The physical and chemical structure of Sagittarius B2

III. Radiative transfer simulations of the hot core Sgr B2(M) for methyl cyanide

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ABSTRACT

Context. We model the emission of methyl cyanide (CH₃CN) lines towards the massive hot molecular core Sgr B2(M).

Aims. We aim to reconstruct the CH₃CN abundance field, and investigate the gas temperature distribution as well as the velocity field.

Methods. Sgr B2(M) was observed with the Atacama Large Millimeter/submillimeter Array (ALMA) in a spectral line survey from 211 to 275 GHz. This frequency range includes several transitions of CH₃CN (including isotopologues and vibrationally excited states).

We employed the three-dimensional radiative transfer toolbox Pandora in order to retrieve the velocity and abundance field by modeling different CH₃CN lines. For this purpose, we based our model on the results of a previous study that determined the physical structure of Sgr B2(M), i.e., the distribution of dust dense cores, ionized regions, and heating sources.

Results. The morphology of the CH₃CN emission can be reproduced by a molecular density field that consists of a superposition of cores with modified Plummer-like density profiles. The averaged relative abundance of CH₃CN with respect to H₂ ranges from 4 × 10⁻¹¹ to 2 × 10⁻⁸ in the northern part of Sgr B2(M) and from 2 × 10⁻¹⁰ to 5 × 10⁻⁷ in the southern part. In general, we find that the relative abundance of CH₃CN is lower at the center of the very dense, hot cores, causing the general morphology of the CH₃CN emission to be shifted with respect to the dust continuum emission. The dust temperature calculated by the radiative transfer simulation based on the available luminosity reaches values up to 900 K. However, in some regions vibrationally excited transitions of CH₃CN are underestimated by the model, indicating that the predicted gas temperature, which is assumed to be equal to the dust temperature, is partly underestimated. The determination of the velocity component along the line of sight reveals that a velocity gradient from the north to the south exists in Sgr B2(M).

Key words. radiation transfer – stars: formation – stars: massive – ISM: clouds – ISM: molecules – ISM: individual objects: SgrB2

1. Introduction

Almost all the information we have about the interstellar medium (ISM) is obtained from the analysis of electromagnetic radiation received by telescopes. Hence, in astrophysics it is crucial to predict the radiative properties of a physical model when interpreting astronomical observations. For this purpose, three-dimensional radiative transfer codes have been developed which can calculate the radiation signature associated with a three-dimensional physical model of a specific source. The results can subsequently be compared to observations to study the physical and chemical properties of astrophysical objects.

In the struggle to understand how the evolution of high-mass stars proceeds from the fragmentation of giant molecular clouds down to dense hot molecular cores (e.g., Tan et al. 2014; Schilke 2015), it is important to study the kinematics, density structure, temperature distribution, and chemical variations of the dense gas associated with these objects, as these parameters determine their dynamical evolution. The study of the emission of lines of certain molecular species can provide this crucial information as the intensity and the line profile are determined by the physical and excitation conditions of the gas.

There are several molecules in the ISM that can be used to study the dense cores where star formation takes place. However, hot molecular cores (e.g., Kurtz et al. 2000; Cesaroni 2005) associated with high temperatures (T > 100 K) and high densities (n_H₂ > 10⁶ cm⁻³) are traced best by complex molecules (i.e., molecules with six or more atoms) that are mainly formed on dust grains and released into the gas phase during the warm-up through the heating produced by the newly born star. Among these complex molecules, CH₃CN has turned out to be an excellent tool to determine the gas temperature due to its symmetry structure (e.g., Araya et al. 2005) and due to the distribution and velocity field of the high-density gas from where high-mass stars form (see, e.g., Remijan et al. 2004; Sánchez-Monge et al. 2013; Hernández-Hernández et al. 2014).

Sagittarius B2 (hereafter Sgr B2) is one of the most massive molecular clouds in the Galaxy. Located at a projected distance of ~100 pc from the Galactic center, which has a distance of 8.34 ± 0.16 kpc from the Sun (Reid et al. 2014), Sgr B2 is an excellent source for studying the formation of high-mass clusters and astrochemistry. It has been shown to harbor active star formation sites (Gordon et al. 1993) and contains a wide range of different molecules including complex organic species, many of which were found for the first time in space towards Sgr B2, for example acetic acid (CH₃COOH, Mehringer et al. 1997) or ethyl formate (C₂H₅OCHO, Belloche et al. 2009). The Sgr B2 complex contains a total mass of ~10³ M☉, and a total luminosity of about 10⁴ L☉ (Goldsmith et al. 1990). Based on its density structure, it has been proposed that Sgr B2 is
composed of three different parts (Hüttemeister et al. 1993): a low-density envelope with \( n_H_2 \sim 10^2\text{ cm}^{-3} \), a moderate-density region with \( n_H_2 \sim 10^5\text{ cm}^{-3} \) extending around local hot molecular cores, which are the most compact and densest regions with \( n_H_2 \sim 10^7\text{ cm}^{-3} \). The two main sites of star formation are the central hot molecular cores Sgr B2(N) and Sgr B2(M), which have sizes of \( \sim 0.5\text{ pc} \) and contain numerous ultracompact H II regions (see, e.g., Mehringer et al. 1993; Gaume et al. 1995). A more detailed description of Sgr B2 can be found in (Schmiedeke et al. 2016, hereafter Paper I) and (Sánchez-Monge et al. 2017, hereafter Paper II).

This is the third in a series of papers investigating the star-forming region Sgr B2. In this work, we model line transitions of methyl cyanide, CH\(_3\)CN, by employing radiative transfer codes. This model is based on a physical model of Sgr B2, which was developed in the first paper of this series (Paper I). The modeling of the CH\(_3\)CN transitions is based on high-resolution observations of Sgr B2 obtained with the Atacama Large Millimeter/submillimeter Array (ALMA, ALMA Partnership et al. 2015). The continuum emission of these observations was presented and analyzed in the second paper of this series (Paper II). In the current paper, we focus our analysis on the hot molecular core Sgr B2(M), which exhibits a very complex and fragmented structure, and appears to be in a more evolved stage of evolution than Sgr B2(N). Earlier observations using the Submillimeter Array (SMA) by Qin et al. (2011) revealed at least 12 dense cores at a frequency of 345 GHz. Recent ALMA observations at 242 GHz (Paper II) increased this number to 27 sources including dust dense cores and some H II regions, and suggested a more complex structure with hints of the presence of filaments.

The current paper is organized as follows. In Sect. 2 we give a brief overview of the ALMA observations. In Sect. 3, we present the CH\(_3\)CN data and compare the distribution of the dense gas to the continuum emission. The modeling procedure is described in Sect. 4. In Sect. 5 we describe the physical model used to model the CH\(_3\)CN emission towards Sgr B2(M). This is followed by a comparison of the simulations with the observational data in Sect. 6. Finally, Sect. 7 summarizes the main results of the paper. Appendices contain a description of the parameters of the physical model as well as several spectra comparing the observational and simulated data.

### 2. Observations

The observations of Sgr B2(M) were conducted using ALMA during its Cycle 2 in June 2014 and June 2015 (project number 2013.1.00332.S). The configuration used 34 and 36 antennas, with extended baselines in the range between 30 m and 650 m. At the frequency range of our observations (from 211 GHz to 275 GHz) this results in an angular resolution of \(0.′4–0.′8\). Sgr B2(M) was observed in track-sharing mode, together with Sgr B2(N), with the phase center at \((\alpha, \delta) = (17^h47^m20.357, -28°23′04′.53)\). The observations were done in the spectral scan mode surveying all of ALMA band 6 from 211 to 275 GHz. The achieved spectral resolution is \(0.5–0.7\text{ km s}^{-1}\) across the full frequency band. Calibration and imaging were performed in CASA\(^1\) version 4.4.0. The resulting data cubes used in this project were restored with a circular Gaussian beam of \(0.′7\). Further information on the calibration, observational details, and imaging can be found in Paper II.

### Table 1. CH\(_3\)CN transitions analyzed in this paper.

<table>
<thead>
<tr>
<th>Transition</th>
<th>Frequency (GHz)</th>
<th>(E_{\text{lower}}) (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Main isotopologue, ground state</td>
<td></td>
<td></td>
</tr>
<tr>
<td>(12_0-11_0)</td>
<td>220.747261</td>
<td>57.87</td>
</tr>
<tr>
<td>(12_1-11_1)</td>
<td>220.743011</td>
<td>64.96</td>
</tr>
<tr>
<td>(12_2-11_2)</td>
<td>220.730261</td>
<td>86.25</td>
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<tr>
<td>(12_3-11_3)</td>
<td>220.709017</td>
<td>121.71</td>
</tr>
<tr>
<td>(12_4-11_4)</td>
<td>220.679287</td>
<td>171.36</td>
</tr>
<tr>
<td>(12_5-11_5)</td>
<td>220.641084</td>
<td>235.17</td>
</tr>
<tr>
<td>(12_6-11_6)</td>
<td>220.594423</td>
<td>313.13</td>
</tr>
<tr>
<td>(13_0-12_0)</td>
<td>239.137916</td>
<td>68.39</td>
</tr>
<tr>
<td>(13_1-12_1)</td>
<td>239.133313</td>
<td>75.48</td>
</tr>
<tr>
<td>(13_2-12_2)</td>
<td>239.119504</td>
<td>96.77</td>
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<td>(13_3-12_3)</td>
<td>239.096497</td>
<td>123.23</td>
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<td>239.064299</td>
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<td>239.029294</td>
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<td>323.64</td>
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<td>(13_7-12_7)</td>
<td>238.912715</td>
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<td>238.843926</td>
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<td>257.527384</td>
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<td>257.522428</td>
<td>86.88</td>
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<td>257.482792</td>
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<td>427.11</td>
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<td>533.31</td>
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<tr>
<td>(14_9-13_9)</td>
<td>257.127035</td>
<td>653.59</td>
</tr>
</tbody>
</table>

| Vibrationally excited \(v_H = 1\) | | |
| \(12_1-11_1\) | 221.625828 | 577.13 |
| \(13_{0-12_0}\) | 232.234188 | 66.38 |
| \(13_{1-12_1}\) | 232.229822 | 73.48 |
| \(13_{2-12_2}\) | 232.216726 | 94.79 |
| \(13_{3-12_3}\) | 232.194906 | 130.30 |
| \(13_{4-12_4}\) | 232.164369 | 180.01 |
| \(13_{5-12_5}\) | 232.125130 | 243.89 |
| \(13_{6-12_6}\) | 232.077203 | 321.94 |
| \(13_{7-12_7}\) | 232.020609 | 414.15 |

\(^1\) The Common Astronomy Software Applications (CASA; McMullin et al. 2007) software can be downloaded at http://casa.nrao.edu

**Notes.** Parameters of the transitions obtained from the molecular databases CDMS (Müller et al. 2005; Endres et al. 2016) and JPL (Pickett et al. 1998). In more detail, the CH\(_3\)CN and \(^{13}\)CH\(_3\)CN entries are based on Müller et al. (2015, 2009), respectively, with important additional data especially from Cazzoli & Puzzarini (2006) and Pearson & Müller (1996). The dipole moment of CH\(_3\)CN used to derive the Einstein \(A_{\ell\ell}\) values is taken from Gadhi et al. (1995); the dipole moment of \(^{13}\)CH\(_3\)CN is assumed to agree with that of the main isotopologue, as is frequently done.

### 3. Observational results

The frequency range of the ALMA observations covers several rotational transitions of CH\(_3\)CN in the vibrational ground state (e.g., \(J = 12–11\) at 220.7 GHz, \(J = 13–12\) at 239.1 GHz, and \(J = 14–13\) at 257.5 GHz) and in the vibrationally excited state \(v_H = 1\). An overview of the CH\(_3\)CN transitions analyzed in this paper is given in Table 1.
The middle panels of Fig. 1 show the Sgr B2(M) peak intensity maps of three CH$_3$CN lines compared with the ALMA continuum emission (black contour; from Paper II). The image maps of the continuum emission for the frequencies of each of the selected CH$_3$CN transitions are shown in the top panels. A first comparison of the distribution of the dense gas and the continuum emission reveals that the CH$_3$CN emission is much more extended than the continuum emission, especially towards the south. Moreover, the local maxima in the line emission do not necessarily coincide with the position of the peaks in the continuum maps. This is clearly seen in the northern part of Sgr B2(M) where a compact CH$_3$CN condensation appears shifted towards the northeast with respect to the continuum. The southern region exhibits a significantly brighter and more extended CH$_3$CN emission than towards the northern part.

**Fig. 1.** Top panels: continuum maps towards Sgr B2(M) determined using STATCONT (Sánchez-Monge et al. 2018) at the frequencies of the spectral windows that cover the three CH$_3$CN ground state transitions: 220 GHz (left), 239 GHz (center), and 257 GHz (right). The black contour shows the 10% level of the continuum emission peak. Middle panels: intensity peak maps of different CH$_3$CN transitions: $J = 12-11$, $K = 3$ (left), $J = 13-12$, $K = 3$ (center), and $J = 14-13$, $K = 3$ (right). The intensity peak maps are obtained from a narrow frequency range around the frequency indicated with a vertical dotted line in the bottom panels. Bottom panels: spectra extracted at three different positions marked with crosses in the top and middle panels. The selected positions are located in the north (Mn, in red), in the center of the region associated with the brightest continuum peak (Mm, in black), and towards the south (Ms, in blue). To enhance the clarity, we shifted the red spectrum by +100 K and the blue spectrum by −200 K. The relative continuum levels are indicated by the dashed gray lines.
In the bottom panels of Fig. 1, we present spectra extracted towards selected positions indicated with crosses in the top and middle panels of the figure. The spectra show the emission of the $K$ lines of the ground state CH$_3$CN transitions $J = 12-11$ (left panel), $J = 13-12$ (central panel), and $J = 14-13$ (right panel). The spectra show the characteristic $K$-ladder of a symmetric top molecule, but also the lines of other molecules that are partly blending the CH$_3$CN lines. For a better identification of which lines actually belong to CH$_3$CN, the reader is referred to Fig. B.1, where the observational spectra are compared to the results of our simulations. Depending on the location within Sgr B2(M), the regions show different spectral characteristics. The spectrum extracted from the northern region (Mn and red cross in Fig. 1) has clear and well-defined lines, all of them in emission. The southern position (Ms and blue cross in the figure) is completely different from those obtained in the south and north. The central spectra show a complex combination of emission and absorption features belonging to CH$_3$CN. The absorption features are related to the strong continuum emission present in the central region, which at the depicted frequency is about 180 K. The emission of a channel map of the strongest absorption feature of CH$_3$CN ($J = 12-11, K = 0$) is shown in Fig. 2. The possible origin of the strong continuum emission that causes the absorption features is the presence of the numerous H II regions in Sgr B2(M). However, a comparison of the position and extent of the known H II regions with the area of absorption shows that they only partly coincide (see black circles in Fig. 2). Moreover, the absorption feature is also present at regions with no H II regions. On the contrary, the ALMA 242 GHz continuum emission (magenta contours in Fig. 2) clearly coincides with the area of absorption, indicating that bright dust continuum emission is the most probable origin of the absorption features found in the central region of Sgr B2(M). A similar absorption produced against bright dust continuum

**Fig. 2.** Channel map at a frequency of 220.765 GHz corresponding to the line of CH$_3$CN ($J = 12-11, K = 0$). Clear absorption is observed in the center of the map. Magenta contours show the ALMA 242 GHz continuum emission from Paper II. Black circles indicate the position and extent of the H II regions (see Paper I).

4. Modeling procedure

We used the radiative transfer tool box Pandora (presented in Paper I), which in one of its implementations can use the radiative transfer code RADMC-3D to model the CH$_3$CN line transitions in Sgr B2(M). A detailed description of the framework Pandora and the RADMC-3D code can be found in Paper I and Dullemond (2012). In this section we focus on the new routines implemented in Pandora that are necessary for the line modeling and that were therefore not described in the previous paper.

4.1. Modeling CH$_3$CN with RADMC-3D

In order to solve the radiative transfer problem, RADMC-3D samples the density structure defined by the user by generating a grid via the method of adaptive mesh refinement. This means that parent cells are refined into children cells if the density gradient within the parent cell exceeds a certain value (details can be found in Paper I). To model the CH$_3$CN line transitions towards Sgr B2(M), we used a cubic grid with a side length of 1 pc centered around Sgr B2(M). We set the allowed maximum density difference between the cells to 10%. This configuration results in a minimum cell size of 100 au and roughly $10^7$ final cells. After the grid is generated the dust temperature is calculated self-consistently based on the luminosity sources by using a Monte Carlo approach (Bjorkman & Wood 2001).

In the last step of the radiative transfer simulations, we used RADMC-3D to calculate the CH$_3$CN line emission. For this purpose, RADMC-3D first calculates the level populations for each cell in dependence of the gas temperature. We make two assumptions: first, that local thermodynamic equilibrium (LTE) conditions are present, i.e., that the energy levels are populated according to the Boltzmann distribution, and second, that the gas temperature equals the dust temperature, which is a valid assumption in high-density regions like those found towards Sgr B2(M).

Due to the high densities present in the small-scale structures of Sgr B2(M), the LTE approximation is a valid assumption.
This can be seen by calculating the critical density $n_{\text{crit}}$, which is defined by the ratio of the Einstein $A_{ul}$ coefficient and the collisional rate coefficient $C_{ul}$:

$$n_{\text{crit}} = \frac{A_{ul}}{C_{ul}} \quad (1)$$

The collisional terms involve the square of the density, whereas the radiative terms only increase linearly with density. Thus, for densities much higher than $n_{\text{crit}}$, the collisional terms become dominant and the level populations are Boltzmann distributed, meaning that the LTE approximation is valid. Because $A_{ul} \propto v^4$, transitions with higher frequencies need higher densities to be thermally excited. For the transitions within one K-ladder of CH$_3$CN this does not really matter because the transitions are closely spaced. We calculated the critical density of all $J = 12-11$ transitions of the main isotopologue based on the values of the Einstein $A_{ul}$ coefficient and the collisional rate coefficients at 100 K from the Leiden Atomic and Molecular Database (LAMDA; Schöier et al. 2005) database. For all transitions the critical density is on the order of $10^9$ cm$^{-3}$. Because the collisional rate coefficient depends on the temperature, the critical density also depends on the temperature. However, in the considered range of temperatures the order of magnitude remains the same. If we now compare the critical densities with the densities in Sgr B2, we find that the LTE approximation is valid within the small-scale structure of Sgr B2(M), for which the densities range from $4 \times 10^4$ to $5 \times 10^8$ cm$^{-3}$. The density profiles of the cores of Sgr B2(M) are described by modified Plummer density profiles (see Paper I and Sect. 5). In Fig. 3 the modified Plummer density profiles used in the model are plotted together with the average of the critical densities. Depending on the exact parameters of the core, the LTE approximation is valid within $\sim 10^4$ au of the center of the core. We note that this is only a lower limit; the overall density is obtained as the superposition of the density profiles of all the cores, thus increasing the value of the density.

To calculate the line transitions in the LTE approximation, RADMC-3D needs information about the molecular energy levels and the transition parameters. The energy levels, transition frequencies, and Einstein $A_{ul}$ coefficients for the ground state transitions were taken from the CDMS (Cologne Database for Molecular Spectroscopy) catalogue (Müller et al. 2005; Endres et al. 2016), while the data of the vibrationally excited state transitions are taken from the JPL (Jet Propulsion Laboratory) database (Pickett et al. 1998). All these data are available via the Virtual Atomic and Molecular Data Centre (VAMDC).

### 4.2. Post-processing with CASA

The aim of the final step in the modeling procedure is to conduct a proper comparison of the radiative transfer images to the observational data obtained with ALMA. To this end we developed a post-processing routine that uses the software package CASA$^2$. The routine uses the $uv$-coverage of the ALMA observations to sample the simulated data cubes. This ensures that the post-processed files filter out and recover the same emission and spatial scales detectable in the observations. In the second step, we image the synthetic data cubes with the same imaging parameters used for the observational ALMA data. Finally, the post-processed synthetic data can be visually compared to the observational data to search for deviations that require a modification in the initial model. If a deviation is present, the physical structure of the model (i.e., molecular density, velocity field; see Sect. 5) is modified. This cycle is iterated to increase the consistency of the simulated images with the observational maps.

### 5. Physical model

The model used in this paper is based on the three-dimensional physical model of Sgr B2 developed in Paper I. The model was created by modeling the dust and free-free continuum emission of Sgr B2 by employing the radiative transfer toolbox Pandora. The density distribution of the cloud complex was reconstructed by comparing the emission of the model to available observational maps, including both single-dish (e.g., from Herschel/HiGAL, Molinari et al. 2010; Herschel/HIFI, Bergin et al. 2010) and high-resolution interferometric images (e.g., VLA radio-continuum maps, De Pree et al. 1998; Rolffs et al. 2011; SMA 345 GHz maps, Qin et al. 2011) covering a frequency range from 1 GHz to 4.5 THz.

The continuum maps obtained with ALMA (see Paper II) are compared with predictions from the model developed in Paper I and presented in Fig. 12 of Paper II. We found a good correspondence between the predicted emission and the observed, with deviations of less than a factor of 2. Continuum maps at different frequencies together with spectral index$^3$ maps were also compared to individual continuum synthetic maps at the same frequencies and to spectral index synthetic maps showing a good agreement between them (see Paper II). The main discrepancies were found to occur towards the central and brightest cores. The discrepancies can be due to different dust opacity coefficients throughout the Sgr B2(M) region. In a following paper, we will present an updated model for the continuum emission of Sgr B2, obtained by using high angular resolution ALMA observations at frequencies from 80 GHz to 275 GHz. In the current paper, we base our analysis on the physical model setup presented in Paper I, and we model several CH$_3$CN line transitions observed with ALMA.

#### 5.1. Physical model of Schmiedeke et al. (2016)

The physical model of Sgr B2 developed in Paper I consists of dense cores (gas and dust), stars, and H II regions. The model covers spatial scales from 45 pc down to 100 au. The density profiles of the individual cores are assumed to be modified Plummer functions given by

$$n(r) = \frac{n_c}{(1 + |r|^2)^{\alpha/2}}, \quad (2)$$

where $n_c$ is the central density given in H$_2$ (cm$^{-3}$) and $|r|$ is the Euclidean norm including scaling factors

$$|r| = \sqrt{\frac{r_x^2}{r_{0,x}^2} + \frac{r_y^2}{r_{0,y}^2} + \frac{r_z^2}{r_{0,z}^2}}, \quad (3)$$

$^2$ In the original version of Pandora the post-processing is done with the software package MIRIAD. In order to compare these data with observational data obtained with ALMA, and processed with CASA, we developed this second alternative within Pandora for the post-processing.

$^3$ The spectral index $\alpha$ is determined as $S_\nu \propto \nu^\alpha$ where $S_\nu$ is the flux at a given frequency $\nu$. A comparison of the observed and synthetic spectral index maps is found in Fig. 13 of Paper II.
where \( r_{x,y,z} \) are the coordinates and \( r_{0,x}, r_{0,y}, \) and \( r_{0,z} \) set the size of the core in the direction of each principal axis. The overall density structure is obtained by the superposition of the density profiles of all cores. The density in a cell \( j \) is then given by

\[
n_j = \sum_{i=1}^{N} n_i(r), \tag{4}
\]

where \( i \) is the index of the dust core and \( N \) the total number of dust cores. The parameters of the cores are described in Table A.1. The left panel of Fig. 4 shows a synthetic map of the continuum emission at 242 GHz. The black numbers indicate the central position of the dust cores included in the model (see Table A.1). The model presented in Paper I, which describes all the scales from 100 au to 45 pc, also includes large-scale components to reproduce the extended envelope visible in the single-dish (and low-resolution) observations. The ALMA observations filter out the extended emission and are only sensitive to the small-scale dense cores.

All stars are assumed to be point sources, i.e., the radius is not taken into account. The model includes early-type high-mass stars and their \( \text{H} \ II \) regions that have been observed (e.g., De Pree et al. 1998; Rolffs et al. 2011). The stars included in the model, based on the existence of \( \text{H} \ II \) regions, only account for stars down to the B0 spectral type. All later spectral types with masses between 0.01 \( \text{M}_\odot \) and \( \sim 19 \text{ M}_\odot \), i.e., stars which cannot produce \( \text{H} \ II \) regions detectable with current observations, were placed by an algorithm that randomly draws stars from the initial mass function (IMF) presented in Kroupa (2001) and distributes the stars randomly throughout the computational domain based on the gravitational potential. The observed \( \text{H} \ II \) regions created by massive stars are included in the model as Strömgren spheres, i.e., spherical structures with uniform electron density with no dust. A more detailed description of the model can be found in Paper I. In the following section we describe how the molecular density and velocity fields (necessary for line modeling) are set up in Pandora. All other constituents of the model, i.e., stars, \( \text{H} \ II \) regions, and dense cores that were introduced in Paper I, remain unchanged.

### 5.2. Molecular density and velocity field

With the aim of modeling the \( \text{CH}_3\text{CN} \) line emission, we implemented a molecular density and velocity field within Pandora and added them to the physical model retrieved from the continuum modeling. The molecular density is set up based on the Plummer density cores described before. Within Pandora it is possible to define a global molecular abundance factor \( \Omega \) for each species. Based on this global abundance factor the molecular density in a cell \( j \) is obtained by multiplying the density in the cell \( n_j \) by \( \Omega \). However, because the molecular abundance can vary significantly from position to position due to different temperatures, presence of a star, shocks, etc., it is necessary to be able to modify the molecular density on a local level. For this reason, we implemented an option to define a local abundance factor \( \omega_i \) for each Plummer density core. In summary, the molecular density \( n(\text{CH}_3\text{CN})_j \) in a cell \( j \) is given by

\[
n(\text{CH}_3\text{CN})_j = \Omega \sum_{i=1}^{N} n_i(r)\omega_i, \tag{5}
\]

where \( i \) is the index of the dust core, \( N \) the total number of dust cores, \( \Omega \) the global abundance factor, and \( \omega_i \) the local abundance factor of the \( i \)th dust core. The abundance for each species is then calculated by dividing the total molecular density by the total \( \text{H}_2 \) density of the cell.

In addition to the molecular density we also include a velocity field in order to describe the line profiles. This velocity field
includes the velocity along the line of sight, as well as the line width due to turbulent motions of the gas. Within Pandora the velocity along the line of sight for each position is determined by defining the velocity $v_1$ for each individual Plummer core. This gives us the possibility of having different velocities at different positions. In order to ensure a smooth velocity field, the velocity of the gas $v_j$ in a cell $j$ is determined by weighting the contribution of each core by its density at this specific cell as

$$v_j = \frac{\sum_{i=1}^{N} v_i n_i(r)}{\sum_{i=1}^{N} n_i(r)}. \quad (6)$$

This means that the resulting velocity is dominated by the value $v_1$ of the core with the highest density at the considered cell. The turbulent line width $\sigma_{\text{line width}}$ is set up equivalently. The resulting line width is also determined by the thermal broadening.

### 5.3. Parametrization of the molecular density field

As described in Sect. 5.2 the line transitions of CH$_3$CN were calculated by introducing an abundance field consisting of individual cores with Plummer-like density profiles. Although we based our CH$_3$CN abundance field on the density structure retrieved from the continuum emission by Paper I, we had to introduce modifications. These modifications are necessary because the morphology of the emission of CH$_3$CN does not completely coincide with the continuum emission (see Fig. 1 and Sect. 3) and therefore also does not coincide with the position of the dust cores.

Moreover, the emission of CH$_3$CN is much more extended than the continuum emission. We inspected the emission of the less abundant $^{13}$CH$_3$CN isotopologue to determine whether the shift between line and continuum emission might be produced by opacity effects. The same morphology is retrieved for the isotopologue as for the main species. This indicates that the CH$_3$CN abundance is in fact enhanced in the regions with local maxima, and that the morphology of the emission is not caused by opacity effects.

For this reason it is not possible to simply use the dust density structure retrieved from the continuum and to define abundance factors in order to model the CH$_3$CN emission. Instead, we introduced new structures, which we call molecular centers (MC). These structures are located at the local maxima of the molecular line emission as seen in the CH$_3$CN lines\(^4\). These molecular centers are diffuse in dust (H$_2$ density) in order to make sure that the continuum remains unchanged, but they possess a high CH$_3$CN abundance in order to reconstruct the local maxima of the line emission. The location of the molecular centers is shown in the right panel of Fig. 4. It is important to note that these newly introduced molecular centers are not necessarily real entities, but are a consequence of the current implementation of the abundance field parametrization in Pandora. By introducing these molecular centers, we are able to model the complex structure of the CH$_3$CN emission which does not coincide with the continuum emission. Hence, only the abundance field resulting from the superposition of the cores and molecular centers as depicted in Fig. 5 should be considered as a real physical structure.

The parameters from the continuum cores and the parameters of the newly introduced molecular centers are given in Table A.1. Each core and molecular center is described by ten parameters: right ascension, declination, the displacement along the line of sight, the spatial scales as defined in Eq. (3), the exponent of the Plummer function, the central density of H$_2$, the central density of CH$_3$CN, and the velocity along the line of sight. For the cores located at the central region of Sgr B2(M) (M-SMA-1a, M-SMA-1b, M-SMA-1c, M-SMA-1d, M-SMA-2a, and M-SMA-2b) no central density of CH$_3$CN is given because the line emission of this region was not modeled (see Sect. 6.6).\(^4\)

In Fig. 5 density maps of H$_2$ and CH$_3$CN as well as of the relative abundance of CH$_3$CN with respect to H$_2$ are depicted. The relative abundance is considerably lower at the position of the continuum cores where the H$_2$ density is the highest.

\(^4\) Shifting the position of the MC by a few pixels does not significantly vary the results of the model compared to the observations. This gives us some freedom in locating the MCs, but also reveals that there is no unique set of MCs that can reproduce the observations. Follow-up papers aimed at modeling other molecular species can help to set more constraints on the location and properties (both physical and chemical) of these structures.
The correlation between the low abundance of CH$_3$CN and the position of the continuum cores indicates that the chemistry at these very dense and hot regions is different and leads to the destruction of CH$_3$CN (see Sect. 6.4).

6. Analysis of simulated and observational data

In the following sections we compare the simulated data to the observational data. For this purpose, in Sects. 6.1 and 6.2 we analyze the general morphology of the CH$_3$CN emission by comparing integrated intensity maps, and spectra taken from the center of the cores. In Sect. 6.3 we discuss the validity of the temperature distribution determined by RADMC-3D. The abundance and velocity field are discussed in Sects. 6.4 and 6.5. Then in Sect. 6.6 we discuss the observational data from the central region, and the limitations of the current model in this region. In Sect. 6.7 we present the results from the model compared to the observations for the isotopologue $^{13}$CH$_3$CN.

6.1. Distribution of the CH$_3$CN emission

As already discussed in Sect. 5.2, the morphology of the CH$_3$CN emission does not completely coincide with the continuum emission. For this reason, it was necessary to introduce molecular centers with a high CH$_3$CN abundance in order to reconstruct the CH$_3$CN emission from the observations. The general morphology of the CH$_3$CN emission can be investigated by producing integrated intensity maps or zeroth-order moment maps following the expression

$$
\mu(x, y) = \int_{-\infty}^{\infty} (F(x, y) - F_{\text{cont}}(x, y)) \, \text{d}v,
$$

where $F(x, y)$ is the flux at position $(x, y)$ and $F_{\text{cont}}$ the corresponding continuum flux. The zeroth-order moment maps of the $J = 12-11$, $K = 3$ transition obtained from the observations and the simulated model are shown in Fig. 6. This line was used to calculate the zeroth-order moment maps because, in most cases, it is not affected by significant line blending of other species and because it is one of the brightest lines. The comparison of the observed and simulated data shows that the emission obtained from the physical model exhibits in general the same morphology as the observed emission. It is evident that the emission indeed peaks at the position of the newly introduced molecular centers and not at the continuum cores. In the northern part we find two regions with strong emission that do not coincide with the continuum cores. For this reason it was necessary to introduce two molecular centers, MC-4 and MC-11, in order to account for the strong emission in these regions. The integrated line intensity in the northern part reaches values up to 120 K km s$^{-1}$. This is significantly lower than in the southern part, where CH$_3$CN is more abundant and the emission peaks at around 800 K km s$^{-1}$. The central part of Sgr B2(M) exhibits a complex combination of CH$_3$CN emission and absorption features (cf. Fig. 1) and only shows absorption at the considered frequency range of the depicted maps. In Sect. 6.6 we discuss in greater detail the modeling of the central region.

In the southern part four molecular centers were introduced to reconstruct the morphology of the CH$_3$CN emission and an additional molecular center was placed near the continuum core M-SMA-10. The molecular center MC-9 was introduced in order to account for the strong emission in the most southern part, where the CH$_3$CN emission is much more extended than the continuum. Furthermore, the molecular center MC-68 was placed between the continuum cores M-SMA-6 and M-SMA-8, and two additional molecular centers MC-7a and MC-7b were placed north and south of the continuum core M-SMA-7, respectively.

From the difference map of the observed and simulated data, we find a good agreement in regions where the CH$_3$CN emission is strong and decreases in regions with weaker emission. This behavior can be more clearly seen by investigating radial profiles of the integrated line intensity. Radial profiles taken from the center of different molecular centers are shown in Fig. 7. The radial profiles proceed in all cases from west to east. These cuts illustrate that the morphology of the CH$_3$CN emission can be described considerably well with modified Plummer-like functions. However, due to the modeling of the cores as spherical structures, deviations from the real structures with a certain degree of asymmetry are inevitable. Additionally, radial profiles are useful tools for identifying local maxima in the emission. e.g., the radial profile centered around molecular center MC-68 reveals that there is an additional peak in the integrated intensity farther to the east, which is associated with the molecular center MC-7b.

6.2. Spectra of the main isotopologue

In this section we compare the spectra of the observational and simulated data taken from the center of the different cores and molecular centers. On the basis of the transitions presented in this section, we reconstructed the abundance field of CH$_3$CN (see Sect 6.4). The rotational spectrum of a symmetric-top molecule like CH$_3$CN consists of a series of components (determined by the quantum number $K$) for each rotational transitions (determined by the quantum number $J$). This $K$-ladder structure results in multiple lines with different energies that are closely spaced in frequency. Several spectra taken from the center of different cores and molecular centers are shown in Fig. B.1. The intensity of the spectra is given in brightness temperatures. These spectra are only taken from cores and molecular centers located at the northern or southern regions of Sgr B2(M), as shown in Fig. 6; the spectra of the central region are discussed in Sect. 6.6.

The spectra show the frequency range from 220.55 to 220.80 GHz, which includes the first seven $K$-components of the $J = 12-11$ transition of the main isotopologue. The $K = 0$ and $K = 1$ are spaced very closely in frequency and therefore often appear as just one line. The observational data also contain higher $K$-components, but they are weak and sometimes blended with other species. Spectra of the $J = 13-12$ and $J = 14-13$ transitions can be found in Figs. B.2 and B.3. The $K = 3$ component, i.e., the line with the fourth highest transition frequency, was used to determine the zeroth-order moment maps discussed in Sect. 6.1 and presented in Fig. 6. The intensity of this line is relatively high because the $K = 3$ state belongs to the ortho-configuration of CH$_3$CN with a higher statistical weight.

The intensity of the simulated lines is in agreement with the observational spectra. The agreement is very good for the first $K$-components up to $K = 3$ and decreases for higher components. However, it is important to point out that the deviations between observational and simulated data are partly caused by line blending. Line blending describes the possibility that spectral lines undergo interference from lines of other molecular species or unidentified features and causes a major difficulty in analyzing and comparing the intensities and widths of observed
Fig. 6. Integrated intensity maps (or zeroth-order moment maps) of the observational (left column) and simulated (middle column) data for the CH$_3$CN $J = 12–11$, $K = 3$ transition. The right panels show the difference between the observational and the simulated data. The center row shows the entire Sgr B2(M) complex except for the central region, which is masked out with a transparent hatched area. The green and magenta boxes indicate the zoomed-in regions that are depicted in the top row (northern part of Sgr B2(M)) and the bottom row (southern part of Sgr B2(M)). As in previous figures, the black numbers indicate the position of the dust cores, whereas the green and magenta crosses depict the positions of the molecular centers (see Table A.1).

Spectral lines. Sgr B2 exhibits an extraordinarily rich chemistry and is composed of various kinds of molecules. As a consequence, the number of detectable species and spectral lines is large and some of the CH$_3$CN lines are indeed blended by other lines. For example, the $K = 5$ component is strongly blended by two spectral features, one of them brighter than the CH$_3$CN transition itself. For this reason the intensity of this component in the simulated data is usually smaller when compared to the observational data. The $K = 4$ transition is also blended with at least another strong line, but not as drastic as the $K = 5$ component. The significance of the line blending effects also depends on the position of the map. At locations close to the center of Sgr B2(M), e.g., the center of the molecular center MC-7a, the line blending effects are very strong due to the high line density. The spectrum of the molecular center MC-7a shows that at this position the intensity does not return to the continuum level between the individual lines. In contrast, at positions farther away from the dense center, e.g., core M-SMA-12, the individual lines are more isolated and line blending effects are less significant. Taking the blending into account would require detailed
Fig. 7. Radial profiles of the integrated line intensity for the CH$_3$CN $J = 12-11$, $K = 3$ transition. The radial profiles proceed from west to east and $r = 0$ corresponds to the center of the considered molecular centers. The first two profiles (MC-4 and MC-11) are taken from the newly introduced molecular centers in the northern region (cf. Fig. 4). The third profile (MC-68) is taken from the molecular center located between the continuum cores M-SMA-6 and M-SMA-8. The last profile (MC-9) is centered around the molecular center south to the continuum core M-SMA-9. In all panels the blue dashed line shows the observational data, whereas the red solid line corresponds to the simulated data.

Two molecules, among others, that blend with the $J = 12-11$ transition are HNCO and SO$_2$. The $J = 10-9$, $K_a = 1$, $K_c = 9-8$ transition of HNCO has a rest frequency of 220.58475 GHz. This strong line is located very close to the $J = 12-11$, $K = 6$ transition with 220.593987 GHz and causes significant line blending due to its higher intensity. SO$_2$ has two transitions at 220.59714 GHz and 220.618499 GHz. The latter could be the origin of the line detected between the $K = 6$ and $K = 5$ transitions of CH$_3$CN. Instead, CH$_3$NH$_2$ has three transitions, which are detected at rest frequencies of 220.76060, 220.78077, and 220.80552 GHz. The blending lines were identified using the software package XCLASS (Möller et al. 2017), which makes use of the CDMS and JPL catalogues. A full identification of the molecular content in the Sgr B2(M) will be presented in a forthcoming paper (Möller et al. in prep).

Nonetheless, there are also $K$-components that are not affected significantly by line blending (e.g., $K = 4$), but whose line intensity is still underestimated by the model. This indicates that the gas temperature, which is assumed to be equal to the dust temperature, is too low and therefore the higher $K$-transitions, which exhibit higher energies, are underpopulated. A detailed discussion of the temperature distribution and the possible reasons for the discrepancy is presented in Sect. 6.3.

Moreover, the spectra emphasize that although the continuum emission is brighter at the position of the continuum cores than at the newly introduced molecular centers, the continuum-subtracted line emission is much stronger at the position of the molecular centers. This can be seen by comparing the spectra towards the molecular center MC-9 and the close dust core M-SMA-9. Also noticeable are the spectra from M-SMA-10 and MC-10, which are very close in space. These regions have relatively small line widths, but the lines exhibit extended wings, which could be related to the presence of a high-velocity outflow.

Finally, there is a qualitative difference between spectra from the northern and the southern regions of Sgr B2(M). The spectra
from the southern region only show emission features, whereas the northern regions have a combination of emission and absorption features. The absorptions, which are overestimated by the model, are likely to be produced by the presence of H\textsc{ii} regions where more H\textsc{ii} gas is present. A previous study of the CH\textsubscript{3}CN abundance in Sgr B2(M) at the \(z=0\) plane is shown in Fig. 8. The temperature ranges from around 50 to 900 K, with the hottest regions located at the position of the continuum cores. The spherical structure in the right lower corner of the southern part is associated with an H\textsc{ii} region. A comparison of Figs. 5 and 8 shows that the hot temperature regions coincide with the continuum cores where the relative abundance of CH\textsubscript{3}CN is relatively low.

In Sect. 6.2, we compared the observational and simulated results of the \(J=12-11\) transition. For most of the lines there is a good agreement between simulation and observation, although the higher \(K\)-transitions are underestimated in some cases. This is partly caused by line blending, so that the line intensities appear to be stronger. However, there are also \(K\)-transitions that are apparently unaffected by line blending but nonetheless show an underestimated intensity. This may suggest that the gas temperature in the model is too low. As described in Sect. 4, the temperature is calculated based on the stellar luminosity, and it does not include a possible contribution from accretion events. Furthermore, the gas temperature can also be increased by other heating mechanisms, for example with a mechanical origin such as turbulent dissipation or outflow shocks that are not included in the model, or local X-rays which are not considered at all. For this reason, the temperature distribution should be regarded as a lower limit for the gas temperature. Another possibility for the overestimation of the excitation is that it is affected by radiative pumping from external dust radiation, which might involve the vibrationally excited level (e.g., Hauschildt et al. 1993). This effect can produce deviations from LTE if the radiation temperature differs from the local gas kinetic temperature, even if the latter is coupled to the local dust temperature.

The states involved in the transitions considered in Sect. 6.2 have energies in the range from approximately 60 to 325 K, so that most of the states have relatively low energies. In order to investigate the validity of the temperature distribution, we have also analyzed higher energy transitions from the CH\textsubscript{3}CN vibrationally excited state \(v_8 = 1\). In particular, the transition \(v_8 = 1, J = 12-11, K = 1 - (-1)\), with a rest frequency of 221.62582 GHz. The involved states have energies of 577 K and 588 K and hence primarily trace the hot gas. Figure 9 shows observational spectra as well as the prediction by our model for the vibrationally excited transition. Further spectra are shown in Fig. B.4. At the center of most cores and molecular centers the vibrationally excited transition is clearly detected. However, there are also regions where the transition is hardly visible, e.g., core M-SMA-12. In most cases the intensity of the transition is only slightly underestimated by our model (see, e.g., cores M-SMA-4 and M-SMA-9), indicating that the calculated temperature is consistent with the observations. However, other regions like cores M-SMA-6 and M-SMA-8 have observed lines for the vibrationally excited transition that are brighter than predicted by the model.

In order to investigate how much the gas temperature is underestimated, we produce different models in which the gas temperature is increased compared to the dust temperature. The results of these tests are shown in Fig. 9 for cores M-SMA-6 and M-SMA-8. The figures show the spectra of the vibrationally excited transition for the temperature calculated by RADMC-3D and for two runs where the gas temperature was increased by 50 GHz and 150 K. While the simulated intensities using the dust temperature as the gas temperature are below the observed intensities, the intensity of the lines in the simulated data is in good agreement for both cores when considering an increase of 150 K in the gas temperature. This suggests that the gas temperature is not coupled to the dust temperature and should be higher in some regions, although it is not drastically underestimated.

### 6.4. CH\textsubscript{3}CN abundance

In this section we discuss the abundance distribution of CH\textsubscript{3}CN in Sgr B2(M). The relative abundance of CH\textsubscript{3}CN varies by three orders of magnitude within the northern and the southern regions of Sgr B2(M). A histogram of the pixel distribution of the relative abundance (CH\textsubscript{3}CN with respect to H\textsubscript{2}) can be seen in Fig. 10. For the northern region the relative abundance ranges from \(4 \times 10^{-11}\) to \(2 \times 10^{-8}\) with an average value of \(1.1 \times 10^{-9}\). In the southern region the relative abundance ranges from \(2 \times 10^{-10}\) to \(5 \times 10^{-7}\) with an average value of \(9.0 \times 10^{-8}\). The histogram illustrates that the abundance of CH\textsubscript{3}CN is significantly higher in the southern region than in the northern region. This may be related to the stronger feedback destroying CH\textsubscript{3}CN in the northern regions where more H\textsc{ii} regions are present. A previous study of the CH\textsubscript{3}CN emission in Sgr B2 derive an average abundance for the hot cores of \(\sim 7 \times 10^{-11}\) (de Vicente et al. 1997), which is much lower than our estimated value. However, the
Fig. 9. Spectra of the vibrationally excited transition \( \nu_8 = 1, J = 12-11, K = 1 - (-1) \) taken from the center of different cores. The blue solid line shows the observational data, while the red solid lines show the simulated data when the gas temperature equals the dust temperature. The bottom panels also show the simulated spectra after modifying the gas temperature by 50 K (green) and 150 GHz (yellow), as discussed in Sect. 6.3. The continuum correction necessary to match the continuum level of the observation and simulation is indicated in the top right corner of each panel.

 angular resolution of the observations by de Vicente et al. (1997) (~10–30") is coarser and most likely smears out the CH_{3}CN emission associated with small-scale structures that are resolved in our data (with a resolution of 0.7)

In Fig. 5 we can see an anti-correlation between the CH_{3}CN abundance and the position of the dense cores with large H_{2} densities. The anti-correlation between H_{2} and CH_{3}CN can be seen more clearly in Fig. 11, where we show the relation between the relative abundance of CH_{3}CN as a function of the H_{2} density. The relative abundance of CH_{3}CN decreases with increasing density according to a power law with an exponent of −0.92. We find a similar behavior for the CH_{3}CN abundance as a function of the temperature (see Fig. 12). In the figure we show how the relative CH_{3}CN abundance decreases with increasing temperature. The relative CH_{3}CN abundance is high in regions with temperatures around 150–250 K, and decreases by one or two orders of magnitude for temperatures in the range 300–500 K.

All this together suggests the existence of chemical processes in the dense regions that lead to the destruction of CH_{3}CN. Although this needs further investigation, which will be done in forthcoming papers using chemical models, we indicate some aspects that may help to understand the anti-correlations shown in Figs. 11 and 12. First, the temperature itself has an important impact on the chemistry because it determines the efficiency of chemical reactions especially on the dust grains. Second, the radiation field of the stars, which are evolving inside the dense cores, affects the chemistry by photo-dissociation reactions and ionizations and might reduce the abundance of CH_{3}CN at the central part of these cores. Chemical models that investigated the chemistry of nitrogen-bearing molecules including CH_{3}CN were conducted by Rodgers & Charnley (2001). In their models they assumed a density of 10^{7} H_{2} cm^{-3} and constant temperatures in the range of 100–300 K. Additionally, they considered different ice compositions. Depending on the time evolution, they find abundance values of CH_{3}CN ranging from 10^{-9} to 10^{-7} for a temperature of 300 K. We find an averaged abundance of roughly 3 \times 10^{-9} at 300 K, which in their model would correspond to a time of 2 \times 10^{4} yr. For a temperature of 100 K they find significantly lower abundance values ranging from 10^{-9} to only 10^{-8}. In contrast to our results, which show a decreasing CH_{3}CN abundance with increasing temperature, their results seem to show an opposite behavior. However, in these models they do not take into account photo-dissociation reactions. If these reactions are included, they point out that the abundance of CH_{3}CN drops by a factor of 100 after 5 \times 10^{8} yr, even if only cosmic-ray-induced photo-dissociation is included. Their results show that CH_{3}CN can be destroyed effectively by photo-dissociation
Fig. 10. Histogram of the distribution of the relative abundance of CH$_3$CN for the northern (red) and southern (blue) region of Sgr B2(M). For this purpose cubes were placed around the northern and southern parts, which were composed of cells with side lengths of 695 AU. The vertical lines indicate the averaged values.

Fig. 11. Histogram of the relative abundance of CH$_3$CN as function of the H$_2$ density based on the developed physical model. The CH$_3$CN abundances decrease with the H$_2$ density with a function that can be described as a power law with an exponent of $-0.92$.

Fig. 12. Histogram of the relative abundance of CH$_3$CN as function of the temperature.

reactions. Hence, as many continuum cores in Sgr B2(M) already contain evolving stars that have a radiation field, this could be the reason for the low abundance of CH$_3$CN at the center of these cores. In the future it will be interesting to investigate if chemical models of hot cores with the parameters (e.g., density, radiation field) like those found towards the cores of Sgr B2(M) can reproduce the radial distribution of CH$_3$CN.

6.5. Core velocities and turbulent line width

The analysis of spectral lines not only provides information about the temperature and the density of certain molecular species, but also provides information about the velocity structure of a cloud and its internal turbulent motion. The component of the velocity along the line of sight of individual cores can be obtained by the shift of the spectral line away from the rest frequency due to the Doppler effect. Information about the internal turbulent motion can be obtained by analyzing the line shape of spectral lines.

The spectra shown in Fig. 13 show the difference in velocity for the emission in different cores. For a northern core like N-SMA-12 (left panel) the lines are clearly shifted to high frequencies (i.e., blue-shifted) with respect to the rest frequency. On the contrary, a southern core like M-SMA-6 has the lines shifted towards lower frequencies (i.e., red-shifted). The different velocities of the cores can be seen in the values listed in Table A.1. Figure 14 shows a velocity (along the line of sight) map of the CH$_3$CN emission in Sgr B2(M) as obtained from the model. Southern regions are clearly red-shifted with respect to the northern regions. This suggests an overall velocity gradient from north (blue-shifted velocities around 50 km s$^{-1}$) to the south (red-shifted velocities around 70 km s$^{-1}$).

The width of a spectral line is determined by the thermal broadening, together with non-thermal motions such as turbulence and global scale motions unresolved in our beam size. The line width $\sigma_{\text{linewidth}}$ as calculated by RADMC-3D in Pandora includes a turbulent and a thermal component as

$$\sigma^2_{\text{linewidth}} = \sigma^2_{\text{turb}} + \frac{2kT_{\text{gas}}}{\mu m_{\text{H}}},$$

where $\sigma_{\text{turb}}$ is the (micro)turbulent line width, $T_{\text{gas}}$ the gas temperature, $k$ the Boltzmann constant, $\mu$ the mean molecular weight, and $m_{\text{H}}$ the mass of a hydrogen atom. In our model of Sgr B2(M) we find differences in the turbulent line width between the northern and southern regions. From the depicted spectra in Fig. 13 (see also Fig. 1) the northern cores (e.g., core N-SMA-12) have a narrower line width compared to the southern cores (e.g., core N-SMA-6). All southern cores and molecular centers are modeled with a turbulent line width of 5 km s$^{-1}$, except for M-SMA-10 and MC-10 for which we used 2.5 km s$^{-1}$. In contrast, all the northern cores and molecular centers (MC-4, MC-11, M-SMA-4, M-SMA-11, M-SMA-12) exhibit a turbulent line width of only 2.5 km s$^{-1}$. The central region exhibits broad line widths similar to the southern region. This indicates that the internal turbulent motions are larger in the southern and central regions of Sgr B2(M) compared to the northern region.

6.6. CH$_3$CN features at the central region

So far we have only presented the simulated and observational data from the northern and southern regions of Sgr B2(M) as selected in Fig. 6, which show CH$_3$CN spectral features in emission with the exception of only a few cases. The central

Fig. 13. Spectra taken from a northern (M-SMA-12) and a southern (M-SMA-6) core to illustrate the shift in frequency due to the velocity component along the line of sight. The green, dashed vertical lines indicate the rest frequency of the $J = 12-11$, $K = 0$ transition. The core M-SMA-12 exhibits a blue-shifted velocity along the line of sight of 50 km s$^{-1}$, while core M-SMA-6 has a red-shifted velocity of 67 km s$^{-1}$. The systemic velocity of Sgr B2(M) is about 64 km s$^{-1}$.

Fig. 14. Distribution of the velocity along the line of sight at the $z = 0$ plane, as derived from the model of Sgr B2(M). The central region is masked out by a transparent, hatched area. The black numbers and green crosses indicate the dense cores and molecular centers, respectively, as in Fig. 4.

region exhibits much more complex features of CH$_3$CN. Spectra taken from the center of cores, which are located in the central region of Sgr B2(M), are presented in Fig. B.5 and exhibit a combination of emission and absorption features.

The reason for these complex spectra is that the continuum emission is very strong at the center of Sgr B2(M). As a consequence, the CH$_3$CN between the observer and the sources leads to deep absorption features in the spectra. Because many H II regions are present in the center of Sgr B2(M), one might think that they are the reason for the deep absorption features. However, the positions of the known H II regions do not entirely coincide with the spatial extent of the observed absorption lines, indicating instead that the dust emission is the cause (see Fig. 2).

As already mentioned, the physical model presented in this paper is not able to reproduce the complex spectra at the center of Sgr B2(M). We investigated various modifications to the model in order to retrieve the behavior at the center, but could not find a model that reproduces all the features of the CH$_3$CN transitions. Nonetheless, we give an overview of these models and briefly discuss where they failed to reproduce the observed features.

First, we tried to reproduce the absorption features by including the large-scale envelope surrounding Sgr B2(M). In addition to the small-scale structure of Sgr B2(M), the physical model developed in Paper I also includes an envelope surrounding Sgr B2(M) with an extent of $\sim 10^4-10^5$ au and densities of $\sim 10^5-10^6$ cm$^{-3}$. One indication that the absorption is caused by CH$_3$CN located in the larger scale structure (where temperatures are much lower) is that in the vibrationally excited transition (which have very high energies) we see almost no absorption features (see Fig. B.5). By defining an abundance factor of CH$_3$CN for the envelope of $10^{-7}$ and a velocity along the line of sight of 44 km s$^{-1}$, we were able to reproduce the deep absorption features at the center (see Fig. 15). However, the model with a CH$_3$CN abundance of $10^{-7}$ in the envelope also produces absorption features in the northern and southern regions of Sgr B2(M) where no deep absorption features are observed. This is likely due to the spatial extent of the envelope, which does not cover only the central region of Sgr B2(M) but rather the entire complex. As a consequence, the CH$_3$CN in the envelope causes absorption features towards the center and also in the northern and southern regions, even though the continuum emission in those regions is much weaker (see Fig. 15).

With the knowledge that the absorption is not caused by the gas in the small-scale structure, but by the gas located farther out, we investigate a model with a shell of enhanced CH$_3$CN density surrounding the central part of Sgr B2(M). We consider a shell with an extent of 5000 au, which only covers the central part but not the northern and southern regions of Sgr B2(M). This prevents the model from producing absorption features at these regions. However, the spectra towards the central positions show emission and no clear sign of absorption. In order to evaluate the origin of this effect we used the software package XCLASS (Möller et al. 2017) to fit the spectrum towards the center of
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Fig. 15. Spectra of the model after including the large-scale envelope with a CH$_3$CN abundance of $10^{-7}$. The left panel shows a spectrum towards the center where absorption features associated with the low-$K$ transitions are reproduced. The right panel shows a spectrum towards the southern location MC-68. This model predicts absorptions for the low-$K$ transitions that are not visible in the observational data.

Fig. 16. Comparison of the CH$_3$CN $J = 12-11$ observational spectrum (in black) towards a central position in Sgr B2(M) and a fit (in red) obtained with the software package XCLASS. The best fit is obtained for a temperature range $\sim 100-150$ K and a column density of $2.9 \times 10^{14}$ cm$^{-2}$.

Fig. 17. Distribution of the dust temperature relative to the center of the model along the line of sight. The plane $z = 0$ has a temperature of about 700 K, while temperatures of $\sim 100-150$ K are found at a distance of $\sim 20000$ au.

6.7. Isotopologue $^{13}$CH$_3$CN

The spectral line survey contains transitions of the isotopologues of CH$_3$CN. We consider the isotopologue in which one of the carbon atoms $^{12}$C is exchanged by the isotope $^{13}$C. Due to the increased mass of the isotopologue it also possess a larger moment of inertia, which results in a shift of the energy levels.

Sgr B2(M) and determine the temperature of the absorption layer. The best fit of the absorbing CH$_3$CN is obtained for a temperature in the range $\sim 100-150$ K. In XLASS a model with a Gaussian-like density distribution centered around 5000 au, a temperature between $\sim 100$ and 150 K, and a column density of $2.9 \times 10^{14}$ cm$^{-2}$ can reproduce the deep absorption features towards the central region (see Fig. 16). The temperature distribution calculated in our model (obtained self-consistently by RADMC-3D) along the line of sight at the center (see Fig. 17) shows that the temperature range of $\sim 100-150$ K is reached at a distance of $\sim 20000$ au, whereas a shell at 5000 au would have a temperature of $\sim 300-400$ K, and therefore would still lead to emission features rather than absorption. For this reason the model with a shell of increased CH$_3$CN abundance does not lead to absorption when using the temperature distribution of RADMC-3D.

All this suggests that the gas temperature distribution predicted by the model may differ in the central part of Sgr B2(M) with respect to the real distribution. In this sense, the analysis of the ALMA continuum images (see Paper II) revealed a number of continuum sources not included in the original physical model (Paper I), which might have an impact on the temperature distribution. An update of the continuum model using the ALMA data presented in Paper II and new ALMA data at lower frequencies (80–150 GHz) is planned in a forthcoming paper. Moreover, we also have to be aware that in all the described models the CH$_3$CN density field is constructed based on spherically symmetric Plummer-like clumps. Hence, the effects of deviations from this spherical symmetry, like elongated structures along the line of sight, may help to explain the observed absorption features since higher column densities can be reached at regions where the temperature is favorable for absorption.
Fig. 18. Integrated intensity maps (or zeroth-order moment maps) of the observational (left column) and simulated (middle column) data for the CH$_3$CN $J = 13-12$, $K = 0, 1$ transitions of the isotopologue $^{13}$CH$_3$CN. The panels in the right column show the difference between the observational and the simulated data. The central row shows the entire Sgr B2(M) complex except for the central region, which is masked out with a transparent, hatched area. The green and magenta boxes indicate the zoomed-in regions that are depicted in the top row (northern part of Sgr B2(M)) and the bottom row (southern part of Sgr B2(M)). As in the previous figures, the black numbers indicate the position of the dust cores, whereas the green and magenta crosses depict the position of the molecular centers (see Table A.1).

For this reason, the isotopologues exhibit transition frequencies which are different from the main isotopologue. Because the moment of inertia also depends on the position of the $^{13}$C atom, the two isotopologues $^{13}$CH$_3$CN and CH$_3^{13}$CN also have different transition frequencies. The isotopologue CH$_3^{13}$CN exhibits transitions that are very close to the main isotopologue and therefore they are strongly blended, whereas the isotopologue $^{13}$CH$_3$CN emits at frequency ranges different from the main isotopologue. For this reason, we considered $^{13}$CH$_3$CN in order to study the isotope ratio.

Spectra of $^{13}$CH$_3$CN taken from the center of the cores and molecular centers of Sgr B2(M) are shown in Fig. B.6. Zeroth-order moment maps comparing the observational data and simulated data of the isotopologue are shown in Fig. 18. From the observational maps it is evident that although the emission of the isotopologue does not show exactly the same morphology as the main isotopologue, the emission does coincide with the positions of the newly introduced molecular centers. This indicates that the abundance is in fact enhanced in those regions and the morphology is not caused by opacity effects.
We used an isotopologue ratio of $^{12}$CH$_3$CN/$^{13}$CH$_3$CN = 20 in order to obtain a fit of the isotopologue transitions. The images in Fig. 18 illustrate that the model reproduces the general morphology of the emission. Nonetheless, there are some differences. In the northern region the strong emission peak in the east is underestimated by the model and it is slightly shifted to the north. In the southern part the strong emission towards MC-7a and M-SMA-7 is considerably underestimated by the model, whereas the emission at core MC-7b is overestimated. Moreover, the spectra depicted in Fig. B.6 in Appendix show that at some cores and molecular centers (e.g., MC-68, M-SMA-7, M-SMA-6, M-SMA-7a) the emission is slightly underestimated. In order to reproduce the strong emission at these regions, it is necessary to decrease the isotopologue ratio for these cores considerably. However, studies of the isotopic ratio $^{13}$CH$_3$CN at the Galactic center determined values of ~20 (Wilson & Rood 1994). Furthermore, the isotopologue ratio of 20 used in the model gives good results when comparing the emission in the other regions of Sgr B2(M), and therefore it would be necessary to introduce an isotopologue ratio that varies within Sgr B2(M) in order to fit all cores and molecular centers.

7. Summary and outlook

In this paper we present ALMA observations of different CH$_3$CN transitions in the range 211–275 GHz (see details on the observations in Paper II) towards the hot molecular core Sgr B2(M). The achieved angular resolution of 0′′.7 (or ~6000 au) permitted us to study the structure of the CH$_3$CN emission at scales not previously studied before. We modeled the CH$_3$CN emission using a three-dimensional radiative transfer model (presented in Paper I) that contains the physical structure (i.e., distribution of dense cores, H II regions, stars) of Sgr B2(M). We reconstructed the abundance field of CH$_3$CN towards Sgr B2(M), and studied the velocity and line width variations in the region. Our main results are listed in the following:

- We derive an average relative abundance of CH$_3$CN with respect to H$_2$ of 1.1 × 10$^{-9}$, covering a range from 4 × 10$^{-11}$ to 2 × 10$^{-8}$, towards the north of Sgr B2(M) and an abundance of 9 × 10$^{-9}$, covering a range from 2 × 10$^{-10}$ to 5 × 10$^{-7}$, towards the south.
- We find that the CH$_3$CN relative abundance is lower at the center of the very dense and hot continuum cores, causing the general morphology of the CH$_3$CN emission to not completely coincide with the dust continuum emission.
- The spectral features of the CH$_3$CN transitions (e.g., line intensity, line width) are reproduced well by the model; however, and especially in the southern region of Sgr B2(M), the higher K-transitions and the vibrationally excited transition are underestimated. This indicates that the gas temperature is higher than the dust temperature or that radiative pumping plays a role.
- The velocity component along the line of sight varies from 67 km s$^{-1}$ (towards the south) to 50 km s$^{-1}$ (towards the north), where the systemic velocity of the cloud is about 64 km s$^{-1}$.
- The central region of Sgr B2(M) exhibits complex CH$_3$CN spectra with a combination of absorption and emission features. We study whether the absorption features are related to the presence of H II regions, but conclude that their origin is the presence of bright dust, which at this high angular resolution reaches a high brightness temperature (about 180 K) and produces the absorption features. Despite different attempts to model this region, our current model does not produce accurate results for all the CH$_3$CN transitions. We suggest that the calculated temperature distribution deviates from the real distribution towards the center or that the assumed spherical symmetry of the dense cores included in the model may be not accurate enough.

Modeling the emission of CH$_3$CN for Sgr B2(M) raised some interesting questions, which deserve further investigation in the future. Some of them are listed in the following:

- Can chemical models of hot molecular cores reproduce the low relative CH$_3$CN abundance found towards the densest and hottest regions of the cores in Sgr B2(M)? In this sense, it is worth studying in more detail which chemical processes are crucial in the destruction of CH$_3$CN.
- The velocity field determined from CH$_3$CN needs to be compared with the velocity field of other molecular tracers (e.g., SiO which traces outflow and shocked gas) and recombination lines (which trace the motions of the ionized gas) in order to study the origin of the velocity gradient from north to south observed in the dense gas.
- Can a better determination of the continuum model or the inclusion of non-spherical symmetric structure reproduce the absorption and emission spectral line features observed towards the central region of Sgr B2(M)? Further investigations and an ongoing improvement of the model may help to better constrain the physical properties of this central region.
- Extending the model of CH$_3$CN to the northern hot core of Sgr B2, i.e., Sgr B2(N), will be more challenging (due to the higher density of spectral line features), but will allow us to compare the properties derived in two distinct but close high-mass star-forming sites: Sgr B2(M) being more evolved and less dense than Sgr B2(N).

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References

Appendix A: Parameters of the cores and molecular centers of the model of Sgr B2(M)

In Table A.1 we list the cores included in the model of Sgr B2(M). The first columns reproduce the dust continuum emission and correspond to the cores introduced in the physical model presented in Paper I. The second list of cores correspond to the molecular centers introduced to reproduce the extension of the CH$_3$CN emission.

Table A.1. Parameters of the cores and molecular centers of the model of Sgr B2(M).

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<th>Dec (J2000)</th>
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<th>$n_2$ (CH$_3$CN cm$^{-3}$)</th>
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Molecular centers included in the model, this work

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Notes. ID: identifier of the cores used in the model. RA: right ascension of the density component given in units of hours:minutes:seconds in the equatorial coordinate system. Dec: declination of the density component given in units of degrees:arcminutes:arcseconds in the equatorial coordinate system. dz: displacement along the line of sight with respect to the model center. The z-axis is oriented such that it points towards the observer. $r_0$: radius defining the density profile as described in Eq. (3). $\eta$: exponent of the density profile. $n_1$: central density of H$_2$. $n_2$: central density of CH$_3$CN. $v_z$: velocity component along the line of sight. Star: this columns indicates whether an additional star was included at the center of the core. If this is the case, the spectral type of the star is given.
Appendix B: Observed and simulated spectra

In Figs. B.1–B.6 we show the observed (in blue) and the simulated (in red) spectra of the different CH$_3$CN, $^{13}$CH$_3$CN, and vibrationally excited states towards the different dense cores and molecular centers included in the model (see Table A.1).

Fig. B.1. Spectra of the observational (in blue) and simulated (in red) data extracted from the position of different cores and molecular centers for the CH$_3$CN $J = 12$–11 transition. The spectra are arranged according to the position of the corresponding cores and molecular centers along a south–north direction, starting from the most southern core. The name of the core and molecular center is shown for each panel. The continuum correction necessary to match the continuum level of the observation and simulation is indicated in the top right corner of each panel.
Fig. B.1. continued
Fig. B.2. Spectra of the observational (in blue) and simulated (in red) data extracted from the position of different cores and molecular centers for the CH$_3$CN $J = 13-12$ transition. The spectra are arranged according to the position of the corresponding cores and molecular centers along a south–north direction, starting from the most southern core. The name of the core and molecular center is shown for each panel. The continuum correction necessary to match the continuum level of the observation and simulation is indicated in the top right corner of each panel.
Fig. B.2. continued
Fig. B.3. Spectra of the observational (in blue) and simulated (in red) data extracted from the position of different cores and molecular centers for the CH$_3$CN $J = 14$–13 transition. The spectra are arranged according to the position of the corresponding cores and molecular centers along a south–north direction, starting from the most southern core. The name of the core and molecular center is shown for each panel. The continuum correction necessary to match the continuum level of the observation and simulation is indicated in the top right corner of each panel.
Fig. B.3, continued
Fig. B.4. Spectra of the observational (in blue) and simulated (in red) data extracted from the position of different cores and molecular centers for the vibrationally excited transition $\text{CH}_3\text{CN} \nu_8 = 1, J = 12 \rightarrow 11, K = 1 \rightarrow (-1)$. The spectra are arranged according to the position of the corresponding cores and molecular centers along a south–north direction, starting from the most southern core. The name of the core and molecular center is shown for each panel. The continuum correction necessary to match the continuum level of the observation and simulation is indicated in the top right corner of each panel.
Fig. B.4. continued
Fig. B.5. Observational spectra (in black) of the ground state CH$_3$CN $J = 12-11$ transition towards the cores located in the central region of Sgr B2(M). The continuum level for core M-SMA-1a is about 60 K, for core M-SMA-1b about 150 K, and for the remaining cores about 100 K. A number of absorption and emission spectral line features are visible in all the spectra.
Fig. B.6. Spectra of the observational (in blue) and simulated (in red) data extracted from the position of different cores and molecular centers for the $^{13}$CH$_3$CN $J = 13–12$ transition. The spectra are arranged according to the position of the corresponding cores and molecular centers along a south–north direction, starting from the most southern core. The name of the core and molecular center is shown for each panel. The continuum correction necessary to match the continuum level of the observation and simulation is indicated in the top right corner of each panel.
Fig. B.6. continued