Effect of the centre-to-limb variation and Rossiter-McLaughlin effect in transmission spectroscopy studies

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ABSTRACT

HD 209458b was the first transiting planet discovered, and the first for which an atmosphere, in particular Na I, was detected. With time, it has become one of the most frequently studied planets, with a large diversity of atmospheric studies using low- and high-resolution spectroscopy. Here, we present transit spectroscopy observations of HD 209458b using the HARPS-N and CARMENES spectrographs. We fit the Rossiter-McLaughlin effect by combining radial velocity data from both instruments (nine transits in total), measuring a projected spin-orbit angle of $\pm 1.6 \pm 0.3$ deg. We also present the analysis of high-resolution transmission spectroscopy around the Na I region at 590 nm, using a total of five transit observations. In contrast to previous studies where atmospheric Na I absorption is detected, we find that for all of the nights, whether individually or combined, the transmission spectra can be explained by the combination of the centre-to-limb variation and the Rossiter-McLaughlin effect. This is also observed in the time-evolution maps and transmission light curves, but at lower signal-to-noise ratio. Other strong lines such as Hα, Ca II IR, the Mg I triplet region, and K I D1 are analysed, and are also consistent with the modelled effects, without considering any contribution from the exoplanet atmosphere. Thus, the transmission spectrum reveals no detectable Na I absorption in HD 209458b. We discuss how previous pioneering studies of this benchmark object may have overlooked these effects. While for some star–planet systems these effects are small, for other planetary atmospheres the results reported in the literature may require revision.

Key words. planetary systems – planets and satellites: individual: HD 209458b – planets and satellites: atmospheres – methods: observational – techniques: spectroscopic

1. Introduction

HD 209458b was the first exoplanet discovered that transits in front of its host star (Charbonneau et al. 2000; Henry et al. 2000), and it was also the first exoplanet for which an atmosphere was detected (Charbonneau et al. 2002). Charbonneau and collaborators detected neutral sodium (Na I) in HD 209458b using data from the Space Telescope Imaging Spectrograph (STIS) onboard the Hubble Space Telescope (HST). The same data were used by Sing et al. (2008), who resolved both the Na I D2 and D1 lines. With high-dispersion spectroscopy, Na I absorption was also detected by Snellen et al. (2008) using the High Dispersion Spectrograph (HDS) at the Subaru telescope, and it was tentatively confirmed by Jensen et al. (2011) using the Hobby–Eberly Telescope. Additionally, Albrecht et al. (2009) detected Na I in two Ultraviolet and Visual Echelle Spectrograph (UVES) data sets taken with the Very Large Telescope (VLT).
The Rossiter–McLaughlin (RM) effect (Rossiter 1924; McLaughlin 1924) is produced when a planet transits in front of its host star, occulting a part of the stellar disc. When the stellar rotation is assumed to be in the same direction as the orbital motion of the planet, the most strongly blue-shifted wings of the stellar disc are partly occulted when the transit starts, yielding red-shifted lines; similarly, the end of transit yields blue-shifted lines. The opposite situation (stellar spin opposite to the revolution of the planet) yields red-shifted lines at the beginning of the transit, and blue-shifted lines at the end. Thus the RM effect allows us to know the geometry of the stellar rotation as compared to the planetary motion, and even to calculate the projected spin-orbit angle. This effect is identified in the radial velocity curve. If this effect is not correctly taken into account, it may lead to a misidentification of the planetary atmospheric spectral lines during transits, which are only a manifestation of the RM effect.

Line-centre-to-limb variations (CLVs) may also potentially affect the line profiles during transits. The stellar continuum in the photosphere has a lower intensity near the stellar limb than at the centre of the disc. This effect is related to the optical depth of the photosphere. A more subtle effect arises from Fraunhofer lines that form at different heights in the stellar atmosphere: the balance between the lines that form at different heights depends on the limb angle and stellar latitude (Abetti & Castelli 1935; Appenzeller & Schröter 1967). The strength of the CLV-induced effect can be of the same order as signals found from hot-Jupiter atmospheres (Yan et al. 2017; Czesla et al. 2015; Khalafinejad et al. 2017).

Here, we report our observations of the benchmark planet HD 209458b using the high-dispersion spectrographs HARPS-N and CARMENES. With the combination of several transits with each instrument and the use of models for the CLV and RM effects, we revisited the observational evidence for the detection of Na i in the atmosphere of HD 209458b.

This paper is organised as follows. In Sect. 2 we detail the observations. In Sect. 3 we estimate the obliquity of the HD 209458b system. The methods for extracting the high-resolution transmission spectra and light curves are explained in Sect. 4. In Sect. 5 we present the results obtained in the analysis of high-resolution transmission spectra around the Na i and other lines, and the analysis of systematic effects. In Sect. 6 our results are compared with previous studies of the same planet around Na i. The discussion and conclusions are presented in Sect. 7.

2. Observations

We used archival transit observations of HD 209458b obtained with the HARPS-N and CARMENES spectrographs. A total of nine transits are available in the archives. However, only five of them are considered in this atmospheric analysis. The other four nights are discarded because the signal-to-noise ratio (S/N) of the observations was low. The information related to the observations is summarised in Table 1. Nights 3 and 7 are the same night, observed simultaneously with the HARPS-N and CARMENES spectrographs.

2.1. HARPS-N observations

A total of five transit observations of HD 209458b are publicly available in the Telescopio Nazionale Galileo (TNG) archive. The HARPS-N (High Accuracy Radial velocity Planet Searcher for the Northern hemisphere) spectrograph (Mayor et al. 2003; Cosentino et al. 2012) is mounted on the Observatorio del Roque de los Muchachos (ORM, La Palma), and covers the optical range from 383 to 690 nm. The observations were carried out under programs A32TAC_41 and A35TAC_14. These observations were performed with continuous exposures during the transit, and some additional exposures were taken before and after.

The two observations with lower \( S/N \) (~60) in the Na i order (nights 2 and 4 in Table 1) were discarded for the atmospheric analysis. For night 1 no data were taken during the ingress, and only three stellar spectra are observed before the transit. The sky emission is observed in fibre B in nights 1, 2, and 4. In nights 3 and 5, fibre B was used for Fabry–Pérot observations, which means that we lack information on possible sky emission during the night. The position of the telluric Na i emission lines for these nights (if existing) is expected to be around 8 and 12 km s\(^{-1}\) from the stellar Na i line cores, respectively. At these separations, the presence of sky contamination would affect the results. The sky emission of night 1 was corrected for by subtracting the sky spectrum in fibre B from the science spectrum in fibre A. Unfortunately, the sensitivity of fibre A and B might not be the same. In this case, it would result in an imperfect removal of the telluric sky emission, which would be propagated throughout the process. As this emission is observed inside the Na i line wings and not in the continuum, we are not able to see it in the stellar spectrum (fibre A), and consequently, the sensitivity of the two fibres cannot be compared. However, the residuals related to

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### Table 1. Observing log of the HD 209458b transit observations.

<table>
<thead>
<tr>
<th>Night</th>
<th>Tel.</th>
<th>Instrument</th>
<th>Date of observation</th>
<th>( t_{\text{exp}} ) [s]</th>
<th>( N_{\text{obs}} )</th>
<th>( S/N^{(a)} )</th>
<th>( S/N^{(b)} )</th>
<th>Analysis atmosphere/RM fit</th>
<th>Fibre B</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>TNG</td>
<td>HARPS-N</td>
<td>2015-09-26</td>
<td>600</td>
<td>32</td>
<td>162</td>
<td>51</td>
<td>Yes/Yes</td>
<td>Na i sky emission</td>
</tr>
<tr>
<td>2</td>
<td>TNG</td>
<td>HARPS-N</td>
<td>2016-07-25</td>
<td>600</td>
<td>42</td>
<td>63</td>
<td>20</td>
<td>No/Yes</td>
<td>Na i sky emission</td>
</tr>
<tr>
<td>3</td>
<td>TNG</td>
<td>HARPS-N</td>
<td>2016-09-16</td>
<td>600</td>
<td>45</td>
<td>136</td>
<td>43</td>
<td>Yes/Yes</td>
<td>Fabry–Pérot observations</td>
</tr>
<tr>
<td>4</td>
<td>TNG</td>
<td>HARPS-N</td>
<td>2017-07-16</td>
<td>300/600</td>
<td>38</td>
<td>64</td>
<td>20</td>
<td>No/Yes</td>
<td>Na i sky emission</td>
</tr>
<tr>
<td>5</td>
<td>TNG</td>
<td>HARPS-N</td>
<td>2017-09-07</td>
<td>300</td>
<td>61</td>
<td>108</td>
<td>33</td>
<td>Yes/Yes</td>
<td>Fabry–Pérot observations</td>
</tr>
<tr>
<td>6</td>
<td>CA 3.5 m</td>
<td>CARMENES</td>
<td>2016-09-09</td>
<td>180</td>
<td>38</td>
<td>82</td>
<td>37</td>
<td>No/Yes</td>
<td>No observable Na i sky emission</td>
</tr>
<tr>
<td>7</td>
<td>CA 3.5 m</td>
<td>CARMENES</td>
<td>2016-09-16</td>
<td>180</td>
<td>70</td>
<td>87</td>
<td>40</td>
<td>Yes/Yes</td>
<td>Na i sky emission</td>
</tr>
<tr>
<td>8</td>
<td>CA 3.5 m</td>
<td>CARMENES</td>
<td>2016-11-08</td>
<td>180</td>
<td>80</td>
<td>54</td>
<td>22</td>
<td>No/Yes</td>
<td>Na i sky emission</td>
</tr>
<tr>
<td>9</td>
<td>CA 3.5 m</td>
<td>CARMENES</td>
<td>2018-09-05</td>
<td>192</td>
<td>84</td>
<td>84</td>
<td>38</td>
<td>Yes/Yes</td>
<td>No observable Na i sky emission</td>
</tr>
</tbody>
</table>

Notes. \(^{(a)}\)Averaged S/N per extracted pixel calculated in the Na i order (53 for HARPS-N and 104 for CARMENES) for each night. \(^{(b)}\)Averaged S/N in the Na i D2 and D1 line cores (calculated in ±5 km s\(^{-1}\) centred on the cores). This calculation is performed by dividing the flux of each pixel by its photon noise.
an imperfect sky emission correction would not reproduce the results presented here. If existing, however, they could affect the amplitude of the results. No interstellar Na i is observable in the spectra.

2.2. CARMENES observations

Four more transits were observed with the CARMENES spectrograph (Calar Alto high-resolution search for M dwarfs with Exo-earths with Near-infrared and optical Echelle Spectrographs; Quirrenbach et al. 2014, 2018) located on the Calar Alto Observatory. CARMENES is a two-channel spectrograph that simultaneously covers the optical range from 520 to 960 nm and the near-infrared range from 960 to 1710 nm. In this study we only use the optical observations. The observations were carried out under programs H16-3.5-24, H16-3.5-22, and H18-3.5-22, and the infrared data were studied by Sánchez-López et al. (2019) and Alonso-Floriano et al. (2019). The observing strategy was the same as for the HARPS-N observations.

We discarded night 8 observations from our atmospheric study because of their lower S/N (around 50). The observations of night 6 could not be used because a technical problem of the telescope led to the loss of the first half of the transit. For this reason, only nights 7 and 9 were used in the atmospheric analysis. In all CARMENES observations, fibre B was used to monitor the sky contribution. When the sky spectra were checked, telluric Na i sky emission was observed in nights 7 and 8.

3. Estimating the obliquity of HD 209458b

The radial velocity anomaly due to the RM effect can be observed in the stellar radial velocity measurements of HD 209458 in all transit observations. In order to obtain the system parameters related to this effect, we performed a joint analysis of the radial velocity values from HARPS-N and CARMENES. To this end, we used all five nights observed with HARPS-N and all four nights observed with CARMENES. Radial velocities for both instruments were obtained using the SERVAL programme (Zechmeister et al. 2018), which uses least-squares fitting with a high S/N template created by co-adding all available spectra of the star to compute the radial velocities.

The fitting procedure of the RM effect model to the radial velocity data was performed using the Markov chain Monte Carlo (MCMC) algorithm implemented in emcee (Foreman-Mackey et al. 2013). We used the RM effect model presented in Ohta et al. (2005) together with a circular orbital radial velocity (both contributions implemented in PyAstronomy (Czesla et al. 2019) as modelSuite.Rmcl and modelSuite.radVel, respectively). The RM model depends on the orbital period (P), the transit epoch (Tc), ratio of the planet-to-star radius (Rpl/R⋆), the angular rotation velocity of the host star (Ω), the linear limb-darkening coefficient (ϵ), the inclination of the orbit (i), the inclination of the stellar rotation axis (i⋆), the sky-projected angle between the stellar rotation axis and the normal to the plane of planetary orbit (λ), and the scaled semi-major axis (a/R⋆). The circular orbit radial velocity contribution depends on P, Tc, the stellar velocity semi-amplitude (K⋆), and the offset with respect to the null radial velocity (Δv).

As in Casasayas-Barris et al. (2017), we fixed i⋆ to 90 deg, and P, a/R⋆, Rpl/R⋆, R⋆, and i were taken from the values presented in Table 2, while the other parameters remained free. Because we fitted different HARPS-N and CARMENES nights, we needed to take into account that some free parameters should be fitted jointly for all nights and instruments, and others that could change. Ω, λ, and Tc were jointly fitted in all cases, while for each night we considered different Δv and K⋆ values. We note that the offset between the model and the data can vary from night to night because in addition to the systematic velocity, the radial velocity information contains possible instrumental and stellar activity effects that are reflected as additional offsets to the data. K⋆ could also be affected by activity and become different for different nights (Oshagh et al. 2018). Finally, because CARMENES and HARPS-N cover different wavelength regions, we defined two different linear limb-darkening coefficient parameters, ϵC and ϵH for the CARMENES and HARPS-N data, respectively.

The system was analysed using 100 walkers with 10^5 steps. The first 7000 steps were discarded as burn-in. Each step was started at a random point near the expected values from the literature, and λ was constrained to ±180 deg. On the other hand, Ω was constrained to (0.25, 0.50) rad d^{-1}. The median values of the posteriors were adopted as the best-fit values, and their error bars correspond to 1σ statistical errors at the corresponding percentiles. The MCMC results are presented in Table 3 (Case 1) and the detrended data and best-fit model in Fig. 1. The radial velocity curves were detrended using the best-fit K⋆ and Δv values of each night. The data and best-fit model for each night and correlation diagrams for the probability distribution are shown in Figs. A.1 and A.2, respectively. All Δv and K⋆ best-fit values are presented in Table A.1.

The best-fit Tc value can be compared to the value measured by Evans et al. (2015) by propagating over different orbits using the orbital period from Table 2. We obtain a transit centre of 2 454 560 ± 0.000 2 BJD, which corresponds to a difference of ~19 s with the measurement reported by Evans et al. (2015). Both measurements are consistent considering the reported uncertainties. The error bar of the propagated transit centre was calculated by considering the Tc uncertainty from Table 3 and the orbital period uncertainty from Table 2.

In Table A.1 we observe that K⋆ has different values for different nights. When these values are compared with the value reported by Bonomo et al. (2017) (see Table 2), nights 5, 7, and 9 do not present consistent results (at 3σ). In addition to the possible K⋆ variations induced by stellar activity (Oshagh et al. 2018), telluric contamination is particularly high when radial velocities are extracted. During the extraction with the SERVAL pipeline, we realised that telluric lines are not entirely masked during the process and introduce radial velocity gradients, which leads to K⋆ variations. Thus, the differences observed in different nights might be produced by the combination of these two factors.

With one transit of HD 209458b, Winn et al. (2005) measured an almost aligned system with λ = −4.4 ± 1.4 and e sin i⋆ = 4.70 ± 0.16 km s^{-1}. On the other hand, Albrecht et al. (2012) found λ = −5 ± 7 deg and e sin i⋆ = 4.4 ± 0.2 km s^{-1}. Here, with nine transits, we measure a spin-orbit angle of −1.6 ± 0.3 deg and an angular rotation velocity of 0.540 ± 0.002 rad d^{-1}. We note that the slight difference (smaller than 2σ) between the previous results and our λ estimate might arise because λ and Ω are degenerate (Brown et al. 2017; Albrecht et al. 2012). In addition, as reported by Bourrier et al. (2017), a traditional velocimetric analysis of the RM effect could lead to biases in the measured spin-orbit angle as a result of changes in the local CCF shape.

In order to determine the dependence of the reported results on the i⋆ value, we fitted the data by leaving this parameter free, constrained to (0–180) deg, hereafter Case 2. As expected, we observe a strong correlation between Ω and i⋆, while the remaining parameters maintain consistency with the results obtained.
Table 2. Physical and orbital parameters of the HD 209458 system from previous studies.

<table>
<thead>
<tr>
<th>Description</th>
<th>Symbol [units]</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Stellar parameters</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Effective temperature(^{(a)})</td>
<td>(T_{\text{eff}}) [K]</td>
<td>6065 ± 50</td>
</tr>
<tr>
<td>Projected rotation speed(^{(b)})</td>
<td>(\sin i_\star) [km s(^{-1})]</td>
<td>4.70 ± 0.16</td>
</tr>
<tr>
<td>Surface gravity(^{(a)})</td>
<td>(\log g) [cgs]</td>
<td>4.361(^{+0.007}_{-0.008})</td>
</tr>
<tr>
<td>Metallicity(^{(a)})</td>
<td>([\text{Fe/H}])</td>
<td>0.00 ± 0.05</td>
</tr>
<tr>
<td>Stellar mass(^{(a)})</td>
<td>(M_\star) [M(_\odot)]</td>
<td>1.119 ± 0.033</td>
</tr>
<tr>
<td>Stellar radius(^{(a)})</td>
<td>(R_\star) [R(_\odot)]</td>
<td>1.155(^{+0.014}_{-0.016})</td>
</tr>
<tr>
<td><strong>Planet parameters</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Planet mass(^{(a)})</td>
<td>(M_p) [M(_{\text{Jup}})]</td>
<td>0.682(^{+0.015}_{-0.014})</td>
</tr>
<tr>
<td>Planet radius(^{(a)})</td>
<td>(R_p) [R(_{\text{Jup}})]</td>
<td>1.359(^{+0.016}_{-0.019})</td>
</tr>
<tr>
<td>Equilibrium temperature(^{(a)})</td>
<td>(T_{\text{eq}}) [K]</td>
<td>1449 ± 12</td>
</tr>
<tr>
<td><strong>Transit parameters</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Epoch(^{(c)})</td>
<td>(T_c) [BJD(_{\text{TDB}})]</td>
<td>2454560.80588 ± 0.000008</td>
</tr>
<tr>
<td>Period(^{(d)})</td>
<td>(P) [day]</td>
<td>3.52474859 ± 0.00000038</td>
</tr>
<tr>
<td>Transit duration(^{(e)})</td>
<td>(T_{14}) [h]</td>
<td>2.978 ± 0.051</td>
</tr>
<tr>
<td>Full in-transit duration(^{(e)})</td>
<td>(T_{23}) [h]</td>
<td>2.254 ± 0.058</td>
</tr>
<tr>
<td><strong>System parameters</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Semi-major axis(^{(a)})</td>
<td>(a) [au]</td>
<td>0.04707(^{+0.00046}_{-0.00047})</td>
</tr>
<tr>
<td>Scaled semi-major axis(^{(a)})</td>
<td>(a/R_\star)</td>
<td>8.76 ± 0.04</td>
</tr>
<tr>
<td>Inclination(^{(a)})</td>
<td>(i) [deg]</td>
<td>86.71 ± 0.05</td>
</tr>
<tr>
<td>Systemic velocity(^{(f)})</td>
<td>(\gamma) [km s(^{-1})]</td>
<td>-14.741 ± 0.002</td>
</tr>
<tr>
<td>Stellar velocity semi-amplitude(^{(d)})</td>
<td>(K_\star) [m s(^{-1})]</td>
<td>84.27(^{+0.09}_{-0.10})</td>
</tr>
<tr>
<td>Projected obliquity(^{(b)})</td>
<td>(\lambda) [deg]</td>
<td>-4.4 ± 1.4</td>
</tr>
</tbody>
</table>


assuming \(i_\star = 90\) deg (i.e. Case 1). This same exercise was performed with the eccentricity (now fixing \(i_\star\) to 90 deg), hereafter Case 3. We left the eccentricity \((e)\) and the argument of periastron \((\omega)\) as free parameters, constrained to \((0, 1)\) and \((0–180)\) deg, respectively. We observe that the radial velocity offset \(\Delta v\) and \(K_\star\) parameters are strongly correlated with \(\omega\) and \(e\), respectively. On the other hand, even the best-fit parameters are consistent with the values obtained under the assumption of a circular orbit (i.e. Cases 1 and 2). The projected obliquity \(\lambda\) presents a small correlation with \(\omega\) and \(e\). The best-fit values obtained in these two cases are shown in Tables 3 and A.1 as Cases 2 and 3, respectively. In both cases, the MCMC analysis was performed using 80 walkers and 10\(^7\) steps.

4. Methods

4.1. Transmission spectrum and light-curve extraction

The HARPS-N observations were reduced with the HARPS-N Data reduction Software (DRS), version 3.7 (Cosentino et al. 2014, Smareglia et al. 2014). The DRS extracts the spectra order by order, and they are then flat-fielded. A blaze correction and the wavelength calibration are applied to each spectral order, and finally, all the spectral orders from each two-dimensional échelle spectrum are combined and resampled with a wavelength step of 0.01 Å into a one-dimensional spectrum. The spectra are referenced to the barycentric rest frame and the wavelengths are given in air.

CARMENES observations were processed with the CARMENES pipeline CARACAL (CARMENES Reduction And Calibration; Caballero et al. 2016), which considers bias, flat-relative optimal extraction (Zechmeister et al. 2014), cosmic-ray correction, and the wavelength calibration described in Bauer et al. (2015). The reduced spectra are referenced to the terrestrial rest frame and the wavelengths are given in vacuum.

The transmission spectrum of each night was extracted as described in Casasayas-Barris et al. (2018, 2019). In summary, we first corrected the telluric absorption contamination using Molecfit (Smette et al. 2015 and Kausch et al. 2015). Then, the spectra were shifted to the stellar rest frame using the stelllar radial velocity semi-amplitude \(K_\star = 84.27\) m s\(^{-1}\) measured by Bonomo et al. (2017), the barycentric radial velocity information, and the system velocity (see the physical and orbital parameters used in Table 2). The RM radial-velocity anomaly during the transit was not considered when we moved the spectra to the stellar rest frame. After the stellar spectra were aligned, we combined all the data taken when the planet was not transiting to a high S/N master spectrum (master out-of-transit spectrum). After this, the ratio of all spectra by the master spectrum was computed, and these residual spectra were moved to the planet rest frame. For this, we computed the planet radial velocity semi-amplitude, \(K_p = 144.89\) km s\(^{-1}\), using the parameters in Table 2. Finally, the in-transit residuals between second and third contacts of the transit were combined to determine the individual transmission spectrum of each night. It should be noted that these operations were all carried out on
continuum-normalised spectra. Therefore the transit is not visible outside the spectral lines.

A small difference with respect to the previous studies is that here, this master out-of-transit spectrum is computed using the S/N of the Na\text{I} order as weights. The reason of using the weighted mean to compute this spectrum is that the S/N inside the Na\text{I} line cores is low. In order to determine one transmission spectrum per instrument, we averaged the results of the individual nights using the mean S/N of each night as weights.

As presented in Yan & Henning (2018) and Casasayas-Barris et al. (2019), we measured the transmission light curves after computing the ratio of the spectra by the master-out spectrum, moved to the planet rest frame. These light curves were measured by integrating the flux (using trapezoidal integration) inside two different bandwidths: 0.4 and 0.75 Å. We strongly note that computing the light curves as detailed here (after computing the ratio of spectra) produces different results than if we had followed the method presented in Snellen et al. (2008) and Albrecht et al. (2009), for example. In these studies, the flux inside a passband centred on the stellar lines is averaged (using the stellar spectra) and is then compared with adjacent passbands of the same size. For this reason, the results cannot be directly compared. The light curves of different nights and instruments were combined by sorting the values measured at different time stamps in chronological order with respect to the centre of the transit. In this way, we avoided an interpolation to a common time axis.

In both transmission spectra and light curve analysis we used the transit centre obtained in the RM fitting presented in Sect. 3 (see Table 3). For the remaining parameters we assumed the literature values presented in Table 2.

### 4.2. Modelling the RM and CLV effects

To evaluate the stellar variation during the transit, we modelled the CLV and RM effects in the Na\text{I} lines as presented in recent studies such as Yan & Henning (2018), Yan et al. (2019), Casasayas-Barris et al. (2019), and Czesla et al. (2015). The stellar spectra were modelled using MARCS (Gustafsson et al. 2008), assuming solar abundance, local thermodynamic equilibrium (LTE), and the stellar parameters presented in Table 2. With the spectroscopy made easy (SME) tool (Piskunov & Valenti 2017) we were then able to compute the stellar spectra for different limb-darkening angles and instrumental resolutions. We used the line lists from the VALD database (Ryabchikova et al. 2015). After this, the CLV for different orbital phases of the planet was modelled following Yan et al. (2017), together with the RM effect as presented by Yan et al. (2019), assuming the system parameters obtained in Sect. 3. The differences observed in the modelled spectra when the obliquity (\(\lambda\)) was assumed to be zero, the value measured in this work or the measurements from Winn et al. (2005) and Albrecht et al. (2012) are not significant when compared with the data.

To observe the variation of the modelled stellar line profiles during the transit of HD 209458b, we divided each continuum-normalised stellar spectrum by the modelled out-of-transit spectrum, as we did for the data (see Sect. 4.1). The evolution of these effects with the orbital phase of the planet can be observed in Fig. 2 in the form of what, hereafter, we call 2D maps. In these maps, we show the wavelength on the horizontal axis, the orbital phase of the planet on the vertical axis, and the relative flux is shown in colour. In this figure, we show the contribution of each individual effect and their combination, which clearly shows that the main contribution comes from the RM effect.

![Fig. 1. Radial velocity anomaly due to the RM effect (top panel) and residuals between the data and model (bottom panel). The detrended stellar radial velocity values observed with CARMENES (four transits) are presented as grey stars. HARPS-N data sets (five transits) are presented as black dots. The blue line shows the model resulting from the combination of the HARPS-N and CARMENES best-fit models. In light blue we present the 1\(\sigma\) and 3\(\sigma\) uncertainties of the model.](image)
The double feature caused by the RM effect (blue and red regions in the 2D maps) is easily recognised. This behaviour can be understood by studying Fig. 3. When the planet crosses the stellar disc, it blocks the stellar light from different regions of the disc, which have different radial velocities. In our calculation, we first computed the integrated stellar disc spectrum when the planet was not transiting (out-of-transit). Then, we computed the spectrum of the regions of the disc that were blocked by the planet at different orbital phases. At a given position of the planet, the spectrum of the blocked region does not contribute to the final integrated disc spectrum, for this reason, it was then subtracted from the integrated stellar spectrum. In Fig. 3 we show the modelled out-of-transit spectrum profile (black) and the spectra of the regions that are blocked by the planet (colours) at different orbital phases (in this case, we only include the RM effect). As expected, the out-of-transit profile is centred at the laboratory position because it includes all velocities from the stellar disc. On the other hand, the coloured spectra are shifted with respect to the out-of-transit spectrum because they come from regions of the stellar disc that are described by different radial velocities. These different shifts and line shapes of the blocked spectra with respect to the integrated disc spectrum produce the double feature observed in the modelled RM effect. We note that in this figure, the spectra have been normalised by their continuum level for a better visualisation of the in-transit residuals. The horizontal dashed lines show the four contacts of the transit. The colour bar describes the relative flux ($F_{\text{in}}/F_{\text{out}} - 1$) in %.

Fig. 2. Two-dimensional map of the modelled CLV and RM effects of HD 209458 system around the Na\textsc{i} lines after dividing all stellar models by the out-of-transit spectrum, shown in the stellar rest frame. Top panel: model containing only the RM effect. Middle panel: model containing only the CLV effect. Bottom panel: model containing both the RM and CLV effects. The black solid lines show the calculated position of the planetary trail extrapolated to the out-of-transit time for better visualisation of the in-transit residuals. The horizontal dashed lines show the four contacts of the transit.

The real contribution of the blocked regions to the out-of-transit spectrum is very small compared to the integrated disc spectrum. In this particular case, for example, the CLV contribution in the transmission spectrum is more than four times smaller than the RM contribution. For atmospheric studies was noted for the first time by Louden & Wheatley (2015). In this same paper, the RM effect in the transmission spectrum of HD 189733b was shown in the planet and in the stellar rest frame, noting how these effects are compensated for in the stellar rest frame.

Fig. 3. Modelled stellar spectra around the Na\textsc{i} D2 line of HD 209458 system, containing only the RM effect. The black dashed line shows the out-of-transit spectrum (integrated stellar disc). The coloured lines show the spectra of the regions that are blocked by the planet at five different orbital phases, which are then subtracted from the integrated stellar disc spectrum to compute the final stellar models. We note that these spectra are all normalised by their own continuum level for a better comparison of the line profile. However, in the real subtraction the blocked spectra represent only a small part of the light received from the stellar disc. The approximate position of the planet in each calculation (colours) is indicated in the subplot located in the bottom right corner of the main figure.

The second and third transit contacts is different from the spectrum in which the ingress and egress spectra are included, especially when the modelled spectrum only contains the CLV effect (see its dependence on orbital phase in Fig. 2). The CLV and RM effects are also partially compensated for when the in-transit exposures were moved to the stellar rest frame considering the RM radial velocity anomaly because of the misalignment that it introduces with respect to the out-of-transit spectra. On the other hand, for the transmission light curves, when we follow the method presented in Snellen et al. (2008) and Albrecht et al. (2009), where the flux is measured in the Na\textsc{i} stellar lines core (in the stellar rest frame), the curves are different than when we use the method presented here (in the planet rest frame and after computing the ratio between the individual spectra and the master-out spectrum; see also Sect. 7). This is particularly important for small bandwidths because the positive part (in relative flux) of the RM effect follows the radial velocities of the planet (see Fig. 2). In Fig. 4 we show some transmission spectra and light-curve models that were computed using different methods. As an example, we also show the CLV effect model presented by Yan et al. (2017), which is computed using non-LTE and in the stellar rest frame. We note how significant the effects become (especially the RM effect) in both transmission spectra and light curves when the spectra are moved to the planetary rest frame. In this particular case, for example, the CLV contribution in the transmission spectrum is more than four times smaller than the RM contribution. The importance of considering the RM effect for atmospheric studies was noted for the first time by Louden & Wheatley (2015). In this same paper, the RM effect in the transmission spectrum of HD 189733b was shown in the planet and in the stellar rest frames, noting how these effects are compensated for in the stellar rest frame.
5. Analysis and results

5.1. Na I transmission spectrum

The transmission spectra around the Na I D lines of HD 209458b are presented in Fig. 5 and a zoom-in on the lines in Fig. 6. The results are the combination of three transits observed with HARPS-N and two with CARMENES. The individual transmission spectra obtained for each night are shown in Figs. B.1 and B.2. The laboratory wavelength of the Na I D2 and D1 lines used here are 5889.951 and 5895.924 Å (in air), from the NIST database (Kramida et al. 2019).

For all individual nights and instruments (including the noisiest nights, which are not shown here and were excluded from the analysis), instead of atmospheric absorption from the planet, we observe a pseudo-emission signal centred on the Na I D2 and D1 line positions. When the data are compared with the model containing CLV and RM contributions (see Fig. 6), we find that the data and the models are consistent. We point out that we directly compared the modelled effects with the data, without any fitting or re-scaling procedure.

Other stellar lines in this wavelength range (at 5884 and 5893 Å for example, consistent with Fe I and Ni I) also follow the expected modelled effects. We measure an averaged relative flux of $0.20 \pm 0.05$ and $0.12 \pm 0.04\%$ in the Na I D2 and D1 lines, respectively, using a passband of 0.4 Å in the transmission spectrum obtained using HARPS-N data. For CARMENES, we get $0.31 \pm 0.08$ and $0.07 \pm 0.06\%$, respectively. If this same measurement is performed in our modelled transmission spectrum, which contains no planetary atmosphere, we obtain 0.22% in both lines. When subtracting the model from the transmission spectrum, some absorption-like residuals remain. This probably results from the combination of the limited model accuracy and the smaller S/N in the line cores.

The 2D maps around the Na I doublet combining the different nights are presented in Fig. 6. The S/N achieved around the Na I line cores is relatively low (see values in Table 1). Even with this low S/N, we are able to visually distinguish the behaviour observed in the modelled CLV+RM effects from Fig. 2 in the in-transit time region when the different nights are combined, however. We note that we did not consider any correction related to the different exposure times of the different nights when the individual results were combined. For CARMENES, a similar exposure time was used in both nights, while for HARPS-N one of the nights has a very different exposure time (300 s less than the others). This produces different smoothing of the signals because in 300 s the projected planetary radial velocity changes by around 0.9 km s$^{-1}$ during the transit, although 0.9 km s$^{-1}$ in
5.2. Na I transmission light curves

The combined transmission light curves of the Na I D2 and D1 lines from both instruments are presented in Fig. 7. In Appendix C we present the individual transmission light curves of each instrument and line.

Because we measured the transmission light curves in the planet rest frame, the modelled light curves were computed in the same way. For small passbands (smaller than 0.4 Å) we mainly included the positive (in relative flux) contribution of the RM effect in the light curves, while for larger passbands the negative contribution was also included, which decreased the overall effect (see Fig. 2) because they cancel each other out. This is the case when a passband of 0.75 Å is used, for example.

Both instruments and individual lines show similar results. For the small 0.4 Å passband, the light curves do not show a transit-like shape, but follow the model describing the RM effect. For broader passbands, the CLV+RM model curve shows very small change in amplitude, which is difficult to observe at the S/N of our data, and indeed, the light curves observed in a 0.75 Å passband are mainly flat, with large scatter. In terms of the absorption depth, we measure 0.25 and 0.07% in the modelled light RM and CLV curves during the transit (T2-T3) for the 0.4 and 0.75 Å passbands, respectively. In the observed transmission light curves we measure absorption depths of ~0.15 and approximately ~0.02%, respectively.

Near the central time of transit, the observed transmission light curves show a drop in the relative flux. This might be caused by the fact that the S/N of the stellar Na I lines is very low in the central cores. At zero orbital phase we measure the flux blocked by the planet in the line core, while for shorter and longer orbital phases, this measurement is performed in the wings of the stellar lines, with a higher S/N (because of the orbital motion of the planet). However, this is not reflected in the error bars because they are calculated using the error propagation from the photon noise level of the observed spectra. In the 2D maps from Fig. 6 the noise in the central regions of the lines (around 0 km s⁻¹) is clearly observed. These maps are shown in the stellar rest frame,
but if they are shifted to the planet rest frame (i.e. in the frame we work in), the noisier region moves to different velocities depending on the orbital phases. At zero orbital phase, however, this noise remains at 0 km s$^{-1}$ (i.e. where the measurement is performed).

5.3. Other lines

Following the same method, we explored other strong lines in the spectrum of HD 209458. Specifically, we analysed the Hα line (5562.81 Å) using CARMENES and HARPS-N data sets, the Mg I triplet region (5167.32, 5172.68 and 5183.60 Å) using HARPS-N, and K I D1 (7698.96 Å) and Ca II IRT (8498.02, 8542.09 and 8662.14 Å) using CARMENES data sets.

The effects studied here are especially noticeable around the Mg I region, from around 5165–5190 Å. In addition to Mg I, other strong lines are present in this region, such as Fe I, Fe II, Ti I, and Ti II. The stellar line cores in this region have higher S/N than in the Na I cores and are not affected by contamination from the Earth atmosphere. Consequently, the combined effects (dominated by the RM effect), which are strong for these lines, are clearly observed (see Fig. 8). In this same figure, we show the observed and modelled 2D maps in the Mg I region. The effects can be observed in the position shown in the models, and are recovered in the transmission spectrum. For the strongest lines (Fe II at 5172, Mg I at 5173, and Mg I at 5183 Å), we computed the transmission light curves, which are presented in Fig. D.1.

For Hα, the transmission spectrum does not show any significant feature. The predicted CLV and RM effects of Hα are weak. The measured contrast is around 0.1% at the line centre. Using CARMENES, we also measured the transmission spectra around the Ca II IRT and K I D1 lines. These transmission spectra are presented in Figs. E.1–E.3. In all cases the transmission spectrum shows emission-like features that can be explained by the RM effect. For the Ca II IRT lines, the estimated effects do not describe the observations as well as for other lines. One of the reasons, and which would similarly affect Hα, is that these lines are created in the upper chromosphere and might therefore be affected differently.

5.4. Systematic effects

The error estimates of our measurements come from the propagation of the photon noise through the full analysis, and systematic effects are therefore not taken into account. One way of quantifying the systematic effects is the empirical Monte Carlo (EMC) analysis, presented by Redfield et al. (2008). The EMC is based on the random selection of individual exposures to build the in-transit and the out-of-transit samples. These samples are then used to compute the transmission spectrum, for which the absorption depth is then measured. In order to have statistical significance, this process was applied 20 000 times with different random samples. With this, we determined the probability that the measured signal is of planetary origin or is caused by a random combination of the data. This method has been applied in several atmospheric studies such as Wytenbach et al. (2017, 2015) and Jensen et al. (2012, 2011).

We investigated four different scenarios, three of them described in Redfield et al. (2008). In summary, the first scenario, called “in–in”, takes half of the spectra taken during the transit as the in-transit sample, and the other half as the out-of-transit sample. The second scenario is called “out–out” and takes half of the spectra taken when the planet is not transiting as the in-transit sample and the other half as the out-of-transit sample. At each iteration we randomly selected the spectra that form each sample. The “in–out” scenario is the real case, where the in- and out-of-transit samples correspond to the data taken when the planet is transiting and when it is not, respectively. In this case, the number of spectra in each sample changes in each iteration, but it always ensured that the number ratio is the same as in the observations and that the smallest number is half the observed in-transit sample. The fourth scenario is called...
“mix–mix”. In this case, the in- and out-of-transit samples contain randomly mixed exposures taken when the planet is and is not transiting. For each scenario, we measured the absorption depth in each of the 20,000 results. This absorption was measured as the averaged flux inside a passband of 0.4 Å centred on the Na I D2 and D1 lines, respectively. For comparison, the EMC was also applied to the modelled spectra containing both the CLV and RM effects. We added random noise to the model considering a standard deviation of 0.01, measured in the continuum of HARPS-N normalised data of night 5, and we used the same number of in- and out-of-transit exposures as in this particular night. The histograms with the absorption depth measured for the 20,000 cases are shown in Fig. 9.

In all cases, the three control scenarios (in–in, out–out, and mix–mix) present distributions that are centred around 0% absorption. The in-out scenario presents distributions centred at 0.19 ± 0.04, 0.15 ± 0.05, and 0.13 ± 0.04% for the three HARPS-N nights. For the two nights observed with CARMENES, these distributions are centred at 0.39 ± 0.05 and −0.04 ± 0.06%. On the other hand, the model shows an in-out distribution centred at 0.17 ± 0.04%. The error bars of the values correspond to the standard deviation of the distributions (see the absorption depth values summarised in Table 4).

Although we observe that the S/N in the line cores is very low as a result of the deep stellar lines, in contrast with the control distributions (which are centred at 0%), the in-out distributions are centred at a positive absorption depth, as measured in the transmission spectra. This does not occur in the case of the CARMENES night 9 observation, for which the in-out distribution is centred near −0%. In the individual transmission spectrum (see right panel of Fig. B.2) a drop in flux can be observed at the left side of the laboratory position for both Na I D2 and D1 lines because the spectra are noisier. In the 0.4 Å passband, this region is partially included and decreases the absorption depth.

### Table 4. Absorption depth (in %) measured on the EMC distributions computed using the 0.4 Å passband.

<table>
<thead>
<tr>
<th></th>
<th>In–in</th>
<th>Out–out</th>
<th>Mix–mix</th>
</tr>
</thead>
<tbody>
<tr>
<td>Night 1</td>
<td>0.19 ± 0.04</td>
<td>−0.01 ± 0.14</td>
<td>0.03 ± 0.10</td>
</tr>
<tr>
<td>Night 3</td>
<td>0.15 ± 0.05</td>
<td>0.04 ± 0.16</td>
<td>0.11 ± 0.13</td>
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<td>Night 5</td>
<td>0.13 ± 0.04</td>
<td>0.00 ± 0.09</td>
<td>0.01 ± 0.12</td>
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<td>Night 7</td>
<td>0.39 ± 0.05</td>
<td>−0.03 ± 0.14</td>
<td>−0.06 ± 0.17</td>
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<tr>
<td>Night 9</td>
<td>−0.04 ± 0.06</td>
<td>−0.06 ± 0.21</td>
<td>−0.03 ± 0.14</td>
</tr>
<tr>
<td>Model</td>
<td>0.17 ± 0.04</td>
<td>0.01 ± 0.15</td>
<td>0.00 ± 0.14</td>
</tr>
</tbody>
</table>

6. Comparison with previous results

HD 209458b is one of the most frequently studied planets, with several detections of the Na I doublet using different facilities. Here, we compare our results around these spectral lines with those presented in Sing et al. (2008), Snellen et al. (2008), and Albrecht et al. (2009).

We compared our results with the transmission spectrum obtained by Sing et al. (2008) using mid-resolution (R = 5540) observations with the STIS at HST (see Fig. 10). For this comparison, we binned the transmission spectra from Fig. 5 in 0.5 Å intervals, which is the STIS pixel size. The centre of each bin was located at the positions presented in Sing et al. (2008). The modelled spectrum was computed using only the orbital phases covered by HST, and was then binned at the same intervals as the data. Our high-resolution binned data and our model are consistent with the HST observations. Sing et al. (2008) discarded the two points falling on the Na I line cores from their analysis because of possible telluric contamination: their wavelength positions were consistent with the Earth’s radial velocities during the observations. However, our results reveal that an alternative explanation is the combination of the RM+CLV effects, which is also valid for other wavelengths such as the Ni I position at
5893 Å, which is also visible in the figure. In HST observations, this telluric contamination is absent in other strong lines such as Fe I, while the CLV and RM effects should remain (see Fig. 8), although they are perhaps not detectable by STIS. When we compared the results, we noted an offset of ∼0.2 Å (half of the STIS pixel size) between HST and the results presented here.

Snellen et al. (2008) and Albrecht et al. (2009) measured the transmission light curves by integrating the flux inside the stellar line cores, in the stellar rest frame, and compared the flux with the one measured inside two reference passbands. They measured a Na I absorption of 0.135 ± 0.017% with a passband of 0.75 Å. Following this same method, we built a transmission light curve with the HARPS-N data. In Fig. 10 we compare our own light curve with those presented in Snellen et al. (2008) and Albrecht et al. (2009). None of the results agrees with the modelled CLV and RM effects light curve. On the other hand, although we are not able to reproduce the full transmission light curve from their results with our data, most of the points are consistent considering the error bars. Light curve observations with higher S/N might help solve these issues. Nevertheless, the agreement between our models and the transmission spectrum results obtained in Sect. 5 (Figs. 5, 6, and 8) gives us confidence that the signals seen in our analysis can be explained without invoking planetary absorption.

Finally, Keles et al. (2019) studied the presence of K I in the atmosphere of HD 209458b. Interestingly, they reported an emission-like behaviour at low bandwidths, which would be consistent with the RM effect and non-detection of K I line at 7699 Å reported in this work.

7. Discussion and conclusions

We combined nine transit observations (five with HARPS-N and four with CARMENES) to measure the RM effect using the radial velocity measurements obtained from SERVAL. The best-fit model shows a projected spin-orbit angle of $\lambda = -1.6 \pm 0.3$, indicating a well-aligned orbit, as presented by Winn et al. (2005) and Albrecht et al. (2012). Because of its brightness and the RM amplitude, HD 209458b is an excellent planet for chromatic RM studies (Snellen et al. 2008, Di Gloria et al. 2015, and Yan et al. 2015), especially using ESPRESSO-like observations with high S/N.

We also computed the transmission spectrum of HD 209458b around the Na I using three archival nights observed with HARPS-N, and two with CARMENES. The importance of considering the CLV and RM effect in atmospheric studies has previously been pointed out. Yan et al. (2017) predicted the significance of the CLV effect in atmospheric studies of HD 209458b around Na I. In particular, we observe that this effect becomes significant in the transmission light curves (∼0.1% of contrast, see Fig. 4). Here, in addition to this effect, we also considered the RM effect contribution, which is found to strongly increase the residual effects in the line cores of the transmission spectrum by a factor of about four when computed in the planet rest frame. For all individual nights, the resulting transmission spectra of the exoplanetary atmosphere show an emission-like signal instead of an expected absorption signal, as has been found in previous studies by Albrecht et al. (2009), Snellen et al. (2008), Sing et al. (2008), and Charbonneau et al. (2002). The transmission spectra presented here are consistent with the modelled CLV and RM effects on the stellar line profiles without considering any contribution from the exoplanet atmosphere.

The same is observed in the transmission light curves that are computed using narrow passbands, where the positive contribution of the RM effect is the dominating factor. For wide passbands, however, the effects are diluted and the transmission light curves do not present enough S/N to observe any clear behaviour. Further observations are needed at higher S/N to build reliable light curves that can be compared to our models.

Finally, we compared our measurements and models to previous studies of the presence of Na I in the atmosphere of HD 209458b. Our results reveal that an alternative explanation for the transmission spectrum derived from HST observations is the combination of the RM and CLV effects. When we compared this to High-Dispersion Spectrograph/Subaru observations, we were unable to reproduce the full transmission light curve from their results with our data, but most of the points are consistent considering the error bars. Moreover, none of the light curves are consistent with the modelled effects. Light curve observations with higher S/N are needed to solve this issue. Nevertheless, the agreement between our models and the transmission spectrum results obtained in Sect. 5 (Figs. 5, 6 and 8) gives us confidence that the signals seen in all data sets can be explained without invoking planetary absorption by Na I in the atmosphere of HD 209458b. Our results also imply that the
detection of atmospheric features needs to account for these effects. Detailed modelling of both RM and CLV effects like this is mandatory when the characterisation of small Earth-like planets around low-mass stars is attempted with the ELTs in the coming decades.

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Appendix A: MCMC results and probability distributions

Fig. A.1. Measured stellar radial velocities of HD 209458 during the transit (black) for different nights and instruments. In blue we show the best-fit model obtained with the MCMC procedure.
Table A.1. Extension of Table 3.

<table>
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<tr>
<th>Parameter</th>
<th>Units</th>
<th>Value 1σ</th>
<th>3σ</th>
<th>Value 1σ</th>
<th>3σ</th>
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<td>ΔυH1</td>
<td>m s⁻¹</td>
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<td>± 0.6</td>
<td>26.4 ± 0.2</td>
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<td>± 0.9</td>
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<tr>
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</tbody>
</table>

| K2H1      | m s⁻¹ | 79.6 ± 1.3 | ± 3.8 | 79.8 ± 1.2 | ± 3.7 | 71.9 ± 5.5 | ± 9.9 |
| K2H2      | m s⁻¹ | 84.9 ± 2.1 | ± 6.0 | 84.0 ± 1.3 | ± 3.8 | 77.1 ± 6.5 | ± 11.6 |
| K2H3      | m s⁻¹ | 85.2 ± 0.8 | ± 2.4 | 85.4 ± 0.8 | ± 2.4 | 77.2 ± 5.7 | ± 10.3 |
| K2H4      | m s⁻¹ | 85.5 ± 3.5 | ± 10.2 | 84.5 ± 3.7 | ± 10.0 | 77.2 ± 6.4 | ± 14.0 |
| K2H5      | m s⁻¹ | 95.9 ± 1.4 | ± 3.7 | 95.5 ± 1.4 | ± 4.0 | 86.7 ± 7.0 | ± 11.8 |
| K2C1      | m s⁻¹ | 83.1 ± 5.5 | ± 14.9 | 85.9 ± 5.2 | ± 15.0 | 75.3 ± 7.8 | ± 20.4 |
| K2C2      | m s⁻¹ | 114.5 ± 2.9 | ± 8.3 | 113.9 ± 2.9 | ± 6.0 | 103.4 ± 8.4 | ± 15.8 |
| K2C3      | m s⁻¹ | 85.8 ± 6.0 | ± 13.7 | 79.5 ± 4.9 | ± 9.7 | 78.1 ± 8.6 | ± 22.7 |
| K2C4      | m s⁻¹ | 108.0 ± 3.1 | ± 8.7 | 109.1 ± 3.0 | ± 8.4 | 97.4 ± 7.3 | ± 15.8 |

Notes. MCMC best-fit Δυ and K values with 1σ and 3σ error bars for different assumptions: iₚ = 90 deg and circular orbit (Case 1), iₚ free and circular orbit (Case 2), and iₚ = 90 deg and free eccentricity (Case 3).

Fig. A.2. Correlation diagrams for the probability distribution of the RM model parameters for HD 209458b, obtained assuming iₚ = 90 deg and circular orbit (Case 1). The dashed lines overimposed on the histograms correspond to the 16 and 84 percentiles used to obtain the 1σ statistical errors. One hundred walkers and 10⁵ steps are used in this analysis.
Appendix B: Individual transmission spectra

B.1. HARPS-N data

Fig. B.1. HD 209458b transmission spectra around the Na I doublet for three different HARPS-N data sets. In light grey we show the original data, and as black dots the data binned by 0.1 Å. In purple we show the RME+CLV model for each data set.

B.2. CARMENES data

Fig. B.2. Same as Fig. B.1, but for CARMENES data.
Appendix C: Individual instrument and Na I lines transmission light curves

**Fig. C.1.** Observed transmission light curves for the Na I doublet computed using HARPS-N (top row panels) and CARMENES (bottom row panels) data sets. In each panel we show the light curves for two different passbands: 0.4 Å (top row) and 0.75 Å (bottom row). Each column corresponds to a different computation: the Na I D2 and D1 lines combined (left column), only Na I D2 (middle column), and only Na I D1 (right column). In all cases, the light grey data correspond to the original data, while the black dots are the data binned by 0.002 in orbital phase. In purple we show the modelled light curves containing the CLV and RM effects.
Appendix D: Transmission light curves around Fe\textsuperscript{II} λ5169, Mg\textsuperscript{I} λ5173, and Mg\textsuperscript{I} λ5183

![Graph showing transmission light curves for Fe\textsuperscript{II}, Mg\textsuperscript{I}, and Mg\textsuperscript{I} at different wavelengths.]

**Fig. D.1.** Same as Fig. C.1, but for the Fe\textsuperscript{II} line at 5169 Å (left), the Mg\textsuperscript{I} line at 5173 Å (middle), and for Mg\textsuperscript{I} 5183 Å (right).

Appendix E: Transmission spectra around H\textalpha, K\textsuperscript{I} D1, and Ca\textsuperscript{II} IRT

![Graph showing transmission spectra around H\textalpha, K\textsuperscript{I} D1, and Ca\textsuperscript{II} IRT.]

**Fig. E.1.** Same as Fig. B.1, but around the H\textalpha line. In the top panel we show the results combining three HARPS-N transits, and in the bottom panel the results after combining two CARMENES observations.
Fig. E.2. Same as Fig. B.1, but around the K\textsc{i} D1 line at 7698.96 Å. This result is the combination of two CARMENES observations (HARPS-N does not cover this wavelength region).

Fig. E.3. Same as Fig. B.1, but around the Ca\textsc{ii} IRT triplet. This result is the combination of two CARMENES observations (HARPS-N does not cover this wavelength region). In each panel we show the transmission spectrum around one of the Ca\textsc{ii} IRT lines. Each line is specified inside the panel. We note that for these lines the model seems to be less intense than the data.