Effects versus precession instabilities on the jets of GRS 1758–258

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ABSTRACT

Aims. The prototypical microquasar GRS 1758–258 exhibits large-scale morphological changes in radio maps over time which have been attributed to the rise of instabilities. Here, we investigate whether these effects could be attributed to jet precession instead.

Methods. We used new and archival radio maps to fit a kinematic jet precession model. The value of the parameters thus obtained were analysed in order to get constraints on the physical properties of the GRS 1758–258 system. Their consistency with different theories of the origins for the jet precession, such as Lense–Thirring effect and tidal torques induced by the secondary star, has previously been studied. Alternatively, we also assessed the possibility that observations are compatible with eventual jet instabilities.

Results. The new radio data presented here confirm that the large-scale radio morphology of GRS 1758–258 is changing over time. Our study shows that the 18.48 day period could plausibly be ascribed to precession, thus implying a reinterpretation of assumptions made for the orbital period to date. However, the observed structural changes in radio jets cannot be easily attributed to jet precession according to our analysis. In contrast, the growth of instabilities certainly appears to be a more realistic explanation of these effects.

Key words. instabilities – stars: jets – X-rays: binaries – X-rays: individuals: GRS 1758-258

1. Introduction

GRS 1758–258 is one of the brightest objects seen in hard X-rays in the close vicinity of the Galactic centre. It was first detected by GRANAT/SIGMA (Sunyaev et al. 1991) and since then this system has enjoyed intense observational coverage at these frequencies over decades from CGRO, RXTE, ROSAT, INTEGRAL, ASCA, Swift, Beppo-SAX, EXOSAT, Chandra, and XMM-Newton (i.e. Lin et al. 2000; Mereghetti et al. 1994, 1997; Smith et al. 2002; Main et al. 1999; Keck et al. 2001; Heindl & Smith 2002; Pottschmidt et al. 2006; Goldwurm et al. 2001; Soria et al. 2011). The source appears to exhibit continuous, variable activity at these wavelengths, spending almost all its time in a hard state. The compact object in GRS 1758–258 is probably a black hole as its X-ray spectrum resembles that of the black hole in Cygnus X-1 (Main et al. 1999). All these characteristics have led to consider GRS 1758–258 as a low mass X-ray binary system (LMXB) with a black hole accreting from a stellar companion. Observations in radio wavelengths show two clearly extended lobes, which suggest that GRS 1758–258 is a prototypical microquasar (Rodríguez et al. 1992; Mirabel et al. 1992). However, the Galactic nature of this system has remained elusive with regard to spectroscopic analysis because of crowded stellar fields, astrometric uncertainties, and significant interstellar extinction towards the Galactic Center in optical and infrared wavelengths (Bignami et al. 1991; Mereghetti et al. 1992; Martí et al. 1998; Eikenberry et al. 2001; Rothstein et al. 2002).

Although a weak stellar counterpart of GRS 1758–258 was finally identified (Muñoz-Arjonilla et al. 2010; Luque-Escamilla et al. 2014), it was not possible to obtain any clear spectral signature even using the 10 m Gran Telescopio Canarias (Muñoz-Arjonilla et al. 2010; Martí et al. 2016). Nevertheless, the system was definitively associated to the Milky Way when large-scale morphological changes were noticed by Martí et al. (2015). These variations in radio shape were attributed to instabilities in the jet and interactions with the interstellar medium, conforming a cocoon observed for the first time in a microquasar, which adds a new aspect of similarity with radio galaxies. A deep inspection of the resulting radio S-shape of GRS 1758–258 revealed it to be a downsized mimic of winged extragalactic radio galaxies, which appear to have some consequences for the black hole merger rate and its corresponding gravitational wave production (Martí et al. 2017).

However, instabilities are not the only mechanisms that could explain the large-scale morphology of astrophysical jets. Precession is often invoked to account for the apparent shape of jets both in extragalatic and Galactic sources. In fact, other known microquasars present observational evidence of jet precession, such as SS 433 (Abell & Margon 1979; Hjellming & Johnston 1981), GRO J1655–40 (Hjellming & Rupen 1995), and 1E 1740.7–2942 (Luque-Escamilla et al. 2015), where the evolution of the large-scale morphology of the jet-lobes is evident over time. Since this mechanism seems to be expected in binary systems similar to GRS 1758–258, due to the torque of the donor star (Larwood 1998) or the relativistic drag from the spinning compact object through Lens-Thirring effect (Bardeen & Petterson 1975), in this paper, we study the possibility that it could be responsible for the changing large-scale radio morphology appearing in GRS 1758–258 at different epochs. In Sect. 2, we show the data and methods used for fitting the radio jet-lobes changing structures of GRS 1758–258 to a kinematic model, following a similar approach to the one we successfully applied to the case of 1E 1740.7–2942 (Luque-Escamilla et al. 2015). We
The root mean squared noise of each radio map amounts to 9.3, 8.2, 10.7, 16.0, 7.3, and 4.5 µJy beam$^{-1}$ for the different epochs, respectively.

Johnston (1981). Horizontal bar shows the scale size and the synthesised beam is on the left-down corner. The vertical scale is expressed in units of the root mean squared noise of each radio map that amounts to 9.3, 8.2, 10.7, 16.0, 7.3, and 4.5 µJy beam$^{-1}$ for the different epochs, respectively.

Fig. 1. Attempt to fit the large-scale radio jets of GRS 1758–258 jets at different epochs using the theoretical kinematic model of Hjellming & Johnston (1981). Horizontal bar shows the scale size and the synthesised beam is on the left-down corner. The vertical scale is expressed in units of the root mean squared noise of each radio map that amounts to 9.3, 8.2, 10.7, 16.0, 7.3, and 4.5 µJy beam$^{-1}$ for the different epochs, respectively. North is up and east is left.

We present a complete set of parameters for the jet precession in Sect. 3 and we analyse the consistency of the results and discuss their consequences in Sects. 4 and 5. We present our conclusions in Sect. 6.

2. Radio data and precession model fitting

As our intention is to study the evolution of the radio jet morphology of GRS 1758–258, we reused historical records of this source at radio wavelengths from the public archives of the VLA interferometer. This task had already been carried out for an earlier study of the source, where four maps exhibiting clear morphological variations in time were obtained (see log of observations and detailed calibration methodology in Martí et al. 2015). In this work, we reuse these four “frames” together with a new one that we obtained from a dedicated campaign on GRS 1758–258 with the VLA in C-configuration conducted in 2016 at the 6 cm wavelength (Project ID. 16A-005, on-source time 7659 s). It is remarkable to note the improvement in sensitivity with regard to this latter observation when compared to the previous ones, which was made possible thanks to the GHz bandwidth available since 2011 following the VLA upgrade, although calibration was applied, taking care to produce a map that would be comparable with previous maps. The final five maps are shown in Fig. 1. As we can see, the new radio map confirms the previously noticed changes in the large-scale morphology of relativistic jets in GRS 1758–258 (Martí et al. 2015).

However, the possibility that these variations are due to precession has never been raised before in the literature. In considering such a case, we tried to fit the well-known precession kinematic model of Hjellming & Johnston (1981) to our data. We follow a similar approach to that successfully used for the case of 1E 1740.7–2942 (Luque-Escamilla et al. 2015), thus achieving a multi-epoch fit of a relativistic jet from their projected paths for the second time. A detailed description of the fit procedure can be found in this last reference; even though for 1E 1740.7–2942, we deal with a more continuous radio jets and their location could be well established thanks to the so-called “skeleton” of the binary image of the maps (see Luque-Escamilla et al. 2015, for details). Unfortunately, GRS 1758–258 presents less continuous jets, so the position of their projection on the maps in Fig. 1 need to be determined in a different way. For this purpose, we slice the image and look for maxima in the emission profiles. The jet points thus obtained conform analogous to the so-called jet ridge in active galaxy nucleus (AGN). It is worth mentioning that these points correspond to the traces of radio jet in the maps, not only to the hotspots, which do not move ballistically.

Once the jet locations are known, we try to fit these data to the kinematic model previously cited. It is worth mentioning that all jet paths on the five different epochs have to be simultaneously fit to the same set of model parameters. There are eight different parameters in the kinematic model, so the least-squares fitting procedure is a very time-consuming task. To achieve a final result in a reasonable amount of time, we try to narrow the limits on some of the parameters whenever some additional, reliable data is available. For instance, the position angle of the jet axis is easily obtained from the maps with enough accuracy to be around $11\degree$. The distance is known to be less than 12 kpc (Martí et al. 2015), so we let this parameter vary only up to this value. The inclination $i$ of the jet precession axis with the line of sight cannot be edge-on due to the lack of eclipses in X-ray data, nor completely face-on, because two jets are visible. In order to constrain an inclination value, we can make use of the brightness ratio between approaching and receding continuous, relativistic jets defined as $BR = [(1 + \beta \cos(i))/(1 - \beta \cos(i))]^{2/3}$. Here, $\alpha$ being the spectral index and $\beta$ the ratio $\nu_{\text{jet}}/\nu_{\text{c}}$, which, in turn, may be related to the apparent jet velocity as $\beta = \beta_s (\sin(i) + \beta_s \cos(i))^{-3}$. From our deep map obtained by combining all available data at 6 cm, we measure jet brightness at equal angular separation on both sides to estimate the observed BR to be of about 2.5, while $\alpha$ ranges from $\sim -0.7$ to $\sim -0.3$ (Martí et al. 2002). Apparent velocity is at least $\beta_s = 0.32$ at the end of the jet (Martí et al. 2015). Therefore, the range of possible $\beta$ is $0.32 - 0.33$ while $i \sim 51\degree - 56\degree$. These inclination angle values, are in fact, compatible with the lack of Fe K$\alpha$ line in observed spectra (see e.g. Soria et al. 2011). However, higher $\beta$ values have been proposed for GRS 1758–258 (Martí et al. 2016), so we let this parameter to exceed the 0.33 limit in...
our fit, although, according to the reasoning presented just above, it would lead to higher \( i \) values.

The fit procedure is performed by varying each parameter value along its range in steps of 10\% of the value in the quest of the minimum reduced \( \chi^2 \) with 301 degrees of freedom. Once the complete set of parameters has been fully explored, we refine the search in the vicinity of the minimum by reducing the step size. The final best-fit parameters are shown in Table 1, and the result is shown in Fig. 1 over-plotted on the original radio maps. The northern jet is the more conspicuous and so it dominates the fit. The reduced \( \chi^2 = 1.32 \) is the minimum obtained when exploring a reasonable range of values in the parameter space. It is calculated based on the fit of the eight parameters and the mean error from the synthesised beam. As can be seen in Fig. 1, these parameters provides a reasonable match between observed jet structures and modelled paths, which suggests that studying the precession effects in the morphological evolution of GRS 1758–258 is not out of the scope of this work. The error in each parameter is estimated with its 90\% uncertainty, obtained as the variation in this parameter which gives an increment of \( e \) in the value of the global, non-reduced \( \chi^2 \).

### 3. Reliability of precession model parameters

In order to ensure that precession is taking place on GRS 1758–258, more than an acceptable fitting accuracy is needed. We have to analyse the implications of the values of the parameters in Table 1 and prove them to be reasonable. In this context, the distance here obtained coincides with the usually assumed value of \( 8.5 \) kpc in the literature (see e.g. Rodriguez et al. 1992; Mereghetti et al. 1994; Keck et al. 2001; Fender 2001; Grimm et al. 2002; Heindl & Smith 2002; Hardcastle 2005; Pottschmidt et al. 2006; Martí et al. 2017). However, some authors put the microquasar much closer, from 2 kpc (Mereghetti et al. 1992) to 5 kpc (Dunn et al. 2010), while others place it as far as 10 kpc based on the low radio flux and a high accretion rate observed (Mereghetti et al. 1997; McConnell et al. 1996). We can try to constrain the distance to the source a bit more based on an independent approach founded on the relations established between extinction, \( E(B-V) \), and distance, \( d \), in the Galaxy (i.e. Lucke 1978; Chen et al. 1999). As \( E(B-V) \) cannot be accurately measured from the overly weak companion star in GRS 1758–258, we can derive it from empirical relations to the column density, \( N_H \) (Güver & Özel 2009; Predel & Schmitt 1995; Reynoso et al. 2006). As a result, assuming \( N_H \approx 1.6 \times 10^{22} \text{cm}^{-2} \) from X-ray data (Soria et al. 2011), the distance to GRS 1758–258 is \( d \approx 8-10 \) kpc and \( d \approx 4-7 \) kpc according to Lucke (1978) and Chen et al. (1999), respectively. Furthermore, taking into account that there is a conspicuous gas cloud possibly related to the jet-ISM interaction in GRS 1758–258 that is located at 8.5 kpc (Martí et al. 2017), the distance value in Table 1 seems reasonable. The existence of such a cloud near the end lobe of the jet could explain a possible slowing down of the jet velocity, lending reliability to the \( \beta \) value obtained in our fitting procedure.

On the other hand, following Soria et al. (2011), \( M_d \approx 5/\cos i \) \( M_\odot \) for the black hole in GRS 1758–258, while the internal radius of the accretion disc would be \( R_m \approx 45/\cos i \) \( \text{km} \). Therefore, for a value of the inclination, \( i \), as in Table 1, would lead to \( M_d \approx 10 \) \( M_\odot \) and \( R_m \approx 80 \) km. It is remarkable that the mass of the black hole in GRS 1758–258 has been derived from X-ray observations and found to be on this order (Keck et al. 2001; Bezayiff 2006; Soria et al. 2011). The internal accretion disc radius \( R_m \) may be identified with \( R_{\text{in}} \), the radius of the marginally stable orbit of a Kerr black hole. This last parameter can be expressed in a non-dimensional form as \( R_{\text{in}} = \xi \mu R_g \), with \( R_g = G M_\odot c^{-2} \) being the gravitational radius. A dependence exists between \( \xi \mu \) and the dimensionless parameter, \( A \), for the black hole such that \( \xi \mu = 3 + A \pm [(3 - A)(3 + A + 2A^2)]^{1/2} \) (upper sign for prograde rotation), with \( A_1 = 1 + (1 - a^2)^{1/2} [1 + a]^{1/2} \) and \( A_2 = (3a^2 + A^2)^{1/2} \) (see, e.g., Bardeen & Petterson 1975). A radio-quiet source like GRS 1758–258 should not have a rapidly rotating compact object (at least from a theoretical point of view, see Blandford et al. 1990; Davis & Tchekhovskoy 2020) unless a geometric effect, due to the inclination of the source with respect to the observer’s line of sight combined with Doppler boosting, was at work (Motta et al. 2018). However, the above observational constraints of Soria et al. (2011) together with the \( \xi \mu \) expression presented above suggest a small to moderate inclination of the GRS 1758–258 system (always \( i < 60^\circ \) decreasing with the black hole spin parameter \( a \)). Therefore, a tentative \( a = 0.1 \) is adopted from this point, which results in \( R_m \approx 84 \) km for a 10 \( M_\odot \) black hole, so the assumed value for \( i \) appears to be appropriate.

However, the precession period, \( P_p \approx 7 \) years, derived from our fit is somehow troublesome. On one hand, it seems to be a reasonable value because \( P_p \) is somewhere in the range of \( 10^{12} \) times the orbital period \( P_o \) proposed for these kinds of sources (see e.g. Larwood 1998), taking into account that the latter is accepted to be \( P_o = 18.45 \pm 0.10 \) days from the X-ray light curve time-series analysis (Smith et al. 2002). On the other hand, no long-term variability greater than \( -600 \) days has been reported from such light curves in spite of the extensive X-ray monitoring of GRS 1758–258. In addition, a new orbital period \( P_o \leq 1 \) day has been recently proposed based on the optical observation of the companion star (Martí et al. 2016), which would not be compatible with \( P_p \approx 7 \) years. This new \( P_o \) value has not been previously reported because it is beyond the typical Nyquist limit in X-ray lightcurves available. What is particularly notable is that this short orbital period clearly appears to be the most usual for LMXB (see the BlackCAT catalogue of stellar black holes in X-ray transients, Corral-Santana et al. 2016). In addition, a significant change within the time frame of the 18.45 day period has been reported from a detailed time-series analysis of RXTE data, ranging from 18.043 to 18.475 days (Hirsch et al. 2020). This is remarkable not only because it would prevent that period from being an orbital modulation, but also because this is the observed behaviour in supra-orbital periods for other known LMXB, such as Her X-1 (with 34 to 36.55 days variability, i.e. Staubert et al. 2013) or SMC X-1 (varying from

### Table 1. Twin-jet kinetic model for GRS 1758–258 radio jets.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Angle of the precession cone</td>
<td>( \psi = (1.4 \pm 0.1)^\circ )</td>
</tr>
<tr>
<td>Inclination of the jet precession axis with the LOS</td>
<td>( i = (59 \pm 2)^\circ )</td>
</tr>
<tr>
<td>Position angle</td>
<td>( \mathrm{PA} = (11.1 \pm 0.1)^\circ )</td>
</tr>
<tr>
<td>Approaching jet (N)</td>
<td>( s_{\text{jet}} = +1 )</td>
</tr>
<tr>
<td>Receding jet (S)</td>
<td>( s_{\text{jet}} = -1 )</td>
</tr>
<tr>
<td>Sense of rotation (clockwise)</td>
<td>( s_{\text{rot}} = -1 )</td>
</tr>
<tr>
<td>Precession period</td>
<td>( P_p = (2774 \pm 11) \text{ d} )</td>
</tr>
<tr>
<td>Jet velocity</td>
<td>( v_j = (0.330 \pm 0.004) \text{ c} )</td>
</tr>
<tr>
<td>Distance</td>
<td>( d = (8.5 \pm 0.1) \text{ kpc} )</td>
</tr>
</tbody>
</table>


\( \chi \) in the value of the global, non-reduced \( e \) as the variation in this parameter which gives an increment of \( \chi^2 \). In the search in the vicinity of the minimum by reducing the step size, the complete set of parameters has been fully explored, we refine the search in the vicinity of the minimum by reducing the step size. The final best-fit parameters are shown in Table 1, and the result is shown in Fig. 1 over-plotted on the original radio maps. The northern jet is the more conspicuous and so it dominates the fit. The reduced \( \chi^2 = 1.32 \) is the minimum obtained when exploring a reasonable range of values in the parameter space. It is calculated based on the fit of the eight parameters and the mean error from the synthesised beam. As can be seen in Fig. 1, these parameters provides a reasonable match between observed jet structures and modelled paths, which suggests that studying the precession effects in the morphological evolution of GRS 1758–258 is not out of the scope of this work. The error in each parameter is estimated with its 90\% uncertainty, obtained as the variation in this parameter which gives an increment of \( e \) in the value of the global, non-reduced \( \chi^2 \).
45 to 60 days, Dage et al. 2019). Various mechanisms have been suggested to explain such supra-orbital modulations, but not all of them could be at work in GRS 1758–258. For instance, the magnetic warping of the disc (Pfeiffer & Lai 2004) requires a highly magnetic compact object in the system, while GRS 1758–258 appears to harbour a black-hole. A wind-driven tilting of the disc (Schandl & Meyer 1994) has been also proposed, but the plausible A-type companion in GRS 1758–258 is hardly capable of emitting strong enough winds. It is also difficult to relate the ≃18.45 day period to a dramatic change in X-ray state change (as the origin of supra-orbital modulations in some sources, e.g. King et al. 1997) because they are not so dramatic nor appeared on such timescales in GRS 1758–258. More likely, a precession period of \( P \), the first features an orbital period of GRS 1758–258. The first features an orbital period of \( P \approx 18.45 \) days and a precession period of \( P_p \approx 7.5 \) years, with radio jets approximately following the paths shown in Fig. 1. The most reliable companion star capable of feeding a black hole of \( M \approx 10 M_\odot \) through Roche lobe overflow would be a K-type giant (Marti et al. 1998; Eikenberry et al. 2001). We refer to this here as the “K-scenario”. On the other hand, the orbital period would be \( P_o \leq 1 \) day and the precession period, \( P_p \), would be the conspicuous 18.45 days from the X-ray light curves. In such a case, the donor star would be a main-sequence A5V (Muñoz-Arjonilla et al. 2010; Luque-Escamilla et al. 2014; Martí et al. 2016) and the system could be an intermediate-mass X-ray binary (Marti et al. 2016; Tauris & van den Heuvel 2006). We call this the “A-scenario”, which could not be related to our kinematic model fitting. Although some observational facts support of this latter case (Luque-Escamilla et al. 2014; Martí et al. 2016) and it fits the \( P_p/P_o \) ratio in the literature, certainly no spectroscopic feature has been obtained from the optical or IR counterpart of GRS 1758–258, so the only way to discriminate between these two pictures is to search for any lack of theoretical support.

4. Discerning the true nature of GRS 1758–258

For black holes, two main mechanisms have been proposed as jet drivers: the black hole spin (Blandford & Znajek 1977, hereafter BZ) and the disc accretion energy (e.g. Blandford & Payne 1982, hereafter BP). According to these two types of jet launching, for jet precession that actually takes place in GRS 1758–258, it would be required to have precession either of the black hole spin axis or instead the disc plane close to the central accretor. For this latter case, the inner part of the disc, where the jet is launched, must be tilted with respect to the whole disc angular momentum. This in turn may be achieved by two mechanisms. One possibility is to have a black hole whose spin axis is misaligned with that of the disc. In such a case, the Bardeen & Petersonson (1975) effect can cause a local warping of the disc, forcing it to be perpendicular to the tilted black hole rotation axis. Another possibility is based on the torques that arise via the misalignment of the accretion disc and the orbital plane of the binary (Katz 1973; Papaloizou & Terquem 1995; Papaloizou & Lin 1995; Larwood 1998, 1997).

Therefore, for jet precession driven by BZ, or by BP together with the Bardeen–Petersonson effect, a tilted, spinning black hole is needed. Although BZ is probably not behind the precession in our system because of the small angular momentum of the disc compared to that of the black hole (which seems to be the common case, making the precession of black hole spin axes difficult to observe at human timescales; see Nixon & King 2013; Banerjee et al. 2019), observational evidence exists to support the idea that the black hole spin axis could be misaligned with the orbital and accretion disc angular momentum in X-ray binaries (see e.g. Hjellming & Rupen 1995; Maccarone 2002; Caproni et al. 2006). This different spinning axis in accretion disc and black holes may be related to the violent birth of the system together with a corresponding long alignment timescale which has been estimated to be on the order of \( \approx 10^6 \) years (Maccarone 2002), or even higher (Banerjee et al. 2019); being, thus, greater than, or at least similar to, the system lifetime. On the other hand, jet precession may be due to a disc tilted by an external torque from the companion and a BP launching mechanisms, no matter the black hole spin. Therefore, the existence of precession in a system such as GRS 1758–258 cannot be excluded. In the following, we try to see if this process is, in fact, taking place according to the different mechanisms mentioned above. In this sense, we ought to note that jet precession can also be driven by deflection at the collision point with super-Eddington winds coming from the disc as suggested for SS 433 (Begelman et al. 2006) or other more sophisticated mechanisms (Liska et al. 2018). We cannot discuss these cases in detail for GRS 1758–258 because of the lack of sufficiently precise observations in the vicinity of the launching site.

4.1. Precession due to relativistic local warping

Although the Bardeen–Petersonson effect alone may be difficult to relate to precession in black hole binaries (Nixon & King 2013), we try to study its reliability on our particular GRS 1758–258 system. We have to consider precession and viscous timescales, \( \tau_v \) and \( \tau_p \), because the Bardeen–Petersonson effect is able to align the inner part of the disc to the black hole spin axis if \( \tau_p \leq \tau_v \) at the inner edge of the accretion disc \( r = R_m \) (Natarajan & Armitage 1999). They are defined as:

\[
\tau_p = \frac{2\pi}{\Omega_p(r)}, \quad \tau_v = \frac{r^2}{v_2(r)},
\]

(1)

where \( v_2(r) \) is the kinematic viscosity of the disc for vertical shear and \( \Omega_p(r) = 2GJ_c r^{-3} \) is the angular velocity due to Lense–Thirring precession (e.g. Wilkins 1972), with \( J_c = GM_c^2 c^{-1} \) as the black hole angular momentum modulus. We do not know \( v_2(r) \) but we can assume \( v_2 \sim v_1 \), which is the viscosity along the disc, and can be parametrised following the Shakura & Sunyaev (1973) prescription as \( v_1 = c_s^2 (GM_c r^{-3})^{-1/2} \). Here, \( c_s \) is the local sound speed, which in turn may be written as \( c_s = H(GM_c r^{-3})^{1/2} \) with \( H \) being the disc scale height. So, if we associate \( R_m \) with the \( R_m \) and adopt the above proposed values for GRS 1758–258 we finally obtain:

\[
\frac{\tau_p}{\tau_v} = 10^{-1} \left( \frac{c}{0.05} \right) \left( \frac{a}{0.1} \right)^{-1} \left( \frac{r}{R_{in}} \right)^{3/2} \left( \frac{H/r}{0.1} \right)^{2}.
\]

(2)

Here, we have assumed a very conservative estimate for \( H/r \) in the inner border of the disc. A reduction in one order of magnitude in this last parameter would lead to a decrease in \( \tau_p/\tau_v \).
where \( \xi \) is the non-dimensional distance rescaled with \( R \). We can again take \( \xi_{\text{in}} = \xi_{\text{out}} \) and assume a potential dependence of the disc density to the distance \( \Sigma(\xi) = \Sigma_0 \xi^p \) with constant parameters. We consider \( s \in [-2, -1, 0] \) to take into account reasonable decreasing or constant behaviours. As the amplitude of the precession angular velocity decreases with the cube of the distance, the exact value of the outer radius of the accretion disc is not critical and we take \( \xi_{\text{out}} = 10^3 \xi_{\text{in}} \) as in Martí et al. (2016). We have numerically integrated Eq. (3) and the resulting precession period, \( P_p \), in days is plotted in Fig. 2 as a function of the spin parameter, \( a \). The upper, grey-dotted line represents the 7.5 years precession period of GRS 1758–258 corresponding to the “K-scenario” defined above, while the lower, magenta-dotted line marks the precession period of ~18.45 days proposed in Martí et al. (2016) according to the “A-scenario”. It may be shown that the yearly precession period for GRS 1758–258 can only be reproduced for an overly slow rotating black hole (\( a \sim 10^{-3} \)) and assuming a constant density along the disc. On the other hand, the daily precession period can be reached with the here adopted rotation for the black hole (\( a = 0.1 \)) or even \( a = -0.2 \) for a retrograde spin under the same density conditions. A smaller disc will lead to shorter periods and, therefore, to more tiny, unrealistic results. If the outer disc is greater than our estimation, then precession periods grow, and a \( \xi_{\text{out}} = 8500 \) with our assumed black hole spin \( a = 0.1 \) and a Sakura–Sunyaev solution \( s = -\frac{1}{2} \) would result on the 18.45 days precession period, while the 7.5 years period is only reached if \( \xi_{\text{out}} = 1.5 \times 10^5 \) under the same conditions. These latter value is difficult to reconcile with both the observed emission from the disc and the binary separation. Thus, precession in GRS 1758–258, if indeed caused by the Bardeen–Petterson effect on the disc, would require an extended disc with a surface density slightly dependent on radius, and clearly would favour the “A-scenario” against the “K-scenario”.

### 4.2. Precession due to external torque

On the other hand, an external torque from the companion could maintain the disc warp and explain the precession in GRS 1758–258. We can follow Papaloizou & Terquem (1995) and assume rigid body precession for a differentially rotating fluid in the accretion disc, and use linear perturbation theory to derive an integral form for the precession frequency. Based on this, Lardow (1998) obtained the ratio between the binary orbital period, \( P_o \), and the precession period, \( P_p \), for a non-relativistic, polytropic equation of state with ratio of specific heats of 5/3, which is:

\[
P_p / P_o = \frac{3}{7} \left( \frac{R_{\text{out}}}{D} \right)^{\frac{3}{2}} \cos \delta,
\]

where \( \delta = \psi_{\text{in}} - \psi_{\text{out}} \) is the orbital inclination, \( D \) is the orbital separation, and \( R_{\text{out}} \) is the outer disc, which is estimated to be a fraction \( k \) of the Roche lobe around the compact object. Here, it is assumed that \( R_{\text{out}} = kR_{\text{Lc}} \gg R_{\text{in}} \). This equation differs by a factor of two from the expression given in Katz (1973) because the tidal torque has been averaged over the disc. The extension of the Roche lobe may be approximated through the expression given by Eggleton (1983):

\[
R_{\text{Lc}} = \frac{0.49}{0.6 + q^{2/3} \ln(1 + q^{-1/3})} D,
\]

so Eq. (4) may be written as:

\[
P_p / P_o = \frac{3}{7} \left( \frac{R_{\text{out}}}{D} \right)^{\frac{3}{2}} \cos \delta.
\]

In this model, the inclination \( \delta \) of the binary orbit with respect to the accretion disc plane gives rise to the observed precession. The jet then subtends a precession cone with a half-opening angle equal to the orbit inclination, so \( \phi = \psi_{\text{in}} \), which we adopt from the model fit \( \phi = 1.4^\circ \), see Table 1). On the other hand, the \( \kappa \) value was determined by Paczyński (1977) for a thin and weakly viscous accretion disc based on the assumption that its size could not exceed the largest orbit with non-intersecting particles in the primary Roche lobe. This parameter depends on the mass ratio, \( q \), although for 0.03 < \( q < 0.3 \) the fraction \( \kappa = 0.86 \) and is roughly independent of \( q \). A similar value, \( \kappa = 0.88 \), was obtained from an independent approach by Papaloizou & Pringle (1977) for 0.2 < \( q < 10 \). This seems to be the right mass ratio interval for GRS 1758–258 harbouring a ~10\( M_\odot \) black hole.

In our “A-scenario” the \( P_o / P_p = 0.03 \), which is similar to the theoretical 0.02 derived from Eq. (6). On the other hand, the “K-scenario” gives \( P_o / P_p = 0.017 \), which is half the theoretical

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**Fig. 2.** The precession period for GRS 1758–258 as a function of the spin parameter. The upper, grey-dotted line represents the 7.5 years precession period of GRS 1758–258 corresponding to the “K-scenario” defined above, while the lower, magenta-dotted line marks the precession period of ~18.45 days proposed in Martí et al. (2016).
value of $0.042$ obtained from Eq. (6). In order to find a better discriminant argument between our two possible scenarios, we can estimate the disc size following the reasoning based on the torque on the accretion disc for a small orbital inclination binary system (Larwood 1998):

$$R_{\text{out}} = \left( \frac{14\pi}{3} \frac{\sqrt{q+1}}{q} \frac{D^3}{G(M_* + M_{\text{donor}}) \rho \cos \delta} \right)^{2/3}. \quad (7)$$

This result is $2^{2/3}$ greater than that proposed in Larwood (1997) and Papaloizou & Terquem (1995), because the considered averaged effect of the donor star tidal torque on the disc. In our “K-scenario”, this would result on $R_{\text{out}} \sim 10^{12}$ cm, which is of the same order than the Paczyński (1977) estimate of $R_{\text{out}} = \kappa R_{L}$. This means a non-dimensional $\xi_{R}$ shorter than 0 value of $R_{\text{system}}$ (Larwood 1998):

This result is $\sim$ that the conspicuous softening events in GRS 1758–258, following Main et al. (1999): $\xi_{R}$ and Papaloizou & Terquem (1995), because the considered average is $\sim 10^4$. We can compare this results to the $R_{\text{out}}$ estimated from the observed delay in brightening and softening events in GRS 1758–258, following Main et al. (1999):

$$\xi_{R} = 1 \times 10^3 \left( \frac{M}{5 \times 10^9 \text{ g s}^{-1}} \right)^{6/25} \left( \frac{M_*}{10 M_\odot} \right)^{-1/5} \left( \frac{M_{\text{donor}}}{M_\odot} \right)^{17/125}. \quad (8)$$

where $M$ is the accretion rate, which for GRS 1758–258, we assume to be $\sim 5 \times 10^{-17}$ g s$^{-1}$ in accordance with the $0.02$ Eddington observed by Soria et al. (2011) and the value adopted in Main et al. (1999). Equation (8) gives a result which is remarkably compatible with our disc size estimation in the “A-scenario”. Thus, the “K-scenario” seems to be less realistic than the former if this precession model is at work, in addition to the yet commented disagreement to the optical and IR proposed counterpart. Moreover, an accretion disc too large should be more powerful than observed and its emission would be conspicuous at optical and IR wavelengths, in contrast to the observed spectrum (Martí et al. 2016). A smaller disc may be present if GRS 1758–258 system were highly eccentric, which is not expected.

4.3. Considering whether precession is actually taking place on GRS 1758–258

From all the previous discussions, we can reach as a preliminary conclusion that there seems to be hints of precession in GRS 1758–258 in any case. A precession period on the order of tens of days is favoured over one on the order of years. However, as pointed out above, such a short period would produce jet paths that are too wiggled to explain their changing morphology shown in the radio maps of Fig. 1, unless GRS 1758–258 is assumed to be unexpectedly closed to us. Therefore, we propose that this source is probably configured in the “A-scenario” and that the conspicuous $\sim 18.54$ day period has to be attributed to precession instead to orbital motion. Thus, as precession could not be responsible for the observed variations in the paths of the radio jets in GRS 1758–258, we proceed to analyse whether these could be attributed to the growth of instabilities.

5. Instabilities as the source of radio-jet changing morphology

Large-scale morphology changes in GRS 1758–258 have already been attributed to the growth of instabilities (Martí et al. 2015, 2017), as is usual in astrophysical jets structure (e.g. Hardee 2011; Perucho 2012). This certainly seems to be the more promising explanation for our source, as it is evident that a lack of symmetry in the wavy patterns of the jet-counterjet structure of GRS 1758–258 in Fig. 1, in contrast to confident cases of precession jets in microquasars such as SS 433 or 1E 1740.7–2942. This is strongly suggestive of some kind of instability developing at large scales rather than a modulation of the jet at the central source is behind the observed evolution of the GRS 1758–258 radio morphology.

Current-driven (CDI) is one of the possible instabilities developing in the jets if magnetic fields are present. Their azimuthal mode $m = 1$ kink instability is the most effective one in modifying the magnetised jet structure (Giannios & Spruit 2006; Hardee 2011), leading even to its disruption. An ideal kink mode is characterised by helical displacements of the cylindrical cross sections of a plasma column. It is expected to grow on a dynamical timescale with respect to an Alfven wave crossing the unstable column. According to simulations of AGN jets (e.g. Mizuno et al. 2012), the timescale for the growth of kink instabilities is on the order of $T_{\text{CDI}} \sim 10 R_{\text{jet}}/v_{\text{A}}$, where $R_{\text{jet}}$ is the jet radius and $v_{\text{A}}$ the Alfven speed. For GRS 1758–258, we measured $R_{\text{jet}} \sim 0.1$ pc (Martí et al., 2015), while $v_{\text{A}}$ could be estimated from ultrarelativistic plasma as $v_{\text{A}} = c B/\pi(R_{\text{jet}} + p_{\text{kin}}) + B^2/12$, where $p_{\text{kin}}$ is the density of kinetic energy of the particles and $p_{\text{kin}}$ is the pressure of the ultrarelativistic plasma (see e.g. Akhiezer et al. 1975). With $p_{\text{kin}} = \frac{1}{3} u_{\text{kin}}$ for this case, and assuming equipartition between the magnetic and particle energy densities ($u_{\text{kin}} = B^2/8\pi$), we finally have $v_{\text{jet}} = (3/5) c = 0.77 \text{c}$. Therefore, we find the instability growth timescale to be $T_{\text{CDI}} \sim 1.5 \times 10^5$ days, in Fig. 1 we can estimate that the helical/ribbon-like pattern arises at about $\sim 50$ arcsec from the core, which for the assumed distance of 8.5 kpc turns out to span a distance of at least $d_{j} \sim 2$ pc. This would imply a flow velocity $d_{j}/T_{\text{CDI}}$ greater than $c$, assuming that the instability starts close to the central engine. Therefore, the CDI kink instabilities do not appear to be responsible of the large-scale structure of GRS 1758–258.

Another possibility is the Kelvin-Helmholtz instability (KHI), which is originated from transverse velocity gradients or discontinuities due to the different kinetic energy between the jet and the typically sub-relativistic ambient medium. Ordinary modes can affect the jet surface or even the whole beam (see e.g. Birkinshaw 1991), leading to shocks, entrainment of ambient material, and eventually the disruption of the jet (Bodo et al. 1998; Martí et al. 2015). KHI seem to produce complex three dimensional helical, ribbon, and thread-like patterns (Hardee 2000; Perucho 2012) with an expected radio emission enhancement of about one order of magnitude. The growth timescale for KHI is of order of $\tau_{\text{KHI}} \sim (2 R_{\text{jet}}/v_{\text{jet}})^{1/2}$, with $v_{\text{jet}}$ being the density contrast between the jet and the medium, and $v_{\text{jet}}$ the jet bulk velocity (Araudo et al. 2009).

Assuming $\eta \sim 10^{-4}$ for GRS 1758–258 (Martí et al., 2015), and $v_{\text{jet}} \sim c$ for establishing a lower limit, this timescale is $\tau_{\text{KHI}} \gtrsim 800$ days, which is even shorter than $\tau_{\text{CDI}}$. Therefore KHI is even less adequate to explain the surge of the helical patterns from the origin following the same reasoning as before, unless it was triggered far from the central engine because the jet would maintain its stability up to that point.

We can reach the same conclusions with an alternate reasoning as well. The helical pattern observed in the jets in the 1997 map of GRS 1758–258 appears to have a wavelength $\lambda \sim 15$ arcsec or $\lambda \sim 0.62$ pc at the assumed distance to the source. If the kink CDI starts near the onset of the structure, the flow speed would then be $v_{\text{jet}} \sim \lambda/\tau_{\text{CDI}} \sim 0.5c$, which seems reasonable. But
In this paper, we have presented a study of the origin of the large structures of GRS 1758–258 (Martí et al. 2015, 2017) attributed to instabilities in the formation of the actual radio jet (et al. 2017). This, in addition, strengthens the role that has been found in other microquasars (see e.g. Migliori et al. 2017). This, in addition, strengthens the role that has been attributed to the growth of instabilities, which has been assumed as the orbital period up until recently. Therefore, some instabilities seem to be capable of explaining the observed morphological changes in GRS 1758–258 radio jets. The KHI need to start far from the central source and could be triggered by jet precession. The wiggling observed in the South jet could be reminiscent of instability-driven structures which has been found in other microquasars (see e.g. Migliori et al. 2017). This, in addition, strengthens the role that has been attributed to instabilities in the formation of the actual radio structures of GRS 1758–258 (Martí et al. 2015, 2017).

6. Conclusions

In this paper, we have presented a study of the origin of the large scale morphological changes in the relativistic jets of GRS 1758–258. Theoretical and observational arguments led us to reach the following conclusions:

1. New radio data confirms that large-scale morphology of GRS 1758–258 indeed changes over time in a matter of years. The observed radio jets clearly exhibit a variable morphology with some structures resembling helical paths;

2. A kinematic model has been fit to the observed radio structures. Although some of the derived parameters may make sense, the precession period of ~7.5 years appears problematic. It would need a giant K-type companion which does not agree with previous optical/IR observations. In addition, the corresponding accretion disc would be too large for the observed emission. Therefore, the radio morphology changes in GRS 1758–258 cannot be attributed to precession;

3. However, our theoretical considerations allow for the existence of precession in GRS 1758–258. Although we cannot assure its precise origin with the present observational evidence, actual data is compatible with precession in both Bardeen–Pettersson and companion torque models. In any case, the favoured scenario is that with an A main-sequence star and an orbital period on the order of a day. This means that the precession period should be on the order of days, which is too short for being compatible with the observed path of the jets;

4. We thus exclude precession as the source of the dramatic changes observed in GRS 1758–258. These changes have presumably been attributed to the growth of instabilities, which have shown to form ribbon-like and helical structures. The absence of symmetry in the wiggles of the jets in the large-scale structure of GRS 1758–258 supports this view. According to our analysis, instabilities developing far away from the central source, rather than a modulation of the outflow speed or mass flux at the compact core, appear to explain the radio observations;

As a result, we propose a new physical scenario for GRS 1758–258 system. It could be a close binary composed of a ~10 M⊙ black hole and a main-sequence A-type, ~2 M⊙ donor star orbiting each other with a period ≲1 day. Although we cannot strictly rule out other mechanisms with currently available data, precession might certainly be at work on this system, it is suggestive to attribute to it the conspicuous observed period of 18.45 days, which has been assumed as the orbital period up until recently. This is the only scenario compatible with available optical/IR observations and with the precession models we put into test. These properties would make GRS 1758–258 a possible intermediate mass X-ray binary. Such a scenario would explain its X-ray behaviour more easily, as it is more similar to high-mass X-ray binaries than to LMXB. The resulting large-scale morphology of the jets is affected by instabilities that originate the ribbon-like and helical-like structures observed. As has been previously claimed, these instabilities would eventually lead to the disruption of the jet.

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