

Dust arcs in the region of Jupiter's Trojan asteroids

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ABSTRACT

Aims. The surfaces of the Trojan asteroids are steadily bombarded by interplanetary micrometeoroids, which releases ejecta of small dust particles. These particles form the faint dust arcs that are associated with asteroid clouds. Here we analyze the particle dynamics and structure of the arc in the region of the L_4 Trojan asteroids.

Methods. We calculate the total cross section of the L_4 Trojan asteroids and the production rate of dust particles. The motion of the particles is perturbed by a variety of forces. We simulate the dynamical evolution of the dust particles, and explore the overall features of the Trojan dust arc.

Results. The simulations show that the arc is mainly composed of grains in the size range 4–10 microns. Compared to the L_4 Trojan asteroids, the dust arc is distributed more widely in the azimuthal direction, extending to a range of [30, 120] degrees relative to Jupiter. The peak number density does not develop at L_4 . There exist two peaks that are azimuthally displaced from L_4 .

Key words. meteorites, meteors, meteoroids – planets and satellites: rings – minor planets, asteroids: general – zodiacal dust – celestial mechanics – solar wind

1. Introduction

The study of the Trojan asteroids is a classical problem of celestial mechanics and astronomy, but it is also a hot topic of recent research and future space exploration (see review papers by Emery et al. 2015; Robutel & Souchay 2010; Dotto et al. 2008; Jewitt et al. 2004, and references therein). In 2021, the NASA mission *Lucy* will explore the Trojan asteroids in a sequence of flybys. In this paper, we focus on the dynamical evolution of dust expelled from the Trojans. Dust carries information about the composition of its source, which gives important constraints on the origin and formation of the Trojan group of asteroids. Several papers studied the dynamics of dust in the Trojan region (Liou & Zook 1995; Liou et al. 1995; Zimmer & Grogan 2014; de Elía & Brunini 2010). However, the configuration of the dust distribution associated with the Trojan asteroids is still unclear to date. In this work, we answer this question through computer simulations of the long-term evolution of dust particles. The simulations are performed on a large computer cluster.

2. Production rate of dust particles

We use the size distribution of the L_4 Trojans published by Fernández et al. (2009) to estimate the total cross section of the Trojan asteroids. This is necessary to derive the production rate of dust particles. The distribution is modified from the distribution derived by Jewitt et al. (2000) by taking into account the systematic dependence of the albedo on asteroid size that has been inferred by Fernández et al. (2009). Although this correlation was not confirmed in the much larger data set from WISE (Grav et al. 2011, 2012), we continue to use the size distribution from Fernández et al. (2009, use their Fig. 6) because it is calibrated to absolute numbers in the same way as the result

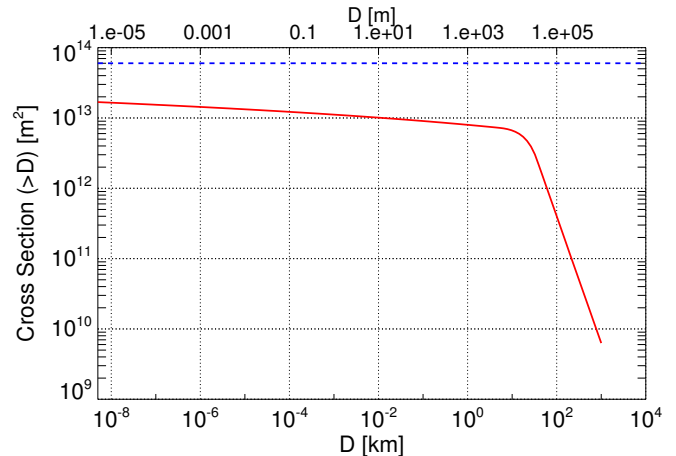


Fig. 1. Total cross section of the L_4 Trojan asteroids (red line). The blue dashed line denotes the upper limit of $6 \times 10^{13} \text{ m}^2$ for the cross section of L_5 Trojan asteroids that are larger than $10 \mu\text{m}$ in radius, as inferred by Kuchner et al. (2000).

by Jewitt et al. (2000) and because the potential bias, if any, is small. The total asteroid cross section is obtained from the second moment of the distribution (Fig. 1). This second moment has a logarithmic divergence toward small asteroid sizes, but for practical purposes, this is not a problem because the change in total cross section is very mild even when we vary the lower cut-off asteroid size from $10 \mu\text{m}$ to 100 km. For our modeling we use a value of 10^{13} m^2 .

To estimate the production rate of dust ejected from the surfaces of the Trojan asteroids by impacts of interplanetary micrometeoroids, we follow the procedure by Krivov et al. (2003).

By normalizing the differential distribution of ejecta particle masses to the total mass production rate M^+ , we obtain

$$p(m) = M^+ \frac{1 - \alpha}{m_{\max}^{1-\alpha} - m_{\min}^{1-\alpha}} m^{-(1+\alpha)}, \quad (1)$$

where m_{\max} and m_{\min} denote the highest and lowest mass of an ejected particle. The exponent α is the slope of the cumulative production rate with a plausible range $0.5 < \alpha < 1$. Here we use the value

$$\alpha = 0.91, \quad (2)$$

which was inferred from measurements on the Moon (Horányi et al. 2015) of the Lunar Dust Experiment dust detector (LDEX) on board the Lunar Atmosphere and Dust Environment Explorer (LADEE) mission.

It is practical to write Eq. (1) in the form

$$p(m) = \frac{1}{m_{\max}} \frac{M^+}{m_{\max}} \frac{1 - \alpha}{1 - \left(\frac{m_{\min}}{m_{\max}}\right)^{1-\alpha}} \left(\frac{m}{m_{\max}}\right)^{-(1+\alpha)}. \quad (3)$$

We frequently use particle radii r_g instead of mass m . From $p(m) dm = p(r_g) dr_g$, we obtain

$$p(r_g) = \frac{3}{r_{\max}} \frac{M^+}{m_{\max}} \frac{1 - \alpha}{1 - \left(\frac{m_{\min}}{m_{\max}}\right)^{1-\alpha}} \left(\frac{r_g}{r_{\max}}\right)^{-1-3\alpha}. \quad (4)$$

Here

$$r_{\min} = \left(\frac{3}{4\pi\rho_g} m_{\min}\right)^{1/3}, \quad r_{\max} = \left(\frac{3}{4\pi\rho_g} m_{\max}\right)^{1/3}, \quad (5)$$

where ρ_g is the grain density. We note that $p(m)$ and $p(r_g)$ are only defined for ejecta masses m with $m_{\min} < m < m_{\max}$.

For the cumulative production rate, we obtain from Eq. (4)

$$p(>r_{\min}) = \int_{r_{\min}}^{r_{\max}} dr_g p(r_g) = \frac{1 - \alpha}{\alpha} \frac{M^+}{m_{\max}} \frac{\left(\frac{r_{\min}}{r_{\max}}\right)^{-3\alpha} - 1}{1 - \left(\frac{r_{\min}}{r_{\max}}\right)^{3(1-\alpha)}}. \quad (6)$$

To proceed, we need to quantify the total mass production rate M^+ . We again follow Krivov et al. (2003) and express it as

$$M^+ = Y F_{\text{imp}} S, \quad (7)$$

where Y is the yield, and S is the total cross section of the target, that is, of all L_4 Trojans (Fig. 1). For the projectile mass flux F_{imp} , we use the value

$$F_{\text{imp}} = 10^{-15} \text{ kg m}^{-2} \text{ s}^{-1}, \quad (8)$$

which was derived by Krivov et al. (2003) from the Divine model (Divine 1993) of the interplanetary meteoroid population for a spherical target with a unit surface that is on a heliocentric circular orbit at the distance of Jupiter. For the Trojans, the effect of the gravitational focusing by a planet is not included. Newer models have been published (Poppe 2016), but we continued to use the number for the mass flux from the Divine model because this has led to a quantitative match with the measured ejecta clouds for the Galilean moons (Krüger et al. 2003), which are located at the same heliocentric distance as the Trojan asteroids.

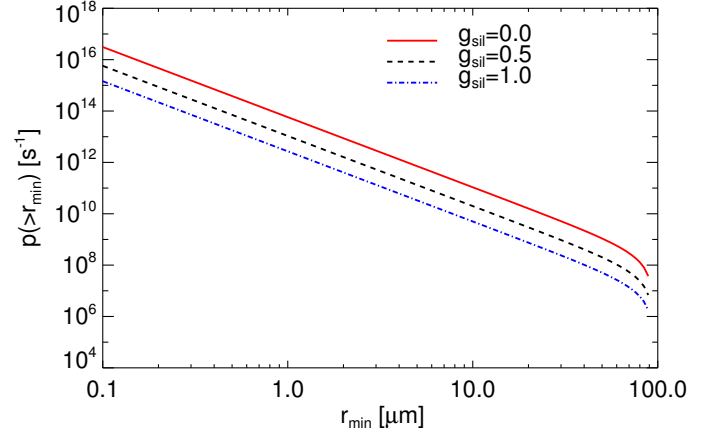


Fig. 2. Cumulative production rate of ejecta particles from Eq. (6). The parameter g_{sil} is the mixing ratio of silicate to ice of the target surface. The red, black, and blue lines denote the cumulative production rates for $g_{\text{sil}} = 0.0$, $g_{\text{sil}} = 0.5$, and $g_{\text{sil}} = 1.0$, respectively.

For a given impact velocity v_{imp} and projectile mass m_{imp} , the yield can be estimated from the empirical formula derived from laboratory experiments by Koschny & Grün (2001a,b),

$$Y = 2.85 \times 10^{-8} \times 0.0149^{g_{\text{sil}}} \times \left(\frac{1 - g_{\text{sil}}}{927} + \frac{g_{\text{sil}}}{2900}\right)^{-1} \times \left(\frac{m_{\text{imp}}}{\text{kg}}\right)^{0.23} \times \left(\frac{v_{\text{imp}}}{\text{m s}^{-1}}\right)^{2.46}, \quad (9)$$

where g_{sil} is the mixing ratio of silicate to ice of the target surface. Equation (9) assumes a density of 927 kg/m^3 for ice and a density of 2900 kg/m^3 for silicate (the original formula by Koschny & Grün (2001a,b) used a density of 2800 kg/m^3 for silicate). For $g_{\text{sil}} = 1$ we have a pure silicate surface and for $g_{\text{sil}} = 0$ we have pure ice. For our modeling we use

$$g_{\text{sil}} = 1, \quad (10)$$

because the asteroid surfaces are most probably silicate rich (even when the asteroid has a substantial interior ice fraction) and because $g_{\text{sil}} = 1$ leads to the smallest yields, which gives a lower bound for the particle number densities inferred from our model (Fig. 2).

For the typical projectile mass we use (Krivov et al. 2003)

$$m_{\text{imp}} = 10^{-8} \text{ kg}, \quad (11)$$

because this particle mass (corresponding roughly to a radius of $100 \mu\text{m}$) dominates the mass flux at the distance of Jupiter. The largest ejecta have a mass on the order of the projectile. Thus, we use

$$m_{\max} = m_{\text{imp}} = 10^{-8} \text{ kg}. \quad (12)$$

The precise choice of m_{\max} has no strong effects on our results because Eq. (1) depends only weakly on m_{\max} .

The average impact velocity

$$v_{\text{imp}} = 9 \text{ km s}^{-1}, \quad (13)$$

was also calculated by Krivov et al. (2003) from the Divine model evaluated at the distance of Jupiter.

3. Dynamical model

The motion of dust particles from the Jupiter Trojans is influenced by a variety of forces. The most important forces are solar gravity, solar radiation pressure, Poynting-Robertson drag, solar wind drag, the Lorentz force exerted by the interplanetary magnetic field, and gravitational perturbations from Jupiter and other planets (Venus, Earth, Mars, Saturn, Uranus, and Neptune). Our code integrates the equations of motion in the Jupiter orbital inertial frame $Oxyz$. Here, the z -axis is defined as the normal to the orbital plane of Jupiter at the J2000 epoch, and the x -axis is aligned with the intersection of the orbital plane and the equatorial plane of Jupiter at the J2000 epoch. The y -axis completes an orthogonal right-handed frame.

The equations of motion of a dust particle in the region of the Trojan asteroids read

$$\begin{aligned} \ddot{\mathbf{r}} = & -\frac{GM_S}{r^3}\mathbf{r} + \sum_{i=1}^7 GM_{P_i} \left(\frac{\mathbf{r}_{dP_i}}{r_{dP_i}^3} - \frac{\mathbf{r}_{P_i}}{r_{P_i}^3} \right) + \frac{Q}{m} (\dot{\mathbf{r}} - \mathbf{v}_{sw}) \times \mathbf{B} \\ & + \frac{3Q_S Q_{pr} AU^2}{4r^2 \rho_g r_g c} \left\{ \left[1 - (1 + sw) \frac{\dot{r}}{c} \right] \hat{\mathbf{r}} - (1 + sw) \frac{\dot{\mathbf{r}}}{c} \right\}. \end{aligned} \quad (14)$$

Here, \mathbf{r} is the heliocentric radius vector of the grain, G is the gravitational constant, M_S is the mass of the Sun, M_{P_i} the mass of the i th planet, \mathbf{r}_{dP_i} the vector from the particle to the i th planet, \mathbf{r}_{P_i} the vector from the Sun to the i th planet, $Q = 4\pi\epsilon_0 r_g \Phi$ is the grain charge with the vacuum permittivity ϵ_0 , Φ is the grain surface potential, \mathbf{v}_{sw} is the solar wind velocity, \mathbf{B} is the interplanetary magnetic field, Q_S is the solar radiation energy flux at one AU (astronomical unit), Q_{pr} is the solar radiation pressure efficiency factor, c is the speed of light, and sw is the ratio of solar wind drag to the Poynting-Robertson drag, which depends on Q_{pr} (Gustafson 1994).

The parameterization of the interplanetary magnetic field described in Gustafson (1994) and Landgraf (2000) is used, and a constant surface potential +5 V (Zook et al. 1996) is adopted. To calculate Q_{pr} , the optical constants for silicate grains are taken from Mukai (1989). The dependence of Q_{pr} on grain size for silicate particles, calculated based on the Mie theory (Mishchenko et al. 1999, 2002) for spherical grains, is shown in Fig. 3 (also compare to Fig. 8 of Krivov et al. 2002).

As a sink for dust particles, impacts on the planets are considered. The probability of a close encounter of a particle with a Trojan asteroid is extremely low. The total cross section of L_4 Trojan asteroids is about 10^{13} m^2 (Fig. 1). With a plausible extension of the L_4 cloud of $(40^\circ \times 5 \text{ AU}) \times (1 \text{ AU})$ in the Jovian orbital plane, this means an optical depth of about $\tau = 10^{-10}$, which translates into a characteristic collision time for dust with a Trojan asteroid that is longer than the lifetime of the solar system. Thus, the Trojan asteroids can be safely neglected as sinks and as gravitational perturbers. We also stop the integration when the distance between the particle and the z -axis is smaller than 0.5 AU or larger than 15 AU, in which case we assume that the particle has escaped from the region of interest. This escape efficiently acts as another sink in our model.

4. Simulational scheme

Integrations for ten different grain sizes (radii) are carried out: $0.5 \mu\text{m}$, $1 \mu\text{m}$, $2 \mu\text{m}$, $4 \mu\text{m}$, $5 \mu\text{m}$, $6 \mu\text{m}$, $8 \mu\text{m}$, $10 \mu\text{m}$, $16 \mu\text{m}$, and $32 \mu\text{m}$. For each grain size, 100 particles are started from randomly selected 100 L_4 Trojan asteroids and integrated forward in time. The initial orbits of the particles are assumed to be the

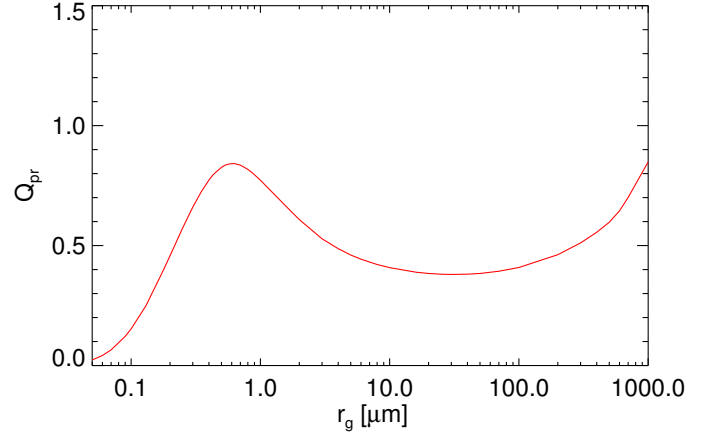


Fig. 3. Size-dependent radiation pressure efficiency Q_{pr} . The values are calculated based on the Mie theory (Mishchenko et al. 1999, 2002), using optical constants for silicate (Mukai 1989).

same as their respective source asteroids. The osculating orbital elements of these Jupiter Trojans at the launching time of the particles are obtained from the JPL Small-Body Database Search Engine. The motions of particles are followed until each of them hit a sink. To handle the heavy computational load, these long-term simulations are performed on the large computer cluster located at the Finnish CSC-IT Center for Science.

We do not store the rapidly changing phase-space coordinates of particles during their evolution because of the huge storage space required. Instead, the slowly changing osculating orbital elements are stored, including the semi-major axis a , the eccentricity e , the inclination i , the argument of pericenter ω , and the longitude of ascending node Ω . Generally, we store the set of elements 100 times per orbit. The storage space required in total is about 280 GB. We assume that the orbital segment between two consecutive stored times t_j and t_{j+1} is Keplerian (with constant values of a , e , i , ω , and Ω , but different values of the true anomaly f). The segment is further divided into m segments of length Δt . The time interval Δt is constant for all trajectories in the whole simulation to ensure that particle positions are stored equidistantly in time. Each storage corresponds to a particle in the simulation (Liu et al. 2016).

The grain trajectories are transformed from the inertial frame $Oxyz$ into a rotating frame $Ox_{rot}y_{rot}z$ in order to evaluate the spatial configuration of dust. The frame $Ox_{rot}y_{rot}z$ shares the z -axis with $Oxyz$. The x_{rot} -axis always points from the Sun to Jupiter, and the y_{rot} -axis completes an orthogonal right-handed frame. Cylindrical coordinates (ρ, ϕ_{rot}, z) in the rotating frame $Ox_{rot}y_{rot}z$ are defined such that $\rho = \sqrt{x_{rot}^2 + y_{rot}^2}$ and $\phi_{rot} = \text{atan2}(y_{rot}, x_{rot})$.

The Trojan region is divided into a number of cylindrical grid cells. For each particle, we determine the cell index $(i_{cell}, j_{cell}, k_{cell})$ where the particle is located. The phase-space number density reads

$$n(i_{cell}, j_{cell}, k_{cell}; > 0.5 \mu\text{m}) = \int_{0.5 \mu\text{m}}^{32 \mu\text{m}} dr_g p(r_g) \Delta t \frac{\tilde{n}(i_{cell}, j_{cell}, k_{cell}; r_g)}{n_{start}(r_g)}. \quad (15)$$

Here $dr_g p(r_g)$ is the number of particles of size in the range $[r_g, r_g + dr_g]$ that are produced per second in the region of the L_4 Trojans, $p(r_g)$ is defined by Eq. (4), and $\tilde{n}(i_{cell}, j_{cell}, k_{cell}; r_g)$ is the number of particles with grain size r_g

in the cell $(i_{\text{cell}}, j_{\text{cell}}, k_{\text{cell}})$ divided by the cell volume, and $n_{\text{start}}(r_g) = 100$ is the number of particles started for each size.

5. Numerical results

The average lifetimes as a function of grain size can be directly determined from the numerical simulations (Fig. 4a). This can be understood in terms of the parameter β , which is defined as the ratio of solar radiation pressure and solar gravitation (Burns et al. 1979),

$$\beta = \frac{3Q_S Q_{\text{pr}} \text{AU}^2}{4GM_S \rho_g r_g c}. \quad (16)$$

Figure 4b shows the values of β for different grain sizes. For particles in the size range $[0.5, 2] \mu\text{m}$, the value of β is high, implying a strong perturbation by solar radiation pressure, which induces high values of the effective semi-major axis and eccentricity (Liou & Zook 1995). As a result, these small particles have short lifetimes from tens of years to tens of thousands of years. With increasing grain size, the value of β becomes lower, and therefore the gravity of the Sun (and Jupiter) becomes dominant. These particles have longer lifetimes, from one hundred thousand years to several millions of years. Most of the particles in the Trojan region are finally transported outward to a distance >15 AU. A few of them are transported inward to a distance <0.5 AU. Very few particles hit Jupiter.

The number density based on Eq. (15) for the size range $[0.5, 32] \mu\text{m}$ in the $x_{\text{rot}} - y_{\text{rot}}$ plane is shown in Fig. 5, vertically averaged over $[-0.55, 0.55]$ AU. Jupiter lies on the x_{rot} -axis, that is, at $\phi_{\text{rot}} = 0^\circ$. The arc spans a wide azimuthal range $30^\circ < \phi_{\text{rot}} < 120^\circ$, much wider than the range of the Trojan asteroids. The reason for this is mainly solar radiation pressure and the drag forces experienced by the dust particles.

The peak number densities from Fig. 5 for different particle sizes are shown in Fig. 6. In this cumulative plot, a steeper gradient corresponds to a larger contribution to the number density. Thus, the particles in the size range $[4, 10] \mu\text{m}$ contribute most to the number density, that is, they are most common in the Trojan arc. These particles stay in the Trojan region for about $10^5 - 10^6$ yrs (Fig. 4a). For particles with grain size $r_g < 2 \mu\text{m}$, the curve is almost flat, which implies that the contribution of particles with grain size $r_g < 2 \mu\text{m}$ to the number density is very small. The reason is that the strong solar radiation pressure (Fig. 4b) rapidly expels the small particles from the Trojan region.

The radial profiles of dust number density at different longitudes are shown in Fig. 7a. Interestingly, the peak is not at L_4 ($\phi_{\text{rot}} = 60^\circ$), but close to $\phi_{\text{rot}} = 78.75^\circ$ and $\phi_{\text{rot}} = 47.25^\circ$, with a projected distance of about $\rho = 5.175$ AU. For the radial profiles along $\phi_{\text{rot}} = 29.25^\circ$ and $\phi_{\text{rot}} = 119.25^\circ$, the peak locations are close to $\rho = 5.025$ AU. The azimuthal profile of the dust number density at $\rho = 5.175$ AU is shown in Fig. 7b. There is a local minimum around the L_4 point ($\phi_{\text{rot}} = 60^\circ$). Based in Fig. 7b, we confirm that the maxima are located close to $\phi_{\text{rot}} = 78.75^\circ$ and $\phi_{\text{rot}} = 47.25^\circ$.

A vertical cut through the densest part of the dust configuration ($\rho = 5.175$ AU, $\phi_{\text{rot}} = 78.75^\circ$) is shown in Fig. 7c. The dust configuration is widely spread out in the vertical direction in the range $[-1, 1]$ AU, with peaks at about $z = \pm 0.4$ AU. The peak values shown in Figs. 5 and 7a,b are slightly lower than those in Fig. 7c because Figs. 5 and 7a,b show a number density that is vertically averaged over $[-0.55, 0.55]$ AU. There is also a local minimum near the mid-plane in Fig. 7c.

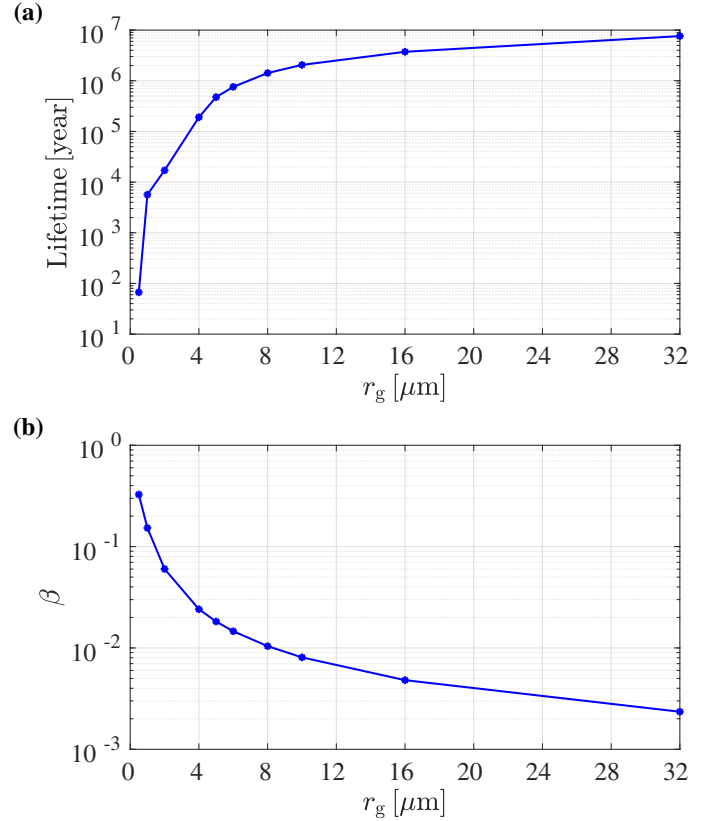


Fig. 4. Panel a: average lifetimes of simulated particles as a function of grain size. Panel b: values of β as a function of grain size.

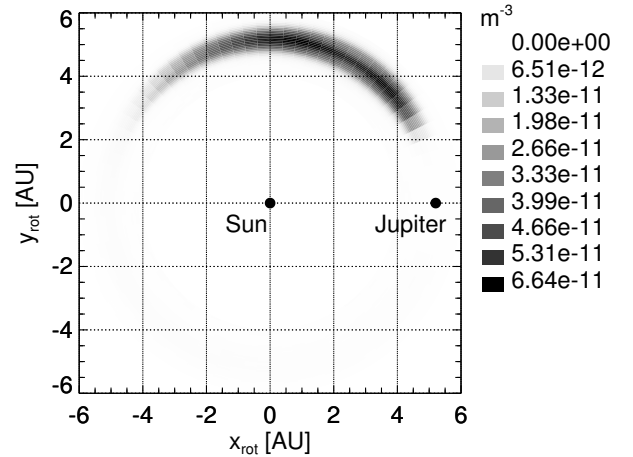


Fig. 5. Dust number density from the simulations of grains from the L_4 Trojan asteroids in the rotating frame $Ox_{\text{rot}}y_{\text{rot}}z$. The cumulative number density is calculated for $r_g > 0.5 \mu\text{m}$, vertically averaged over $[-0.55, 0.55]$ AU. The Sun is located at the origin and Jupiter is close to 5.2 AU on the x_{rot} -axis.

6. Comparison with observations and prospect for detection

An upper limit for the dust number density in the Trojan region can be obtained from the upper limit on the infrared flux inferred from the Cosmic Background Explorer (COBE) satellite data reported by Kuchner et al. (2000). The authors estimated that the cross section of material in the region of L_5 is no more than $6 \times 10^{13} \text{m}^2$. Because the COBE measurement was made at $60 \mu\text{m}$ and only bodies with radii fulfilling $2\pi r_g \geq \lambda$ contribute to the

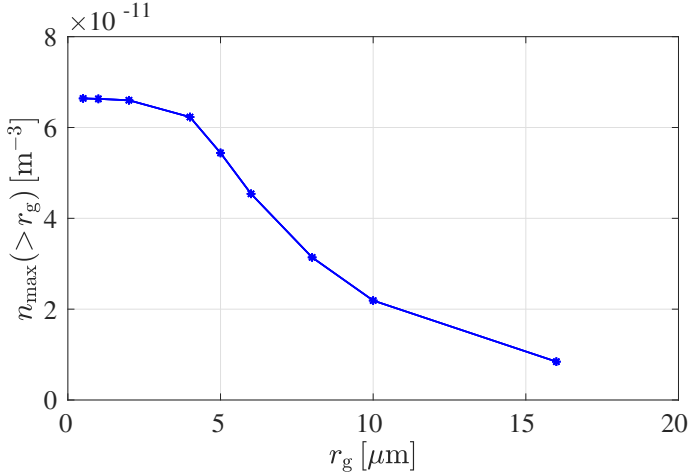


Fig. 6. Peak values of cumulative dust number density from Fig. 5 for different minimum particle sizes r_g .

flux, the measurements constrain the cross section of particles larger than roughly $10\mu\text{m}$ in radius (Jewitt et al. 2000). Thus, the COBE non-detection of brightness in the L_5 region implies that the number of $10\mu\text{m}$ particles is smaller than 2×10^{23} . We use a volume for the Trojan region (at either L_4 or L_5) of roughly $(40^\circ \times 5 \text{ AU}) \times (1 \text{ AU}) \times (0.2 \text{ AU}) \approx 2 \times 10^{33} \text{ m}^3$ (azimuthal \times radial extent \times vertical). This gives a rough upper limit for the number density of particles with $r_g > 10\mu\text{m}$

$$n(>10\mu\text{m}) \lesssim 10^{-10} \text{ m}^{-3}. \quad (17)$$

According to our simulations (Sect. 5), the peak density of grains larger than $0.5\mu\text{m}$ in radius should be around $6.6 \times 10^{-11} \text{ m}^{-3}$, and for grains larger than $10\mu\text{m}$ in radius, it should be around $2.2 \times 10^{-11} \text{ m}^{-3}$ (Fig. 6). This is fairly close to but still consistent with the upper limit of 10^{-10} m^{-3} for $r_g > 10\mu\text{m}$ grains that was derived from COBE data.

The amount of dust produced in collisions of Trojans was estimated by de Elfa & Brunini (2010), who used a collisional fragmentation code to follow the evolution of a Trojan swarm. Their Eq. (16) together with their Fig. 5 gives for dust in the diameter range of $5\text{--}500\mu\text{m}$ a cross section of 10^{18} m^2 for the L_4 Trojan clouds. This is more than four orders of magnitude larger than the upper limit of $6 \times 10^{13} \text{ m}^2$ derived by Kuchner et al. (2000). One possible explanation is that de Elfa & Brunini (2010) did not include the direct solar radiation pressure in their model and therefore obtained dust lifetimes that are too long.

To estimate the particle counts that are expected for a dust detector on a spacecraft, we calculate column number densities of grains larger than $0.5\mu\text{m}$ along characteristic paths through the dust configuration. First, for a radial path in the mid-plane at an angle of $\phi_{\text{rot}} = 78.75^\circ$ from Jupiter (corresponding to the location of the maximum dust number density in the azimuthal direction, see Figs. 5 and 7a,b), we obtain about 7 particles per m^2 . Second, along a vertical path at $\rho = 5.175 \text{ AU}$ and $\phi_{\text{rot}} = 78.75^\circ$ (passing through the location of highest dust density), we obtain about 19 particles per m^2 . These numbers are for a pure silicate surface of the Trojans. If the surfaces contain a fraction of ice, the production rate will be higher (Fig. 2). For a pure ice surface, the particle counts would be higher by more than one order of magnitude than for the pure silicate case, assuming the same lifetimes for ice and silicate particles.

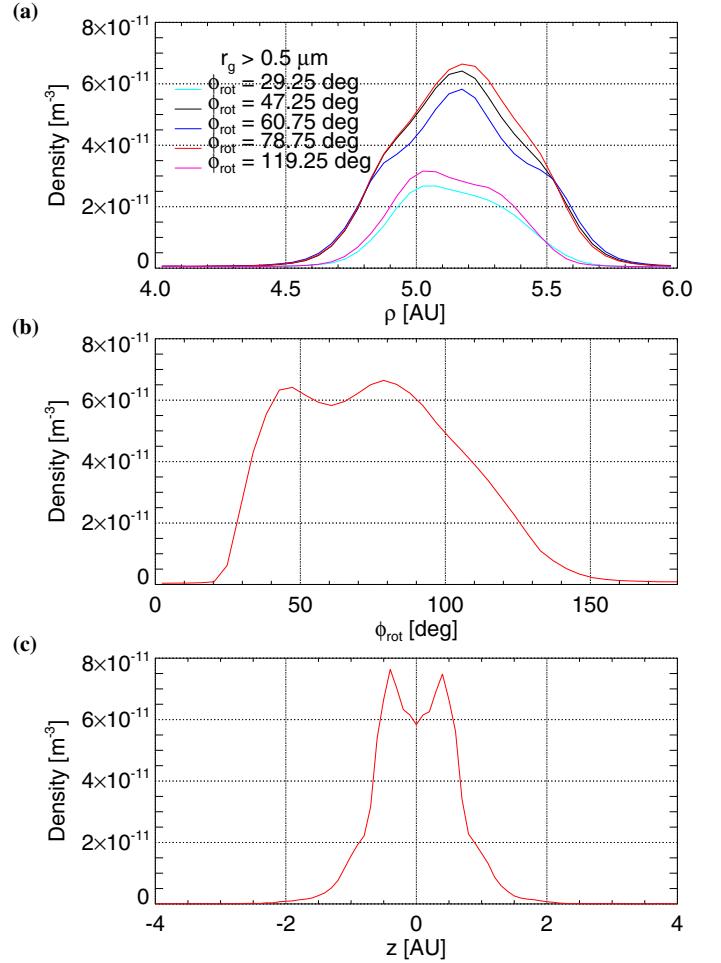


Fig. 7. Panel a: radial profiles of the dust number density at different azimuthal angles from the position of Jupiter. Panel b: azimuthal profile of the dust number density for $\rho = 5.175 \text{ AU}$ from Fig. 5. Panel c: vertical cut through the densest part ($\rho = 5.175 \text{ AU}$ and $\phi_{\text{rot}} = 78.75^\circ$) of the dust configuration.

7. Conclusions

We have analyzed the properties of a faint dust population associated with the Jupiter L_4 Trojan asteroids. With massive simulations, we find that particles in the size range of $[4, 10]$ microns are dominant. We derive the overall shape of the steady-state dust configuration. Compared to their sources, that is, the Trojan asteroids, the dust particles are distributed more widely in the azimuthal direction, covering a range of $[30^\circ, 120^\circ]$ relative to Jupiter. The peak number density does not lie at the L_4 point, but close to 78.75° and 47.25° in the azimuthal direction relative to Jupiter. Dust particles are also widely distributed in the vertical direction, with peaks of the number density located at about $z = \pm 0.4 \text{ AU}$. There is a local minimum of the number density around the L_4 point and the mid-plane. We expect similar properties of the dust distribution in the region of the L_5 Trojan asteroids because the dynamical environment is similar.

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