

Exploring the bulk of the BL Lacertae object population

II. Gamma-ray properties

F. D'Ammando¹, M. Giroletti¹, and S. Rainó^{2,3}

¹ INAF Istituto di Radioastronomia, via Gobetti 101, 40129 Bologna, Italy
e-mail: dammando@ira.inaf.it

² Dipartimento Interateneo di Fisica “M. Merlin” dell’Università e del Politecnico di Bari, 70126 Bari, Italy

³ Istituto Nazionale di Fisica Nucleare, Sezione di Bari, 70126 Bari, Italy

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ABSTRACT

Aims. We are studying an unbiased sample of 42 nearby ($z < 0.2$) BL Lacertae objects with a multi-wavelength approach. The results of Very Long Baseline Interferometry observations were presented in the first paper of this series. In this paper, we study the γ -ray properties of the sample.

Methods. We analyse data collected by the *Fermi*-Large Area Telescope (LAT) during its first 8.5 yr of operation in the energy range 0.1–300 GeV.

Results. We reveal 23 sources with a test statistic greater than 25 (corresponding to $\sim 4.6\sigma$) out of 42, with 3 sources not detected in the third LAT active galactic nucleus (AGN) catalogue, and fluxes between 3.5×10^{-10} and 7.4×10^{-8} ph cm⁻² s⁻¹. The majority of the sources have hard spectra ($\Gamma \leq 2$), with only four having values in the range 2.1–2.4. The three newly detected sources have fluxes in the range between 0.54×10^{-9} and 1.35×10^{-9} ph cm⁻² s⁻¹ and photon index 1.7–1.9. Among the 23 LAT-detected sources, 19 are included in the third catalogue of hard *Fermi*-LAT sources, with a spectrum that connects relatively smoothly from 0.1 GeV to 2 TeV. LAT-detected BL Lacs are more luminous on parsec scales with respect to non-LAT-detected sources and have larger core dominance according to the unified models.

Conclusions. The LAT-detected BL Lacs seem to be composed of a bulk of “classical” sources dominated by Doppler boosting and characterised by compact and bright radio emission as well as hard γ -ray spectra. Moreover, we have identified a possible population of low-luminosity BL Lacs not detected by LAT, lacking a VLBI core, and with a small Doppler factor. Furthermore, three LAT-detected sources show non-classical properties for γ -ray emitting BL Lacs (no evidence of relativistic jet, low Doppler factor in radio images, relatively low core dominance) and three other sources, while showing radio emission on parsec scales, are not detected in γ rays so far.

Key words. BL Lacertae objects: general – gamma rays: galaxies – galaxies: active – galaxies: jets

1. Introduction

Blazars are the rarest and yet most extreme class of active galactic nuclei (AGNs), characterised by the presence of a relativistically beamed jet of plasma pointing within a few degrees of our line of sight. On the basis of their optical spectra, they are classified as flat spectrum radio quasars (FSRQs, characterised by strong emission lines) or BL Lacertae objects (BL Lacs, with nearly featureless optical spectra). Besides the difference in optical spectra, the two classes differ in many other observational properties, including luminosity, accretion regime, spectral energy distribution (SED), morphology and kinematics of the radio jet, and evolution over cosmic time (e.g. Ackermann et al. 2015; Ghisellini et al. 2017; Jorstad et al. 2017).

In Liuzzo et al. (2013; hereafter Paper I), a sample of 42 BL Lacs has been selected purely on their optical spectra. The sources were selected from the Roma BZCAT catalogue of known blazars (Massaro et al. 2009) to have a measured redshift $z < 0.2$ and to be located within the sky area covered by the Sloan Digital Sky Survey (SDSS, Abazajian et al. 2009). These two criteria allow us to study with high resolution the bulk of the BL Lac population, including the weakest

sources, and grant us the availability of good multi-wavelength coverage.

The results of a dual-frequency Very Long Baseline Interferometry (VLBI) survey of the sample were presented in Paper I of this series. Out of the 42 sources in the sample, 27 sources (64%) were detected on parsec scales. A radio source can remain undetected in a VLBI observation if it is either below the image sensitivity limit defined by the observation setup or if the bulk emission is distributed over scales substantially larger than the restoring beam of the experiment (typically 1–10 parsec in the case of Liuzzo et al. 2013). Among the sources detected by the VLBI observations, some appeared to be of the “classical” type, that is, bright, compact, with flat spectra and large core dominance (ratio of compact to extended flux). On the other hand, several sources are faint (down to a few mJy and a monochromatic luminosity of $P_r \sim 10^{23.5}$ WHz⁻¹), with moderately steep radio spectra and low core dominance. These properties, in addition to the 15 non-detections, suggest that a significant fraction of BL Lacs are not strongly Doppler boosted.

It is therefore of great importance to study the same population also at high energy. Since the start of operation of the Large Area Telescope (LAT) on board the *Fermi* Gamma-ray Space Telescope, the number of BL Lacs detected in γ rays has rapidly

Table 1. List of BL Lac sources in our sample.

Source name	RA (J2000) deg	Dec (J2000) deg	Redshift	3FGL name	Photon index	Flux ($E > 0.1$ GeV) (10^{-9} ph cm $^{-2}$ s $^{-1}$)
J0751+1730	117.8545	17.5142	0.185	–		
J0751+2913	117.7899	29.2265	0.194	–		
J0753+2921	118.3525	29.3589	0.161	–		
J0754+3910	118.6545	39.1799	0.096	–		
J0809+3455	122.4120	34.9270	0.083	3FGL J0809.6+3456	1.67 ± 0.13	1.56 ± 0.60
J0809+5218	122.4548	52.3163	0.138	3FGL J0809.8+5218	1.88 ± 0.02	34.90 ± 1.83
J0810+4911	122.7275	49.1844	0.115	–		
J0847+1133	131.8039	11.5639	0.199	3FGL J0847.1+1134	1.74 ± 0.12	2.86 ± 0.95
J0850+3455	132.6508	34.9230	0.145	3FGL J0850.2+3500	1.92 ± 0.20	2.09 ± 1.10
J0903+4055	135.8113	40.9333	0.188	–		
J0916+5238	139.2164	52.6412	0.19	–		
J0930+4950	142.6565	49.8404	0.187	3FGL J0930.0+4951	1.45 ± 0.21	0.56 ± 0.40
J1012+3932	153.2432	39.5442	0.171	–		
J1022+5124	155.5526	51.4001	0.142	–		
J1053+4929	163.4339	49.4989	0.14	3FGL J1053.7+4929	1.80 ± 0.10	3.63 ± 0.93
J1058+5628	164.6572	56.4698	0.143	3FGL J1058.6+5627	1.95 ± 0.03	32.40 ± 1.62
J1120+4212	170.2003	42.2034	0.124	3FGL J1120.8+4212	1.62 ± 0.06	5.04 ± 0.79
J1136+6737	174.1253	67.6179	0.136	3FGL J1136.6+6736	1.72 ± 0.08	3.21 ± 0.73
J1145–0340	176.3963	–3.6671	0.167	–		
J1156+4238	179.1940	42.6354	0.172	–		
J1201–0007	180.2758	–0.1171	0.165	–		
J1201–0011	180.4319	–0.1872	0.164	–		
J1215+0732	183.7958	7.5346	0.136	–		
J1217+3007	184.4670	30.1168	0.13	3FGL J1217.8+3007	1.97 ± 0.02	57.70 ± 2.75
J1221+3010	185.3414	30.1770	0.182	3FGL J1221.3+3010	1.97 ± 0.02	15.70 ± 1.67
J1221+2813	185.3820	28.2329	0.102	3FGL J1221.4+2814	2.10 ± 0.03	52.50 ± 2.65
J1221+0821	185.3836	8.3623	0.132	–		
J1231+6414	187.8808	64.2384	0.163	3FGL J1231.5+6414	1.94 ± 0.20	2.11 ± 1.18
J1253+0326	193.4458	3.4417	0.066	3FGL J1253.7+0327	1.84 ± 0.10	5.30 ± 1.45
J1257+2412	194.3830	24.2111	0.141	–		
J1341+3959	205.2713	39.9959	0.172	3FGL J1341.0+3955	2.54 ± 0.18	7.42 ± 2.33
J1419+5423	214.9442	54.3874	0.153	3FGL J1419.9+5425	2.31 ± 0.06	19.6 ± 2.20
J1427+5409	216.8761	54.1566	0.106	–		
J1427+3908	216.9413	39.1423	0.165	–		
J1428+4240	217.1361	42.6724	0.129	3FGL J1428.5+4240	1.58 ± 0.09	2.62 ± 0.64
J1436+5639	219.2408	56.6569	0.15	3FGL J1436.8+5639	1.99 ± 0.13	4.59 ± 1.46
J1442+1200	220.7012	12.0112	0.163	3FGL J1442.8+1200	1.80 ± 0.12	3.57 ± 1.14
J1510+3335	227.6716	33.5846	0.114	–		
J1516+2918	229.1733	29.3026	0.13	–		
J1534+3715	233.6967	37.2652	0.143	3FGL J1535.0+3721	2.11 ± 0.12	5.36 ± 1.47
J1604+3345	241.1938	33.7561	0.177	–		
J1647+2909	251.8619	29.1639	0.132	–		

Notes. Sources are sorted by increasing RA. Column 1: the source name; Cols. 2 and 3: Right ascension and declination in J2000; Col. 4: redshift taken from BZCAT; Col. 5: 3FGL name; Col 6: 3FGL photon index; Col 7: 3FGL integrated flux.

increased, reaching 632 in the third LAT AGN Catalog (3LAC, Ackermann et al. 2015): BL Lacs are now the most abundant population of γ -ray sources in the sky. Among the sources of our sample, 20/42 are listed in the 3LAC but it is natural to expect that, in the course of the ongoing all-sky survey executed by the LAT, more and more of the sources could be detected in γ rays. We list our sources in Table 1.

The main goal of the present paper is therefore to characterise the high-energy properties of the sample with a larger dataset and an improved LAT-data analysis. We present a dedicated analysis of 8.5 yr of *Fermi* data for all the sources in the sample, used to characterise the γ -ray detection rate, the γ -ray

flux, and the photon index. The paper is organised as follows. We present LAT data in Sect. 2 and the results in Sect. 3. We then discuss the results in Sect. 4, and compare them to the 3LAC, the γ -ray data above 10 GeV reported in the third catalogue of Hard Fermi-LAT sources (3FHL; Ajello et al. 2017) and the radio properties of our sample. Finally, we draw our conclusions in Sect. 5.

Throughout the paper, we use a Λ cold dark matter cosmology with $h = 0.68$, $\Omega_m = 0.31$, and $\Omega_\Lambda = 0.69$ (Ade et al. 2016). The γ -ray photon index Γ is defined such that $dN/dE \propto E^{-\Gamma}$. The quoted uncertainties are given at the 1σ level, unless otherwise stated.

2. Fermi-LAT data

The LAT, the primary instrument onboard the *Fermi* γ -ray observatory, is an electron-positron pair conversion telescope sensitive to γ -rays of energies from 20 MeV to >300 GeV. The LAT consists of a high-resolution silicon microstrip tracker, a CsI hodoscopic electromagnetic calorimeter, and an anticoincidence detector for the identification of charged-particle background. The full description of the instrument and its performance can be found in [Atwood et al. \(2009\)](#). The large field of view (~ 2.4 sr) allows the LAT to observe the full sky in survey mode every 3 h. The LAT point spread function (PSF) strongly depends on both the energy and the conversion point in the tracker, and less so on the incidence angle. For 1 GeV normal-incidence conversions in the upper section of the tracker, the PSF 68% containment radius is 0.8° ¹.

The *Fermi*-LAT data presented here have been obtained in a time period of 102 months from 2008 August 5 to 2017 January 31 in the 0.1–300 GeV energy range. During this time, the LAT instrument operated almost entirely in survey mode. The Pass 8 data ([Atwood et al. 2013](#)), based on a complete and improved revision of the entire LAT event-level analysis, were used. The analysis was performed with the ScienceTools software package version v10r0p5. Only events belonging to the “Source” class (evclass=128, evtype=3) were used. We selected only events within a maximum zenith angle of 90° to reduce contamination from the Earth limb γ rays, which are produced by cosmic rays interacting with the upper atmosphere. The spectral analysis was performed with the instrument response functions P8R2_SOURCE_V6 using a binned maximum-likelihood method implemented in the Science tool `gtlike`. Isotropic (“iso_source_v06.txt”) and Galactic diffuse emission (“gll_iem_v06.fit”) components were used to model the background ([Acero et al. 2016](#))². The normalization of both components was allowed to vary freely during the spectral fitting.

We analysed a region of interest of 30° radius centred at the location of each target. We used the coordinates of the γ -ray sources associated to the radio source as reported in the third *Fermi*-LAT catalogue of sources (3FGL; [Acero et al. 2015](#)). All BL Lacs of our sample included in the 3FGL have power-law spectra. If the source is not included in the 3FGL we used the radio coordinates of the source. We evaluated the significance of the γ -ray signal from the source by means of a maximum-likelihood test statistic (TS) defined as $TS = 2 \times (\log L_1 - \log L_0)$, where L is the likelihood of the data given the model with (L_1) or without (L_0) a point source at the position of the target (e.g. [Mattox et al. 1996](#)). The source model used in `gtlike` includes all the point sources from the 3FGL catalogue that fall within 40° of the target. The spectra of these sources were parametrized by a power-law, a log-parabola, or a super exponential cut-off, according to the model description in the 3FGL catalogue. We also included new candidates within 10° of our target from the preliminary LAT 8-year point source List (FL8Y)³.

For the sources under analysis, we modelled the data with a power-law function with both the normalization factor and photon index left free in the likelihood fit. A first maximum likeli-

hood analysis was performed over the whole period to remove the sources with $TS < 25$ from the model. A second maximum likelihood analysis was performed on the updated source model. In the fitting procedure, the normalization factors and the spectral parameters of the sources lying within 10° of the target were left as free parameters. For the sources located between 10° and 40° from our target, we kept the normalization and the spectral shape parameters fixed to the values from the catalogue.

For the new detected sources, we ran a point source localization using the `gtfindsrc` tool over the photons with $E > 1$ GeV extracted during the whole period. We also tried to parameterize the spectrum of these sources with a log parabola model, but the fit with a log parabola did not provide a statistically significant improvement with respect to a power-law. These three sources are included in the FL8Y list.

3. Results of the Fermi-LAT data analysis

Here, the γ -ray detection rate, fluxes, and photon indexes of the sources in our sample are reported. We detected 23 out of 42 sources with $TS \geq 25$ (corresponding to a $\sim 4.6\text{-}\sigma$ confidence level for two degrees of freedom). The results of our analysis for the LAT-detected sources are summarised in Table 2. For the sources not detected in our γ -ray analysis, a $2\text{-}\sigma$ upper limit of the integrated flux (assuming a photon index $\Gamma = 2$) is reported in Table 3. For two sources the likelihood analysis results in a TS between 10 and 25: J0754+3910 (TS = 12) and J0810+4911 (TS = 11). Adding more data, these sources could be detected by *Fermi*-LAT in the future.

We confirm the detection of all the sources previously reported in the 3FGL. In addition, three γ -ray sources not in the 3FGL and associated with BL Lacs in our sample have been revealed, raising the overall detection rate for the sample from 48% to 55%. We ran a localization of the three new detected sources, and the results are reported in Table 4. This further analysis confirms a strict spatial association between the γ -ray source and the radio counterpart associated with the BL Lac. Two out of three sources (J0916+5238 and J1215+0732) are included in the Brazil ICRANet Gamma-ray Blazar (IBIGB) catalogue ([Arsioli & Chang 2017](#)).

In Fig. 1, we show the distribution of the integral fluxes in the 0.1–300 GeV energy range (left panel), the photon indexes (middle panel), and the γ -ray luminosity (right panel) for the sources in our sample including $2\text{-}\sigma$ upper limits of the flux and corresponding luminosity for non-LAT-detected sources. The integral fluxes of the LAT-detected sources span the range between 3.5×10^{-10} and 7.4×10^{-8} $\text{ph cm}^{-2} \text{s}^{-1}$, with a peak at $\sim 4 \times 10^{-9}$ $\text{ph cm}^{-2} \text{s}^{-1}$. The photon index distribution has a peak at around $\Gamma = 1.7\text{--}2.0$, with only four sources having values in the range 2.1–2.4. The average photon index of the LAT-detected sources in our sample is $\langle \Gamma \rangle = 1.87 \pm 0.06$. The three new detected sources have fluxes below 1.4×10^{-8} $\text{ph cm}^{-2} \text{s}^{-1}$, luminosity below 2.5×10^{44} erg s^{-1} , and photon index 1.7–1.9.

For the sources not detected by LAT the $2\text{-}\sigma$ upper limit of the flux ranges between 0.2×10^{-9} and 2.7×10^{-9} $\text{ph cm}^{-2} \text{s}^{-1}$. The lack of detection of these sources in γ rays is in agreement with the LAT sensitivity limit⁴ estimated for 10 yr of observations assuming a photon index $\Gamma = 2$, that is, $1\text{--}2 \times 10^{-9}$ $\text{ph cm}^{-2} \text{s}^{-1}$.

All sources with luminosity $> 5 \times 10^{44}$ erg s^{-1} have been detected in γ rays by LAT. On the other hand, no sources have

¹ https://www.slac.stanford.edu/exp/glast/groups/canda/lat_Performance.htm

² <http://fermi.gsfc.nasa.gov/ssc/data/access/lat/BackgroundModels.html>

³ <https://fermi.gsfc.nasa.gov/ssc/data/access/lat/fl8y/>

⁴ http://www.slac.stanford.edu/exp/glast/groups/canda/lat_Performance.htm

Table 2. New analysis results for the LAT-detected sources.

Source name	TS	Flux (10^{-9} ph cm $^{-2}$ s $^{-1}$)	Photon index
J0809+3455	83	1.96 ± 0.51	1.90 ± 0.09
J0809+5218	6513	28.26 ± 1.02	1.85 ± 0.02
J0847+1133	242	4.11 ± 0.82	1.89 ± 0.08
J0850+3455	109	2.63 ± 0.57	1.93 ± 0.08
J0916+5238	34	0.54 ± 0.19	1.67 ± 0.11
J0930+4950	28	0.35 ± 0.17	1.50 ± 0.07
J1053+4929	216	2.71 ± 0.41	1.82 ± 0.06
J1058+5628	5001	24.45 ± 0.91	1.92 ± 0.02
J1120+4212	1246	4.45 ± 0.39	1.57 ± 0.03
J1136+6737	356	2.20 ± 0.19	1.68 ± 0.03
J1215+0732	57	1.35 ± 0.44	1.81 ± 0.11
J1217+3007	15910	74.12 ± 1.29	1.93 ± 0.01
J1221+3010	3127	16.53 ± 0.98	1.70 ± 0.02
J1221+2813	4812	43.94 ± 1.54	2.12 ± 0.02
J1231+6414	87	1.92 ± 0.47	1.94 ± 0.09
J1253+0326	370	8.23 ± 1.23	2.02 ± 0.06
J1341+3959	62	2.59 ± 0.56	2.16 ± 0.12
J1419+5423	1982	31.54 ± 1.30	2.41 ± 0.03
J1428+4240	512	2.02 ± 0.29	1.53 ± 0.05
J1436+5639	439	4.80 ± 0.66	1.89 ± 0.06
J1442+1200	280	3.40 ± 0.53	1.79 ± 0.06
J1534+3715	220	7.17 ± 0.87	2.18 ± 0.06
J1647+2909	29	0.81 ± 0.27	1.86 ± 0.11

Notes. Column 1: the source name; Col. 2: TS; Col. 3: flux in the 0.1–300 GeV energy range; Col. 4: γ -ray photon index.

been detected in γ rays below 8×10^{43} erg s $^{-1}$ so far, suggesting that a significant portion of the bulk of the BL Lac object population has not been probed yet with *Fermi*-LAT. There is no clear distinction between the distribution of the LAT-detected and non-LAT-detected sources in the range of luminosity $1\text{--}5 \times 10^{44}$ erg s $^{-1}$.

The LAT-detected and non-LAT-detected sources are equally distributed in redshift ($0.066 < z < 0.199$ for the former, $0.096 < z < 0.187$ for the latter), suggesting that the redshift has no impact on the γ -ray detection in our sample. A Kolmogorov–Smirnov (K–S) test (Press et al. 1992) does not show a significant difference between the redshift distributions of LAT-detected and non-LAT-detected BL Lacs in our sample.

If we consider the distribution of flux density at 1.4 GHz obtained by NRAO VLA Sky Survey (NVSS), it is evident that the radio flux densities of LAT-detected sources is usually higher than those of the non-LAT detected sources in our sample (Fig. 2). However there are 12 LAT-detected BL Lacs with flux density < 85 mJy (i.e. the flux limit of the VLBA Imaging and Polarimetry Survey, VIPS; Helmboldt et al. 2007), showing that our sample is representative of a population of LAT-detected BL Lacs for which pc-scale radio properties were unexplored in detail up to our VLBA observations.

4. Discussion

The project described in this work is aimed to improve our knowledge of the BL Lac population, through VLBI and *Fermi*-LAT observations of a sample of BL Lacs, independently of their γ -ray properties and with multi-wavelength information available on all targets.

Table 3. Analysis results for the non-LAT-detected sources.

Source name	Upper limit integrated flux (10^{-9} ph cm $^{-2}$ s $^{-1}$)
J0751+1730	0.23
J0751+2913	0.80
J0753+2921	0.24
J0754+3910	1.34
J0810+4911	1.14
J0903+4055	1.16
J1012+3932	0.38
J1022+5124	0.99
J1145–0340	1.94
J1156+4238	0.71
J1201–0007	2.35
J1201–0011	2.34
J1221+0821	2.72
J1257+2412	0.51
J1427+5409	2.68
J1427+3908	0.65
J1510+3335	1.08
J1516+2918	0.38
J1604+3345	2.34

Notes. Column 1: the source name; Col. 2: $2\text{-}\sigma$ upper limit of the integrated flux in the 0.1–300 GeV energy range.

4.1. Comparison with 3LAC

For the 20 sources already reported in the 3LAC, we show in Fig. 3 the plot of the flux and photon index obtained in this work with 8.5 yr of Pass 8 LAT data with respect to the values reported in the 3FGL for 4 yr of Pass 7 reprocessed LAT data. In Fig. 4, we show the ratio of the γ -ray fluxes obtained in 8.5 yr and 4 yr and the photon index variation in the two periods of LAT observations. The fluxes are in general in agreement, with a mean value of the ratio between the value over 8.5 yr and that reported in the 3FGL of 1.01 ± 0.28 . The most prominent outliers are: J1419+5423, whose flux has increased by 60%, and J1341+3959, whose flux decreased by a factor of three when considering 8.5 yr of LAT data. This is in agreement with the moderate variability usually observed in the LAT energy range for BL Lacs (e.g. Ackermann et al. 2015).

In the right panel of Fig. 3, we plot the 8.5-yr photon index versus the values reported in the 3FGL. The photon indexes are generally consistent, having $\langle \Delta\Gamma \rangle = \langle \Gamma_{8.5\text{-yr}} - \Gamma_{3\text{FGL}} \rangle = 0.08 \pm 0.16$. Only for J1341+3959 there is a hint of change of the photon index, from $\Gamma_{3\text{FGL}} = 2.54 \pm 0.18$ to $\Gamma_{8.5\text{-yr}} = 2.16 \pm 0.12$.

In general, variations in γ -ray flux and in photon index are not correlated. Neither softer-when-brighter nor harder-when-brighter trends are found, as shown by the comparison between the γ -ray flux ratio and the photon index variation presented in Fig. 4, with the exception of J1341+3959 that shows a softer-when-brighter trend.

In Fig. 5, we compare the γ -ray photon index and luminosity obtained over 8.5 yr for the 23 LAT-detected BL Lacs in our sample with values in the 3LAC for the other BL Lacs with known redshift, separating sources with $z < 0.2$ and $z > 0.2$. The average apparent γ -ray isotropic luminosity in the 0.1–300 GeV energy range of the LAT-detected sources in our sample ranges between 6×10^{43} and 6×10^{45} erg s $^{-1}$, which are typical luminosities for BL Lacs and within the range of

Table 4. Localization of the new γ -ray sources.

Source name	RA deg	Dec deg	95% error circle radius deg	Angular separation deg
J0916+5238	139.189	52.647	0.038	0.018
J1215+0732	183.773	7.519	0.039	0.027
J1647+2909	251.861	29.170	0.042	0.006

Notes. Column 1: the source name; Cols. 2 and 3: right ascension and declination of the γ -ray source; Col. 4: LAT 95% error circle radius; Col. 5: angular separation between the coordinates of the γ -ray source and those of the radio counterpart.

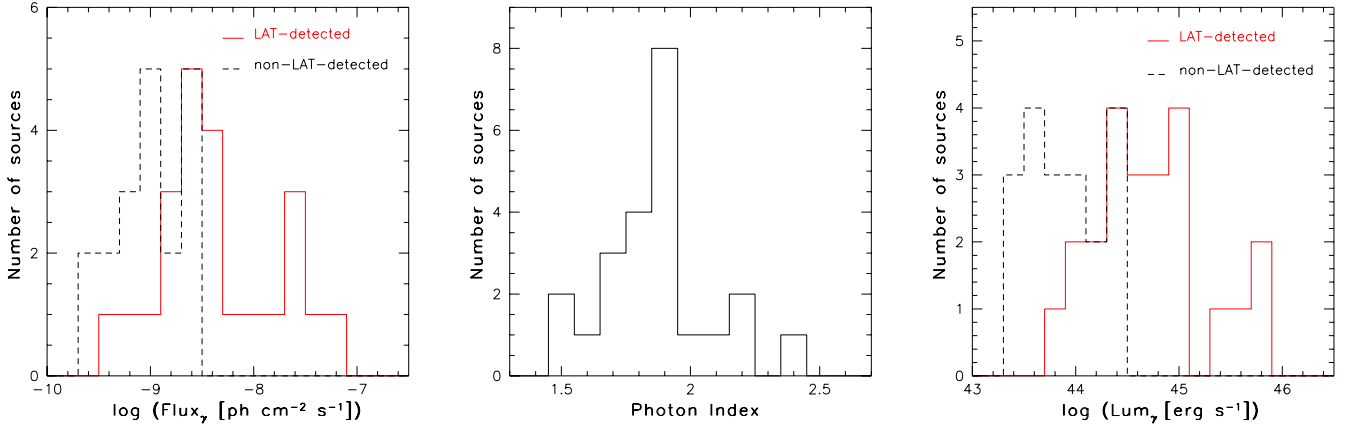


Fig. 1. Histogram of the distribution of various quantities obtained by the LAT analysis for the sources in our sample. Short dash line indicates non-LAT-detected sources ($TS < 25$), for which $2\text{-}\sigma$ upper limits of the flux are considered; red solid line indicates LAT-detected sources ($TS \geq 25$). *Left panel:* integral fluxes in the 0.1–300 GeV energy range; *middle:* γ -ray photon index for the 23 LAT-detected sources; *right:* γ -ray luminosity in the 0.1–300 GeV energy range.

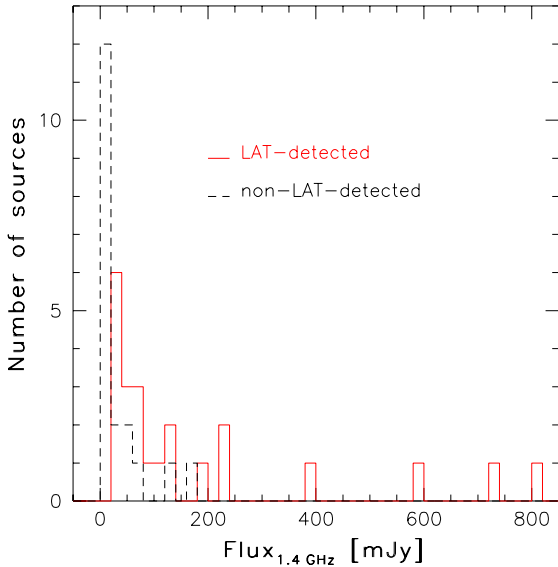


Fig. 2. Histogram of the NVSS flux at 1.4 GHz of the sources in our sample. Short dash line indicates non-LAT-detected sources ($TS < 25$), red solid line indicates LAT-detected sources ($TS \geq 25$).

values observed for the other BL Lacs with $z < 0.2$ in the 3LAC ($6 \times 10^{42} - 5 \times 10^{46} \text{ erg s}^{-1}$; Ackermann et al. 2015). In the same way, the average photon index of the LAT-detected sources ranges between 1.5 and 2.4, in agreement with what is observed for BL Lacs in the 3LAC. In particular, the average photon index of our sample, $\langle \Gamma_{8.5\text{-yr}} \rangle = 1.87 \pm 0.06$, is compatible with the average photon index reported in the 3LAC for the other BL

Lacs with $z < 0.2$, $\langle \Gamma_{3\text{LAC}, z < 0.2} \rangle = 1.95 \pm 0.11$. This suggests that the γ -ray spectra of the LAT-detected BL Lacs in our sample are similar to the spectra of the other BL Lacs in the 3LAC, in particular at $z < 0.2$. Further observations at other wavelengths are needed to investigate differences and similarities between the properties of this sample and those of the other BL Lacs detected by LAT.

Based on the frequency of the synchrotron peak ($\nu_{\text{peak}}^{\text{syn}}$), BL Lacs can be divided into low-synchrotron-peaked (LSP; $\nu_{\text{peak}}^{\text{syn}} < 10^{14} \text{ Hz}$), intermediate-synchrotron-peaked (ISP; $10^{14} < \nu_{\text{peak}}^{\text{syn}} < 10^{15} \text{ Hz}$), and high-synchrotron-peaked (HSP; $\nu_{\text{peak}}^{\text{syn}} > 10^{15} \text{ Hz}$) BL Lacs (Abdo et al. 2010). Based on the $\nu_{\text{peak}}^{\text{syn}}$ values reported in the 3LAC, among the LAT-detected sources in our sample 16 are HSP, 3 ISP, and 1 LSP BL Lac. Two out of the three new LAT-detected sources are classified as HSP BL Lac in the second Wide-field Infrared Survey Explorer (WISE) HSP catalogue (2WHSP; Chang et al. 2017). Among the 19 BL Lacs not detected by LAT, 11 are classified as HSP or HSP candidates in the 2WHSP; therefore in our sample 30 of 42 sources (71%) are classified as HSP or candidate HSP BL Lacs. Low-synchrotron-peaked sources are usually the brightest BL Lacs detected by LAT. The rising part and high-energy peak of the SED of HSP BL Lacs lies within the LAT energy range, favouring their detection by LAT, as shown by the large number of HSP BL Lacs in the 3LAC. Among the 30 HSP BL Lacs in our sample, 19 sources (63%) are detected in γ rays, while only 4 out of the 12 (33%) ISP/LSP BL Lacs have been detected by *Fermi*-LAT so far.

An anti-correlation between the synchrotron peak frequency and the LAT photon index measured over 8.5 yr is observed for the LAT-detected BL Lacs in our sample (Fig. 6), as

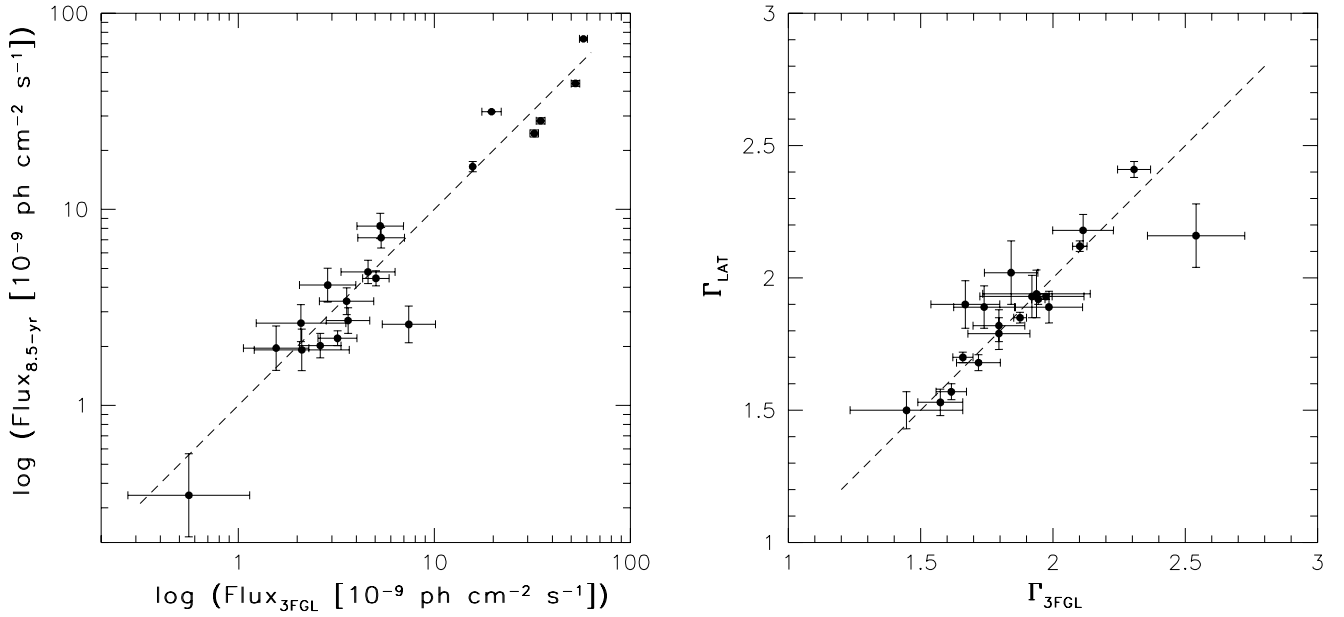


Fig. 3. γ -ray flux (left panel) and photon index (right panel) obtained in this work vs. the values reported in the 3FGL. A one-to-one reference short dashed line is plotted.

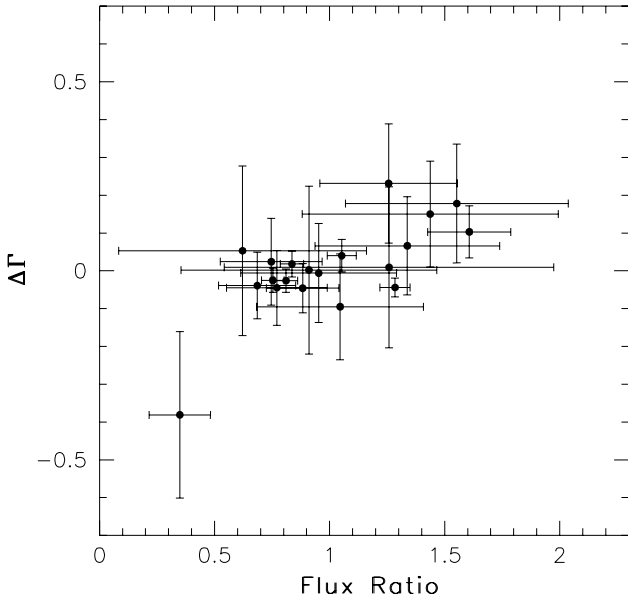


Fig. 4. Photon index difference between 8.5-yr and 3FGL values vs. flux ratio ($\text{Flux}_{8.5\text{-yr}}/\text{Flux}_{3\text{FGL}}$) is shown.

already observed for the whole sample of blazars reported in the 3LAC (Ackermann et al. 2015), and expected by the blazar sequence proposed by Fossati et al. (1998) and Ghisellini et al. (1998).

Only three HSP sources of our sample (SWIFT J1136+6738, SWIFT J1221+3012, and SWIFT J1428+4234) with very high synchrotron peak frequency (i.e. 10^{17} – 10^{18} Hz) are included in the 105-month *Swift*-BAT catalogue (Oh et al. 2018). These three sources have an X-ray photon index in the 14–195 keV energy range of 2.3–2.9 and a corresponding γ -ray photon index of 1.5–1.7, indicating that we are observing the declining part of the synchrotron emission in hard X-rays and the rising part of the inverse Compton emission in γ rays.

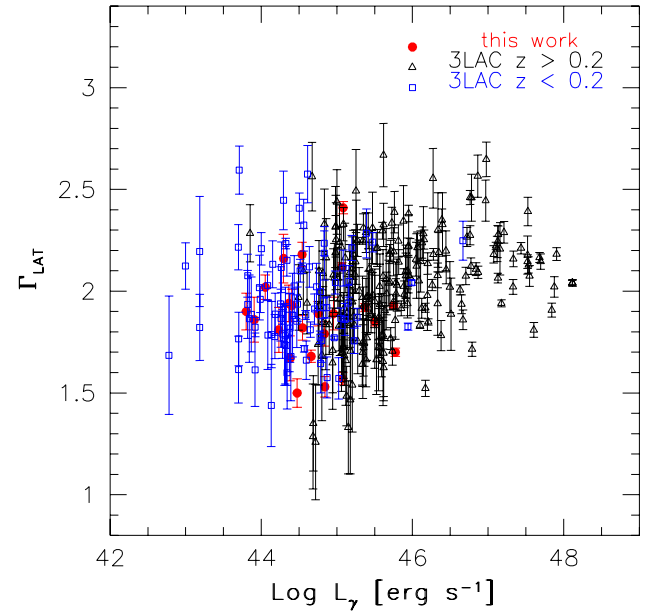


Fig. 5. Photon index vs. γ -ray luminosity in the 0.1–300 GeV energy range. Red stars: BL Lacs detected from our sample, black open triangles: BL Lacs in the 3LAC with $z > 0.2$, blue open squares: BL Lacs in the 3LAC with $z < 0.2$.

4.2. Comparison with 3FHL

In addition to the LAT catalogues with low-energy threshold of 0.1 GeV, three hard-source catalogues have been released, the most recent one being the 3FHL, based on 7yr of data analysed in the 10 GeV–2 TeV energy range. The 3FHL contains 1556 objects and takes advantage of the improvement provided by Pass 8 data by using the PSF-type event classification. The vast majority of detected sources (79%) are associated with extragalactic counterparts at lower energies; in particular, BL Lacs are the dominant extragalactic population (i.e. 750 objects). Among the 23 BL Lacs detected by *Fermi*-LAT

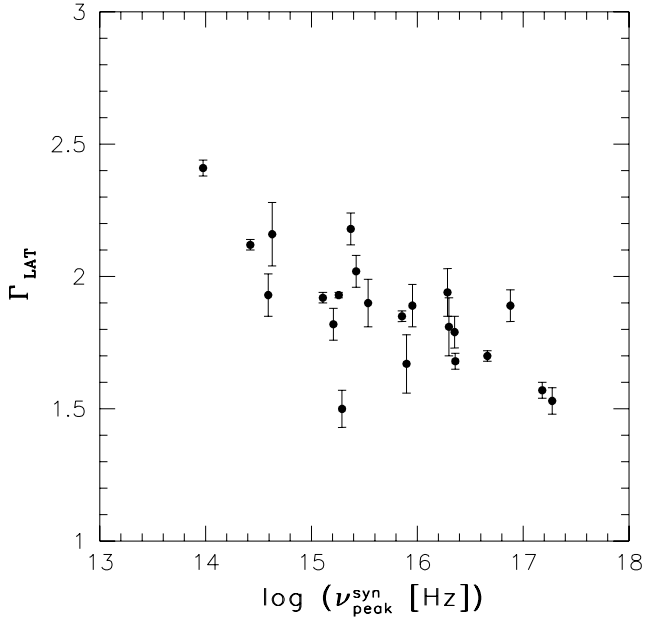


Fig. 6. γ -ray photon index vs. synchrotron peak frequency of the 22 LAT-detected sources in our sample with ν_{peak} estimated.

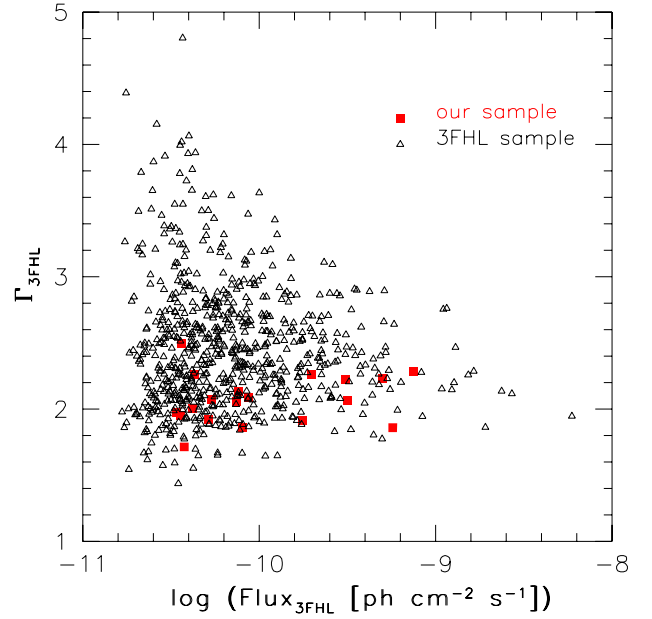


Fig. 8. Photon index vs. flux of the BL Lacs included in the 3FHL. Red squares show the BL Lacs included in our sample.

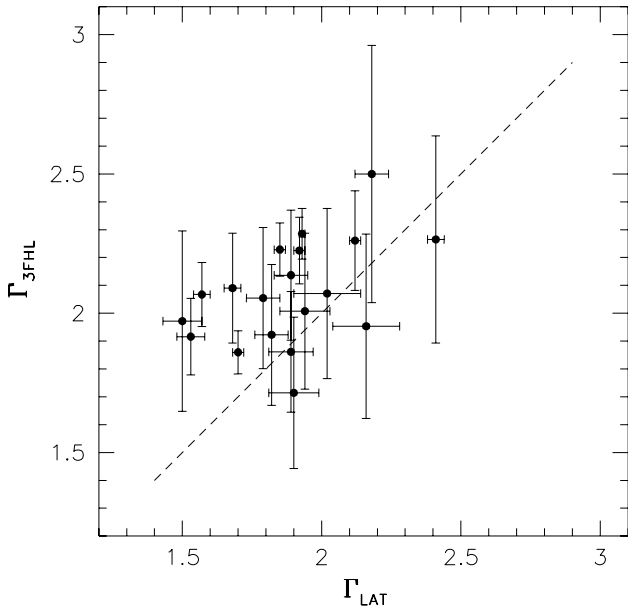


Fig. 7. 3FHL photon index vs. photon index estimated over 8.5 yr in the 0.1–300 GeV energy range. A one-to-one reference short dashed line is plotted.

in the 0.1–300 GeV energy range, 19 are included in the 3FHL. This is not surprising, considering that most of the LAT-detected sources in our sample are HSP, with the high-energy peak within the energy range covered by the 3FHL. All sources of our sample included in the 3FHL are also detected in the 0.1–300 GeV energy range. Among the 19 sources in the 3FHL, 9 are also detected at very high energy (VHE; $E > 100$ GeV) by the current Imaging Atmospheric Cherenkov Telescopes⁵. Moreover, 11 out of 19 3FHL sources are included also in the 2FHL (Ackermann et al. 2016), where a higher energy threshold of 50 GeV was considered for the analysis. Four 2FHL sources in

our sample (2FHL J0809.5+3455, 2FHL J1053.5+4930, 2FHL J1058.5+5625, 2FHL J1120.8+4212) are not detected at VHE and could be good targets for the current Cherenkov Telescopes.

The difference between the 3FHL photon index and the photon index estimated in this work in the 0.1–300 GeV energy range ranges between -0.21 and 0.50 . In Fig. 7 we compare the 3FHL photon index with the LAT photon index in the 0.1–300 GeV energy range. The average 3FHL photon index of the 19 sources in our sample is $\langle \Gamma_{\text{3FHL}} \rangle = 2.07 \pm 0.23$. As a comparison the average photon index estimated in this work in the 0.1–300 GeV energy range is $\langle \Gamma_{8.5\text{-yr}} \rangle = 1.88 \pm 0.05$, indicating a small difference between the photon index estimated in the two energy ranges. The difference between the two photon indices of the 19 LAT-detected sources in both samples is $-0.21 < \Delta \Gamma_{\text{3FHL}} \equiv (\Gamma_{\text{3FHL}} - \Gamma_{8.5\text{yr}}) < 0.50$, suggesting that the average γ -ray spectrum of these sources below 300 GeV connects rather smoothly with the spectrum in the 10 GeV–2 TeV energy range. For five sources, even considering the uncertainties, the 3FHL photon index is larger than the 3FGL photon index, suggesting a possible curvature in the overall γ -ray spectrum. Removing these five sources, the average photon index estimated in the 0.1–300 GeV energy range ($\langle \Gamma_{8.5\text{-yr}} \rangle = 1.99 \pm 0.06$) and in the 10 GeV–2 TeV energy range ($\langle \Gamma_{\text{3FHL}} \rangle = 2.11 \pm 0.25$) are still compatible. In case of sources with $\Delta \Gamma_{\text{3FHL}} < 0$, and therefore a harder 3FHL photon index value with respect to the 0.1–300 GeV value, the two photon indexes are compatible within the uncertainties, as shown in Fig. 7. This is an indication of no significant break or softening in the observed spectra between 0.1 GeV and 2 TeV. This should be related also to the small effect of absorption due to interactions with the extragalactic background light (EBL, Dominguez et al. 2011) on the spectra of BL Lacs at low redshift, such as those in our sample (see e.g. Dominguez & Ajello 2015).

In Fig. 8, we plot the γ -ray photon index versus flux in the 10 GeV–2 TeV energy range of the BL Lacs included in the 3FHL, with the 19 BL Lacs of our sample shown with filled red squares, with the 19 BL Lacs of our sample detected above 10 GeV have a photon index $\Gamma_{\text{3FHL}} < 2.6$, independently from the flux.

⁵ TeVCat v3.400: <http://tevcat.uchicago.edu/>

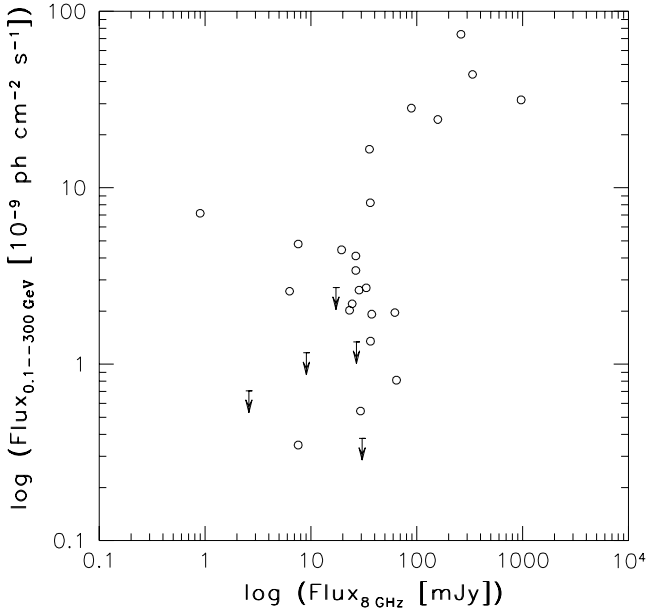


Fig. 9. Flux density at 8 GHz vs. γ -ray flux estimated in the 0.1–300 GeV energy range over 8.5 yr of LAT data. Arrows show $2\text{-}\sigma$ upper limits of the γ -ray flux.

Therefore, the photon index seems to be more important than the flux for detecting sources at high energies, at least when considering a sample in the same bin of redshift, that is, with similar effect of absorption due to interactions with the EBL. All the 3FHL sources in our sample are good candidates for future observations with the Cherenkov Telescope Array (Acharya et al. 2018).

4.3. Comparison with VLBI data at 8 and 15 GHz

Radio and γ -ray emission are strongly correlated in blazars (e.g. Ghirlanda et al. 2010; Ackermann et al. 2011; Richards et al. 2014; Mufakharov et al. 2015; Böck et al. 2016). However, given the small field of view of VLBI arrays, large surveys with milliarcsecond angular resolution are not available and for parsec scale studies one has to resort to dedicated pointed observations. Linford et al. (2012) present VLBI data for a large sample of γ -ray sources, including as many as 95 BL Lacs; interestingly, they find that LAT-detected BL Lacs do not differ significantly from a control sample of non-LAT-detected BL Lacs in terms of brightness and morphology.

The results of dual frequency (8 and 15 GHz) VLBA observations for the sources in our sample were presented in Paper I. Compact components were found for 27 sources. The presence of γ -ray emission and of a compact radio component seem to be well connected: 21 of the 23 LAT-detected sources (91%) reported in this paper have a VLBI component with respect to 6 of the 19 non-LAT-detected sources (32%). The only LAT-detected sources undetected at parsec scale are J0847+1133 and J1534+3715. However, the lack of detection of J0847+1133 is likely due to observational problems during VLBI observations reported in Paper I. Nevertheless, a compact emission has been observed with the European VLBI Network (EVN) at 5 GHz (Mantovani et al. 2015) and with VLBA at 8 GHz (Bourda et al. 2010) for this source. On the other hand, no radio emission has been revealed at both 8 GHz and 15 GHz for J1534+3715 with VLBA. It is worth noticing that this source has the lowest NVSS flux densities at 1.4 GHz among the

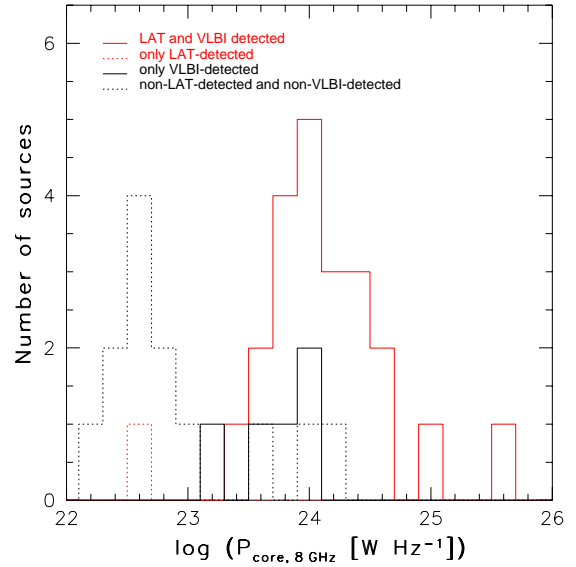


Fig. 10. Histogram of the core power at 8 GHz of the sources in our sample. Solid line indicates that the source is detected and short-dash line shows the upper limit. Red lines refer to LAT-detection and black lines refer to VLBI-detection.

LAT-detected sources in our sample, suggesting that the radio emission is not concentrated in the core region but extended emission is present on scales which are not probed by VLBI arrays.

The six non-LAT-detected sources with a compact component detected by VLBA have a 8 GHz flux density in the range 2.6–30.0 mJy with respect to the range of flux densities of 6.0–969.5 mJy for the LAT-detected sources. This result suggests that these sources are in the low-values part of the distribution of 8 GHz flux density in our sample. Comparing the γ -ray flux in the 0.1–300 GeV energy range with the 8 GHz flux density of the 27 sources for which parsec scale emission is detected by VLBA (Fig. 9), a connection between the radio and γ -ray emission is evident, in agreement with the radio/ γ -ray flux correlation reported in Ackermann et al. (2011). We calculate a Pearson correlation coefficient between 8 GHz flux densities and γ -ray fluxes and obtain $R = 0.5746$, indicating a moderate positive correlation (P -value = 0.001384).

In Fig. 10 we compare the VLBA core power at 8 GHz for 41 sources (J0751+2913 has not been observed at 8 GHz). Upper limits are reported for 14 sources (see Paper I, Table 5 for details); all of them are non-LAT-detected sources, except for J1534+371. The LAT-detected sources have on average a higher core power at 8 GHz, $\langle P_{\text{core}, 8 \text{ GHz}}^{\text{LAT}} \rangle = 1.3 \times 10^{24} \text{ W Hz}^{-1}$, with respect to non-LAT-detected sources, $\langle P_{\text{core}, 8 \text{ GHz}}^{\text{non-LAT}} \rangle = 1.4 \times 10^{23} \text{ W Hz}^{-1}$. All sources with $P_{\text{core}, 8 \text{ GHz}} > 2 \times 10^{24} \text{ W Hz}^{-1}$ have been detected in γ rays by LAT. On the other hand, only one source with $P_{\text{core}, 8 \text{ GHz}} < 3 \times 10^{23} \text{ W Hz}^{-1}$, J1534+3715, has been detected by LAT. This indicates that LAT-detected sources are the most luminous radio sources of our sample on parsec scale. Moreover, it suggests that there is a population of BL Lacs that lack a VLBI core, have a low γ -ray emission, and likely have a small Doppler factor. This is even more evident by comparing the γ -ray luminosity in the 0.1–300 GeV energy range with the radio luminosity of the core at 8 GHz (Fig. 11): the bottom-left part of the plot is populated by sources with a low luminosity in both the radio and γ -ray bands. All the sources that lie in that part of the

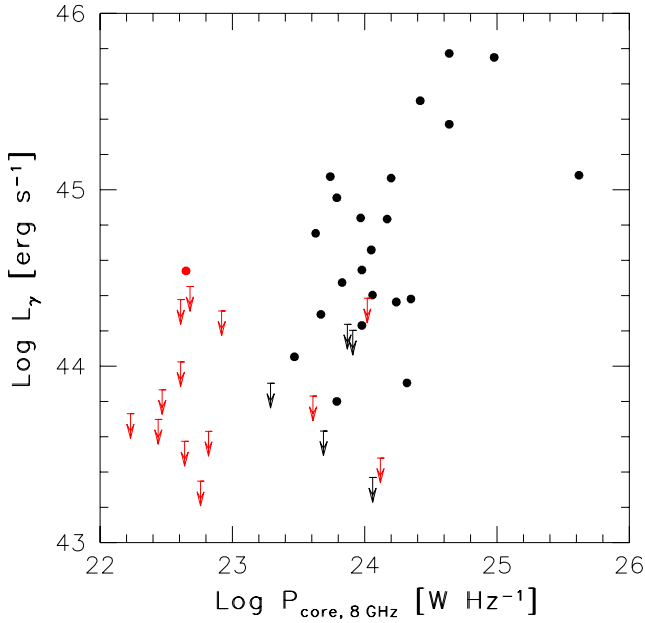


Fig. 11. Luminosity of the core at 8 GHz vs. γ -ray luminosity in the 0.1–300 GeV energy range for the sources in our sample. Filled circles indicate LAT-detected sources, while arrows show upper limits of the γ -ray luminosity. If only an upper limit on the radio luminosity has been estimated, the data are reported in red.

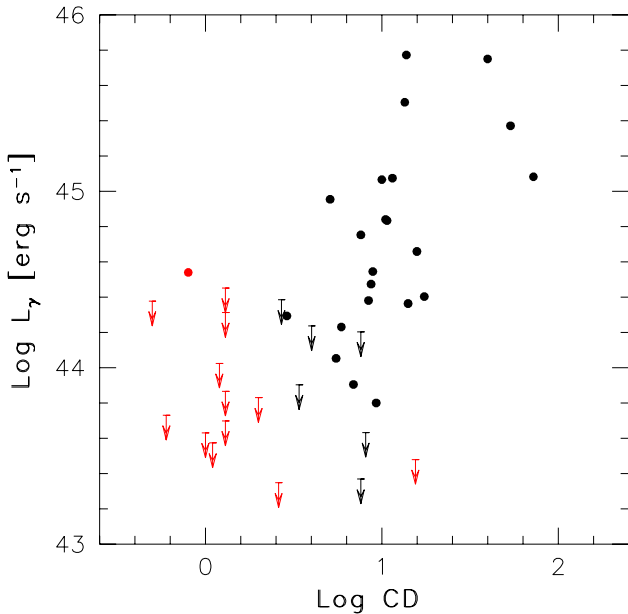


Fig. 12. Core dominance vs. γ -ray luminosity in the 0.1–300 GeV energy range for the sources in our sample. Filled circles indicate LAT-detected sources, while arrows show upper limits of the γ -ray luminosity. If only an upper limit on the CD has been estimated, the data are reported in red.

luminosity-luminosity plot are not yet detected by *Fermi*-LAT, except for J1534+3715.

On the basis of the radio properties (i.e. source compactness, Core Dominance, CD⁶, source morphology and radio spectrum) in Paper I, all the sources have been classified in three groups: Doppler-dominated (DD, 23 cases), lobe-dominated (LD, 11

⁶ CD is defined as ratio between the observed core radio power and the estimated unbeamed total radio power at low frequency.

cases), and undetermined type (U, 8 cases) sources. In DD sources, the luminosity of the core is much larger than the luminosity of the extended component, implying relativistic jets and small viewing angles; LD sources have less prominent or undetected cores, and significant extended emission; U sources are undetected with VLBI but their overall flux density is so low that it does not provide stringent limits on the ratio between nuclear and extended emission. Among the 23 LAT-detected sources, 20 are classified as DD, and 3 as LD (J0847+1133, J1341+3959, and J1534+3715). All three newly detected γ -ray sources are classified as DD. European VLBI Network and VLBA observations at 5 GHz and 8 GHz, respectively, and a CD of 5.1 suggests an intermediate classification of J0847+1133 between LD and DD. Faint radio emission has been detected with VLBA observations of the other two LAT-detected sources classified as LD. On the other hand, three sources classified as DD for their radio properties (J0754+3910, J0903+4055, J1516+2918) are not detected in γ rays by LAT up to now. These three sources have a relatively low CD (7.6–8.0) with respect to the LAT-detected sources classified as DD (5.5–72.4). Considering that CD is a strong indication of Doppler beaming of the emission, this suggests that the DD sources not detected by LAT have a lower Doppler factor with respect to the LAT-detected ones. In Fig. 12, the CD versus γ -ray luminosity of sources in our sample has been shown. The plot confirms that sources with large γ -ray luminosity also have high CD values. In the cases of J0754+3910 and J0903+4055, the upper limits on the γ -ray flux estimated over 8.5 yr of LAT observations are compatible with the sensitivity limit estimated over 10 yr of LAT observations, indicating that, accumulating more data, these sources may be detected by the LAT in the near future.

5. Summary

With the advent of the *Fermi* satellite, our understanding of the radio and γ -ray connection in blazars significantly increased. BL Lacs are found to be the most abundant class of extragalactic objects observed by LAT. However, they are relatively weak radio sources and the parsec-scale structure has not been studied in detail for most of them. We have selected a sample of 42 BL Lacs included in the BZCAT catalogue with $z < 0.2$, located within the sky area covered by SDSS, and with no selection limit on γ -ray flux. Most of the sources (31/42) have a 1.4 GHz flux density that is lower than the sensitivity limit of VIPS (i.e. 85 mJy). These sources have been observed with the VLBA at 8 GHz and 15 GHz, and the results are reported in Liuzzo et al. (2013). In this paper we have investigated the γ -ray properties of the radio fainter BL Lac sources and the connection with the radio properties.

Among the sources in the sample, 23 out of 42 have been detected by our LAT analysis, with an average photon index $\langle \Gamma \rangle = 1.87 \pm 0.06$ and a luminosity varying between 6×10^{43} and 6×10^{45} erg s⁻¹, a range of values typical of γ -ray emitting BL Lacs and within the range of values observed for the other BL Lacs with $z < 0.2$ in the 3FGL. All sources reported in the 3FGL are confirmed by our analysis. In addition we have revealed three new sources with respect to the 3FGL. These three new detections have fluxes below 1.4×10^{-8} ph cm⁻² s⁻¹ and photon index 1.7–1.9.

Based on the $\nu_{\text{peak}}^{\text{syn}}$, 30 sources in our sample are classified as HSP; in particular 19 out of 23 LAT-detected sources are HSP BL Lacs. An anti-correlation between $\nu_{\text{peak}}^{\text{syn}}$ and γ -ray photon index is observed for the LAT-detected BL Lacs, in agreement with the blazar sequence. Among the 23

LAT-detected sources, 19 are included in the 3FHL, for which a small difference between the photon index estimated in the 0.1–300 GeV and 10 GeV–2 TeV energy range has been observed. This suggests that the average γ -ray spectrum of these sources connects rather smoothly from 0.1 GeV to 2 TeV, as expected due to the low EBL attenuation at $z < 0.2$.

A compact radio component in the VLBA images has been detected in 22 out of the 23 LAT-detected sources, and only 6 out of 19 non-LAT-detected sources. LAT-detected BL Lacs are more luminous on parsec scales with respect to non-LAT-detected sources and tend to have larger core dominance according to the Unified models. All sources with $P_{\text{core}, 8\text{GHz}} > 2 \times 10^{24} \text{ W Hz}^{-1}$ have been detected in γ rays by LAT, confirming the strong correlation between radio and γ -ray properties. In the same way, we have identified a possible population of low-luminosity BL Lacs in both the radio and γ rays, lacking a VLBI core, and with a small Doppler factor. This highlights an opportunity for future γ -ray observations to discover low-luminosity BL Lacs with *Fermi*-LAT and the next generation of γ -ray satellites.

Radio and γ -ray emission in blazars are both related to the presence of relativistic particles in jets. Among the 23 LAT-detected sources, 20 are classified as DD, indicating the presence of a relativistic jet in radio images. All these characteristics confirm that LAT-detected BL Lacs are dominated by Doppler boosting effects. However, three LAT-detected sources are classified as LD, with no evidence of relativistic jet with high Doppler factor in radio images and relatively low core dominance, showing non-classical properties for a γ -ray-emitting BL Lac. The properties of these peculiar sources will be investigated in detail by means of multi-frequency observations.

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Accelerator Research Organization (KEK) and Japan Aerospace Exploration Agency (JAXA) in Japan, and the K. A. Wallenberg Foundation, the Swedish Research Council and the Swedish National Space Board in Sweden. Additional support for science analysis during the operations phase is gratefully acknowledged from the Istituto Nazionale di Astrofisica in Italy and the Centre National d’Études Spatiales in France. This work performed in part under DOE Contract DE-AC02-76SF00515.

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