Semi-empirical model atmospheres for the chromosphere of the sunspot penumbra and umbral flashes★

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ABSTRACT

Context. The solar chromosphere and the lower transition region are believed to play a crucial role in the heating of the solar corona. Models that describe the chromosphere (and the lower transition region), accounting for its highly dynamic and structured character are, so far, found to be lacking. This is partly due to the breakdown of complete frequency redistribution (CRD) in the chromospheric layers and also because of the difficulty in obtaining complete sets of observations that adequately constrain the solar atmosphere at all relevant heights.

Aims. We aim to obtain semi-empirical model atmospheres that reproduce the features of the Mg II h&k line profiles that sample the middle chromosphere with focus on a sunspot.

Methods. We used spectropolarimetric observations of the Ca II 8542 Å spectra obtained with the Swedish 1 m Solar Telescope and used NICOLE inversions to obtain semi-empirical model atmospheres for different features in and around a sunspot. These were used to synthesize Mg II h&k spectra using the RH1.5D code, which we compared with observations taken with the Interface Region Imaging Spectrograph (IRIS).

Results. Comparison of the synthetic profiles with IRIS observations reveals that there are several areas, especially in the penumbra of the sunspot, where most of the observed Mg II h&k profiles are very well reproduced. In addition, we find that supersonic hot downflows, present in our collection of models in the umbra, lead to synthetic profiles that agree well with the IRIS Mg II h&k profiles, with the exception of the line core.

Conclusions. We put forward and make available four semi-empirical model atmospheres. Two for the penumbra, reflecting the range of temperatures obtained for the chromosphere, one for umbral flashes, and a model representative of the quiet surroundings of a sunspot.

Key words. Sun: atmosphere – Sun: chromosphere – Sun: transition region – sunspots – radiative transfer

1. Introduction

The solar chromosphere is of much interest to the solar physics community because of its highly dynamic nature and also due to the crucial role it is believed to play in the heating of the solar corona. It is sandwiched between the photosphere and the corona and its density decreases radially outwards from the surface of the Sun, whereas the temperature decreases from the photosphere-chromosphere boundary, reaches a minimum, and then undergoes a drastic increase into the transition region (see Vernazza et al. 1981; Avrett et al. 2003).

The study and analysis of the chromosphere is challenging as well as rewarding; challenging because of its complex spatial and temporal structures that are not completely resolved by the present state-of-the-art instrumentation, and rewarding because the energy that leads to coronal heating, the magnetic flux that passes through it to form the coronal magnetic field, is thought to be taking place in the chromosphere (e.g., de la Cruz Rodríguez et al. 2016). Furthermore, the spectral lines that are observed in this region are strictly formed under optically thick non-local thermodynamic equilibrium (non-LTE),

which makes the interpretation and analysis rather difficult. Nevertheless, there have been various successful attempts to interpret chromospheric observations using non-LTE inversions. Some of the available non-LTE inversion codes are HAZEL (Asensio Ramos et al. 2008), HELIX (Lagg et al. 2009), NICOLE (Socas-Navarro et al. 2015), STiC (de la Cruz Rodríguez et al. 2019), and SNAPi (Milić & van Noort 2018). The aim behind all of these codes is to obtain a best fit of the observed chromospheric profiles by iteratively modifying the atmospheric parameters.

Seated above the chromosphere is a thin region where the temperature rises drastically from 0.02 MK to about 0.8 MK and the density falls off rapidly. This layer is called the solar transition region (TR). It transitions between collisionally dominated and partially ionized plasma, and collision-less, fully ionized plasma. One-dimensional solar atmospheric models such as that of Vernazza et al. (1981) predict that this sharp temperature rise takes place within 100 km in the solar atmosphere. However, recent spectroscopic and imaging observations from the Interface Region Imaging Spectrograph (IRIS: De Pontieu et al. 2014) reveal that the TR is very structured and inhomogeneous in nature. Most of the spectral lines that form in this region fall in the range between near ultraviolet (~3000 Å) and far ultraviolet (~400 Å) where the continuum opacity is very high.

★ Data of semi-empirical model atmospheres are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/627/A46>.

The IRIS Mg II h&k spectral lines in particular provide us with one of the richest diagnostics of the upper chromosphere and lower TR (Leenaarts et al. 2013a; Pereira et al. 2015; de la Cruz Rodríguez et al. 2016). Results from Leenaarts et al. (2013a,b) and Sukhorukov & Leenaarts (2017) reveal that these lines are strictly non-LTE and the k_2 & h_2 emission peaks are affected by partial frequency redistribution (PRD). These peaks are representative of the conditions that exist in the middle and in the upper-middle chromosphere. The k_3 & h_3 line cores (formed higher up) are also partially affected by PRD (Sukhorukov & Leenaarts 2017). Furthermore, 3D radiative transfer effects need to be accounted for (Leenaarts et al. 2013b; Sukhorukov & Leenaarts 2017) to model these cores. However, this effect is smaller for higher μ of the observations (with μ being the cosine of the heliocentric angle) and the difference between 3D and 1D radiative transfer is often negligible (as is the case with the Fontenla, Avrett and Loeser (FAL-C) atmosphere modified with different velocity fields, Sukhorukov & Leenaarts 2017).

Leenaarts et al. (2013a) note that the Ca II K and Mg II k cores have very similar formation heights, and are formed significantly higher than Ca II 8542 Å and H α . Both Ca II H&K and Mg II h&k lines have similar oscillator strengths. However, because Mg is about 18 times more abundant than Ca (Asplund et al. 2009), the h&k lines are stronger and therefore form slightly higher than the H&K lines.

While several studies exist on simultaneous observations of the chromosphere and the TR, semi-empirical atmospheric models of a sunspot that effectively characterize the chromosphere and the lower TR are rather uncommon, especially for the penumbra. Socas-Navarro (2007) presented the first chromospheric semi-empirical models for a sunspot, where they used non-LTE inversions of four Ca II and Fe I spectra. However, the uncertainties in the chromosphere are quite high, perhaps due to the difficulty in properly constraining chromospheric penumbral models.

In this paper, we aim to obtain semi-empirical model atmospheres that reproduce the line profiles formed in the chromosphere of a sunspot, especially the penumbra and the umbral flashes. An empirical understanding of these atmospheres will help us to set better observational estimates of this highly dynamic region and will further allow us to obtain the height dependencies of various physical parameters like temperature, hydrogen populations, microturbulence, line-of-sight (LOS) velocities, and electron density from the solar surface. Spectral inversions of these layers in sunspots have so far proven difficult because semi-empirical models, used as starting atmospheres, did not account for effects such as PRD.

In this regard, we focus on the chromospheric model atmospheres obtained with NICOLE inversions of the Ca II 8542 Å line observed with the Swedish 1 m Solar Telescope (SST: Scharmer et al. 2003), and then synthesize upper chromospheric line profiles, such as Mg II h&k, using RH1.5D (Pereira & Uitenbroek 2015) with the chromospheric atmospheres as a starting point. Then the synthetic profiles are compared with the observed IRIS spectra to further empirically test the validity of selected models. This approach serves as a consistency check on these semi-empirical atmospheres, and adequately constrains the solar atmosphere at all heights for the highly dynamic small-scale features of a sunspot.

This paper is divided into the following sections. Section 2 describes the data we used in this paper. In Sect. 3 we discuss the methodology, followed by Sect. 4, where we describe the

results. Finally, we finish off with discussions and conclusions in Sect. 5.

2. Observations

We used observations of the active region NOAA 12533 in a coordinated campaign between the SST and IRIS on 29 April 2016 starting from 09:42 UT, with solar (x, y) coordinates of (623'', 19'') and $\mu = 0.745$. We used the CRISP Imaging Spectropolarimeter (CRISP: Scharmer et al. 2008) to record the data with the SST in imaging spectropolarimetric mode. CRISP is a dual etalon interferometer with low resolution etalons in a telecentric beam configuration. The Multi-Object Multi-Frame Blind Deconvolution (MOMFBD: van Noort et al. 2005) technique was used in the reduction of the raw data. The CRISP data reduction pipeline was used for further reduction as in de la Cruz Rodríguez et al. (2015a) with the small-scale seeing consistency method for spectral profiles as described in Henriques (2012). CRISP sampled the Ca II 8542 Å line at 21 wavelength positions between ± 1.75 Å with respect to the line core, in spectropolarimetric mode. IRIS observed in a medium sparse eight-step raster mode with 4 s exposure time and 1'' raster steps (OBS-ID 3620106129). The Ca II 8542 Å line-profiles were normalized to disk-center quiet Sun continuum levels as measured in the atlas of Brault & Neckel (1987) and Neckel (1999) following the procedure of de la Cruz Rodríguez et al. (2013). The calibration factor was found by fitting a μ -angle compensated average quiet-Sun profile, from a region away from the sunspot, to the atlas convolved with CRISP's transmission profile. Compensation for the μ angle was done using the tables from de la Cruz Rodríguez et al. (2011).

The CRISP data, with a spatial sampling of 0''.058 per pixel and diffraction limit $\lambda/D = 0''.18$ at 8542 Å, was rotated, aligned, and re-sampled to the IRIS Slit-Jaw (SJI) Mg II 2796 Å data. The co-temporal and co-spatial field of view (FOV) of the data was 34.4×34.76 arcsec² with a final pixel scale of about 0''.167 pixel⁻¹. For the current work, we considered a single scan of the data obtained at 09:55 UT along with the IRIS observations as shown in Fig. 1.

3. Methods and analysis

3.1. NICOLE inversions

We performed spectropolarimetric inversions of the Ca II 8542 Å data over the region enclosed by the yellow dashed line shown in Fig. 1 using the NICOLE code (Socas-Navarro et al. 2015). The inverted FOV covers an area of 3.2×23 arcsec² (i.e., 19×138 pixel²). NICOLE is a multipurpose inversion code that is parallelized for both synthesis and inversions of Stokes profiles under non-LTE conditions. It requires an initial guess atmosphere to calculate the emergent profiles. In inversion mode, the code iteratively modifies the different physical parameters such as temperature, velocity, and microturbulence of the initial guess atmosphere using a Marquardt nonlinear least-squares minimization algorithm incorporating response functions (as in Ruiz Cobo & del Toro Iniesta 1992) to reach a match between the synthetic and the observed profiles. The chosen initial atmosphere was the quiet-sun model commonly referred to as FAL-C, from Fontenla et al. (1993), for all pixels in the FOV.

The Ca II ion was modeled by a five-bound-level plus continuum Ca III atom, as used by Leenaarts et al. (2009). NICOLE

Fig. 1. Full FOV of the scans from the SST and IRIS on the 29 April 2016, at 09:55 UT. Tick-marks around the figures are indicated in solar coordinates. *Left panel:* Ca II 8542 Å red wing image obtained from CRISP. *Right panel:* corresponding IRIS SJI at 2796 Å. The yellow dashed region shows the inverted FOV for reference. The plus sign, cross, asterisk, and square correspond to selected locations featuring an umbral flash, the cool penumbra model, the hot penumbra model, and a quiet surrounding pixel, respectively. The atmospheric models corresponding to these regions are provided in this paper.

operates under complete angle and frequency redistribution (CRD, [Scharmer & Carlsson 1985](#)), which is a very good approximation for the Ca II infrared lines ([Uitenbroek 1989](#)). The starting LTE populations were determined using the MULTI approach, as implemented by [Carlsson \(1986\)](#), where the sum of statistical weights in the Saha equation is done over the finite number of levels of the model atom. A Gaussian quadrature with three angles was selected for the rays.

The cubic DELO-Bezier formal solver ([de la Cruz Rodríguez & Piskunov 2013](#)) was chosen for the radiative transfer equation. Following [Leenaarts et al. \(2014\)](#), we included the Ca II isotopes to obtain good fits to the observations in the red wing of the profiles.

Nodes were placed regularly at equidistant heights from the topmost optical depth of $\log \tau_{5000} = -8$ to approximately $\log \tau = 1$. We used the native NICOLE equation of state. The electron pressure at the topmost height for all pixels remained unchanged by the inversion cycles, and was kept at a value of $10^{-1} \text{ dyn cm}^{-2}$ as an upper boundary condition. Hydrostatic equilibrium was then used to stratify the atmosphere. Five iterative inversion cycles, where the results from each cycle were used as starting guesses for the next cycle, were used to improve convergence and avoid local minima when minimizing the χ^2 . The number of nodes per cycle are shown in Table 1. We performed multiple tests with lower nodes in temperature and LOS velocity, which led to significantly worse fits, especially for umbral flashes. Tests with one node in the LOS magnetic field led to the same models as averaging the three node inversions in the way described in Sect. 4.3 but, paradoxically, poorer matches for Stokes Q and U for otherwise well-fitted penumbra profiles. Applied across the whole atmosphere, perturbations in microturbulence are

Table 1. Number of nodes for different parameters.

Nodes cycle 1	Nodes cycle 2–5	Parameters
5	8	Temperature
3	5	Velocity
1	1	Microturbulence ^(a)
0	3	B_z
0	1	B_x
0	1	B_y
0	0	Macroturbulence

Notes. ^(a) Perturbations in microturbulence are additive, applied to the stratification of the initial atmosphere.

additive to the stratification of the initial guess atmosphere (FAL-C). For cycles 3–5 the weights of Stokes V for the merit function were half of those for Stokes I. For Stokes Q and U the weights were four times lower than those of Stokes I. For cycle 2 these relations were doubled as they were biased in favor of Stokes I. This was to account for the different levels of noise and to guarantee that the correct valley in the minimization of χ^2 was selected early on. The comparison of the observed and the inverted Stokes parameters, corresponding to the selected locations of a hot penumbra, a cool penumbra, and an umbral flash (as indicated in Fig. 1), is shown in the first four rows of Fig. 2. The last two rows of the same figure show the stratification of the respective model atmospheric parameters such as the temperature, LOS velocity, magnetic field, and micro-turbulent velocity, as derived from the NICOLE inversions.

3.2. Radiative transfer using RH1.5D

The RH1.5D¹ (Pereira & Uitenbroek 2015) is a massively parallel radiative transfer code based on RH (Uitenbroek 2001). It is capable of solving multilevel, multi-atom, non-LTE calculations by considering PRD and can also include Zeeman splitting effects allowing full Stokes synthesizing capabilities. We use the fast angle hybrid approximation for the PRD calculations as described in Leenaarts et al. (2012). This code can compute the spectra from either a 3D or 2D or 1D model atmosphere on a column-by-column basis (hence 1.5D) and it is designed to run over multiple nodes in a supercomputing cluster.

The column-by-column approach, though faster, has one major limitation. It can only calculate the emergent profile vertically along the column. This means that the effect of inclined rays, crossing different atmospheres, is neglected, an effect that can be accounted for in a true 2D or 3D calculation. Furthermore, the noninclusion of the inclined rays might lead to a different mean radiation field, thereby affecting the non-LTE source function and ultimately the emergent intensity profile that may result in unexpected cooler cores of some very strong spectral lines (Leenaarts et al. 2013a,b). Compared to a column-by-column approach, this can also lead to a decreased RMS contrast at the line core of some spectra such as the Ca II 8542 Å as shown by Leenaarts & Carlsson (2009). However, recently de la Cruz Rodríguez & van Noort (2017, and references therein) suggested that a 1.5D geometry suffices for modeling the Ca infrared triplet lines. Nevertheless, for most non-LTE computations the 1.5D approach suffices, and does a reasonably good job. Besides, the ability of treating the spectra in PRD outweighs the drawbacks significantly.

3.3. Synthesizing Mg II h&k spectra

One of the major goals of this paper is to provide semi-empirical model atmospheres of a sunspot that are well constrained from the photosphere to the chromosphere, to obtain a pool of inverted models from NICOLE that can satisfactorily reproduce the Mg II h&k profiles. In this regard, we performed syntheses of the Mg II h&k spectra under PRD (using RH1.5D) with the set of model atmospheres obtained from the NICOLE inversions of the SST data. We compared these synthetic profiles with the actual co-temporal and co-spatial observations from IRIS, which effectively serve as a check on the quality and the reliability of these semi-empirical models.

We used a ten level plus continuum model of the Mg atom for the radiative transfer computations. In observations, the Mg II h&k lines have blends from various other atomic species besides Mg II, and the most appropriate way would be to synthesize the spectra from RH by including as many atoms as possible in non-LTE. However, this adds tremendously to the time consumption of the synthesis. To circumvent the problem, we treated those atoms in LTE and used a line list that contained a list of bound-bound transitions and their parameters. RH supports line lists in Kurucz format². Once the spectra are synthesized, they were spectrally smeared by convolving with the IRIS instrumental profile to compare with the observations (see Pereira et al. 2013).

4. Results and discussion

4.1. Model atmospheres

The three columns in Fig. 2 show the observed and the inverted Stokes parameters along with the model atmospheric parameters for a hot penumbra, a cool penumbra, and an umbral flash, respectively, obtained from the NICOLE inversions. The different parameters shown are temperature, LOS velocity, LOS magnetic field, and the microturbulent velocity. The cool and hot penumbra selection is representative of the range of temperature stratification obtained between $\log \tau = -5$ and -7 , where the atmospheres show a divergence when compared to other layers. The multiple nodes in temperature, LOS velocity, and LOS magnetic field, as indicated in Table 1, are used to capture the variations in the vertical stratification of the solar atmosphere, including those of the upper chromospheric layers, as made possible by the different formation heights of the different wavelengths sampled. Atmospheric models such as these are used as inputs for the RH1.5D radiative transfer code for synthesizing the Mg II h&k spectra. For the purposes of this approach, the occasional extrapolation performed by NICOLE, or the occasional large change in a node where the response in the Ca II 8542 line profile is relatively limited by the observations, is considered as an advantage. Extrapolations as such led to a pool of models that work well in reproducing the observed properties of the Mg II h&k line profiles.

4.2. Comparison between the synthetic and IRIS spectral profiles

In Fig. 3 we show the comparison between the Mg II h&k profiles synthesized with RH1.5D (black) and the ones observed with the IRIS spectrograph (red). We show spectra of nine pixels (including the four marked in Fig. 1) spread over the FOV, selected based on the χ^2 values between the observed and the synthetic profiles for the penumbra, and manually for the umbral flash and the quiet surrounding regions. We have labeled them from A through I corresponding to different solar features such as the penumbra, umbra, and the relatively quiet areas away from the spot (termed as quiet surroundings). The synthetic profiles were spectrally smeared by convolving with a Gaussian profile, as described in Sect. 3.3, to match the observations. Both the observed and the synthetic profiles were normalized to a reference intensity in the wavelength region between 2800 Å and 2802 Å averaged over a quiet area covering $0''.834 \times 1''.67$, located away from the sunspot. We also show the fits to the Ca II 8542 Stokes I profiles in Fig. 4, corresponding to the pixels shown in Fig. 3, to indicate the excellent quality of the fits obtained from inversions.

4.2.1. Penumbral profiles

A closer look at Fig. 3 reveals that for most of the pixels across the different features in the FOV, the synthetic spectra corresponding to the Mg II triplet, as well as the photospheric spectral regions between k_2 and h_{2v} peaks along with the blended lines, match well with the IRIS observations. Furthermore, the Mg II triplet lines bear a structural resemblance to the Ca atom where the infrared triplets (8498, 8542, and 8662 Å) are allocated to the higher levels of the corresponding h & k lines and are known to sample mid-chromospheric regions (Pereira et al. 2015). A reasonable match of the synthetic spectra with the IRIS observations in these wavelength regions also builds confidence in our approach.

¹ The code is publicly available at <https://github.com/ITA-Solar/rh>.

² As described in <http://kurucz.harvard.edu/linelists.html>

Fig. 2. Columns showing the observed (black dots) and synthetic (red) full Stokes spectra in units of normalized HSRA (Gingerich et al. 1971) continuum intensity at disk center at a wavelength in the middle of the spectral range, and their atmospheric parameters such as temperature, LOS magnetic field, velocity, and microturbulent velocity for three different models: hot penumbra (asterisk), cool penumbra (“cross”), and umbral flash (“plus sign”), respectively. The continuous line overplotted on the dashed line for the LOS magnetic field, shows the variation of the magnetic field in the region $\log \tau = [-6, -2]$ where the Ca 8542 spectra is most sensitive.

Fig. 3. Comparison of the synthesized Mg II h&k spectra (black) with co-spatial and co-temporal IRIS observations (red) for various features in the FOV like penumbra, umbra, and quiet surroundings. Profiles A, E, G, and I correspond to the hot penumbra, cool penumbra, umbral flash, and quiet surroundings, respectively, with atmospheric models described in the previous section. The insets in each of the subplots zooms in on the profiles for the Mg II k region. Both the IRIS and the RH profiles were normalized to a reference intensity (I_c) as described in Sect. 4.2.

More interestingly, the k_1 , k_2 and h_1 , h_2 line features from the observations are also well reproduced by the synthesis, including the peak separations. We verify that this is indeed the case for the vast majority of the penumbra of the sunspot. Six selected profiles corresponding to different locations in the penumbra are shown in Figs. 3A–F. Figures 3A and E in particular, show the spectra derived from the hot and cool penumbral model atmospheres and respective observations, as indicated in the bottom two rows of Fig. 2. We also note from Fig. 2 that the hot penumbra has a relatively weak horizontal or perpendicular (given by $B_{\text{HOR}} = \sqrt{B_x^2 + B_y^2}$; B_x and B_y being the fields in the horizontal x and y plane, respectively) and LOS magnetic field compared to the cool penumbra. This is the case for the vast majority of different hot penumbral pixels in the FOV, where the cool penumbral magnetic field is greater than its hot counterpart.

Each sub-figure in Fig. 3 has an inset window that shows the observed and the synthetic spectra for the Mg II k region, for the sake of clarity and better visualization. The sufficiently good quality match (except for the line core) between the observed and the synthetic spectra indicates that the stratification of the

different physical parameters are indeed good enough to capture the features of two very different spectral lines formed over a wide range in the solar chromosphere. Leenaarts et al. (2013a) describe the $\tau = 1$ distribution of the k_1 , k_2 , h_1 , h_2 peaks to be between 1.3 to 1.7 Mm, which is of the same order of the peak sensitivity of the Ca II 8542 line core. Detailed analysis based on the contribution functions (discussed further in Sect. 4.6 and Fig. 8) indicates that though the peak contribution of both the k_2 wavelength and the 8542 line core is roughly around the same optical depth, the former has a wider spread towards lower optical depth and thereby samples atmospheric layers slightly higher than Ca II 8542. A successful reproduction of the Mg II h&k peak intensities, including their separation, demonstrates the strength of our models. It is known that the peak separation is indicative of the velocity variations from the mid to the upper chromosphere (Leenaarts et al. 2013a), and a satisfactory match between the synthetic and the observed profiles indicate that we are able to capture the intricate velocity variations with a significant level of accuracy. This suggests that these models can successfully explain the atmospheric properties above a sunspot penumbra up to the chromosphere.

Fig. 4. Comparison of the observed (black dots) and their corresponding synthetic (red) Ca II 8542 Å Stokes I profiles for the co-observed spectra shown in Fig. 3 above. The fits show a very good agreement with the observed spectra that further reinforces the reliability of the model atmospheres used to synthesize the Mg II h&k spectra.

In this paper, we propose two models corresponding to a hot (Table A.1) and a cool (Table A.2) penumbra. To the best of our knowledge, these are the first chromospheric penumbral models that reproduce different chromospheric lines observed with different instruments (with one of them being a space-based slit-spectrograph and the other a ground-based Fabry-Perot instrument).

4.2.2. Umbral profiles

The synthetic profiles obtained for the two umbral pixels as shown in Figs. 3G and H, show significant self-reversals compared to the observed ones. In almost all the pixels across the FOV we end up with a central depression in the synthetic line profiles whereas the observed ones indicate an emission core. Lites & Skumanich (1982) also reported this behavior with more depressed central line cores in the umbra, however the reason behind this is still not fully clear.

Umbral profiles with strong asymmetries between the k_{2v} , k_{2r} , and h_{2v} , h_{2r} peaks, similar to Figs. 3G and H, have been observed across multiple pixels in the FOV. The presence of a

strong emission in the blue and a corresponding suppressed red k_2 peak is a possible indication of strong gradients in the down-flows in the upper chromosphere and TR. Such strong down-flows were part of the models that best reproduced some umbral flashes in Henriques et al. (2017). In fact Lites & Skumanich (1982) also introduced a strong downdraft of about 40 km s^{-1} on top of their atmosphere in order to take into account this asymmetry in their umbral profiles. We discuss this further in Sect. 4.6.

Except for the self-reversal, the synthetic spectra in Fig. 3G seem to capture the shape of the observed line profile over the entire spectral range, including the peaks and exterior slopes of h_2 and k_2 (as an envelope). Unlike the penumbra, the signal level between k_{2r} and h_{2v} is negligible and therefore it is difficult to comment on the match between the observed and the synthetic spectra in this wavelength range; nevertheless, based on the reasonable matches in the k_2 and h_2 peaks we feel confident of the strong down-flow scenario in our model atmosphere. This is further clarified by the velocity stratification shown in Fig. 2 (third column), where the NICOLE inversions reveal a strongly positive LOS velocity of up to 10 km s^{-1} with decreasing optical depth.

Fig. 5. Stokes I profile and the corresponding stratification of the LOS and microturbulent velocity for the stronger umbral flash. *Top panel:* umbral flash intensity profile corresponding to a region of strong down-flow as shown in Fig. 3H. *Bottom panel:* corresponding stratification of LOS and microturbulent velocity. We clearly see that the LOS velocity is higher in this case.

Furthermore, the Stokes parameters corresponding to the umbral pixel in Figs. 2 and 4G show a typical flash-like behavior with an emission feature. The model atmosphere corresponding to such an umbral flash has been proposed in Table A.3.

Supersonic down-flows, of the order of 100 km s^{-1} , have been observed on a number of occasions in the TR above sunspot umbrae in the recent past (Kleint et al. 2014; Straus et al. 2015; Chitta et al. 2016; Samanta et al. 2018). Some of these studies (such as Chitta et al. 2016; Samanta et al. 2018) reported signatures of strong down-flows in the chromospheric Mg II h&k lines, which originate in the TR and were found to be associated with coronal loops and sometimes in a coronal rain. Chitta et al. (2016) argue that the high-speed supersonic down-flows in the corona would have to undergo a shock transition to subsonic speeds, lower in the solar atmosphere and thereby affect the lines formed in the chromosphere.

Figure 3H (also Fig. 4H) indicates the presence of another strong supersonic down-flow in an umbral flash observed in the Mg II h&k spectral line (and in the Ca II 8542 Å spectra), which is mainly chromospheric. Line-of-sight velocities up to $+20 \text{ km s}^{-1}$ with a strong gradient were found from the Ca II 8542 inversions for the corresponding pixel as shown in Fig. 5. These velocities are stronger than the one shown in Fig. 2. The highest values of the velocity occur at the highest layers, towards the end of an up-trending slope, where Ca II 8542 is no longer well constrained. However, the synthetic Mg II spectra show a direct consequence of this strong down-flow by an enhanced blue-red peak asymmetry, which is stronger than what was found in Fig. 3G. The significantly higher Doppler-shifted IRIS Mg II spectra indicates the possibility of even stronger down-flows that are not captured by the Ca II 8542 inversions. Statistical investigations by Samanta et al. (2018) report the detection of down-flows of the order of at least 40 km s^{-1} in both the penumbra and umbra of different sunspots observed by IRIS between September 2013 and April 2015, across multiple chromospheric and TR lines. Though they do not indicate the presence of umbral flashes in their observations, it is possible that sometimes these down-flows in the umbra may be associated with a flash, as we

report in this paper. With such a high gradient in the LOS velocity, it would be enough to cause a significant redshift of the k_3 and h_3 line core and cause the opacity to shift in such a way that it causes a stronger emission in the blue and a suppressed emission peak in the red. Our model atmospheres, however, do not include velocities much higher than 20 km s^{-1} , even for the most extreme models and at heights where the observations do not allow a good constraint; this could be a possible reason why the synthetic umbral flash Mg II profiles do not reproduce the shift that is present in the observed profiles.

Since their discovery, umbral flashes have been understood as a manifestation of up-flows (Beckers & Tallant 1969). Recent semi-empirical investigations of umbral flashes by Socas-Navarro et al. (2000a,b), de la Cruz Rodríguez et al. (2013) and Joshi & de la Cruz Rodríguez (2018) support such an interpretation by obtaining, via inversions, purely up-flowing atmospheres that reproduce the observed umbral flash profiles after non-LTE CRD radiative transfer of the Ca II IR lines. Bard & Carlsson (2010) modeled umbral flashes in the Ca II H&K lines using hydrodynamic simulations followed by non-LTE CRD synthesis. They concluded that flashes are a result of acoustic waves generated in the photosphere, which steepen into a shock in the chromosphere. Similarly, Felipe et al. (2014) synthesized full Stokes spectropolarimetric profiles in the Ca II IR of an umbral flash generated by a numerical simulation. In both studies the contribution functions to the wavelength of the flashed blue emission peaks are highest at atmospheric heights that feature up-flowing atmospheres. This, together with the majority of the semi-empirical work mentioned and the success of the simulation synthetics in reproducing the properties of umbral flashes, including spectral evolution in time, lends strong support for a model of umbral flashes that is up-flowing. However, the highest opacity and thus highest formation height is at the line minimum, which is captured in the observations (and thus the inversions). Both numerical models include strong down-flows in the upper layers of the solar atmosphere, immediately above the weaker up-flows. Furthermore, the flash formation of Bard & Carlsson (2010) is remarkably similar to that of bright grain formation (see Carlsson & Stein 1997) and, in the latter, it is made unambiguously clear that the opacity shift produced by the strong down-flows is critical for the formation of the strong blue peak itself. This is similar to the opacity effect described by Scharmer (1984) and also important for the line formation of magnetic bubbles observed in flux emergence regions (de la Cruz Rodríguez et al. 2015b). As far as we are aware, there are no simulations of umbral flashes with purely up-flowing atmospheres and the down-flows are always stronger than the up-flows. The agreement of previous semi-empirical results in the literature means that we should still regard umbral flashes as likely occurring in, or leading to, up-flowing atmospheres. However, we find strongly down-flowing models, similar to those of Henriques et al. (2017), but reproducing both the observed Ca II and Mg II flash profiles. In addition, unlike Henriques et al. (2017) and the other semi-empirical modeling studies, we do not find atmospheres that reproduce umbral flashes with just up-flows; this, coupled with the observed asymmetries in the k_2 and h_2 peaks, leads us to believe that umbral flashes, even at the maximum intensity stage when their blue emission peak is strongest, can be formed under down-flowing conditions in the Sun. Finally, such down-flows might modulate the location at which upward propagating waves steepen into shocks, similarly to one of the scenarios described in Nelson et al. (2017) to explain small-scale umbral brightenings.

Fig. 6. Comparison of the quiet surrounding Mg II h&k spectrum synthesized by RH1.5D (black) and IRIS observation (red). *Left panel:* synthetic spectrum from original model atmosphere. *Right panel:* resynthesized spectra with the temperature manually reduced by 75 K across all layers as described in the text.

4.2.3. Quiet surroundings: Located at the edge of the FOV

The quiet surroundings are basically defined to be the regions around the sunspot, but close to it, where there is no magnetic activity going on with time. We chose these regions based on visual inspection with the CRISP SPectral EXplorer (CRISPEX; Vissers & Rouppe van der Voort 2012), an IDL widget-based tool designed for effective visualization. Unlike the penumbra and the umbra, the quieter areas on the inverted FOV (marked with a square in Fig. 1), have mismatches in the extended wings of the Mg II spectrum as seen in the left panel of Fig. 6, over the entire spectral range of interest. Based on these differences between the observed and the synthetic Mg spectra, it is our contention that the discrepancy in the far wings of the profiles could be due to a small difference in the temperature stratification compared to what was obtained from the inversions. Since the synthetic profiles have higher intensities in the far wings than the observations, we resynthesized the Mg II spectra with an atmosphere where the temperature was reduced by 75 K as a whole. As expected, this resulted in acceptable matches between the observed and the synthetic profiles (Fig. 6: right panel), which otherwise were distinctly different in the original synthesis. The spectra in Fig. 3I (same as in the right panel of Fig. 6) show the synthetic spectra after the manual adjustment described above. The synthetic profiles from the adjusted atmospheres provide a good match with the observed spectra in the line wings, k_2 and h_2 features, and the far wings.

Synthesizing the Ca II 8542 spectra for the modified atmosphere, allowing for self-consistent changes in the hydrodynamic parameters via NICOLE's equation of state, led to a profile that was no longer a perfect fit to the observations, with the synthetic profile being lower in intensity at all wavelengths. In this regard, we describe the model atmosphere for the quiet surrounding in Table A.4 below, which corresponds to the original NICOLE inversions (i.e., without the 75 K change). Therefore, unlike the case of the penumbra, we find a situation where multiple lines cannot successfully be reproduced by our approach. In such situations the best approach is likely to attempt multiline PRD inversions, recently made available with the STiC code (de la Cruz Rodríguez et al. 2019). Nevertheless, with the proposed temperature adjustment, the quiet atmosphere could prove to be an excellent starting atmosphere for inversions.

Fig. 7. Comparison of the images obtained from the RH synthesis and images composed from the IRIS slit scan observations for the inverted FOV and for a narrow range of wavelengths: A: Mg k_{2v} IRIS image, B: Mg k_{2v} image obtained from RH1.5D synthesis, C: Mg h_{2v} IRIS image, D: Mg h_{2v} image obtained from RH1.5D synthesis, E: Mg II k wing image at 2794.7 Å from IRIS, and F: Mg II k wing image at 2794.7 Å from RH1.5D synthesis. The spectra were integrated over a definite wavelength window as described in Sect. 4.4. Each pair of images was scaled between a common intensity range for efficient comparisons.

4.3. Magnetic field stratification in the model atmospheres

The semi-empirical models shown in Tables A.1, A.2, and A.3 have a constant magnetic field with height. The Mg spectra were synthesized by averaging the value of B_{LOS} and B_{HOR} between $\log \tau = [-6, -2]$ for the penumbra and only B_{LOS} for the umbra, where the sensitivity of the Ca II 8542 Å would be maximum (Quintero Noda et al. 2016). This approach ensures the B_{LOS} does not change polarity with height as obtained from the NICOLE inversions (Fig. 2) and provides a more consistent picture of the magnetic field. The B_{HOR} for the umbra was set to zero for all heights and the model describing the quiet surroundings does not include magnetic field.

4.4. Synthetic versus observed spectroheliograms

We generated spectroheliograms from both the IRIS observations and RH1.5D synthesis and compare them in Fig. 7. They were integrated over 0.6 Å windows around 2796.2 Å (k_{2v}), 2803.33 Å (h_{2v}), and 2794.7 Å (wing). Because IRIS was observing an eight-step sparse raster with 1'' steps of the 0'33 wide spectrograph slit, there are gaps with missing data in the x direction. For an easier visual comparison of the raster maps, we widened the data to fill the gaps. This further emphasizes the difference in resolution between IRIS and the synthetic profiles (derived from SST observations). Nevertheless, the synthetic images agree well with the IRIS observations, highlighting the reliability of the semi-empirical models used to generate them.

4.5. Deeper k_3 and h_3 line cores

The most distinct difference between the observed and the synthetic spectra is the relatively cooler k_3 and h_3 line cores in the synthetic profiles for almost all the pixels in the FOV. This is clear from Fig. 3. This can be explained by the fact that the Mg II h and k line cores form higher than the Ca 8542 line core.

Therefore, the sensitivity of the inversions is fairly low at such heights, which has an impact on the validity of the resulting models in those locations. Studies by [Leenaarts et al. \(2013a,b\)](#) and [Pereira et al. \(2015\)](#), for example, have shown that the peak sensitivity of the Mg II line core is typically less than 200 km below the TR (or around heights between 2 and 3 Mm in their model). The inverted model atmospheres obtained from Ca 8542 are certainly not sensitive to those heights.

As shown in [Carlsson et al. \(2015\)](#), single-peaked or flat-topped profiles in Mg can possibly be explained by shifting the TR to a higher column mass. Though this approach fills up the k_3 minimum in the synthetic profiles to some extent, their best fit model still has some central reversal unlike the observations. Nevertheless, this mechanism can indeed provide a good starting point in investigating the single peaked profiles. In our analysis, the initial guess model (FAL-C) has the TR at a lower column mass. NICOLE does not change or attempt to fit the uppermost point of the reference hydro-dynamical variable (in our case electron pressure), which makes it hard for the TR to shift greatly in column mass. More recent codes such as STiC ([de la Cruz Rodríguez et al. 2019](#)) have a mechanism to allow changes to the boundary condition and thus may be able to address the core of such profiles in the future. Nonetheless, the 1.5D approach works well in reproducing the h&k line profiles outside the very cores, and lets us select a number of interesting semi-empirical candidate atmospheric models, which is the main intent of this paper.

4.6. Where do our models stand in comparison with earlier approaches?

There have been some attempts in the past to model sunspot atmospheres but they have been mostly restricted to the photosphere ([del Toro Iniesta et al. 1994](#); [Roupe van der Voort 2002](#); [Fontenla et al. 2006](#)). Out of these, the models from [del Toro Iniesta et al. \(1994\)](#) and [Roupe van der Voort \(2002\)](#) were based on spectral inversions, whereas [Fontenla et al. \(2006\)](#) used a “radiation-effective” forward modeling approach to construct the semi-empirical model atmospheres. [Fontenla et al. \(2009\)](#), also based on a forward modeling approach) was an improvement over the former ([Fontenla et al. 2006](#)) model atmospheres due to the fact that it was the first time that they introduced upper-chromospheric layers into these models for the quiet Sun and active region features, and they further computed the spectra from these semi-empirical model atmospheres to compare with the actual observations. However, comparisons with the observed upper chromospheric spectra of Ca II H&K and Mg II h&k (see also [Fontenla et al. 2011](#)) revealed that there was a significant mismatch between the two, thereby highlighting the shortcomings in their models. One of the major reasons was the lack of PRD in their radiative transfer calculations. We, on the other hand, took PRD into consideration while computing the spectra from our model atmospheres presented in this paper, and ended up with reasonable matches with the observed IRIS Mg II spectra for a number of pixels over a sunspot. This enhanced the strength and the applicability of our models.

[Lites & Skumanich \(1982\)](#) proposed an umbral model for the upper chromosphere and TR based on the observations in the Lyman α , Ca II H&K, and Mg II h&k spectra. Their models did not account for the magnetic field, but they performed radiative transfer calculations under PRD. Assuming a strong down-flow of about 40 km s^{-1} on top of their model atmosphere, they were able to reproduce the observed asymmetries in the umbral line profiles. They further showed that the profiles are sensitive

to temperature and both the LOS and microturbulent velocity, which we also find in our investigation. However, neither their observations included a flash, nor could they reproduce the single emission profiles that are mostly observed in the umbra. Nevertheless, it remains one of the earliest known attempts to obtain an umbral atmosphere that intends to describe the blue-red peak asymmetry in the Mg line profile. [Maltby et al. \(1986\)](#) also provided a semi-empirical model atmosphere for the dark umbral cores and their variation with the solar cycle that remains, along with [Lites & Skumanich \(1982\)](#), one of the earliest known models for the chromosphere of the umbra. However, we propose an umbral model in this paper that has a supersonic down-flow associated with it, similar to [Henriques et al. \(2017\)](#), but supported further by Mg II observations.

The temperature stratification of the penumbral models presented in this paper not only compares reasonably well with [del Toro Iniesta et al. \(1994\)](#), [Roupe van der Voort \(2002\)](#), and [Fontenla et al. \(2006\)](#) down to the photosphere, but it also extends higher up into the chromosphere. For the sake of completeness, we show also the temperature stratification of our models together with that of [Socas-Navarro \(2007, Model-C\)](#) in the left-panel Fig. 8 as a function of $\log \tau_{5000}$. As far as we are aware, the latter is the only complete chromospheric model for the penumbra, including hydrodynamical variables, preceding this work. More recently, [Joshi & de la Cruz Rodríguez \(2018\)](#) modeled the temperature and V_{LOS} stratification as a function of optical depth and up to $\log \tau = -5.5$, for the average quiescent and flash atmosphere of a sunspot, including both umbral flashes and running penumbral waves. Their models indicate that the temperature is hotter by about 0.2–0.5 kK in a running penumbral wave atmosphere between $\log \tau = -4.5$ and -5 . They also find an increase in velocity of 1 km s^{-1} in LOS velocity when a wave is present in the penumbra.

The temperature variation of six different models in Fig. 8, corresponds to the six penumbral profiles in Fig. 3. This also includes the cool and the hot penumbra. It is apparent that the cool models depart from their hot counterparts around $\log \tau = -5.5$, which is well within the sensitivity of both the Ca II 8542 core and Mg II k_2 peaks, with the sensitivity extending somewhat further upwards in the solar atmosphere. This is evident from the contribution function distributions that are also shown in the left panel of Fig. 8. This departure is stronger than other variations at lower heights and occurs at optical depths not modeled in any previous work. Being close to the limit of detection, it may be that this departure can only be identified with the benefit of a slight inclination in the LOS (that being $\mu = 0.745$ in this case), which slightly increases the length of our atmosphere that is under upper chromospheric conditions. From the figure it is also clear that the height dependence of our derived models is rather gradual and smooth, unlike the Model-C by [Socas-Navarro \(2007\)](#) that has large uncertainties beyond $\log \tau = -5$. This is perhaps due to the earlier lack of adequate data to properly constrain the inversions. All the penumbral models shown in the left panel of Fig. 8 have their TR shifted deeper, as measured in the $\log \tau_{5000}$ scale, compared to the FAL-C atmosphere. For the sake of completeness, we also show the temperature stratification of our hot penumbra and the quiet surrounding model, along with a purely photospheric penumbral model from [Fontenla et al. \(2006\)](#) in the right panel of Fig. 8.

The approaches by the various authors described above yielded several atmospheres over the past years. However, as discussed, a model complete with hydro-dynamical variables, which is effectively constrained from the photosphere to the chromosphere, is found to be lacking for sunspots, especially for

Fig. 8. Comparison of the temperature stratification with optical depth for the different penumbral atmospheres indicated in Fig. 3. *Left panel:* temperature stratification of six different models corresponding to the six different pixels in the penumbra of the sunspot as a function of optical depth. The model with the lowest uncertainty from Socas-Navarro (2007), is also shown for the sake of comparison. Contribution functions computed from the cool penumbral model for the Mg II k_{2v} , Ca II 8542 core, and Ca II wing-averaged over the wavelength range between 8541.15 Å and 8542.28 Å, are plotted (in arbitrary units) with solid, dash-dotted, and dashed lines, respectively. *Right panel:* temperature stratification as a function of geometric and optical depth of our hot penumbral and quiet surrounding model compared to the purely photospheric model-R of Fontenla et al. (2006).

the penumbra. We hope that the models proposed in this paper will fill that void and be used as useful references or starting atmospheres to describe the penumbra of sunspots in the future.

5. Conclusions

The goal of this work is to obtain semi-empirical model atmospheres for a sunspot that work well for both the Ca II and Mg II spectra and are well constrained from the photosphere to the chromosphere. We chose to invert the chromospheric Ca II 8542 Å full Stokes profiles observed with the CRISP instrument at the SST, with the NICOLE inversion code to obtain the model atmospheres. To test the strength of the models, we synthesized Mg II h&k line profiles with the help of the RH1.5D radiative transfer code with the chromospheric models as inputs.

The synthetic spectra were compared with co-temporal and co-spatial IRIS observations over the full FOV. Detailed comparisons showed that our models reasonably reproduced the entire observed spectra of the penumbra, an umbral flash, and a quiet surrounding region of the sunspot, with the exception of the line cores. Since the Mg II lines are sensitive to the upper chromospheric conditions, this comparison served as a consistency check for the models that have been obtained purely from Ca II 8542 inversions. It also indicated how well our models were constrained across multiple heights in the solar atmosphere. Based on these matches, we propose two penumbral models (hot penumbra and cool penumbra) in Tables A.1 and A.2, respectively, reflecting a departure in temperature observed in the upper chromosphere.

Comparing the temperatures we obtain over the formation range of the Mg II h&k peaks with those of Jafarzadeh et al.

(2019) for Atacama Large Millimeter/submillimeter Array’s (ALMA: Wootten & Thompson 2009) band 6 (1.3 mm), we find a good match for the penumbral case (6–7 kK in both works). This suggests that ALMA’s band 6 forms at the same height as the peaks of the k_2 and h_2 when non-LTE is accounted for, or slightly higher, likely in the h_3 and k_3 range, once one considers the difference in the observing angle.

The umbral model as described in Table A.3 reproduces the profiles of a typical umbral flash, but with supersonic down-flows reaching a maximum of 12 km s^{-1} in the upper layers of the solar atmosphere. We found that velocities such as these are essential to account for the strong blue-red peak asymmetries as observed in Mg II h_{2v} and h_{2r} and also k_{2v} and k_{2r} umbral spectra. Based on recently published works, we also speculate that stronger down-flows of the order of $30\text{--}40 \text{ km s}^{-1}$ could be present in the upper chromosphere and the TR in strong umbral flashes that may have a relation to coronal loops rooted deep into the umbra.

Furthermore, we also find that a slightly modified atmosphere, 75 K colder than the one obtained from inversions, leads to a much better match in the far wings for the Mg II quiet-sun-like profiles, which otherwise have a distinct mismatch. This behavior shows the strong dependence of the majority of Mg II profiles on temperature. We describe the quiet surrounding atmosphere in Table A.4.

In all cases, we obtain models that reproduce all spectral features with the exception of the Mg II k_3 and h_3 line cores. Our procedure is limited by Ca II 8542 spectra not being sensitive to the height of formation of k_3 and h_3 . We anticipated that large changes at heights where Ca II 8542 is not very sensitive would, as part of the single-line fitting procedure, lead to some selected atmospheres that would approximately reproduce

the k_3 and h_3 line cores. However, the bias at heights where sensitivity is low seems to go in the direction of producing colder atmospheres. This, along with the fact that NICOLE cannot move the TR to a higher column mass, may have prevented the reproduction of line cores. Furthermore, when dealing with active regions it may be necessary to adjust the upper boundary condition in NICOLE, namely the value of the hydrodynamic parameter used as a starting point for the hydrostatic equilibrium stratification, an adjustment that this method does not allow. These reasons must contribute to deeper and cooler cores in the synthesized spectra and can be taken into account in future investigations. Apart from these discrepancies, it is important to understand that we compare profiles obtained from two different but overlapping height ranges in the solar atmosphere, using data that were recorded from two different instruments. The matches between the observed and the synthetic profiles for both the Mg II h&k spectral region and the Ca II 8542 line, allow us to put forward semi-empirical models for the chromosphere with a higher degree of confidence than possible in previous works. Our results also highlight the consistency between the two independent radiative transfer codes.

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References

- Asensio Ramos, A., Trujillo Bueno, J., & Landi Degl'Innocenti, E. 2008, *ApJ*, **683**, 542
- Asplund, M., Grevesse, N., Sauval, A. J., & Scott, P. 2009, *ARA&A*, **47**, 481
- Avrett, E. H. 2003, in *Current Theoretical Models and Future High Resolution Solar Observations: Preparing for ATST*, eds. A. A. Pevtsov, & H. Uitenbroek, *ASP Conf. Ser.*, **286**, 419
- Bard, S., & Carlsson, M. 2010, *ApJ*, **722**, 888
- Beckers, J. M., & Tallant, P. E. 1969, *Sol. Phys.*, **7**, 351
- Brault, J. W., & Neckel, H. 1987, *Spectral Atlas of Solar Absolute Disk-averaged and Disk-Center Intensity from 3290 to 12510 Å*, <ftp://ftp.hs.uni-hamburg.de/pub/outgoing/FTS-Atlas>
- Carlsson, M. 1986, *Uppsala Astron. Observatory Rep.*, **33**
- Carlsson, M., & Stein, R. F. 1997, *ApJ*, **481**, 500
- Carlsson, M., Leenaarts, J., & De Pontieu, B. 2015, *ApJ*, **809**, L30
- Chitta, L. P., Peter, H., & Young, P. R. 2016, *A&A*, **587**, A20
- de la Cruz Rodríguez, J., & Piskunov, N. 2013, *ApJ*, **764**, 33
- de la Cruz Rodríguez, J., & van Noort, M. 2017, *Space Sci. Rev.*, **210**, 109
- de la Cruz Rodríguez, J., Kiselman, D., & Carlsson, M. 2011, *A&A*, **528**, A113
- de la Cruz Rodríguez, J., Rouppe van der Voort, L., Socas-Navarro, H., & van Noort, M. 2013, *A&A*, **556**, A115
- de la Cruz Rodríguez, J., Löfdahl, M. G., Sütterlin, P., & Hillberg, T. 2015a, *A&A*, **573**, A40
- de la Cruz Rodríguez, J., Hansteen, V., Bellot-Rubio, L., & Ortiz, A. 2015b, *ApJ*, **810**, 145
- de la Cruz Rodríguez, J., Leenaarts, J., & Asensio Ramos, A. 2016, *ApJ*, **830**, L30
- de la Cruz Rodríguez, J., Leenaarts, J., Danilovic, S., & Uitenbroek, H. 2019, *A&A*, **623**, A74
- De Pontieu, B., Title, A. M., Lemen, J. R., et al. 2014, *Sol. Phys.*, **289**, 2733
- del Toro Iniesta, J. C., & Ruiz Cobo, B. 2016, *Liv. Rev. Sol. Phys.*, **13**, 4
- del Toro Iniesta, J. C., Tarbell, T. D., & Ruiz Cobo, B. 1994, *ApJ*, **436**, 400
- Felipe, T., Socas-Navarro, H., & Khomenko, E. 2014, *ApJ*, **795**, 9
- Fontenla, J. M., Avrett, E. H., & Loeser, R. 1993, *ApJ*, **406**, 319
- Fontenla, J. M., Avrett, E., Thuillier, G., & Harder, J. 2006, *ApJ*, **639**, 441
- Fontenla, J. M., Curdt, W., Haberleiter, M., Harder, J., & Tian, H. 2009, *ApJ*, **707**, 482
- Fontenla, J. M., Harder, J., Livingston, W., Snow, M., & Woods, T. 2011, *J. Geophys. Res. (Atmos.)*, **116**, D20108
- Gingerich, O., Noyes, R. W., Kalkofen, W., & Cuny, Y. 1971, *Sol. Phys.*, **18**, 347
- Henriques, V. M. J. 2012, *A&A*, **548**, A114
- Henriques, V. M. J., Mathioudakis, M., Socas-Navarro, H., & de la Cruz Rodríguez, J. 2017, *ApJ*, **845**, 102
- Jafarzadeh, S., Wedemeyer, S., Szydlarski, M., et al. 2019, *A&A*, **622**, A150
- Joshi, J., & de la Cruz Rodríguez, J. 2018, *A&A*, **619**, A63
- Kleint, L., Antolin, P., Tian, H., et al. 2014, *ApJ*, **789**, L42
- Lagg, A., Ishikawa, R., Merenda, L., et al. 2009, in *The Second Hinode Science Meeting: Beyond Discovery-Toward Understanding*, eds. B. Lites, M. Cheung, T. Magara, J. Mariska, & K. Reeves, *ASP Conf. Ser.*, **415**, 327
- Leenaarts, J., & Carlsson, M. 2009, in *The Second Hinode Science Meeting: Beyond Discovery-Toward Understanding*, eds. B. Lites, M. Cheung, T. Magara, J. Mariska, & K. Reeves, *ASP Conf. Ser.*, **415**, 87
- Leenaarts, J., Carlsson, M., Hansteen, V., & Rouppe van der Voort, L. 2009, *ApJ*, **694**, L128
- Leenaarts, J., Pereira, T., & Uitenbroek, H. 2012, *A&A*, **543**, A109
- Leenaarts, J., Pereira, T. M. D., Carlsson, M., Uitenbroek, H., & De Pontieu, B. 2013a, *ApJ*, **772**, 90
- Leenaarts, J., Pereira, T. M. D., Carlsson, M., Uitenbroek, H., & De Pontieu, B. 2013b, *ApJ*, **772**, 89
- Leenaarts, J., de la Cruz Rodríguez, J., Kochukhov, O., & Carlsson, M. 2014, *ApJ*, **784**, L17
- Lites, B. W., & Skumanich, A. 1982, *ApJS*, **49**, 293
- Maltby, P., Avrett, E. H., Carlsson, M., et al. 1986, *ApJ*, **306**, 284
- Milić, I., & van Noort, M. 2018, *A&A*, **617**, A24
- Neckel, H. 1999, *Sol. Phys.*, **184**, 421
- Nelson, C. J., Henriques, V. M. J., Mathioudakis, M., & Keenan, F. P. 2017, *A&A*, **605**, A14
- Pereira, T. M. D., & Uitenbroek, H. 2015, *A&A*, **574**, A3
- Pereira, T. M. D., Leenaarts, J., De Pontieu, B., Carlsson, M., & Uitenbroek, H. 2013, *ApJ*, **778**, 143
- Pereira, T. M. D., Carlsson, M., De Pontieu, B., & Hansteen, V. 2015, *ApJ*, **806**, 14
- Quintero Noda, C., Shimizu, T., de la Cruz Rodríguez, J., et al. 2016, *MNRAS*, **459**, 3363
- Rouppe van der Voort, L. H. M. 2002, *A&A*, **389**, 1020
- Ruiz Cobo, B., & del Toro Iniesta, J. C. 1992, *ApJ*, **398**, 375
- Samanta, T., Tian, H., & Prasad Choudhary, D. 2018, *ApJ*, **859**, 158
- Scharmer, G. B. 1984, in *Accurate Solutions to Non-LTE Problems Using Approximate Lambda Operators*, ed. W. Kalkofen, 173
- Scharmer, G. B., & Carlsson, M. 1985, *J. Comput. Phys.*, **59**, 56
- Scharmer, G. B., Bjelksjö, K., Korhonen, T. K., Lindberg, B., & Petterson, B. 2003, in *Innovative Telescopes and Instrumentation for Solar Astrophysics*, eds. S. L. Keil, & S. V. Avakyan, *Proc. SPIE*, **4853**, 341
- Scharmer, G. B., Narayan, G., Hillberg, T., et al. 2008, *ApJ*, **689**, L69
- Socas-Navarro, H. 2007, *ApJS*, **169**, 439
- Socas-Navarro, H., Trujillo Bueno, J., & Ruiz Cobo, B. 2000a, *ApJ*, **544**, 1141
- Socas-Navarro, H., Trujillo Bueno, J., & Ruiz Cobo, B. 2000b, *Science*, **288**, 1396
- Socas-Navarro, H., de la Cruz Rodríguez, J., Asensio Ramos, A., Trujillo Bueno, J., & Ruiz Cobo, B. 2015, *A&A*, **577**, A7
- Straus, T., Fleck, B., & Andretta, V. 2015, *A&A*, **582**, A116
- Sukhorukov, A. V., & Leenaarts, J. 2017, *A&A*, **597**, A46
- Uitenbroek, H. 1989, *A&A*, **213**, 360
- Uitenbroek, H. 2001, *ApJ*, **557**, 389
- van Noort, M., Rouppe van der Voort, L., & Löfdahl, M. G. 2005, *Sol. Phys.*, **228**, 191
- Vernazza, J. E., Avrett, E. H., & Loeser, R. 1981, *ApJS*, **45**, 635
- Vissers, G., & Rouppe van der Voort, L. 2012, *ApJ*, **750**, 22
- Wootten, A., & Thompson, A. R. 2009, *IEEE Proc.*, **97**, 1463

Appendix A: Tabulated form of the semi-empirical models

(Table A.3), and the quiet surrounding (Table A.4), respectively, in a standard table format. These tables are available at the CDS.

In this appendix, we provide the model atmospheres for the cool (Table A.2), and hot penumbra (Table A.1), umbral flash

Table A.1. Semi-empirical model atmospheric parameters for the hot penumbra.

$\log \tau_{5000}$	Height (km)	Temperature (K)	V_{LOS} (m s^{-1})	V_{micro} (m s^{-1})	$N_{\text{H}_{\text{tot}}}$ (m^{-3})	N_{e} (m^{-3})	ρ (kg m^{-3})
-8.000	1744.147	88 415.80	2801.12	11342.74	4.941e+05	8.212e+15	2.236e-11
-7.767	1743.714	35 886.21	2636.51	9921.28	1.351e+07	2.031e+16	5.531e-11
-7.744	1743.103	28 736.84	2619.55	9603.69	4.265e+07	2.537e+16	6.910e-11
-7.716	1742.474	21 448.55	2598.28	9230.50	3.115e+08	3.275e+16	9.379e-11
-7.688	1741.958	16 452.96	2576.94	8904.13	5.090e+09	4.267e+16	1.225e-10
-7.670	1741.677	14 563.79	2563.49	8750.85	2.616e+10	4.821e+16	1.384e-10
-7.650	1741.375	13 281.36	2547.98	8629.99	1.005e+11	5.288e+16	1.519e-10
-7.619	1740.932	12 438.50	2524.56	8527.31	2.811e+11	5.644e+16	1.624e-10
-7.569	1740.181	11 755.87	2485.82	8421.37	7.181e+11	5.955e+16	1.724e-10
-7.493	1738.929	11 153.57	2426.15	8320.97	1.792e+12	6.221e+16	1.829e-10
-7.367	1736.366	11 025.04	2326.12	8290.33	2.231e+12	6.314e+16	1.865e-10
-7.181	1731.037	10 720.53	2177.02	8224.20	3.797e+12	6.526e+16	1.951e-10
-6.970	1721.974	10 265.58	2011.09	8124.05	8.916e+12	6.922e+16	2.095e-10
-6.749	1707.465	9715.99	1844.65	7988.06	2.802e+13	7.593e+16	2.312e-10
-6.526	1686.144	8856.01	1690.74	7735.67	2.137e+14	8.882e+16	2.712e-10
-6.309	1658.224	7795.31	1559.66	7304.40	4.410e+15	1.091e+17	3.418e-10
-6.117	1624.854	7028.60	1462.92	6763.86	5.158e+16	1.145e+17	4.578e-10
-5.941	1574.098	6557.72	1394.07	6236.97	1.917e+17	9.365e+16	7.011e-10
-5.813	1513.174	6329.25	1356.97	5795.15	3.791e+17	8.313e+16	1.091e-09
-5.718	1450.404	6170.02	1337.55	5436.53	6.566e+17	7.788e+16	1.707e-09
-5.629	1377.409	6035.16	1322.88	5094.15	1.166e+18	7.684e+16	2.868e-09
-5.545	1297.198	5917.21	1308.94	4743.88	2.138e+18	7.918e+16	5.097e-09
-5.462	1213.885	5811.51	1295.43	4372.04	3.987e+18	8.403e+16	9.343e-09
-5.378	1131.328	5721.67	1281.85	3966.16	7.399e+18	9.193e+16	1.718e-08
-5.292	1053.377	5621.87	1268.10	3560.69	1.340e+19	9.640e+16	3.095e-08
-5.204	981.679	5530.10	1253.97	3173.21	2.334e+19	1.007e+17	5.373e-08
-5.108	915.365	5437.09	1238.75	2799.66	3.935e+19	1.027e+17	9.041e-08
-5.005	853.993	5324.35	1222.61	2472.34	6.470e+19	9.790e+16	1.485e-07
-4.898	797.356	5181.83	1206.00	2156.96	1.043e+20	8.519e+16	2.392e-07
-4.788	744.541	5024.00	1189.04	1900.43	1.656e+20	7.182e+16	3.797e-07
-4.674	695.532	4832.58	1171.63	1639.21	2.605e+20	5.969e+16	5.971e-07
-4.561	653.802	4597.13	1154.41	1419.12	3.962e+20	5.659e+16	9.082e-07
-4.447	622.481	4407.45	1137.25	1265.00	5.528e+20	6.721e+16	1.267e-06
-4.328	597.786	4272.76	1119.65	1128.31	7.230e+20	8.015e+16	1.657e-06
-4.195	574.639	4191.44	1099.93	1012.22	9.263e+20	9.434e+16	2.123e-06
-4.034	549.903	4133.98	1076.47	911.45	1.203e+21	1.120e+17	2.758e-06
-3.831	520.729	4101.84	1047.05	822.50	1.631e+21	1.389e+17	3.737e-06
-3.561	483.854	4100.38	1008.59	727.04	2.376e+21	1.871e+17	5.447e-06
-3.204	436.227	4114.42	954.39	628.79	3.813e+21	2.769e+17	8.827e-06
-2.814	384.834	4168.77	878.54	525.51	6.337e+21	4.386e+17	1.467e-05
-2.420	333.047	4256.59	785.46	478.56	1.039e+22	7.174e+17	2.408e-05
-2.024	280.491	4367.86	677.34	533.85	1.689e+22	1.195e+18	3.912e-05
-1.626	226.800	4493.61	556.53	627.63	2.729e+22	2.003e+18	6.323e-05
-1.231	172.810	4632.97	426.63	842.48	4.348e+22	3.342e+18	1.008e-04
-0.885	123.237	4878.05	339.81	1060.48	6.401e+22	5.723e+18	1.482e-04
-0.585	77.334	5237.55	308.28	1254.70	8.724e+22	9.795e+18	2.018e-04
-0.273	28.924	5819.11	309.23	1440.88	1.145e+23	2.281e+19	2.624e-04
0.111	-14.283	6756.06	344.39	1611.76	1.317e+23	1.227e+20	3.020e-04
0.512	-39.556	7928.25	403.81	1688.35	1.284e+23	7.189e+20	2.960e-04
0.909	-57.325	9022.77	466.76	1740.88	1.195e+23	2.526e+21	2.802e-04

Notes. The B_{LOS} is equal to 214.48 G and B_{HOR} is equal to 146.5 G for all heights.

Table A.2. Semi-empirical model atmospheric parameters for the cool penumbra.

$\log \tau_{5000}$	Height (km)	Temperature (K)	V_{LOS} (m s^{-1})	V_{micro} (m s^{-1})	$N_{\text{H}_{\text{igt}}}$ (m^{-3})	N_{e} (m^{-3})	ρ (kg m^{-3})
-8.000	1725.286	87 122.94	728.22	8454.59	5.154e+05	8.334e+15	2.269e-11
-7.767	1724.869	34 579.29	869.62	7415.96	1.614e+07	2.108e+16	5.740e-11
-7.744	1724.282	27 427.06	884.57	7183.91	5.596e+07	2.658e+16	7.243e-11
-7.716	1723.682	20 134.96	903.39	6911.22	5.423e+08	3.484e+16	9.995e-11
-7.688	1723.202	15 135.31	922.36	6672.75	1.533e+10	4.637e+16	1.331e-10
-7.670	1722.946	13 243.49	934.35	6560.75	1.048e+11	5.300e+16	1.522e-10
-7.650	1722.673	11 957.92	948.22	6472.44	5.361e+11	5.849e+16	1.689e-10
-7.619	1722.273	11 110.17	969.21	6397.42	1.901e+12	6.209e+16	1.828e-10
-7.569	1721.591	10 419.21	1004.11	6320.01	6.118e+12	6.512e+16	1.964e-10
-7.493	1720.463	9803.81	1058.20	6246.65	1.970e+13	6.897e+16	2.098e-10
-7.367	1718.176	9654.15	1149.56	6224.26	2.706e+13	7.048e+16	2.146e-10
-7.181	1713.479	9325.36	1286.67	6175.94	5.588e+13	7.395e+16	2.254e-10
-6.970	1705.646	8864.21	1439.43	6102.76	1.689e+14	7.968e+16	2.432e-10
-6.749	1693.278	8347.34	1591.21	6003.40	6.782e+14	8.797e+16	2.695e-10
-6.526	1675.111	7607.47	1728.20	5818.98	6.356e+15	1.002e+17	3.187e-10
-6.309	1647.528	6754.56	1839.46	5503.86	8.152e+16	8.864e+16	4.439e-10
-6.117	1591.181	6215.44	1914.82	5108.90	2.657e+17	5.464e+16	7.546e-10
-5.941	1483.928	5963.00	1960.29	4723.91	6.653e+17	4.908e+16	1.650e-09
-5.813	1387.891	5888.87	1977.50	4401.08	1.352e+18	5.880e+16	3.246e-09
-5.718	1314.753	5835.11	1980.54	4139.05	2.317e+18	6.773e+16	5.479e-09
-5.629	1247.096	5786.99	1977.29	3888.88	3.819e+18	7.743e+16	8.943e-09
-5.545	1184.271	5737.75	1970.53	3632.94	6.093e+18	8.675e+16	1.418e-08
-5.462	1125.302	5682.96	1960.77	3361.24	9.488e+18	9.457e+16	2.197e-08
-5.378	1068.843	5626.97	1948.01	3064.68	1.456e+19	1.019e+17	3.360e-08
-5.292	1014.794	5557.02	1932.29	2768.41	2.209e+19	1.051e+17	5.088e-08
-5.204	963.200	5495.71	1913.47	2485.28	3.300e+19	1.098e+17	7.589e-08
-5.108	913.011	5435.00	1890.51	2212.34	4.897e+19	1.144e+17	1.125e-07
-5.005	864.302	5355.64	1863.51	1973.17	7.245e+19	1.132e+17	1.663e-07
-4.898	817.129	5246.05	1833.40	1742.73	1.073e+20	1.033e+17	2.461e-07
-4.788	771.021	5119.95	1800.76	1555.29	1.592e+20	9.090e+16	3.652e-07
-4.674	725.797	4958.57	1765.94	1364.42	2.389e+20	7.572e+16	5.477e-07
-4.561	683.237	4749.79	1730.84	1203.60	3.596e+20	6.418e+16	8.243e-07
-4.447	647.910	4583.05	1696.00	1090.99	5.114e+20	6.980e+16	1.172e-06
-4.328	619.563	4467.54	1661.16	991.12	6.814e+20	8.398e+16	1.562e-06
-4.195	593.137	4401.64	1624.25	906.29	8.871e+20	1.034e+17	2.033e-06
-4.034	565.973	4353.16	1585.00	832.66	1.162e+21	1.285e+17	2.664e-06
-3.831	534.992	4321.13	1546.21	767.67	1.578e+21	1.648e+17	3.616e-06
-3.561	496.785	4302.75	1520.46	697.92	2.295e+21	2.242e+17	5.260e-06
-3.204	448.469	4276.44	1546.02	626.13	3.705e+21	3.254e+17	8.491e-06
-2.814	396.318	4301.86	1645.70	550.66	6.076e+21	5.012e+17	1.407e-05
-2.420	343.362	4367.05	1789.39	516.36	9.993e+21	7.975e+17	2.314e-05
-2.024	289.566	4450.60	1942.17	556.76	1.636e+22	1.286e+18	3.789e-05
-1.626	235.260	4551.44	2067.85	625.28	2.655e+22	2.091e+18	6.148e-05
-1.231	180.041	4673.97	2129.63	782.27	4.271e+22	3.439e+18	9.894e-05
-0.885	129.745	4869.13	2103.23	941.55	6.383e+22	5.666e+18	1.478e-04
-0.585	84.055	5133.40	2021.40	1083.47	8.877e+22	9.164e+18	2.053e-04
-0.273	34.528	5572.78	1892.92	1219.50	1.217e+23	1.731e+19	2.789e-04
0.111	-19.862	6267.29	1694.59	1344.36	1.593e+23	5.846e+19	3.651e-04
0.512	-59.310	7095.04	1468.08	1400.33	1.799e+23	2.529e+20	4.128e-04
0.909	-91.246	7829.55	1253.84	1438.71	1.938e+23	7.757e+20	4.461e-04

Notes. The B_{LOS} is equal to 1343.61 G and B_{HOR} is equal to 1561.73 G for all heights.

Table A.3. Semi-empirical model atmospheric parameters for the umbral flash.

$\log \tau_{5000}$	Height (km)	Temperature (K)	V_{LOS} (m s^{-1})	V_{micro} (m s^{-1})	$N_{\text{H}_{\text{tot}}}$ (m^{-3})	N_{e} (m^{-3})	ρ (kg m^{-3})
-8.000	1654.248	90 033.87	12 111.70	10 730.73	4.692e+05	8.064e+15	2.195e-11
-7.767	1653.794	37 810.17	11 824.80	9326.73	1.059e+07	1.928e+16	5.249e-11
-7.744	1653.146	30 694.74	11 796.83	9013.04	2.967e+07	2.376e+16	6.470e-11
-7.716	1652.472	23 449.14	11 762.00	8644.43	1.561e+08	3.037e+16	8.541e-11
-7.688	1651.901	18 496.46	11 727.24	8322.07	1.269e+09	3.796e+16	1.089e-10
-7.670	1651.583	16 634.27	11 705.45	8170.68	4.424e+09	4.222e+16	1.212e-10
-7.650	1651.236	15 382.89	11 680.35	8051.30	1.232e+10	4.567e+16	1.311e-10
-7.619	1650.718	14 586.59	11 642.57	7949.88	2.566e+10	4.821e+16	1.384e-10
-7.569	1649.831	13 979.85	11 580.16	7845.24	4.725e+10	5.038e+16	1.447e-10
-7.493	1648.341	13 490.22	11 483.74	7746.08	8.039e+10	5.237e+16	1.504e-10
-7.367	1645.260	13 532.87	11 319.21	7715.81	7.768e+10	5.254e+16	1.509e-10
-7.181	1638.772	13 420.09	11 059.57	7650.49	9.051e+10	5.372e+16	1.543e-10
-6.970	1627.627	13 041.14	10 734.64	7551.58	1.467e+11	5.661e+16	1.627e-10
-6.749	1609.696	12 340.98	10 345.11	7417.26	3.821e+11	6.218e+16	1.790e-10
-6.526	1583.246	11 088.77	9889.73	7167.97	2.677e+12	7.240e+16	2.138e-10
-6.309	1548.190	9517.37	9373.38	6741.99	5.820e+13	9.090e+16	2.770e-10
-6.117	1510.208	8256.89	8844.09	6208.09	1.522e+15	1.179e+17	3.625e-10
-5.941	1469.702	7353.24	8295.94	5687.68	2.718e+16	1.411e+17	4.870e-10
-5.813	1431.003	6843.85	7850.20	5251.28	1.281e+17	1.307e+17	6.715e-10
-5.718	1387.965	6508.08	7495.06	4897.07	2.934e+17	1.051e+17	9.613e-10
-5.629	1325.962	6230.52	7156.98	4558.89	5.787e+17	8.335e+16	1.545e-09
-5.545	1239.268	5991.23	6838.40	4212.93	1.196e+18	7.033e+16	2.918e-09
-5.462	1131.062	5785.73	6532.82	3845.65	2.749e+18	6.540e+16	6.461e-09
-5.378	1015.390	5616.16	6229.45	3444.76	6.648e+18	6.654e+16	1.540e-08
-5.292	908.743	5439.70	5926.76	3044.27	1.537e+19	6.377e+16	3.537e-08
-5.204	817.634	5267.88	5621.31	2661.55	3.228e+19	5.809e+16	7.411e-08
-5.108	740.030	5088.01	5299.66	2292.59	6.245e+19	4.945e+16	1.432e-07
-5.005	673.424	4883.30	4967.67	1969.29	1.136e+20	3.948e+16	2.604e-07
-4.898	618.331	4647.59	4637.78	1657.78	1.933e+20	3.361e+16	4.431e-07
-4.788	577.021	4397.33	4314.39	1404.41	2.992e+20	3.794e+16	6.858e-07
-4.674	548.312	4115.43	3998.50	1146.39	4.235e+20	4.504e+16	9.708e-07
-4.561	527.361	3796.38	3703.65	929.01	5.727e+20	4.050e+16	1.313e-06
-4.447	508.172	3530.97	3429.59	776.78	7.587e+20	2.871e+16	1.756e-06
-4.328	487.696	3328.18	3170.74	641.77	1.027e+21	1.994e+16	2.391e-06
-4.195	464.538	3184.40	2910.10	527.11	1.422e+21	1.675e+16	3.362e-06
-4.034	438.912	3077.41	2645.02	427.58	2.005e+21	1.705e+16	4.900e-06
-3.831	410.283	3050.59	2389.47	339.72	2.889e+21	2.185e+16	7.313e-06
-3.561	376.920	3148.82	2202.44	245.43	4.438e+21	3.698e+16	1.113e-05
-3.204	337.707	3349.05	2049.13	148.39	7.139e+21	8.060e+16	1.737e-05
-2.814	297.305	3473.04	1498.97	46.38	1.133e+22	1.496e+17	2.747e-05
-2.420	254.185	3469.77	751.60	0.00	1.856e+22	2.122e+17	4.629e-05
-2.024	208.486	3460.80	79.44	54.62	3.089e+22	3.074e+17	8.072e-05
-1.626	161.803	3477.48	-236.50	147.24	5.115e+22	4.749e+17	1.413e-04
-1.231	115.809	3548.18	81.02	359.46	8.408e+22	7.999e+17	2.403e-04
-0.885	77.213	3715.15	754.06	574.77	1.302e+23	1.484e+18	3.588e-04
-0.585	46.587	3965.82	1384.56	766.61	1.816e+23	2.999e+18	4.695e-04
-0.273	19.110	4399.76	2067.41	950.50	2.434e+23	7.884e+18	5.579e-04
0.111	-14.600	5101.98	2920.66	1119.28	2.825e+23	2.218e+19	6.475e-04
0.512	-60.880	5960.08	3787.71	1194.93	3.426e+23	5.926e+19	7.853e-04
0.909	-104.583	6729.88	4583.35	1246.82	4.047e+23	2.164e+20	9.281e-04

Notes. The B_{LOS} is equal to 3313.25 G and B_{HOR} is zero, for all heights.

Table A.4. Semi-empirical model atmospheric parameters for the quiet surrounding.

$\log \tau_{5000}$	Height (km)	Temperature (K)	V_{LOS} (m s^{-1})	V_{micro} (m s^{-1})	$N_{\text{H}_{\text{tot}}}$ (m^{-3})	N_{e} (m^{-3})	ρ (kg m^{-3})
-8.000	1865.676	89 004.53	909.94	13 303.88	4.848e+05	8.164e+15	2.221e-11
-7.767	1865.237	36 457.91	974.66	11 882.42	1.258e+07	2.007e+16	5.453e-11
-7.744	1864.616	29 306.78	981.31	11 564.83	3.833e+07	2.499e+16	6.789e-11
-7.716	1863.974	22 016.33	989.65	11 191.64	2.520e+08	3.208e+16	9.134e-11
-7.688	1863.442	17 018.64	998.02	10 865.27	3.305e+09	4.135e+16	1.181e-10
-7.670	1863.150	15 128.18	1003.30	10 711.99	1.539e+10	4.657e+16	1.330e-10
-7.650	1862.836	13 844.31	1009.40	10 591.13	5.401e+10	5.094e+16	1.455e-10
-7.619	1862.372	12 999.36	1018.61	10 488.45	1.391e+11	5.432e+16	1.552e-10
-7.569	1861.587	12 313.58	1033.90	10 382.51	3.327e+11	5.746e+16	1.644e-10
-7.493	1860.284	11 707.25	1057.57	10 282.11	7.743e+11	6.030e+16	1.736e-10
-7.367	1857.621	11 574.88	1097.73	10 251.47	9.553e+11	6.137e+16	1.771e-10
-7.181	1852.086	11 273.84	1159.15	10 185.34	1.550e+12	6.349e+16	1.848e-10
-6.970	1842.638	10 841.06	1230.73	10 085.19	3.262e+12	6.686e+16	1.977e-10
-6.749	1827.328	10 342.49	1307.69	9949.20	8.394e+12	7.210e+16	2.164e-10
-6.526	1804.379	9546.44	1386.20	9696.81	4.520e+13	8.300e+16	2.509e-10
-6.309	1773.802	8536.72	1462.71	9265.54	5.720e+14	1.022e+17	3.100e-10
-6.117	1739.139	7802.42	1530.14	8725.00	5.496e+15	1.242e+17	3.865e-10
-5.941	1699.475	7347.79	1590.71	8198.11	2.790e+16	1.432e+17	4.905e-10
-5.813	1663.136	7121.77	1634.33	7756.29	6.714e+16	1.544e+17	6.073e-10
-5.718	1630.667	6958.60	1666.05	7397.67	1.233e+17	1.587e+17	7.406e-10
-5.629	1594.551	6815.30	1695.07	7055.29	2.094e+17	1.605e+17	9.332e-10
-5.545	1553.203	6685.12	1722.39	6705.02	3.395e+17	1.608e+17	1.222e-09
-5.462	1505.071	6563.95	1748.57	6333.18	5.427e+17	1.614e+17	1.678e-09
-5.378	1448.031	6455.17	1774.54	5927.30	8.725e+17	1.652e+17	2.433e-09
-5.292	1380.786	6332.76	1800.42	5521.83	1.484e+18	1.678e+17	3.831e-09
-5.204	1301.957	6214.36	1826.52	5134.35	2.664e+18	1.752e+17	6.545e-09
-5.108	1210.525	6089.27	1853.97	4760.80	5.191e+18	1.860e+17	1.235e-08
-5.005	1109.752	5939.13	1882.26	4433.48	1.089e+19	1.916e+17	2.542e-08
-4.898	1007.872	5755.19	1910.33	4118.10	2.334e+19	1.812e+17	5.392e-08
-4.788	913.033	5552.68	1937.81	3861.57	4.890e+19	1.582e+17	1.124e-07
-4.674	827.766	5313.74	1964.60	3600.35	9.813e+19	1.202e+17	2.252e-07
-4.561	751.574	5030.49	1989.54	3380.26	1.916e+20	8.082e+16	4.393e-07
-4.447	689.063	4793.38	2012.68	3226.14	3.431e+20	6.805e+16	7.864e-07
-4.328	642.639	4611.21	2034.45	3089.45	5.372e+20	7.590e+16	1.231e-06
-4.195	606.191	4479.43	2056.29	2973.36	7.729e+20	9.647e+16	1.772e-06
-4.034	573.350	4368.14	2078.35	2872.60	1.084e+21	1.239e+17	2.484e-06
-3.831	539.644	4284.63	2099.33	2783.64	1.533e+21	1.593e+17	3.513e-06
-3.561	500.174	4251.23	2114.00	2688.19	2.269e+21	2.160e+17	5.200e-06
-3.204	450.950	4280.42	2094.87	2589.94	3.660e+21	3.293e+17	8.390e-06
-2.814	397.912	4366.82	1985.54	2486.65	5.956e+21	5.373e+17	1.379e-05
-2.420	343.609	4485.59	1791.30	2439.70	9.685e+21	8.927e+17	2.242e-05
-2.024	288.647	4628.22	1524.57	2495.00	1.557e+22	1.492e+18	3.605e-05
-1.626	231.283	4791.76	1198.88	2588.77	2.507e+22	2.522e+18	5.804e-05
-1.231	172.118	4978.11	831.86	2803.63	4.015e+22	4.292e+18	9.292e-05
-0.885	118.163	5236.73	484.64	3021.62	6.006e+22	7.249e+18	1.377e-04
-0.585	70.483	5566.51	172.68	3215.84	8.168e+22	1.287e+19	1.872e-04
-0.273	25.737	6083.30	-155.86	3402.02	1.031e+23	3.319e+19	2.363e-04
0.111	-13.797	6888.11	-557.48	3572.90	1.177e+23	1.461e+20	2.700e-04
0.512	-41.669	7849.90	-959.63	3649.49	1.198e+23	6.309e+20	2.761e-04
0.909	-65.000	8721.04	-1326.95	3702.02	1.190e+23	1.835e+21	2.771e-04

Notes. The magnetic field is absent in this case.

Appendix B: Uncertainties in the inverted atmospheric parameters.

In this appendix we provide an estimate of the uncertainties in tabulated form (indicated in Tables B.1–B.4), for the main atmospheric parameters and for each of the proposed atmospheric models, by using the inversion uncertainties as defined in Eq. (42) of [del Toro Iniesta & Ruiz Cobo \(2016\)](#). These are computed per height on the basis of the response functions and do not take into account that a change in a node will affect the atmosphere at all heights between such a node and the next. Furthermore, these uncertainties best apply to the inversion but do not reflect the selection procedure performed to select only models that also lead to Mg II h&k profiles that reproduce the observations.

Table B.1. Inversion uncertainties for the cool penumbra.

$\log \tau_{5000}$	Height (km)	σ_T (K)	$\sigma_{V_{\text{LOS}}}$ (m s ⁻¹)
-8.000	1725.29	2.41e+06	Unconstrained
-7.767	1724.87	75 687	Unconstrained
-7.744	1724.28	75 519	Unconstrained
-7.716	1723.68	1.16e+06	Unconstrained
-7.688	1723.20	3.89e+06	Unconstrained
-7.670	1722.95	75 520	3.87582e+09
-7.650	1722.67	145 298	2.74062e+09
-7.619	1722.27	65 477	4.27003e+06
-7.569	1721.59	49 919	604 313
-7.493	1720.46	74 840	235 983
-7.367	1718.18	67 594	95 582.8
-7.181	1713.48	52 340	29 101.7
-6.970	1705.65	33 572	26 215.9
-6.749	1693.28	20 767	15 094.3
-6.526	1675.11	8457	8927.92
-6.309	1647.53	1357	4454.89
-6.117	1591.18	263	1428.14
-5.941	1483.93	19	467.590
-5.813	1387.89	1.0	392.19
-5.718	1314.75	1.1	287.53
-5.629	1247.10	1.4	246.31
-5.545	1184.27	112	243.99
-5.462	1125.30	1.0	277.88
-5.378	1068.84	1.1	387.79
-5.292	1014.79	1.0	688.50
-5.204	963.200	41	1587.36
-5.108	913.011	1.0	936.64
-5.005	864.302	19	613.87
-4.898	817.129	1.0	579.29
-4.788	771.021	20	625.75
-4.674	725.797	1.0	788.91
-4.561	683.237	106	911.00
-4.447	647.910	3.5	1182.19
-4.328	619.563	217	2882.66
-4.195	593.137	8.0	3082.49
-4.034	565.973	60	4851.83
-3.831	534.992	120	4785.97
-3.561	496.785	73	2880.21
-3.204	448.469	60	1435.90
-2.814	396.318	35	1023.88
-2.420	343.362	21	1023.33
-2.024	289.566	15	1202.77
-1.626	235.260	13	1533.09
-1.231	180.041	14	1894.30
-0.8850	129.745	22	3328.24
-0.5850	84.0550	30	6020.62
-0.2730	34.5280	129	38 906.0
0.1110	-19.8620	7561	5.93534e+07
0.5120	-59.3100	26 951	2.22578e+09
0.9090	-91.2460	987 007	Unconstrained

Table B.2. Inversion uncertainties for the hot penumbra.

$\log \tau_{5000}$	Height (km)	σ_T (K)	$\sigma_{V_{\text{LOS}}}$ (m s ⁻¹)
-8.000	1744.15	118 612	Unconstrained
-7.767	1743.71	118 623	Unconstrained
-7.744	1743.10	118 562	Unconstrained
-7.716	1742.47	5.95e+06	Unconstrained
-7.688	1741.96	6.07e+06	Unconstrained
-7.670	1741.68	37496	Unconstrained
-7.650	1741.38	8490	Unconstrained
-7.619	1740.93	5441	6.47402e+10
-7.569	1740.18	7751	1.47092e+06
-7.493	1738.93	8143	318 707
-7.367	1736.37	117 993	123 977
-7.181	1731.04	116 613	45 272.1
-6.970	1721.97	116 031	28 301.1
-6.749	1707.46	25 796	16 165.0
-6.526	1686.14	11 798	9065.94
-6.309	1658.22	9115	5749.42
-6.117	1624.85	1358	3411.52
-5.941	1574.10	338	1525.96
-5.813	1513.17	191	1165.83
-5.718	1450.40	245	652.720
-5.629	1377.41	181	381.230
-5.545	1297.20	36	247.800
-5.462	1213.89	69	195.230
-5.378	1131.33	31	209.930
-5.292	1053.38	36	339.220
-5.204	981.679	39	848.060
-5.108	915.365	37	779.030
-5.005	853.993	71	626.160
-4.898	797.356	65	692.850
-4.788	744.541	73	777.870
-4.674	695.532	154	1008.00
-4.561	653.802	1.0	1224.20
-4.447	622.481	437	2752.99
-4.328	597.786	362	5826.92
-4.195	574.639	422	9630.23
-4.034	549.903	354	5907.76
-3.831	520.729	235	2768.92
-3.561	483.854	88	1296.33
-3.204	436.227	56	771.810
-2.814	384.834	31	688.420
-2.420	333.047	17	684.780
-2.024	280.491	11	792.890
-1.626	226.800	9.7	1011.89
-1.231	172.810	11	1160.48
-0.8850	123.237	17	1871.28
-0.5850	77.3340	23	3291.10
-0.2730	28.9240	94	20 742.6
0.1110	-14.2830	2464	4.19414e+06
0.5120	-39.5560	7167	2.97225e+11
0.9090	-57.3250	83 506	Unconstrained

Table B.3. Inversion uncertainties for the umbral flash.

$\log \tau_{5000}$	Height (km)	σ_T (K)	$\sigma_{V_{\text{LOS}}}$ (m s ⁻¹)
-8.000	1654.25	1.12e+07	Unconstrained
-7.767	1653.79	1.33e+07	Unconstrained
-7.744	1653.15	8.61e+06	Unconstrained
-7.716	1652.47	2787	Unconstrained
-7.688	1651.90	2787	Unconstrained
-7.670	1651.58	2787	2.44988e+10
-7.650	1651.24	2787	2.44988e+10
-7.619	1650.72	3057	3.03871e+09
-7.569	1649.83	459 809	2.86737e+09
-7.493	1648.34	1.77e+06	Unconstrained
-7.367	1645.26	3006	149 073
-7.181	1638.77	3362	169 516
-6.970	1627.63	3772	141 635
-6.749	1609.70	63 243	127 651
-6.526	1583.25	50 463	49 830.9
-6.309	1548.19	96 373	24 696.8
-6.117	1510.21	33 227	15 868.9
-5.941	1469.70	3963	10 947.3
-5.813	1431.	3081	10 031.6
-5.718	1387.96	814	5475.48
-5.629	1325.96	830	2644.51
-5.545	1239.27	430	1240.73
-5.462	1131.06	29	682.570
-5.378	1015.39	108	581.610
-5.292	908.743	66	847.070
-5.204	817.634	61	1299.57
-5.108	740.030	62	1086.93
-5.005	673.424	121	929.480
-4.898	618.331	166	1076.94
-4.788	577.021	261	1292.72
-4.674	548.312	297	1894.41
-4.561	527.361	536	2576.64
-4.447	508.172	780	2569.30
-4.328	487.696	352	2104.04
-4.195	464.538	594	1806.49
-4.034	438.912	586	2227.58
-3.831	410.283	548	3065.70
-3.561	376.920	875	4482.95
-3.204	337.707	109	1468.87
-2.814	297.305	38	3782.62
-2.420	254.185	30	3581.27
-2.024	208.486	50	12 757.9
-1.626	161.803	36	7170.65
-1.231	115.809	37	5882.61
-0.8850	77.2130	52	8824.87
-0.5850	46.5870	73	150 58.8
-0.2730	19.1100	301	82 536.7
0.1110	-14.6000	1834	2.29667e+08
0.5120	-60.8800	5302	1.90139e+11
0.9090	-104.583	132 329	Unconstrained

Table B.4. Inversion uncertainties for the quiet surrounding atmosphere.

$\log \tau_{5000}$	Height (km)	σ_T (K)	$\sigma_{V_{\text{LOS}}}$ (m s ⁻¹)
-7.767	1865.24	143 691	Unconstrained
-7.716	1863.97	143 691	Unconstrained
-7.650	1862.84	143 691	Unconstrained
-7.619	1862.37	143 691	Unconstrained
-7.569	1861.59	143 691	8.29600e+06
-7.367	1857.62	132.1	190 944
-7.181	1852.09	132.1	83 749.6
-6.970	1842.64	132.2	44 219.1
-6.749	1827.33	132.3	23 202.3
-6.526	1804.38	18 867.6	12 134.4
-6.309	1773.80	11 431.4	7238.16
-6.117	1739.14	2460.6	4711.14
-5.941	1699.47	1874.51	3069.99
-5.813	1663.14	64.5	3308.33
-5.718	1630.67	62.7	2420.50
-5.629	1594.55	59.7	1701.09
-5.545	1553.20	282.1	1147.10
-5.462	1505.07	108.2	743.14
-5.378	1448.03	140.	471.51
-5.292	1380.79	113.6	311.25
-5.204	1301.96	77.9	225.07
-5.108	1210.53	30.7	210.80
-5.005	1109.75	18.3	331.82
-4.898	1007.87	37.1	828.04
-4.788	913.033	29.5	360.19
-4.674	827.766	48.2	340.51
-4.561	751.574	81.7	454.13
-4.447	689.063	56.9	441.29
-4.328	642.639	53.6	1324.25
-4.195	606.191	76.8	2909.85
-4.034	573.350	58.7	5062.82
-3.831	539.644	59.2	2728.15
-3.561	500.174	123.6	1123.31
-3.204	450.950	76.3	667.40
-2.814	397.912	42.7	620.17
-2.420	343.609	23	641.39
-2.024	288.647	13.7	736.75
-1.626	231.283	11.4	955.91
-1.231	172.118	12.6	1368.50
-0.8850	118.163	18.3	2424.72
-0.5850	70.4830	27.2	4822.81
-0.2730	25.7370	126.2	29 102.8
0.1110	-13.7970	3107.6	1.8e+06
0.5120	-41.6690	12 459.6	Unconstrained
0.9090	-65.0000	64 260.6	Unconstrained