain the smoother CO(1–0) maps as the ALMA spectra are free from sky-line residuals.

In the particular case of the HATLAS090750 system, the K-band and Paα intensity images show two asymmetric features that may be related to gas inflow, gas outflow or tidal interaction. These features suggest an ongoing merging process. Both features account for ~18% of the total Paα flux suggesting ongoing star-formation activity. One of the asymmetric features has a projected velocity blueshift of ~300 km s$^{-1}$ compared to the system centre, while the other feature presents a velocity redshift of ~80 km s$^{-1}$, suggesting that this system has a complex three-dimensional shape. The ALMA observation just traces the CO(1–0) emission coming from the central part of this system, probably due to sensitivity limitations. Interestingly, the central part of this system shows a rotational pattern in the CO(1–0) and Paα velocity maps, with a peak-to-peak rotational velocity of $V_{\text{max}}\sin(i) \sim 90$ km s$^{-1}$.

In contrast, HATLAS114625 and HATLAS121446 show clear disc-like rotational patterns in their CO(1–0) and Paα velocity maps. The ionized and molecular gas kinematics broadly agree in both starbursts, with peak-to-peak rotational velocities of $V_{\text{max}}\sin(i) \sim 360$–460 km s$^{-1}$, respectively.

3.2.1. Kinematic modelling

We modelled the ionized and molecular gas ISM kinematics by fitting the two-dimensional LOS velocity fields. The model velocity maps were constructed by assuming an input arctan rotation curve:

$$ V(R) = V_0 + \frac{2}{\pi} V_{\text{asym}} \arctan(R/R_i), $$

where $R_i$ is the radius at which the rotation curve turns over, $V_0$ is the systemic velocity (i.e. redshift), and $V_{\text{asym}}$ is the asymptotic rotational velocity (Courteau 1997).

For each observation, the kinematic model considers seven free parameters ($V_0$, $V_{\text{asym}}$, $R_i$, PA, $[x/y]$, and inclination angle). We convolved the velocity model map with the PSF or synthesized beam, and we used the EMCEE PYTHON package (Foreman-Mackey et al. 2013) to find the best-fit model.

We used the K-band Sérsic photometric models (Sérsic 1963) to constrain the inclination angle values. We used the K-band best-fit minor-to-major axis ratio ($b/a$; Table 3) as initial guess inputs to the kinematic modelling, and we allowed it to
search the best-fit inclination value within a 3-$\sigma$ range. To better account for the $K$-band model $b/a$ uncertainty, we adopted a $b/a$ ratio 1-$\sigma$ relative error equal to 10%, as suggested by Epinat et al. (2012). The inclination angle was derived from $b/a$ by considering an oblate spheroid geometry (Holmberg 1958):

$$\cos^2(i) = \frac{(b/a)^2 - q_0^2}{1 - q_0^2},$$

where “$i$” is the galaxy inclination angle and $q_0$ is the intrinsic minor-to-major axis ratio (i.e. disc thickness) of the galaxy. For edge-on systems ($i = 90$ deg), $q_0 = b/a$. We used the $q_0 = 0.14$ mean value reported for edge-on galaxies at low redshift ($z < 0.05$, Mosenkov et al. 2015).

The model best-fit parameters and $\chi^2$ values are given in Table 4, and the rms values are shown in each residual map (Fig. 3). The kinematic position angles roughly agree with each
Table 4. Best-fit kinematic parameters for the galaxies in our sample.

<table>
<thead>
<tr>
<th></th>
<th>HATLAS090750</th>
<th>HATLAS114625</th>
<th>HATLAS121446</th>
</tr>
</thead>
<tbody>
<tr>
<td>$i_{\text{CO}}$ (deg)</td>
<td>65</td>
<td>70</td>
<td>80</td>
</tr>
<tr>
<td>$\text{PA}_{\text{CO}}$ (deg)</td>
<td>$-132 \pm 1$</td>
<td>$-76 \pm 1$</td>
<td>$-10 \pm 1$</td>
</tr>
<tr>
<td>$R_{1/2,\text{CO}}$ (kpc)</td>
<td>1.44 $\pm 0.01$</td>
<td>2.09 $\pm 0.01$</td>
<td>2.74 $\pm 0.01$</td>
</tr>
<tr>
<td>$V_{\text{rot,CO}}$ (km s$^{-1}$)</td>
<td>67 $\pm 2$</td>
<td>198 $\pm 22$</td>
<td>245 $\pm 5$</td>
</tr>
<tr>
<td>$\sigma_{r,\text{CO}}$ (km s$^{-1}$)</td>
<td>35 $\pm 12$</td>
<td>26 $\pm 10$</td>
<td>34 $\pm 11$</td>
</tr>
<tr>
<td>$X_{r,\text{CO}}$</td>
<td>11.2</td>
<td>10.4</td>
<td>7.0</td>
</tr>
<tr>
<td>$i_{\text{Pa}}$ (deg)</td>
<td>65</td>
<td>70</td>
<td>80</td>
</tr>
<tr>
<td>$\text{PA}_{\text{Pa}}$ (deg)</td>
<td>$-123 \pm 1$</td>
<td>$-81 \pm 1$</td>
<td>$-9 \pm 1$</td>
</tr>
<tr>
<td>$R_{1/2,\text{Pa}}$ (kpc)</td>
<td>2.10 $\pm 0.05$</td>
<td>1.72 $\pm 0.01$</td>
<td>2.52 $\pm 0.03$</td>
</tr>
<tr>
<td>$V_{\text{rot,Pa}}$ (km s$^{-1}$)</td>
<td>68 $\pm 4$</td>
<td>190 $\pm 7$</td>
<td>246 $\pm 9$</td>
</tr>
<tr>
<td>$\sigma_{r,\text{Pa}}$ (km s$^{-1}$)</td>
<td>66 $\pm 18$</td>
<td>51 $\pm 30$</td>
<td>51 $\pm 31$</td>
</tr>
<tr>
<td>$X_{r,\text{Pa}}$</td>
<td>7.1</td>
<td>5.0</td>
<td>7.8</td>
</tr>
</tbody>
</table>

Notes. PA is the kinematic major-axis position angle. $R_{1/2}$ is the half-light radius corrected by beam-smearing effects. $\sigma_r$ is the global velocity dispersion value (see Sect. 3.2.2). $V_{\text{rot}}$ is the rotational velocity measured across the major kinematic axis. $i$ is the inclination angle (for a face-on galaxy, $i = 0$ deg). We do not give uncertainty estimates for $i$ as it is constrained by the $K$-band image model. The “CO” and “Pa” sub-indices indicate the emission line from the component whose parametric values were estimated.

other ($\Delta \text{PA} = \text{PA}_{\text{Pa}} - \text{PA}_{\text{CO}} \leq 10$ deg). For the HATLAS114625 and HATLAS121446 galaxies, these also roughly agree with the position angles derived from the K-band image modelling.

The best-fit disc model gives a reasonable fit to the inner ionized and molecular gas kinematics of the HATLAS090750 galaxy, as suggested by the low reported rms value. This may indicate a fast relaxation process of the ISM molecular gaseous phase into a disc-like galaxy in the central zone of this system (e.g. Kronberger et al. 2007). For the other two galaxies, the rms values presented in the Pa$\alpha$ velocity residual maps tend to be larger than the values derived from the CO(1–0) observations, suggesting that the ionized gas ISM phase may be a more sensitive tracer of non-circular motions compared to the molecular gas ISM phase. However, these high rms values are also a consequence of the coarser SINFONI spectral resolution compared to the ALMA observations as well as additional noise induced by the OH sky-line features present in some pixels at the wavelengths where the Pa$\alpha$ emission line is found.

3.2.2. Kinematic parameters

We used the best-fit dynamical models to simulate a slit observation along the major kinematic axis, and we extracted the one-dimensional rotation velocity and velocity dispersion curves for both ISM phases (Fig. 4). We considered a slit width equal to the synthesized beam or PSF FWHM. The half-light radii for the ionized and molecular gas ISM phases ($R_{1/2,\text{Pa}}$, $R_{1/2,\text{CO}}$) were calculated by using a tilted ring approach. From the rotation curve, we defined the rotational velocity for the Pa$\alpha$ and CO observations ($V_{\text{rot,Pa}}$, $V_{\text{rot,CO}}$) as the inclination-corrected values observed at two times the Pa$\alpha$ and CO half-light radii, respectively.

To correct the velocity dispersion values for beam-smearing effects, we applied the correction suggested by Stott et al. (2016). This corresponds to a linear subtraction of the local velocity gradient $\Delta V/\Delta R$ from the beam-smeread line widths. However, to further consider beam-smearing residual effects from this correction, we defined the global velocity dispersion for each gas phase ($\sigma_{r,\text{CO}}$, $\sigma_{r,\text{Pa}}$) as the median value taken from the pixels located beyond three times the synthesized beam or PSF FWHM from the dynamical centre (white circumferences in velocity dispersion maps in Fig. 3).

For HATLAS090750, we find a very compact CO light distribution, as suggested by its half-light radius. In its central zone, this system shows a low rotational velocity value ($V_{\text{rot,CO}} \sim 70$ km s$^{-1}$) and a high median velocity dispersion $\sigma_{r,\text{CO}} \sim 35$ km s$^{-1}$, suggesting a molecular gas ISM phase with highly supersonic turbulent motions and a CO-traced kinematic ratio $V_{\text{rot,CO}}/\sigma_{r,\text{CO}} \sim 2$. The CO- and Pa$\alpha$-based rotation curves clearly agree at the radius at which CO(1–0) is detected (Fig. 4), implying that the $V_{\text{rot,CO}}$ and $V_{\text{rot,Pa}}$ values also agree.

In contrast, the Pa$\alpha$ emission tends to show broader line widths compared to the CO emission line ($\sigma_{r,\text{Pa}} \sim 66$ km s$^{-1}$). This is unlikely to be produced by beam-smeread flux coming from the asymmetric features as the broader Pa$\alpha$ line widths are seen across the entirety of the major kinematic axis. Assuming that the line widths trace the turbulent kinematic state of the respective ISM gas phase, this result suggests that the molecular gas phase may be able to dissipate the turbulent kinetic energy faster than the ionized gas phase. Another possibility could be an additional energy injection in the ionized gas from stellar feedback such as stellar winds, supernovae feedback, and/or Wolf-Rayet episodes (e.g. Thornton et al. 1998; Crowther 2007; Kim & Ostriker 2015; Martizzi et al. 2015; Kim et al. 2017). The expansion of over-pressured Hii regions is also a possibility (Elmegreen & Scalo 2004). We recall that we have corrected the SINFONI observations by using instrumental line broadening effects.

For HATLAS114625 and HATLAS121446, the molecular and ionized gas ISM phases show similar scale sizes $R_{1/2,\text{Pa}}/R_{1/2,\text{CO}} \approx 0.85 \pm 0.01$ and 0.96 $\pm 0.01$, respectively. For HATLAS12146, these half-light radius estimates also agree with $R_{1/2,\text{K}}$ (see Table 3). However, for HATLAS114625, we find that $R_{1/2,\text{K}}/R_{1/2,\text{CO}}/\text{Pa} \approx 1.3\sim1.6$ kpc, suggesting that the ionized and molecular gas ISM phases are distributed in a more compact disc-like structure in this galaxy.

For both starbursts, the velocity curves agree, and we derived ionized to molecular gas rotation velocity ratios $V_{\text{rot,Pa}}/V_{\text{rot,CO}} \approx 1.04 \pm 0.04$ and 0.94 $\pm 0.14$ for HATLAS121446 and HATLAS114625, respectively. The consistency between the CO- and H$\alpha$-based velocity curves tends to be found in local galaxies.
Fig. 4. Rotation velocity (left) and velocity dispersion (right) profiles across the major kinematic axis for the HATLAS090750 (top), HATLAS114625 (middle), and HATLAS121446 (bottom) galaxies. The errorbars show the 1-σ uncertainties. The vertical black-dashed line represents the best-fit dynamical centre. The light grey shaded area represents the 3× synthesized beam size region centred at the best-fit molecular gas dynamical centre, whereas the dark grey dashed area represents the 3× PSF FWHM zone centred at the best-fit ionized gas dynamical centre. In the rotation velocity profile panels, the dashed- and solid-green curves show the rotation curves extracted from the beam-smeared Paα and CO(1–0) two-dimensional best-fit models, respectively. In the velocity dispersion profile panels, the green- and magenta-dashed lines show the median galactic value estimated from the outskirts of the galactic disc (Table 4) for the CO(1–0) and Paα observations, respectively. We find a good agreement between the rotation curves derived from the ionized and molecular gas ISM phases in the three starbursts.

where the ionized gas emission seems to come from recent star-formation activity episodes (Levy et al. 2018).

In both systems, the median $\sigma_{\text{Pa}α}$ values are lower than the corresponding $\sigma_{\text{Pa}α}$ estimates ($\sigma_{\text{Pa}α}/\sigma_{\text{CO}} \sim 1.5–2$); however, they still agree within 1-σ uncertainties. The CO and Paα velocity dispersion values seen in both galaxies suggest a dominant common nature. The CO and Paα velocity dispersion profiles (Fig. 4) suggests even closer $\sigma_{\text{Pa}α}$ and $\sigma_{\text{CO}}$ values. Nevertheless, we note that our measured $\sigma_{\text{Pa}α}$ values tend to be higher than the estimates reported from local systems ($\approx 9–19$ km s$^{-1}$, Levy et al. 2018). Indeed, these median $\sigma_{\text{Pa}α}$ values are consistent with the lower end of the velocity dispersion estimates measured from ULIRGs ($\approx 30–140$ km s$^{-1}$, Downes & Solomon 1998; Wilson et al. 2019).

We derive an average CO-based rotational velocity to dispersion velocity ratio ($V_{\text{rot,CO}}/\sigma_{\text{CO}}$) of 8 ± 3 and 7 ± 2 for HATLAS114625 and HATLAS121446, respectively. If we consider the Paα observations, we derive $V_{\text{rot,Paα}}/\sigma_{\text{Paα}} \sim 4 \pm 2$ and $\sim 5 \pm 3$, respectively. Independent of the emission line considered, the $V_{\text{rot}}/\sigma_{\text{v}}$ ratios measured for HATLAS114625 and HATLAS121446 suggest that the rotational motions are the main support against self-gravity in both starburst galaxies.

### 3.2.3. Comparison with previous VALES works

Using our kpc-scale resolution data (~0.5″), we tried to test if the previous kinematic analysis done for the VALES galaxies (Molina et al. 2019a) may be biased due to beam-smearing effects. These previous CO(1–0) observations were performed by using a more compact ALMA array configuration, thereby delivering a coarser spatial resolution ($\sim 3–4″ \approx 5–7$ kpc). Beam-smearing could hide galaxy morpho-kinematic properties, making it hard to recover unbiased intrinsic properties when the spatial resolution is of the order of several kpc.

The galaxies presented in this work, HATLAS114625 and HATLAS121446, were not described in Molina et al. (2019a) as they were not extended enough for a dynamical interpretation. However, we can still make a brief comparison with the VALES systems that share similar global properties.

We concentrated on VALES sources with specific SFR values ($\text{sSFR} \equiv \text{SFR}/M_\star$; $\log(\text{sSFR}) < 0.3$ dex) similar to those estimated for HATLAS114625 and HATLAS121446 ($\text{sSFR} \approx 10–100$ Gyr, respectively). For these sources, we find that the kinematic maps present marginally resolved rotation ($V_{\text{rot,CO}} \approx 40–200$ km s$^{-1}$) and high velocity dispersion values ($\sigma_{\text{CO}} \approx 40–70$ km s$^{-1}$), implying $V_{\text{rot,CO}}/\sigma_{\text{CO}}$ ratios in the range of 1–3. These values are lower than the ones presented in this work, suggesting that the kinematic parameters presented in Molina et al. (2019a) might be systematically biased due to beam smearing. This comparison is not straightforward as the resolution presented in this work is five to seven times higher than in Molina et al. (2019a); however, it highlights the importance of high-resolution imaging for extracting more precise dynamical information.

### 3.3. The CO-to-H$_2$ conversion factor from dynamics

A CO-to-H$_2$ conversion factor must be used to estimate molecular gas masses from the CO luminosities ($M_\text{H}_2 = \alpha_{\text{CO}} L_{\text{CO}}^\prime$). Traditionally, two different $\alpha_{\text{CO}}$ values have been considered to calculate $M_\text{H}_2$ for galaxies as a whole (Solomon & Vanden Bout 2005). An $\alpha_{\text{CO,MW}} \approx 4.6$ M$_\odot$ (K km s$^{-1}$ pc$^2$)$^{-1}$ value seems to be more appropriate for disc-like galaxies (e.g. Solomon et al. 1987), whereas an $\alpha_{\text{CO,ULIRG}} \approx 0.8$ M$_\odot$ (K km s$^{-1}$ pc$^2$)$^{-1}$ value has been estimated for ULIRGs and assumed to be representative for merger-like systems (e.g. Downes & Solomon 1998). However, it is unlikely that $\alpha_{\text{CO}}$ follows a bi-modal distribution. Models suggest a smooth transition that depends on the ISM physical properties (e.g. Narayanan et al. 2012).

We exploited the dynamical mass estimate [$M_{\text{dyn}}(R) = \frac{V_r^2 R}{G}$] to constrain the $\alpha_{\text{CO}}$ value. In this procedure, we assumed that
the dynamical mass estimate corresponds to the sum of the stellar, molecular, and dark matter masses (e.g. Motta et al. 2018; Molina et al. 2019b). This is true when looking at the central regions of galaxies. The HI component at larger scales dominates the gas mass, while the ionized gas might have a role as well. Additionally, for the sake of simplicity, we also assumed a constant $\alpha_{\text{CO}}$ value across each galactic disc. Therefore, by quantifying the dark matter content in terms of the dark matter fraction ($f_{\text{DM}}$) at each galactocentric radius, we obtain the following constraint:

$$f_{\text{DM}}(R) = 1 - \frac{M_*(R) + \alpha_{\text{CO}} L_{\text{CO}}(R)}{M_{\text{dyn}}(R)}, \quad (4)$$

where the CO luminosities inside each radius are calculated directly from the ALMA observations, and the stellar masses are truncated using the $K$-band Sérsic model profile following Molina et al. (2019b).

To estimate the dynamical mass values and use Eq. (4), we first needed to calculate the circular velocity $V_{\text{circ}}$ at each galactocentric radius. To do this, we considered two cases, the thin- and thick-disc hydrostatic equilibrium approximations. In the first case, the galaxy support against self-gravity is assumed to be purely rotational, and $V_{\text{circ}}$ corresponds to the observed rotational velocity ($V_{\text{circ}} = V_{\text{rot,CO}}$, Genzel et al. 2015). In the second case, the galaxy scale height cannot be neglected, and the self-gravity is balanced by the joint support between the rotational motions and the pressure gradient across the galactic disc (Burkert et al. 2010).

In this “thick-disc” approximation, an analytic expression for $V_{\text{circ}}$ can be derived by parameterizing the pressure gradients in terms of $\sigma_r$, which is assumed to be constant across the galactic height and radius) and the mass distribution, which we assumed followed the best-fit Sérsic model of the $K$-band surface brightness distribution:

$$V_{\text{circ}}^2(R) = V_{\text{rot,CO}}^2(R) + 2 \frac{\sigma_r^2 b_{r,s}}{n_S} \left( \frac{R}{R_{1/2,K}} \right)^{(1/n_S)}, \quad (5)$$

where $V_{\text{rot,CO}}(R)$ is the rotation velocity profile (Fig. 4) and $b_{r,s}$ is the Sérsic coefficient that sets $R_{1/2,K}$ as the $K$-band half-light radius (e.g. Burkert et al. 2016; Lang et al. 2017; Molina et al. 2019a).

**Table 5.** CO-to-H$_2$ conversion factor, molecular gas masses, and gas fractions for HATLAS114625 and HATLAS121446 starbursts.

<table>
<thead>
<tr>
<th></th>
<th>HATLAS114625</th>
<th>HATLAS121446</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha_{\text{CO}} M_\odot (K \text{ km s}^{-1} \text{pc}^2)^{-1}$</td>
<td>$0.7^{+0.3}_{-0.5}$</td>
<td>$1.2^{+1.0}_{-0.6}$</td>
</tr>
<tr>
<td>$M_{\text{HI}} \times 10^4 M_\odot$</td>
<td>$6.0^{+4.3}_{-2.6}$</td>
<td>$10.3^{+8.7}_{-5.3}$</td>
</tr>
<tr>
<td>$f_{\text{H}_2}$</td>
<td>$0.11^{+0.07}_{-0.05}$</td>
<td>$0.14^{+0.10}_{-0.07}$</td>
</tr>
</tbody>
</table>

The disc radial coordinates are determined by the best-fit two-dimensional model. Additionally, to minimize beam-smearing effects, we only considered the $V_{\text{rot,CO}}$ values extracted from a zone beyond three times the synthesized beam FWHM from the dynamical centre (see “$\sigma_r$” panels in Fig. 3). However, as we still expected some residual beam-smearing effect at these radii, we also applied a correction factor ($\leq 10\%$) to the rotation velocity values based on the ratio between the intrinsic-to-smoothed best-fit arctan velocity models across the galaxy major kinematic axis (Appendix D).

We note that this method suffers from a degeneracy between the $\alpha_{\text{CO}}$ and $f_{\text{DM}}(R)$ parameters; along with it, there is a strong dependence on the accuracy of the $M_{\text{dyn}}$ and $M_*$ values. To try to overcome these issues, we used the Markov chain Monte Carlo (MCMC) technique (Calistro Rivera et al. 2018; Molina et al. 2019b) implemented in EMCEE (Foreman-Mackey et al. 2013). We estimated the posterior probability density function (PDF) for the CO-to-H$_2$ conversion factor and the dark matter fraction parameters by sampling the $\alpha_{\text{CO}} - f_{\text{DM}}(R)$ phase-space defined in Eq. (4) and by considering the likelihood of the estimated $L_{\text{CO}}^\prime$, $M_{\text{dyn}}$, and $M_*$ values.

In addition to the thin- and thick-disc dynamical model assumptions, we explored the effect of the chosen underlying mass distribution by assuming that the galaxies follow an exponential total-mass surface density distribution (Freeman 1970). We note that this assumption produces a variation in our thick-disc $M_{\text{dyn}}$ and truncated $M_*$ estimates. Thus, we employed a total of four different dynamical models per galaxy.

We did not derive an $\alpha_{\text{CO}}$ value for the HATLAS090750 system. This is because this ongoing merger may not fulfill the virial assumption necessary to obtain a dynamical mass estimate.

In Fig. 5, we show the $\alpha_{\text{CO}}$ posterior PDFs for the HATLAS114750 and HATLAS121664 starbursts. We note that the
thick-disc Sérsic mass-profile model suggests slightly higher $\alpha_{\text{CO}}$ values than the other three models for both galaxies. This is produced by two effects; (1) the additional pressure gradient support against self-gravity, which is low for our galaxies as suggested by the $V_{\text{rot,CO}}/\sigma_{\text{CO}} \sim 7$ ratios; and (2) surface density profiles steeper than the ones derived from an exponential model profile as indicated by the Sérsic indices $n_\delta \gtrsim 1$. This tends to increase the $M_{\text{dyn}}$ values by a larger amount compared to the truncated $M_*$ values at smaller galactocentric radii.

We note that a possible systematic overestimation of $M_*$ by MAGPHYS may bias the $\alpha_{\text{CO}}$ estimates towards lower values than the reported ones. This scenario is unlikely as we have input a large wavelength SED coverage ($\gtrsim 3\sigma$ range) to obtain accurate $M_*$ values (see also Michałowski et al. 2014). However, to be conservative, we assumed the $\alpha_{\text{CO}}$ upper limit values ($\alpha_{\text{CO,uplim}}$) given by the PDFs $3\sigma$ range. We obtain $\alpha_{\text{CO,uplim}} = 2.7$ and $5.1 M_\odot (\text{K km s}^{-1} \text{pc}^2)^{-1}$ for HATLAS114625 and HATLAS121446, respectively.

In the remainder of this work, we estimate the molecular gas masses by adopting the median CO-to-H$_2$ conversion factor value derived from the thick-disc Sérsic mass-profile dynamical model, that is, by considering the model that suggests the higher median $\alpha_{\text{CO}}$ value. This election does not affect our results as the differences between the four dynamical models are marginal compared to the uncertainties behind the galaxy estimates as seen by the broad $\alpha_{\text{CO}}$ PDFs. Our analysis suggests low $\alpha_{\text{CO}}$ values that are consistent with the ULIRG-like value for both starbursts. We present this value along with the molecular gas estimates in Table 5.

A direct result of adopting that $\alpha_{\text{CO}}$ value is that our early expectation about observing gas-rich systems was wrong. Indeed, the measured $h_{\text{HI}}$ values are consistent with the average estimate for local SFGs ($h_{\text{HI}} \sim 0.1$, Leroy et al. 2009; Saintonge et al. 2017). This suggests that these starburst galaxies may not be gas-rich, as originally expected, implying that without a robust molecular gas estimate, it is not straightforward to catalogue these systems as possible analogues of the high-$z$ SFG population.

4. Discussion

4.1. What sets the molecular gas velocity dispersions?

HATLAS114625 and HATLAS121446 present $\sigma_{\text{v,CO}}$ values that are comparable with the lower end estimates observed in ULIRGs ($\sigma_{\text{v,CO}} \approx 30$–140 km s$^{-1}$, Downes & Solomon 1998; Wilson et al. 2019). However, both galaxies show regular disc-like kinematics with little evidence of interactions that may enhance the internal $\sigma_{\text{v,CO}}$ values, suggesting that the high molecular gas velocity dispersion values may be produced by internal secular processes.

Wilson et al. (2019) found that, in ULIRGs, the $\sigma_{\text{v,CO}}$ values roughly increase with the molecular surface density ($\Sigma_{\text{HI}}$), following a power-law relationship with a tentative exponent of $\sim 0.5$. Wilson et al. (2019) suggested that this correlation can be explained if ULIRGs are in vertical pressure balance. In this section, we explore whether or not their model is able to explain the $\sigma_{\text{v,CO}}$ values measured for the HATLAS114625 and HATLAS121446 galaxies. We chose the ISM pressure balance model from Wilson et al. (2019) because we lack the stellar velocity dispersion measurement for our sources. This quantity is required to calculate the pressure set by self-gravity in other ISM models such as, for example, the traditional Elmegreen (1989) ISM model.

In the Wilson et al. (2019) model, a downwards pressure on the molecular gas (modelled as a gas layer) is produced by the disc self-gravity plus an additional contribution from the dark matter halo. This pressure can be calculated as:

$$P_{\text{grav,W+19}} = 0.5\pi G \Sigma_{\text{HI}} \Sigma_{\text{tot}} (1 + \gamma),$$

where $\Sigma_{\text{HI}}$ is the disc total-mass surface density and $\gamma$ is a factor that accounts for the vertical pull towards the galaxy midplane produced by dark matter. This factor depends inversely on $V_{\text{rot}}/\sigma_*$ squared, thus it contributes a small correction for both galaxies ($\gamma \sim 0.05$).

The upwards pressure is parameterized as a function of the average mid-plane density $\rho_{\text{mid}}$ and the thermal plus turbulent velocity dispersions:

$$P_{\text{ISM}} = \rho_{\text{mid}} \sigma_{v,\text{HI}}^2 (1 + \psi) = \frac{\Sigma_{\text{HI}} \sigma_{v,\text{HI}}^2 (1 + \psi)}{2 h_{\text{HI}}},$$

where $\rho_{\text{mid}} = \Sigma_{\text{HI}}/2h_{\text{HI}}$, $h_{\text{HI}}$ is the molecular gas disc scale height, $\sigma_{v,\text{HI}}$ is the molecular gas velocity dispersion (hereafter we assume $\sigma_{v,\text{HI}} = \sigma_{\text{v,CO}}$), and $\psi$ is a factor that accounts principally for the magnetic-to-thermal support ratio ($\sim 0.3$, Kim & Ostriker 2015) as the cosmic ray-to-turbulent support ratio is negligible (see Wilson et al. 2019 for more details).

The vertical equilibrium condition requires $P_{\text{grav,W+19}} = P_{\text{ISM}}$ and allows us to write Eq. (6) from Wilson et al. (2019) in a more compact form:

$$h_{\text{HI}} = \frac{\sigma_{v,\text{CO}}^2}{\pi G \Sigma_{\text{tot}}} \times \left(\frac{1 + \psi}{1 + \gamma}\right).$$

From this equation, if galaxies have similar $\Sigma_{\text{HI}}/\Sigma_{\text{tot}}$ ratios, then $\sigma_{v,\text{CO}} \propto \Sigma_{\text{HI}}^{0.5}$, and $h_{\text{HI}}$ is constant across the galactic radius, that is, the correlation found by Wilson et al. (2019) for local ULIRGs.

In the left-hand panel of Fig. 6, we plot the pixel-by-pixel $\sigma_{\text{v,CO}}$ values as a function of $\Sigma_{\text{HI}}$ (corrected by projection effects) for HATLAS114625 and HATLAS121446. All the values associated with the pixels that reside inside the central galactic region$^4$ are shown in grey, highlighting that these $\sigma_{\text{v,CO}}$ values are likely to be overestimated due to beam-smearing residual effects.

We also show the values presented by Wilson et al. (2019) for the local ULIRG sample (measured at 450–650 pc scales) and the average galactic values for a sub-sample of 17 SFGs taken from the EDGE-CALIFA survey (Bolatto et al. 2017). For these SFGs, the $\sigma_{\text{v,CO}}$ values are taken from Levy et al. (2018), whereas the average $\Sigma_{\text{HI}}$ values are calculated by using the $M_{\text{HI}}$ and $R_{1/2,\text{CO}}$ estimates presented in Bolatto et al. (2017) and assuming a radial spatial extension of $2 \times R_{1/2,\text{CO}}$. The “$\sim 1.5$” SFG data correspond to ~kpc-scale measurements for a main-sequence galaxy presented in Molina et al. (2019b).

Despite comparing data observed at different spatial resolutions, both starbursts exhibit $\sigma_{\text{v,CO}}$ values mainly in the range between the local SFGs and ULIRGs, but their ~kpc-scale $\Sigma_{\text{HI}}$ values are comparable to the average estimates measured for the local SFGs and much lower than the estimates reported for the ULIRG sample. However, similar to the ULIRGs, the starburst data seem to follow a roughly $\sigma_{\text{v,CO}} \propto \Sigma_{\text{HI}}^{0.5}$ power-law relationship. This is shown by the dashed line that represents the pressure balance model suggested by Wilson et al. (2019) but scaled

$^4$ Defined as the region within three times the synthesized beam size from the best-fit galactic dynamical centre (see Fig. 3).
to the average $\Sigma_{H_2}/\Sigma_{\text{tot}}$ and $V_{\text{rot}, CO}/\sigma_{\text{CO}}$ ratios measured for both systems. Additionally, the solid line shows the Wilson et al. (2019) model for the local ULIRGs.

We now consider the total surface density $\Sigma_{\text{tot}}$ (Fig. 6). We approximated $\Sigma_{\text{tot}}$ by the sum of $\Sigma_{H_2}$ and the stellar surface density $\Sigma_{*}$, $(\Sigma_{\text{tot}} \equiv \Sigma_{H_2} + \Sigma_{*})$. For each starburst, the pixel-by-pixel $\Sigma_{*}$ values were calculated by scaling the SINFONI $K$-band continuum image surface brightness distribution (Fig. E.1) to the global $M_{*}$ value derived by MAGPHYS.

The HATLAS114625 and HATLAS121446 starbursts tend to be located in the lower $\Sigma_{\text{tot}}$ limit covered by the ULIRG sample. Despite of the large scatter ($\pm 0.22$ dex for non-masked values), the vertical pressure balance model (solid line) gives a reasonable representation of the data. We note that the systematic uncertainty added by the adopted $\alpha_{CO}$ conversion factor is low since the $\Sigma_{\text{tot}}$ values are mainly dictated by $\Sigma_{*}$ in both starbursts (sources have low integrated molecular gas fractions; see Table 5). The scatter is probably increased by the use of a constant mass-to-light ratio to estimate $\Sigma_{*}$.

By using Eq. (8), we roughly estimated $h_{H_2}$ for both starbursts. We plot the $h_{H_2}$ pixel-by-pixel distribution in the right-hand panel of Fig. 6. From the non-masked pixels, we obtain $h_{H_2} \sim 200^{+250}_{-130}$ and $160^{+570}_{-40}$ pc median values for HATLAS114625 and HATLAS121446, respectively. Those values are consistent with the average estimate reported for the ULIRG systems ($\sim 150$ pc; Wilson et al. 2019). Our data support the scenario in which the molecular gas velocity dispersion on large scales ($\sim$ kpc-scales) is set by the local gravitational potential of the galaxy through the reaching of the vertical pressure balance as suggested by Wilson et al. (2019).

We note that the main difference between the two starbursts analysed in this work and the ULIRGs presented by Wilson et al. (2019) is that, in the former, the vertical gravitational pressure is mainly dictated by the stellar component ($h_{H_2} \sim 0.1$) and not by a nearly equal gravitational contribution from stars and gas. Indeed, if in Eq. (6) we take the approximation $\Sigma_{\text{tot}} \sim \Sigma_{*}$ and we assume vertical pressure equilibrium, then we obtain $\sigma_{\text{CO}} \propto \Sigma_{*}^{0.5}$, suggesting that, even in starburst systems, the molecular gas dynamical properties can be set by the stellar gravity.

Momentum injected by stellar feedback may be insufficient to produce the observed $\sigma_{\text{CO}}/\Sigma_{\text{tot}}$ trend. Hydrodynamical simulations suggest that stellar feedback can only account for $\sigma_{\text{CO}}$ values up to $\sim 6-10$ km s$^{-1}$ for the diffuse gas component and that the $\sigma_{\text{CO}}$ values increase moderately with respect to gas surface density (Ostriker & Shetty 2011; Shetty & Ostriker 2012). However, our data sample the $\sigma_{\text{CO}} \gtrsim 15$ km s$^{-1}$ range, and additional pressure sources, such as stellar feedback, may still set the $\sigma_{\text{CO}}$ values below this limit.

Resolution effects should be present as our $\sim$ kpc-scale measurements may underestimate the ambient pressure at smaller scales. This effect has been measured recently by high-resolution ($\sim 60$ pc) molecular gas observations in nearby galaxies (Sun et al. 2020). Indeed, Sun et al. (2020) suggest a correction for the $\sim$ kpc-scale pressure estimates. However, their observations cover a considerably lower Galactic pressure range ($\sim 10^{5.5} \text{ kPa}$), see Fig. 5) and, thus, extrapolating such a correction and applying it to our measurements is uncertain. Nevertheless, these high-resolution observations also suggest that the molecular gas is in pressure balance with its weight and the local ISM self-gravity (see also Schruba et al. 2019).

Another major caveat in our analysis comes from the assumption behind Eq. (6). This equation corresponds to a corrected form of the Spitzer (1942) formula for an isothermal layer embedded in a spherical mass component. It does not consider a multi-component composition of the ISM and may not be appropriate to describe the vertical pressure produced by a gaseous plus stellar ISM. For example, in the traditional Elmegreen (1989) ISM pressure formula, the $\Sigma_{*}$ term is weighted by the ratio between the molecular-to-stellar velocity dispersions $(s \equiv \sigma_{\text{CO}}/\sigma_{*})$.

In this case, the additional vertical pressure set by $\Sigma_{*}$ can be neglected in the limit $s \ll 1$. Only if $s \sim 1$ is Eq. (6) recovered. Thus, Eq. (6) should be considered as an upper limit case of the Elmegreen (1989) formula.

$5$ Compared to Eq. (6), $\Sigma_{\text{tot}}$ is replaced by $[\Sigma_{H_2} + s \Sigma_{*}]$ and $y = 0$. 

Fig. 6. Left: pixel-by-pixel molecular gas velocity dispersion estimates as a function of molecular gas surface density. For each starburst galaxy, in grey, we show the $\sigma_{\text{CO}}$ values that may be overestimated due to beam-smearing residual effects. The errorbar in the lower-right corner indicates the typical 1-$\sigma$ uncertainty, whereas the arrow represents the systematic uncertainty given by the use of our $\alpha_{CO}$ upper limit instead of the adopted value. The “$z \sim 0$ ULIRGs” sample is taken from Wilson et al. (2019). The “$z \sim 0$ SFGs” sample estimates are galactic average values measured for a sub-sample of galaxies taken from the CARMA-EDGE survey (Bolatto et al. 2017; Levy et al. 2018). The “$z \sim 1.5$ SFGs” data correspond to the $\sim$ kpc-scale measurements for a main-sequence galaxy presented in Molina et al. (2019b). The solid line represents the empirical relationship suggested by Wilson et al. (2019). The dashed line shows the empirical relationship corrected by the average $\Sigma_{\text{Mg}}/\Sigma_{\text{tot}}$ and $V_{\text{rot}, CO}/\sigma_{\text{CO}}$ ratios measured for both systems. Middle: pixel-by-pixel $\alpha_{\text{CO}}$ values as a function of the total surface density. Right: molecular gas scale height as a function of the total gas surface density. The last two panels are colour-coded in the same way as the left panel. The vertical pressure equilibrium model gives a reasonable representation of our data.
4.2. The star-formation activity traced at ~kpc-scales

Our CO(1–0) and Paα observations are ideal for studying the star-formation activity in dusty starburst galaxies. The CO(1–0) emission provides a direct estimate of the molecular gas mass (albeit an αCO), and Paα does not suffer from significant extinction (compared to Hα), facilitating a direct view to the star-formation activity in dusty environments.

The star-formation activity can be described as a power-law relationship between the SFR surface density (ΣSFR) and total gas surface density (Σgas) or ΣHI, the well-known Kennicutt-Schmidt relationship (Kennicutt 1998a). For typical local SFGs, when ΣHI is used, it is well characterized by a linear relation with an observed average molecular gas depletion time τdep ≡ ΣHI/ΣSFR = 2.2 ± 0.3 Gyr (Leroy et al. 2013). However, this linear trend seems not to be followed by galaxies with enhanced SFRs as those tend to exhibit shorter molecular gas depletion times or higher star-formation efficiencies (SFE ≡ τ−1 dep, e.g. Daddi et al. 2010).

In Fig. 7, we show the pixel-by-pixel distribution in the ΣSFR–ΣHI plane for HATLAS114625 and HATLAS121446. The ΣSFR and ΣHI quantities are directly estimated from the spatially resolved SINFONI and ALMA observations, assuming the median αCO value (Table 5) and employing the dynamical modelling to correct for projection effects.

We used the HASTROM task written in the Interactive Data Language (IDL) to register the images on the same pixel scales and orientation. While implementing this routine, we considered that the total flux is conserved in each map. We preferred not to include the HATLAS090750 system in our analysis due to its complex geometry and uncertain αCO value.

We compared our ΣSFR–ΣHI estimates with ~kpc-scale local galaxy measurements and the ~sub-kpc data from local ULIRGs. Briefly, the ~kpc-scale data are represented by the median trend reported from the HERA CO-Line Extragalactic Survey (HERACLES, Leroy et al. 2008) for normal star-forming systems and measurements from two LIRGs (NGC 3110 and NGC 232; Espada et al. 2018). The local ULIRG data correspond to the CO(1–0)-based ~350–650 pc-scale estimates presented in Wilson et al. (2019).

The two galaxies presented in this work exhibit τdep values in the range of ~0.1–1 Gyr, that is, τdep values comparable to those derived for ULIRGs (τdep ≤ 0.1 Gyr) but in a low ΣHI environment. The τdep internal galactic trends are not clear due to the considerable data scatter.

If we assume our αCOatom estimates, we obtain τdep median values of ~0.5 and 0.6 Gyr for HATLAS114625 and HATLAS121446, respectively. In this case, both starbursts mainly present τdep values within 0.2–2.2 Gyr, a range similar to that reported for the two local LIRGs (0.2–1.6 Gyr; Espada et al. 2018). In any case, the depletion times estimated for both galaxies are lower than the τdep median values reported for local SFGs with similar ΣHI and fHI values (Leroy et al. 2013). This suggests that the enhancement of the SFE seen in starburst galaxies may not be only related to high ΣHI estimates.

4.3. Pressure regulated star-formation activity

If star-formation activity also depends on the dynamics of the molecular gas, then ΣSFR should also correlate with the physical variables that regulate these properties. Thus, if the vertical pressure equilibrium sets the molecular gas properties on
Our data clearly fill the gap between the ULIRG the PHANGS data in terms of pressure set by self-gravity. We find that $\Sigma_{\text{SFR}}$ is correlated with $P_{\text{grav}}$ across nearly seven and six orders of magnitude in terms of $P_{\text{grav}}$ and $\Sigma_{\text{SFR}}$, respectively.

By performing a linear fit in the log-log parameter space ($\log_{10}(\Sigma_{\text{SFR}}) = N \times \log_{10}(P_{\text{grav}}/P_{\odot})$) using EMCEE (Foreman-Mackey et al. 2013), we find a best-fit slope $N = 0.78 \pm 0.01$ with an intercept value $\log_{10}(P_{\odot}/k_{\text{B}}[\text{cm}^{-3}\text{K}]) = 5.38 \pm 0.04$. This is represented by the red solid line in Fig. 8. In this fitting procedure, we adopted conservative 0.2 dex uncertainties for the PHANGS data estimates (Sun et al. 2020), and we have not included the THINGS sample as we lack measured uncertainties for those data. Nevertheless, the THINGS data are in rough agreement with the best-fit trend. We note that we have included the $\sim 1.5$ SFG data, but the exclusion of these data only produced a slight variation of the best-fit results ($N = 0.80 \pm 0.01$, $\log_{10}(P_{\odot}/k_{\text{B}}[\text{cm}^{-3}\text{K}]) = 5.57 \pm 0.02$).

Our best-fit estimates agree within 1-$\sigma$ uncertainty with the values reported for the DYNAMO (Fisher et al. 2019) and THINGS data ($N = 0.76 \pm 0.06$, $\log_{10}(P_{\odot}/k_{\text{B}}[\text{cm}^{-3}\text{K}]) = 5.89 \pm 0.35$). However, we find that the Fisher et al. (2019) best fit is offset from the kpc-scale data by $\sim 0.5$ dex, suggesting that their result was probably affected by the assumptions behind using unresolved CO data. Sun et al. (2020) report $N = 0.84 \pm 0.01$ and $\log_{10}(P_{\odot}/k_{\text{B}}[\text{cm}^{-3}\text{K}]) = 5.85 \pm 0.01$ best-fit estimates for the PHANGS data, but they caution that their best-fit uncertainties may be underestimated due to not considering systematic errors. This problem may be affecting our uncertainty estimates as well.

To compare our results with theirs, we estimated the rms of the best-fit residuals. We measured $r_{\text{rms}} = 0.34$ and $0.36$ dex from our best fits and the Sun et al. (2020) best fits, respectively. We note that these values are considerably increased by considering the $\sim 1.5$ SFG data. However, these data seem to be an outlier compared to the other kpc-scale measurements, and, perhaps, the discrepancy is produced by an underestimated dust extinction correction applied to the observed SFR for this system. If we do not consider the $\sim 1.5$ SFG data, we find $r_{\text{rms}} = 0.25$ dex from both best-fit residuals. Thus, in both cases, we obtain a good agreement between our results and the Sun et al. (2020) results.

The stellar-feedback regulated model predicts a $\Sigma_{\text{SFR}}$ and ISM pressure correlation with a slope close to unity (Ostriker & Shetty 2011). In this model, stellar feedback (e.g. photonization, radiation, supernovae, winds) heats the ISM gas while the energy and pressure losses occur via turbulent dissipation and cooling. The star-formation activity gives pressure support against self-gravity (hence, $P_{\text{ISM}} = P_{\text{grav}}$). $\Sigma_{\text{SFR}}$ and $P_{\text{ISM}}$ are closely related due to a nearly constant injected feedback momentum per stellar mass formed: $p_\star/\Sigma_{\text{ISM}} = 4(p_\star/\Sigma_{\text{SFR}})^{-1} P_{\text{ISM}}$; e.g. Ostriker et al. 2010; Ostriker & Shetty 2011; Shetty & Ostriker 2012).

This is highlighted by the dot-dashed line in Fig. 8, which represents the best-fit power law ($N \approx 1.1$) for the hydrodynamical simulations presented in Kim et al. (2013). This power law overestimates the ISM pressure for the ULIRG systems. However, those systems display larger $\Sigma_{\text{SFR}}$ values than that covered by the simulations ($\Sigma_{\text{SFR}}^{\text{sim}} \lesssim 10^{-2} M_{\odot} \text{yr}^{-1} \text{kpc}^{-2}$; Kim et al. 2013).

To further test the plausibility of $\Sigma_{\text{SFR}} \propto P_{\text{grav}}$, we fitted a linear function to our data. We obtain a best-fit intercept value $\log_{10}(P_{\odot}/k_{\text{B}}[\text{cm}^{-3}\text{K}]) = 6.74 \pm 0.01$ (we caution that the uncertainty may be underestimated due to systematic errors) and a residual rms of $\approx 0.47$ or $\approx 0.31$ dex depending on whether we include the $\sim 1.5$ SFG data or not. The rms values are slightly larger scales ($\sim$kpc-scales, Sect. 4.1), then $\Sigma_{\text{SFR}}$ should correlate with the ISM pressure set by self-gravity $P_{\text{grav}}$. The correlation between $\Sigma_{\text{SFR}}$ and ISM pressure has been suggested and observed previously by many authors (e.g. Genzel et al. 2010; Ostriker et al. 2010; Ostriker & Shetty 2011; Bolatto et al. 2017; Herrera-Camus et al. 2017; Fisher et al. 2019) and also used to explain the so-called extended Kennicutt-Schmidt relation (Shi et al. 2011). Indeed, the mid-plane hydrostatic pressure seems to predict the SFE better than gas surface density in atomic-dominated regimes (Leroy et al. 2008).

In Fig. 8, we show $\Sigma_{\text{SFR}}$ as a function $P_{\text{grav}}$. The Physics at High Angular resolution in Nearby Galaxies (PHANGS; Leroy et al., in prep.) data correspond to measurements from 28 nearby galaxies presented in Sun et al. (2020) and artificially convolved to a kpc-scale by them. We also consider the spatially resolved ULIRG data presented in Wilson et al. (2019) and The Hi Nearby Galaxy Survey (THINGS; Walter et al. 2008; de Blok et al. 2008) and DYNAMO (Green et al. 2014) galactic averages presented in Fisher et al. (2019). We caution, however, that the DYNAMO pressure data are based on ionized gas velocity dispersions and unresolved CO emission line measurements, while we are using spatially resolved molecular gas estimates. We also show the $\sim$kpc-scale data measured for a typical SFG at $z \sim 1.5$ (Molina et al. 2019b).
higher than the reported estimates from our previous best fit. The intercep-ter value translates to $p_*/m_*=\sim4600\,\text{km}\,\text{s}^{-1}$, a value that is $\sim1.5$ times higher than the estimate typically adopted for single supernova feedback ($\sim3000\,\text{km}\,\text{s}^{-1}$; e.g. Thornton et al. 1998; Martizzi et al. 2015; Ostriker & Shetty 2011; Kim & Ostriker 2015). Enhanced feedback from clustered supernovae may be needed to explain such a $p_*/m_*$ value (e.g. Sharma et al. 2014; Gentry et al. 2017; Kim et al. 2017). However its effective-ness is still under debate (Gentry et al. 2019).

Additional energy sources that regulate the star-formation activity should also be considered. Mass transport through the galactic disc could be such a source (e.g. Krumholz et al. 2018). Nevertheless, this may require understanding how the gas dissi-pates the gravitational energy from larger scales towards smaller scales (e.g. Bournaud et al. 2010; Combes et al. 2012).

Our observations suggest that, in our dusty starburst galaxies, the molecular gas properties seem to be regulated by the pressure set by self-gravity (Sect. 4.1). Therefore, one possibility is that the gravitational instabilities may induce large-scale gas motions that then are dissipated through energy cascades towards small scales (e.g. Bournaud et al. 2010; Combes et al. 2012) until the range where stellar feedback operates and stops the local grav-itational collapse through momentum and/or energy injection. In this picture, the observed star-formation activity occurs as a response to the ISM pressure balance.

It is also worth mentioning that Sun et al. (2020) calculated $P_{\text{grav}}$ by using the “dynamical equilibrium pressure” ($P_{\text{DE}}$ e.g. Elmegreen 1989; Wong & Blitz 2002; Ostriker et al. 2010; Ostriker & Shetty 2011; Fisher et al. 2019), which accounts for the gas and stellar galaxy self-gravity in the limit in which the gas disc scale height ($h_{\text{gas}}$) is much smaller than the stellar disc scale height ($h_*$; Benincasa et al. 2016). They neglected the grav-itational pressure set by the dark matter component as this pres-sure source is small in the galaxies they analysed. This is also the case for our galaxies and the ULIRGs presented in Wilson et al. (2019). We determined $P_{\text{grav}}$ by using Eq. (6). This equation corresponds to a $P_{\text{DE}}$ upper limit case where $h_{\text{gas}}\sim h_*$ (see Appendix A of Benincasa et al. 2016). Thus, a possible correction to our $P_{\text{grav}}$ estimates may lead to a steeper $\Sigma_{\text{SFR}}^{-1}P_{\text{grav}}$ correlation.

Another possible source of uncertainty comes from the limited spatial resolution of our observations. Due to the beam-smearing effect, $\Sigma_{\text{SFR}}$ and $\Sigma_{\text{H}_2}$ (hence, $P_{\text{grav}}$) are average $\sim$kpc-scale estimates of the patchy underlying surface density distributions. This artificial dilution effect is quantified for the PHANGS molecular gas data (see Sun et al. 2020 for more details); however, it is unknown for the starburst galaxy popula-tion where the ISM is denser. Higher spatial resolution observa-tions ($\sim10$--$100\,\text{pc}$) may be needed to quantify this.

### 4.4. Limitations of our dynamical mass approach

One of the stronger constraints for the dynamical modelling is given by the assumption of a constant CO-to-H$_2$ conversion fac-tor across the galactic disc. This may not be an ideal assumption due to possible $\alpha_{\text{CO}}$ variation with the galactocentric radius (e.g. Sandstrom et al. 2013). Indeed, lower $\alpha_{\text{CO}}$ values are likely to be measured towards the centre of the Galaxy (Bolatto et al. 2013). Based on dynamical mass modelling, determining an $\alpha_{\text{CO}}$ radial variation is highly uncertain due to the unconstrained dark matter fraction values. We need to assume a halo model. However, we cannot accurately constrain the halo properties as the observed rotation curves do not extend more than $\sim6\,\text{kpc}$ away from the galactic centre (Fig. 4). A constant $\alpha_{\text{CO}}$ assumption is reasonable given our data limitations.

The dynamical interpretation is mainly limited by the degen-eracy between $\alpha_{\text{CO}}$ and $f_{\text{DM}}$ values constrained at the inner galactocentric radius considered in each galaxy ($R\approx2.3\,\text{kpc}$, Fig. 4). The (over-)underestimation of $f_{\text{DM}}$ at this radius will bias our result towards (lower) higher $\alpha_{\text{CO}}$ estimates. In the event that we are underestimating $f_{\text{DM}}$, then the median $\alpha_{\text{CO}}$ values should be considered as an upper limit of the true values, implying that both starburst galaxies might have lower molecular gas masses and may have $\alpha_{\text{CO}}$ values even lower than those reported for ULIRGs.

On the other hand, a possible overestimation of the $f_{\text{DM}}$ does not affect our results. If we assume the limit case that there is no dark matter, then the median $\alpha_{\text{CO}}$ values increase by $\lesssim14\%$ compared to these estimated values when the dark matter content is considered. This variation is smaller than the $1-$σ range of the $\alpha_{\text{CO}}$ PDF, and it is independent of the dynamical mass model assumed (see Fig. 5).

Another limitation comes from the adopted dynamical mass formula. We have not considered any geometrical factor that should multiply the $V_{\text{rot},\text{CO}}$ values in Eq. (5). This is the equiv-alent of the assumption of spherical geometry when calculating enclosed mass estimates from rotational motions. However, this source of uncertainty is not expected to affect our conclusions. For example, the $V_{\text{gas}}$ difference between an exponential disc and the equivalent spherical mass distribution is $\lesssim15\%$, and it highly depends on the disc radius (see Fig. 2.17 in Binney & Tremaine 2008). By adopting this $V_{\text{gas}}$ difference value (translated into the enclosed mass difference), the median $\alpha_{\text{CO}}$ values would increase by $\sim30\%$. Again, this variation is smaller than the estimated $1-$σ range of the $\alpha_{\text{CO}}$ PDF.

The CO($1-0$) emission source is also a concern. From our $\sim$kpc-scale observations, we cannot distinguish between the CO($1-0$) emission originated in giant molecular clouds and any significant molecular gas diffuse emission. This diffuse compo-nent may not be negligible in galaxies (e.g. Goldsmith et al. 2008; Schinnerer et al. 2010), and it is enhanced in dense and high ISM pressure galactic environments (Sandstrom et al. 2013). If the diffuse molecular gas phase dominates the CO($1-0$) emission, then low $\alpha_{\text{CO}}$ values may underestimate the high density molecular gas mass content for both starbursts (Papadopoulos et al. 2012). This effect is highlighted by the difference in the estimated $\alpha_{\text{CO}}$ values between the one- and two-component models for ULIRGs (Fig. 9, see Papadopoulos et al. 2012).

However, it should be noted that molecular gas diffuse emission and its contribution to the estimated $\alpha_{\text{CO}}$ values are uncertain. The CO-to-H$_2$ conversion factor may vary significantly for this gas component depending on local environment properties (e.g. Liszt & Pety 2012). Additional observations tracing the dense molecular gas phase may help to determine whether our $\alpha_{\text{CO}}$ estimations are biased towards low values or not.

We note that we have not considered the H$_2$ content in our dynamical mass approach as we expect a negligible amount of H$_2$ mass within the inner radius ($R\approx2.3\,\text{kpc}$) where $M_{\text{dyn}}$ was calculated. We recall that the $M_{\text{dyn}}$ values calculated at these radii are the ones that strongly constrain the $\alpha_{\text{CO}}$ esti-mates in our procedure. In local spirals, the transition from an H$_2$-dominated ISM to an H$_2$-dominated ISM ($\Sigma_{\text{H}_2}\approx\Sigma_{\text{H}_1}$) occurs at $\Sigma_{\text{gas}}\sim12\pm6\,M_\odot\text{pc}^{-2}$ (Leroy et al. 2008). From the spatially resolved CO($1-0$) observations and the adopted $\alpha_{\text{CO}}$ values, we estimated $\Sigma_{\text{H}_2}\sim146\pm93$ and $127\pm50\,M_\odot\text{pc}^{-2}$ at $R\approx2.3\,\text{kpc}$ for the HATLAS114625 and HATLAS121446 galaxies, which supports our assumption.
Finally, we checked if our $\alpha_{\text{CO}}$ estimates are reasonable given the theoretical expectation (Bolatto et al. 2013). From theories, it is expected that $\alpha_{\text{CO}}$ mainly varies with the system metallicity and total surface density. However, before making any comparison, we note that HATLAS114625 and HATLAS121446 present supra-solar metallicity values in terms of the gas phase oxygen abundance ($12 + \log(O/H) = 8.99$ and 8.72, respectively). We note that, from metallicities equal to or higher than the solar value, we do not expect any significant variation of $\alpha_{\text{CO}}$ due to the high metal content (Bolatto et al. 2013). Thus, we simply assumed a solar metallicity when comparing our estimates with the theoretical prediction in Bolatto et al. (2013). We show this comparison in Fig. 9. We find that the reported median CO-to-H$_2$ values are somewhat lower than the theoretical expectation but still consistent within the scatter. Our $\alpha_{\text{CO}}$ estimates are, therefore, reasonable given the measured $12 + \log(O/H)$ and $\Sigma_{\text{Tot}}$ values for both starbursts.

5. Conclusions

We present new ALMA Cycle-3 and VLT-SINFONI observations tracing the CO(1–0) and Paα emission lines from three starburst galaxies at $z \sim 0.12$–0.18 taken from the VALES survey. The ALMA observations were designed to deliver spatially resolved observations of the molecular gas content at $\sim0''5$, that is, approximately the resolution of the seeing-limited SINFONI observations ($\sim0''4$–0''8). Combining near-IR and sub-mm observations, we study the ionized and molecular gas dynamics at $\sim$kpc-scales.

One target, HATLAS090750, presents highly asymmetric morpho-kinematics, suggesting an ongoing merger. From its SINFONI observation, we also detected fainter ro-vibrational warm molecular gas transitions along with an ionized helium line in its central galactic zone. The H$_2$ emission lines were used to determine a warm molecular gas temperature of $\sim1700$±$500$ K (Fig. C.1), which was probably produced by supernova remnant (SNR) shocks. However, we could not discard non-thermal gas excitation sources due to the lack of H$_2$ emission line intensity measurements with different vibrational energy levels (e.g. Davies et al. 2003).

The other two starburst galaxies, HATLAS114625 and HATLAS121446, show disc-like morpho-kinematics, with rotation as the dominant component supporting self-gravity ($V_{\text{rot}}/\sigma_\text{e} \sim 7$–8). For both systems, we model the CO and Paα galactic dynamics, and we aid the kinematic modelling by using $K$-band photometric models to constrain the inclination angle parameter. From those analyses, we find that the CO and Paα dynamics present a good agreement in both galaxies (Fig. 3), as suggested by similar kinematic position angles ($\Delta$PA $\sim 4$ deg) and emission line spatial extensions ($R_{\text{e}/2\text{Paα}}/R_{\text{e}/2\text{CO}} \sim 1$). Our observations suggest that the ionized and molecular gas components display roughly the same galaxy morpho-kinematics.

We estimate the total mass budget for both the HATLAS114625 and HATLAS121446 galaxies by calculating the dynamical masses assuming the thin- and thick-disc hydrostatic equilibrium approximations (Burkert et al. 2010) along with two different surface density profile models. We obtain $\alpha_{\text{CO}}$ values in the range of $0.7$–$1.2 M_{\odot}/(\text{K} \text{km}^\text{s}^{-1} \text{pc}^{-2})^{-1}$ for both galaxies (Fig. 5), that is, similar values to those reported for ULIRGs (Downes & Solomon 1998). These values do not depend strongly on the hydrostatic equilibrium and total surface density assumptions. Our conversion factor estimates are somewhat lower but still consistent with the $\alpha_{\text{CO}} \propto \Sigma_{\text{Tot}}^{0.5}$ trend suggested from theoretical expectations (Fig. 9, Bolatto et al. 2013).

By adopting the dynamically based $\alpha_{\text{CO}}$ values, we obtain molecular gas fractions of the order of $\sim0.1$ for both starbursts, far below our initial expectations and consistent with values measured in local SFGs. Therefore, the sources are not gas-rich, as initially thought, highlighting the difficulties in estimating molecular gas masses due to the uncertainty of the CO-to-H$_2$ conversion factor.

We find that the HATLAS114625 and HATLAS121446 molecular gas velocity dispersion values are reasonably represented by a $\sigma_{\text{e}/\text{CO}} \propto \Sigma_{\text{Tot}}^{0.5}$ trend, where $\Sigma_{\text{Tot}}$ is the total galaxy surface density (Fig. 6). This suggests that the molecular gas velocity dispersion values are consistent with being set by the galaxy self-gravity to maintain the vertical pressure balance.

We study the star-formation activity traced at $\sim$kpc-scales in the HATLAS114625 and HATLAS121446 starbursts. Both galaxies exhibit $\tau_{\text{dep}}$ values in the range of $\sim0.1$–1 Gyr (Fig. 7), that is, values consistent with the reported estimates for ULIRGs ($\tau_{\text{dep}} \sim 0.1$ Gyr). However, both systems present $\Sigma_{\text{H}_2}$ values that are comparable to those seen in local star-forming disc galaxies (Leroy et al. 2013). This suggests that the decrease in $\tau_{\text{dep}}$ (or enhancement of the SFE) is also produced by additional physical processes that may not only be related to high-$\Sigma_{\text{H}_2}$ environments.

To further explore this, we study the correlation between $\Sigma_{\text{SFR}}$ and the gravitational pressure $P_{\text{grav}}$. HATLAS114625 and HATLAS121446 fill the gap between normal galaxies and ULIRG systems in terms of pressure set by self-gravity. We find a linear relation in the log-log space.

---

6 We base our metallicity estimates on the Pettini & Pagel (2004) calibration scale and the [NII] and H$\alpha$ line intensities reported in Table A.1. We also adopt a solar abundance of $12 + \log(O/H) = 8.69$ (Asplund et al. 2009).
Appendix A: Emission line and WISE colour fluxes

Table A.1. Summary of the emission line and WISE colour fluxes used in this work and taken from the GAMA DR3 (Baldry et al. 2018).

<table>
<thead>
<tr>
<th>Model</th>
<th>HATLAS090750</th>
<th>HATLAS114625</th>
<th>HATLAS121446</th>
</tr>
</thead>
<tbody>
<tr>
<td>f_{Br}(1–0)S(1)</td>
<td>1.04 ± 0.02</td>
<td>0.063 ± 0.005</td>
<td>0.072 ± 0.016</td>
</tr>
<tr>
<td>f_{Br}(1–0)S(2)</td>
<td>0.41 ± 0.03</td>
<td>0.107 ± 0.006</td>
<td>0.028 ± 0.006</td>
</tr>
<tr>
<td>W1 (mJy)</td>
<td>0.35 ± 0.02</td>
<td>0.016 ± 0.006</td>
<td>0.007 ± 0.001</td>
</tr>
<tr>
<td>W2 (mJy)</td>
<td>2.04 ± 0.005</td>
<td>0.005 ± 0.001</td>
<td>0.011 ± 0.006</td>
</tr>
<tr>
<td>W3 (mJy)</td>
<td>6.89 ± 0.41</td>
<td>1.119 ± 0.34</td>
<td>8.65 ± 0.35</td>
</tr>
</tbody>
</table>

Notes. W1, W2, and W3 correspond to the “profile-fit photometry” WISE filter fluxes measured at 3.4, 4.6, and 12 µm (Cluver et al. 2014). The uncertainties indicate 1–σ errors. Our three galaxies are catalogued as unresolved by WISE.

Appendix B: Experimental observation results

We performed an on-source experimental jittering pattern to optimize the S/N of the Paα emission line for HATLAS090750. In this experimental observation, the pointing was kept fixed at the galaxy location. Hence, an OOOO jitter sequence was used. As we do not observe the sky during this observation, the emission and telluric absorption bandpass lines need to be subtracted using sky models. Specifically, we used the SKYCOR and MOLECFIT pipelines. This implies that the performance of this experimental observation is mainly limited by the accuracy of the sky emission modelling and the ability to detect the line emission (S/N ≥ 15; Godoy et al., in prep.).

Figure 2 clearly shows that we were able to detect the targeted emission line (Paα) for this galaxy (S/N = 80). We were also able to observe many other fainter near-IR emission lines (Table C.1) that allowed us to study the conditions of the host molecular gas ISM (Appendix C). Faint tidal features were also detected for this system, demonstrating the ability of this observation to recover the galaxy spatial distribution when compared, for example, to the CO(1–0) observation (Fig. 3). Thus, this experimental observation delivered more information than initially expected and allowed us to study HATLAS090750 in great detail.

Even though we have not provided a reliable flux calibration for HATLAS090750, we note that this was because we were unable to accurately model the telluric standard star (HD 56006) observation. For most of the observed telluric standards, the effective temperature agrees well in the literature with very low dispersion, allowing an appropriate calibration using a black body. However, HD 56006 has very uncertain stellar parameters (e.g. Niemczura et al. 2009; Lefever et al. 2010), making a reliable calibration impossible even in the case when more sophisticated approaches were attempted. We highlight that this problem is only related to this standard star observation. If a flux standard star had been observed, then the OOOO observation flux calibration would have been straightforward. Thus, we conclude that our observational experiment was a success. We recommend adopting this experimental OOOO observational setup when the expected line emission S/N is ~15 or greater.

Appendix C: Near-IR emission lines

Near-IR emission lines are useful for determining the excitation mechanism of the gaseous line-emitting ISM. Similar to the well-established optical diagnostic diagrams (e.g. the BPT diagram), the ratio between star-formation line tracers (e.g. Paα, Paβ) and shock tracers, such as ro-vibrational molecular hydrogen emission lines (e.g. H2(1–0)S(1,2,12.2 µm) or forbidden iron lines ([FeII]11.64 µm), can be used to determine the dominant excitation mechanism (e.g. Larkin et al. 1998; Riffel et al. 2013; Fazeli et al. 2019).

From the central brightest pixels from our SINIFONI K-band observations, we detected more near-IR emission lines than only Paα (Fig. 2). By considering a circular aperture with a radius equal to the PSF FWHM and centred at the galaxy Paα luminosity peak, we measured several other emission lines fluxes (see Table C.1). These values were estimated by fitting a Gaussian function to each emission line in the spatially collapsed spectrum, and the 1–σ uncertainties were derived by bootstrapping via Monte Carlo simulations the flux-density errors. These ratio values were corrected by assuming a Calzetti et al. (2000) attenuation law (A_{Paα} = 0.145A_V, A_{Brγ} = 0.132A_V, A_{HeII} = 0.113A_V, A_{H2(1–0)S(1)} = 0.130A_V, A_{H2(1–0)S(2)} = 0.117A_V, A_{H2(1–0)S(1)} = 0.103A_V). We note that this correction is determined by the shape of the assumed attenuation law.

We could only apply the near-IR emission line analysis to the HATLAS090750 galaxy as we lack enough H2 emission line flux measurements for the other two systems. For this galaxy, we used the Paα flux intensity to differentiate between the possible excitation mechanisms. The other option, the use of the Brγ emission line, was impeded given that this emission line is redshifted out of the SINIFONI K-band wavelength range. This means that the H2(1–0)S(1,2,12.2 µm) line is only related to this standard star observation. If a flux standard star had been observed, then the OOOO observational setup when the expected line emission S/N is ~15 or greater.

Table C.1. Spatially integrated Brγ1.9444 µm, ro-vibrational H2(1–0)S(1,2)1.9575 µm, H2(1–0)S(2,1)0.0233 µm, H2(1–0)S(1,2)1.1222 µm, and Het.0.0588 µm fluxes relative to the Paα emission line flux.

<table>
<thead>
<tr>
<th>HATLAS090750</th>
<th>HATLAS114625</th>
<th>HATLAS121446</th>
</tr>
</thead>
<tbody>
<tr>
<td>Brγ1Paα</td>
<td>0.055 ± 0.002</td>
<td>&lt;0.12</td>
</tr>
<tr>
<td>H2(1–0)S(3)/Paα</td>
<td>0.063 ± 0.005</td>
<td>0.107 ± 0.006</td>
</tr>
<tr>
<td>H2(1–0)S(2)/Paα</td>
<td>0.028 ± 0.006</td>
<td>&lt;0.17</td>
</tr>
<tr>
<td>H2(1–0)S(1)/Paα</td>
<td>0.072 ± 0.016</td>
<td>&lt;0.33</td>
</tr>
<tr>
<td>Het.0.058Paα</td>
<td>0.051 ± 0.006</td>
<td>&lt;0.27</td>
</tr>
</tbody>
</table>

Notes. We note that the H2(1–0)S(1) emission is redshifted out of the SINIFONI K-band wavelength range for the later two galaxies. The upper emission line flux limits are calculated as rms × σ_{Paα,obs}, where the rms values are estimated within a 30 channel spectral window width centred at the expected emission line location in the spectra, and σ_{Paα,obs} is the Paα emission line width.
diagram (Davies et al. 2003). In this diagram, \(N_{v,J}\) is the molecular column density, \(g_{0,J}\) is the statistical weight, and \(E\) is the upper energy level of the ro-vibrational transition. From the \(H_2\) emission line fluxes \(f_{v,J}\), the column densities in the upper ro-vibrational levels are computed as:

\[
N_{v,J} \equiv \left( \frac{4\pi f_{v,J}}{A_v \Omega} \right) \left( \frac{\lambda}{\hbar c} \right),
\]

(C.1)

where \(\Omega\) is the spectrum extraction aperture size, \(A_v\) is the Einstein coefficient computed by Wolniewicz et al. (1998), and \(\lambda/\hbar c\) is the photon energy. Additionally, the \(N_{v,J}/g_{0,J}\) ratios need to be normalized to a specific population distribution value \(N_{v,J}/g_{0,J}\) given from a determined \(H_2\) transition. We normalized them to the inferred value from the \(H_2(1–0)S(3)\) emission line transition (e.g. Bedregal et al. 2009). We note that if the warm molecular gas phase is in local thermodynamic equilibrium (LTE), then the data are well described by a simple linear function that represents a Boltzmann distribution characterized by a single excitation temperature.

In Fig. C.1, we show the excitation diagram. As we lack \(H_2\) emission line intensity measurements with different vibrational energy levels, we can only measure rotational temperature \(T_{rot}\) for the vibrational \(H_2(1–0)\) transition. We find that the data are well fitted by a linear fit with \(T_{rot} \approx 1600 \pm 400\) K, suggesting that the warm \(H_2\) ISM phase in the central brightest zone of this galaxy is in LTE.

This temperature value also suggests that the warm \(H_2\) gas may be mainly heated by SNR shocks (Brand et al. 1989; Oliva et al. 1990), with perhaps some contribution from thermal X-ray heating from SNRs \((T_{rot} \gtrsim 2000\) K, e.g. Draine & Woods 1990). Thermal UV heating is unlikely as models suggest lower temperature values \((T_{rot} \lesssim 1000\) K, Sternberg 1989). However, we stress that we cannot rule out non-thermal UV excitation (e.g. fluorescence; Black & van Dishoeck 1987) as we lack \(H_2\) emission line observations with different vibrational energy levels (Bedregal et al. 2009). Nevertheless, our \(T_{rot}\) estimate is slightly higher than, but still consistent with, the average value \((\langle T_{rot} \rangle \sim 1360 \pm 390\) K) reported for local \((z < 0.08)\) LIRGs (U et al. 2019).

**Appendix D: Beam-smearing effect on the rotation velocity values**

Fig. D.1. Beam-smearing effect on the recovered rotation velocity values across the major kinematic axis for HATLAS114625 (left) and HATLAS121446 (right) galaxies. We mask the values at \(R \leq 0.5\times\) synthesized beam or PSF FWHM due to the highly uncertain estimates and to improve visualization. The colour codes are the same as in Fig. 4. At a radius \(R \gtrsim 1.5\times\) synthesized beam or PSF FWHM from the dynamical centre, we estimate that a moderate correction \((\lesssim10\%)\) needs to be applied to the observed rotation velocity values.

Accurate rotation velocities cannot be derived towards the centres of galaxies due to beam-smearing effects. Rotation velocities tend to be underestimated due to the flux-weighted nature of the data convolution with the PSF and/or synthesized beam. Thus, a beam-smearing correction needs to be applied.

Based on our best-fit two-dimensional models, we quantified the beam-smearing effect on rotation velocities by computing the beam-smeread to intrinsic ARCTAN best-fit velocity model ratio and measured across the galaxies major kinematic axes. We show the estimation of this ratio in Fig. D.1 for the ALMA and VLT-SINFONI observations of the HATLAS114625 and HATLAS121446 galaxies. We find that a moderate beam-smearing correction \((\lesssim10\%)\) needs to be applied to the rotation velocity values measured at a galactocentric radius longer than \(1.5\times\) projected synthesized beam or PSF FWHM. At smaller radii, the beam-smearing effect tends to increase dramatically.

**Appendix E: SINFONI K-band continuum maps**

In Fig. E.1, we show the continuum maps used to calculate the pixel-by-pixel \(\Sigma_\star\) values. These maps are scaled to the respective galaxy \(M_\star\) value, that is, by assuming a constant mass-to-light ratio across the galactic disc.

Fig. E.1. SINFONI K-band continuum maps for HATLAS114625 (left) and HATLAS121446 (right) targets.
Appendix F: Full $\alpha_{CO}$ and dark matter PDFs

Our dynamical mass approach is limited by the degeneracy between $\alpha_{CO}$ and the dark matter fraction $f_{DM}$ variables. Due to our assumption of a constant $\alpha_{CO}$ value across the galactic disc, the dynamical mass value estimated at the innermost galactocentric radius limits the maximum $\alpha_{CO}$ value that can be obtained. At this radius, $f_{DM}$ is consistent with zero, but this does not necessarily hold at longer radii.

In Fig. F.1, we show the $\alpha_{CO}$ and $f_{DM}(R)$ PDFs derived from the “thick-disc plus Sérsic” dynamical mass model, that is, the model that determines the adopted median $\alpha_{CO}$ value in our work. There is no major difference between the $\alpha_{CO}$ PDF obtained from this model and those derived from other dynamical models, as the broad $\alpha_{CO}$ PDF shapes prove (Fig. 5).

The HATLAS114625 galaxy shows a higher increase in $f_{DM}$ as a function of galactocentric radius compared to HATLAS121446, suggesting that baryonic matter is distributed more compactly in the former system. This is consistent with the reported $K$-band Sérsic index value (Table 3) and the steeper velocity gradient that is seen in HATLAS114625 (Fig. 4).

Fig. F.1. Corner plot for $\alpha_{CO}$ and $f_{DM}(R)$ variables for the HATLAS114625 (top) and HATLAS121446 (bottom) starbursts.