Global millimeter VLBI array survey of ultracompact extragalactic radio sources at 86 GHz[★]

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ABSTRACT

Context. Very long baseline interferometry (VLBI) observations at 86 GHz (wavelength, $\lambda = 3$ mm) reach a resolution of about $50 \mu\text{as}$, probing the collimation and acceleration regions of relativistic outflows in active galactic nuclei (AGN). The physical conditions in these regions can be studied by performing 86 GHz VLBI surveys of representative samples of compact extragalactic radio sources.

Aims. To extend the statistical studies of compact extragalactic jets, a large global 86 GHz VLBI survey of 162 compact radio sources was conducted in 2010–2011 using the Global Millimeter VLBI Array (GMVA).

Methods. The survey observations were made in a snapshot mode, with up to five scans per target spread over a range of hour angles in order to optimize the visibility coverage. The survey data attained a typical baseline sensitivity of 0.1 Jy and a typical image sensitivity of 5 mJy beam^{-1} , providing successful detections and images for all of the survey targets. For 138 objects, the survey provides the first ever VLBI images made at 86 GHz. Gaussian model fitting of the visibility data was applied to represent the structure of the observed sources and to estimate the flux densities and sizes of distinct emitting regions (components) in their jets. These estimates were used for calculating the brightness temperature (T_b) at the jet base (core) and in one or more moving regions (jet components) downstream from the core. These model-fit-based estimates of T_b were compared to the estimates of brightness temperature limits made directly from the visibility data, demonstrating a good agreement between the two methods.

Results. The apparent brightness temperature estimates for the jet cores in our sample range from 2.5×10^9 K to 1.3×10^{12} K, with the mean value of 1.8×10^{11} K. The apparent brightness temperature estimates for the inner jet components in our sample range from 7.0×10^7 K to 4.0×10^{11} K. A simple population model with a single intrinsic value of brightness temperature, T_0 , is applied to reproduce the observed distribution. It yields $T_0 = (3.77^{+0.10}_{-0.14}) \times 10^{11}$ K for the jet cores, implying that the inverse Compton losses dominate the emission. In the nearest jet components, $T_0 = (1.42^{+0.16}_{-0.19}) \times 10^{11}$ K is found, which is slightly higher than the equipartition limit of $\sim 5 \times 10^{10}$ K expected for these jet regions. For objects with sufficient structural detail detected, the adiabatic energy losses are shown to dominate the observed changes of brightness temperature along the jet.

Key words. galaxies: active – galaxies: jets – quasars: general – radio continuum: galaxies – techniques: interferometric – surveys

1. Introduction

Very long baseline interferometry (VLBI) observations at 86 GHz (wavelength, $\lambda = 3$ mm) enable detailed studies to be made of compact radio sources at a resolution of $\sim (40\text{--}100) \mu\text{as}$. This resolution corresponds to linear scales as small as $10^3\text{--}10^4$ Schwarzschild radii and uncovers the structure of the jet regions where acceleration and collimation of the flow

takes place (Vlahakis & Königl 2004; Lee et al. 2008, 2016; Asada et al. 2014; Boccardi et al. 2016; Mertens et al. 2016).

To date, five 86 GHz VLBI surveys have been conducted (Beasley et al. 1997; Lonsdale et al. 1998; Rantakyrö et al. 1998; Lobanov et al. 2000; Lee et al. 2008, see Table 1), with the total number of objects imaged reaching just over a hundred. No complete sample of objects imaged at 86 GHz has been established so far. Recent works (e.g., Homan et al. 2006; Cohen et al. 2007; Lister et al. 2016) have demonstrated that high-resolution studies of complete (or nearly complete) samples of compact jets yield a wealth of information about the intrinsic properties of compact extragalactic flows.

[★] The reduced images and visibility tables (FITS files) and the full Tables 5–7 are only available at the CDS via anonymous ftp to [cdsarc.u-strasbg.fr](ftp://cdsarc.u-strasbg.fr) (130.79.128.5) or via <http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/622/A92>

Measuring brightness temperature in a statistically viable sample enables the performance of detailed investigations of the physical conditions in this region. The distribution of observed brightness temperatures, T_b , derived at 86 GHz can be combined with the T_b distributions measured at lower frequencies (e.g., Kovalev et al. 2005). This can help to constrain the bulk Lorentz factor, Γ_j , and the intrinsic brightness temperature, T_0 , of the jet plasma, using different types of population models of relativistic jets (Vermeulen & Cohen 1994; Lobanov et al. 2000; Lister 2003; Homan et al. 2006). Changes of T_0 in the compact jets with frequency can be used to distinguish between the emission coming from accelerating or decelerating plasma and from electron-positron or electron-proton plasma. Theoretical models predict $T_0 \propto \nu^\epsilon$, with $\epsilon \approx 2.8$, below a critical frequency ν_{break} at which energy losses begin to dominate the emission (Marscher 1995). Above ν_{break} , ϵ can vary from -1 to $+1$, depending on the jet composition and dynamics. By measuring this break and the power-law slopes above and below, it would be possible to distinguish between different physical situations in the compact jets.

Previous studies (Lobanov et al. 2000; Lee et al. 2008) indicate that the value of ν_{break} is likely to be below 86 GHz. Indeed, a compilation of brightness temperatures measured at 2, 8, 15, and 86 GHz (Lee et al. 2008) indicates that brightness temperatures measured at 86 GHz are systematically lower and ν_{break} can be as low as 20 GHz. This needs to be confirmed on a complete sample observed at 86 GHz. If T_0 starts to decrease at 86 GHz, there will be only a few sources suitable for VLBI > 230 GHz and higher frequencies. Such a decrease of T_0 will also provide a strong argument in favour of the decelerating jet model or particle-cascade models as discussed by Marscher (1995). In view of these arguments, it is important to undertake a dedicated 86 GHz VLBI study of a larger complete sample of extragalactic radio sources.

In this paper, we present results from a large global VLBI survey of compact radio sources carried out in 2010–2011 with the Global Millimeter VLBI Array (GMVA)¹. This survey has provided images of 162 unique radio sources, increasing the total number of sources ever imaged with VLBI at 86 GHz by a factor of 1.5. The combined database resulting from this survey and Lee et al. (2008) comprises 256 sources. This information provides a basis for investigations of the collimation and acceleration of relativistic flows and probing the physical conditions in the vicinity of supermassive black holes.

The survey data reach a typical baseline sensitivity of 0.1 Jy and a typical image sensitivity of 5 mJy beam⁻¹. A total of 162 unique compact radio sources have been observed in this survey and all the sources are detected and imaged. With the present survey, the overall sample of compact radio sources imaged with VLBI at 86 GHz is representative down to ~ 0.5 Jy for J2000 declinations of $\delta \geq 15^\circ$.

Section 2 describes the source selection and the survey observations. In Sect. 3, we describe the data processing, amplitude and phase calibration, imaging, model fitting procedures and a method for estimating errors of the model-fit parameters. Section 4 describes the images and derived parameters of the target sources. Examples of images of four selected sources obtained from the survey data are presented in Sect. 4.1². Brightness temperatures of the survey sources are derived and discussed in Sect. 4.3. Section 5.1 describes population modelling

of the brightness temperature distribution observed at the base (VLBI core) of the jet and in the innermost moving jet components. Evolution of the observed brightness temperature along the jet is studied in Sect. 5.2 for the target sources with sufficient extended emission detected.

2. GMVA survey of compact AGN

Dedicated VLBI observations at 86 GHz are made with the GMVA and with the Very Long Baseline Array (VLBA)³ working in a stand-alone mode (VLBA also takes part in GMVA observations). The GMVA has been operating since 2002, superseding the operations of the Coordinated Millimeter VLBI Array (CMVA; Rogers et al. 1995) and earlier ad hoc arrangements employed since the early 1980s (Readhead et al. 1983). The GMVA carries out regular, coordinated observations at 86 GHz, providing good quality images with a typical angular resolution of $\sim (50\text{--}70) \mu\text{as}$.

The array comprises up to 16 telescopes located in Europe, the USA and Korea operating at a frequency of 86 GHz. The following telescopes took part in the GMVA observations for this survey in 2010 and 2011: eight VLBA antennae equipped with 3 mm receivers, the Institut de Radio Astronomie Millimétrique (IRAM) 30 m telescope on Pico Veleta (Spain), the phased six-element IRAM interferometer on Plateau de Bure (France), the Max-Planck-Institut für Radioastronomie (MPIfR) 100 m radio telescope in Effelsberg (Germany), the Onsala Space Observatory (OSO) 20 m radio telescope at Onsala (Sweden), the 14 m telescope in Metsähovi (Finland), and the Observatorio Astronómico Nacional (OAN) 40 m telescope in Yebes (Spain).

2.1. Source selection

The prime aims of the survey were to establish a complete sample of compact radio sources imaged with VLBI at 86 GHz and to study their morphology and polarization, to study the distribution of brightness temperatures, to investigate collimation and acceleration of relativistic flows and to probe physical conditions in the vicinity of supermassive black holes. To meet these aims, the survey target source list has been compiled from the MOJAVE (Monitoring of Jets in Active Galactic Nuclei with VLBA Experiments) sample (Kellermann et al. 2004; Kovalev et al. 2005; Lister & Homan 2005; Lister et al. 2009), using the following selection criteria: *a*) 15 GHz correlated flux density, $S_c \geq 0.5$ Jy on baselines of ≥ 400 M λ ; *b*) compactness at longest spacings, $S_c/S_{\text{VLBA}} \geq 0.4$ where S_{VLBA} is the 15 GHz total clean flux density; *c*) declination $\delta \geq 15^\circ$. With these selection criteria, a total of 162 unique sources have been selected, comprising 89 quasars, 26 BL Lac objects, 22 radio galaxies and 25 unidentified sources. Eight bright sources, 3C 84, OJ 287, 3C 273B, 3C 279, 3C 345, BL Lac, 0716+714 and 3C 454.3 have been added to this list for fringe finding and calibration purposes. The basic information about the selected target sources is summarized in Table 5.

The distribution of the total single dish flux of the sources, measured at 86 GHz at Pico Veleta or Plateau de Bure during the observations, is shown in Fig. 1 and compared with the respective distribution of the source sample observed in Lee et al. (2008). This comparison shows that our survey observations probe objects at about one order of magnitude weaker sources

¹ <http://www3.mpi-fr-bonn.mpg.de/div/vlbi/globalmm/>

² The complete set of images of all the target sources are presented in Appendix A.

³ Very Long Baseline Array of the National Radioastronomy Observatory, Socorro, NM; <https://www.lbo.us/>

Table 1. VLBI surveys at 86 GHz.

Survey (1)	N_{ant} (2)	B_{rec} (3)	ΔS (4)	ΔI_{m} (5)	D_{img} (6)	N_{obs} (7)	N_{det} (8)	N_{img} (8)
Beasley et al. (1997)	3	112	~ 0.5	...	...	51	12	...
Lonsdale et al. (1998)	2–5	112/224	~ 0.7	...	...	79	14	...
Rantakyrö et al. (1998)	6–9	128	~ 0.5	~ 30	70	68	16	12
Lobanov et al. (2000)	3–5	224	~ 0.4	~ 20	100	28	26	14
Lee et al. (2008)	12	256	~ 0.3	10	200	127	121	109
This survey	13–14	512	~ 0.1	~ 5	>400	162	162	162

Notes. Columns: 1 – survey ; 2 – number of participating antennae; 3 – recording bit rate [Mbps]; 4 – average baseline sensitivity [Jy]; 5 – average image sensitivity [mJy beam⁻¹]; 6 – typical dynamic range of images; 7 – number of sources observed; 8 – number of sources detected; 9 – number of sources imaged.

Fig. 1. Distribution of the total single dish flux density of the sources, measured at 86 GHz at Pico Veleta or Plateau de Bure during the observations, S_{86} , broken down according to different host galaxy types and compared to the respective distribution for the sources from the sample of Lee et al. (2008). The present survey provides a nearly twofold increase in the number of objects imaged with VLBI at 3 mm.

and provide a roughly twofold increase of the total number of objects imaged with VLBI at 3 mm wavelength (see Table 5 for details).

2.2. Observations

The survey observations have been made over a total of six days (144 h), scheduled within three separate GMVA sessions. Up to 14 telescopes took part in the observations (see Table 2). The observations were typically scheduled with five scans per hour, each of 300 s in duration. Gaps of five to ten minutes were introduced between the scans for antennae pointing at Effelsberg (Eb) and Pico Veleta (Pv) and for phasing of the Plateau de Bure (Pb) interferometer. This observing scheme yielded the total of 720 scans distributed between 174 observing targets (162 unique radio sources), ensuring that each object was observed with four to five scans distributed over a wide range of hour angles. Despite the rather modest observing time spent on each target, the large number of participating antennae ensured good uv -coverages for all survey sources down to the lowest declinations (see Fig. 2).

The observations were performed at a sampling rate of 512 Mbit s⁻¹ and with a two-bit sampling. There were four intermediate frequencies (IFs) in Epoch A and C, and two IFs in Epoch B. The typical baseline sensitivities for a 20 s integration time are ~ 0.05 Jy on the Pb–Pv baseline, ~ 0.1 Jy on the Eb–Pv baseline, ~ 0.2 Jy on the baselines between Eb/Pv and other antennae, and ~ 0.4 Jy on the baselines between the VLBA antennae. With such baseline sensitivities and an on-source integration time of about 20 min, the typical point source sensitivity of a survey observation is ~ 5 mJy beam⁻¹, which is sufficient to obtain robust images of most of the survey sources.

3. Data processing

3.1. Correlation and fringe fitting

The data were correlated at the DiFX correlator (Deller et al. 2011) of the Max-Planck-Institut für Radioastronomie (MPIfR) at Bonn. After correlation, the data were loaded into AIPS (Astronomical Image Processing System; Greisen et al. 1990). After applying the correlator model, the residual fringe delays and rates were determined and corrected for both within the individual IFs (single-band fringe fitting) and between the IFs (multi-band fringe fitting).

At the first step of the fringe fitting, manual phasecal correction was applied by obtaining the single band delay and delay rate solutions from a scan on a strong source that gives high signal-to-noise ratio (S/N) of the fringe solutions (an $S/N \geq 7$ threshold was set) over the typical coherence time (~ 20 s) for all the antennae. The resulting fringe solutions were applied to the entire dataset. After the manual phasecal correction, antenna-based global fringe fitting (Schwab & Cotton 1983; Alef & Porcas 1986) was performed, setting the solution interval to the full scan length in order to improve the detection S/N. Pico Veleta was used as the reference antenna for almost all the data. Whenever Pico Veleta was not present in the data, Plateau de Bure or Pie Town were used as the reference antennae. To minimize the chance of false detections, the data were fringe fitted with a S/N threshold of five and a search window width of 200 ns for the fringe delay and 400 mHz for the fringe rate.

Once the global fringe fit was done, the S/N of the fringe solutions were inspected for all the sources, and strong sources which give relatively very high S/N were determined. Whenever feasible, the solutions from those strong sources were interpolated to nearby weak sources, using a procedure similar to that adopted in the similar earlier VLBI survey observations at 86 GHz (cf., Lee et al. 2008). Application of the interpolated

Fig. 2. Examples of uv -coverages of the survey observations for a low declination source (*left*; J1811+1704, $\delta = +17^\circ$) and a high declination source (*right*; J0642+8811, $\delta = +88^\circ$).

Table 2. Log of survey observations.

Part (1)	Date (2)	N_{obj} (3)	Pol. (4)	w_{bit} (5)	BW (6)	n_{ch} (7)	n_{bit} (8)	Telescopes (9)
A	Oct 2010	68	LCP	512	128 (4IF x 32)	32	2	8 VLBA+(Eb,On,Mh,Pb,Pv)
B	May 2011	46	LCP	512	128 (2IF x 64)	64	2	8 VLBA+(Eb,On,Pb,Pv,Mh)
C	Oct 2011	60	LCP	512	128 (4IF x 32)	32	2	8 VLBA+(Eb,On,Pb,Pv,Mh,Ys)

Notes. Columns: 1 – survey epoch; 2 – observing date; 3 – number of objects observed; 4 – polarization; 5 – recording bit rate [Mbps]; 6 – total bandwidth (number of IF bands x IF bandwidth) [MHz]; 7 – number of frequency channels per IF band; 8 – correlator sampling [bits]; 9 – participating telescopes.

solutions has resulted in the detection of amplitude and phase signals for all of the survey targets.

3.2. Amplitude calibration

A priori amplitude calibration was done using the measured values of antenna gain and system temperature. The weather information from each station during the observation was used to correct for the atmospheric opacity. The initial opacity correction was implemented by setting the opacity $\tau = 0.1$ and fitting for the receiver temperatures, T_{rec} . At the second step, the fitted receiver temperatures were used as initial values for fitting simultaneously for τ and T_{rec} .

The accuracy and self-consistency of the amplitude calibration was checked with a procedure developed and used in the earlier 86 GHz survey experiments (Lobanov et al. 2000; Lee et al. 2008). The calibrated visibility data were model fitted for each of the survey targets, using two-dimensional Gaussian components and allowing for scaling the individual antenna gains by a constant factor. The resulting average gain scale corrections are listed in Table 4. The scale offsets are within 25% for most of the antennae, except Metsähovi which had suffered from persistently bad weather during each of the three observing sessions. The averaged offsets are within about 3% of the unity implying that there is no significant bias in the calibration and their rms

(root mean square) is less than 10% for each of the three observing epochs. Based on this analysis, we conclude that the a priori amplitude calibration should be accurate to within about 25%, providing a sufficient initial calibration accuracy for the hybrid imaging of the source structure.

3.3. Hybrid imaging and model fitting

After the phase and amplitude calibration was applied on the data, the visibility data were averaged for 10 s for most of the sources and in some cases, the data were averaged for 30 s. The data were then processed in the the Caltech DIFMAP software package (Shepherd et al. 1994), modelling them with circular Gaussian patterns (model fitting; Fomalont 1999) and obtaining hybrid images. The data were not uv -tapered and the imaging was performed using the natural weighting.

The initial model fitting was performed on the calibrated data and was used, in some cases, to facilitate the hybrid imaging. The final model fitting was done on the self-calibrated data resulting from the hybrid imaging. The total number of Gaussian components used for model fitting a given source was determined using the χ^2 statistics of the fits. The final models were obtained when the addition of another Gaussian component did not provide a statistically significant change of the χ^2 agreement factors (Schinzel et al. 2012).

Table 3. Participating telescopes.

Name	Code	D (m)	G (K Jy ⁻¹)	T_{sys} (K)	η_A	SEFD (Jy)	$\Delta_{512,20}$ (mJy)	σ_{rms} (mJy)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Brewster	Br	25	0.033	110	0.22	3333.3	23.44	164.09
Effelsberg	Eb	80 ^a	0.140	140	0.08	1000	12.84	89.87
Fort Davis	Fd	25	0.039	140	0.22	3589.7	24.32	170.28
Kitt Peak	Kp	25	0.028	100	0.22	3571.4	24.26	169.85
Los Alamos	La	25	0.042	120	0.22	2857.1	21.70	151.91
Metsähovi	Mh	14	0.017	300	0.3	17647.1	53.94	377.55
Mauna Kea	Mk	25	0.019	100	0.22	5263.2	29.45	206.18
North Liberty	Nl	25	0.022	130	0.22	5909.1	31.21	218.47
Onsala	On	20	0.049	250	0.43	5102	29.00	203.00
Owens Valley	Ov	25	0.035	120	0.22	3428.6	23.77	166.41
Plateau de Bure	Pb	36 ^b	0.22	180	0.7	818.2	11.61	81.29
Pie Town	Pt	25	0.044	100	0.22	2272.7	19.36	135.52
Pico Veleta	Pv	30	0.153	100	0.6	653.6	...	...
Yebes	Ys	40	0.09	150	0.2	1666.7	16.58	116.03

Notes. Columns: 1 – telescope name; 2 – abbreviation for the telescope name; 3 – diameter; 4 – antenna gain; 5 – zenith system temperature; 6 – aperture efficiency; 7 – zenith SEFD; 8 – sensitivity on the baseline to Pico Veleta, for a 20 s fringe fit interval and 512 Mbps recording rate; 9 – 7σ detection threshold. ^(a)Effective diameter at 86 GHz. ^(b)Effective diameter in the phased array mode.

Table 4. Average antenna gain corrections.

Telescope (1)	Epoch A (2)	Epoch B (3)	Epoch C (4)
Br	1.008 ± 0.406	1.054 ± 0.137	1.010 ± 0.192
Eb	1.103 ± 0.264	1.028 ± 0.224	0.925 ± 0.182
Fd	0.992 ± 0.206	1.105 ± 0.289	0.958 ± 0.162
Kp	0.881 ± 0.154	0.933 ± 0.104	0.931 ± 0.102
La	0.819 ± 0.199	0.940 ± 0.172	0.987 ± 0.133
Mh	...	...	1.620 ± 0.573
Mk	0.919 ± 0.256	1.188 ± 0.438	0.844 ± 0.199
Nl	1.224 ± 0.386	1.190 ± 0.296	0.798 ± 0.264
On	0.934 ± 0.292	0.935 ± 0.114	0.889 ± 0.147
Ov	0.900 ± 0.371	0.868 ± 0.148	0.939 ± 0.382
Pb	1.081 ± 0.146	1.087 ± 0.225	1.095 ± 0.203
Pt	0.841 ± 0.113	0.878 ± 0.109	1.041 ± 0.098
Pv	1.006 ± 0.116	1.088 ± 0.220	1.010 ± 0.086
Ys	...	...	1.009 ± 0.196
Array average	1.037 ± 0.084	0.991 ± 0.074	1.027 ± 0.097

Notes. Columns: 1 – abbreviation for the participating telescope; 2,3,4 – average and rms of antenna gains for observing epochs A, B, and C, respectively.

The hybrid imaging procedure comprised the CLEAN deconvolution (Clark 1980) and self calibration (Cornwell & Fomalont 1999; Cornwell 1995). For most of the objects, the hybrid imaging procedure was initiated with a point source model. For objects with sparse visibility data, the initial Gaussian model fits were used as the initial models. Only visibility phases were allowed to be modified during the initial iterations of the hybrid imaging. At the last step, a single time constant antenna gain correction factor was applied to the visibility amplitudes (hence not allowing for time variable antenna gains in order to avoid the imprint of model errors into data). The parameters of the final images are listed in Table 6, together with the correlated flux densities measured on short and long baselines.

Fig. 3. Distribution of the noise quality factor ξ_r for the residual images of all the sources in the survey.

The quality of the residual noise in the final images, which ideally should have a zero-mean Gaussian distribution, was checked by calculating the expectation value for the maximum absolute flux density $|S_{r,\text{exp}}|$ in a residual image (Lee et al. 2008),

$$|S_{r,\text{exp}}| = \sigma_r \sqrt{2 \ln \left(\frac{N_{\text{pix}}}{\sqrt{2\pi}\sigma_r} \right)^2}, \quad (1)$$

where N_{pix} is the total number of pixels in the image. The quality of the residual noise is given by $\xi_r = S_r / S_{r,\text{exp}}$, where S_r is the maximum flux density in the residual image and σ_r is the rms noise in the residual image. When the residual noise approaches Gaussian noise, ξ_r tends to 1. If $\xi_r > 1$, not all the structure has been adequately recovered; if $\xi_r < 1$, the image model has an excessively large number of degrees of freedom (Lobanov et al. 2006).

Fig. 4. Distribution of the imaging S/N of all the sources in the survey calculated from the ratio of the peak flux density of the map, S_p , to the rms noise in the map, σ_{rms} .

Figure 3 shows the overall distribution of ξ_r for the residual maps of all the sources in this survey. Column 14 in Table 6 shows the quality factor, ξ_r , obtained for all the 3 mm images implying that the images adequately represent the source structure detected in the visibility data. The Gaussianity of the residual noise is also reflected in the median and the mean of the ξ_r distributions, which are within 10% of the unity factor.

In order to check the effect of the amplitude (antenna gain) corrections applied during the final self calibration step, we compared the visibility amplitudes obtained without and with it. This was done by comparing the ratios of the visibility amplitudes obtained without and with the antenna gain correction on short B_S and long B_L baselines (see Table 6). The average of the ratios are found to be (1.24 ± 0.18) and (1.01 ± 0.14) for the short and long baselines, respectively. These ratios imply that the amplitude self-calibration did not introduce substantial gain corrections, thus further indicating the overall good quality of the a priori amplitude calibration of the survey data.

3.4. Gaussian models of the source structure

The final self calibrated data were fitted with circular Gaussian components, using the initial model fits as a starting guess. The resulting models were used to obtain the total, S_{tot} , and peak flux density, S_{peak} , the size, d , and the positional offset, (in polar coordinates r, θ) of the component from the brightest region (core) at the base of the jet, taken to be at the coordinate origin. The uncertainties of the model parameters were estimated analytically, based on the S/N of detection of individual components, following Fomalont (1999) and Schinzel et al. (2012):

$$\sigma_{\text{peak}} = \sigma_{\text{rms}} \left(1 + \frac{S_{\text{peak}}}{\sigma_{\text{rms}}} \right)^{1/2}, \quad \sigma_{\text{tot}} = \sigma_{\text{peak}} \left(1 + \frac{S_{\text{tot}}^2}{S_{\text{peak}}^2} \right)^{1/2},$$

$$\sigma_d = d \frac{\sigma_{\text{peak}}}{S_{\text{peak}}}, \quad \sigma_r = \frac{1}{2} \sigma_d, \quad \sigma_\theta = a \tan \left(\frac{\sigma_r}{r} \right), \quad (2)$$

where σ_{rms} is the rms noise in the residual image after subtraction of the Gaussian model fit. To assess whether a given component is extended (resolved), the minimum resolvable size of

the component was also calculated and compared with the size obtained with the model fitting. The minimum resolvable size, d_{min} of a Gaussian component is given in Lobanov (2005) as

$$d_{\text{min}} = \frac{2^{(1+\beta/2)}}{\pi} \left[\pi a b \log \left(\frac{S/N + 1}{S/N} \right) \right]^{1/2}, \quad (3)$$

where a and b are the axes of the restoring beam, S/N is the signal-to-noise ratio, and β is the weighing function that is 0 for natural weighting or 2 for uniform weighting. For components that have size estimates $< d_{\text{min}}$, the latter is taken as an upper limit of the size and used for estimating the uncertainties of the other model fit parameters of the respective component (see Table 7).

3.5. Brightness temperature estimates

We use the total flux density S_{tot} and size d of the model fit components to estimate the brightness temperature, $T_b = I_\nu c^2 / 2k_B \nu$ (with ν , k_B , and c denoting the observing frequency, the Boltzmann constant, and the light speed, respectively) of the individual emitting regions in the jets.

For a circular Gaussian component, $I_\nu = (4 \log 2/2) S_{\text{tot}} / d^2$, and the respective brightness temperature can be obtained from

$$T_b[\text{K}] = 1.22 \times 10^{12} \left(\frac{S_{\text{tot}}}{\text{Jy}} \right) \left(\frac{d}{\text{mas}} \right)^{-2} \left(\frac{\nu}{\text{GHz}} \right)^{-2} (1+z). \quad (4)$$

The factor $(1+z)$ reflects the effect of the cosmological redshift z on the observed brightness temperature. For the sources with unknown redshift, we calculated the brightness temperature simply in the observer's frame of reference. If the size of the Gaussian component d is less than d_{min} , given by Eq. (3), the latter is used for estimating the lower limit on T_b .

In addition to this estimate, we also use visibility-based estimates of brightness temperature (Lobanov 2015) and calculate the minimum brightness temperature,

$$T_{b,\text{min}}[\text{K}] = 3.09 \left(\frac{V_q}{\text{mJy}} \right) \left(\frac{B_L}{\text{km}} \right)^2, \quad (5)$$

and limiting resolved brightness temperature,

$$T_{b,\text{lim}}[\text{K}] = 1.14 \left(\frac{V_q + \sigma_q}{\text{mJy}} \right) \left(\frac{B_L}{\text{km}} \right)^2 \left(\ln \frac{V_q + \sigma_q}{V_q} \right)^{-1}, \quad (6)$$

directly from the visibility amplitude, V_q , and its error, σ_q , measured at a given long baseline, B_L , in the survey data.

4. Results

4.1. Images

Using the procedures described above, we have made hybrid maps of all 174 observations of 162 unique sources in this survey. For 138 objects, the survey provides the first ever VLBI images made at 86 GHz. Most of the imaged sources show extended radio emission, revealing the jet morphology down to sub-parsec scales. For a small number of weaker sources with poor uv -coverages, only the brightest core at the base of the jet could be imaged. To illustrate our results, we present images of four weak target radio sources J1130+3815, J0700+1709, J1044+8054 and J0748+2400 in Fig. 6 (a total of 174 contour maps of 162 unique sources imaged at 3 mm in this survey are available in Appendix A).

Fig. 5. Distribution of the correlated flux densities corresponding to the longest baselines, S_L (left) and the total clean image flux density, S_{CLEAN} of the survey targets broken down according to different host galaxy types (right). The distribution of S_{CLEAN} for the sources in this survey is also compared with the respective distribution for the sources from the sample of Lee et al. (2008) on the right panel.

Figure 5 illustrates the properties of the survey sample by plotting the distributions of the correlated flux density, S_L , measured on long baselines and the total flux density, S_{CLEAN} , in the CLEAN images of the observed sources. Both distributions indicate that objects with flux densities ≥ 80 mJy can be successfully detected and imaged with the survey data, signifying the sensitivity improvement by a factor of approximately two compared to the observations presented in Lee et al. (2008). The mean of the correlated flux density at the longest baseline, S_L , is 0.2 Jy. Amongst 157 sources whose S_L can be measured at projected baselines longer than 2000 M λ , 135 sources have an S_L greater than 0.1 Jy.

In Table 6, we present the basic parameters of the images, listing (1) source name, (2) observing epoch, (3) single dish 86 GHz flux density, S_{86} , measured at Pico Veleta or Plateau de Bure, (4) correlated flux density on the shortest baseline, S_S , (5) shortest baseline, B_S , (6) correlated flux density on the longest baseline, S_L , (7) longest baseline, B_L , (8) major axis, B_a , (9) minor axis, B_b , and (10) position angle, B_{PA} of the major axis of the restoring beam, (11) total CLEAN flux density, S_{tot} , and (12) peak flux density, S_{peak} , in the image, (13) image rms noise, σ_{rms} , and (14) the quality factor of the residual noise in the image, ξ_r .

Table 7 summarizes the model fits obtained for all of the survey sources providing (1) the source name, (2) observing epoch, (3) sequential number of the Gaussian component, (4) total flux density, S_t , and (5) peak flux density, S_{peak} , of the component, (6) size, d , of the component, (7) separation, r , and (8) position angle, θ of the component with respect to the brightest feature in the model (core, taken to be located at the coordinate origin), (9) brightness temperature, $T_{\text{b,mod}}$, estimated from the model fit, and (10) minimum, $T_{\text{b,min}}$ and (11) limiting resolved, $T_{\text{b,lim}}$, brightness temperatures estimated from the visibility amplitudes (Lobanov 2015) at the longest baselines given in Col. 7 in Table 6.

Table 7 contains the model fit parameters for a total 174 VLBI cores and 205 jet components, with 42 and 37 of these unresolved, as reflected also in the lower limits of the model-fit-based brightness temperature estimates, $T_{\text{b,mod}}$, listed for these components.

4.2. Source compactness

Compactness of the source structure can be evaluated by comparing the single dish flux density, S_{86} , listed in Table 6, to the total clean flux density, S_{CLEAN} , listed in Table 6 and the core flux density, S_{CORE} , listed in Table 7, to the total clean flux density, S_{CLEAN} . These comparisons are presented in Fig. 7.

To study the relation between the total and VLBI flux densities, we apply the Pearson correlation test. The Pearson correlation coefficient calculated for S_{86} and S_{CLEAN} gives a significant value of 0.924 for this survey and 0.908 for this survey combined with the results from Lee et al. (2008). The respective plot in the left panel of Fig. 7 indicates that almost all the flux measured by a single dish (here Pv or PdB) is recovered in the VLBI clean flux. The median of the core dominance index defined as $S_{\text{CORE}}/S_{\text{CLEAN}}$ is 0.84, and the two are also correlated, as demonstrated in the right panel of Fig. 7.

Figure 7 shows that the stronger sources have more structures (right panel) some of which are completely resolved out even on the shortest baselines of the survey observations (left panel). A small number of cases for which $S_{\text{CLEAN}} > S_{86}$ or $S_{\text{CORE}} > S_{\text{CLEAN}}$ are observed for the weaker objects. These can be reconciled with the errors in the measurements, and they essentially imply very compact objects, with $S_{86} \approx S_{\text{CLEAN}}$ and $S_{\text{CORE}} \approx S_{\text{CLEAN}}$, respectively.

4.3. Brightness temperatures

In our further analysis, we use the model-fit-based and visibility-based estimates of the brightness temperature of the VLBI bright core (base) and the inner ($r_{\text{proj}} < 1$ pc) jet components, taking into account the resolution limits of the data at 3 mm. The brightness temperature estimates for the jet cores in our sample range from 2.5×10^9 K to 1.3×10^{12} K. The brightness temperature estimates for the inner jet components in our sample range from 7.0×10^7 K to 4.0×10^{11} K. The median and mean of the brightness temperature distribution for the core regions are 8.6×10^{10} K and 1.8×10^{11} K, respectively. For the inner jet components, the respective figures are 7.2×10^9 K and 2.2×10^{10} K. This shows that the brightness temperature drops by approximately

Fig. 6. GMVA maps of J1130+3815, J0700+1709, J1044+8054, and J0748+2400 (*left panel*), shown together with the respective radial amplitude distributions (*right panel*) and *uv*-coverages (inset in the *right panel*) of the respective visibility datasets. The contouring of images is made at $3\sigma_{\text{rms}} \times (-1, 1, \sqrt{2}, 2, \dots)$ levels, with σ_{rms} representing the off-source rms noise in the residual image. The lowest contour in the maps, $L = 21.2 \text{ mJy beam}^{-1}$, $15.8 \text{ mJy beam}^{-1}$, $18.8 \text{ mJy beam}^{-1}$, and $26.6 \text{ mJy beam}^{-1}$, respectively. A total of 174 contour maps of 162 unique sources imaged at 3 mm in this survey are available in Appendix A.

Table 5. List of sources.

Source (J2000) (1)	Source (B1950) (2)	Common name (3)	Epoch (4)	α_{2000} (5)	δ_{2000} (6)	z (7)	Type (8)	m_v (9)
J0013+4051	0010+405	4C 40.01	C	00 13 31.130201	+40 51 37.14403	0.2560	G	17.9
J0017+8135	0014+813		B	00 17 08.474904	+81 35 08.13656	3.3660	Q	16.5
J0030+7037	0027+703		B	00 30 14.412959	+70 37 40.06069	...	U	17.0
J0034+2754	0032+276		C	00 34 43.486179	+27 54 25.72112	2.9642	G	18.0
J0044+6803	0041+677		B	00 44 50.759603	+68 03 02.68574	...	U	...
J0046+2456	0043+246		A	00 46 07.825730	+24 56 32.52437	0.7467	Q	17.1
J0057+3021	0055+300	NGC 315	A	00 57 48.883342	+30 21 08.81194	0.0165	G	12.2
J0102+5824	0059+581	7C 0059+5808	B	01 02 45.762380	+58 24 11.13659	0.6440	Q	17.6
J0109+6133	0106+612		B	01 09 46.344370	+61 33 30.45531	0.7830	G	19.4
J0112+3522	0109+351		A	01 12 12.944409	+35 22 19.33615	0.4500	Q	17.8
J0113+4948	0110+495		A	01 13 27.006813	+49 48 24.04306	0.3890	Q	18.4
J0126+7046	0122+705		B	01 26 7.8495750	+70 46 52.38656	...	U	18.7
J0136+4751	0133+476	DA 55	B,C	01 36 58.594700	+47 51 29.10000	0.8590	Q	18.0
J0137+2145	0134+215		A	01 37 15.624949	+21 45 44.27088	...	U	...
J0154+4743	0151+474		B	01 54 56.289889	+47 43 26.53956	1.0260	Q	...
J0205+3212	0202+319		A	02 05 04.925360	+32 12 30.09541	1.4660	Q	18.2
J0253+3217	0250+320		A	02 53 33.650138	+32 17 20.89168	0.8590	Q	...
J0254+2343	0251+235		A	02 54 24.718127	+23 43 26.47461	1.9870	Q	...
J0310+3814	0307+380		B	03 10 49.879930	+38 14 53.83778	0.9450	Q	18.5
J0313+4120	0309+411	NRAO 128	B	03 13 01.962125	+41 20 01.18349	0.1340	G	18.0
J0319+4130	0316+413	3C 84	A,B,C	03 19 48.160100	+59 33 22.21466	0.0176	G	12.6
J0325+2224	0322+222		C	03 25 36.814357	+22 24 00.36551	2.0660	Q	18.9
J0325+4655	0321+467		C	03 25 20.303800	+46 55 06.63500	...	B	14.1
J0333+6536	0329+654		C	03 33 56.737600	+65 36 56.18400	...	B	19.3
J0344+6827	0339+683		A,C	03 44 41.441278	+68 27 47.81028	...	U	...
J0359+3220	0356+322		A	03 59 44.912917	+32 20 47.15548	1.3310	Q	19.9
J0359+5057	0355+508	NRAO 150	A	03 59 29.747200	+50 57 50.16100	1.5200	Q	22.9
J0428+3259	0424+328		A	04 28 05.808725	+32 59 52.04381	0.4760	Q	20.2
J0512+4041	0509+406		A	05 12 52.542864	+40 41 43.62019	...	Q	...
J0533+4822	0529+483		A	05 33 15.865792	+48 22 52.80771	1.1620	Q	19.9
J0604+2429	0601+245	4C 24.11	A	06 04 55.121380	+24 29 55.03635	1.1330	G	...
J0612+4122	0609+413		A	06 12 51.185236	+41 22 37.40815	...	B	15.7
J0618+4207	0614+421		A	06 18 08.619909	+42 07 59.84609	...	U	...
J0632+3200	0629+320		A	06 32 30.782861	+32 00 53.63193	1.8310	Q	...
J0638+5933	0633+595		B	06 38 02.871950	+59 33 22.21466	...	B	...
J0639+7324	0633+734		C	06 39 21.961200	+73 24 58.04000	1.8500	Q	17.8
J0642+8811	0604+882		C	06 42 6.1363170	+88 11 55.01734	...	B	19.5
J0650+6001	0646+600		B	06 50 31.254355	+60 01 44.55601	0.4550	Q	18.9
J0700+1709	0657+172		A	07 00 01.525539	+17 09 21.70130	...	U	21.0
J0707+6110	0702+612		B	07 07 00.615678	+61 10 11.60689	...	U	17.0
J0713+1935	0710+196	WB92 0711+1940	A	07 13 30.782861	+19 35 00.40875	0.5400	Q	18.6
J0721+7120	0716+714	S5 0716+71	B,C	07 21 53.448400	+71 20 36.36300	0.3000	B	15.5
J0733+5022	0730+504		C	07 33 52.520500	+50 22 09.06200	0.7200	Q	19.0
J0741+3112	0738+313	OI 363	C	07 41 10.703310	+31 12 00.22894	0.6320	Q	16.7
J0747+7639	0740+767		B	07 47 14.607565	+76 39 17.27140	...	B	20.0
J0748+2400	0745+241	S3 0745+24	C	07 48 36.109275	+24 00 24.11002	0.4092	Q	19.7
J0753+5352	0749+540	4C 54.15	C	07 53 01.384569	+53 52 59.63709	0.2000	B	18.5
J0808+4052	0805+410		C	08 08 56.652043	+40 52 44.88880	1.4193	Q	19.0
J0809+5341	0805+538		C	08 09 41.732819	+53 41 25.09245	2.1330	Q	19.8
J0814+6431	0810+646		C	08 14 39.190224	+64 31 22.02696	...	B	17.9

Notes. Columns: 1 – IAU source name (J2000); 2 – IAU source name (B1950); 3 – common name; 4 – observing epochs – A: October 2010; B: May 2011 and C: October 2011; 5,6 – source coordinates in J2000 epoch: right ascension and declination; 7 – redshift; 8 – optical class – Q: quasar; B: BL Lac object; G: Galaxy; U: Unidentified source; 9 – optical V magnitude information for Cols. 7–9 obtained from the Simbad Astronomical Database (<http://simbad.u-strasbg.fr/simbad>; Wenger et al. 2000), Sloan Digital Sky Survey (<http://www.sdss.org/>) and NASA/IPAC Extragalactic Database (<https://ned.ipac.caltech.edu>). The full table is available at the CDS and in a machine-readable and Virtual Observatory (VO) forms in the online journal.

Table 6. Image parameters.

Source (J2000) (1)	Obs (2)	$S_{86\text{GHz}}$ (3)	S_S (4)	B_S (5)	S_L (6)	B_L (7)	B_a (8)	B_b (9)	B_{PA} (10)	S_t (11)	S_p (12)	σ (13)	ξ_r (14)
J0013+4051	C	0.79	0.656 ± 0.020	56	0.192 ± 0.006	3136	159	35	-16.8	436	317	8	1.43
J0017+8135	B	0.18	0.263 ± 0.018	60	0.075 ± 0.004	3062	74	35	62.1	143	81	2	1.36
J0030+7037	B	0.34	0.363 ± 0.026	65	0.115 ± 0.009	3070	76	36	66.5	155	92	3	1.34
J0034+2754	C	0.07	0.124 ± 0.015	54	0.156 ± 0.021	3086	262	36	-14.2	159	60	2	1.04
J0044+6803	B	0.17	0.315 ± 0.023	65	0.097 ± 0.006	3034	75	36	70.4	133	99	3	1.15
J0046+2456	A	0.47	0.252 ± 0.019	59	0.137 ± 0.009	3060	267	37	-15.0	235	160	6	1.17
J0057+3021	A	0.48	0.361 ± 0.023	58	0.233 ± 0.017	3060	308	37	-14.5	306	226	8	1.07
J0102+5824	B	3.11	3.579 ± 0.037	44	0.336 ± 0.020	3050	59	43	-19.5	2221	1075	19	1.58
J0109+6133	B	0.64	0.706 ± 0.026	45	0.242 ± 0.023	3048	111	37	-12.9	381	239	5	1.17
J0112+3522	A	0.53	0.624 ± 0.031	58	0.105 ± 0.008	3054	205	37	-18.3	238	119	3	1.08
J0113+4948	A	0.61	0.547 ± 0.026	56	0.156 ± 0.011	3066	119	36	-28.2	269	234	9	1.32
J0126+7046	B	0.07	0.233 ± 0.018	48	0.071 ± 0.004	2474	115	36	-13.4	76	69	2	1.20
J0136+4751	B	1.95	2.531 ± 0.060	33	1.324 ± 0.037	2388	157	43	-14.4	2090	862	14	1.21
J0136+4751	C	1.76	1.811 ± 0.026	46	0.518 ± 0.045	2870	230	36	-0.5	1317	740	15	1.15
J0137+2145	A	0.07	0.289 ± 0.018	54	0.184 ± 0.007	3070	259	40	-10.2	278	175	3	1.03
J0154+4743	B	...	0.436 ± 0.022	32	0.315 ± 0.026	2860	150	42	-11.2	239	172	4	1.12
J0205+3212	A	0.81	0.530 ± 0.037	49	0.228 ± 0.019	3052	185	38	-11.6	499	182	4	1.09
J0253+3217	A	0.37	0.579 ± 0.032	43	0.276 ± 0.014	3070	190	39	-9.0	259	205	5	1.01
J0254+2343	A	0.05	0.342 ± 0.035	48	0.340 ± 0.027	3060	245	39	-8.7	186	170	5	0.99
J0310+3814	B	0.44	0.320 ± 0.017	58	0.272 ± 0.021	3050	193	40	-29.3	190	182	9	1.35
J0313+4120	B	0.89	0.823 ± 0.031	58	0.294 ± 0.018	3020	178	39	-30.9	663	349	8	1.26
J0319+4130	A	12.06	4.690 ± 0.181	26	0.506 ± 0.054	3064	155	33	-12.2	7677	978	10	1.16
J0319+4130	B	12.15	9.885 ± 0.206	55	0.357 ± 0.074	2972	170	44	-24.1	8865	724	9	1.12
J0319+4130	C	13.85	3.290 ± 0.126	67	0.158 ± 0.017	1634	185	116	2.7	3504	625	6	0.66
J0325+2224	C	0.90	0.879 ± 0.037	39	0.266 ± 0.010	3131	203	37	-9.0	621	370	12	1.12
J0325+4655	C	0.27	0.258 ± 0.018	33	0.074 ± 0.008	3135	127	40	-9.3	190	88	4	0.81
J0333+6536	C	0.07	0.189 ± 0.020	40	0.158 ± 0.013	3050	109	37	-12.0	77	64	3	1.04
J0344+6827	A	0.06	0.187 ± 0.023	62	0.136 ± 0.007	3138	122	39	-35.5	105	97	3	1.10

Notes. Columns: (1) – IAU source name (J2000); (2) – observing epochs – A: October 2010; B: May 2011 and C: October 2011; (3) – total single dish flux density measured at 86 GHz obtained from the pointing and calibration scan measurements at Pico Veleta or Plateau de Bure (Jy); (4),(6) – correlated flux densities (Jy) measured on projected baseline lengths listed in Cols. (5) and (7) (Mλ); (8) – major axis of the restoring beam (μas); (9) – minor axis of the restoring beam (μas); (10) – position angle of the major axis (degrees); (11) – total clean flux density (mJy); (12) – peak flux density (mJy beam $^{-1}$); (13) – off-source rms noise in the residual image (mJy beam $^{-1}$); (14) – quality factor of the residual noise in the image. The full table is available at the CDS and in a machine-readable and Virtual Observatory (VO) forms in the online journal.

an order of magnitude already on sub-parsec scales in the jets, with inverse Compton, synchrotron, and adiabatic losses subsequently dominating the energy losses (cf. [Marscher 1995](#); [Lobanov & Zensus 1999](#)). Only 8% of the jet cores show a brightness temperature greater than 5×10^{11} K and only 3% have a brightness temperature greater than 10^{12} K.

We also inspect the distribution of the minimum and maximum limiting brightness temperature of the core components (using averaged values of brightness temperature for objects with multiple observations) in the sample, making these estimates from the visibility amplitudes on the longest baselines ([Lobanov 2015](#)). The minimum, $T_{b,\text{min}}$, and limiting, $T_{b,\text{lim}}$, brightness temperatures are given in Table 7, in Cols. 10 and 11, respectively.

The median and mean of the maximum limiting brightness temperature distribution for the core regions is 1.06×10^{11} K and 3.0×10^{11} K, respectively. We find that the limiting $T_{b,\text{lim}}$ correlates well with $T_{b,\text{mod}}$ estimated from imaging method as seen in Fig. 8, supporting the fidelity of $T_{b,\text{mod}}$ measurements obtained from model fitting. The residual logarithmic distribution of the $T_{b,\text{mod}}/T_{b,\text{lim}}$ ratio is well approximated by the Gaussian PDF, with mean value, $\mu = 0.001$ and standard deviation, $\sigma = 0.46$.

5. Discussion

5.1. Modelling the observed brightness temperatures

The brightness temperature distribution can be used for obtaining estimates of the conditions in the extra galactic radio sources and to test the models proposed for the inner jets ([Marscher 1995](#); [Lobanov et al. 2000](#); [Homan et al. 2006](#); [Lee et al. 2008](#)). A basic population model ([Lobanov et al. 2000](#)) can be used for representing the observed brightness temperature distribution under the assumption that the jets have the same intrinsic brightness temperature, T_0 , Lorentz factor, Γ_j , and synchrotron spectral index, α ($S_\nu \propto \nu^\alpha$), and they are randomly oriented in space (within the limits of viewing angles, θ , required by Doppler boosting bias). The jets are also assumed to remain straight within the spatial scales (~ 0.5 – 10 pc) probed by the observations.

The assumptions of single values of T_0 and Γ_j describing the whole sample are clearly simplified, as jets are known to feature a range of Lorentz factors (see [Lister et al. 2016](#), and references therein). However, as has been shown earlier ([Lobanov et al. 2000](#)), factoring a distribution of Lorentz factors into the present model is not viable without amending the brightness temperature measurements with additional information, prefer-

Fig. 7. Compactness parameters, S_{86}/S_{CLEAN} and $S_{\text{core}}/S_{\text{CLEAN}}$ are shown on the *left* and *right panel* respectively, where S_{86} is the single dish 86GHz flux density measured at Pico Veleta or Plateau de Bure. The Pearson correlation coefficients $\rho(S_{86}, S_{\text{CLEAN}}) = 0.908$ and $\rho(S_{\text{core}}, S_{\text{CLEAN}}) = 0.874$ are obtained for the combined data from this survey and Lee et al. (2008).

Table 7. Model fit parameters.

Source (J2000) (1)	Obs (2)	Comp (3)	S_{tot} (4)	S_{peak} (5)	d (6)	r (7)	θ (8)	T_b (9)	$T_{b,\text{min}}$ (10)	$T_{b,\text{lim}}$ (11)
J0013+4051	C	1	288 ± 71	278 ± 49	<14	...	...	>28.642	4.46	9.69
J0013+4051	C	2	194 ± 61	136 ± 35	34 ± 9	41 ± 4	-30.5 ± 6.2	3.428 ± 1.647	...	...
J0017+8135	B	1	99 ± 22	69 ± 12	30 ± 5	...	...	8.115 ± 2.745	1.89	3
J0017+8135	B	2	35 ± 18	11 ± 5	77 ± 38	431 ± 19	-179.3 ± 2.5	0.435 ± 0.377	...	...
J0030+7037	B	1	121 ± 26	90 ± 16	26 ± 5	...	...	2.947 ± 0.970	1.78	2.26

Notes. Columns: (1) – IAU source name(J2000); (2) – observing epochs – A: October 2010; B: May 2011 and C: October 2011; (3) – I.D. number of Gaussian model fit component; (4) – total flux density of the component (mJy); (5) – peak flux density of the component (mJy beam^{-1}); (6) – component size (μas), or upper limits; (7) – component’s offset from the core (μas); (8) – position angle of the offset (degrees); (9) – brightness temperature obtained from the model fits ($\times 10^{10}$ K), or lower limits; (10) – visibility based estimate of the minimum brightness temperature ($\times 10^{10}$ K); (11) – visibility based estimate of the maximum resolved brightness temperature ($\times 10^{10}$ K). The full table is available at the CDS and in a machine-readable and Virtual Observatory (VO) forms in the online journal.

ably about the apparent speeds of the target sources. We are currently compiling such a combined database, and will engage in a more detailed modelling of the compact jets after the completion of this database.

In a population of jets described by the settings summarized above, the measured brightness temperature, T_b , is determined solely by the relativistic Doppler boosting of the jet emission. Therefore, the observed brightness temperature, T_b , can be related to the intrinsic brightness temperature, T_0 , so that $T_b = T_0 \delta^{1/\epsilon}$, where the power index ϵ is $1/(2 - \alpha)$ for a continuous jet (steady state jet) and $1/(3 - \alpha)$ for a jet with spherical blobs (or optically thin “plasmoids”), and δ is the Doppler factor.

The probability of finding a radio source with the brightness temperature T_b in such a population of sources is

$$p(T_b) \propto \left[\frac{2 \Gamma_j (T_b/T_0)^\epsilon - (T_b/T_0)^{2\epsilon} - 1}{\Gamma_j^2 - 1} \right]^{\frac{1}{2}}. \quad (7)$$

The lower end of the observed distribution of brightness temperatures depends on the sensitivity of VLBI data since

the flux of the observed sample is biased by Doppler boosting (Lobanov et al. 2000). The lowest brightness temperature that can be measured from our data, $T_{b,\text{sens}}$, can be obtained from

$$T_{b,\text{sens}}[\text{K}] = 1.65 \times 10^5 \left(\frac{\sigma_{\text{rms}}}{\text{mJy beam}^{-1}} \right) \left(\frac{b}{\text{mas}} \right)^{-2}, \quad (8)$$

where σ_{rms} is the array sensitivity in mJy beam^{-1} and b is the average size of the resolving beam. In this survey, the typical observation time on a target source Δt is 20 min and bandwidth is 128 MHz. Therefore, the value of beam size for the sources in this survey is 0.12 mas and the σ_{rms} of the array is $0.54 \text{ mJy beam}^{-1}$. Thus, we have obtained a 3σ level estimation of $T_{b,\text{sens}}$ as $2.0 \times 10^8 \text{ K}$ using Eq. (8), which is set as the lowest brightness temperature in modelling.

We normalize the results obtained from Eq. (7) to the number of objects in the lowest bin of the histogram. For our modelling, we first make a generic assumption of $\alpha = -0.7$ (homogeneous synchrotron source) and use $\Gamma_j \approx 10$ implied from the kinematic analysis of the MOJAVE VLBI survey data (Lister et al. 2016). We assume that the jet is continuous, so $\epsilon = 0.37$ is

Fig. 8. Comparison of $T_{b,mod}$ measured from circular Gaussian representation of source structure and $T_{b,lim}$ estimated from the interferometric visibilities at uv -radii within 10% of the maximum baseline B_{max} in the data for a given source (*top panel*). Correlation between the two distributions is illustrated by the residual logarithmic distribution of the $T_{b,mod}/T_{b,limit}$ ratio (*bottom panel*), which is well approximated by the Gaussian distribution with $\mu = 0.001$ and $\sigma = 0.46$.

taken. For the population modelling analysis, we have included the data from Lobanov et al. (2000), Lee et al. (2008), and the present survey, yielding a final database of 271 VLBI core components and 344 jet components. For objects with multiple measurements, we have used the median of the measurements. The resulting model distributions obtained for various values of T_0 are shown in Figs. 9–10 for the VLBI cores and the inner jet components, respectively.

This approach yields $T_{0,core} = (3.77^{+0.10}_{-0.14}) \times 10^{11}$ K for the VLBI cores and $T_{0,jet} = (1.42^{+0.16}_{-0.19}) \times 10^{11}$ K for the inner jet components. The estimated $T_{0,core}$ is in good agreement with the inverse Compton limit of $\approx 5.0 \times 10^{11}$ K (Kellermann & Pauliny-Toth 1969), beyond which the inverse Compton effect causes rapid electron energy losses and extinguishes the synchrotron radiation. The inferred $T_{0,jet}$ of jet components are about a factor of three higher than the equipartition limit of $\approx 5 \times 10^{10}$ K (Readhead et al. 1983) for which the magnetic field energy and particle energy are in equilibrium. This may indicate that opacity is still non-negligible in these regions of the flow. The intrinsic brightness temperature obtained for the cores is within the upper limit

Fig. 9. Distribution of the brightness temperatures, T_b , measured in the core components and represented by the population models calculated for $\Gamma_j = 10$ and different values of T_0 . The best approximation of the observed T_b distribution is obtained with $T_{0,core} = (3.77^{+0.10}_{-0.14}) \times 10^{11}$ K. For better viewing of the observed distribution, one core component with a very high $T_b = 5.5 \times 10^{12}$ K for the source BL Lac obtained from Lee et al. (2008) is not shown but is included in the modelling.

Fig. 10. Distribution of the brightness temperatures, T_b , measured in the inner jet components and represented by the population models calculated for $\Gamma_j = 10$ and different values of T_0 . The best approximation of the observed T_b distribution is obtained with $T_{0,jet} = (1.42^{+0.16}_{-0.19}) \times 10^{11}$ K.

5.0×10^{11} K predicted for the population modelling of the cores (Lobanov et al. 2000).

A simultaneous fit for T_0 and Γ_j is impeded by the implicit correlation, $T_0 \propto \Gamma_j^a$ (with $a \approx 2-3$), between these two parameters, as implied by Eq. (7). This is also illustrated in Fig. 11, from which a dependence $T_0[\text{K}] \approx (7.7 \times 10^8) \Gamma_j^{2.7}$ can be inferred for the fit to the brightness temperatures measured in the VLBI cores. This correlation between T_0 and Γ_j precludes simultaneously fitting for both these parameters, and hence the Lorentz factor has to be constrained (or assumed) separately. One should also keep in mind that this correlation results from the model description and does not have an immediate physical

Fig. 11. Two-dimensional χ^2 distribution plot in the $\Gamma_j - T_0$ space, calculated for the brightness temperatures measured in the VLBI cores. The blank area shows the ranges of the parameter space disallowed by the observed distribution. The distribution of the χ^2 values indicates a $(\Gamma_j - T_0)$ correlation, with $T_0[\text{K}] \approx (7.7 \times 10^8) \Gamma_j^{2.7}$, thus precluding a simultaneous fit for Γ_j and T_0 .

implication. Equation (7) clearly shows that the predicted distribution of T_b is valid within the range

$$\left(\Gamma_j - \sqrt{\Gamma_j^2 - 1} \right) \leq \left(\frac{T_0}{T_b} \right)^\epsilon \leq \left(\Gamma_j + \sqrt{\Gamma_j^2 - 1} \right). \quad (9)$$

The region outside this range is represented by the blank area in Fig. 11.

The intrinsic brightness temperature we obtained is higher than the mean and median observed brightness temperature T_b . This is readily explained by the Doppler deboosting. For a given viewing angle, θ , sources with $\Gamma_j > 1/\theta$ would be deboosted so that the observed brightness temperature will be reduced below its intrinsic value. It can be easily shown that the observed and intrinsic brightness temperatures are equal if the jet viewing angle is given by

$$\theta_{\text{eq}} = \arccos \left[\frac{1 - (1/\Gamma_j) (T_0/T_b)^\epsilon}{\sqrt{1 - \Gamma_j^{-2}}} \right]. \quad (10)$$

For the VLBI cores, the mean of the observed T_b is 1.8×10^{11} K and intrinsic $T_{0,\text{core}}$ is 3.77×10^{11} K, therefore, the resulting $\theta_{\text{eq}} = 29^\circ$ for $\Gamma_j = 10$ and $\epsilon = 0.37$. In this case any object observed at a larger viewing angle would be deboosted resulting in a lower observed T_b than intrinsic T_0 .

5.2. Testing the adiabatic expansion of jets

As discussed in Sects. 4.3 and 5.1, intrinsic T_0 and the observed T_b in core and jets show that the brightness temperature drops by approximately a factor of two to ten already on sub-parsec scales in the jets. This evolution might occur with the inverse Compton, synchrotron, and adiabatic losses subsequently dominating the energy losses (cf., Marscher 1995; Lobanov & Zensus 1999).

For four objects in our data (3C84, 0716+714, 3C454.3, and J2322+507) for which multiple jet components have been identified during the model fitting, it is possible to use the brightness

temperatures of the jet components to test whether the evolution of the jet brightness on sub parsec scales could be explained by adiabatic energy losses (Marscher & Gear 1985). For this analysis, we assume that the jet components are independent relativistic shocks embedded in the jet plasma, which has a power-law distribution $N(E) dE \propto E^{-s} dE$, where s is the energy spectral index that depends on spectral index α as $\alpha = (1 - s)/2$, and is pervaded by the magnetic field $B \propto d^{-a}$, where d is the width of the jet and a depends on the type of magnetic field ($a = 1$ for poloidal magnetic field and 2 for toroidal magnetic field). With these assumptions, we can relate the brightness temperatures, $T_{b,J}$, of the jet components to the brightness temperature, $T_{b,C}$, of the core (Lobanov et al. 2000; Lee et al. 2008),

$$T_{b,J} = T_{b,C} \left(\frac{d_J}{d_C} \right)^{-\xi}, \quad (11)$$

where d_J and d_C are the measured sizes of the jet component and core, respectively, and

$$\xi = \frac{2(2s + 1) + 3a(s + 1)}{6}. \quad (12)$$

Assuming the synchrotron emission with spectral index $\alpha = -0.5$, we use $s = 2.0$ and adopt $a = 1.0$ for the description of the magnetic field in the jet. With these assumptions, we calculate the predicted $T_{b,J}$ for individual jet components and compare them in Fig. 12 to the measured brightness temperatures. The measured and predicted values of brightness temperature agree well, and this suggests that the jet components can be viewed as adiabatically expanding relativistic shocks (cf., Kadler et al. 2004; Pushkarev & Kovalev 2012; Kravchenko et al. 2016).

6. Summary

We have used the Global Millimeter VLBI Array (GMVA) to conduct a large global 86 GHz VLBI survey comprising 174 snapshot observations of 162 unique targets selected from a sample of

Fig. 12. Changes of the brightness temperature as a function of jet width for four sources – J2322+5037, J1033+6051, 3C 345, and 0716+714 from this survey. Blue squares denote the measured T_b from this survey. The red circles connected with a dotted line represent theoretically expected T_b under the assumption of adiabatic jet expansion. The initial brightness temperature in each jet is assumed to be the same as that measured in the VLBI core.

compact radio sources. The survey observations have reached a typical baseline sensitivity of 0.1 Jy and a typical image sensitivity of 5 mJy beam^{-1} , owing to the increased recording bandwidth of the GMVA observations and the participation of very sensitive European antennae at Pico Veleta and Plateau de Bure. All of the 162 objects have been detected and imaged, thereby increasing the total number of AGN imaged with VLBI at 86 GHz by a factor of ~ 1.5 . We imaged 138 sources for the first time with VLBI at 86 GHz through this survey.

We have used Gaussian model fitting to represent the structure of the observed sources and estimate the flux densities and sizes of the core and jet components. We used the model fit parameters and visibility data on the longest baselines to make independent estimates of brightness temperatures at the jet base as described by the most compact and bright “VLBI core” component. These estimates are consistent with each other. For sources with extended structure detected, the model fit parameters have been also used to calculate brightness temperature in the jet components downstream from the core. The apparent brightness temperature estimates for the jet cores in our sample range from $2.5 \times 10^9 \text{ K}$ to $1.3 \times 10^{12} \text{ K}$, with the mean value of $1.8 \times 10^{11} \text{ K}$. The brightness temperature estimates for the inner jet components in our sample range from $7.0 \times 10^7 \text{ K}$

to $4.0 \times 10^{11} \text{ K}$. The overall amplitude calibration error for the observations is about 25%.

We describe the observed brightness temperature distributions by a basic population model which assumes that all jets are intrinsically similar and can be described by a single value of the intrinsic brightness temperature, T_0 , and Lorentz factor, Γ_j . The population modelling shows that our data are consistent with a population of sources that has $T_0 = (3.77^{+0.10}_{-0.14}) \times 10^{11} \text{ K}$ in the VLBI cores and $T_0 = (1.42^{+0.16}_{-0.19}) \times 10^{11} \text{ K}$ in the jets, both obtained for $\Gamma_j = 10$ adopted from the kinematic analysis of the MOJAVE VLBI survey of AGN jets (Lister et al. 2016). A correlation between T_0 and Γ_j inherent to the model description precludes fitting for these two parameters simultaneously. We find that a relation $T_0[\text{K}] \approx (7.7 \times 10^8) \Gamma_j^{2.7}$ is implied for this modelling framework by the survey data. For sources with sufficient structural detail, there is an agreement between the brightness temperatures measured in multiple components along the jet and the predicted brightness temperatures for relativistic shocks with adiabatic losses dominating the emission.

The results of the survey can be combined with brightness temperature measurements made from VLBI observations at lower frequencies (e.g., Kovalev et al. 2005; Petrov et al. 2007) to study the evolution of T_0 with frequency and along the jet

(Lee et al. 2008, 2016). This approach can be used to better constrain the bulk Lorentz factor and the intrinsic brightness temperature, to distinguish between the acceleration and deceleration scenario for the flow (cf., Marscher 1995), and to test several alternative acceleration scenarios including hydrodynamic acceleration (Bodo et al. 1985), acceleration by tangled magnetic field (Heinz & Begelman 2000), and magnetohydrodynamics acceleration (Vlahakis & Königl 2004).

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Appendix A: Images, visibility amplitude distributions, and uv -coverages of the survey targets

Fig. A.1. A total of 174 contour maps of 162 unique sources imaged at 3 mm in this survey (*left panel*), shown together with the respective radial amplitude distributions (*right panel*) and uv -coverages (inset in the *right panel*) of the respective visibility datasets. The contouring of images is made at $3\sigma_{\text{rms}} \times (-1, 1, \sqrt{2}, 2, \dots)$ levels, with σ_{rms} representing the off-source rms noise in the residual image. The off-source rms noise in the residual image σ_{rms} is given in Table 7 and the lowest contour, which is $3\sigma_{\text{rms}}$, is indicated at the bottom right of the image figure panels.

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