First core properties: from low- to high-mass star formation

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ABSTRACT

Aims. In this study, the main goal is to understand the molecular cloud core collapse through the stages of first and second hydrostatic core formation. We investigate the properties of Larson’s first and second cores following the evolution of the molecular cloud core until the formation of Larson’s cores. We expand these collapse studies for the first time to span a wide range of initial cloud masses from 0.5 to 100 \( M_\odot \).

Methods. Understanding the complexity of the numerous physical processes involved in the very early stages of star formation requires detailed thermonodynamical modelling in terms of radiation transport and phase transitions. For this we used a realistic gas equation of state via a density- and temperature-dependent adiabatic index and mean molecular weight to model the phase transitions. We used a grey treatment of radiative transfer coupled with hydrodynamics to simulate Larson’s collapse in spherical symmetry.

Results. We reveal a dependence of a variety of first core properties on the initial cloud mass. The first core radius and mass increase from the low-mass to intermediate-mass regime and decrease from the intermediate-mass to high-mass regime. The lifetime of first cores strongly decreases towards the intermediate- and high-mass regimes.

Conclusions. Our studies show the presence of a transition region in the intermediate-mass regime. Low-mass protostars tend to evolve through two distinct stages of formation that are related to the first and second hydrostatic cores. In contrast, in the high-mass star formation regime, collapsing cloud cores rapidly evolve through the first collapse phase and essentially immediately form Larson’s second cores.

Key words. stars: formation – methods: numerical – hydrodynamics – radiative transfer – gravitation – equation of state

1. Introduction

Stars are formed by the gravitational collapse of dense, gaseous, and dusty cores within magnetized molecular clouds. Details of the earliest epochs of star formation and protostellar evolution however remain far from fully understood because of the complexity of the physical processes involved such as hydrodynamics, radiative transfer, and magnetic fields. Understanding how stars form has thus been one of the most fundamental questions raised for several decades (see detailed reviews by Larson 2003; McKee & Ostriker 2007; Inutsuka 2012). Owing to the optically thick regime, it is still very challenging to obtain reliable observational constraints during the earliest phases of star formation (e.g. Nielbock et al. 2012; Launhardt et al. 2013; Dunham et al. 2014). Numerical studies by Larson (1969) were among the first to indicate the presence of two quasi-hydrostatic cores that are formed during a non-homologous collapse of the molecular cloud. They investigated the faster collapse of the denser inner region in comparison to the less dense outer region with one-dimensional (1D) hydrodynamic simulations using the diffusion approximation for radiative transfer. Since then there have been detailed numerical investigations using both grid-based (Bodenheimer & Sweigart 1968; Winkler & Newman 1980a,b; Stahler et al. 1980a,b, 1981; Masunaga et al. 1998; Masunaga & Inutsuka 2000; Tomida et al. 2010b; Commerçon et al. 2011a; Vaytet et al. 2012, 2013; Tomida et al. 2013; Vaytet & Haugbolle 2017, and references therein) and smoothed particle hydrodynamics (SPH) simulations (Whitehouse & Bate 2006; Stamatellos et al. 2007; Bate et al. 2014) to better understand the isolated collapse scenario. The early phases of low- and intermediate-mass star formation can briefly be summarized as follows.

Initially, the optically thin cloud collapses isothermally under its own gravity due to the efficient thermal emission from dust grains during this phase. The collapse may be initiated either by ambipolar diffusion of magnetic fields that once supported the cloud against gravitational collapse (e.g. Shu et al. 1987) or by dissipation of turbulence, which reduces the effective speed of sound in cloud cores (e.g. Nakano 1998). This collapse can start from a contracting, marginally stable Bonnor–Ebert sphere or the collapse can be triggered by an external shock wave running over the previously stable cloud (Masunaga & Inutsuka 2000).

As the density increases, the optical depth becomes greater than unity and radiation cooling becomes inefficient. As the cloud compresses further, the temperature in this dense central region gradually increases. This almost halts the collapse and leads to the formation of the first hydrostatic core, which subsequently contracts adiabatically with an adiabatic index \( \gamma = 5/3 \). With a rise in temperature, the rotational degrees of freedom of the diatomic gas get excited and the adiabatic index changes...
to \( \approx 7.5 \). Once the temperature inside the first core reaches \( \sim 2000 \, \text{K} \), \( \text{H}_2 \) molecules begin to dissociate. Gravity wins over pressure since \( \text{H}_2 \) dissociation is a strongly endothermic process. The core thus becomes unstable which leads to the second collapse phase. Once most of the \( \text{H}_2 \) has been dissociated, it is followed by the formation of the second hydrostatic core. The second core forms almost instantaneously and hence the second collapse phase lasts only for a few years, in comparison to the first collapse phase, which lasts for about \( 10^5 \, \text{yr} \) for an initially \( 1 \, \text{M}_\odot \) cloud. The collapse is then stopped by an increase in thermal pressure. The surrounding envelope continues to fall onto the central core as the core grows in mass through the main accretion phase with a further increase in temperature. A star is born when the core reaches ignition temperatures for nuclear reactions.

In the studies presented in this paper, we simulate the gravitational collapse for isolated gas spheres with a uniform temperature and initial Bonnor–Ebert density profile. Thermodynamical modelling in terms of radiation transport and phase transitions is crucial to better understand the complex physical mechanisms involved. Hence, we use grey flux-limited diffusion (FLD) radiative transfer (Levermore & Pomraning 1981) coupled with hydrodynamics to simulate Larson’s collapse. Using 1D spherically symmetric collapse simulations, we investigate properties of Larson’s first and second core. One-dimensional studies have proven to be of importance in understanding the role of different physical processes involved while 3D studies can still be computationally very expensive. In this work, we focus on properties of the hydrostatic cores governed by gravity and thermal pressure and not of the environment. Since the thermal pressure is isotropic, a 1D approach is a good approximation for these objects, even though the collapsing environment is not described accurately.

Different chemical species affect gas hydrodynamics via heat capacity, line cooling, and chemical energy and radiation via gas and dust opacities. In order to take into account effects such as dissociation, ionization, rotational, and vibrational degrees of freedom for the molecules in our studies, we use a realistic gas equation of state (EOS) with a density- and temperature-dependent adiabatic index and mean molecular weight to model phase transitions. Using a non-constant adiabatic index is particularly important since it has a strong influence on the thermal evolution of the gas and in general also on the stability of the gas against gravitational collapse (Stamatellos & Whitworth 2009). The specific heat and mean molecular weight are computed as a function of temperature by solving partition functions for rotational, vibrational, and translational energy levels of \( \text{H}_2 \) instead of using a constant value.

The main goal of this paper is to understand the entire collapse phase through the stages of first and second core formation by incorporating a realistic gas EOS and appropriate opacity tables for a wide range of initial cloud masses from 0.5 to 100.0 \( \text{M}_\odot \). In doing so, we quantify the dependence of the first core properties on the initial cloud mass.

The paper is organized as follows. The microphysics used in our studies is detailed in Sect. 2. We describe our numerical scheme and initial setup in Sect. 3. The evolution of the cloud through various stages until the formation of the second hydrostatic core is presented in Sect. 4. We first provide a detailed description of the collapse of an initial 1.0 \( \text{M}_\odot \) cloud in Sect. 4.1 and then extend this explanation to all other cases for different initial cloud masses from 0.5 up to 100 \( \text{M}_\odot \) in Sect. 4.2. We further discuss the dependence of the first core properties on the initial cloud mass in Sect. 4.3. In Sect. 4.4 we extend our parameter space to study the influence of initial cloud properties on the first core properties. Our results are in good agreement with previous work and comparisons are provided in Sect. 4.5. We note the limitations of our method and discuss the outlook in Sect. 4.6. Section 5 summarizes the results presented herein.

### 2. Equations of radiation hydrodynamics

Gas thermodynamics is considered under the approximation of local thermodynamic equilibrium (LTE) and a two-temperature approach (2T), for the gas and radiation. The basic hydrodynamics equations that account for the conservation of mass, momentum, and energy, i.e. the continuity, Euler’s, and energy equation, respectively, are given as

\[
\partial_t \rho + \nabla \cdot (\rho \mathbf{u}) = 0, \quad (1)
\]

\[
\partial_t (\rho \mathbf{u}) + \nabla \cdot (\rho \mathbf{u} \otimes \mathbf{u} + P) = \rho \mathbf{a}, \quad (2)
\]

\[
\partial_t E + \nabla \cdot ((E + P) \mathbf{u}) = \rho u \cdot \mathbf{a}, \quad (3)
\]

where \( \rho \) is the density, \( \mathbf{u} \) is the dynamical velocity, \( P \) is the thermal pressure, and \( \mathbf{a} \) denotes the acceleration source term due to self-gravity given by

\[
\mathbf{a} = -\nabla \Phi_{\text{sg}}, \quad (4)
\]

where \( \Phi_{\text{sg}} \) is the gravitational potential determined using Poisson’s equation, expressed as

\[
\nabla^2 \Phi_{\text{sg}} = 4\pi G\rho. \quad (5)
\]

The total energy \( E = E_{\text{int}} + E_{\text{kin}} \) is the sum of internal and kinetic energy. The kinetic energy density \( E_{\text{kin}} = \frac{1}{2} \rho \mathbf{u}^2 \), whereas the internal energy density is calculated by taking into account the contributions from various hydrogen and helium species. This is described in Sect. 2.1.

The time-dependent radiation transport equation in case of locally isotropic radiation when neglecting small contributions due to scattering can be written as

\[
\partial_t E_{\text{rad}} + \nabla \cdot F_{\text{rad}} = c \chi_{\text{abs}} (B_{\text{rad}} - E_{\text{rad}}), \quad (6)
\]

where \( E_{\text{rad}} \) is the radiation energy density, \( F_{\text{rad}} \) is the radiation energy flux, \( c \) is the speed of light, \( \chi_{\text{abs}} \) is the coefficient of absorption, and \( B_{\text{rad}} \) is the integral of the black-body Planck spectrum. The flux of radiation energy density \( F_{\text{rad}} \) in the FLD approximation is determined as

\[
F_{\text{rad}} = -D_{\text{rad}} \nabla E_{\text{rad}} = -\frac{\lambda c}{\kappa_R \rho} \nabla E_{\text{rad}}, \quad (7)
\]

where \( \kappa_R \) is the Rosseland mean opacity and the flux limiter \( \lambda \) is chosen following Levermore & Pomraning (1981). The flux limiter recovers the limiting cases of diffusion and free streaming, respectively.

Using Eq. (7) in the conservation, Eq. (6) gives the time evolution of radiation energy density as

\[
\partial_t E_{\text{rad}} - \nabla \cdot (D_{\text{rad}} \nabla E_{\text{rad}}) = c \chi_{\text{abs}} (B_{\text{rad}} - E_{\text{rad}}), \quad (8)
\]

The two unknowns in Eq. (8), namely, the radiation energy density \( E_{\text{rad}} \) and the local temperature of the medium \( B_{\text{rad}} = a T^4 \), where \( a \) is the radiation constant are coupled to each other via
heating and cooling processes. The time evolution of the local internal energy is given by

$$\partial_t E_{\text{int}} = -c \chi_{\text{abs}} (B_{\text{rad}} - E_{\text{rad}}). \quad (9)$$

For the 2T model, the coupled Eqs. (8) and (9) can be reduced to a single equation using a linearization approach in which the radiation and medium temperatures evolve as two different quantities (Commerçon et al. 2011b). Additionally, the specific heat capacity is taken to be constant over the course of a single main iteration.

A detailed description of the numerical code in use can be found in Mignone et al. (2007, 2012) for the hydrodynamics, Vaidya et al. (2015) and Marleau et al. (in prep.) for the gas EOS (see also the following section), Kuiper et al. (2010a, 2018) for the radiation transport, and Kuiper et al. (2010b, 2011) for the self-gravity.

2.1. Gas equation of state

We use the gas EOS of D’Angelo & Bodenheimer (2013) to account for effects such as ionization of atomic hydrogen and helium, dissociation of molecular hydrogen (H$_2$), and molecular vibrations and rotations. This is a realistic approach for modeling the second collapse phase where H$_2$ begins to dissociate depending on the pressure, temperature, and density. This EOS has been implemented in the PLUTO code by Vaidya et al. (2015) and we now updated the radiation transport module to make use of this (see details in Marleau et al., in prep.).

The adiabatic index or ratio of specific heats γ, which takes into account the translational, rotational, and vibrational degrees of freedom, is defined as

$$\gamma = \frac{C_p}{C_V}. \quad (10)$$

Figure 1 shows the mean molecular weight µ and γ as a function of temperature and also indicates the dependence on gas density. The mean molecular weight µ has an upper limit of ~2.3 and a lower limit of ~0.6. The first transition (i.e. the plateau region) indicates the dissociation of H$_2$, whereas the second transition shows the ionization phase. In the plot showing γ as a function of temperature, the gas behaves as a monatomic ideal gas with γ = 5/3 at lower temperatures. The transition from a monatomic gas γ = 5/3 (where rotational degrees of freedom of H$_2$ are frozen) to a diatomic gas γ = 7/5 and further to the dissociation phase where γ > 1.1 is also seen as dips in γ. Following the curve to higher temperatures, the other dips occur at the ionization of hydrogen and at the first and second ionization of helium. Increasing density raises the temperature at which these processes occur. Since the range in log $T$ over which they occur widens and the γ dips become shallower, the dips gradually blend. This is clear when comparing the curves at $\rho = 10^{-19}$ g cm$^{-3}$ at and $\rho = 10^{-3}$ g cm$^{-3}$.

In our studies, we assume the ortho:para ratio of molecular hydrogen to be in thermal equilibrium at all temperatures. Vaytet et al. (2014) showed that the ortho:para ratio influences the thermal evolution of the first core but has negligible effects on the core properties. An appropriate ortho:para ratio as initial conditions for star formation still remains unclear.

Considering LTE, the ionization–recombination and dissociation processes for hydrogen are respectively given by

$$H + e^- \leftrightarrow H^+ + 2e^-, \quad \text{H}_2 \leftrightarrow H + H. \quad (11)$$

The degree of ionization of atomic hydrogen $x$, the degree of dissociation of molecular hydrogen $y$, and the degrees of single $z_1$ and double $z_2$ ionization of helium are defined from D’Angelo & Bodenheimer (2013) as

$$x = \frac{\rho_{H^+}}{\rho_{H^+} + \rho_{H}}, \quad (12)$$

$$y = \frac{\rho_H}{\rho_{H^+} + \rho_{H_2}}, \quad (13)$$

$$z_1 = \frac{\rho_{He^+}}{\rho_{He^+} + \rho_{He}}, \quad (14)$$

$$z_2 = \frac{\rho_{He^{2+}}}{\rho_{He^{2+}} + \rho_{He^+}}. \quad (15)$$

Following the Boltzmann law of the energy distribution, the ionization and dissociation degrees using Saha equations are given as (see e.g. Black & Bodenheimer 1975)

$$x^2 \frac{1}{1-x} = \frac{m_H}{X_H} \left( \frac{m_e k_B T}{2 \pi \hbar^2} \right)^{3/2} e^{-13.60 \text{eV}/(k_B T)}, \quad (16)$$
where $m_e$ is the electron mass, $m_H$ is the hydrogen mass, $k_B$ is the Boltzmann constant, $\hbar$ is the Planck’s constant divided by $2\pi$, and $\rho = m_H n_H$ is the total gas density. The hydrogen and helium mass fractions are taken as $X = 0.711$ and $Y = 0.289$, respectively.

For a gas mixture mainly consisting of hydrogen (atoms, molecules, and ions), helium, and a negligible fraction of metals, the mean molecular weight $\mu$ is given as (e.g. Black & Bodenheimer 1975)

$$\frac{\mu}{4} = \frac{[2X(1+y+2xy) + Y(1 + z_1 + z_1 z_2)]^{-1}}{1},$$

and the gas internal energy density $(\epsilon)$, given by

$$(\epsilon) = (\epsilon_{H_2} + \epsilon_{H + e} + \epsilon_{H + H} + \epsilon_{H + e^+} + \epsilon_{He^+}),$$

expressed as a function of temperature and density, given as

$$(\rho e)_{gas} = \frac{\rho k_B T}{m_p}.$$ (21)

The quantity $m_p$ is the atomic mass unit and contributions from various species in the parenthesis are dimensionless and can be obtained using an appropriate partition function $\mathcal{Z}$ by taking into account the translational, rotational, and vibrational degrees of freedom as detailed in D’Angelo & Bodenheimer (2013).

The stability condition needed for numerical calculations requires an estimate of the sound speed $c_s$, which relates pressure and density and is defined as

$$c_s^2 = \frac{\Gamma_1 P}{\rho}.$$ (22)

The parameter $\Gamma_1$ is the first adiabatic index, which has a functional dependence on temperature and density, given as

$$\Gamma_1 = \frac{1}{C_v(T)} \left( \frac{P}{\rho T} \right) \frac{X_H^2 + X_P}{X_T^2 + X_P},$$ (23)

where $C_v(T)$ is obtained by taking the derivative of the specific gas internal energy $e(T)$ with respect to temperature at a constant volume and the temperature $X_T$ and density $X_P$ exponents (see D’Angelo & Bodenheimer 2013) are defined by

$$X_T = \left( \frac{\partial \ln P}{\partial \ln T} \right)_\rho = 1 - \frac{\partial \ln \mu}{\partial \ln T},$$ (24)

$$X_P = \left( \frac{\partial \ln P}{\partial \ln \rho} \right)_T = 1 - \frac{\partial \ln \mu}{\partial \ln \rho}.$$ (25)

We note that for an ideal gas where phase transitions are ignored, i.e. with constant $\mu$ and $\gamma$, $\Gamma_1$ is equal to the adiabatic index $\gamma$.

With all of the above considerations, the thermal EOS (relating pressure, temperature, and volume) and the caloric EOS (relating internal energy, volume, and temperature) can be expressed as

$$P = \frac{\rho k_B T}{m_p \mu(X)},$$ (26)

$$e = \epsilon(T, X),$$

where the mean molecular weight $\mu(X)$ depends on the gas composition. The chemical fractions are not solved independently and can be expressed as $X = X(T, \rho)$ under equilibrium assumptions. Thus, the thermal and caloric EOS can also be expressed as a function of temperature and density, $P = P(\rho, T)$ and $e = \epsilon(T, \rho)$, respectively. Owing to the explicit temperature dependence, the conversion between pressure and internal energy density and vice versa is preceded by computing temperatures using the thermal EOS and pre-computed lookup tables of pressure and internal energy density. Further details on the implementation of lookup tables can be found in Vaidya et al. (2015).

### 2.2. Opacities

We make use of tabulated dust opacities from Ossenkopf & Henning (1994) and tabulated gas opacities from Malygin et al. (2014). At lower temperatures the contribution from dust dominates, whereas at higher temperatures this is negligible since the dust is evaporated.

Code-wise, we updated the evaporation and sublimation module to account for the time-dependent evolution of the dust. The dust is treated as being perfectly coupled to the gas, i.e. the dust is moving with the gas flow, but the dust content is allowed to change in time owing to evaporation and sublimation of dust grains. Hence, we store, in addition to the gas mass density, the local dust-to-gas mass ratio $R_t = M_{dust}/M_{gas}$.

The evaporation temperature $T_{evap}$ is computed based on Pollack et al. (1994) utilizing the power-law formula by Isella & Natta (2005, their Eq. (16)):

$$T_{evap} = \beta_1 \times \left( \frac{\rho_{gas}}{1 \text{ g cm}^{-2}} \right)^{\beta_2},$$ (27)

where $\beta_1 = 2000 \text{ K}$ and $\beta_2 = 1.95 \times 10^{-2}$. In the sublimation regime $T_{dust} < T_{evap}$, the temporal evolution of the dust-to-gas mass ratio $R(t)$ is described by

$$R(t + \Delta t) = R(t) + dR \times R_{max} \times \left[ 1 - \exp \left( -\frac{\Delta t}{\tau_{subl} \times dT \times dR} \right) \right],$$ (28)

where $dT = |T_{evap} - T_{dust}|/T_{evap}$ and $dR = (R_{max} - R(t))/R_{max}$. In the evaporation regime $T_{dust} > T_{evap}$, the temporal evolution of the dust-to-gas mass ratio is described by

$$R(t + \Delta t) = R(t) \times \exp \left( -\frac{\Delta t}{\tau_{evap} \times dT \times \frac{1}{dR + \omega}} \right).$$ (29)

The value $\omega$ serves as a lower limit to the $dR$ term, which prevents the $dR^{-1}$ term from diverging.

In a nutshell, evaporation and sublimation become more efficient for higher temperature differences between dust and evaporation temperature. Furthermore, the evaporation efficiency decreases towards lower dust-to-gas mass ratios, and the sublimation efficiency decreases towards the maximum dust-to-gas mass ratio allowed. For all simulations performed, we used $R_{max} = 0.01$, $\tau_{subl} = 10 \text{ yr}$, $\tau_{evap} = 100 \text{ yr}$, and $\omega = 0.01$. 

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3. Numerics and initial setup

In this study, 1D spherically symmetric collapse simulations are performed using the (magnetohydrodynamic code PLUTO (Mignone et al. 2007) combined with the grey FLD radiation transport module MAKEMAKE. The theory and numerics of the radiation transfer scheme are described and tested in Kuiper et al. (2010a, 2018).

Vaytet et al. (2012, 2013) have indicated slight differences in the core properties between grey and multi-group methods. However, they argued that the grey method proves sufficient for the 1D case and the multi-group radiative transfer may be more important in the later evolutionary stages of the protostar. The hydrodynamic equations are solved using a shock capturing Riemann solver within a conservative finite volume scheme, whereas the FLD equation is solved in an implicit way using the generalized minimal residual solver (GMRES). We used the Harten-Lax-VanLeer approximate Riemann solver that restores with the middle contact discontinuity (hllc), a monotonized central difference (MC) flux limiter using piecewise linear interpolation and a Runge–Kutta 2 (RK2) time integration.

As an initial density distribution, we used a stable Bonnor–Ebert (Bonnor 1956; Ebert 1955) sphere like density profile. Comparisons to an initially uniform density cloud are described in Appendix A.

Given an initial cloud mass $M_{0}$ and outer radius $R_{\text{out}}$, the initial sound speed $c_{\text{s}0}$ is computed as

$$c_{\text{s}0}^2 = \frac{GM_{0}}{\ln(14.1) R_{\text{out}}},$$  \hspace{1cm} (30)

where $G$ is the gravitational constant. The initial cloud masses range from 0.5 to 100.0 $M_{\odot}$.

The temperature $T_{\text{BE}}$ for the stable sphere is calculated as

$$T_{\text{BE}} = \frac{\mu c_{\text{s}0}^2}{\gamma R},$$  \hspace{1cm} (31)

where $\mu = 2.353$, $\gamma = 5/3$, and $R$ is the universal gas constant. The initial outer $\rho_{\text{out}}$ and central $\rho_{c}$ densities are determined by

$$\rho_{\text{out}} = \left( \frac{1.18 c_{\text{s}0}^3}{M_{0} G^{3/2}} \right)^{2},$$ \hspace{1cm} (32)

$$\rho_{c} = 14.1 \rho_{\text{out}},$$

The density contrast between the centre and edge of the sphere corresponds to a dimensionless radius of $\xi = 6.45$, where $\xi$ is defined as

$$\xi = \sqrt{\frac{4\pi G\rho_{\text{out}}}{c_{\text{s}0}^2} R_{\text{cloud}}},$$  \hspace{1cm} (33)

where $R_{\text{cloud}}$ is the cloud radius. The integrated mass of the cloud is the same as that of a critical Bonnor–Ebert sphere. The thermal pressure is computed using Eq. (26) for a fixed lower temperature $T_{0}$ in comparison to the stable Bonnor–Ebert sphere setup, which causes gravity to dominate and initiates the collapse. This temperature $T_{0}$ varies from 5 to 100 K. The radiation temperature is initially in equilibrium with the gas temperature and the dust and gas temperatures are closely coupled.

For the first set of numerical calculations (see Table 1), the inner radius is fixed to $10^{-4}$ au and the outer radius is fixed to 3000 au. This setup implies that the central density of the different Bonnor–Ebert spheres scales as a function of initial cloud mass.

The computational grid for these simulations is comprised of 4416 cells. We used 320 uniformly spaced cells from $10^{-4}$ to $10^{-2}$ au and 4096 logarithmically spaced cells from $10^{-2}$ to 3000 au. We made sure that the last uniform cell and the first logarithmic cell are identical in size. The integration time step in the inner dense core regions becomes very small if a logarithmic binning is used throughout, which would become computationally very expensive. Therefore, we chose a linear grid in the very inner part of the computational domain. We performed convergence tests using different resolutions (see Appendix B.1) and different inner radii $R_{\text{in}}$ (see Appendix B.2) in order to test our approach. These tests show that the applied resolution is fully sufficient and hence there is no need to use higher resolution in the inner parts.

In addition, in order to investigate the dependence on the initial cloud properties, we explored a range of initial conditions by performing three different set of simulations using a different constant stability parameter $M_{\text{BE}}/M_{0}$ for the low-mass ($0.5–10 M_{\odot}$), intermediate-mass ($8–20 M_{\odot}$) and high-mass regimes ($30–100 M_{\odot}$), respectively. For these runs, we fixed the outer radius to 3000 au but varied the initial cloud temperature from 5 to 100 K. The initial cloud properties for the selected parameter space are listed in Table 3 and the implications on the first core properties are described in Sect. 4.4. We also perform a set of simulations detailed in Table C.1 with an outer radius of 5000 au and a constant initial temperature of 10 K for initial cloud masses ranging from 1 to 100 $M_{\odot}$.

At the inner edge $R_{\text{in}}$ we used a reflective boundary condition for the hydrodynamics as well as for radiation transport (no radiative flux should cross the inner boundary interface). At the outer edge $R_{\text{out}}$, we used a Dirichlet boundary condition on the radiation temperature with a constant boundary value of $T_{0}$ and an outflow-no-inflow condition for the hydrodynamics that includes a zero-gradient (i.e. no-force) boundary condition for

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</table>

Notes. Listed above are the cloud properties for runs with different initial cloud mass $M_{0}$ ($M_{\odot}$), outer radius $R_{\text{out}}$ (au), temperature $T_{0}$ (K), stability parameter $M_{\text{BE}}/M_{0}$, and central density $\rho_{c}$ (g cm$^{-3}$).
the thermal pressure given as
\[
\frac{dP}{dr} = 0.
\]

(34)

4. Results: from clouds to cores

4.1. Fiducial 1 \(M_\odot\) case

In this section, we present a general overview of the collapse evolution and its effects on various properties for an initial 1 \(M_\odot\) cloud. Figure 2 shows the radial profiles of the density, pressure, gas temperature, velocity, enclosed mass, optical depth, Mach number, mean molecular weight \(\mu\), and the thermal structure at a time step right after second core formation. We consider an initial Bonnor–Ebert sphere like density profile (as described in Sect. 3), where the initial central density is \(\rho_c \approx 10^{-17} \text{ g cm}^{-3}\). The evolution of the cloud through its first and second collapse phases can be understood as follows:

- Initially the optically thin cloud collapses isothermally with \(\gamma_{\text{actual}} \approx 1\) under its own gravity, where \(\gamma_{\text{actual}}\) is the change in the slope of the temperature evolution with density (see Fig. 3).
- During the first collapse phase, as the density and pressure increases, the optical depth becomes greater than unity (Masunaga & Inutsuka 1999) and the cloud compresses adiabatically. The cloud starts absorbing the thermal radiation and heats up leading to an adiabatic collapse phase.
– Once most of the H\textsubscript{2}– As the molecular hydrogen and neutral helium concentration changes, the fraction of atomic hydrogen increases during the dissociation phase, μ gradually decreases in the inner regions, as seen in Fig. 2h.
– Once most of the H\textsubscript{2} has been dissociated, it is followed by the formation of the second hydrostatic core with initial values of $R_{sc} \approx 1.8 \times 10^{-2}$ au $\approx 3.9$ $R_\odot$, $M_{sc} \approx 4.6 \times 10^{-3}$ $M_\odot$.
– The second shock at the border of the second core is seen in the velocity profile (Fig. 2d). Comparing this to the temperature profile, the second shock is seen to be subcritical, i.e. the pre-shock temperature being higher than the post-shock temperature, suggesting that the accretion energy is transferred onto the second core and not radiated away.
– The central density rapidly rises up to $\rho_c \approx 10^{-1}$ g cm\textsuperscript{-3} at the end of the second collapse phase, which lasts only for a few years since the second hydrostatic core forms almost instantaneously.
– At later times when $\rho_c \approx 10^{-1}$ g cm\textsuperscript{-3}, the outer layers tend to have higher temperatures due to the effects of shock heating and absorption of radiation from the hot central region. Differences in the thermal evolution of the central region (black line) and the thermal structure at a time when $\rho_c \approx 10^{-1}$ g cm\textsuperscript{-3} (bluish purple line) can be seen in Fig. 2i.
– Finally (not simulated here), once the temperature inside the second core reaches ignition temperatures ($\geq 10^6$ K) for nuclear reactions, it eventually leads to the birth of a star.

Figure 3 summarizes the different evolutionary stages that the molecular cloud undergoes to form the first and second Larson’s cores and indicates the phase transition from monatomic to diatomic gas, i.e. the change in the adiabatic index $\gamma_{actual}$.

4.2. Effect of different initial cloud masses

In this section, we discuss the core collapse scenario for different initial cloud masses. We span a wide range of initial cloud masses from 0.5 to 100 $M_\odot$. The clouds with different initial masses $M_0$ and central densities $\rho_c$ at the same initial temperature of 10 K and an outer radius of 3000 au follow a similar evolution as seen in Fig. 4. Most significant differences are seen outwards from the first shock as a horizontal spread.

The thermal structure for cases with different initial cloud masses (Fig. 4f) shows that the clouds begin with the same isothermal phase but eventually heat up at different densities. This difference in thermal evolution can have a significant effect on the properties of the first and second cores since for the intermediate- and high-mass clouds ($M_0 \geq 8$ $M_\odot$) the dissociation temperature is reached earlier when the cloud is at a comparatively lower density, which in turn affects the lifetime of the first and second cores. The change in optical depth shown
Fig. 4. Shown above are the radial profiles (across and down) of density (panel a), pressure (panel b), gas temperature (panel c), velocity (panel d), and enclosed mass (panel e) as well as the thermal structure (panel f), Mach number (panel g), ratio of gas to ram pressure (panel h), internal energy density as a function of temperature (panel i), optical depth (panel j), Rosseland mean opacity (panel k), and dissociation fraction at the snapshot after second core formation (panel l). Different colours indicate clouds with different initial masses as seen in the colour bar. The grey lines in the thermal structure plot show the 50% dissociation and ionization curves according to Eqs. (16) and (17).
in Fig. 4j as the cloud evolves is mainly governed by the balance between radiative cooling and compressional heating. The sharp
in Fig. 4j as the cloud evolves is mainly governed by the balance
mass up to around 8–10
profile, is seen to increase with an increase in the initial cloud
For the initial clouds of mass 40, 60, 80, and 100
that of the first core lifetime.
the collapse simulations with different initial cloud masses. In our studies, since we span a wide range from 0.5 to 100
in the radial density profile).
For the initial clouds of mass 40, 60, 80, and 100
the second core formation. The vertical lines span the minimum
to maximum first core radius as the core evolves. The transition
As already noted, the first core radius increases with an
in the high-mass regime, first cores do not exist.
In summary, in the high-mass regime, first cores do not exist.
For comparison with the low- and intermediate-mass regimes, the shock-like velocity structure is still referred to as an
the first core radius with the first core forming
The evolution of the first core radius from the onset of the
Figure 8 shows the first core lifetime as a function of initial
in the low-mass range (M⊙ ≤ 8 M⊙), the cloud is seen to undergo a comparatively slower collapse hence initiating the first core formation after ≈5000–18 000 yr. On the other hand, in the intermediate- and high-mass regimes, the collapse is seen to be much faster with the first core forming after a few thousand years (≤5000 yr) followed by an instantaneous second collapse phase that prevents the first core from growing.
Figure 8 shows the first core lifetime as a function of initial cloud mass. The first core lifetime is defined as the time between
Table 2. Properties of the first and second cores estimated at the snapshot after second core formation for different initial cloud masses M⊙ with a fixed outer radius R⊙ = 3000 au and initial temperature T⊙ = 10 K.

<table>
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<tr>
<th>M⊙ (M⊙)</th>
<th>Rfc (au)</th>
<th>Mfc (M⊙)</th>
<th>Tfc (K)</th>
<th>Mfc (M⊙ yr⁻¹)</th>
<th>Rsc (au)</th>
<th>Msc (M⊙)</th>
<th>Tsc (K)</th>
<th>Msc (M⊙ yr⁻¹)</th>
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</tbody>
</table>

Notes. The properties listed are the first core radius Rfc, mass Mfc, temperature Tfc, accretion rate Mfc, and second core radius Rsc, mass Msc, temperature Tsc, accretion rate Msc.
As seen in all the previous studies, we also note that in the low-mass regime ($\leq 8 M_\odot$) the first core lifetime scales as $M^{-0.5}$ as seen in Fig. 8.

In the intermediate- and high-mass regimes due to the vanishing thermal pressure support, this dependence changes to $M^{-2.5}$ (see Fig. 8), which can be analytically derived as follows.

The accretion energy $\dot{E}$ is given as

$$\dot{E} = \frac{E_{fc}}{\tau_{fc}} \propto \frac{GM_{fc}}{R_{fc}} M_{fc}, \quad (35)$$

where $M_{fc}$ is the mass enclosed within the first core, $R_{fc}$ is the first core radius, $\tau_{fc}$ is the first core lifetime, and $M_{fc}$ is the accretion rate. The internal energy profiles seen in Fig. 4i look strikingly similar at the onset of the second collapse phase (i.e. at $T \approx 2000$ K) for all the different initial cloud masses. This indicates that indeed the internal energy of the first core $E_{fc}$, at the onset of the second collapse phase, is independent of the initial cloud mass.

Now, we consider the ratio $M_{fc}/R_{fc}$ and multiply and divide by the velocity $u_{fc}$ as follows:

$$\frac{M_{fc}}{R_{fc}} = \frac{4\pi}{3} \rho_{fc} R_{fc}^2 = \frac{4\pi}{3} \rho_{fc} R_{fc}^2 u_{fc} = \frac{M_{fc}}{3 u_{fc}}. \quad (36)$$

Inserting this into the expression for the accretion energy $\dot{E}$ yields

$$\dot{E} \propto \frac{GM_{fc}}{R_{fc}} M_{fc} \propto \frac{GM_{fc}^2}{3 u_{fc}}. \quad (37)$$
In the intermediate- and high-mass regimes, we assume that the whole cloud to be in free fall and hence we can relate the local properties to the large scale properties. The accretion rate $M_{\text{fc}}$ is then defined as

$$M_{\text{fc}} = \frac{M_0}{t_{\text{ff}}}.$$  \hfill (38)

where $t_{\text{ff}}$ is the free fall time. We then assume that the accretion is constant in space (and time), which is valid only for a $\rho \propto R^{-2}$ profile, seen in the outer parts of a Bonnor–Ebert sphere like density profile. In this case, the mean velocity $u_{\text{fc}}$ can be estimated as

$$u_{\text{fc}} = \frac{R_{\text{cloud}}}{t_{\text{ff}}}.$$  \hfill (39)

Now, the free-fall time of a collapsing cloud is given by

$$t_{\text{ff}} = \sqrt{\frac{3\pi}{32G\rho_c}} \propto \sqrt{\frac{R_{\text{cloud}}^3}{M_0}}.$$  \hfill (40)

Using these relations in the expression for accretion energy $E$, Eq. (37) yields

$$E \propto \frac{M_{\text{fc}}^2}{u_{\text{fc}}} \propto \left(\frac{M_0}{R_{\text{cloud}}}ight)^{5/2}.$$  \hfill (41)

Furthermore, from Eq. (35)

$$\tau_{\text{fc}} \propto \frac{1}{E} \propto \left(\frac{R_{\text{cloud}}}{M_0}\right)^{5/2}.$$  \hfill (42)

Thus, in the intermediate- and high-mass regimes, the first core lifetime scales as $M^{-2.5}$ as seen in Fig. 8. The dependence on the cloud radius is seen in Fig. C.2 and discussed in Appendix C.

4.4. Dependence on initial conditions

In order to assess the robustness of the transition region seen in properties of the first core, we performed three additional set of simulations using a different constant stability parameter $M_{\text{BE}}/M_0$ for the low-mass (0.5–10 $M_\odot$), intermediate-mass (8–20 $M_\odot$), and high-mass regimes (30–100 $M_\odot$), respectively, with some overlap between the low and intermediate masses. This implies a change in the initial temperature for the different cases, which now varies from 5 to 100 K. We used three different stability parameters to avoid extremely high initial cloud temperatures in the intermediate- and high-mass regimes. The outer radius for the various simulations is fixed to 3000 au. The different runs with constant stability parameters are listed in Table 3.

We find a transition region in the intermediate-mass regime similar to that described in Sect. 4.3. The mean first core radius increases with an increase in the initial cloud mass until around 5–8 $M_\odot$ and then decreases towards the intermediate- and high-mass regimes. We compare this to the previously described runs with a fixed initial cloud temperature of 10 K in Fig. 9.

Figure 10 shows the dependence of the first core lifetime on the initial cloud mass. It is very similar to that previously seen in Fig. 8, thereby confirming that the first cores are non-existent in the high-mass regime. These results also indicate that the first core properties do not have a very strong dependence on the initial cloud properties.

We also investigated the dependence of the first core properties on the outer cloud radius by performing a set of simulations for the various cases from 1–100 $M_\odot$ using an outer radius of 5000 au. The initial temperature for these runs was kept constant at 10 K. We see a similar transition region in the intermediate-mass regime. The initial cloud properties and first core properties for these runs are described in Appendix C.

4.5. Comparison to previous results

In this paper, we expand the collapse simulations for the first time, to cover a wide range of initial cloud masses from 0.5
Mean first core radius $[\text{au}]$

First core lifetime $[\text{years}]$

gradually contracts back to $\sim 5 \text{ au}$ and stays roughly constant for a few hundred years roughly $2 \text{ au}$ at the time of formation, which then expands to $\sim 8 \text{ au}$.

Both the simulations use an initial Bonnor–Ebert density profile with an outer boundary $R_{\text{out}} \approx 3000 \text{ au}$, $\rho_c \approx 10^{-17} \text{ g cm}^{-3}$, and initial temperature of $10 \text{ K}$.

We note that since the temporal evolution is slightly different in both our studies owing to the differences in the gas EOS (Saumon et al. 1995, used by Vaytet & Haugbølle 2017 versus D’Angelo & Bodenheimer 2013 used in this work), opacities, and griding scheme (Lagrangian versus Eulerian), the comparisons are not made at the exact same time but when the central density $\rho_c$ in both simulations reaches $\sim 10^{-11} \text{ g cm}^{-3}$.

Vaytet & Haugbølle (2017) reported a first core radius of roughly $2 \text{ au}$ at the time of formation, which then expands to about $5 \text{ au}$ and stays roughly constant for a few hundred years and undergoes a second expansion phase, which increases the core radius to $\sim 8 \text{ au}$. In our simulations, the radius is also roughly $2 \text{ au}$ at the time of formation, which then grows to about $5 \text{ au}$ and gradually contracts back to $\sim 3 \text{ au}$. Some earlier studies also estimate a first core radius of roughly $3 \text{ au}$, however the core is seen only to be contracting with time (Masunaga et al. 1998; Tomida et al. 2013).

The first core lifetime is $\sim 450 \text{ yr}$ in comparison to $\sim 415 \text{ yr}$ obtained by Vaytet & Haugbølle (2017) and $\sim 650 \text{ yr}$ by Masunaga & Inutsuka (2000) and Tomida et al. (2013).

For an initial $1 M_\odot$ cloud, at the end of our simulation, the second core radius is $\sim 3.95 R_\odot$ in agreement with Masunaga & Inutsuka (2000; $\sim 4 R_\odot$) and still expanding as seen by Tomida et al. (2013; $\sim 10 R_\odot$). We note an initial contraction phase followed by expansion due to heating or mass accumulation as also seen by earlier studies (Larson 1969; Masunaga & Inutsuka 2000; Tomida et al. 2013). In comparison, Vaytet & Haugbølle (2017) obtained a much smaller second core of roughly $1 R_\odot$ but they expect the core to expand to larger radii.

Notes. Listed above are the cloud properties for runs with different initial cloud mass $M_\odot$ ($M_0$), outer radius $R_{\text{out}}$ (au), temperature $T_0$ (K), stability parameter $M_{\text{BE}}/M_0$, and central density $\rho_c$ (g cm$^{-3}$).

Fig. 10. First core lifetime, i.e. time between the onset of formation of the first and second cores for different initial cloud masses. The circles indicate results from the simulation runs with a constant initial temperature of $10 \text{ K}$, whereas the diamonds, triangles, and crosses indicate results from the simulation runs with constant stability parameters $M_{\text{BE}}/M_0$ of $5.27e-01$, $5.27e-02$, and $5.27e-03$ for the low-, intermediate-, and high-mass regimes, respectively.

We note that Masunaga & Inutsuka (2000) supposed an initial uniform density profile with $\rho = 1.415 \times 10^{-19} \text{ g cm}^{-3}$, an outer boundary $R_{\text{out}} = 10^2 \text{ au}$, and initial temperature $T_0$ of $10 \text{ K}$, whereas Tomida et al. (2013) adopted an initial Bonnor–Ebert density $\rho$ of $5.27e-01$, $5.27e-02$, and $5.27e-03$ for the low-, intermediate-, and high-mass regimes, respectively.
density profile with $\rho_c = 1.2 \times 10^{-18} \text{ g cm}^{-3}$, an outer boundary $R_{\text{out}} \approx 8800 \text{ au}$, and $T_0 = 10 \text{ K}$.

Since the studies by Vaytet & Haugbølle (2017) are closest to our approach, we further investigated the differences between our results for the collapse of an initial $1 M_\odot$ cloud using the same temperature-dependent opacities instead of opacity tables (see Appendix D).

All of the previous 1D spherically symmetric radiation hydrodynamic (RHD) studies using frequency-dependent (Masunaga et al. 1998; Masunaga & Inutsuka 2000) and grey FLD approximation (Vaytet & Haugbølle 2017) as well as 3D radiation magnetohydrodynamic (RMHD) simulations without rotation and magnetic fields (Tomida et al. 2013) were limited to the low-mass regime ($M_0 \leq 10 M_\odot$). The thermal evolution and properties of the first and second cores from our low-mass runs are in good agreement with these previous works.

In their collapse calculations for the low-mass regime, Vaytet & Haugbølle (2017) showed comparisons for different initial cloud masses ($M_0 \leq 8 M_\odot$) at a time after the formation of the second core, which indicates that most significant differences in the radial profiles of different core properties are seen outwards from the first shock as a horizontal spread (see their Fig. 4) that is similar to our results presented in Sect. 4.2.

Baraffe et al. (2012), Vaytet et al. (2013), and Vaytet & Haugbølle (2017) found the first core radius and mass to be similar within an order of magnitude for their collapse simulations with different initial cloud masses similar to the results presented herein for the low-mass regime (see Sect. 4.3). Masunaga et al. (1998) noted that the first core radius and mass are independent of the initial cloud mass and density profile, but are weakly dependent on initial cloud temperature and opacity. We also find this weak dependence on initial cloud temperature as discussed in Sect. 4.4.

Tomida et al. (2010a) suggested that the thermal evolution may depend on the initial conditions such as cloud mass, opacities, and temperature. In our studies, since we span a wide range of initial cloud masses beyond $10 M_\odot$, we find a transition region in the intermediate-mass regime, which indicates a dependence on the initial cloud mass as discussed in Sect. 4.3. We also find a linear dependence of this transition region on the initial cloud radius (see Appendix C).

4.6. Limitations

In our studies, we use spherically symmetric models that neglect the effects of rotation and turbulence. It is however important to take into account effects due to non-negligible internal motions in molecular clouds. Rotation and magnetic fields are expected to have a significant effect on the evolution of the cloud and properties of hydrostatic cores. These effects will be investigated in our future work.

In comparison to pure RHD simulations without rotation, depending on an ideal or a resistive magnetohydrodynamics model and how slow or fast the rotation is, Tomida et al. (2013) found significant differences mostly in the first core lifetime and second core radius (see their Table 2). Tomida et al. (2013) and Vaytet et al. (2013) suggested that the first core lifetime increases slightly in the presence of rotation since it would slow down the collapse.

The lifetimes estimated in our studies can thus be considered as lower limits. Despite the absence of rotation and magnetic fields, our results can still be used as initial conditions in stellar evolution simulations.
5. Summary
We performed 1D radiation hydrodynamic simulations to model the gravitational collapse of a molecular cloud through the formation of the first and second hydrostatic cores. As carried out by some previous studies, we emphasize the importance of using a realistic gas EOS, which takes into account effects such as dissociation, ionization, rotational, and vibrational degrees of freedom for the molecules and which also plays a significant role in accounting for the phase transitions from the monatomic to diatomic gas.

Using an initial constant cloud temperature ranging from 5 to 100 K and an outer radius of 3000 and 5000 au, we model clouds with different initial masses spanning a range from 0.5 to 100 $M_\odot$. For each of these cases, we trace the evolution through an initial isothermal collapse phase, first core formation, adiabatic contraction, H$_2$ dissociation, second collapse phase, and the second core formation. The thermal evolution of the cloud for the 1 $M_\odot$ cloud is summarized in Fig. 3.

First, we varied the initial cloud mass, keeping a constant initial temperature of 10 K and an outer radius of 3000 au. We note the differences (within an order of magnitude) in the first core properties (listed in Table 2), although the clouds with different initial masses follow a similar evolution. We examine the dependence of the first core properties on the initial cloud mass and find a transition region in the intermediate-mass regime. Our results indicate an increase in the first core radius with an increase in the initial cloud mass until around 8–10 $M_\odot$, after which the first core radius decreases towards the higher initial cloud masses. This trend is also observed when comparing the first core mass for different initial cloud masses.

We would like to draw more attention to the diminishing first core lifetimes for higher initial cloud masses, which in turn affects the size and mass of the first core. It is also highly unlikely to observe first cores with such small lifetimes. Massive clouds have the highest accretion rate and are the most unstable, which is why they evolve faster. For these cases, since the ram pressure is higher than the gas pressure, gravity acts as a dominant force that prevents a strong accretion shock. Hence, we predict that the first cores are non-existent in the high-mass regime.

We confirmed the presence of the transition region in the intermediate-mass regime by performing an additional set of simulations. We use a different constant stability parameter $M_{\text{BE}}/M_{\text{cl}}$ for the low-mass (0.5–10 $M_\odot$), intermediate-mass (8–20 $M_\odot$), and high-mass regimes (30–100 $M_\odot$), respectively. This implies that the initial cloud temperatures range from 5 to 100 K. The outer cloud radius for these runs is always fixed to 3000 au. We also investigated the influence of the outer cloud radius on the first core properties by performing simulations with a cloud radius of 5000 au for a constant initial temperature of 10 K. We found a similar transition region in the intermediate-mass regime. These results also indicate the weak dependence of the first core properties on the initial cloud temperature and outer radius.

We note that the results for the first core lifetimes presented in this work should be treated as lower bounds on the core properties since we neglect the effects of rotation and magnetic fields, which could slow down the collapse and in turn affect the core properties. These effects will be taken into account in future studies.

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Appendix A: Comparisons to a uniform density cloud

There have been previous collapse studies using a uniform density cloud as an initial setup instead of the Bonnor–Ebert sphere as considered in this work. However, the uniform density cloud eventually evolves into a Bonnor–Ebert-like profile (Larson 1969; Masunaga et al. 1998). We compare the effect of a uniform density and Bonnor–Ebert-like density profile on the core properties. Figure A.1 shows the radial profiles of the density and velocity and the ratio of gas to ram pressure for collapse of a 1 $M_\odot$ cloud for three different cases, using an initial Bonnor–Ebert sphere at 10 K (blue) and a uniform cloud at 10 K (dashed red) and 30 K (dashed yellow).

For the 30 K uniform density cloud and the 10 K Bonnor–Ebert sphere clouds, we note that the initial density profile does not have a significant effect on evolution of the cloud as also seen by Vaytet & Haugbølle (2017). However, in comparison to the Bonnor–Ebert sphere setup, the evolution of a uniform density cloud is much slower (~3 × 10^4 yr). In contrast, Masunaga & Inutsuka (2000) argued that the initial density profile does affect the protostellar evolution due to different dynamics. Since there are no significant differences between the two density profiles, in our studies we used a Bonnor–Ebert sphere as an initial density profile. Vaytet & Haugbølle (2017) also suggested that a Bonnor–Ebert sphere is a better representation of the collapsing cloud.

In case of a 10 K uniform density cloud, we note a different behaviour. In this case, the strong ram pressure due to the high infall velocities is always higher than the gas pressure as seen in Fig. A.1. This may be because the clouds are highly unstable and gravity acts as the dominant force and there is little effect due to pressure forces, which prevents the formation of the first hydrostatic core. A similar case devoid of the first accretion shock is seen by Vaytet & Haugbølle (2017). They used an initial uniform density setup for a 4 $M_\odot$ cloud collapse at an initial temperature of 5 K. This behaviour of the 10 K uniform density cloud does not invalidate the previous studies that used initial uniform density, since the clouds were not unstable to skip the first core formation.

Appendix B: Numerical convergence

B.1. Resolution tests

Resolution plays an important role especially when treating regions near accretion shocks. For an initial 1 $M_\odot$ cloud, we performed core collapse simulations with the exact same initial conditions but using different resolutions. The simulations using different resolutions have no significant effects on the evolution seen in Fig. B.1, which indicates the numerically convergence for our studies. As expected for the lowest resolution, owing to fewer grid cells in the inner region, we see slight differences at the second shock position. These differences probably increase for even lower resolutions. There seems to be a convergence around 4400 cells and above. This indicates a minimum resolution of around 4400 cells required for our simulations.

B.2. Comparisons for different inner radii

In order to ensure that the inner radius does not affect the second shock position, we ran some tests with different inner radii. As seen in Fig. B.2, all of the runs evolve in a similar manner. We note the differences for the simulations with $R_{\text{in}} = 3 \times 10^{-4}$ au and $R_{\text{in}} = 10^{-3}$ au. However, there seems to be a convergence for an inner radius around $10^{-4}$ au. For our studies, we chose an inner radius of $10^{-4}$ au to avoid the boundary being too close to the second shock.
Radial profiles of the density, velocity, and gas temperature for an initial 1 $M_\odot$ cloud at an initial temperature $T_0$ of 10 K are shown at a time step after the second core formation. The different lines indicate the results each using a different inner radius of the cloud. The dashed blue line indicates $R_{in} = 10^{-4}$ au, the red line indicates $10^{-3}$ au, the green line indicates $3 \times 10^{-4}$ au, and the dashed yellow line indicates $10^{-5}$ au.

Radial profiles of the density, velocity, and gas temperature for an initial 1 $M_\odot$ cloud are shown at a time step after the second core formation. The different lines indicate the results each using a different inner radius of the cloud. The dashed blue line indicates $R_{in} = 10^{-4}$ au, the red line indicates $10^{-3}$ au, the green line indicates $3 \times 10^{-4}$ au, and the dashed yellow line indicates $10^{-5}$ au.
Table C.1. Initial cloud properties.

<table>
<thead>
<tr>
<th>$M_0$ ($M_\odot$)</th>
<th>$R_{\text{out}}$ (au)</th>
<th>$T_0$ (K)</th>
<th>$M_{\text{BE}}/M_0$</th>
<th>$\rho_c$ (g cm$^{-3}$)</th>
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</thead>
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<tr>
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<tr>
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<tr>
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</tbody>
</table>

Notes. Listed above are the cloud properties for runs with different initial cloud mass $M_0$ ($M_\odot$), outer radius $R_{\text{out}}$ (au), temperature $T_0$ (K), stability parameter $M_{\text{BE}}/M_0$, and central density $\rho_c$ (g cm$^{-3}$).

Appendix C: Dependence on initial cloud radius

In order to test the robustness of the transition region seen in the first core properties as described in our results, we performed an additional set of simulations spanning initial cloud masses from 1–100 $M_\odot$ at a constant initial temperature of 10 K, but with a larger outer radius $R_{\text{out}}$ of 5000 au. The computational grid for these simulations comprises of 4568 cells. We use 320 uniformly spaced cells from $10^{-4}$ to $10^{-2}$ au and 4248 logarithmically spaced cells from $10^{-2}$ to 5000 au. We again made sure that the last uniform cell and the first logarithmic cell are identical in size as described previously in Sect. 3.

Figure C.1 shows an increase in the mean first core radius until around 12–14 $M_\odot$ beyond which it decreases towards the high-mass regime. Figure C.2 indicates a shorter first core lifetime towards intermediate- and high-mass regimes. In this figure, we compare the mean first core radius and first core lifetime from the runs with an outer radius of 3000 au (shown as circles) to those with an outer radius of 5000 au (shown as diamonds). We see that the lifetime scales as $M^{-2.5}$ in the intermediate- and high-mass regimes. In this case, the fit (dashed line) also incorporates the radial dependence of $R^{-2.5}$ as derived in Sect. 4.3.

We thus confirm the presence of a transition region in the intermediate-mass regime seen in the first core radius and lifetime, which indicates that first cores are non-existent in the high-mass regime. We find a linear dependence of the transition mass on the initial cloud radius.

Fig. C.1. Mean first core radius as a function of initial cloud mass. The mean radius is calculated over the time from the onset of the first core formation until the second core formation. Comparisons from two different set of simulations with an outer cloud radius of 3000 au (circles) and 5000 au (diamonds) are shown.

Fig. C.2. First core lifetime, i.e. time between the onset of formation of the first and second cores for different initial cloud masses. Comparisons from two different set of simulations with an outer cloud radius of 3000 au (circles) and 5000 au (diamonds) are shown.
Appendix D: Effect of opacities

We present comparison studies between our simulations and those kindly provided by N. Vaytet (2017, priv. comm.) mainly focussing on the effect of opacities.

As described in Sect. 4.5, since the studies by Vaytet & Haugbølle (2017) are closest to our approach we compared our results for the collapse of a 1 $M_\odot$ cloud at an initial temperature of 10 K. We note the discrepancies owing to the differences in the gas EOS (Saumon et al. 1995 used by Vaytet & Haugbølle 2017 versus D’Angelo & Bodenheimer 2013 used in this work), opacity tables, and griding scheme (Lagrangian versus Eulerian) as seen in Fig. 11.

In order to investigate the effect of opacities, we compared our simulation for the collapse of a 1 $M_\odot$ cloud using a temperature-dependent opacity $\kappa = 0.02 \left( T/T_0 \right)^2 \text{ cm}^2 \text{ g}^{-1}$ to the simulation provided by N. Vaytet (2017, priv. comm.) performed for an identical initial setup using the same temperature-dependent opacity. In both these runs, $T_0 = 10$ K. As seen in Fig. D.1, although his simulations (dashed red line) still tend to produce a bigger first core radius, the difference is smaller compared to using different opacity tables (see Fig. 11). The second core does not contract as much in our simulations (bluish purple line), however as predicted the second core in his simulation may expand to obtain a value close to ours. These comparisons indicate that opacities play a role in determining the core properties but only provide some fine-tuning. Thus, the main properties derived herein are still robust.

In addition, the different treatment of the gas EOS and griding scheme may also contribute to the differences. We note that since the temporal evolution is slightly different in both our studies owing to these differences, the comparisons are not made at the exact same time but when the central density $\rho_c$ in both simulations reaches $\sim 10^{-1} \text{ g cm}^{-3}$.

**Fig. D.1.** Radial profiles of the density, velocity, and gas temperature of an initial 1 $M_\odot$ cloud at an initial temperature $T_0$ of 10 K are shown at the time when central density $\rho_c$ in both simulations reach roughly $10^{-1} \text{ g cm}^{-3}$. The bluish purple solid lines show results from simulations described in Sect. 3, while the dashed red line represents results from simulations provided by N. Vaytet (2017, priv. comm.). We note that for this comparison both codes use the same temperature-dependent opacity $\kappa = 0.02 \left( T/T_0 \right)^2 \text{ cm}^2 \text{ g}^{-1}$.