Evolution of the anti-truncated stellar profiles of S0 galaxies since $z = 0.6$ in the SHARDS survey

I. Sample and methods

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ABSTRACT

Context. The controversy about the origin of the structure of early-type S0–E/S0 galaxies may be due to the difficulty of comparing surface brightness profiles with different depths, photometric corrections and point spread function (PSF) effects (which are almost always ignored).

Aims. We aim to quantify the properties of Type-III (anti-truncated) discs in a sample of S0 galaxies at $0.2 < z < 0.6$. In this paper, we present the sample selection and describe in detail the methods to robustly trace the structure in their outskirts and correct for PSF effects.

Methods. We have selected and classified a sample of 150 quiescent galaxies at $0.2 < z < 0.6$ in the GOODS-N field. We performed a quantitative structural analysis of 44 S0–E/S0 galaxies. We have corrected their surface brightness profiles for PSF distortions and analysed the biases in the structural and photometric parameters when the PSF correction is not applied. Additionally, we have developed Elbow, an automatic statistical method to determine whether a possible break is significant – or not – and its type. We have made this method publicly available.

Results. We find 14 anti-truncated S0–E/S0 galaxies in the range $0.2 < z < 0.6$ (~30% of the final sample). This fraction is similar to the those reported in the local Universe. In our sample, ~25% of the Type-III breaks observed in PSF-uncorrected profiles are artifacts, and their profiles turn into a Type I after PSF correction. PSF effects also soften Type-II profiles. We find that the profiles of Type-I S0 and E/S0 galaxies of our sample are compatible with the inner profiles of the Type-III, in contrast with the outer profiles.

Conclusions. We have obtained the first robust and reliable sample of 14 anti-truncated S0–E/S0 galaxies beyond the local Universe, in the range $0.2 < z < 0.6$. PSF effects significantly affect the shape of the surface brightness profiles in galaxy discs even in the case of the narrow PSF of HST/ACS images, so future studies on the subject should make an effort to correct them.

Key words. methods: observational – methods: statistical – galaxies: fundamental parameters – galaxies: structure – galaxies: elliptical and lenticular, cD

1. Introduction

The origin and evolution of lenticular (or S0) galaxies is still a matter of debate. Traditionally they were classified as the natural transition between the elliptical galaxies and more complex galaxy types; spirals, in the Hubble morphological sequence (de Vaucouleurs 1959; Sandage 1961). The cause of this is that S0 galaxies usually appear without any spiral structure or signs of recent star formation in their discs. Freeman (1970) pointed out that the discs of spiral and S0 galaxies usually show surface brightness profiles that are (to first order approximation) reasonably well-fitted by an exponential function out to a certain radius, due to the stellar density decline as a function of galactocentric radius (Sérsic 1963).

Nevertheless, as deeper observations allowed the study of the outskirts of galactic discs, it was found that many lenticular galaxies do not follow a purely exponential profile along their whole observable radius (Sil'chenko 2009; Kormendy & Bender 2012; Ilyina & Sil'chenko 2012). Erwin et al. (2005) pointed out that a significant fraction of S0 galaxies present light excesses in the outskirts of the discs, which also show an exponential decline but with a shallower slope than their inner discs. Erwin et al. (2008, E08 hereafter) expanded the stellar disc classification of galaxies from Freeman (1970), according to the profile structure. Type-I discs are well modelled with a single radial exponential profile. Type-II galaxies present a down-bending profile, this is, a brightness deficit in the outer parts of the disc with respect to the extrapolated trend of the inner regions beyond a

given break radius. Type-III discs becomes less steep outside the break radius than the extrapolation of the exponential trend of the inner parts (anti-truncation, see Pohlen & Trujillo 2006). E08 and Gutiérrez et al. (2011, G11 hereafter) showed that the fraction of anti-truncated discs was higher for S0 galaxies than for any other morphological type, increasing from $\sim 10\text{--}20\%$ in Sc–Sd galaxies, up to $\sim 20\text{--}50\%$ in S0–Sa galaxies (see also Ilyina & Sil’chenko 2012; Maltby et al. 2015). In the present study we will focus on the Type-III profiles.

A high fraction of the anti-truncated profiles are due entirely to disc structure, although $\sim 15\%$ might be due to outer stellar haloes (Maltby et al. 2012). In some cases, transitions between the inner and outer profiles are associated with structural components of the galaxy such as rings or lenses (Laine et al. 2014). Some authors (e.g. Comerón et al. 2012) pointed out that these transitions might be caused by combinations of thin+thick discs with different radial scale-lengths. The role of environmental density in the formation of these structures is still a matter of debate. Some authors do not find a significant correlation between the presence of Type-III profiles and the environment (Maltby et al. 2012) while other authors do (Laine et al. 2014). A recent study (Pranger et al. 2017) found that the outer scale-lengths of both Type-II and Type-III profiles are $\sim 10\%$ larger in the cluster environment compared to the field. These authors also suggest that the Type-I profiles would be an intermediate step in the transformation of Type-II into Type-III profiles. Nevertheless, Type-III profiles are ubiquitous regardless of their environment (Erwin et al. 2012; Pranger et al. 2017), and the observed suppression of Type-II profiles in the clusters argues against a common origin for both Type-II and Type-III profiles. On the contrary, this suggests that the two types of profiles are caused by completely different phenomena (Erwin et al. 2012; Roediger et al. 2012; Laine et al. 2014).

Radially varying profiles of star formation have been proposed as a cause for both Type-II and Type-III profiles (Elmegreen & Hunter 2006). However, most of the proposed mechanisms to explain Type-III profiles are based on different modes of gravitational interactions, such as close encounters (Peñarrubia et al. 2006), accretion of dark matter sub halos (Kazantzidis et al. 2009) or minor mergers (Younger & Bryan 2007). In addition, Herpich et al. (2015) also proposed radial mass redistribution as a cause for the different types of profiles due to different initial angular momentum of the host halo. Borlaff et al. (2014) tested whether major mergers can produce anti-truncated stellar profiles in S0 galaxies using hydrodynamical N-body simulations. They found that Type-III profiles of S0 remnants can be produced after a major merger event, and that those profiles obey similar scaling relations to those found in observed Type-III S0 galaxies. In a later paper, Eliche-Moral et al. (2015) reported that these relations are similar to those found in Type-III spiral galaxies, which suggests that fundamental processes must be responsible for the formation of these structures in disc galaxies along the whole Hubble Sequence. However, no study has analysed the properties of anti-truncated S0 and E/S0 galaxies beyond the local universe to learn about their possible evolution, because cosmological dimming efficiently moves these structures towards even fainter (and prohibitive) surface brightness levels.

The controversy that arises out of the comparison between different datasets may be due to the difficulty of comparing samples with different depths and surface brightness profile corrections. Measuring robust surface brightness profiles down to $\mu_{\text{lim}} \sim 27\text{--}28 \text{ mag arcsec}^{-2}$ is a challenging task. de Jong (2008) showed that the detection of an apparent halo around the minor

axis of an edge-on galaxy in the *Hubble* Ultra Deep Field can be largely explained by scattered light from the inner regions. This light spreading follows a point spread function (PSF) whose shape depends on the telescope, instrument, filter and even time (Sandin 2014, 2015). It modifies the true light distribution of the object as a convolution, “blurring” the resulting image. The PSF effect scales with the intensity of the source, and it usually becomes smaller rapidly with increasing radii. Nevertheless, the contribution of the outer wings of the PSF profile can be significant in the outskirts of galaxies, where the light intensity is very faint. This would produce apparent light emission excesses where they otherwise would not be found. Thus estimating and correcting the PSF effect is a crucial step for any study of surface brightness profiles in the outskirts of galaxies, especially when looking for Type-III profiles.

In order to estimate the surface brightness profile of an object, the observer must know the shape of the PSF out to (at least) 1.5 times the maximum size of the object in radius (Sandin 2014). To estimate precise measurements of the structural parameters of galaxies, it is not enough to simply scale the PSF profile to the central surface brightness of the profile (de Jong 2008). The observer must subtract the PSF contribution created by the whole 2D light distribution (or at least by a realistic model) not only by the innermost region but also from the outer regions of the object. Direct image deconvolution methods such as the Richardson-Lucy (Prato et al. 2012) are tempting, but inefficient (see Karabal et al. 2017, for a recent and less time-consuming method of direct deconvolution) and may lead to disruptions of the low surface brightness regions. In contrast to these, recent papers propose accurate methods for removing the PSF contribution by fitting 2D models of the galaxy taking into account the PSF (Trujillo & Fliri 2016). This method permits the derivation of reliable surface brightness profiles down to $\sim 31 \text{ mag arcsec}^{-2}$, according to these authors. In the present work we will follow a similar procedure, even though our profiles are limited to radii where the profiles are $3\text{--}4 \text{ mag arcsec}^{-2}$ brighter, where the effects of the PSF are less significant.

In order to shed light on the evolution of these structures, we have selected a sample of galaxies from the red sequence and then we have identified the S0 and E/S0 galaxies at $0.2 < z < 0.6$ by studying their star formation rate, morphology and analysing their surface brightness profiles. We have quantified the properties of Type-III discs in this sample and compared them to the Type-III profiles from the samples at $z \approx 0$. In this paper, we present the sample selection and describe in detail the statistical methods to trace the structure in their outskirts and correct for PSF effects. We will analyse the scaling relations at $0.2 < z < 0.6$ and compare them with their local counterparts in a forthcoming paper (Borlaff et al., in prep.).

The outline of this paper is as follows. The method is described in detail in Sect. 2. The results are presented and discussed in Sect. 3. The final conclusions can be found in Sect. 4. We tabulate the general properties of the initial red galaxy sample in Appendix A. Appendix B contains the profile classifications for the S0 – E/S0 sample and their structural and photometric parameters. Appendix C describes the final sample of anti-truncated S0 and E/S0 galaxies individually and shows the RGB images used for the morphological classification as well as the decompositions performed to the profiles. We assume a concordant cosmology ($\Omega_{\text{M}} = 0.3, \Omega_{\Lambda} = 0.7, H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, see Spergel et al. 2007). All magnitudes are in the AB system unless otherwise noted.

2. Methods

In order to study the properties of the surface brightness profiles of non-local S0 – E/S0 galaxies in the GOODS-N field at $z < 0.6$, first we had to create a sample of quiescent candidates, that must include S0 and E/S0 galaxies, by definition. The data used are presented in Sect. 2.1 and the selection of a sample of quiescent candidates with $z < 0.6$ is described in Sect. 2.2. Secondly, we performed a visual morphological classification based on the data available for the selected objects (2D structure, presence of AGN activity, star formation rate (SFR), total stellar mass and surface brightness profile), as described in Sects. 2.2 and 2.8. Thirdly, we modelled each object and corrected any possible PSF contributions to the surface brightness profiles. After this, we estimated the necessary corrections for dust extinction, cosmological dimming and K-correction for each S0 and E/S0 object (Sects. 2.5). This is explained in detail in Sects. 2.3–2.4 and 2.7. Finally, we performed the identification, characterisation and analysis of the structure of the components in the surface brightness profiles as described in Sect. 2.6. The efficiency and reliability of the PSF correction performed to the galaxies in our sample is checked in Sect. 2.7.

2.1. Data description

2.1.1. SHARDS and the Rainbow database

The Survey for High- z Absorption Red and Dead Sources (SHARDS, Pérez-González et al. 2013) is an ESO/GTC Large Program carried out with the OSIRIS instrument on the 10.4 m Gran Telescopio Canarias (GTC). This survey obtained data between 5000 Å and 9500 Å for galaxies in the GOODS-N field down to magnitudes $m < 26.5$ AB mag, in 25 medium band filters with a full width at half maximum (FWHM) of ~ 170 Å. The main goal of this survey was to study the properties of stellar populations of massive galaxies in quiescent evolution at $z = 1.0$ – 2.3 through the pseudospectra resulting from the data of this photometric medium band filter system (the set is equivalent to low resolution integral field spectroscopy, $R \sim 50$) and deep ancillary broad-band data. The wavelengths include key absorption indexes such as Mg(UV) ($\lambda \sim 2800$ Å), essential for the study of high- z early-type galaxies. This technique allowed the SHARDS team to select quiescent objects, calculate star formation histories (SFH) and photometric redshifts with a precision better than $\Delta z/(1+z) \sim 0.007$ (Domínguez Sánchez et al. 2016). See Pérez-González et al. (2013) for a detailed description.

SHARDS data are available through the Rainbow Database (Barro et al. 2011a,b) in compilation with multiple photometric and spectroscopic data for several cosmological fields, such as GOODS-N and GOODS-S, COSMOS, or the Extended Groth Strip. The authors used all the available photometry to build spectral energy distributions (SEDs) from X-ray to radio. Using the SED fitting procedure, they derived photometric redshifts and estimates of parameters such as the stellar mass, the UV- and IR-based SFRs, the stellar population age and rest-frame magnitudes in different filters (Pérez-González et al. 2005, 2008, 2013).

In this study, we have selected a sample of GOODS-N galaxies included in the SHARDS survey, that: 1) have low star formation rates, compatible with being early-type galaxies; 2) have total stellar masses similar to those of the available local samples ($M \sim 10^9$ – $10^{11} M_\odot$), and 3) have morphologies compatible with being S0 – E/S0 objects. We restricted the selection only to the objects with reliable SHARDS data because: 1) we wanted to

ensure that the S0 and E/S0 galaxies included in the sample are really quiescent and have stellar masses comparable with the local sample; and 2) we aimed to create a sample of anti-truncated S0 and E/S0 galaxies that can be used in a forthcoming study to investigate the properties of the stellar populations, metallicities and star formation rates of their inner and outer profiles. We have used SHARDS data release 2 in the database (iDR2beta).

2.1.2. HST/ACS data in the GOODS-N field

We have derived, corrected and analysed the surface brightness profiles using the deepest images available in our dataset tracing the rest-frame V and R bands, that is, those in the $F775W$ band of HST/ACS. The GOODS-N field is a large cosmological field with HST/ACS imaging centred on the *Hubble* Deep Field North (Dickinson et al. 2003). The spatial resolution of these images is 0.06 arcsec/px and the 1σ fluctuation level of the surface brightness on a area of 1 arcsec² is 27.7 mag. The average FWHM for the $F775W$ filter mosaic is 0.11 arcsec (Skelton et al. 2014, see Table 6). In order to derive the surface brightness profiles for the SHARDS objects, we relied on the ACS $F775W$ mosaic from the ACS V2.0 data release (HST Cycle 11, programme IDs 9425 and 9583, Giavalisco et al. 2004) available at the 3D-HST project webpage¹ (Skelton et al. 2014). The zeropoints of the images are available in Table 6 of Skelton et al., such that:

$$\mu_{F775W} = -2.5 \cdot \log_{10}(\text{counts/area}) + 25.671. \quad (1)$$

The reduction process of the raw data was performed by using the CALACS software, available at the Space Telescope Science Institute site (Pavlovsky et al. 1999). This pipeline accounts for the bias subtraction, gain correction, and flat-fielding correction of each individual exposure. The corrected (flt.fits) individual images were then drizzled to the final mosaic through the Multidrizzle software package (Koekemoer et al. 2003), and corrected for geometric distortion at the same time, removing cosmic-rays and performing sky-subtraction. For more details on the process of reduction and the data, we refer the reader to Giavalisco et al. (2004).

We set the upper limit on redshift for the initial sample at $z = 0.6$, in order to cover, with the $F775W$ filter from HST/ACS, a similar wavelength range as the local universe observations we wanted to compare with (usually, in the V or R bands). This band traces similar wavelengths as the R band from $z = 0.1$ to $z \sim 0.3$ and is equivalent to $F606W$ (tracing approximately V) between $z = 0.2$ and $z = 0.6$. Thus, we selected the initial sample within $0.2 < z < 0.6$. In order to compare the surface brightness profiles between the local sample and ours, we also performed a photometric K-correction to our data to transform them into the rest-frame R filter (see Sect. 2.5).

2.2. Red sample selection and morphological classification

In the local universe and beyond, galaxies are divided into two main classes: star-forming galaxies and quiescent galaxies (van Dokkum et al. 2000; Willmer et al. 2006; Kodama et al. 2007; Williams et al. 2009; Brammer et al. 2011; Whitaker et al. 2011). These two populations of galaxies show very different distributions in rest-frame colour-magnitude diagrams: quiescent galaxies usually have high luminosities and red colours while the star-forming galaxies present lower luminosities and

¹ 3D-HST – A Spectroscopic Galaxy Evolution Survey with the *Hubble* Space Telescope: <http://3dhst.research.yale.edu/Home.html>

Fig. 1. Initial sample selection with the $(U - V)$ vs. $(V - J)$ colour-colour diagram by redshift intervals up to $z = 0.6$. Dashed line: Whitaker et al. (2011, 2012) boundaries for identifying the quiescent galaxy population and the star-forming galaxies (see Eqs. (2)–(4)). Red dots: quiescent galaxies from the initial SHARDS sample. Blue stars: star-forming galaxies from the initial SHARDS sample. The number of objects selected in each class and interval of redshift are given on the panels.

bluer colours. This means that the two populations of galaxies appear as two well separated sequences in the $(U - V)$ vs. $(V - J)$ colour-colour diagram, so we can select a quiescent sample (that includes S0 and E/S0 galaxies, in which we are interested) by using the following boundary-relations (Whitaker et al. 2011, 2012):

$$U - V > 0.8 \times (V - J) + 0.7 \quad (2)$$

$$U - V > 1.3 \quad (3)$$

$$V - J < 1.5. \quad (4)$$

The galaxies selected within these boundaries present very red colours, either because they depleted their gas reservoir and cannot create new stars or because they are extremely extinguished by interstellar dust. We selected all sources from the GOODS-N field in the SHARDS catalogue (excluding those classified as stars) which present redshifts $0.2 < z < 0.6$, and we have used the previous boundaries in the colour-colour diagram to select those in the red sequence. We have excluded objects with $z < 0.2$ in the catalogue because of the high uncertainties detected in the estimates of the photometric redshifts at these distances (Barro et al. 2011b). In addition to this, we used visual morphology classification as well as near-IR (NIR) and UV SFR to prevent reddened spiral and irregular galaxies from being included in the sample of quiescent galaxies (see Sect. 3.2). In Fig. 1 we show an example of this first selection process. Rest-frame U , V and J magnitudes as well as the redshifts and stellar masses were taken from the Rainbow Database (see Sect. 2.1.1). The panel shows those SHARDS objects within the red sample

according to the criteria outlined previously. With blue stars, we represent the discarded objects. For the sake of completeness we show the diagrams corresponding to the interval $z = [0, 0.6]$ with $\Delta z = 0.1$. We removed eight objects with $0.2 < z < 0.6$: seven of them were artifacts and spurious detections (SHARDS10007608, SHARDS10009632, SHARDS10012462, SHARDS10012556, SHARDS20013873, SHARDS20001446 and SHARDS20009949) and one object was clearly affected by nearby star contamination (SHARDS20008526). Finally we identified 150 objects as “red” (mostly quiescent, as we will show in Sect. 3.2) in total between $0.2 < z < 0.6$. The sample presents median value of $z = 0.41$. We note that $\sim 75\%$ of the objects have $z > 0.27$. The red objects in our sample and their main properties (coordinates, morphological type, photometric and spectroscopic redshifts, stellar mass, SFR, rest-frame absolute K and V magnitudes, extinction and K -correction for the $F775W$ filter) are provided in Table A.1.

We have performed a visual morphological classification of the objects based on the HST/ACS images in the $F435W$, $F606W$ and $F775W$ bands, and a false colour combined image of these three ones. In Fig. 2 we present a summary of the morphological classification process by showing the available information of one object of each morphological class that we have considered, which we describe below. From left to right, the first three columns represent the images of each object in the three filters used for this analysis: $F435W$, $F606W$ and $F775W$. We used the $F435W$ filter to detect possible star formation regions that may not be detectable in the other redder filters. This allowed us to

Fig. 2. *F435W*, *F606W* and *F775W* images of some objects from the initial selected red sample, used for the morphological classification. Columns, from left to right: 1) *F435W* image; 2) *F606W* image; 3) *F775W* image; 4) RGB colour image, using the previous filters for the blue, green and red colours, respectively; 5) information panel with the identifier of the object in the SHARDS data release 2, position (α , δ), total stellar mass, SFR and z .

discard from the red sample the dust-reddened spirals that had not been rejected using the colour-colour criteria, or contamination sources which were very bright in the bluer bands but difficult to identify in the redder bands, such as small satellites, tidal tails or minor mergers in the outskirts of the objects. The RGB images shown in the fourth column were created by the combination of the previous three filters. These RGB images were used

for the morphological classification, together with the individual filter images. In addition, preliminary surface brightness profiles (i.e. without PSF correction) as well as some characteristic parameters of each object (see the right column of Fig. 2) were used for the classification process. The images used during the classification presented a field-of-view (FoV, hereafter) of $7 \times R_{kr}$ were R_{kr} is the Kron radius (Kron 1980) of the object (available from

the Rainbow Database, see Sect. 2.1.1). It was defined in this way to show a sufficient portion of the surrounding areas around the object to identify possible interactions, close companions or sources of diffuse light contamination.

We classified the objects of the initially selected red sample morphologically according to the following criteria (see an example of each morphological type in Fig. 2):

– A. Morphological types assigned to well-resolved galaxies:

1. *Elliptical galaxies (E)*: they do not present any signs of a disc component, but a smooth light distribution surrounding a bright compact core with very low ellipticity. The surface brightness profiles usually decrease with a steeper and non-constant slope when compared to an exponential profile. The surface brightness profiles are usually well-fitted with a single Sérsic profile with index $n \sim 3-5$. They do not show appreciable star formation signs, bars, or spiral arms.
2. *S0 – E/S0 galaxies*: they show a noticeable disc component with a smooth light distribution, without any signs of spiral structure or star-forming regions. For those objects where the dominant component is the disc, we have assigned the S0 classification. On the contrary, the objects with a dominant central bulge or halo were classified as E/S0. Some S0 galaxies at low inclination may be mistaken for elliptical galaxies in the visual classification. To avoid contamination between the types, we refined our visual classification by using the surface brightness profiles and the multi-component GALFIT3.0 analysis, as detailed in Sect. 2.3.
3. *Spiral galaxies (Sp)*: they present a disc component and a spiral pattern with clear star-forming regions detected in the *F435W* band.
4. *Ongoing mergers (OM)*: these objects present highly irregular and distorted light distributions in the images. The progenitors can still be identified separately. Close pairs without clear signs of tidal interaction were not included in this category and we have classified them as two independent galaxies.

– B. Morphological types associated with low signal-to-noise ratio (S/N) or low resolution data:

1. *Compact post-starbursts (CPSTB) and green peas (GP)*: these are very compact objects. The spatial resolution is not enough to resolve their structure or different components. Some of these objects present recent merger signs. The CPSTBs present extremely red colours, possibly caused by extreme dust extinction. In contrast, the GPs usually present green colours in the false RGB images used to classify them. We adopted the green peas nomenclature following Cardamone et al. (2009), but in order to confirm the objects within this class as real GPs according to their definition we would require specific observations, which are beyond the scope of this paper.
2. *Diffuse galaxies (DF)*: we classify as diffuse galaxies those objects with very low S/N ratio, usually with elongated morphologies. Faint spirals or interacting disc galaxies are possible candidates to appear as diffuse galaxies. They fall into the red sequence probably because of dust extinction. The surface brightness profiles are too faint and noisy due to the low apparent luminosities.

As explained before, S0 galaxies can be confused with elliptical galaxies, especially those at low inclination. The discs of spiral and S0 galaxies usually show surface brightness profiles that follow an exponential law (Freeman 1970) out to a certain radius. In contrast, elliptical galaxies show a steeper surface brightness decline, usually well fitted by a $n \sim 4$ Sérsic profile (i.e. a de Vaucouleurs profile). We exploited these structural characteristics to distinguish S0 from E galaxies even at low inclination. Thus, for the elliptical, S0 and E/S0 galaxies identified visually, we refined the morphological classification using the surface brightness profiles, as well as the 2D decomposition, to ensure that we are not including elliptical objects in the final S0 – E/S0 sample (see Sect. 2.3). We found 50 S0 and E/S0 galaxies within our initial sample of 150 red galaxies (38 S0 and 12 E/S0). We could correct for PSF effects 44 out of these 50 S0 and E/S0 galaxies, as explained in Sect. 2.3. The remaining objects were removed from the final sample because they did not present stable bulge+disc 2D decompositions (SHARDS10001928, SHARDS10002901, SHARDS10005029, SHARDS10008552, SHARDS20000858 and SHARDS20004273). The morphologies of our red galaxy sample and their global properties are described in detail in Sects. 3.1 and 3.2. The final morphological classification for all objects in our red sample is provided in Table A.1. The RGB images of the objects finally classified as S0 and E/S0 that could be corrected for PSF effects are provided in Appendix C.

2.3. GALFIT modelling and PSF correction

In order to estimate and correct the amount of dispersed light by the PSF in the HST/ACS images, especially in the outskirts of the galaxies, we cannot simply perform a numerical deconvolution of the image, because it would affect the light distribution in the low surface brightness region (see Sect. 1). We have followed a similar procedure to that presented in Trujillo & Bakos (2013).

First, we performed careful masking in all the images, in order to avoid contamination by foreground objects, non-symmetric components such as satellites, compact bright regions or close stars or their PSF spikes. We created these masks in two steps. We performed an automatic masking by using SExtractor (Bertin & Arnouts 1996), which is later manually checked. We manually extended the masks of the largest foreground objects with circular masks in order to prevent the scattered light from contaminating the surface brightness profiles of the galaxies. We estimated the limits of each manual masking by analysing the isophotal map on smoothed images. We gradually increased the smoothing kernel from two up to eight to ten pixels, checking on each step the possible features that appeared. By using the isophotal contours, we checked the possible distortions due to contamination sources or extreme changes in the position angle and ellipticity in each object. Finally we used the masked images (centred on each object, with a FoV of 100×100 arcsec) to measure individually the sky noise distribution, which defines for each object the limiting magnitude of the profile. See some examples of isophotal maps and masked regions in the figures of Appendix C. The effects of PSF correction on the resulting profiles are analysed in Sect. 3.5.

We used GALFIT3.0 (Peng et al. 2002) to fit two sets of models for each object within our sample of 50 S0 and E/S0 galaxies: a single free Sérsic model and a free Sérsic model + exponential profile. In this step, we discarded from the S0 and E/S0 sample those objects which: 1) cannot be fitted with a stable model, due to small size or irregularities; 2) are well fitted with a single (high n) Sérsic profile, so the profile corresponds to

an elliptical galaxy rather than an E/S0 or S0 (see Sect. 2.2); or 3) do not drastically reduce the residuals of the fit by adding a second component to the first one. This revision was performed individually by three co-authors, checking the differences between the modelled and the original profiles. In this phase we distinguished between the elliptical galaxies from face-on S0 galaxies by analysing their surface brightness profiles. In order to do that, we have estimated for all the objects two different 2D decompositions: 1) using a single Sérsic profile and 2) with a Sérsic bulge + exponential disc profile. We note that each 2D decomposition implies a different PSF deconvolution. We analysed the residual profile of each object, and identified those which do not drastically improve with the addition of a disc component and present a smooth decrease of the slope with the galactocentric radius. Finally we confirmed that the nine objects that visually presented elliptical morphologies really were ellipticals according to their surface brightness profiles. We show the surface brightness profiles, with the corresponding models and residual profiles, for the S0 and E/S0 galaxies with successful PSF correction in Appendix C.

We have estimated the errors of the parameters of each model by performing Monte Carlo simulations over the original images, varying each pixel value within the noise level and fitting sequentially. We note that we assume 1, 2 and 3σ limits as those values that enclose 68%, 95% and 99.7% of the probability distribution of the sample. In the case of the noise level of our images the sample are the sky-dominated pixels. We define as sky-dominated pixels any pixel that was not identified as part of a source in the masks generated before to create the GALFIT3.0 models and the surface brightness profiles. We estimated the noise level as the upper 1σ fluctuation of the sky background distribution. This value is equivalent to the standard deviation if we assume that the sky background follows a nearly Gaussian distribution with a mean of zero and dispersion equal to the measured noise level. By providing GALFIT3.0 a PSF model for the image, the programme tries to fit the best model that, after convolution with the PSF, matches the original image. This allows us to estimate the amount of diffuse light scattered into the outskirts of the image. We estimate the deconvolved image through the following image operation:

$$\text{Residuals} = \text{Image raw} - \text{PSF} * \text{Model}_{\text{GALFIT}}. \quad (5)$$

$$\text{Deconvolved final image} = \text{Model}_{\text{GALFIT}} + \text{Residuals}. \quad (6)$$

The 3DHST team provides a star-stacked PSF, but the model size is very small for our purposes (~ 4 arcsec in diameter) while we need at least a ~ 25 arcsec diameter PSF to perform any kind of PSF subtraction (Sandin 2014, 2015). Otherwise, the reconvolved model (i.e., the fitted PSF-free model, again convolved by the PSF) would systematically underestimate the amount of dispersed light at radii larger than half the diameter of the PSF. This limit in size was calculated by multiple iterations in the surface brightness profile fitting, and roughly corresponds to 1.5 times the limiting radius at $S/N = 3$ in the surface brightness profiles of the larger galaxies in our sample. We show an example of the deconvolution and modelling in Fig. 3. In the top panel, we represent the surface brightness profiles of the original and PSF-corrected image, as well as the profiles of the models used for the deconvolution. We note that the deconvolved profile is systematically biased towards brighter magnitudes in the centre and dimmer magnitudes in the outskirts. This effect is clear in the bottom panel, where we show the differences between the original and the PSF-corrected profiles (red dots). We also note that the original and reconvolved profile (black squares) are nearly

Fig. 3. *Top panel:* surface brightness profiles of the Type-III S0 galaxy SHARDS10009610. Blue squares: surface brightness profile of the original image. Black dots: the same for the PSF-corrected image (black). We represent the magnitude scale for the observed $F775W$ band (*left axis*) and for the rest-frame R band (*right axis*). The red solid and blue dashed lines correspond to the models fitted during the deconvolution and used for checking the visual morphological selection (see the legend). *Bottom panel:* residuals between the original and corrected profiles. Red circles: difference between the original and the PSF-corrected profiles. We note that the PSF effects create a systematic upturn beyond ~ 1.0 arcsec. Black squares: difference between the original profile and the reconvolved PSF-corrected image profile. The vertical red line represents the limiting radius.

identical along the whole profile, showing that the PSF correction and the fit are adequate, under the assumption that the PSF model is robust and realistic (we demonstrate this in Fig. 4, see below).

GOODS-N is an extremely star-clean field, so PSF modelling using star stacking may lead to noisy and biased distributions in the outskirts of the profiles due to the lack of bright stars in the field. Instead, we have created a model of the PSF using the Tiny Tim software (Krist et al. 2011) for the PSF outskirts, combined with a GOODS-N stacked star PSF for the inner regions of the PSF provided by 3DHST. Tiny Tim is a modelling tool for generating HST model PSFs for multiple cameras and filters. The synthetic PSFs generated by Tiny Tim have been previously used in similar studies (See de Jong 2008; Trujillo & Bakos 2013). GOODS-N has a covering grid of 3×5 individual ACS pointings, with some overlap to check the photometric and astrometry consistency between individual pointings. There is a rotation of the field of 45° between the odd-numbered epochs and the even-numbered epochs. In order to approximate the effect of the combination of rotated images in the final mosaic, we combined two Tiny Tim PSF model images of 29 arcsec in diameter, rotated 45° degrees (Trujillo & Fliri 2016). After that, the centre of the resulting PSF model was replaced by the natural star PSF model of 3DHST, which is reliable only out to 4 arcsec. We measure a FWHM of our combined PSF model is 0.09 arcsec. As mentioned in Sect. 2.1.2, in Skelton et al. (2014) (see Table 6), the authors report an average FWHM of 0.11 arcsec for the $F775W$ band mosaic of GOODS-N.

Fig. 4. Comparison of the subtraction of a star with GALFIT3.0, using a 15 arcsec Tiny Tim PSF (*upper row*) and our combined PSF (*lower row*). *Top left panel:* F775W image of a star. *Bottom left panel:* intensity profiles for the star, the PSF models and the residual images after the subtraction of the Tiny Tim PSF and after the subtraction using our combined PSF (see the legend for details). *Middle column:* PSF scaled models for the Tiny Tim model (*top*) and the combined PSF (*bottom*). *Right column:* residuals of the subtraction for the Tiny Tim model (*top*) and the combined PSF (*bottom*). We note that the residuals for the wings in case of using our combined PSF are smaller at all radii than those resulting from using the Tiny Tim PSF, despite the common central underestimate. The FoV of all the images is 24×24 arcsec². All images are in the same colour scale.

In Fig. 4 we show a quality test to show that our PSF model is robust and realistic. The upper panels show the test using a standard PSF created by Tiny Tim for the F775W filter, whereas the lower panels show the test using our combined PSF. We have fitted each PSF to a well-centred field star in the GOODS-N image, using GALFIT3.0. The residuals of the two cases are shown in the right panels, and the residuals profile in the bottom left panel. We find that our combined PSF model significantly reduces the residuals of the PSF modelling of the star when compared to the original Tiny Tim model. The success of the subtraction is significant especially for the intermediate and external parts where the characteristic spikes and rings of the HST PSF are removed almost completely. In addition, the remaining residuals in the centre do not show circular symmetry, which would introduce contamination in our azimuthally averaged profiles.

Additionally, in order to test on each object the validity of the PSF-deconvolved model obtained, we again convolve the PSF-deconvolved image by the PSF model (or reconvolved image), and compute the differences between the surface brightness profiles derived from the original and reconvolved images. We found that the differences between the original and the reconvolved profiles were less than 1σ in the surface brightness profiles up to the limiting radius in each case. Thus, we concluded that the applied PSF correction is robust and self-consistent.

2.4. Surface brightness profiles

We derived the surface brightness profiles by two different methods, depending on the inclination of the object. For the low

inclined objects we relied on the ellipse task from IRAF. We fixed the position angle and ellipticity of the ellipses to the mean values obtained with SExtractor in the galaxy disc on the original image, with the limiting threshold set at 1σ . By doing so, we avoid unstable solutions for the position angle and ellipticity, especially common in the outskirts, where the S/N ratio is low (see E08) and where we will be centring our attention. As a side effect, the innermost parts of the profiles (the first five or six pixels in radius) may be slightly biased towards lower values, but we discarded this region in the vast majority of the cases, so it does not affect our results. On the other hand, the nearly edge-on objects were analysed by using ISOFIT (Ciambur 2015). This task replaces the angular parameter that defines quasi-elliptical isophotes in polar coordinates for the eccentric anomaly. By doing this, ISOFIT provides more accurate modelling of galaxies with non-elliptical shapes, such as disc galaxies viewed edge-on, and thus recovers more accurate surface brightness profiles. We have used free position angle and ellipticity in this case.

In order to separate the edge-on objects from the rest of the sample, we have used the results from the 2D decomposition models performed previously for the deconvolution process. The Monte Carlo simulations that we performed on the GALFIT3.0 models provide the probability distribution for the axis ratio ($q = b/a$) of the disc component. We assumed an intrinsic axis ratio for the S0 galaxies of $q_0 \sim 0.25$ (Weijmans et al. 2014), with the exception of those objects with $q < 0.25$ where we used $q_0 = 0.1$, which is the lower limit of the q_0 distribution from Weijmans et al. (2014). We note that we apply this ratio only as a median value in order to

Fig. 5. *Left panel:* estimated K-correction for the $F775W$ filters to the R band as a function of z . It is important to highlight that the linear fit applies to the observed correlation of the S0 and E/S0 galaxies of the sample. The intensity levels of the linear fit represent the 1, 2 and 3 σ confidence regions of the fit. *Right panel:* stellar mass for the initial red sequence sample vs. z . Consult the legend in the figure for the morphological classification.

select objects with high inclinations, and it is not used to extract conclusions for single objects. The values of the inclination angle for each object are included in Table B.1. The median dispersion for these values are ± 3 degrees. We identify five objects with $q_0 < 0.25$ as nearly edge-on galaxies (SHARDS10000845, SHARDS10001727, SHARDS20000827, SHARDS20003134 and SHARDS20011817). In addition to these, after visual classification, we added SHARDS10002351 and SHARDS10003402 to the edge-on sample. For them, the surface brightness profiles have been derived with ISOFIT instead of ellipse, as commented above.

We defined the outer limit of the profile on the major axis as the outermost elliptical bin with an integrated intensity with $S/N > 3$. The 1 σ sky noise level was defined for each azimuthal bin as

$$\sigma_{\text{sky,bin}} = \frac{\sigma_{\text{sky,pixel}}}{\sqrt{N}} \quad (7)$$

where $\sigma_{\text{sky,pixel}}$ represents the standard deviation of the background, measured on the masked images and N is the number of pixels included in each radial bin. The sky noise for each ellipse is then combined by addition in quadrature with the intrinsic dispersion along the azimuthal direction for each ellipse. The upper and lower limits of the magnitude values have been calculated by performing Monte Carlo simulations of the final noise distribution for each bin. The median limiting magnitude for our profiles is $\mu_{F775W,\text{lim}} = 27.092^{+0.024}_{-0.032}$ mag arcsec $^{-2}$ (the uncertainties refer to the percentiles 84.1 and 15.6, equivalent to $\pm 1\sigma$ in a Gaussian distribution).

2.5. Photometric corrections

The rest-frame wavelength range for a filter varies as a function of z , so we need to apply a K-correction (Humason et al. 1956; Oke & Sandage 1968) to the photometry of our profiles. We

have performed the K-correction directly by estimating the variation of the colour between the apparent magnitude estimated from the fitted SED in the rest-frame filter we want to compare with (R band) and the observed magnitude in the $F775W$ filter. The rest frame (synthetic) R and the observed $F775W$ apparent magnitudes for each object of our sample are available at the Rainbow Database. Rest-frame magnitudes have been calculated by direct integration over the best-fit SED for each object (Pérez-González et al. 2013). In the left panel of Fig. 5 we show the K-correction derived for the S0 and E/S0 galaxies of our sample, as a function of z . It nearly follows a linear relation for S0 and E/S0 galaxies, which we have fitted by using 10 000 bootstrapping simulations of a least squares fit, resulting in:

$$R - F775W = 0.340^{+0.033}_{-0.042} - 1.619^{+0.065}_{-0.072} \cdot z, \quad (8)$$

with a Spearman correlation coefficient of $\rho = -0.838$, and a Pearson test probability $p < 2.2 \times 10^{-16}$. We calculate the K-corrections for each object by using the previous linear relation, which applies a median correction as a function of z . The final K-corrections for each object are shown in Table A.1 in Appendix 4 (the median uncertainty for $R - F775W$ is ± 0.060). Therefore, the final surface brightness profiles of our $0.2 < z < 0.6$ sample are in the rest-frame R band, as the available data on local Type-III S0s by E08 and G11.

In order to check the goodness of the Rainbow photometric redshift for our subsample of S0 and E/S0 galaxies at $0.2 < z < 0.6$, we have estimated the difference between the spectroscopic and the photometric redshifts for those objects where the former is available (47 out of the selected 50 S0 and E/S0 galaxies have spectroscopic redshift). We found an excellent overall agreement between the spectroscopic z and the photometric z with a median dispersion in our subsample of $\Delta z / (1 + z) = 0.0024$, meaning that the photometric z estimated in Rainbow from SED fitting are very good for the galaxies of our sample. A notable exception is the object SHARDS10000845 ($z_{\text{photo}} = 0.36$, but

$z_{\text{spec}} = 0.5123$). The spectroscopic redshift flag at the Rainbow Database is four, which means a very reliable value for z_{spec} . Nevertheless, this discrepancy does not affect the results, as the z_{spec} was used instead of the z_{photo} result in all the calculations when available. Only three S0 – E/S0 galaxies did not present available z_{spec} values (SHARDS10005029, SHARDS10008552 and SHARDS20011817). However, the two first cases were removed from the final sample (see the reasons in Sect. 2.2) and the last was finally classified as an S0 galaxy with a Type-I profile.

We corrected our profiles for Milky Way dust extinction too. To estimate the necessary corrections, we used the dust reddening maps from Schlegel et al. (1998), available through the NASA/IPAC Infrared Science Archive². We extracted the extinction factor $E(B - V)$ for each object at its position. We assumed a Landolt V band extinction in magnitudes $A_V = 3.315 \times E(B - V)$, and the ratio $A_{F775W}/A_V = 0.65$ (Fitzpatrick 1999; Indebetouw et al. 2005). We corrected for the calculated extinction correction for each object in the sample. The values obtained are available in Table A.1.

Finally, we have corrected the profile for cosmological dimming, which entails a factor $\Delta\mu = -10 \times \log_{10}(1 + z)$. We use the best z value for each object available in the Rainbow Database to perform this correction (see Table A.1).

2.6. Elbow: automated break analysis of disc surface brightness profiles

After the surface brightness profile calculation, we proceeded to classify the profiles into the three types described in Sect. 1, paying special attention to those objects showing a Type-III profile. We have performed this classification using two procedures: 1) simple visual classification and 2) an automated break analysis via an algorithm written by us in R³ (R Core Team 2016) that we called Elbow. Elbow accepts as input the surface brightness profile and the errors in both magnitude and position of each bin, as well as minimum and maximum radial limits for the analysis. The tasks of the programme are: 1) to estimate the best double exponential fit to a surface brightness profile and 2) to calculate the probability that the slopes of the inner and outer fitted profiles are statistically different. The algorithm works by carrying out Monte Carlo + bootstrapping simulations on the input profile, using the uncertainties provided by the user for each data point in both radius and magnitude. This is a two-step process. First, for each simulation, Elbow generates a new profile by random re-sampling with replacement (bootstrapping). This implies that the new profile contains the same number of points as the original one, but some points are not included in each simulation. Secondly, we replace each data point with the values from a Gaussian distribution with a mean value equal to the original data point and σ equal to the original error (Monte Carlo). This is done for both variables (r and μ). We take advantage of the combination of the bootstrapping and Monte Carlo methods in order to take into account the different uncertainties associated to each point and obtain an accurate probability distribution of the parameters at the same time. One of the main benefits of the re-sampling methods is to avoid any assumptions of normality on the sample and hence obtain a more accurate distribution for certain statistics. In addition, the shape of the resulting probability distributions for the parameters give us information about the presence of outliers and irregularities. This method of fitting

breaks in linear trends via bootstrapping was already tested in Cardiel et al. (1998) to detect changes in the slope of the line-strength gradients of Mg₂ and the $\lambda 4000$ Å break as a function of the galactocentric radius in central cluster galaxies, and more recently by Marino et al. (2016) to detect breaks in surface brightness profiles.

We have avoided the inner parts of the profile – which are dominated by the bulge emission – by using the bulge model fitted with the GALFIT3.0 and removing from the fit the section of the profile where the bulge dominates the emission over the exponential profile. For several objects this minimum limit was not enough to properly mask the central part of the profile (because of additional inner components), and it had to be set to a more restrictive and larger radius by visual inspection of the profile and the model decompositions. Similarly, we cut the profile of several objects before reaching the limiting radius, due to the presence of irregularities or possible contamination sources that we wanted to avoid in the final profile fit.

For each simulation, Elbow minimises the residual distances of the input observational profile to a broken profile modelled as

$$\mu(r) = \begin{cases} \mu_{0,i} + \frac{2.5}{\ln(10)} \cdot \frac{r}{h_i} & \text{if } r < R_{\text{break}}, \\ \mu_{0,o} + \frac{2.5}{\ln(10)} \cdot \frac{r}{h_o} & \text{if } r > R_{\text{break}}, \end{cases} \quad (9)$$

$$R_{\text{break}} = h_i \cdot h_o \cdot \frac{\ln(10)}{2.5} \cdot \frac{\mu_{0,i} - \mu_{0,o}}{h_i - h_o} \quad (10)$$

hence we obtain the probability distribution of the characteristic parameters for both inner and outer profiles, as well as the R_{break} probability distribution. We estimate the maximum likelihood solution for h_i , $\mu_{0,i}$, h_o and $\mu_{0,o}$ (or best solutions) as the mode of the corresponding distribution. For each simulation, we calculate a value for R_{break} following Eq. (10). The best solution of R_{break} is defined as the value corresponding to the maximum likelihood solution for h_i , $\mu_{0,i}$, h_o and $\mu_{0,o}$. Thus, R_{break} is a dependent parameter of the inner and outer fits to the profile. In contrast to that, the corresponding μ_{break} values are calculated from the interpolation of the input profile at the break position $R = R_{\text{break}}$.

Elbow estimates the probability density distributions (PDDs, hereafter) as the distribution of each parameter resulting from the simulations ($\sim 100\,000$ in our case). We used these PDDs to estimate the central values of each distribution (maximum probability values, which is the mode of the distribution, as mentioned above) and the uncertainty intervals (for 1, 2 and 3σ). We also used these PDDs to estimate the probability that the inner and outer profiles are significantly different. That is:

$$H_{0,1}: h_i = h_o, \quad (11)$$

$$H_{0,2}: \mu_{0,i} = \mu_{0,o}. \quad (12)$$

Our null hypothesis is that the two profiles are not different, so that the inner slope and the outer slope would be the same ($H_{0,1}$) or that the central magnitude of the inner profile is compatible with that of the outer profile ($H_{0,2}$). Thus the probability for this test consists of two estimators: 1) the fraction of simulations that gave an $h_o > h_i$ in the case of a Type-III profile (and $h_o < h_i$ in the case of a Type-II profile) and 2) the fraction of simulations that gave $\mu_{0,o} > \mu_{0,i}$ in the case of a Type-III profile (and $\mu_{0,o} < \mu_{0,i}$ in the case of a Type-II profile). These two p -values are extremely consistent and in most cases they present equivalent or equal results (see Table B.1). We note that this test does

² <http://irsa.ipac.caltech.edu/applications/DUST/>

³ R: A language and environment for statistical computing <http://www.R-project.org>

not only take into account the presence of a noticeable excess of light in the outskirts of the galaxy, but it also would give negative results if this light distribution is not well fitted by a double exponential disc function. This was the case in several objects with irregularities in the outer regions of their profiles.

After that, we ran the simulations and identified those objects with significant breaks in their final profiles. Finally we visually checked the profiles and the fits, and classified all the objects in the three different classes (Type I, II or III). We assume a p -value of 10^{-2} as the limit value beyond to accept a profile as a Type III, which corresponds to a 99% confidence level that the PDDs of the characteristic parameters of the profile are not compatible with a Type-I profile. The same was applied for the Type-II profiles.

In Fig. 6 we show three examples of the final break analysis performed to the deconvolved profiles. The top panels show the composed RGB images of each object with the limiting radius indicated. The intermediate panels of Fig. 6 represent the corresponding surface brightness profile in the R band corrected for dust extinction, cosmological dimming and K -correction of each object. We plot those radial bins that were included in the final break fit. We systematically avoided the innermost regions due the dominant bulge emission. We plot the best fits to the inner and outer regions, along with the best R_{break} and μ_{break} respectively, with their 1σ confidence regions, also indicated. The best results obtained for the inner and outer fitted profiles along with their respective confidence intervals are indicated in the intermediate panels.

For the profile of the object in the first column of panels of Fig. 6 (SHARDS20002966) the confidence regions of the inner outer profiles completely overlap (see the left bottom panel). The p -value associated with this profile is $p = 0.224$, so the null hypothesis is not discarded and therefore, we do not find any difference between the inner and outer profiles, meaning that this galaxy has a Type-I profile. On the contrary, SHARDS10000845 (second column of panels) presents a clear Type-II profile. The associated p -value calculated with Elbow for this profile is $p = 3.4 \times 10^{-4}$, thus we can discard the null hypothesis and the break is statistically significant. A clear Type-III case is SHARDS10000327 (see the third column of panels in Fig. 6). The associated p -value for this Type-III break is $p = 3.0 \times 10^{-4}$, thus the break is statistically significant. The lower row of panels of Fig. 6 represents the 2D probability distribution (PDD) of the scale-length h and central surface brightness μ_0 for the three cases. The colour scale is linear and represents density of solutions of both inner ($\mu_{0,i}$, h_i) and outer profiles ($\mu_{0,o}$, h_o) in an arbitrary scale. These 2D histograms represent where the fitted solutions concentrate for each profile, in order to find the best central surface brightness and scale-length. In the case of SHARDS10000327 and SHARDS10000845 (which present a clear break) the solutions converge on a bimodal distribution with two maxima, marked with black crosses. On the contrary, the PDD of SHARDS20002966 only presents one clear maximum, meaning that it is a Type-I profile.

In Fig. 7 we show the PDDs for each parameter of the surface brightness profile of SHARDS10000327 (h_i , h_o and R_{break} in the upper row, and $\mu_{0,i}$, $\mu_{0,o}$ and μ_{break} in the lower row). We show the maximum likelihood solution for h_i , $\mu_{0,i}$, h_o and $\mu_{0,o}$. The PDD for R_{break} shows the solution derived from these best-fit parameters following Eq. (10). Finally, we show the corresponding PDD for the μ_{break} measured over the surface brightness profile with the best fit solution marked also with a vertical dashed-dotted line. As detailed before, SHARDS10000327 shows a Type-III surface brightness profile. This causes that the

PDD for h_i is centred at a lower value than the PDD for h_o . An analogous result is found for $\mu_{0,i}$ and $\mu_{0,o}$. As a consequence of this, the histograms for R_{break} and μ_{break} show single-peaked and Gaussian-like PDDs, meaning that the break is well-defined and statistically significant.

The best fitting results for the 44 S0 and E/S0 galaxies at $z < 0.6$ within our sample, along with the confidence intervals and p -values, are available in Table B.1.

2.7. Efficiency and reliability of the PSF correction

We also tested the reliability and efficiency of the PSF correction process by including synthetic images of galaxies with intrinsic exponential profiles into the GOODS-N image convolved with our PSF. After that, we analysed the type of profile which is recovered following the same procedure that we have used with real ones. To do this, we generated nine synthetic galaxy models with bulge + pure Type-I exponential discs. We chose three different size ranges: small, medium and large, with $R_{\text{eff,bulge}} = 0.06, 0.12$ and 0.18 arcsec and $h = 0.24, 0.42$ and 0.6 arcsec respectively. We used three different inclinations (0° , 45° and 90°) in order to test the variation of the PSF effects and the dependence of the result of the deconvolution with disc inclination. The models were generated with GALFIT3.0.

The synthetic images were generated by convolving the models created with GALFIT3.0 with our PSF model (see Sect. 2.3). After this, we included the resulting image in a region free of detections in the GOODS-N mosaic. We took into account: 1) the possible presence of background sources not resolved or with low S/N ratio that were not detected in the masking process; and 2) the noise distribution, which had to be similar to the one in the real images. We did not find any differences with the results described next when a pure Gaussian noise distribution was added to the images, which indicates that the sky level and the background sources were not affecting our profiles. After the synthetic galaxies are generated, we used the same procedure as in the case of the real images (see Sects. 2.4–2.6).

In Fig. 8 we show the surface brightness profiles of our synthetic Type-I models convolved (analogous to our original data) and not (i.e., the real profile) by the PSF of our data, and the surface brightness profiles of the deconvolved images, meaning the profiles recovered after using the same extraction and analysis procedures as in our real data. We also plot the radius at which $S/N = 3$. The surface brightness profiles of the PSF-affected models present clear excesses in the outskirts compared to the real (non-affected by the PSF) profiles, which systematically increases the radial region where the object has a $S/N > 3$. The main result is that, after the PSF correction, we successfully remove or reduce most of the scattered light, reconstructing the real shape of the profiles in the centre at the same time (see the differences between the real, original Type-I profiles and those recovered by our procedure in the corresponding subpanels, as a function of radius).

We also used Elbow to analyse whether the PSF wings can create apparent Type-III profiles in the synthetic Type-I galaxies that we have simulated. This test was also useful as a benchmark to test Elbow on a synthetic model. The results of the analysis are summarised in Table 1. In the table we show the p -values associated with the likelihood of each surface brightness profile to be well-represented by a single exponential profile. We find that:

- The amount of light scattered by the PSF to the outskirts of the synthetic objects is generally small, but it is detectable as

a break by Elbow in PSF-uncorrected profiles (especially in the face-on and 45° inclination cases of the small objects).

– The PSF deconvolution procedure efficiently removes the scattered light in the outskirts and recovers the inner profile at the same time.

Fig. 7. Probability density distributions of the surface brightness profile fit for the Type-III S0 galaxy SHARDS10000327. *Upper row, from left to right:* scale-length for the inner disc profile h_i (kpc), scale-length for the outer profile h_o (kpc), break radius R_{break} (kpc). *Lower row, from left to right:* central surface brightness profile of the inner profile $\mu_{0,i}$ (mag arcsec $^{-2}$), central surface brightness profile of the outer profile $\mu_{0,o}$ (mag arcsec $^{-2}$), surface brightness at the break radius (μ_{break}). The dashed-dotted lines represent the best solutions for each parameter, and the dotted lines mask the limits of the 68% (1σ) confidence region.

Table 1. Likelihood (p -values) for the surface brightness profiles of the synthetic models, so that the PSF uncorrected images and the deconvolved models present a Type-I (pure exponential) profile.

Orientation	PSF	Large	Medium	Small
Face-on	Uncorrected	0.105	0.010	6×10^{-4}
	Deconvolved	0.199	0.499	0.120
45°	Uncorrected	0.119	0.013	2×10^{-4}
	Deconvolved	0.489	0.185	0.079
Edge-on	Uncorrected	0.009	0.131	0.085
	Deconvolved	0.365	0.230	0.496

Notes. The small, medium and large models present $R_{\text{eff,bulge}} = 0.18$, 0.12 and 0.06 arcsec and $h = 0.6$, 0.42 and 0.24 arcsec respectively. The models were deconvolved following the procedure described in Sect. 2.3, and analysed with Elbow.

Consequently, the deconvolved images are completely free of misclassified Type-III profiles in all ranges of sizes and orientations due to PSF effects. We can therefore conclude that the procedure that we have followed for extracting and correcting the surface brightness profiles for PSF effects is reliable and efficient for recovering the real profiles.

2.8. AGN in the initial sample

We detailed in the previous sections that the deconvolution procedure relies on the fact that the light distribution of the objects is sufficiently well approximated by a certain analytical function (in our case, different combinations of Sérsic profiles). For galaxies hosting a powerful active galactic nucleus (AGN), this may not be the case. The light distribution of the central regions of AGN host galaxies may be much brighter than those with no AGN emission. As a consequence of this, we may be systematically underestimating the PSF contribution in the outskirts.

Alexander et al. (2003) have identified X-ray emitters in the Chandra Deep Field North, which covers the entire GOODS-N field. They detected 503 sources in 7 X-ray bands between 0.5–8 keV. Barger et al. (2003) found optical and infrared counterparts for the objects identified by Alexander et al. (2003). In Bauer et al. (2004), the authors classified the 504 objects in the categories AGN, star-forming galaxies and Galactic stars by using their optical spectral classifications, radio morphologies, variability, X-ray-to-optical flux ratios, X-ray spectra and their intrinsic luminosities. In order to take into account the presence of AGN in our sample, we have cross-correlated our initial red sample with the AGN catalogues in GOODS-N. We used the optical coordinates from Barger et al. (2003) to find the matching sources within 1 arcsec of separation.

We found nine matching sources, four of which are classified as star-forming galaxy candidates (SHARDS10001344, SHARDS20000827, SHARDS20002935 and SHARDS20003134) and five of them classified as AGN

Fig. 8. Surface brightness profiles of the synthetic images of galaxies: *Top panels:* $i = 0^\circ$. *Middle panels:* $i = 45^\circ$. *Bottom panels:* $i = 90^\circ$. *Left column:* large sized model. *Middle column:* medium sized model. *Right column:* small sized model. Blue dashed profile: non-PSF affected surface brightness profile (real profile). Red dashed-dotted profile: PSF-affected surface brightness profile (analogous to our original uncorrected data). Black solid profile: PSF-corrected surface brightness profile. The vertical solid lines represent the limiting radius of each profile (solid black line: PSF-corrected profile, dashed blue line: non-PSF affected model profile, dashed-dotted red line: PSF-convolved model profile). *Lower panels:* black dotted line differences between the non-PSF affected and the corrected surface brightness profile. Dashed line differences between the non-PSF affected and the PSF affected surface brightness profile.

(SHARDS10000827, SHARDS20002147, SHARDS20003119, SHARDS20003377 and SHARDS20004440). All nine sources are S0 or E/S0s in our classification, with the exception of SHARDS20003119, which was classified as a red spiral by us. The maximum distance between the matching sources in the Rainbow catalogue and the optical coordinates was less than 0.3 arcsec and we did not find any other possible counterparts until we increased the matching radius to 5 arcsec, well above the precision of the astrometry.

The emission of a source smaller than the pixel size of the detector would create a 2D light distribution equal to the PSF, by definition. To account for the possible optical emission of the AGN in these objects, we have added a PSF component to their GALFIT3.0 model. Therefore, we fitted the AGN, the bulge

component and the disc as the sum of a PSF, a free Sérsic and an exponential ($n = 1$) Sérsic profile. The model fitting was performed inside out, starting from a PSF + free Sérsic profile for the inner regions and then adding the disc component once a stable solution was reached for the inner regions. In some cases, we needed to fix several parameters alternatively, such as total fluxes or the centres of the components. Finally, we inspected the residuals and the solution, paying attention to the innermost regions. Due to unavoidable degeneracies between the PSF and the bulge total flux as a result of the limited spatial resolution, we have flagged the AGN objects in our sample in Table B.1, although we have kept them in the final sample of S0–E/S0 galaxies.

Furthermore, the classification of 4 S0 galaxies by Bauer et al. (2004) as star-forming galaxies appears to be in

contradiction with the results from the SFR calculated using the data in the Rainbow Database (see Sect. 3.2). We checked ancillary data for each one of these objects for signs of star-formation.

SHARDS20000827 was included in the sample from [Treu et al. \(2005\)](#) (Table 1, ID 1267). These authors do not report any [OII] or [H δ] emission lines in a $S/N = 32.12$ spectrum and the galaxy was also classified as S0. This object was also studied in [Georgakakis et al. \(2007\)](#) (Table 1, ID 81). They do not find any IR emission excess above the stellar expectation. They pointed out that X-ray emission of this object may be due to hot gas and low mass X-ray binaries.

SHARDS10001344 was also classified as an IR-faint object in [Georgakakis et al.](#), (Table 1, ID 354). These authors propose a post-starburst classification (possibly due to a past merger event) as a cause for the observed X-ray emission, although the observed IR luminosity is compatible with those of early-type galaxies.

The observed wavelength of the H α emission line for SHARDS20002935 is $\lambda_{H\alpha} \sim 9677 \text{ \AA}$ ($z = 0.4745$), which is in the observable spectral window of the WFC3 grism in the NIR (G141). The Rainbow Database contains a G141 1D spectrum, which we analysed looking for any signs of emission lines. We found an H α emission line candidate at $\lambda = 9692 \text{ \AA}$, with a total flux of $f_{H\alpha} = 1.61^{+1.61}_{-0.82} \times 10^{-16} \text{ erg cm}^{-2} \text{ s}^{-1}$. This emission entails a total H α luminosity in of $L_{H\alpha} = 1.34^{+1.36}_{-0.69} \times 10^{40} \text{ erg s}^{-1}$. Assuming the expression given by [Kennicutt et al. \(1994\)](#):

$$SFR_{H\alpha} (M_{\odot} \text{ yr}^{-1}) = 7.9 \times 10^{-42} L_{H\alpha} (\text{erg s}^{-1}), \quad (13)$$

we estimate a $SFR_{H\alpha} = 1.06^{+1.07}_{-0.54} M_{\odot} \text{ yr}^{-1}$. This value is very similar to the total SFR obtained by the combination of the NIR and 2800 $\text{\AA}$ emission and thus compatible with a quiescent galaxy ($SFR = 3.05 M_{\odot} \text{ yr}^{-1}$ and $\log_{10} M/M_{\odot} = 10.92$, see Sect. 3.2).

The Team Keck Treasury Redshift Survey (TKRS, [Wirth et al. 2004](#)) has an available optical spectrum between 5000–10 000 $\text{\AA}$ of SHARDS20003134 (ID 4554). Simple visual inspection of the data was sufficient to discard any signs of emission lines associated with star formation.

Finally, [Ptak et al. \(2007\)](#) uses SED fitting procedures to estimate photometric redshift and separate galaxy types. According to their results the SEDs of SHARDS10001344, SHARDS20000827, SHARDS20002935 and SHARDS20003134 are compatible with those of early-type galaxies.

In conclusion, we have identified the objects and corrected the images and the profiles of the sources with possible AGN activity accounting for the central AGN light emission. In addition to this, the ancillary data studied supports our morphological classification, and confirms that the SFR levels of the objects included in our sample are compatible with those of early-type galaxies. Therefore, these four AGN with S0 morphology were finally kept in the final S0 – E/S0 sample.

3. Results and discussion

3.1. Statistics of the red galaxy sample by morphology

After the revision performed to the visual morphological classification by checking the images and the PSF-corrected surface brightness profiles, we find that, from the original sample of 150 red galaxies at $0.2 < z < 0.6$, 38 were finally classified as S0 (25.3%) and 12 as E/S0 (8.0%) – this is a total of 33.3% S0 and E/S0 objects in the red galaxy sample. Additionally, 40 sources

were classified as compact post-starburst objects (26.6%), 32 objects have been classified as diffuse objects (21.3%), nine objects present clear signs of being in interaction with others (6.0%), seven are classified as “green peas” (4.7%), nine objects have been confirmed as E galaxies (6.0%), and we have also identified three spiral galaxies.

The results of the morphological classification of the red galaxy sample selected at $0.2 < z < 0.6$ within the SHARDS catalogue in the GOODS-N field and the following physical parameters are presented in Appendix A: position (α, δ), morphological type, photometric redshift (z_{phot}), spectroscopic redshift when available (z_{spec}), stellar mass, SFR, rest-frame absolute magnitude in the Johnson V (M_V) and K_s bands (M_K), the extinction correction (A_{F775W}) and the median ($R - F775W$) colours used for K-correction. In conclusion, from 150 objects from the red sample we have removed 100 objects and we have obtained a final sample of 38 S0s and 12 E/S0s (50 objects in total) from which to search for Type-III disc profiles.

3.2. Star formation rates and masses as a function of the morphology

The right panel of Fig. 5 represents the stellar masses of the objects of the red sequence sample vs. their redshift. We have used different symbols according to the assigned morphology, to compare the properties of our selected subsample of 50 S0 and E/S0 with those of all galaxies in the initial red sequence sample. The objects classified within the well-resolved high-S/N morphological types (see Sect. 2.2) present stellar masses two orders of magnitude higher than the low-S/N counterparts. The S0 and E/S0 galaxies have stellar masses between 10^9 and $10^{11} M_{\odot}$.

One of the fundamental characteristics of the S0 galaxies is their low SFR in the discs, by definition. We have selected our initial sample by using a colour-colour diagram that isolates the objects in the red sequence, which are good candidates for having old stellar populations and no recent star formation episodes (see Sect. 2.2). In order to confirm their quiescence, we have used the available data in the Rainbow Database to ensure that the SFRs of the selected S0 and E/S0 objects are low, coherently with their morphological type. In Fig. 9 we represent the SFR (top panels) and the specific SFR, defined as $sSFR = SFR/M_{\star}$ (bottom panels) for the objects of the initial red sequence sample, as a function of z (left column) and the stellar mass ($M_{\star}$, right column). We show the typical values for the SFR of different morphological types in the local universe ([Thronson et al. 1989](#); [Young & Knezek 1989](#); [Young & Scoville 1991](#); [Caldwell et al. 1994](#); [Kennicutt 1998](#); [Sansom et al. 2000](#); [Wei et al. 2010a,b](#); [Amblard et al. 2014](#)). In the bottom panels we plot a conservative upper limit for the $sSFR$ in quiescent galaxies ($sSFR = 0.2 \text{ Gyr}^{-1}$, see [Domínguez Sánchez et al. 2016](#)), along with a higher value for this limit of quiescence ($sSFR = 0.32 \text{ Gyr}^{-1}$, see [Barro et al. 2013](#)). The procedure to estimate the total SFR from the UV emission at 2800 $\text{\AA}$ (caused by young stars) and the total IR emission between 8 and 1000 μm (caused by dust re-emission) is fully detailed in [Barro et al. \(2013\)](#), and references therein.

The data available in the Rainbow database do not provide direct SFR values for most of our objects. In fact, 129 out of 150 only have upper limits for the SFR (represented by down-pointing arrows, see the top panels in Fig. 9). We note that the observed correlation of the SFR upper limits is a systematic effect due to the detection limits in NIR and UV. Thus, for the objects at increasing z , we obtain higher upper limits. Nevertheless,

Fig. 9. SFR (top row) and sSFR (bottom row) for the objects of the initial red sequence sample, as a function of z (left column) and the stellar mass (right column), according to their morphological types. Arrows indicate upper limits for the SFRs. The horizontal dashed lines in the top panels represent the typical values for the SFR for different morphological types in the local universe (see references in the text). Note that these values change with z (see the text). The blue dash-dotted line and the green dashed line in the bottom panels correspond to two typical reference upper limits for the sSFR in early-type galaxies (see the text). Consult the legend in the figure for the morphological type.

this does not affect our aim, because we only needed to test whether the objects present low levels of star formation or not and the detection limits are low enough to do so. In the upper panels of Fig. 9, it is shown that the galaxies classified as S0 and E/S0 present SFR levels close to the typical values of local S0-Sa galaxies, as expected for the quiescent nature of S0s and E/S0s, corroborating the morphological classification that we have performed. Multiple studies indicate that galaxies were forming stars more actively in the past, regardless of their environment (Lilly et al. 1996; Schiminovich et al. 2005). The typical SFR of S0 and E/S0 galaxies increases from the local universe to $z = 0.8$ and it reaches values of $4 M_{\odot} \text{ yr}^{-1}$ at $z = 0.6$ (Menanteau et al. 2001). This is in good agreement with the SFR distribution of our S0 and E/S0 sample ($\langle SFR \rangle = 2.4^{+1.0}_{-1.9} M_{\odot} \text{ yr}^{-1}$).

We also show that the sSFR of those objects classified as S0 and E/S0 is lower than -or close to- the typical values usually considered as the upper limit to identify quiescent objects in the bottom panels of Fig. 9. The only object that presents an upper limit for the sSFR higher than the reference values is SHARDS20002889 ($SFR < 1.68 M_{\odot} \text{ yr}^{-1}$, $sSFR < 0.95 \text{ Gyr}^{-1}$, $\log_{10} M/M_{\odot} = 9.25$). Careful visual inspection of the images reveals a close bright galaxy in the $F435W$ band, which has a clumpy structure and could be a face-on spiral galaxy. Traces of star formation in the outskirts of our object by this spiral galaxy may be biasing the sSFR derived from Rainbow data towards higher values. We note that the objects classified as diffuse, green peas, and compact post-starburst galaxies show higher sSFR than the S0 and E/S0s, clearly above the limits of quiescence. Those

Fig. 10. Synthetic rest-frame absolute magnitude distribution of the objects in the red sample versus z , as a function of their morphological types. *Left panel:* Johnson V band rest-frame absolute magnitude. *Right panel:* K_s band rest-frame absolute magnitude.

objects present similar values for the total SFR as our S0s and E/S0s but much lower stellar masses, thus resulting in higher sSFR values.

In Fig. 10 we show the distribution of rest-frame absolute magnitudes in the Johnson V band and K_s band, as a function of their redshift and the morphological type. We find that the objects classified as S0 or E/S0 present absolute V band magnitudes between $-22 < M_V < -18$. Quiescent galaxies present colours with typical values of $(B - V) \sim 1.0$ (Kinney et al. 1996; Bell & de Jong 2001), so the objects classified as S0s and E/S0s in our sample, would present absolute magnitudes in the Johnson B band of $-17 > M_B > -21$. The available data on local Type-III S0 galaxies present a similar range of absolute magnitudes in the B band (Erwin et al. 2008; Gutiérrez et al. 2011), so the S0 and E/S0 galaxies in our sample at $0.2 < z < 0.6$ are analogous to those in the available local samples, enabling the direct comparison with them.

The right panel of Fig. 10 shows the same diagram as in the left panel, but for the rest-frame K_s absolute magnitude. We find that the S0 and E/S0 galaxies of our sample present values between $-19 > M_K > -23$. By using the stellar masses in the Rainbow database we find a mass-to-light ratio in the K band of $M/L_K = 0.68^{+0.43}_{-0.16} M_\odot/L_{K,\odot}$. Assuming $(B - V) \sim 1.0$, Bell et al. (2003) predict a mass-to-light ratio in the K_s band of $M/L_K \sim 0.85 M_\odot/L_{K,\odot}$ for quiescent galaxies, which is compatible with the results found for the objects in our sample.

We conclude that the SFR and sSFR of the objects that we have identified visually as S0s and E/S0s are characteristic of quiescent objects at the corresponding redshifts of each galaxy, therefore supporting our morphological classification.

3.3. Types of disc profiles in the S0 sample

We created GALFIT3.0 models for 44 objects from the sample of 50 S0 and E/S0s ($\sim 88\%$). We discarded the six remaining objects because they presented an apparent size too small and/or a GALFIT3.0 solution too unstable for a bulge+disc model

(SHARDS10001928, SHARDS10002901, SHARDS10005029, SHARDS10008552, SHARDS20000858, SHARDS20004273). The presence of significant breaks in the S0 – E/S0 sample was confirmed quantitatively by Elbow. Using automatic fitting classification, we classified the galaxies into three types: Type I (23 objects, 52% of the sample), Type II (seven objects, 16% of the sample) and Type III (14 objects, 32% of the sample).

Due to the limiting depth of the observations, we find three different cases where a Type-III profile may be detectable by the automated break analysis routine Elbow:

1. The outer profile is clearly resolved, usually associated with bright values of the μ_{break} and low p -values of Elbow (e.g., SHARDS10000327).
2. The outer profile is not clearly resolved, because it presents low values of the h_o/h_i ratio or dimmer values of the μ_{break} , that usually result in smaller detectable radial zones to fit (e.g. SHARDS10003647).
3. The anti-truncation is observed on a bright region, but the outer profile presents irregularities or is not well represented by an exponential disc (e.g., SHARDS10001344).

In order to estimate the effects of the PSF on the profiles, we also analysed the original profiles without the PSF correction. We found that 6 anti-truncations detected in PSF-uncorrected images were removed from the profiles after the PSF correction (SHARDS10001269, SHARDS20002147, SHARDS20003377, SHARDS20003678, SHARDS20004440, and the apparent hybrid Type II+III profile, SHARDS10001847, which resulted to be a simple Type-II profile). Two Type-I profiles were classified as Type-II after the PSF subtraction (SHARDS10004777 and SHARDS20002995). None of the Type-II profiles was classified as Type I or Type III after PSF correction. Due to the shape of the PSF – that disperses light from the brighter and (almost always) inner parts of a source – this was an expected result, given that it is extremely unlikely for any object to present more light in the outskirts after PSF deconvolution.

Finally, we report that 14 out of a final sample of 44 S0 and E/S0 galaxies present anti-truncated surface stellar profiles once corrected for PSF effects. As explained above, this final sample of 44 objects only includes those S0 and E/S0 galaxies that were successfully corrected from PSF effects through 2D modelling and were not contaminated by FoV objects. We note that the p -values for the break test in SHARDS20003134 present very different values ($p_h = 2.0 \times 10^{-2}$ and $p_{\mu_0} = 7.6 \times 10^{-4}$). The profile clearly shows a Type-II break, although with an irregular inner profile, which could be the cause of the lack of agreement in this case. 13 out of the 14 the Type-III objects have z values equal or higher than 0.4, with the exception of SHARDS20000593, which has a spectroscopic redshift of $z = 0.247$. The lack of objects at the lower redshift range is expected since the 82.6% of the S0 and E/S0 sample have redshifts higher than $z = 0.4$. This means that we find a fraction of $\sim 30\%$ of Type-III profiles in S0 and E/S0 galaxies at $0.4 < z < 0.6$. This fraction of Type-III profiles from the total S0 and E/S0 sample is slightly lower than the observed ratio of Type-III profiles in local S0 and E/S0 galaxies in E08 and G11 ($\sim 50\%$), but compatible to the ~ 20 – 30% detected in Laine et al. (2014, 2016).

The final profile classification is available in Table B.1. Comments on individual objects, RGB images and the piecewise fits to the PSF-corrected disc surface brightness profiles of the 44 S0 and E/S0 galaxies in our PSF-corrected sample are available in Appendix C.

Finally, we compare the surface brightness profiles of the identified Type-I galaxies with the surface brightness profiles of the Type-II and Type-III galaxies from our sample. We fit single exponential profiles to the Type-I profiles and estimate their values of scale length h and central surface brightness μ_0 . We found a median value for the scale length of the Type-I galaxies of $h = 1.69^{+0.42}_{-0.29}$ kpc, and the central surface brightness of $\mu_0 = 18.65^{+0.39}_{-0.14}$ mag arcsec $^{-2}$. In contrast, the median values for the scale-lengths of Type-II profiles are $h_i = 3.15^{+0.00}_{-0.27}$ kpc and $h_o = 2.23^{+0.09}_{-0.12}$ kpc, and $\mu_{0,i} = 17.92^{+0.96}_{-0.15}$ mag arcsec $^{-2}$, $\mu_{0,o} = 16.84^{+0.56}_{-0.48}$ mag arcsec $^{-2}$ for the central surface brightness. In the case of Type-III profiles, these values are $h_i = 1.94^{+0.21}_{-0.34}$ kpc and $h_o = 3.31^{+0.13}_{-0.61}$ kpc, and $\mu_{0,i} = 18.19^{+0.20}_{-0.28}$ mag arcsec $^{-2}$, $\mu_{0,o} = 20.21^{+0.10}_{-0.43}$ mag arcsec $^{-2}$ for the central surface brightness (see Table 2). As before, the median values were estimated by 50.000 1σ bootstrapping + Monte Carlo simulations. In Fig. 11 we show the distribution of the central surface brightness μ_0 vs. scale-length h for each profile type. We have represented the inner and outer profile parameters by separate in the case of Type-II and Type-III galaxies. We found an overall agreement between the distributions of the inner parts from the Type-III profiles and the same parameters from Type-I profiles, which is not observed in the outer Type-III profiles or in the Type-II profile parameters. We conclude that the profiles of the Type-I S0 and E/S0 galaxies in our sample at $0.2 < z < 0.6$ have values for the characteristic parameters more similar to the inner discs of the Type-III galaxies than those of the outer profiles of Type-III galaxies (see Table 2).

3.4. Comparison of anti-truncated discs of S0 galaxies at $0.2 < z < 0.6$ with local analogs

In Fig. 12 we show the distributions of the characteristic parameters of the Type-III surface brightness profiles of our sample of S0 and E/S0 galaxies at $0.2 < z < 0.6$, compared to those of local Type-III S0 galaxies by E08 and G11. This local sample consists

Fig. 11. Central surface brightness μ_0 vs. scale-length h diagram showing the distribution of the Type-I, Type-II and Type-III profile parameters. See the legend for details.

Table 2. Median values of the structural and photometric parameters fitted to Type-III profiles of real S0s.

Parameter			$z \approx 0$	$0.2 < z < 0.6$
a)	$\langle R_{\text{break}} \rangle$	[kpc]	$7.8^{+1.1}_{-1.1}$	$7.88^{+1.10}_{-0.98}$
b)	$\langle h_i \rangle$	[kpc]	$1.96^{+0.49}_{-0.13}$	$1.94^{+0.21}_{-0.34}$
c)	$\langle h_o \rangle$	[kpc]	$3.58^{+0.21}_{-0.83}$	$3.31^{+0.13}_{-0.61}$
d)	$\langle \mu_{\text{break}} \rangle$	[mag arcsec $^{-2}$]	$24.30^{+0.50}_{-0.10}$	$22.68^{+0.17}_{-0.32}$
e)	$\langle \mu_{0,i} \rangle$	[mag arcsec $^{-2}$]	$19.59^{+0.52}_{-0.25}$	$18.19^{+0.20}_{-0.28}$
f)	$\langle \mu_{0,o} \rangle$	[mag arcsec $^{-2}$]	$21.60^{+0.27}_{-0.30}$	$20.21^{+0.10}_{-0.43}$

Notes. *Left column:* values for the samples on the local Universe (E08, G11). *Right column:* Values for the sample at $0.2 < z < 0.6$. *Rows from top to bottom:* a) Break radius R_{break} (kpc); b) inner profile scale length h_i (kpc); c) outer profile scale length h_o (kpc); d) surface brightness at the break radius μ_{break} (mag arcsec $^{-2}$); e) central surface brightness of the inner profile $\mu_{0,i}$ (mag arcsec $^{-2}$); f) central surface brightness of the outer profile $\mu_{0,o}$ (mag arcsec $^{-2}$).

20 antitruncated S0 – E/S0 galaxies. Thus the sample size is low but comparable to our own ($N = 14$). The median values of each distribution are shown with solid vertical lines. The top panels represent the distribution of the structural parameters (R_{break} , h_i and h_o), and the lower panels represent the distribution of the photometric parameters (μ_{break} , $\mu_{0,i}$ and $\mu_{0,o}$). The median values of the distributions for each parameter, for both samples, are summarised in Table 2, and were estimated by 50.000 1σ Monte Carlo + bootstrapping simulations.

The distributions of the structural parameters R_{break} , h_i , and h_o in the top panels of Fig. 12 are very similar for the local and our $0.2 < z < 0.6$ sample, showing compatible median values (see also Table 2). We use the Anderson-Darling criterion (Scholz & Stephens 1987) in order to test whether the parameters from both samples arose from a common unspecified distribution function (null hypothesis). The results indicate that there are no noticeable differences between the distributions of the structural parameters (the p -values are $p = 0.463$ for R_{break} ,

Fig. 12. Normalised distributions of the structural and photometric parameters of the Type-III breaks of the our sample of S0 and E/S0 at $0.2 < z < 0.6$, compared to those from the local universe (E08 and G11). *Upper row, from left to right:* break radius R_{break} (kpc), scale-length of the inner disc profile h_i (kpc), scale-length of the outer profile h_o (kpc). *Lower row, from left to right:* surface brightness at the break radius μ_{break} (mag arcsec $^{-2}$), central surface brightness of the inner disc profile $\mu_{0,i}$ (mag arcsec $^{-2}$), central surface brightness of the outer profile $\mu_{0,o}$ (mag arcsec $^{-2}$). The red solid histogram marks our sample of Type-III S0 and E/S0 galaxies at $0.2 < z < 0.6$. The blue dashed histogram represents the distributions found for local universe sample from data by E08 and G11.

$p = 0.243$ for h_i and $p = 0.542$ for h_o). We found that our sample at $0.2 < z < 0.6$ shows lower maximum values of h_o (i.e., the largest outer profile scale length in the local sample has a value $h_o = 22.26$ kpc, while the maximum of the our higher redshift sample is $h_o \sim 7$ kpc). Similarly, the outermost break of the local sample presents a $R_{\text{break}} = 18.6$ kpc compared with the maximum value $R_{\text{break}} = 10.89^{+3.44}_{-0.44}$ kpc of the sample at $0.2 < z < 0.6$. This could be for two reasons: 1) the local sample contains deeper data than ours at $0.2 < z < 0.6$, and therefore, we could be losing the outermost parts of the corresponding analogs at $z \sim 0.5$; or 2) the profiles of the local sample with such large values of R_{break} and h_o could be affected by diffuse PSF tails that were misidentified with real Type-III profiles, because these authors did not correct for PSF effects. Nevertheless, we note that the Anderson-Darling test did not find any noticeable differences between the general distributions of the structural parameters, thus the impact of these effects would require to be tested with larger samples. We also note that the Type-III S0 with the largest R_{break} from the sample at $0.2 < z < 0.6$ is also the only edge-on S0 galaxy with a Type-III profile.

The lower panels of Fig. 12 show the distributions of μ_{break} , $\mu_{0,i}$ and $\mu_{0,o}$. Contrary to the structural parameters, the photometric parameters of the two samples do not give either compatible distributions or median values. We apply again the

Anderson-Darling criterion to test whether the parameters from both samples arose from a common parent sample. The p -values are $p = 6.9 \times 10^{-3}$ for μ_{break} , $p = 4.4 \times 10^{-3}$ for $\mu_{0,i}$ and $p = 3.1 \times 10^{-3}$ for $\mu_{0,o}$. The results indicate that there are noticeable differences between the distributions of the photometric parameters of the samples of Type-III S0-E/S0 galaxies at $0.2 < z < 0.6$ when comparing to the local sample. The μ_{break} , $\mu_{0,i}$ and $\mu_{0,o}$ values of the sample at $0.2 < z < 0.6$ are brighter than the local sample by ~ 1.5 mag arcsec $^{-2}$ ($\Delta\mu_{\text{break}} = -1.61^{+0.33}_{-0.53}$ mag arcsec $^{-2}$, $\Delta\mu_{0,i} = -1.40^{+0.39}_{-0.56}$ mag arcsec $^{-2}$, $\Delta\mu_{0,o} = -1.49^{+0.46}_{-0.46}$ mag arcsec $^{-2}$). Deeper surface brightness profiles and a possible PSF contribution could possibly explain this result. But, in any case, we expect a general brightening of the surface brightness profiles of galaxies with increasing z , due to the stellar population evolution, which could also explain this difference (see Bruzual & Charlot 2003; Tapia et al. 2017, and references therein).

3.5. Effects of the PSF on the profiles

In order to test the effects of the scattered light on the surface brightness distribution, we have analysed the profiles of the original images without the PSF correction and compared them with the PSF-corrected profiles. In Fig. 13 we compare the results of

Fig. 13. Comparison between the PSF corrected and non-corrected values of the structural and photometric parameters of the Type-III S0 and E/S0 at $0.2 < z < 0.6$ sample. *Upper row, from left to right:* decimal logarithm of the ratio between the PSF corrected structural parameters and the same parameters measured on the original profile: break radius R_{break} (kpc), scale-length of the inner profile h_i (kpc), scale-length of the outer profile h_o (kpc). *Lower row, from left to right:* differences between the PSF corrected structural parameters and the same measured on the original profile: surface brightness at the break radius μ_{break} (mag arcsec $^{-2}$), central surface brightness of the inner profile $\mu_{0,i}$ (mag arcsec $^{-2}$), central surface brightness of the outer profile $\mu_{0,o}$ (mag arcsec $^{-2}$). The black dashed vertical line represents the ratio or difference where the PSF correction would not have any effect.

the structural and photometric parameters of the Type-III profiles in our S0 and E/S0 sample before and after being corrected by PSF contribution. The histograms in the upper row show the decimal logarithm of the ratio of the R_{break} , h_i and h_o values measured on the corrected profiles over those parameters measured on the uncorrected profiles. We plot the value that would result if the PSF did not have any effect on the observed structure. We found that h_o can have significantly higher values in the uncorrected profiles than in the PSF-corrected ones ($\Delta h_o = h_{o,\text{corr}} - h_{o,\text{uncorr}} = -0.37^{+0.33}_{-0.37}$ kpc). Thus, the dispersed light can increase systematically the outer profile scale length. This also happens with the distribution of h_i ($\Delta h_i = -0.105^{+0.082}_{-0.083}$ kpc) although the results are less significant. In contrast, the distribution of ratios of R_{break} does not show any clear bias ($\Delta R_{\text{break}} = -0.087^{+0.54}_{-0.55}$ kpc).

In the lower panels of Fig. 13, we represent the differences between the values of μ_{break} , $\mu_{0,i}$ and $\mu_{0,o}$ measured on the profiles corrected for PSF effects and the original (uncorrected) ones. Again, the dashed lines represent the position in a case in which the dispersed light did not have any effect on our profiles. We do not find any systematic effect in their distributions ($\Delta \mu_{\text{break}} = 0.16^{+0.23}_{-0.23}$ mag arcsec $^{-2}$, $\Delta \mu_{0,i} = -0.07^{+0.11}_{-0.11}$ mag arcsec $^{-2}$, $\Delta \mu_{0,o} = -0.10^{+0.25}_{-0.26}$ mag arcsec $^{-2}$). In conclusion, the inner and outer disc scale-lengths are the parameters that are most affected by the PSF scattered light.

4. Conclusions

We present the first sample of S0 and E/S0 galaxies with anti-truncated discs obtained beyond the local Universe (at $0.2 < z < 0.6$), on the basis of PSF-corrected surface brightness profiles. We have described in detail the selection procedure and analysis performed to characterise them on a sample of 150 red galaxies at $0.2 < z < 0.6$ on the GOODS-N field, by using both HST/ACS and SHARDS data from the Rainbow database. We have selected a sample of quiescent disc galaxies with visual S0 and E/S0 morphologies, and studied their SFRs, sSFRs, stellar masses and their surface brightness profiles. Additionally, we have corrected for PSF-scattered light in their $F775W$ images, to obtain surface brightness profiles unbiased by the light dispersion produced by the PSF of our data.

To estimate the break parameters accurately and perform a quantitative morphological classification of the surface brightness profiles, we have developed *Elbow*, a programme to detect, classify and fit breaks in surface brightness profiles, which we have made publicly available. We identified S0 and E/S0 objects at $0.2 < z < 0.6$, with exponential (Type I), truncated (Type II) and anti-truncated (Type III) profiles and fitted their different disc components with exponential functions. We compared the structural and photometric parameters from the sample of Type-III galaxies in the range $0.2 < z < 0.6$ with the local samples

from previous studies (E08 and G11). Our main results are the following:

1. We report the first sample of Type-III profiles in S0 and E/S0 galaxies at $0.2 < z < 0.6$, corrected for PSF effects. We found that 14 out of 44 S0-E/S0 galaxies at $0.2 < z < 0.6$ after PSF corrections have antitruncated profiles ($\sim 30\%$). This fraction is similar to the those reported in the local Universe by Laine et al. (2014, 2016).
2. As a result of correcting the profiles for scattered light by the PSF, we found that $\sim 25\text{--}30\%$ of the apparent Type-III S0 discs detected in uncorrected profiles are false positives and can be explained by a combination of pure exponential profiles and scattered light from the inner regions. In two cases, we found significant down-bending breaks (Type-II profile) after the PSF deconvolution.
3. The structural parameters (R_{break} , h_i and h_o) of the Type-III profiles at $0.2 < z < 0.6$ present similar distributions to their local counterparts. In contrast, the photometric parameters (μ_{break} , $\mu_{0,i}$ and $\mu_{0,o}$) have values $\sim 1.5 \text{ mag arcsec}^{-2}$ brighter than the local sample from E08 and G11.
4. The PSF-dispersed light tends to increase the scale-lengths of the inner and outer disc profiles (h_i , h_o) in our sample of Type-III S0 and E/S0 galaxies, but it does not significantly affect either the central surface brightness values of the inner and outer discs ($\mu_{0,i}$, $\mu_{0,o}$) or the break location, R_{break} .
5. The profiles of Type-I of our S0 and E/S0 sample have characteristic values compatible with the inner profiles ($\mu_{0,i}$ and h_i) of Type-III S0 and E/S0 galaxies, but they are not consistent with the equivalent parameters ($\mu_{0,o}$ and h_o) of the outer profiles.

The wings of the PSF tend to create an apparent excess of emission in the outskirts of the galaxies. This tends to increase both h_i and h_o in Type-III profiles. For any study that does not take into account the effects of the PSF on the profiles, this will yield a systematic bias in the results. This applies not only to Type-III profiles, but also to Type-II profiles, as commented above. We also show that the PSF-corrected images recover some Type-II breaks, which were not detectable in the original images. Therefore; in PSF-uncorrected data, an unknown fraction of the real Type-II profiles may be softened to the point of being misclassified as Type-I by the observers.

In this work we have presented Elbow⁴, a statistically robust and automated method to fit, classify the surface brightness profiles and calculate the likelihood associated with a certain break to exist (Types II and III) or not (Type I). This tool is free and we make it available for the scientific community. The non-linear nature of the surface brightness magnitudes demands a careful treatment of the uncertainties and error propagation, especially when measuring quantities in the low S/N regime. In order to properly account for the uncertainties associated with the surface brightness profiles, Elbow calculates the errors using non-parametric statistics, such as the bootstrap resampling and the Monte Carlo method. Future studies may analyse what percentage of the reported surface brightness profiles have been previously misidentified due to the lack of an appropriate statistical method. Moreover, the results from the present and other recent studies (such as Sandin 2014; Trujillo & Fliri 2016, and references in Sect. 1) demonstrate that the PSF corrections are clearly necessary in this sort of studies, especially when working with low surface-brightness Type-III profiles.

⁴ Elbow is publicly available at GitHub (<https://github.com/Borlaff/Elbow>)

According to the results presented here, the structure of the Type-III profiles of S0 galaxies at $0.2 < z < 0.6$ appears to be similar to the local ones. Nevertheless, the $\mu_{0,i}$, $\mu_{0,o}$ and μ_{break} have brighter values than the local sample by $\sim 1.5 \text{ mag arcsec}^{-2}$. This could be due to one or several of the following reasons:

1. The difference may be due to the evolution of the stellar populations. This is expected to produce general brightening of the surface brightness profiles of galaxies with increasing z , sufficient to explain the difference between the samples (see Bruzual & Charlot 2003; Tapia et al. 2017, and references therein).
2. Due to the observational depth limit in the surface brightness, we could be biased to the innermost (and thus brighter) Type-III breaks. Nevertheless, we think this effect is negligible in our sample, because the R_{break} , h_i and h_o distributions of our $0.2 < z < 0.6$ S0 and E/S0 galaxies are highly compatible with those of the local sample, and only differ for the high values.
3. The local sample studies traditionally have not corrected for PSF effects. The wings created by the PSF tend to create Type-III profiles with dimmer values of $\mu_{0,o}$ and larger values of h_o . Still, although the scattered light may introduce systematic biases in the results – especially in the h_o values – it is highly unlikely that most Type-III profiles in the current local samples have been dramatically modified (or produced) by the PSF effects alone.

Recent papers have thrown doubt on the real nature of some Type-III profiles, attributing them to central light scattered radially outwards by the PSF of the telescope optics. Here we have carried out a successful detailed procedure to correct this effect from a large sample of objects and get unbiased samples of discs with real breaks in their surface brightness profiles. As a result, we present the first sample of proven Type-III profiles of S0 and E/S0 objects beyond the local Universe, in the range $0.2 < z < 0.6$, and that will be analysed in detail in a forthcoming paper (Borlaff et al., in prep.).

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Appendix A: Global properties of the initial sample of galaxies on the red sequence at $0.2 < z < 0.6$ in the GOODS-N field

Table A.1. Properties of the initial red sample and morphological classification.

Number	SHARDS ID	α ($^{\circ}$)	δ ($^{\circ}$)	Morph type	z_{phot}	z_{spec}	$\log_{10}(M_{\star}/M_{\odot})$	SFR $M_{\odot}/\text{yr}$	M_V [mag]	M_K [mag]	A_{F775W} [10^{-2} mag]	$R - F775W$ [mag]
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)
1	SHARDS10000327	189.3624	62.2135	E/S0	0.46	0.4755	10.177 ± 0.073	-2.210	-19.42	-20.25	$-2.54^{+0.11}_{-0.17}$	-0.433
2	SHARDS10000478	189.3746	62.2169	E	0.52	0.5117	11.02 ± 0.10	-4.308	-21.27	-22.25	$-2.52^{+0.13}_{-0.15}$	—
3	SHARDS10000488	189.3237	62.2208	DF	0.38	—	8.73 ± 0.13	-0.595	-16.34	-17.45	$-2.564^{+0.086}_{-0.151}$	—
4	SHARDS10000536	189.4165	62.2231	CPSTB	0.23	—	8.31 ± 0.18	0.112	-14.58	-15.98	$-2.52^{+0.11}_{-0.13}$	—
5	SHARDS10000737	189.3396	62.2263	E	0.47	0.4747	11.188 ± 0.081	-3.615	-21.48	-22.72	$-2.54^{+0.11}_{-0.13}$	—
6	SHARDS10000762	189.3593	62.2297	S0	0.47	0.4742	10.755 ± 0.092	2.484	-21.16	-22.40	$-2.54^{+0.11}_{-0.13}$	-0.430
7	SHARDS10000827	189.4341	62.2329	S0	0.51	0.5116	10.223 ± 0.060	2.398	-20.56	-22.08	$-2.50^{+0.13}_{-0.13}$	-0.491
8	SHARDS10000840	189.4244	62.2330	E/S0	0.52	0.5118	10.901 ± 0.054	-2.725	-20.97	-21.95	$-2.52^{+0.13}_{-0.13}$	-0.493
9	SHARDS10000845	189.4441	62.2332	S0	0.36	0.5123	11.247 ± 0.062	4.570	-21.83	-22.82	$-2.50^{+0.13}_{-0.13}$	-0.493
10	SHARDS10000849	189.3590	62.2342	S0	0.47	0.4746	10.736 ± 0.084	-2.371	-20.63	-22.03	$-2.54^{+0.11}_{-0.13}$	-0.432
11	SHARDS10001013	189.2899	62.2399	S0	0.47	0.4753	10.793 ± 0.063	-1.976	-20.49	-21.73	$-2.59^{+0.11}_{-0.13}$	-0.433
12	SHARDS10001052	189.2839	62.2396	Sp	0.57	0.5639	11.091 ± 0.092	9.220	-21.52	-22.92	$-2.59^{+0.11}_{-0.13}$	—
13	SHARDS10001058	189.4457	62.2420	CPSTB	0.47	—	8.970 ± 0.100	-1.100	-16.90	-17.03	$-2.50^{+0.13}_{-0.13}$	—
14	SHARDS10001235	189.4768	62.2475	OM	0.38	0.4620	9.939 ± 0.080	-1.521	-18.81	-19.87	$-2.50^{+0.13}_{-0.13}$	—
15	SHARDS10001269	189.4690	62.2470	S0	0.51	0.5116	10.958 ± 0.074	-4.443	-21.61	-22.89	$-2.50^{+0.13}_{-0.13}$	-0.492
16	SHARDS10001314	189.2334	62.2486	S0	0.31	0.3215	9.662 ± 0.057	-0.510	-18.42	-19.50	$-2.586^{+0.108}_{-0.086}$	-0.183
17	SHARDS10001344	189.2860	62.2504	S0	0.57	0.5673	10.375 ± 0.086	-2.813	-20.19	-21.30	$-2.586^{+0.108}_{-0.086}$	-0.584
18	SHARDS10001350	189.4721	62.2483	S0	0.50	0.5106	10.935 ± 0.071	-4.234	-21.55	-22.83	$-2.50^{+0.13}_{-0.13}$	-0.492
19	SHARDS10001629	189.4774	62.2575	E	0.45	0.4566	10.846 ± 0.058	-1.869	-20.62	-21.86	$-2.50^{+0.13}_{-0.13}$	—
20	SHARDS10001648	189.4680	62.2582	S0	0.45	0.4540	10.501 ± 0.080	-1.874	-20.47	-21.75	$-2.50^{+0.15}_{-0.13}$	-0.397
21	SHARDS10001727	189.2911	62.2567	S0	0.22	0.2013	10.113 ± 0.046	-0.984	-19.62	-21.15	$-2.607^{+0.086}_{-0.086}$	0.014
22	SHARDS10001847	189.4818	62.2618	S0	0.46	0.4598	10.761 ± 0.096	2.576	-21.12	-22.40	$-2.50^{+0.13}_{-0.13}$	-0.408
23	SHARDS10001928	189.4598	62.2647	S0	0.44	0.4535	9.824 ± 0.055	-1.959	-19.48	-21.01	$-2.52^{+0.15}_{-0.15}$	-0.398
24	SHARDS10001971	189.4888	62.2633	E	0.46	0.4574	11.072 ± 0.088	3.896	-21.19	-22.43	$-2.50^{+0.13}_{-0.13}$	—
25	SHARDS10002351	189.5065	62.2742	S0	0.48	0.4834	10.483 ± 0.047	-1.745	-20.23	-21.51	$-2.48^{+0.15}_{-0.11}$	-0.446
26	SHARDS10002730	189.3097	62.2823	S0	0.44	0.4472	10.339 ± 0.062	-1.660	-20.11	-21.20	$-2.63^{+0.11}_{-0.11}$	-0.386
27	SHARDS10002769	189.4826	62.2824	E/S0	0.44	0.4417	10.539 ± 0.074	1.187	-20.06	-21.05	$-2.52^{+0.24}_{-0.15}$	-0.378
28	SHARDS10002901	189.3599	62.2869	E/S0	0.57	0.5642	10.23 ± 0.14	5.088	-19.73	-21.11	$-2.61^{+0.15}_{-0.15}$	-0.579
29	SHARDS10002942	189.3608	62.2871	S0	0.57	0.5644	10.77 ± 0.12	-4.363	-20.84	-21.80	$-2.61^{+0.15}_{-0.15}$	-0.578
30	SHARDS10003216	189.2486	62.3041	E/S0	0.49	0.4970	10.024 ± 0.059	-2.081	-19.28	-20.20	$-2.650^{+0.108}_{-0.086}$	-0.468
31	SHARDS10003299	189.1697	62.3019	DF	0.32	—	8.50 ± 0.20	-0.289	-15.19	-16.06	$-2.63^{+0.13}_{-0.13}$	—
32	SHARDS10003312	189.2352	62.3012	E/S0	0.49	0.4973	10.731 ± 0.084	-2.475	-20.54	-21.53	$-2.650^{+0.108}_{-0.086}$	-0.468
33	SHARDS10003402	189.4151	62.2974	S0	0.20	0.2133	10.817 ± 0.062	-1.592	-20.07	-21.31	$-2.59^{+0.17}_{-0.17}$	-0.007
34	SHARDS10003647	189.1583	62.2914	S0	0.56	0.5553	10.926 ± 0.068	-4.616	-21.11	-22.51	$-2.61^{+0.15}_{-0.15}$	-0.563
35	SHARDS10004066	189.3262	62.3433	E	0.25	0.2544	10.357 ± 0.052	0.649	-20.23	-21.76	$-2.69^{+0.17}_{-0.15}$	—
36	SHARDS10004234	189.3083	62.3435	E	0.53	0.5323	11.064 ± 0.061	5.750	-21.63	-22.58	$-2.71^{+0.15}_{-0.15}$	—
37	SHARDS10004423	189.3738	62.3263	Sp	0.32	0.3186	10.58 ± 0.41	1.968	-21.03	-22.37	$-2.65^{+0.15}_{-0.19}$	—
38	SHARDS10004592	189.3917	62.3270	E	0.27	0.2733	10.435 ± 0.070	1.140	-20.67	-22.01	$-2.65^{+0.22}_{-0.19}$	—
39	SHARDS10004719	189.3806	62.3472	GP	0.30	—	8.31 ± 0.30	-0.328	-14.58	-15.98	$-2.69^{+0.17}_{-0.22}$	—
40	SHARDS10004777	189.2822	62.3143	S0	0.24	0.2010	10.219 ± 0.041	1.133	-19.88	-21.41	$-2.67^{+0.11}_{-0.11}$	0.014
41	SHARDS10005029	189.2326	62.2485	E/S0	0.30	—	9.155 ± 0.069	-0.341	-17.45	-18.27	$-2.586^{+0.108}_{-0.086}$	-0.147
42	SHARDS10005391	189.4568	62.2852	CPSTB	0.23	—	8.614 ± 0.084	-0.161	-14.55	-15.82	$-2.54^{+0.22}_{-0.17}$	—
43	SHARDS10005533	189.3459	62.2152	CPSTB	0.46	—	8.58 ± 0.18	-1.399	-16.60	-17.03	$-2.54^{+0.11}_{-0.17}$	—
44	SHARDS10005598	189.3552	62.2282	DF	0.38	—	8.46 ± 0.18	-0.584	-15.81	-16.89	$-2.54^{+0.11}_{-0.13}$	—
45	SHARDS10006521	189.3817	62.2372	DF	0.46	—	9.04 ± 0.22	-1.208	-16.12	-16.98	$-2.54^{+0.11}_{-0.13}$	—
46	SHARDS10006744	189.4309	62.2823	CPSTB	0.22	—	7.51 ± 0.24	-0.327	-13.08	-14.03	$-2.56^{+0.19}_{-0.19}$	—

Notes. Columns: (1) ID sample. (2) ID SHARDS (release DR2 beta). (3) Right ascension (degrees). (4) Declination (degrees). (5) Morphological classification: E (elliptical), E/S0, S0, Sp (spiral), CPSTB (compact post-starburst), OM (ongoing merger), GP (green pea), DF (diffuse galaxy). (6) Photometric redshift. (7) Spectroscopic redshift (when available). (8) Decimal logarithm of the stellar mass. (9) Total SFR (from the emission in $24 \mu\text{m}$ and $2800 \text{ \AA}$ provided in the Rainbow database, following the procedure described in Barro et al. 2013). Negative values correspond to upper limits following the notation on the Rainbow Database (see Sect. 3). (10) Absolute synthetic rest-frame magnitude in Johnson V band from the Rainbow database (Sect. 2.5). (11) Absolute rest-frame synthetic magnitude in the K_s band from the Rainbow database (Sect. 2.5). (12) Milky Way extinction in the $F775W$ band (magnitudes). (13) Estimated K-correction for the $F775W$ filters to the Steidel R band for the redshift of each galaxy, considering the fit in Eq. (8) (see Sect. 2.5).

Table A.1. continued.

Number	SHARDS ID	α ($^{\circ}$)	δ ($^{\circ}$)	Morph type	z_{phot}	z_{spec}	$\log_{10}(M_{\star}/M_{\odot})$	SFR $M_{\odot}/\text{yr}$	M_V [mag]	M_K [mag]	A_{F775W} [10^{-2} mag]	$R - F775W$ [mag]
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)
47	SHARDS10006819	189.4873	62.2901	DF	0.25	–	7.92 ± 0.21	–0.167	–13.69	–14.93	$-2.52^{+0.24}_{-0.15}$	–
48	SHARDS10006931	189.4210	62.3015	OM	0.37	–	8.05 ± 0.23	–0.336	–14.66	–15.55	$-2.59^{+0.17}_{-0.17}$	–
49	SHARDS10007413	189.3688	62.3567	CPSTB	0.24	–	8.34 ± 0.21	–0.129	–14.61	–15.53	$-2.71^{+0.17}_{-0.17}$	–
50	SHARDS10007672	189.4374	62.2383	DF	0.20	–	7.77 ± 0.36	–0.112	–13.18	–14.47	$-2.50^{+0.13}_{-0.13}$	–
51	SHARDS10007737	189.1887	62.2536	GP	0.26	–	7.13 ± 0.30	–0.229	–12.90	–13.76	$-2.59^{+0.15}_{-0.11}$	–
52	SHARDS10007846	189.2103	62.2692	CPSTB	0.20	–	7.97 ± 0.15	–0.074	–13.25	–14.59	$-2.61^{+0.13}_{-0.11}$	–
53	SHARDS10007883	189.5146	62.2755	GP	0.26	–	8.05 ± 0.12	–0.194	–14.37	–15.48	$-2.48^{+0.15}_{-0.11}$	–
54	SHARDS10007902	189.2121	62.2778	CPSTB	0.26	–	8.39 ± 0.33	–0.224	–14.52	–15.62	$-2.61^{+0.15}_{-0.11}$	–
55	SHARDS10008552	189.4493	62.2348	S0	0.38	–	9.372 ± 0.099	–0.761	–17.55	–18.99	$-2.50^{+0.13}_{-0.13}$	–0.279
56	SHARDS10008997	189.3576	62.2331	DF	0.41	–	8.71 ± 0.13	–0.669	–15.67	–16.76	$-2.54^{+0.11}_{-0.13}$	–
57	SHARDS10009032	189.4216	62.2412	CPSTB	0.25	–	8.13 ± 0.26	–0.202	–14.12	–15.52	$-2.52^{+0.13}_{-0.13}$	–
58	SHARDS10009131	189.4763	62.2589	DF	0.39	–	8.50 ± 0.12	–0.543	–15.22	–16.28	$-2.50^{+0.13}_{-0.13}$	–
59	SHARDS10009411	189.3849	62.2949	DF	0.30	–	8.29 ± 0.26	–0.311	–14.20	–15.51	$-2.61^{+0.15}_{-0.19}$	–
60	SHARDS10009577	189.3581	62.3522	DF	0.28	–	8.42 ± 0.22	–0.189	–14.52	–15.84	$-2.71^{+0.17}_{-0.17}$	–
61	SHARDS10009610	189.1628	62.3059	S0	0.55	0.5568	11.209 ± 0.069	–5.768	–21.53	–22.77	$-2.65^{+0.11}_{-0.15}$	–0.565
62	SHARDS10009819	189.2794	62.2468	CPSTB	0.27	–	8.40 ± 0.26	–0.206	–14.04	–15.28	$-2.586^{+0.108}_{-0.086}$	–
63	SHARDS10009927	189.1876	62.2756	DF	0.21	–	7.84 ± 0.18	–0.080	–13.71	–14.00	$-2.61^{+0.13}_{-0.11}$	–
64	SHARDS10010084	189.2336	62.3079	DF	0.34	–	8.24 ± 0.20	–0.443	–14.57	–15.62	$-2.672^{+0.086}_{-0.108}$	–
65	SHARDS10010282	189.3884	62.2943	DF	0.36	–	8.50 ± 0.19	–0.431	–14.81	–15.91	$-2.59^{+0.17}_{-0.17}$	–
66	SHARDS10010726	189.3233	62.2166	DF	0.54	–	8.72 ± 0.10	–2.152	–16.02	–16.51	$-2.54^{+0.11}_{-0.15}$	–
67	SHARDS10010775	189.4538	62.2429	DF	0.34	–	8.23 ± 0.11	–0.471	–14.32	–15.24	$-2.50^{+0.13}_{-0.13}$	–
68	SHARDS10011094	189.3024	62.3716	CPSTB	0.57	–	8.99 ± 0.18	–2.633	–17.38	–17.82	$-2.76^{+0.13}_{-0.13}$	–
69	SHARDS10011171	189.3521	62.2071	CPSTB	0.32	–	7.80 ± 0.17	–0.265	–13.97	–14.11	$-2.52^{+0.11}_{-0.24}$	–
70	SHARDS10011229	189.2272	62.2494	DF	0.43	–	7.97 ± 0.23	–0.991	–15.11	–15.86	$-2.586^{+0.108}_{-0.086}$	–
71	SHARDS10011544	189.3378	62.2820	GP	0.24	–	7.40 ± 0.20	–0.166	–13.62	–14.44	$-2.61^{+0.13}_{-0.15}$	–
72	SHARDS10012012	189.4065	62.2628	DF	0.35	–	7.63 ± 0.28	–0.496	–14.26	–15.02	$-2.56^{+0.13}_{-0.15}$	–
73	SHARDS20000593	189.1656	62.1385	S0	0.24	0.2470	9.766 ± 0.038	–0.407	–19.07	–20.32	$-2.43^{+0.15}_{-0.13}$	–0.060
74	SHARDS20000668	189.0924	62.1440	CPSTB	0.33	–	9.351 ± 0.087	–1.754	–17.53	–18.91	$-2.46^{+0.11}_{-0.11}$	–
75	SHARDS20000827	189.0335	62.1475	S0	0.40	0.4090	11.177 ± 0.079	–4.065	–20.97	–22.21	$-2.435^{+0.108}_{-0.086}$	–0.324
76	SHARDS20000858	189.2628	62.1502	S0	0.55	0.5600	10.391 ± 0.056	4.298	–19.77	–21.17	$-2.46^{+0.15}_{-0.19}$	–0.571
77	SHARDS20001051	189.1201	62.1564	S0	0.52	0.5183	10.602 ± 0.061	–2.607	–20.52	–21.81	$-2.46^{+0.15}_{-0.11}$	–0.502
78	SHARDS20001223	189.0208	62.1619	GP	0.23	–	7.88 ± 0.16	–0.157	–13.72	–14.93	$-2.456^{+0.086}_{-0.086}$	–
79	SHARDS20001534	189.2412	62.1702	S0	0.40	0.4101	10.249 ± 0.062	–1.112	–19.15	–20.01	$-2.50^{+0.13}_{-0.13}$	–0.327
80	SHARDS20002147	189.1471	62.1861	S0	0.40	0.4101	10.190 ± 0.057	–1.183	–20.19	–21.47	$-2.50^{+0.13}_{-0.11}$	–0.327
81	SHARDS20002235	189.2818	62.1867	E/S0	0.46	0.4714	10.583 ± 0.057	–1.989	–20.42	–21.48	$-2.52^{+0.11}_{-0.15}$	–0.426
82	SHARDS20002542	189.1283	62.1996	DF	0.32	–	8.30 ± 0.11	–0.328	–15.45	–16.78	$-2.500^{+0.129}_{-0.065}$	–
83	SHARDS20002550	189.0022	62.1988	E/S0	0.55	0.5616	11.139 ± 0.090	–7.355	–21.86	–22.86	$-2.478^{+0.086}_{-0.043}$	–0.573
84	SHARDS20002599	189.0414	62.2324	DF	0.22	–	7.914 ± 0.073	–0.143	–14.97	–15.83	$-2.500^{+0.129}_{-0.065}$	–
85	SHARDS20002889	189.2019	62.2213	S0	0.47	0.4760	9.25 ± 0.12	–1.681	–18.12	–19.64	$-2.564^{+0.086}_{-0.086}$	–0.434
86	SHARDS20002935	189.2003	62.2192	S0	0.47	0.4745	10.924 ± 0.068	3.046	–20.82	–22.06	$-2.564^{+0.086}_{-0.086}$	–0.431
87	SHARDS20002966	189.1671	62.2182	S0	0.49	0.4854	10.953 ± 0.066	–2.720	–20.89	–22.13	$-2.543^{+0.108}_{-0.086}$	–0.449
88	SHARDS20002995	189.1044	62.2168	S0	0.52	0.5185	10.958 ± 0.072	2.404	–20.90	–22.14	$-2.521^{+0.108}_{-0.086}$	–0.503
89	SHARDS20003119	189.2360	62.2126	Sp	0.52	0.5178	10.67 ± 0.10	4.251	–20.94	–22.19	$-2.564^{+0.086}_{-0.151}$	–
90	SHARDS20003134	189.0950	62.2166	S0	0.47	0.4725	10.807 ± 0.071	9.135	–20.99	–21.94	$-2.521^{+0.108}_{-0.086}$	–0.427
91	SHARDS20003210	189.2523	62.2096	S0	0.56	0.5631	10.800 ± 0.063	–2.855	–20.53	–21.39	$-2.564^{+0.086}_{-0.151}$	–0.576
92	SHARDS20003217	189.1158	62.2113	S0	0.52	0.5153	10.808 ± 0.066	–2.485	–20.53	–21.77	$-2.521^{+0.108}_{-0.086}$	–0.499
93	SHARDS20003377	189.0637	62.2060	S0	0.32	0.3198	9.930 ± 0.061	–0.568	–19.54	–20.82	$-2.500^{+0.129}_{-0.065}$	–0.180
94	SHARDS20003678	189.1938	62.1976	E/S0	0.50	0.5039	10.421 ± 0.061	–2.014	–19.77	–20.75	$-2.52^{+0.11}_{-0.11}$	–0.480
95	SHARDS20003814	189.1394	62.2842	E	0.46	0.4543	10.100 ± 0.091	–1.459	–19.52	–20.77	$-2.61^{+0.13}_{-0.15}$	–
96	SHARDS20003909	189.1583	62.2709	E	0.53	0.5290	10.581 ± 0.081	–2.256	–20.40	–21.27	$-2.59^{+0.15}_{-0.13}$	–
97	SHARDS20003969	189.1071	62.2617	CPSTB	0.20	–	8.339 ± 0.080	–0.107	–14.45	–15.07	$-2.56^{+0.15}_{-0.13}$	–
98	SHARDS20004069	189.0768	62.2552	OM	0.27	–	7.93 ± 0.22	–0.233	–14.36	–14.62	$-2.54^{+0.11}_{-0.11}$	–
99	SHARDS20004113	189.1728	62.2557	CPSTB	0.27	–	7.93 ± 0.30	–0.256	–13.79	–14.85	$-2.59^{+0.15}_{-0.13}$	–
100	SHARDS20004273	189.1426	62.2425	S0	0.52	0.5184	10.758 ± 0.086	5.286	–21.11	–22.39	$-2.56^{+0.11}_{-0.11}$	–0.502
101	SHARDS20004275	189.1439	62.2424	CPSTB	0.26	–	9.60 ± 0.14	1.078	–17.02	–18.30	$-2.56^{+0.11}_{-0.11}$	–
102	SHARDS20004328	189.1245	62.2393	CPSTB	0.52	0.5195	9.920 ± 0.049	9.615	–18.95	–20.34	$-2.54^{+0.13}_{-0.11}$	–
103	SHARDS20004359	189.2638	62.2383	S0	0.51	0.5120	10.597 ± 0.091	–2.385	–20.66	–21.51	$-2.59^{+0.11}_{-0.11}$	–0.493
104	SHARDS20004420	189.1728	62.2341	E/S0	0.55	0.5556	10.774 ± 0.069	–3.640	–20.95	–21.94	$-2.56^{+0.11}_{-0.11}$	–0.565

Table A.1. continued.

Number	SHARDS ID	α (°)	δ (°)	Morph type	z_{phot}	z_{spec}	$\log_{10}(M_{\star}/M_{\odot})$	SFR $M_{\odot}/\text{yr}$	M_V [mag]	M_K [mag]	A_{F775W} [10 ⁻² mag]	$R - F775W$ [mag]
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)
105	SHARDS20004440	189.0736	62.2290	E/S0	0.53	0.5337	10.649 ± 0.085	3.126	-20.89	-22.14	$-2.521^{+0.108}_{-0.086}$	-0.527
106	SHARDS20004586	189.1416	62.1314	OM	0.46	–	9.01 ± 0.27	-3.901	-17.23	-17.75	$-2.43^{+0.13}_{-0.17}$	–
107	SHARDS20004857	189.0668	62.1637	CPSTB	0.44	–	8.77 ± 0.20	-1.145	-16.01	-17.07	$-2.456^{+0.108}_{-0.065}$	–
108	SHARDS20005328	189.2706	62.1944	OM	0.30	–	7.95 ± 0.16	-0.345	-13.98	-14.26	$-2.52^{+0.11}_{-0.15}$	–
109	SHARDS20005718	189.1152	62.2396	DF	0.29	–	7.848 ± 0.098	-0.216	-14.77	-15.20	$-2.54^{+0.11}_{-0.15}$	–
110	SHARDS20006178	189.1600	62.1373	CPSTB	0.26	–	8.25 ± 0.21	-0.211	-14.55	-15.51	$-2.43^{+0.15}_{-0.13}$	–
111	SHARDS20006262	189.1689	62.1475	DF	0.23	–	8.04 ± 0.25	-0.161	-13.75	-14.76	$-2.46^{+0.15}_{-0.15}$	–
112	SHARDS20006283	189.2127	62.1492	CPSTB	0.35	–	8.774 ± 0.094	-0.537	-15.87	-16.50	$-2.46^{+0.15}_{-0.15}$	–
113	SHARDS20006429	189.0748	62.1624	CPSTB	0.27	–	7.99 ± 0.22	-0.138	-14.97	-16.49	$-2.456^{+0.108}_{-0.086}$	–
114	SHARDS20006437	189.0413	62.1627	CPSTB	0.43	–	8.40 ± 0.11	-1.042	-16.19	-16.94	$-2.456^{+0.086}_{-0.086}$	–
115	SHARDS20006480	188.9992	62.1661	CPSTB	0.24	–	8.36 ± 0.25	-0.172	-14.54	-15.55	$-2.456^{+0.086}_{-0.086}$	–
116	SHARDS20006824	188.9935	62.1913	CPSTB	0.27	–	7.63 ± 0.12	-0.171	-13.37	-14.59	$-2.478^{+0.065}_{-0.043}$	–
117	SHARDS20006985	189.1612	62.2029	CPSTB	0.24	–	7.86 ± 0.16	-0.164	-13.86	-14.67	$-2.521^{+0.108}_{-0.086}$	–
118	SHARDS20007009	189.1015	62.2041	DF	0.36	–	8.24 ± 0.14	-0.535	-15.20	-15.76	$-2.500^{+0.129}_{-0.065}$	–
119	SHARDS20007308	189.1162	62.2174	DF	0.37	–	8.13 ± 0.13	-0.408	-15.14	-16.25	$-2.521^{+0.129}_{-0.086}$	–
120	SHARDS20007309	189.2030	62.2174	GP	0.22	–	7.80 ± 0.19	-0.152	-13.90	-14.71	$-2.564^{+0.086}_{-0.108}$	–
121	SHARDS20007395	189.1077	62.2634	DF	0.47	–	9.57 ± 0.13	4.176	-17.45	-18.32	$-2.56^{+0.15}_{-0.13}$	–
122	SHARDS20007536	189.0747	62.2394	OM	0.56	–	9.10 ± 0.17	23.937	-17.28	-18.30	$-2.521^{+0.129}_{-0.086}$	–
123	SHARDS20007647	189.1417	62.1105	CPSTB	0.25	–	8.29 ± 0.14	-0.122	-14.25	-15.38	$-2.39^{+0.17}_{-0.15}$	–
124	SHARDS20008604	189.2621	62.2185	CPSTB	0.52	–	8.46 ± 0.11	-1.583	-15.90	-16.92	$-2.564^{+0.086}_{-0.129}$	–
125	SHARDS20008789	189.2519	62.2283	OM	0.35	–	8.01 ± 0.17	-0.539	-14.49	-14.62	$-2.59^{+0.11}_{-0.13}$	–
126	SHARDS20008811	189.2151	62.2298	CPSTB	0.22	–	8.22 ± 0.11	-0.145	-13.49	-14.82	$-2.586^{+0.086}_{-0.108}$	–
127	SHARDS20009039	189.1674	62.2450	CPSTB	0.30	–	8.52 ± 0.28	-0.258	-14.34	-15.57	$-2.56^{+0.13}_{-0.11}$	–
128	SHARDS20009057	189.1712	62.2444	GP	0.36	–	8.24 ± 0.17	-0.586	-15.34	-15.94	$-2.56^{+0.13}_{-0.11}$	–
129	SHARDS20009101	189.1076	62.2419	DF	0.46	–	8.90 ± 0.11	-1.254	-16.53	-17.63	$-2.54^{+0.11}_{-0.11}$	–
130	SHARDS20009404	189.1490	62.2593	CPSTB	0.59	–	9.06 ± 0.16	-2.542	-16.67	-17.96	$-2.59^{+0.15}_{-0.13}$	–
131	SHARDS20009676	189.0200	62.1704	CPSTB	0.54	–	9.23 ± 0.13	-2.136	-17.23	-18.61	$-2.456^{+0.086}_{-0.065}$	–
132	SHARDS20009942	189.1314	62.1832	DF	0.44	–	8.21 ± 0.23	-0.947	-15.29	-16.44	$-2.50^{+0.13}_{-0.11}$	–
133	SHARDS20010138	189.1646	62.2442	DF	0.29	–	7.84 ± 0.13	-0.313	-14.35	-14.96	$-2.56^{+0.13}_{-0.11}$	–
134	SHARDS20010154	189.0798	62.2310	CPSTB	0.56	–	9.315 ± 0.087	-3.841	-17.44	-18.82	$-2.521^{+0.108}_{-0.086}$	–
135	SHARDS20010466	189.0968	62.2099	CPSTB	0.46	–	8.04 ± 0.25	1.105	-15.84	-16.14	$-2.500^{+0.129}_{-0.065}$	–
136	SHARDS20010555	189.2050	62.2566	DF	0.26	–	8.11 ± 0.21	-0.164	-14.63	-15.24	$-2.61^{+0.13}_{-0.13}$	–
137	SHARDS20010777	189.2606	62.2381	CPSTB	0.22	–	7.84 ± 0.21	-0.083	-14.06	-14.69	$-2.59^{+0.11}_{-0.11}$	–
138	SHARDS20010793	189.2710	62.2300	DF	0.33	–	7.53 ± 0.24	-0.448	-13.92	-14.44	$-2.59^{+0.11}_{-0.13}$	–
139	SHARDS20010969	189.1317	62.1697	CPSTB	0.43	–	8.07 ± 0.24	-0.841	-15.15	-16.12	$-2.48^{+0.15}_{-0.11}$	–
140	SHARDS20011001	188.9709	62.1863	DF	0.50	–	8.87 ± 0.34	-0.995	-16.11	-16.74	$-2.478^{+0.086}_{-0.065}$	–
141	SHARDS20011033	188.9454	62.1989	CPSTB	0.27	–	8.30 ± 0.21	-0.287	-14.39	-15.40	$-2.478^{+0.108}_{-0.043}$	–
142	SHARDS20011279	189.1110	62.2383	CPSTB	0.51	–	8.93 ± 0.14	-1.873	-15.83	-17.07	$-2.54^{+0.11}_{-0.11}$	–
143	SHARDS20011817	189.0578	62.1248	S0	0.50	–	10.843 ± 0.054	-2.207	-20.62	-21.86	$-2.41^{+0.11}_{-0.13}$	-0.472
144	SHARDS20011862	189.0222	62.1519	OM	0.42	–	8.82 ± 0.22	2.370	-15.51	-16.83	$-2.456^{+0.086}_{-0.108}$	–
145	SHARDS20012018	189.2125	62.2069	DF	0.35	–	8.08 ± 0.11	-0.522	-14.23	-14.77	$-2.54^{+0.11}_{-0.13}$	–
146	SHARDS20012798	189.0583	62.2140	CPSTB	0.34	–	8.24 ± 0.20	-0.469	-14.54	-15.41	$-2.500^{+0.129}_{-0.065}$	–
147	SHARDS20013012	189.0228	62.2195	CPSTB	0.57	–	8.84 ± 0.17	-1.565	-15.72	-16.56	$-2.500^{+0.108}_{-0.065}$	–
148	SHARDS20013475	189.1848	62.2321	CPSTB	0.22	–	7.83 ± 0.15	-0.109	-13.24	-14.25	$-2.56^{+0.11}_{-0.11}$	–
149	SHARDS20013783	189.1933	62.2540	DF	0.24	–	8.01 ± 0.22	-0.166	-13.57	-14.67	$-2.59^{+0.15}_{-0.11}$	–
150	SHARDS20014088	189.1593	62.2771	OM	0.20	–	7.93 ± 0.21	-0.095	-13.01	-14.18	$-2.61^{+0.13}_{-0.15}$	–

Appendix B: Profile parameters of the sample of S0 and E/S0 galaxies at $0.2 < z < 0.6$

Table B.1. Profile classification and photometric parameters of S0 and E/S0 galaxies at $0.2 < z < 0.6$ in the GOODS-N field.

#	ID	Profile type	i (°)	μ_{break} (mag arcsec ⁻²)	R_{break} (kpc)	$\mu_{0,i}$ (mag arcsec ⁻²)	h_i (kpc)	$\mu_{0,o}$ (mag arcsec ⁻²)	h_o (kpc)	p_h (11)	p_{μ_0} (12)	R_{23} (kpc)	R_{lim} (kpc)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
1	SHARDS10000327	III	54	23.05 ^{+0.29} _{-0.68}	5.45 ^{+0.66} _{-0.95}	18.96 ^{+0.21} _{-0.27}	1.42 ^{+0.12} _{-0.15}	20.86 ^{+0.56} _{-0.42}	2.61 ^{+0.65} _{-0.26}	3.0×10^{-4}	3.0×10^{-4}	5.42 ^{+0.22} _{-0.18}	10.34
2	SHARDS10000762	I	64	—	—	19.19 ^{+0.13} _{-0.13}	4.50 ^{+0.16} _{-0.15}	—	—	2.0×10^{-1}	2.0×10^{-1}	16.06 ^{+0.39} _{-0.45}	24.19
3	† SHARDS10000827	III	55	22.44 ^{+1.31} _{-0.41}	8.08 ^{+4.44} _{-0.93}	18.63 ^{+0.18} _{-0.16}	2.29 ^{+0.21} _{-0.15}	20.23 ^{+1.23} _{-0.49}	3.92 ^{+1.98} _{-0.59}	2.4×10^{-3}	2.4×10^{-3}	10.18 ^{+0.42} _{-0.39}	15.20
4	SHARDS10000840	III	48	21.96 ^{+0.33} _{-0.52}	6.10 ^{+0.77} _{-0.84}	18.18 ^{+0.21} _{-0.35}	1.73 ^{+0.15} _{-0.21}	19.67 ^{+0.41} _{-0.26}	2.83 ^{+0.43} _{-0.20}	2.3×10^{-4}	2.3×10^{-4}	8.72 ^{+0.25} _{-0.27}	13.72
5	SHARDS10000845	II	84	19.71 ^{+0.29} _{-0.30}	8.86 ^{+0.75} _{-0.93}	16.68 ^{+0.21} _{-0.11}	3.15 ^{+0.38} _{-0.13}	15.41 ^{+0.23} _{-0.37}	2.23 ^{+0.11} _{-0.12}	3.4×10^{-4}	2.4×10^{-4}	15.89 ^{+0.62} _{-0.45}	18.17
6	SHARDS10000849	III	69	23.23 ^{+0.18} _{-0.36}	8.86 ^{+0.69} _{-0.60}	18.36 ^{+0.18} _{-0.22}	1.97 ^{+0.11} _{-0.12}	21.09 ^{+0.84} _{-0.82}	4.4 ^{+2.2} _{-1.1}	3.1×10^{-4}	3.1×10^{-4}	8.45 ^{+0.21} _{-0.18}	12.10
7	SHARDS10001013	I	45	—	—	17.356 ^{+0.060} _{-0.075}	1.132 ^{+0.018} _{-0.018}	—	—	2.4×10^{-1}	2.4×10^{-1}	5.87 ^{+0.15} _{-0.17}	7.48
8	SHARDS10001269	I	67	—	—	17.75 ^{+0.14} _{-0.13}	2.751 ^{+0.087} _{-0.076}	—	—	1.8×10^{-2}	1.8×10^{-2}	13.12 ^{+0.27} _{-0.29}	18.54
9	SHARDS10001314	I	49	—	—	20.12 ^{+0.13} _{-0.11}	1.843 ^{+0.068} _{-0.059}	—	—	3.9×10^{-2}	3.9×10^{-2}	4.60 ^{+0.14} _{-0.15}	9.81
10	SHARDS10001344	III	54	22.578 ^{+1.311} _{-0.050}	10.21 ^{+7.30} _{-0.43}	19.70 ^{+0.48} _{-0.27}	3.64 ^{+1.10} _{-0.32}	21.16 ^{+0.98} _{-0.17}	6.99 ^{+3.31} _{-0.43}	1.6×10^{-3}	1.6×10^{-3}	12.41 ^{+0.66} _{-0.81}	24.22
11	SHARDS10001350	II	45	21.64 ^{+0.42} _{-0.26}	10.21 ^{+1.22} _{-0.87}	18.89 ^{+0.21} _{-0.16}	4.02 ^{+0.59} _{-0.22}	17.40 ^{+0.26} _{-0.63}	2.61 ^{+0.16} _{-0.24}	5.8×10^{-4}	5.8×10^{-4}	13.52 ^{+0.21} _{-0.19}	17.77
12	SHARDS10001648	III	72	23.01 ^{+0.52} _{-0.53}	7.7 ^{+1.1} _{-1.1}	17.99 ^{+0.29} _{-0.38}	1.60 ^{+0.15} _{-0.17}	20.63 ^{+0.87} _{-0.50}	3.23 ^{+1.16} _{-0.34}	2.9×10^{-4}	2.9×10^{-4}	7.70 ^{+0.20} _{-0.24}	13.90
13	SHARDS10001727	I	84	—	—	17.447 ^{+0.052} _{-0.052}	2.104 ^{+0.029} _{-0.027}	—	—	1.6×10^{-2}	1.6×10^{-2}	11.08 ^{+0.14} _{-0.14}	16.14
14	SHARDS10001847	II	75	21.33 ^{+0.59} _{-0.37}	9.9 ^{+1.4} _{-1.0}	17.924 ^{+0.156} _{-0.092}	3.148 ^{+0.259} _{-0.095}	16.84 ^{+0.24} _{-0.69}	2.39 ^{+0.13} _{-0.23}	4.0×10^{-5}	5.0×10^{-5}	13.68 ^{+0.20} _{-0.25}	21.34
15	SHARDS10002351	I	86	—	—	16.95 ^{+0.13} _{-0.14}	1.290 ^{+0.048} _{-0.050}	—	—	4.0×10^{-1}	4.2×10^{-1}	7.08 ^{+0.60} _{-0.34}	8.63
16	SHARDS10002730	III	53	23.49 ^{+1.10} _{-0.85}	6.8 ^{+1.7} _{-1.2}	18.20 ^{+0.12} _{-0.20}	1.361 ^{+0.045} _{-0.098}	19.76 ^{+2.88} _{-0.64}	1.92 ^{+2.78} _{-0.23}	7.8×10^{-3}	7.8×10^{-3}	6.04 ^{+0.16} _{-0.15}	9.99
17	SHARDS10002769	I	39	—	—	20.41 ^{+0.15} _{-0.13}	3.79 ^{+0.19} _{-0.16}	—	—	9.1×10^{-2}	9.1×10^{-2}	11.28 ^{+0.84} _{-0.77}	16.07
18	SHARDS10002942	III	21	22.01 ^{+1.69} _{-0.34}	5.70 ^{+2.81} _{-0.57}	17.70 ^{+0.17} _{-0.22}	1.410 ^{+0.119} _{-0.096}	19.08 ^{+2.00} _{-0.31}	2.06 ^{+1.41} _{-0.15}	3.2×10^{-3}	3.2×10^{-3}	7.54 ^{+0.24} _{-0.26}	10.90
19	SHARDS10003216	I	19	—	—	18.66 ^{+0.17} _{-0.24}	1.049 ^{+0.060} _{-0.075}	—	—	4.2×10^{-1}	4.2×10^{-1}	4.16 ^{+0.15} _{-0.15}	5.84
20	SHARDS10003312	III	38	23.850 ^{+0.021} _{-0.799}	10.43 ^{+0.22} _{-2.02}	19.64 ^{+0.17} _{-0.31}	2.71 ^{+0.16} _{-0.33}	21.79 ^{+0.42} _{-0.50}	5.60 ^{+1.51} _{-0.68}	2.6×10^{-4}	2.6×10^{-4}	8.31 ^{+0.31} _{-0.32}	17.90
21	SHARDS10003402	II	84	20.09 ^{+0.19} _{-0.29}	3.96 ^{+0.25} _{-0.41}	17.78 ^{+0.14} _{-0.11}	1.88 ^{+0.25} _{-0.10}	16.36 ^{+0.13} _{-0.035}	1.161 ^{+0.029} _{-0.035}	1.1×10^{-4}	8.0×10^{-5}	7.067 ^{+0.117} _{-0.099}	10.62
22	SHARDS10003647	III	66	22.40 ^{+1.43} _{-0.36}	8.88 ^{+3.23} _{-0.95}	17.57 ^{+0.33} _{-0.24}	1.92 ^{+0.24} _{-0.13}	19.64 ^{+2.02} _{-0.37}	3.26 ^{+2.69} _{-0.24}	4.6×10^{-4}	4.6×10^{-4}	10.41 ^{+0.34} _{-0.35}	16.23
23	SHARDS10004777	II	62	24.854 ^{+0.076} _{-0.461}	12.92 ^{+0.37} _{-1.18}	19.939 ^{+0.064} _{-0.058}	2.875 ^{+0.064} _{-0.045}	18.37 ^{+0.44} _{-1.18}	2.11 ^{+0.19} _{-0.26}	$< 1.0 \times 10^{-5}$	$< 1.0 \times 10^{-5}$	8.22 ^{+0.14} _{-0.14}	16.29

Notes. Columns: (1) Numerical ID in our final sample of S0 and E/S0 galaxies at $0.2 < z < 0.6$. (2) ID SHARDS (release DR2 beta). (3) Profile type. (4) Galaxy inclination (degrees). (5) Surface brightness of the profile at the break radius μ_{break} in mag arcsec⁻². (6) Break radius R_{break} in kpc. (7) Central surface brightness of the inner profile $\mu_{0,i}$ in mag arcsec⁻². (8) Scale-length of the inner profile h_i in kpc. (9) Central surface brightness of the outer profile $\mu_{0,o}$ in mag arcsec⁻². (10) Scale-length of the outer profile h_o in kpc. (11) Elbow p -value for the likelihood that h_i and h_o are equal. (12) Elbow p -value for the likelihood that $\mu_{0,i}$ and $\mu_{0,o}$ are equal. (13) Isophotal radius for 23 mag arcsec⁻² of the object in the corrected Steidel R band in kpc. (14) Limiting radius of the profile in kpc. The objects flagged with an † symbol after their ID SHARDS correspond to those objects in the AGN subsample (see Sect. 2.8).

Table B.1. continued.

#	ID	Profile type	i (°)	μ_{break} (mag arcsec ⁻²)	R_{break} (kpc)	$\mu_{0,i}$ (mag arcsec ⁻²)	h_i (kpc)	$\mu_{0,o}$ (mag arcsec ⁻²)	h_o (kpc)	p_h (11)	p_{μ_0} (12)	R_{23} (kpc)	R_{lim} (kpc)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
24	SHARDS10009610	III	53	22.54 ^{+0.31} _{-0.38}	10.37 ^{+1.21} _{-0.99}	17.80 ^{+0.23} _{-0.24}	2.32 ^{+0.17} _{-0.17}	20.03 ^{+0.47} _{-0.34}	4.31 ^{+0.66} _{-0.36}	1.2 × 10 ⁻⁴	1.2 × 10 ⁻⁴	12.11 ^{+0.29} _{-0.38}	20.51
25	SHARDS20000593	III	46	23.10 ^{+0.27} _{-0.21}	6.09 ^{+0.60} _{-0.60}	20.32 ^{+0.10} _{-0.15}	2.34 ^{+0.12} _{-0.17}	21.17 ^{+0.15} _{-0.11}	3.36 ^{+0.17} _{-0.12}	3.8 × 10 ⁻³	3.8 × 10 ⁻³	5.79 ^{+0.15} _{-0.16}	17.23
26	SHARDS20000827	III	84	22.79 ^{+1.31} _{-0.18}	10.90 ^{+3.45} _{-0.44}	17.83 ^{+0.30} _{-0.14}	2.333 ^{+0.260} _{-0.088}	20.17 ^{+2.29} _{-0.37}	4.34 ^{+6.24} _{-0.36}	1.5 × 10 ⁻⁵	1.5 × 10 ⁻⁵	11.67 ^{+0.39} _{-0.39}	17.66
27	SHARDS20001051	I	27	—	—	18.407 ^{+0.083} _{-0.084}	1.689 ^{+0.038} _{-0.036}	—	—	4.3 × 10 ⁻¹	4.3 × 10 ⁻¹	7.21 ^{+0.21} _{-0.22}	10.45
28	SHARDS20001534	I	63	—	—	18.507 ^{+0.058} _{-0.056}	1.257 ^{+0.019} _{-0.017}	—	—	4.9 × 10 ⁻¹	4.9 × 10 ⁻¹	5.24 ^{+0.17} _{-0.17}	7.85
29	† SHARDS20002147	I	24	—	—	18.63 ^{+0.15} _{-0.14}	1.312 ^{+0.056} _{-0.051}	—	—	8.8 × 10 ⁻²	8.8 × 10 ⁻²	5.25 ^{+0.19} _{-0.20}	7.848
30	SHARDS20002235	I	31	—	—	19.05 ^{+0.12} _{-0.10}	2.256 ^{+0.080} _{-0.077}	—	—	2.9 × 10 ⁻²	2.9 × 10 ⁻²	8.06 ^{+0.29} _{-0.24}	11.70
31	SHARDS20002550	I	38	—	—	19.22 ^{+0.16} _{-0.14}	4.74 ^{+0.21} _{-0.20}	—	—	4.9 × 10 ⁻²	4.9 × 10 ⁻²	16.34 ^{+0.47} _{-0.40}	24.49
32	SHARDS20002889	I	17	—	—	20.07 ^{+0.18} _{-0.14}	1.292 ^{+0.077} _{-0.062}	—	—	1.8 × 10 ⁻¹	1.8 × 10 ⁻¹	3.42 ^{+0.18} _{-0.18}	5.35
33	SHARDS20002935	I	38	—	—	19.36 ^{+0.13} _{-0.12}	2.92 ^{+0.11} _{-0.10}	—	—	1.6 × 10 ⁻²	1.6 × 10 ⁻²	9.59 ^{+0.24} _{-0.24}	15.30
34	SHARDS20002966	I	47	—	—	18.334 ^{+0.091} _{-0.096}	2.184 ^{+0.054} _{-0.048}	—	—	2.3 × 10 ⁻¹	2.3 × 10 ⁻¹	9.50 ^{+0.25} _{-0.25}	13.70
35	SHARDS20002995	II	31	22.67 ^{+0.48} _{-0.41}	10.7 ^{+1.2} _{-1.2}	19.25 ^{+0.14} _{-0.11}	3.40 ^{+0.22} _{-0.15}	17.66 ^{+0.62} _{-1.00}	2.32 ^{+0.27} _{-0.33}	6.0 × 10 ⁻⁴	5.8 × 10 ⁻⁴	11.50 ^{+0.25} _{-0.24}	15.30
36	SHARDS20003134	II	78	20.40 ^{+1.14} _{-0.97}	5.47 ^{+0.99} _{-1.11}	16.38 ^{+0.84} _{-0.54}	1.53 ^{+0.73} _{-0.24}	12.7 ^{+1.2} _{-1.5}	0.78 ^{+0.12} _{-0.10}	2.0 × 10 ⁻²	7.6 × 10 ⁻⁴	7.54 ^{+0.18} _{-0.20}	8.52
37	SHARDS20003210	III	22	22.06 ^{+0.35} _{-0.39}	5.69 ^{+0.68} _{-0.64}	17.95 ^{+0.27} _{-0.40}	1.46 ^{+0.15} _{-0.19}	20.21 ^{+0.32} _{-0.28}	3.13 ^{+0.36} _{-0.25}	9.9 × 10 ⁻⁴	9.9 × 10 ⁻⁴	8.06 ^{+0.26} _{-0.29}	13.63
38	SHARDS20003217	I	28	—	—	17.787 ^{+0.080} _{-0.090}	1.359 ^{+0.028} _{-0.030}	—	—	2.8 × 10 ⁻¹	2.7 × 10 ⁻¹	6.37 ^{+0.19} _{-0.19}	8.56
39	† SHARDS20003377	I	68	—	—	18.70 ^{+0.21} _{-0.18}	1.313 ^{+0.060} _{-0.059}	—	—	2.1 × 10 ⁻³	2.2 × 10 ⁻²	4.95 ^{+0.16} _{-0.14}	8.93
40	SHARDS20003678	I	38	—	—	19.56 ^{+0.25} _{-0.22}	1.392 ^{+0.088} _{-0.068}	—	—	1.8 × 10 ⁻²	1.8 × 10 ⁻²	4.11 ^{+0.22} _{-0.21}	6.99
41	SHARDS20004359	I	40	—	—	19.97 ^{+0.17} _{-0.16}	3.56 ^{+0.19} _{-0.17}	—	—	1.1 × 10 ⁻²	1.1 × 10 ⁻²	9.82 ^{+0.25} _{-0.30}	17.80
42	SHARDS20004420	I	42	—	—	19.81 ^{+0.17} _{-0.15}	4.13 ^{+0.22} _{-0.19}	—	—	8.2 × 10 ⁻²	8.2 × 10 ⁻²	11.84 ^{+0.36} _{-0.34}	18.55
43	† SHARDS20004440	I	34	—	—	18.13 ^{+0.15} _{-0.13}	1.668 ^{+0.067} _{-0.061}	—	—	1.3 × 10 ⁻²	1.3 × 10 ⁻²	7.46 ^{+0.27} _{-0.24}	9.86
44	SHARDS20011817	I	82	—	—	16.283 ^{+0.077} _{-0.076}	1.097 ^{+0.022} _{-0.020}	—	—	2.6 × 10 ⁻¹	2.5 × 10 ⁻¹	6.83 ^{+0.35} _{-0.31}	8.42

Appendix C: Specific comments on images, surface brightness profiles and disc profile analysis for the S0 and E/S0 galaxies at $z < 0.6$

Here we detail some of the most important characteristics of the S0 and E/S0 objects within our sample (see Table B.1), accounting for their PSF-corrected photometric profiles. Only the first galaxy is provided in the printed edition.

SHARDS10000327: E/S0 galaxy with a Type-III profile, with no nearby galaxies, and medium inclination (see Table B.1). The object shows a clear Type-III break at 5.4 kpc from the centre. The PDDs for h and μ_0 show two clearly separated peaks corresponding to the two sections of the surface brightness profile.

Fig. C.1. Upper row, left panel: masked false RGB image centred on the source (red: F775W, green: F606W, blue: F435W). The red segment represents 3 arcsec. Upper row, right panel: deconvolved F775W image. The black lines represent the isophotal contours of the image in magnitudes. The white regions represent the masked areas. The red ellipse indicates the limiting radius. Lower row, left panel: surface brightness profiles of the original image (blue) and the PSF-corrected image (black) for the observed F775W band (left axis) and for the rest-frame Steidel R band (right axis). The red solid and blue dashed lines correspond to the models fitted during the deconvolution and used for checking the visual morphological selection (see the legend). The lower panel represents the differences between the original and the PSF-corrected profiles (red circles) and the difference between the original profile and the reconvolved PSF-corrected image profile (black squares). The vertical red line represents the limiting radius. Lower row, right panel: surface brightness profile in the rest-frame Steidel R band corrected for dust extinction, cosmological dimming and K-correction. The dashed lines and the shaded areas correspond to the exponential fittings of the inner and outer profiles in red and blue colours, respectively. The vertical and horizontal black dotted lines correspond to the peak of the PDD for the break radius and the surface brightness value at that location (R_{break} and μ_{break}). The results of the break analysis are provided in the panel.

SHARDS10000762: we classify with object as S0 galaxy with a Type-I profile. It presents a medium to high inclination (see Table B.1). There are not any nearby galaxies. The inner profile shows an slightly but noticeable bump in the inner region, possibly a lens component. We apply masking to a small source of $\mu_{F775W} \sim 23$ mag arcsec $^{-2}$ on the north direction along the semimajor axis. After masking the lens dominated part of the profile, the PDDs do not show any noticeable break.

Fig. C.2. See caption of Fig. 1.

SHARDS10000827: S0 galaxy with Type-III profile. The object presents a medium inclination (see Table B.1). It was flagged as an AGN source (see Sect. 2.8). A high level of masking was needed due to a low surface brightness field object to the SW. To avoid any contamination, we calculated the surface brightness profile by using the opposite part of the galaxy and performing a manual aggressive masking to the whole FoV. The isophotal curves are centred around the main object, they do not present any large perturbations or deviations and show a position angle and ellipticity that is almost constant.

Fig. C.3. See caption of Fig. 1.

SHARDS10000840: E/S0 galaxy with Type-III profile. The object presents a medium to low inclination (see Table B.1). The image needed an aggressive level of masking due to two nearby edge on field galaxies to the NE, including manual masking and revision of the whole FoV. We do not find any significant perturbations in the isophotes that could be due to the field objects. The PDDs for h and μ_0 show two clearly separated peaks corresponding to the two profiles.

Fig. C.4. See caption of Fig. 1.

SHARDS10000845: S0 galaxy with Type-II profile. Its profile was generated by ISOFIT instead of ellipse due to its completely edge on orientation (see Table B.1). The object appears to be isolated, therefore manual masking was not needed. The profile shows a clear and compact bulge component. The PDDs for h and μ_0 show two clearly separated peaks corresponding to the two profiles. The corresponding PDDs for R_{break} and μ_{break} appear to be clearly Gaussian and narrow.

Fig. C.5. See caption of Fig. 1.

SHARDS10000849: S0 galaxy with Type-III profile. The object presents medium to high inclination (see Table B.1). We have applied manual masking to two main sources in the FoV and a smaller one. Nevertheless, no source appears to be close enough to distort the profile and any contribution to the outer parts of our profile was discarded. The PDDs for h and μ_0 show two clearly separated distributions, although the outer profile is somewhat skewed due to deviations from a pure exponential profile.

Fig. C.6. See caption of Fig. 1.

SHARDS10001013: small S0 galaxy with Type-I profile. The original surface brightness profile appears to be almost bulgeless. It presents medium inclination and small apparent size (~ 1.4 arcsec to $S/N = 3$). There are not any nearby galaxies or FoV objects. The resolution is not high enough to resolve any possible detail apart from the disc itself. Elbow does not reveal significant differences of any part on the disc.

Fig. C.7. See caption of Fig. 1.

SHARDS10001269: S0 galaxy with Type-I profile. The object presents medium to high inclination (see Table B.1). Some close field objects to the NW along the major axis required extensive manual masking, although only few masked pixels finally were within inside the fitting region. An apparent excess of light dominates at the very outer parts of the galaxy, but it is not significant after PSF subtraction ($p \sim 0.018$). This is a quite similar case to SHARDS10000845. The PDDs of h and μ_0 reveal a clear inner disc profile in contrast with the wider and skewed PDD of the outer profile.

Fig. C.8. See caption of Fig. 1.

SHARDS10001314: S0 galaxy, apparently in interaction or at least overlapped with another source of similar size. The galaxy does not seem to be highly disturbed or asymmetric. High contamination from a close object required extensive masking of almost 30% of the galaxy, leaving the other 70% to analyse the surface brightness profile. The non-PSF corrected image shows an excess of light with almost constant surface brightness at 9–12 kpc from the centre, which results negligible after PSF subtraction. The exponential profile appears to be slightly bended, but the break parameters present high uncertainties. The probabilities of the both distributions (inner and outer profile for being equal) are slightly lower than 5% both in μ and h . We finally classified this object as Type I.

Fig. C.9. See caption of Fig. 1.

SHARDS10001344: S0 Type-III galaxy with medium inclination (see Table B.1) and a very bright central component ($\mu_R = 16 \text{ mag arcsec}^{-2}$) in contrast with the low surface brightness of the disc structure. We applied an extensive masking to a nearby region to the N-EE and a small close source to the N-NW. The PDDs for h and μ_0 show two separated peaks corresponding to the two profiles. The PDDs of the inner disc profile appear with two peaks and distorted due to the low statistics that result from the aggressive masking performed to the central bulge to avoid contamination.

Fig. C.10. See caption of Fig. 1.

SHARDS10001350: S0 galaxy with a Type-II profile. The image shows a nearby galaxy to the main object, similar in size, that was carefully masked to prevent any flux contribution to the outer profile. Finally, the masked region was outside the limiting radius. We find no significant perturbations on the isophotes that could be due to the field objects, which are all beyond the fitting region. The PDDs for h and μ_0 show two clearly separated peaks corresponding to the two profiles.

Fig. C.11. See caption of Fig. 1.

SHARDS10001648: isolated Type-III S0 galaxy with medium inclination (see Table B.1). The PDDs of h and μ_0 reveal that the excess of light found at $R_{\text{break}} = 8\text{--}14$ kpc is significant and compatible with an outer exponential profile, different from the inner disc profile.

Fig. C.12. See caption of Fig. 1.

SHARDS10001727: S0 galaxy with Type-I profile. It was analysed by ISOFIT instead of ellipse due to its completely edge-on orientation (see Table B.1). The PDDs of h and μ_0 show no significant break, and the general profile can be successfully modelled as a single exponential function.

Fig. C.13. See caption of Fig. 1.

SHARDS10001847: S0 galaxy with Type II profile (see Table B.1). The galaxy appears at a medium to high inclination. The limits for the profiles were chosen by hand, based several fittings performed varying the initial configurations, with the aim to reduce multiple peaks that appeared on the PDDs of h and μ_0 . The profile show a Type-II break which is statistically significant. The outskirts present an apparent excess of light, but it is not statistically significant after PSF subtraction.

Fig. C.14. See caption of Fig. 1.

SHARDS10002351: small S0 galaxy with pure exponential profile (Type I). It was analysed by ISOFIT instead of ellipse due to its edge on-orientation. The object is almost isolated. The PDDs of h and μ_0 show no statistically significant differences between any parts of the disc.

Fig. C.15. See caption of Fig. 1.

SHARDS10002730: small S0 galaxy with Type-III profile. It has a medium inclination (see Table B.1). It required extensive masking, but no masked pixel finally was inside the fitting region. The automated break analysis reveals that the excess of light shown at the outermost part of the galaxy is statistically significant as a Type-III break despite the PSF subtraction, although the probability of being a Type I is ~ 0.008 .

Fig. C.16. See caption of Fig. 1.

SHARDS10002769: E/S0 galaxy with Type-I profile and a low to medium inclination (see Table B.1). Manual and extensive masking was required due to multiple close field objects. The profile shows a very bright bulge and a wavy exponential profile. The PDDs of h and μ_0 reveal multiple Gaussian peaked distributions, due to the irregularities along the radius. None of them is compatible with a double exponential profile.

Fig. C.17. See caption of Fig. 1.

SHARDS10002942: Type-III S0 galaxy with face on orientation (see Table B.1). Multiple and extensive masking was required due to the presence of nearby objects. The profile shows a bulge and Type-III disc composition, as the small excess of light at the outermost part of the galaxy is proved to be statistically significant by the automatic break analysis after the PSF subtraction.

Fig. C.18. See caption of Fig. 1.

SHARDS10003216: E/S0 galaxy with very small size. The profile appears to be almost featureless, with no visible bulge or break, so it was classified as a Type I.

Fig. C.19. See caption of Fig. 1.

SHARDS10003312: E/S0 galaxy with Type-III profile. It has a medium inclination (see Table B.1) and it is almost isolated, so no manual masking was needed. The automated break analysis successfully detected two exponential profiles, with narrow and separated PDDs, although the distributions associated with the outer profile presented higher dispersions due to the irregularities found in the profile.

Fig. C.20. See caption of Fig. 1.

SHARDS10003402: S0 galaxy with a Type-II profile. Manual masking was required due to the presence of multiple field objects, none of them inside the fitting region. It was analysed by ISOFIT instead of ellipse due to its completely edge-on orientation (see Table B.1). The outer region ($R > 9$ kpc) was removed from the profile analysis due to the presence of several irregularities. The PDDs show two close, but clearly separated distributions for h and μ_0 , thus the disc is well represented by a Type-II profile.

Fig. C.21. See caption of Fig. 1.

SHARDS10003647: S0 galaxy with a Type-III profile. It shows a medium inclination (see Table B.1). Manual masking was required to avoid contamination from small field objects. The outermost region of the disc profile seems to be wavy, distorting the PDDs. The PDD of h and μ_0 appear to be clearly separated for the inner and outer profiles, although the outer profile is clearly skewed and wider than the inner one. The object present a significant Type-III profile despite the wide distribution of the outer profile.

Fig. C.22. See caption of Fig. 1.

SHARDS10004777: S0 galaxy with a Type-II profile. The galaxy presents a medium inclination (see Table B.1). Manual masking was applied to small sources at the outermost region (SE). We avoided the inner bump in the fit, because it probably traces a lens component, rather than a disc. The PDDs for h and μ_0 show clearly separated peaks corresponding to the outermost Type-II break.

Fig. C.23. See caption of Fig. 1.

SHARDS10009610: S0 galaxy with a Type-III profile. Manual masking was applied to multiple sources, but none of them finally laid within in the final fitting region. The PDDs for h and μ_0 show two clearly separated peaks corresponding to the inner and outer profiles. The outer profile PDD seems to be slightly wider than the inner one due to small distortions at high radius (see Table B.1).

Fig. C.24. See caption of Fig. 1.

SHARDS20000593: Type-III S0 galaxy. The central bulge is very bright, and the ellipticity is low, but there is a prominent exponential component in the surface brightness profile that led us to classify it as S0, instead of elliptical. Extensive masking in the low emission regions. The disc profile presents a significant excess of emission beyond $R \sim 6$ kpc with respect to the inner exponential section of the disc that cannot be explained by PSF contribution. The PDDs for h and μ_0 show two clearly separated peaks corresponding to the two profiles.

Fig. C.25. See caption of Fig. 1.

SHARDS20000827: Type-III S0 galaxy. It is highly inclined (see Table B.1) so it was analysed with ISOFIT instead of Ellipse. The profile presents a significant excess of emission since $R \sim 10$ kpc that cannot be explained by PSF contribution. The PDDs for h and μ_0 show two clearly separated peaks corresponding to the two profiles, although they present large uncertainties for the outer profile fit.

Fig. C.26. See caption of Fig. 1.

SHARDS20001051: small S0 galaxy with a Type-I profile. The object appears to be completely face on (see Table B.1), but inspection of the surface brightness profile reveals a typical bulge + exponential disc distribution. The disc appears to be featureless, and Elbow reveals no significant breaks within the observed disc region.

Fig. C.27. See caption of Fig. 1.

SHARDS20001534: small S0 galaxy with a Type-I profile. It has a very similar profile to SHARDS20001051, but in this case, the object reveals a clear disc structure with medium to high inclination (see Table B.1). After inspection of the surface brightness profile, we detected a typical bulge + exponential disc distribution. The disc appears to be featureless, and the automatic break analysis does not reveal any significant breaks within the limiting radius.

Fig. C.28. See caption of Fig. 1.

SHARDS20002147: small S0 galaxy with a Type-I disc and with very similar morphology to SHARDS20001051. It was flagged as an AGN source (see Sect. 2.8). The image presents some small isophotal irregularities, but they all are outside the fitting region. Masking was applied to two sources (to the N and SW of the main object). The surface brightness profile presents as typical of a bulge + exponential disc shape. The automatic break analysis reveals that, despite of the large uncertainties associated with the break parameters, the probability for this object of being compatible with a Type-I profile is $p = 0.022$, thus we classified it as Type I.

Fig. C.29. See caption of Fig. 1.

SHARDS20002235: E/S0 galaxy of Type-I disc partially overlapped with a galaxy of similar apparent size. Extensive manual masking has been applied to this object in order to extract the surface brightness profile from the farthest regions of the companion. Inspection of the surface brightness profile reveals a typical bulge + exponential disc distribution. The disc appears to be featureless, and the automatic break analysis detects no significant breaks within the limiting radius.

Fig. C.30. See caption of Fig. 1.

SHARDS20002550: E/S0 galaxy with a Type-I profile. The image required extensive masking due to the presence of a nearby saturated star. The masked area lies outside the final fitting region. It shows a clear bulge + exponential surface brightness profile. The automated break analysis revealed a noticeable change of profile in the transition zone between the bulge and the main disc, but we discarded it as it was too close to the centre, in order to avoid bulge contributions. (see Table B.1)

Fig. C.31. See caption of Fig. 1.

SHARDS20002889: small S0 galaxy with Type-I profile. The original surface brightness profile appears to be almost bulgeless. It has a medium inclination and small apparent size. It has no nearby galaxies or field objects. The resolution is not enough to resolve any possible detail besides the disc itself. Automatic break analysis reveals no significant differences between of any part of the disc.

Fig. C.32. See caption of Fig. 1.

SHARDS20002935: S0 galaxy with a face-on orientation (see Table B.1). We classified it as Type-I profile despite the noticeable bump found in the outskirts that cannot be explained by PSF dispersed light. Multiple and extensive masking was required due to the presence of multiple field objects. The profile shows a simple bulge + exponential disc structure. The small excess of light at the outermost part of the galaxy is not compatible with an exponential component.

Fig. C.33. See caption of Fig. 1.

SHARDS20002966: S0 galaxy with a Type-I profile. The object presents medium inclination (see Table B.1). The image did not require any masking inside the final fitting region. After inspection of the surface brightness profile, we found a typical bulge + exponential disc distribution. The disc appears to be featureless. The automatic break analysis reveals no significant breaks.

Fig. C.34. See caption of Fig. 1.

SHARDS20002995: S0 galaxy with a Type-II profile. Manual masking was required for three nearby sources, one of them an apparent satellite in accretion. The smooth surface brightness profile free from spikes ensure us that the masking was enough and successful. The inner region was removed for the fit to avoid possible contamination from the bulge or an inner lens. The outer profile presents some irregularities at the outskirts ($\sim 13\text{--}15$ kpc). The break presents smooth and statistically significant PDDs.

Fig. C.35. See caption of Fig. 1.

SHARDS20003134: S0 galaxy with a Type-II profile. Manual masking was required to avoid the contamination by compact bright object located to the W. It was analysed by ISOFIT instead of ellipse due to its edge-on orientation (see Table B.1). The PDDs for h and μ_0 show two clearly separated peaks corresponding to the two profiles.

Fig. C.36. See caption of Fig. 1.

SHARDS20003210: S0 galaxy with a Type-III profile. The object presents a face-on orientation (see Table B.1). The profile reveal a clear bulge + double exponential structure. The PDDs for h and μ_0 show two clearly separated peaks corresponding to the two profiles.

Fig. C.37. See caption of Fig. 1.

SHARDS20003217: S0 galaxy with a Type-I profile (see Table B.1). The object presents a very low inclination, but shows a clear bulge + exponential structure. A small bump at $\sim 3\text{--}4$ kpc in the surface brightness profile originates double peaked PDDs when performing automated break analysis, but the p -values associated to this bump were negligible.

Fig. C.38. See caption of Fig. 1.

SHARDS20003377: S0 galaxy with a Type-I profile. It has a medium to high inclination (see Table B.1). It was flagged as an AGN source (see Sect. 2.8). The profile shows a simple bulge and exponential disc composition. The disc appears to be clear and featureless, with a small deviation from the exponential profile in the middle region ($\sim 4\text{--}6$ kpc). The automatic break analysis reveals no significant breaks.

Fig. C.39. See caption of Fig. 1.

SHARDS20003678: small E/S0 galaxy with with a Type-I disc and very low inclination (see Table B.1). The profile shows a profile with a bulge + exponential disc structure. Due to the low resolution in this galaxy, the radial extension of the inner bulge is uncertain.

Fig. C.40. See caption of Fig. 1.

SHARDS20004359: S0 galaxy with a Type-I profile. The object presents low inclination (see Table B.1). Manual masking was applied to the image in many regions to avoid contamination from a tadpole irregular galaxy located to the N. The model greatly reduces residuals when adding an exponential profile to the free Sersic model, so we discarded the elliptical morphology for it. The profile generates too noisy PDDs to detect any statistically significant break. The visual analysis of the isophotes reveals a distortion between $\mu_{F775W} \sim 25\text{--}26 \text{ mag arcsec}^{-2}$, that coincides with a step observed in the surface brightness profile at $\sim 14\text{--}16 \text{ kpc}$. Finally the object was classified as a Type-I disc.

Fig. C.41. See caption of Fig. 1.

SHARDS20004420: E/S0 galaxy with a Type-I profile. The object presents low inclination (see Table B.1). Manual masking was applied to several small field objects to avoid contamination. The innermost part of the galaxy present higher ellipticity than the outer parts when performing visual inspection of the image. The model greatly improves when adding an exponential disc to a free Sersic profile, so we classified it as an E/S0 instead of an elliptical. The PDDs of h and μ_0 present a two peaked distribution, although no significant no significant break is detected. We note the small spike at ~ 14 kpc.

Fig. C.42. See caption of Fig. 1.

SHARDS20004440: E/S0 galaxy with a Type-I profile. It was flagged as an AGN source (see Sect. 2.8). It has a low inclination (see Table B.1). Multiple and extensive masking was applied to the outer parts of the galaxy, where tiny spot-like objects were detected through smoothing and re-masking. The excess of light detected before PSF correction appears to be caused by the dispersed light from the centre. The automatic break analysis reveals no significant breaks.

Fig. C.43. See caption of Fig. 1.

SHARDS20011817: small S0 galaxy with a Type-I profile. The orientation is edge-on (see Table B.1). No masking was needed into the fitting region. The surface brightness profile presents a small bulge + exponential disc distribution. The disc appears to be clear and featureless. Elbow reveals no any significant breaks.

Fig. C.44. See caption of Fig. 1.