Nature of the Galactic centre NIR-excess sources

I. What can we learn from the continuum observations of the DSO/G2 source?

Michal Zajaček\textsuperscript{1,2,3}, Silke Britzen\textsuperscript{2}, Andreas Eckart\textsuperscript{1,2}, Banafsheh Shahzamanian\textsuperscript{1}, Gerold Busch\textsuperscript{1}, Vladimír Karas\textsuperscript{3}, Marzieh Parsa\textsuperscript{1,2}, Florian Peissker\textsuperscript{1}, Michal Dovciak\textsuperscript{3}, Matthias Subroweit\textsuperscript{1}, František Dinibier\textsuperscript{1,3}, and J. Anton Zensus\textsuperscript{2}

\textsuperscript{1} I. Physikalisches Institut der Universität zu Köln, Zülpicher Strasse 77, 50937 Köln, Germany
e-mail: zajacek@ph1.uni-koeln.de
\textsuperscript{2} Max-Planck-Institut für Radioastronomie (MPIfR), Auf dem Hügel 69, 53121 Bonn, Germany
\textsuperscript{3} Astronomical Institute, Academy of Sciences, Boční I 1401, 14131 Prague, Czech Republic

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ABSTRACT

\textbf{Context.} The Dusty S-cluster Object (DSO/G2) orbiting the supermassive black hole (Sgr A\textsuperscript{*}) in the Galactic centre has been monitored in both near-infrared continuum and line emission. There has been a dispute about the character and the compactness of the object: it being interpreted as either a gas cloud or a dust-enshrouded star. A recent analysis of polarimetry data in $K_s$-band (2.2 $\mu$m) allows us to put further constraints on the geometry of the DSO.

\textbf{Aims.} The purpose of this paper is to constrain the nature and the geometry of the DSO.

\textbf{Methods.} We compared 3D radiative transfer models of the DSO with the near-infrared (NIR) continuum data including polarimetry. In the analysis, we used basic dust continuum radiative transfer theory implemented in the 3D Monte Carlo code Hyperion. Moreover, we implemented analytical results of the two-body problem mechanics and the theory of non-thermal processes.

\textbf{Results.} We present a composite model of the DSO – a dust-enshrouded star that consists of a stellar source, dusty, optically thick envelope, bipolar cavities, and a bow shock. This scheme can match the NIR total as well as polarized properties of the observed spectral energy distribution (SED). The SED may be also explained in theory by a young pulsar wind nebula that typically exhibits a large linear polarization degree due to magnetospheric synchrotron emission.

\textbf{Conclusions.} The analysis of NIR polarimetry data combined with the radiative transfer modelling shows that the DSO is a peculiar source of compact nature in the S cluster ($r \lesssim 0.04\text{ pc}$). It is most probably a young stellar object embedded in a non-spherical dusty envelope, whose components include optically thick dusty envelope, bipolar cavities, and a bow shock. Alternatively, the continuum emission could be of a non-thermal origin due to the presence of a young neutron star and its wind nebula. Although there has been so far no detection of X-ray and radio counterparts of the DSO, the analysis of the neutron star model shows that young, energetic neutron stars similar to the Crab pulsar could in principle be detected in the S cluster with current NIR facilities and they appear as apparent reddened, near-infrared-excess sources. The searches for pulsars in the NIR bands can thus complement standard radio searches, which can put further constraints on the unexplored pulsar population in the Galactic centre. Both thermal and non-thermal models are in accordance with the observed compactness, total as well polarized continuum emission of the DSO.

\textbf{Key words.} black hole physics – Galaxy: center – radiative transfer – polarization – stars: pre-main sequence – stars: neutron domains (Mossoux et al. 2016); see however Ponti et al. (2015) for the discussion of a possible increase in the bright X-ray flaring rate.

Despite many monitoring programmes and detailed analyses, there has been a dispute about the significance of the detection of tidal stretching of the DSO, which has naturally led to a variety of interpretations. A careful treatment of the background emission by Valencia-S. et al. (2015) revealed the DSO as a compact, single-peak emission-line source at each epoch, both shortly before and after the pericentre passage (see however Pfuhl et al. 2015). Moreover, the DSO was detected as a compact continuum source in near-infrared (NIR) $L$-band by Witzel et al. (2014), and as a fainter, stable $K_s$-band source (Eckart et al. 2013; Shahzamanian et al. 2016).

Most of the scenarios that have been proposed so far to explain the DSO and related phenomena may be grouped into the three following categories:

1. Introduction

Since its discovery in 2012 (Gillessen et al. 2012) the near-infrared excess and recombination-line emitting source Dusty S-cluster Object also known as G2 (DSO/G2)\textsuperscript{1} has caught a lot of attention because of its highly eccentric orbit around the supermassive black hole associated with the compact radio source Sgr A\textsuperscript{*} at the Galactic centre. It has been intensively monitored, especially close to its pericentre passage in the spring of 2014 (Valencia-S. et al. 2015; Pfuhl et al. 2015), when it passed the black hole at the distance of about 160 AU. No enhanced activity of Sgr A\textsuperscript{*} has been detected so far in the $L$-band by Witzel et al. (2014), and as a fainter, stable $K_s$-band source (Eckart et al. 2013; Shahzamanian et al. 2016).

\textsuperscript{1} The name G2 first appeared in Burkert et al. (2012) to distinguish the source from the first object of a similar type – G1 (Clénet et al. 2004). The acronym DSO (Dusty S-cluster Object) was introduced by Eckart et al. (2013) to stress the dust emission of the source and the overall NIR excess.
The apparent variety of studies may be explained by a lack of information about the intrinsic geometry of the DSO, which makes the problem of determining the DSO nature degenerate, which means that more interpretations of the source SED and line emission are plausible. Also, several observational studies denied the detection of \( K \)-band counterpart of the object (Gillessen et al. 2012; Witzel et al. 2014), which led to very few constraints on the SED, making both scenarios – core-less cloud and dust-enshrouded cloud – theoretically possible (Eckart et al. 2013). On the other hand, Eckart et al. (2013) and Eckart et al. (2014) show the \( K \)-band detection of the DSO in both VLT and Keck data, which together with the overall compactness of the source in both line (Valencia-S. et al. 2015) and continuum emission (Witzel et al. 2014) strengthened the hypothesis of a dust-enshrouded star-binary.

New constraints on the intrinsic geometry of the source has recently been obtained by Shahzamanian et al. (2016) thanks to the detection of polarized continuum emission in NIR \( K_s \) band in the polarimetry mode of the NACO imager at the ESO VLT. In Shahzamanian et al. (2016) we also obtained an improved \( K_s \)-band identification of the source in median polarimetry images at different epochs 2008–2012 (before the pericentre passage). The main result is that the DSO is an intrinsically polarized source with a significant polarization degree of \( \sim 30\% \), which is larger than the typical foreground polarization in the Galactic centre region at the level of \( \sim 6\% \), with an alternating polarization angle as the source approaches the position of Sgr A*.

Apart from the DSO, Eckart et al. (2013) and Meyer et al. (2014) showed that the central arcsecond contains several (\( \lesssim 10 \)) NIR-excess sources, some of which exhibit \( B \)-band excess, with respect to B-type S stars in their spectra. We show their approximate positions with respect to B-type S stars in Fig. 1. It is not yet clear whether these sources are related to each other, that is whether they have a common origin. However, they are definitely peculiar sources with respect to the prevailing population of main-sequence B-type S stars (Eckart & Genzel 1996, 1997; Ghez et al. 1998; Gillessen et al. 2009, 2017).

In this paper, we further elaborate on a model of the DSO (see previous models presented in Zajaček et al. 2014, 2016) taking into account the new \( K_s \)-band measurements and analysis as presented by Shahzamanian et al. (2016). By comparing theoretical and numerical calculations with the NIR data, we can explain the peculiar characteristics of the DSO by using the model of a young embedded and accreting star surrounded by a non-spherical dusty envelope. This model can be also used for other NIR excess sources, although with a certain caution, since they may be of a different nature. The comparison of different formation scenarios for NIR-excess sources is studied in Zajaček et al. in prep. (hereafter Paper II).

In this study, we focus on the total as well as linearly polarized NIR continuum characteristics of the DSO. We do not include line radiative transfer in the modelling. We refer the reader to Valencia-S. et al. (2015) and Zajaček et al. (2015, 2016), where we studied the basics of the line emission mechanisms potentially responsible for generating broad Br\( \gamma \) line. For a pre-main-sequence star, the large line width of the Br\( \gamma \) emission line can be explained by the magnetospheric accretion mechanism, where the gas is channelled along the magnetic field lines from the inner parts of a circumstellar accretion disc, reaching nearly free-fall velocities of several 100 km s\(^{-1}\). The line emission can thus be formed within a very compact region of a few stellar radii and the line luminosity is scaled by the accretion luminosity (Alcalá et al. 2014).

Furthermore, we also investigate whether the SED of the DSO and that of other excess sources could be of a non-thermal rather than a thermal origin by using the model of a PWN.
Although the PWN model has a smaller number of parameters and thus a certain elegance in comparison with the model of an embedded star, observationally we miss a clear X-ray or radio counterpart of the DSO, which would be expected for a young neutron star of a few $10^3$ yr. On the other hand, our analysis shows that young PWNs resulting from SNII explosions, if present in the nuclear star cluster, could be detected by standard NIR imaging and would indeed manifest themselves as apparent NIR-excess, polarized sources.

2. Summary of observational constraints

There are several important constraints that every model of the DSO must explain:

(a) near-infrared excess or reddening of $K_s - L' > 3$;
(b) broad emission lines, especially $\text{Br}\gamma$, with the FWHM of the order of $100\ \text{km s}^{-1}$;
(c) a stable $L'$-band as well as $K_s$-band continuum emission;
(d) a polarized $K_s$-band continuum emission of $P_L \approx 30\%$.

Besides (a)–(d) characteristics, one should also consider the overall compactness or the diffuseness of the source (i.e. whether the object can be resolved given the PSF of the instrument used), and the overall orbital evolution (i.e. if one can detect significant drag/inspiral along the orbit as would be expected for a core-less cloud).

Since different aspects are involved, we set up the roadmap towards solving the DSO nature, which is illustrated in Fig. 2. In the further analysis, we consider the results of Valencia-S. et al. (2015) that show that the DSO exhibits a single-peak Br$\gamma$ emission line at each epoch, in other words they detect no significant stretching along the orbit as would be expected for a core-less cloud. A consistent result is presented by Witzel et al. (2014),

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**Fig. 2.** Roadmap for solving the nature of the DSO/G2 source. The ticks (✓) label the implications of the analysis of observational data by Valencia-S. et al. (2015), Witzel et al. (2014), and Shahzamanian et al. (2016). The question-mark (?) on the left implies that the NIR continuum of the DSO can be either thermal (standard interpretation) or non-thermal. The orange colour marks the possible nature of the DSO that would explain the observed characteristics.
who detect a compact \( \lambda \)-band emission of the DSO/G2 during the peribothron\(^2\) passage in 2014.

Therefore, we are not going to consider the tidal stretching, which according to the roadmap in Fig. 2 would either indicate an extended circumstellar envelope that does not feel the gravitational field of the star, or a core-less cloud. These two scenarios will be further tested by the orbital evolution in the post-peribothron phase.

Concerning the spectral energy distribution of the DSO, we adopt the results of Gillessen et al. (2012), Eckart et al. (2013), and Shahzamanian et al. (2016); see also Shcherbakov (2014) for the first SED analysis of the DSO assuming a core-less cloud scenario. As analysed by Eckart et al. (2013) and confirmed by Shahzamanian et al. (2016), the source shows prominent reddening between NIR \( K_s \) and \( L' \) bands, \( K_s - L' > 3 \). Further measurements in \( M \) band were performed by Gillessen et al. (2012). The \( H \)-band flux density is an upper limit since there was no detection (Gillessen et al. 2012; Eckart et al. 2013).

In the NIR H band, Eckart et al. (2013) derive the minimum apparent magnitude of \( m_{H1} > 21.2 \) based on the background level of the neighbouring stars. Using the extinction correction of \( A_H = 4.21 \), the upper limit on the flux density is \( F_{H1} \leq 0.17 \text{ mJy} \).

For the flux density in NIR \( K_s \)-band, we take a weighted mean of the measurements by Shahzamanian et al. (2016) (see our Table 3 for the summary of measurements). We obtain the mean flux density value of \( F_{2.2} = (0.23 \pm 0.02) \text{ mJy} \), both with and without considering the epoch 2011, when the ratio \( S/N \) was low.

For the \( L' \)-band magnitude, we consider the value of \( m_{L'} = 14.4 \pm 0.3 \) (Eckart et al. 2013). Using \( A_{L'} = 1.09 \), we obtain the flux density of \( F_{3.8} = (1.2 \pm 0.3) \text{ mJy} \).

The absolute dereddened \( M \)-band magnitude obtained by Gillessen et al. (2012) is \( M_{M} = -1.8 \pm 0.5 \), which yields \( F_{4.7} = (1.2 \pm 0.4) \text{ mJy} \). All of the inferred flux densities are summarized in Table 2. Based on the flux density measurements, the upper limit on the overall luminosity was set to \( L_{\text{DSO}} < 30 L_{\odot} \) (Eckart et al. 2013; Witzel et al. 2014).

Another important constraint is the detection of polarized emission in NIR \( K_s \) band by Shahzamanian et al. (2016) with

\[^2\] We use pericentre and peribothron interchangeably; peribothron is derived from Greek bothros, which means a hole dug in the ground, also a pit used for drink offerings for subterranean gods in the Greek mythology.

**Table 2. Summary of NIR flux densities of the DSO.**

<table>
<thead>
<tr>
<th>Band</th>
<th>Wavelength ([\mu m])</th>
<th>Frequency ([\text{Hz}])</th>
<th>Flux density ([\text{mJy}])</th>
<th>Refs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>( H )</td>
<td>1.65</td>
<td>( 1.82 \times 10^{14} )</td>
<td>( \leq 0.17 )</td>
<td>1</td>
</tr>
<tr>
<td>( K_s )</td>
<td>2.2</td>
<td>( 1.36 \times 10^{14} )</td>
<td>( 0.23 \pm 0.02 )</td>
<td>2</td>
</tr>
<tr>
<td>( L' )</td>
<td>3.8</td>
<td>( 7.89 \times 10^{13} )</td>
<td>( 1.2 \pm 0.3 )</td>
<td>3</td>
</tr>
<tr>
<td>( M )</td>
<td>4.7</td>
<td>( 6.38 \times 10^{13} )</td>
<td>( 1.2 \pm 0.4 )</td>
<td>4</td>
</tr>
</tbody>
</table>

**References.** (1) Eckart et al. (2013); (2) Eckart et al. (2013), Shahzamanian et al. (2016); (3) Gillessen et al. (2012), Eckart et al. (2013), Witzel et al. (2014); (4) Gillessen et al. (2012).

**Table 3. Summary of observational constraints for the DSO nature.**

<table>
<thead>
<tr>
<th>Constraint</th>
<th>Source</th>
<th>Note</th>
</tr>
</thead>
<tbody>
<tr>
<td>SED</td>
<td>“red” source; ( K_s - L' &gt; 3 )</td>
<td></td>
</tr>
<tr>
<td>source of polarized ( K_s ) band emission</td>
<td>FWHM(_{60}) ( \approx 100 \text{ km s}^{-1} )</td>
<td></td>
</tr>
<tr>
<td>stability and compactness</td>
<td>polarization degree ( \sim 30% )</td>
<td>no significant tidal elongation</td>
</tr>
</tbody>
</table>

The polarization degree \( \sim 30\% \) and a variable polarization angle for four consecutive epochs (2008, 2009, 2011, and 2012). The summary of all observational constraints is in Table 3.

The dereddened, continuum flux densities in the NIR domain were attributed to the warm dust emission in the temperature interval \( T_{\text{dust}} = 400-600 \text{ K} \) (Gillessen et al. 2012; Eckart et al. 2013), which can reproduce the flux densities between \( K_s \) and \( M \) bands. In Fig. 3, we repeat the fit of the dereddened flux densities with a single-temperature black-body flux density profile \( S_\nu(T,R) = (R/d)^2 \pi B_\nu(T) \), where \( B_\nu(T) \) is a black-body specific intensity at temperature \( T \), \( R \) is the characteristic radius of the object, and \( d \) is the distance to the Galactic centre, which we set to \( d = 8 \text{ kpc} \) (Eckart et al. 2005, 2017; Genzel et al. 2010).

The black-body fits give the temperature of \( T = (874 \pm 54) \text{ K} \), which corresponds to the warm dust component, and the characteristic radius of \( R = (0.31 \pm 0.07) \text{ AU} \) for an optically thick black body. This corresponds to a rather compact source in comparison with the originally proposed mean length-scale of \( R_c \approx 15 \text{ mas} \approx 120 \text{ AU} \) for a core-less gas cloud (Gillessen et al. 2012), in which case the emission would necessarily be optically thin. For comparison, we also plot the black-body curve corresponding to the star of \( T_\star = 4200 \text{ K} \) and \( L_\star = 20 L_\odot \) (without any circumstellar envelope), which naturally has a reversed slope than that of the DSO continuum (see Fig. 3).

On the other hand, an alternative model for the origin of the SED with increasing flux values towards longer wavelengths (smaller frequencies) is a nonthermal power law, \( S_\nu = S_\nu(\nu_0)/\nu^\alpha \). A naive fit of the power law model to the detected flux densities yields the profile,

\[ S_\nu \approx 2.0 \left( \frac{\nu}{5.37 \times 10^{15} \text{ Hz}} \right)^{-2.0 \pm 0.3} \text{ mJy}, \tag{1} \]

with partial power-law slopes \( \alpha_{ij} = -\log(S_{\nu_i}/S_{\nu_j})/\log(\nu_i/\nu_j) \) between bands \( i \) and \( j \): \( \alpha_{HK} \approx 1.05, \alpha_{KL} = 3.02, \) and \( \alpha_{LM} \approx 0 \). The qualitative behaviour of the continuum radiation of the DSO

![Fig. 3. Detected, dereddened flux densities of the DSO (black points) and the fitted continuum: thermal black-body fit curve corresponding to warm dust (orange solid and dashed lines) and non-thermal power-law emission fit \( S_\nu = S_\nu(\nu_0)/\nu^\alpha \) with the index \( \alpha = 2.0 \pm 0.3 \) (red solid and dashed lines). For comparison, we also plot the black-body curve corresponding to the star of \( T_\star = 4200 \text{ K} \) and \( L_\star = 20 L_\odot \) (pre-main-sequence star without a dusty envelope: grey solid line).](image-url)
is similar to the SED of few young pulsars detected in NIR domains (Mignani et al. 2012; Zharikov et al. 2013; Zynuzin et al. 2016) that are dominated by magnetospheric synchrotron radiation. Moreover, they exhibit a significant linear polarized emission with the polarization degree of a few 10% (Zajczyk et al. 2012). Thus, DSO-like sources could in principle be neutron stars and the detection of significant linearly polarized emission strengthens this hypothesis. The crucial point for the confirmation of this association is the detection of the counterparts in different domains, specifically radio and X-ray domains.

3. On the compactness of the DSO

In the literature, it is still debated whether the DSO/G2 source is of compact nature or not. In the further analysis we assume that the DSO has a compact nature, that is the source is not significantly stretched and elongated by tidal forces of the SMBH. This conclusion is based on the fact that both the line emission (Bry) and the \(L′\)-band continuum emission did not show signs of tidal interaction during the closest passage (Valencia-S. et al. 2015; Witzel et al. 2014); see however Pfuhl et al. (2015) for a different view. In addition, \(K\)-band flux density was constant within uncertainties for four consecutive epochs (2008, 2009, 2011, and 2012, Shahzamanian et al. 2016). Since the DSO appears as a point-like source, it is only possible to infer an upper limit for its length-scale based on the minimum FWHM of the point spread function, \(\theta_{\text{min}} \approx 63(\lambda/2 \mu\text{m})\) mas.

A simple test of the compactness of the DSO is provided by the comparison of the observed evolution with that of a core-less gaseous stream approaching the black hole of \(M_∗ = 4 \times 10^6 M_\odot\). When the parts of the cloud move independently in the potential of the black hole, the cloud with initial radius \(R_{\text{init}}\) is stretched along the orbit and compressed in the perpendicular direction.

According to Shcherbakov (2014), we can express the relative prolongation as function of distance \(r\) from the SMBH in terms of the half-length \(L_{\perp}\):

\[
\Lambda = \frac{L}{R_{\text{init}}} = \left(\frac{r_{\text{init}}}{r}\right)^{1/2} \left(\frac{r_a + r_p - r}{r_a + r_p - r_{\text{init}}}\right)^{1/2},
\]

where \(r_{\text{init}}\) is the initial distance at which the cloud was formed, having a spherical shape with the radius \(R_{\text{init}}\), and \(r_p\) and \(r_a\) are pericentre and apocentre distances of the DSO, respectively. We set \(r_{\text{init}}\) to the distance that corresponds to 10 yr before the peribothron passage (earlier date of formation would lead to larger prolongation). Similarly, the relative compression \(\rho\) in the direction perpendicular to the orbit may be expressed as,

\[
\rho = H/R_{\text{init}} = \frac{r}{r_{\text{init}}},
\]

where \(H\) is the actual perpendicular cross-section of the cloud. For the orbital parameters of the DSO (Valencia-S. et al. 2015), both the relative prolongation \(\Lambda(t)\) and compression \(\rho(t)\) are plotted in Fig. 4 (right panel) as functions of time before the peribothron passage. For the observed dimensions of the object, the foreshortening due to the orbital inclination is important. The foreshortening factor as function of time is plotted in Fig. 4 (left panel). At the peribothron, the source should be viewed at full size and the relative prolongation is \(≈6\) times that of the initial size \(≈10\) times when foreshortening is taken into account. The compression in the perpendicular direction should lead to the general spaghettification of the cloud. The tidal elongation of this order was, however, not detected (Witzel et al. 2014; Valencia-S. et al. 2015).

Specifically, between the epoch 2011.39 (3 yr before the peribothron) and the peribothron passage, the prolongation factor is \(\Lambda ≈ 3.45\). If the DSO was a core-less cloud, it should have a pericentre length-scale \(L_{\perp} = \Lambda R_{\text{init}}\). Gillessen et al. (2013b) infer the FWHM length-scale \(R_{\text{FWHM}} = (42 \pm 10)\) mas from the Gaussian fit for epochs 2008.0, 2010.0, 2011.0, 2012.0, 2013.0. The pericentre size, with respect to 2011 epoch, should then be \(L_{\perp} ≈ 145\) mas \(> \theta_{\text{min}}\), which is more than a factor of two larger than PSF FWHM. Such a large size is inconsistent with a rather compact line emission detected by Valencia-S. et al. (2015) during the pericentre passage. In fact, the analysis of the \(L\)-band continuum emission of the DSO during the pericentre passage by Witzel et al. (2014) yields the diameter of 32 mas, which is fully consistent with the DSO being a point source.

On the other hand, since the DSO was detected as a point source at the pericentre, the upper limit on its length-scale is given by the diffraction limit \(L_{\perp} ≤ \theta_{\text{min}} ≈ 63\) mas. A core-less cloud or an extended envelope of a star that reached the size of \(L_{\perp}\) by tidal stretching must have been smaller by a factor of \(\Lambda(−10\text{yr}) ≈ 6\), that is 10 yr before the peribothron passage, yielding the characteristic size of \(L(−10\text{yr}) ≤ 10\) mas \(≈ 80\) AU.

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**Fig. 4.** Left: foreshortening factor for the size of any structure calculated for the DSO orbit with inclination \(i = 113°\). Right: relative tidal stretching and compression as function of time (in years with respect to the peribothron passage) in the orbital plane (solid lines) and with respect to the inclined orbit to the DSO (dashed lines).
Based on this estimate, we set the characteristic radius of the potentially tidally perturbed part of the DSO to $R_e \lesssim 5$ mas.

Using the observationally inferred B"ury luminosity of $L_{\text{B"ury}} \approx 2 \times 10^3 L_\odot$ (Gillessen et al. 2012; Valencia-S. et al. 2015), we can estimate the electron density in the envelope assuming case B recombination (Gillessen et al. 2012),

$$n_e = 1.35 \times 10^6 f_v^{1/2} \left( \frac{R_e}{5 \text{ mas}} \right)^{-3/2} \left( \frac{T_g}{10^4 \text{ K}} \right)^{0.54} \text{ cm}^{-3},$$

(4)

where $T_g$ is the expected gas temperature of the DSO and $f_v$ is the volume filling factor, which we set to $f_v \leq 1$. For the mass of the DSO, in case it would be a gas cloud, we get

$$M_{\text{DSO,cloud}} \approx 2.2 \times 10^{-7} f_v^{1/2} \left( \frac{R_e}{5 \text{ mas}} \right)^{3/2} \left( \frac{T_g}{10^4 \text{ K}} \right)^{0.54} \text{ g},$$

(5)

which is about $M_{\text{DSO,cloud}} = 0.4 f_v^{1/2} M_{\text{Earth}}$. A smaller mass and a required higher density than originally estimated (Gillessen et al. 2012) shorten typical hydrodynamical time-scales that determine the lifetime of the cloud, specifically the cloud evaporation time-scale is (Burkert et al. 2012)

$$\tau_{\text{evap}} = 43 \left( \frac{r}{5.4 \times 10^{16}} \right)^{1/6} \left( \frac{M_{\text{DSO,cloud}}}{2.2 \times 10^{-7} \text{ g}} \right)^{1/3} \text{ yr},$$

(6)

where $r$ is the distance from Sgr A* in units of $5.4 \times 10^{16}$ cm, which corresponds approx. to the epoch of 2004. Such a short evaporation time-scale for a small, cold clump in the hot ambient plasma would necessarily lead to observable changes in the cloud line and continuum luminosities. However, the observations imply that the DSO is a rather compact, stable source in both line and continuum emission (Witzel et al. 2014; Valencia-S. et al. 2015; Shahzamanian et al. 2016).

Although a magnetically arrested cloud was suggested to explain the apparent stability (Shcherbakov 2014), it would still not prevent the cloud from the progressive evaporation and disruption (McCourt et al. 2015) as well as the loss of angular momentum when interacting with the ambient medium, leading to the inspiral and deviation from the original ellipse (Pfuhl et al. 2015; McCourt et al. 2015). Therefore, given the reasons above, a stellar nature of the DSO is more consistent with its observed line and continuum characteristics.

The basic estimate of the distance $r_1$ where an object with a characteristic radius $R_{\text{DSO}}$ and mass $M_{\text{DSO}}$ is tidally disrupted is given by $r_1 = R_{\text{DSO}}(3M_e/M_{\text{DSO}})^{1/3}$. For a stellar source, we get an estimate $r_1 \approx 1.07(R_{\text{DSO}}/1 \text{ mas})(M_{\text{DSO}}/1 M_e)^{1/3}$ AU. Since the peribothron distance of the DSO is $r_p = a(1 - e) = 0.033 \text{pc} \times (1 - 0.976) \approx 163$ AU (Valencia-S. et al. 2015) and no visible tidal interaction was observed, the upper limit on the length-scale of the stellar system that stays stable is $R_{\text{DSO}} \approx 0.7(M_{\text{DSO}}/1 M_e)^{1/3}$ AU. On the other hand, for the cloud of $R_{\text{DSO}} = 15$ mas $\approx 2.7 \times 10^4 R_e$ and the mass of three Earth mass, $M_{\text{DSO}} \approx 10^{-5} M_e$ (Gillessen et al. 2012), the tidal radius is $r_1 \approx 1.3 \times 10^9$ AU. Hence, the cloud should be strongly perturbed not only at the pericentre, but during the whole phase of infall, since the apocentre distance is $r_a = a(1 + e) \approx 1.3 \times 10^9$ AU. In summary, to explain the compact behaviour of the object, the emitting material (gas+dust) should be located in the inner astronomical unit from the star.

On the other hand, since the NIR-continuum is dominated by thermal dust emission (for a dust-enshrouded star), one can estimate the lower distance limit where the dust is located from the dust sublimation radius $r_{\text{sub}}$ (Monnier & Millan-Gabet 2002),

$$r_{\text{sub}} = 1.1 \sqrt{Q_b \left( \frac{L_{\text{DSO}}}{1000 L_\odot} \right)^{1/2} \left( \frac{T_{\text{sub}}}{1500 \text{ K}} \right)^{-2} \text{ AU}},$$

(7)

where $Q_b$ is the ratio of absorption efficiencies, which we consider to be of the order of unity, and $T_{\text{sub}}$ is the dust sublimation temperature, for which we take 1500 K. The inferred luminosity of the DSO is of the order of $L_{\text{DSO}} \approx 10 L_\odot$ (Eckart et al. 2013; Witzel et al. 2014), and so the expected sublimation radius is $r_{\text{sub}} \approx 0.1$ AU. Hence, since the continuum emission seems to be compact and no clear evidence of tidal interaction was detected during the peribothron passage (Witzel et al. 2014), the distance range, where the dust emitting the NIR-continuum is located and stays gravitationally unperturbed, is quite narrow, $r_{\text{sub}} \lesssim r \lesssim r_1$, that is 0.1 AU $\lesssim r \lesssim 1$ AU.

### 4. Modelling the total and polarized continuum emission of the DSO

In this section, we focus on the modelling of the total as well as polarized flux density in corresponding NIR bands. The main aim is the continuum radiative transfer in the dense dusty envelope surrounding a star with the emphasis on the linearly polarized emission (Sect. 4.1). The continuum profile is shaped by reprocessing the stellar emission by the surrounding dusty envelope. Linear polarization may arise due to (i) photon scattering on spherical dust grains (Mie scattering); (ii) dichroic extinction caused by selective absorption of photons in the medium where non-spherical grains are aligned due to radiation or magnetic field. The overall linear polarization degree for young stars may vary from the fraction of a percent up to a few 10%, depending on the geometry as well as the extinction of the dusty envelope (see Kolokolova et al. 2015, for a review).

In case of a hypothetical non-thermal origin of the DSO continuum (Sect. 4.2, one expects a slope of the flux density $S_\nu \propto \nu^{n}$, where $n > 0$. Typically, young neutron stars exhibit a multiwavelength non-thermal continuum, which arises due to the synchrotron process in the magnetosphere of young neutron stars. Another contribution is the thermal emission of the cooling surface. However, for young ($\lesssim 10$ kyr) and middle-aged ($\gtrsim 100$ kyr) neutron stars, the non-thermal component dominates in NIR bands. Since neutron stars typically possess a highly-ordered strong magnetic field, the non-thermal component is expected to be partially linearly polarized. Using the homogeneous magnetic field approximation, the linear polarization degree for the synchrotron emission can be determined as (Rybicki & Lightman 1979),

$$P_L \lesssim \frac{n + 1}{n + 5/3},$$

(8)

where for $n \approx 0.7$ one gets $P_L \lesssim 0.72$, whereas the measured value in $K_s$ band (VLT/ISAAC) is $P_L^{K_s} \approx 0.47$ (Zajczyk et al. 2012) for the surrounding PWN.

### 4.1. Thermal origin of the SED: DSO as a dust-enshrouded star

To find the model of a dust-enshrouded star that reproduces the observed characteristics (SED, broad emission lines, linear polarization, and overall stability and compactness; see also Table 3 for the summary) we perform a set of 3D dust continuum radiative transfer simulations with different components and morphologies of dusty envelopes. For solving the radiative transfer
equation, we choose a Monte Carlo technique suitable for arbitrary three-dimensional dusty envelopes (Whitney 2011). For all our simulations of a dust-enshrouded star, we used an open-source parallelized code Hyperion (Robitaille 2011), which enables to create SEDs as well as images for a required wavelength range as well as different inclinations of the source. Since in the random walk of photons the scattering process is also included, we obtain a full Stokes vector \((I, Q, U, V)\), which enables us to calculate the linear polarization degree as well as the angle according to standard definitions,

\[
P_L = \frac{\sqrt{Q^2 + U^2}}{I},
\]

\[
\phi = \frac{1}{2} \arctan \left( \frac{U}{Q} \right).
\]  

(9)

Since the extinction is expected to be high in the innermost parts of the envelope, we make use of a modified random walk (MRW) implemented in the code in the thickest regions.

An important part of the modelling is the generation of the dust distribution, for which we use the code hmi e by C.F. Bohren and D. Huffman (improved by B. Draine; Bohren et al. 1998), which provides solutions to the Mie scattering and absorption of light by spherical dust particles. We generate dust grains with a power-law distribution \(n(a) \propto a^{-3.5}\) with the smallest and the largest grain size of \((a_{\text{min}}, a_{\text{max}}) = (0.01, 10.0) \mu \text{m}\). The gas-to-dust mass ratio in the dusty circumstellar envelope for all geometries is assumed to be 100. The distance to the Galactic centre is set to 8 kpc for flux density calculations.

For most of the simulations, we set up a 3D spherical grid that contains 400 \(\times\) 200 \(\times\) 10 grid points, and add a density grid of gaseous-dusty mixture with the dust properties as explained above. For all synthetic SEDs and images, the total flux density was determined via the integration over the whole source and then compared to observationally determined values in Table 2.

4.1.1. Different morphologies: source components

At first, we performed radiative transfer calculations for different geometries of circumstellar envelopes to assess whether they can reproduce the detected high polarization degree in \(K_s\)-band and the NIR-excess. First, we started with the simplest models with a star at the centre and flattened envelope and/or bow shock. For all these cases, the polarization degree remains below 10%. Breaking the spherical symmetry by introducing the cavities, having half-opening angle of 45°, increases the polarization degree to \(\approx 10\%\) (without a bow shock layer). Adding a dense bow shock layer, the linear polarization fraction typically reaches >20%, depending on the density of the envelope and the inclination. Qualitatively, the dependence of the linear polarization degree on the envelope geometry is sketched in Fig. 9.

The density grid in the radiative transfer models has different morphological and density components, whose characteristics are explained below:

- **Star**: based on the upper luminosity limit of \(L_{\text{DSO}} \leq 30 L_\odot\) (Eckart et al. 2013; Witzel et al. 2014), the central star of the DSO should belong to the category of pre-main-sequence stars with the mass constraint \(M_* \leq 3 M_\odot\) (Zajaček et al. 2015). Given the NIR-excess, that is the rising SED due to a different inclination of the source. Since in the random walk of photons the scattering process is also included, we obtain a full Stokes vector \((I, Q, U, V)\), which enables us to calculate the linear polarization degree as well as the angle according to standard definitions,

\[
P_L = \frac{\sqrt{Q^2 + U^2}}{I},
\]

\[
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For most of the simulations, we set up a 3D spherical grid that contains 400 \(\times\) 200 \(\times\) 10 grid points, and add a density grid of gaseous-dusty mixture with the dust properties as explained above. For all synthetic SEDs and images, the total flux density was determined via the integration over the whole source and then compared to observationally determined values in Table 2.

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The density grid in the radiative transfer models has different morphological and density components, whose characteristics are explained below:

- **Star**: based on the upper luminosity limit of \(L_{\text{DSO}} \leq 30 L_\odot\)
- **Flattened envelope**: to the first approximation, the dust-enshrouded star may be modelled as a star surrounded by a rotationally flattened, infalling dusty envelope that forms a disc at the corotation radius \(r_c\). The density profile is given by (Ulrich 1976),

\[
\rho(r, \theta) = \frac{M_{\text{acc}}}{4\pi(GM_{\text{DSO}}r_c^2)^{1/2}} \left( \frac{r}{r_c} \right)^{-3/2} \left( 1 + \frac{\mu}{\mu_0} \right)^{-1/2} \left( \frac{\mu_0}{\mu} + \frac{2\mu_0 r_c^2}{r} \right)^{-1},
\]

where \(M_{\text{acc}}\) is the infall rate. The quantities \(\mu\) and \(\mu_0\) are related by an equation of the streamline, \(\mu_0 = \mu_0(r/r_c) = 1 - \mu(r/r_c) = 0\).

The model of Ulrich envelope can match the SED of the DSO for stellar parameters \(M_* = 1.3 M_\odot, L_* = 4.3 L_\odot, T_\text{eff} = 4400 \text{ K}, R_* = 3.3 R_\odot\) (age ~ 760 000 yr). The suitable parameters of the envelope are \(M_{\text{acc}} = 5 \times 10^{-7} M_0\text{ yr}^{-1}, r_{\min} = 10 R_\odot, \text{ and } r_c = 20 R_\odot\), where \(r_{\min}\) is the minimal distance of the envelope from the star. We vary the maximum distance of the envelope \(r_{\max}\) from 0.5 AU up to 50 AU, which affects the SED due to a different dust temperature distribution. For the SEDs of the flattened envelope at different inclinations (0°, 30°, 60°, 90°) and three different maximum radii \(r_{\max}\) = [0.5, 5, 50] AU, see Fig. 6. Because of observational uncertainties, more suitable configurations are possible, for example \(r_{\max} = 5\text{ AU}\) and the inclination of 90° or \(r_{\max} = 50\text{ AU}\) and the inclination in the range of...
\[ i = (60^\circ, 90^\circ). \] The lower value of \( r_{\text{max}} = 0.5 \text{ AU} \) is not suitable because of the large flux in \( K_s \) band, which can be explained by a lower extinction and a more prominent stellar emission. In the range \( r_{\text{max}} = (5, 50) \text{ AU} \), theSED does not depend much on this parameter because of the decreasing gas and dust density according to Eq. (10). On the other hand, theSED depends strongly on the accretion rate \( \dot{M}_{\text{acc}} \). We vary the accretion rate between \( \dot{M}_{\text{acc}} = (5 \times 10^{-6}, 5 \times 10^{-10}) \text{ M}_\odot \text{ yr}^{-1} \) for the fixed maximum radius of \( r_{\text{max}} = 5 \text{ AU} \), see Fig. 7. Clearly, the best match of SED values is for an intermediate value of \( \dot{M}_{\text{acc}} = 5 \times 10^{-7} \text{ M}_\odot \text{ yr}^{-1} \) (middle panel), increasing or decreasing the accretion rate by an order of magnitude significantly changes calculated fluxes, which is caused by large changes in the dust density, \( \rho \propto \dot{M}_{\text{acc}} \), see Eq. (10). Although a star surrounded by a flattened envelope can satisfactorily explain the SED of the DSO, the calculated polarized emission in \( K_s \) band from radiative transfer models yields the maximum total polarization degree of \( P_{\text{KL}} \) = 2.7% for \( i = 90^\circ \), which is well below the detected value of \( \sim 30\% \) (Shahzamanian et al. 2016). This implies that the simple geometry of the flattened envelope cannot alone explain the properties of the DSO.

- **Spherically concentrated dusty envelope/flat disc**: for more complex models, we set up a stratified spherical dusty envelope that was intersected by bipolar cavities in some models with smaller number densities (see below). In the final set of models, the spectral slope could be reproduced by the following mean mass densities of the gas+dust mixture: \( 1 \times 10^{-13} \text{ g cm}^{-3} \) for \( r = 0.1\text{–}1.0 \text{ AU} \), \( 1 \times 10^{-14} \text{ g cm}^{-3} \) for \( r = 1.0\text{–}2.0 \text{ AU} \), and \( 1 \times 10^{-15} \text{ g cm}^{-3} \) for \( r = 2.0\text{–}3.0 \text{ AU} \).

- **Bipolar cavity**: the bipolar cavities were introduced in the model to increase the non-spherical nature of the DSO, which is naturally needed to obtain a non-zero total polarization degree in the model, see Fig. 9. Furthermore, the walls of cavities also provide effective space for single scattering events of stellar and dust photons that escape from the star and the envelope, respectively. The density inside cavities is set to be uniform and smaller than in the envelope by several orders of magnitude: \( 1 \times 10^{-20} \text{ g cm}^{-3} \), which is a typical order of magnitude (see e.g. Sanchez-Bermudez et al. 2016). The half-opening angle of the cavity is initially varied to investigate the impact of the parameter space on the SED and the polarization, then set to \( \theta_c = 45^\circ \).

- **Bow shock**: the DSO and other objects in the S-cluster are expected to move supersonically through the ambient medium, especially close to the pericentre of their orbits (see Fig. 1 in Zajaček et al. 2016), see also De Colle et al. (2014), Ballone et al. (2013, 2016), Christie et al. (2016). The expected Mach number of the DSO is \( M = v_{\text{rel}}/c_s \leq 10 \) (Zajaček et al. 2016), where \( v_{\text{rel}} \) is the relative velocity of the DSO with respect to the medium and \( c_s \) is the local sound speed. This necessarily leads to the formation of the bow shock layer whose densest part lies ahead of the star close to the stagnation point. It was shown that the bow shock of the DSO can contribute to the continuum as well as line emission of the source (Scoville & Burkert 2013). The contribution of the bow-shock NIR continuum emission depends on the dust content and dust size distribution in the bow shock layer, which by itself is not a trivial hydrodynamical problem (van Marle et al. 2011). However, the existence of a bow...
shock would further increase the overall asymmetry of the source and hence make the total linear polarization degree larger, see Fig. 9.

For modelling the stellar bow shock associated with the supersonic motion of the DSO, we apply the analytical model of Wilkin (1996) for the shape of the axisymmetric layer,

$$ R(\theta) = R_0 \csc \theta \sqrt{3(1 - \theta \cot \theta)}, \quad (11) $$

where $\theta$ is a polar angle from the axis of symmetry as seen from the star that lies at the coordinate origin. The standoff distance $R_0$ depends on two intrinsic stellar parameters – the mass-loss rate $\dot{m}_w$ and the terminal wind velocity $v_w$ – as well as the density profile of the ambient medium $\rho_a(r)$ and the relative velocity of the star with respect to the ambient medium $v_{rel}$. The general form for the standoff distance is (Wilkin 1996; Zhang & Zheng 1997; Christie et al. 2016),

$$ R_0 = \left( \frac{\dot{m}_w v_w}{\Omega(1 + \beta)\rho_a v_{rel}^2} \right)^{1/2}, \quad (12) $$

where $\beta$ is the ratio of the thermal and the ram pressure of the ambient medium, $\beta = P_\text{th}/P_\text{ram}$. When a star moves supersonically, its Mach number is larger than one, $M = v_{rel}/c_s = 1/\sqrt{\beta} > 1$, where $\kappa$ is an adiabatic index. When the thermal pressure is low, that is the ram pressure is much higher than the thermal pressure of the medium, the term $\beta \to 0$. For the ambient medium, we assume the radial profile as in Zajaček et al. (2016),

$$ n_a \approx n_0 \left( \frac{r}{r_0} \right)^{-\gamma_a}, \quad (13) $$

$$ T_a \approx T_0 \left( \frac{r}{r_0} \right)^{-\gamma_T}, \quad (14) $$

where we set $r_0$ to the Schwarzschild radius $r_s \left( r_s \equiv 2GM_*/c^2 \approx 2.95 \times 10^5 M_\odot/M_\odot \text{cm} \right)$. The normalisation parameters are $n_0^a = 1.3 \times 10^6 \text{cm}^{-3}$ and $T_0^a = 9.5 \times 10^4 \text{K}$ and the power-law indices are $\gamma_a \approx \gamma_T \approx 1$. At the pericentre, the estimated distance of the DSO according to Valencia-S. et al. (2013) is $r_p = a(1-e) \approx 1925 r_s$ and the corresponding orbital velocity is $v_p \approx 6600 \text{km s}^{-1}$. If we assume $v_{rel} \approx v_p$ and $\kappa \approx 1$, then the factor $\beta \approx 0.01$, so the thermal pressure may be neglected at the pericentre.\footnote{The factor $\Omega$ is the solid angle, into which the stellar wind/outflow is blown. For a general case, the factor $\Omega = 2\pi(1 - \sin^2 \theta_0)$, where $\theta_0$ is a half-opening angle of the outflow. For an isotropic stellar wind, we have $\theta_0 = \pi$, and so we naturally get $\Omega = 4\pi$. For bipolar cavities with $\theta_0 = \pi/4$, we get $\Omega = 2\pi(1 - \sqrt{2}/2) \approx 1.84$.}

The density of the shocked wind layer $\rho_{sh}$ may be estimated from the Rankine-Hugoniot jump conditions (Christie et al. 2016),

$$ \rho_{sh} = \rho_a \left( \frac{\kappa + 1}{\kappa - 1} \right) \left( \frac{v_{rel}}{v_w} \right)^2 (1 + \beta). \quad (15) $$

In case the motion of the ambient medium may be neglected, $v_{rel} = v_*$, and the thermal pressure is negligible (close to the pericentre), $\beta \to 0$, then the relative change in density of the shocked layer between the years 2008–2012 (or any two points at the distance of $r_0$ and $r'$ along the orbit) may be expressed as,

$$ \frac{\rho'}{\rho_0} = \left( \frac{r_0}{r'} \right)^{\gamma+1} \left( \frac{2a - r'}{2a - r_0} \right). \quad (16) $$

\footnote{However, at the apocentre of the DSO orbit, the factor $\beta \approx 0.9$, since the ratio of the thermal factors at the apocentre and the pericentre may be expressed as $\beta_a/\beta_p = (1 + e)/(1 - e)$.}
which for $\gamma_0 = 1$ and the orbital elements according to Valencia-S. et al. (2015) yields $\rho_{2012}/\rho_{2008} \approx 4.35$. The number density of the shocked layer as function of time as well as the relative change between the years (2008-2012) are plotted in Fig. 8 in left and right panels, respectively. For these calculations, the thermal term was included according to Eq. (15), which explains a small difference with respect to the estimate of the relative density increase above. The stellar parameters were adopted from the previous analysis of Scoville & Burkert (2013) and Zajacék et al. (2016): the mass-loss rate $m_\text{w} = 10^{-8} M_\odot \text{yr}^{-1}$ and variable wind velocities in the range 10–1000 km s$^{-1}$. For the radiative transfer simulations, we tried different values of the bow-shock density and the best match to the observed SED and the polarized emission was reached for $v_\text{w} = 10 \text{ km s}^{-1}$, which is a rather slow outflow.

The summary of the polarization degree and the source colour ($K_s - L'$) (with and without line-of-sight extinction) for all the circumstellar geometries, which were tested, is summarized in Table 4. In total, there are eight radiative transfer models presented as well as corresponding, observationally inferred values.

### 4.1.2. Final model: supersonic, dust-enshrouded star with non-spherical envelope

From the set of radiative transfer simulations with different circumstellar geometries (see Table 4), the model that can meet all constraints listed in Table 3 consists of the following components:

- a pre-main-sequence star;
- spherically concentrated dusty envelope/geometrically thick disc;
- bipolar cavity with a half-opening angle $\theta_0 = 45^\circ$;
- bow shock.

The detailed discussion of the adopted parameters and densities of the gas/dust envelope is in the previous subsection. The illustration of the model is in Fig. 10 (left panel). An important parameter in terms of the intrinsic geometry is the angle $\delta$ that determines the orientation of the bipolar outflow with respect to the axis of symmetry of the bow shock. Unless otherwise indicated, we set $\delta = 0^\circ$, that is the bipolar cavities are aligned with the symmetry axis of the bow shock.

An exemplary model SED is in Fig. 10 (right panel) calculated for the viewing angle of 90°. Here we use the same convention for the viewing angle as Mužić et al. (2010, see their Fig. 3) – 0° corresponds to the front view of the bow shock (circular shape in projection), 90° corresponds to the side view (bow-shock shape), and 180° corresponds to the view from the tail part (also circular shape in projection). The thick black solid line represents the total continuum flux density and thinner, grey lines stand for individual components: stellar emission, scattered emission, and scattered dust emission. It is important to note the total linear polarization degree as function of wavelength is depicted in Fig. 11 (right panel). The largest total polarization degree is $\lesssim 10\%$, since the source appears rather circular.

The linear polarization degree as function of wavelength is depicted in Fig. 11 (right panel). The largest total polarization degree, $P_L \geq 20\%$, is for the viewing angles close to 90° when the source is highly non-spherical. On the other hand, for the viewing angle either close to 0° or 180°, the total linear polarization degree is $\lesssim 10\%$, since the source appears rather circular.

The dependence of the total linear polarization degree in $K_s$ band on the inclination is in Fig 12 (right panel). The largest total polarization degree, $P_L \geq 20\%$, for the viewing angles close to 90° when the source is highly non-spherical. On the other hand, for the viewing angle either close to 0° or 180°, the total linear polarization degree is $\lesssim 10\%$, since the source appears rather circular.

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for the largest density (epoch 2012.0). Given our model set-up and an expected range of viewing angles (see the shaded area in Fig. 12), the polarization degree of ~30% is better reproduced by the configuration, in which the position angle δ of the bipolar outflow is between 0°–45°, that is more aligned towards the bow-shock symmetry axis. When the orientation of the bipolar outflow is perpendicular to the symmetry axis, δ = 90°, the dependence of the polarization degree on the inclination is rather flat and stays below or around 20%.

Qualitatively, all the polarization curves in Fig. 11 (right panel) have a peak that is close to 2.2 µm for the viewing angles around 90°, and the peak shifts towards shorter wavelengths for both smaller and larger viewing angles than 90°. The curves resemble the empirical Serkowski law, $p_L = p_{\text{max}} \exp \{ -K \ln^2 (\lambda_{\text{max}} / \lambda) \}$ (Kolokolova et al. 2015), where $\lambda_{\text{max}}$ is the wavelength at which the polarization curve reaches the maximum $p_L = p_{\text{max}}$ and the coefficient $K$ determines the width of the curve. However, the Serkowski law is used to fit the linear polarization degree in the ISM that arises due to dicroic extinction, whereas the simulations presented here are performed for spherical grains, and without the implementation of the magnetic field, whose configuration at the studied distances from Sgr A* is still highly uncertain and beyond the scope of this paper.

The variation of the position angle δ of the bipolar cavity leads to the change of the brightness distribution in the total as well as the linearly polarized light, and hence the change of the polarization angle Φ. In Shahzamanian et al. (2016) we fitted the dependency of the polarization angle on the position angle with the relation that is approximately equal to $\Phi \approx -(+δ + (-)90°$ (see Fig. 9 in Shahzamanian et al. 2016). This relation is also

Fig. 10. Left: illustration of the components of the DSO model explained as a pre-main-sequence star. The right side explains possible sources of the changes in the continuum emission of the DSO/G2 (polarization degree and angle). Right: calculated SED for the composite model of the DSO (star, dusty envelope, bipolar cavities, bow shock) for the viewing angle of 90°. The thick solid line stands for the total continuum flux density, whereas grey lines represent individual source contributions (see the key). The points represent observationally inferred flux densities/limits for H, Ks, L′, and M bands.

Fig. 11. Left: spectral energy distribution of the composite stellar model of the DSO as function of the viewing angle. The points represent observationally inferred values. Different viewing angles from 0° up to 180° are labelled by different colours according to the key. Right: linear polarization degree as function of wavelength for different viewing angles (see the key). The vertical thick line marks the values along the $K_s$ band (2.2 µm), the horizontal line denotes the value of $p_L = 30\%$, which is close to observationally inferred values for four consecutive epochs (2008, 2009, 2011, 2012; Shahzamanian et al., 2016).
Fig. 12. Left: schematic plot of the bow-shock evolution of the DSO along the orbit. The mass-loss rate was taken to be $\dot{m}_w = 10^{-8} \, M_\odot \, \text{yr}^{-1}$ and the terminal wind velocity is $v_w = 100 \, \text{km} \, \text{s}^{-1}$. The ambient density was colour-coded according to the direction expression by Eq. (13). Right: total linear polarization degree in $K_\alpha$ band for different inclinations (0–180 degrees) of the DSO composite model. According to the key, the solid lines represent different epochs, 2008–2012, with a gradually increasing bow-shock density (see also Fig. 8). The three orange lines associated with the largest bow-shock density represent the set-ups for three different position angles of the bipolar outflow, $\delta = 0^\circ$, $45^\circ$, and $90^\circ$. The shaded rectangular regions represent different angles of the bow-shock axis with respect to the line of sight for the period of 10 yr before the pericentre passage of the DSO, assuming a negligible motion of the ambient medium in comparison with the orbital velocity of the DSO. The horizontal dashed line marks the polarization degree value of $p_L = 30\%$, which is approximately the observationally inferred degree for the DSO (Shahzamanian et al. 2016).

evident in the simulated images of the linear polarized light in Fig. 13, where we change the position angle in $45^\circ$ steps from $0^\circ$ up to $90^\circ$ (from the top to the bottom panels in Fig. 13). Most of the scattered, polarized light comes from the region where the bipolar cavities intersect the bow-shock shell. On the other hand, the minimum of the polarized emission is overlapping naturally with the optically thick dusty envelope that also hides the star at the centre.

Shahzamanian et al. (2016) measured a variable polarization angle for four epochs, see their Fig. 4 (right panel). There are two possible mechanisms that can be employed to explain a variable polarization angle – see also the left panel of Fig. 10 for the illustration:

(i) intrinsic changes in the star-envelope orientation: these changes would be due to the torques induced by the massive black hole, which would lead to the precession of the circumstellar disc/bipolar outflows in case the disc is misaligned with respect to the orbital plane. The precession time-scale is longer than the orbital time-scale, $T_{\text{prec}} > T_{\text{orb}}$. On the other hand, the wobbling of the disc takes place on the time-scale shorter than one orbital period, approx. $T_{\text{wobble}} \approx 1/2 T_{\text{orb}}$ (Bate et al. 2000);

(ii) external interaction of the star with the nuclear outflow/inflow: such an interaction could change the viewing angle on the star-bow shock-bipolar outflow system, especially for the case when the outflow/inflow velocity is comparable to the orbital velocity of the star, which would significantly affect the relative velocity, $v_{\text{rel}} = v_{\text{star}} - v_{\text{w}}$, and hence also the orientation of the bow shock with respect to the observer, see the modelling by Zajaček et al. (2016).

The simulated RGB image (Red colour – $L^\prime$ band, Green colour – $M$ band, Blue colour – $K_\alpha$ band) of the source model of the DSO is in Fig. 14 with the labels of the components. For the simulated image, we set the position angle $\delta$ to $90^\circ$, that is perpendicular to the symmetry axis of the bow shock (compare with the simulated image in Fig. 11 in Shahzamanian et al. 2016, which was computed for $\delta = 0^\circ$). The inset in Fig. 14 illustrates the magnetospheric accretion that was used to explain the origin of the broad Bry line of the DSO (Valencia-S. et al. 2015; Zajaček et al. 2015).

Independently of the previous analysis, where the $K_\alpha$-band flux density is linearly polarized mainly due to dust photons scattering off spherical dust grains, a correlation was found between the linear polarization degree in $K_\alpha$ towards luminous stars embedded in molecular clouds and the optical depth $\tau_{K_\alpha}$, which can be fitted by a power law (Kolokolova et al. 2015),

$$P_{L,K} = 2.2 \tau_{K_\alpha}^{0.75} \%.$$

Jones et al. (1992) explain this correlation by a 50/50 mixture of the constant, that is a perfectly aligned component to the magnetic field, with random components.

When applied to the DSO with $P_{\text{DSO}} \approx 30\%$, we get $\tau_{\text{DSO}} \approx 33$ as an estimate for the optical depth to the object along the line of sight, most of which can be attributed to the locally dense, optically thick envelope surrounding the stellar core. Similar values for the polarization degree and the optical depth in $K_\alpha$ band were found for the Becklin-Neugebauer object and OMC1-25 in the Orion star-forming region (Kolokolova et al. 2015), which are both deeply embedded objects detected as prominent infrared excess sources.

4.1.3. Effect of surrounding stars on the polarized emission

In the previous analysis, we assumed that the main source of photons that are absorbed and scattered off dust grains in the surrounding envelope is the star at the centre. The question arises to what extent other stars in the S cluster contribute to the detected polarized emission. There are about $N_S = 30$ stars of mostly spectral type $B$ in the innermost arcsecond, $r_{{\text{S}}} \approx 1'' \approx 0.04$ pc (Eckart et al. 2005). Under the assumption of an approximately uniform distribution of stars in the sphere of radius $r_{{\text{S}}}$, this gives the stellar number density in the $S$ cluster $n_S = N/4(3/4)^{1/3} \approx 10^5 \, \text{pc}^{-3}$. The average distance of any star from the DSO then is $D_{{\text{S}}} \approx (n_S)^{-1/3} \approx 0.02$ pc $= 4.4 \times 10^3$ AU.
Fig. 13. Simulated images of the total flux density in $K_s$ band (first panels from the left side), linearly polarized flux density (second panels from the left side), the distribution of the polarization degree (second panels from the right side), and the distribution of the polarization angle (first panels from the right side) for the different position angle of the bipolar outflow; $\delta = 0^\circ$, $45^\circ$, and $90^\circ$ from the top to the bottom panels.

The ratio of total fluxes at the position where photons are scattered off grains is,

$$
\frac{F_{DSO}}{F_S} = \left( \frac{T_{DSO}}{T_S} \right)^4 \left( \frac{R_S}{R_{DSO}} \right)^2 \left( \frac{D_S}{D_{DSO}} \right)^2,
$$

where $T_{DSO}$ and $T_S$ are effective temperatures of the DSO and a typical S star, respectively. For the DSO, assuming it is a pre-main-sequence star, we take the previous value $T_{DSO} \approx 4200$ K. For a typical B0 star, the effective temperature is $T_S \approx 25 000$ K. In terms of stellar radii, both the pre-main-sequence star and the B0 star have similar stellar radii of the order of $R_{DSO} \approx R_S \approx 10 R_\odot$. Finally, distances of stellar sources from the scattering material are approximately $D_S \approx D_{DSO} \approx 4.4 \times 10^3$ AU and for the DSO star, $D_{DSO} \approx 1$ AU. Plugging these estimated values into Eq. (18), we get $F_{DSO}/F_S \approx 1.5 \times 10^4$, hence the contribution of other S stars is on average negligible in comparison with the central source.

An occasional close approach of an S star could contribute more. However, if these events were frequent, they should be reflected in a larger degree of variability of both the total and the polarized continuum emission. So far the DSO has appeared to be a rather stable source (Shahzamanian et al. 2016).

4.2. Possible non-thermal origin of the SED: NIR-“excess” sources as young neutron stars?

In this subsection, we discuss the possibility that young neutron stars can in principle be detected in the central arcsecond of the Galactic centre and, under certain conditions, their characteristics would be similar to the Dusty S-cluster Object and other infrared excess sources, namely the positive spectral slope (larger flux density for longer wavelengths) and a significant polarized emission in NIR wavebands. As the first step, we check the energetics that would be required to produce flux densities comparable to the DSO. The flux density in $K_s$ band is $F_{K_s} = 0.23 \pm 0.02$ mJy (see Table 2). This leads to the overall $K_s$ band luminosity of $L_{K_s} = \nu F_\nu 4\pi r^2 = 0.23 \times 10^{-3} \times 10^{-23} \times 1.36 \times 10^{14} \times 4\pi (800 \text{ pc})^2\text{ erg s}^{-1} = 2.4 \times 10^{33}\text{ erg s}^{-1}$. This luminosity is of the same order of magnitude as the one found for PSR B0540-69 in the Large Magellanic Cloud (Mignani et al. 2012). Mignani et al. (2012) also show that the $K_s$ band luminosity and the spin-down energy $\dot{E}$ are correlated, $L_{K_s} \propto \dot{E}^{1.72 \pm 0.03}$, which implies that NIR emission is rotation-powered and associated with the magnetospheric origin and/or the neutron star wind termination shock. Using the correlation, $L_{K_s} \approx 6.1 \times 10^{-33}\dot{E}^{1.72}$.
we can estimate a spin-down power of the pulsar potentially associated with the DSO, \( E_{\text{DSO}} \approx 1.4 \times 10^{38} \text{ erg s}^{-1} \), which is of the same order of magnitude as the Crab pulsar, J0534+2200 (Manchester et al. 2005).

Hence, the neutron star associated with the DSO and other NIR-excess sources would have to be a rather young, Crab-like PWN with the characteristic age of \( \tau = P/2P \approx 10^3 \) yr, where \( P \) is a pulsar period and \( P \) is the period derivative or spin-down rate. The origin would be young, massive OB stars having an age of a few millions observed in the central parsec (Buchholz et al. 2009). The power-law slope inferred for the DSO, see Eq. (1), is qualitatively consistent with the observations of neutron stars in near-infrared bands (Mignani et al. 2012; Zharikov et al. 2013; Zyuzin et al. 2016), however, it appears to be steeper than for observed pulsars (Mignani et al. 2012), which have the mean spectral index \( \alpha \approx 0.7 \).

TheSED alone does not give any convincing argument for the neutron star hypothesis and the dust-enshrouded star is thought to be a more natural scenario. On the other hand, the detection of linearly polarized emission in \( K_s \) band and a high polarization degree of \( \sim 30\% \) (Shahzamanian et al. 2016) imply that the DSO may indeed be a peculiar source in the S cluster and the neutron star model can naturally explain the polarized emission via the synchrotron mechanism in the dipole magnetic field, see Eq. (8). For instance, the infrared imaging and polarimetric observations of the PWN SNR G21.5-0.9 (Zajczyk et al. 2012) indeed show a high degree of linear polarization in \( K_s \) band, \( P_L \approx 0.47 \) and a comparably high polarization degree is expected for other PWNe.

Young, rotation-powered neutron stars are expected to have radio and X-ray counterparts whose luminosities are proportional to the spin-down power \( E_{\text{rad}} = -E_{\text{spin-down}} = 4\pi^2 I P/\dot{P}^2 \), where \( I \) is the moment of inertia of the neutron star, \( \dot{P} \approx 10^{-8} \text{ g cm}^2 \). In general, there seems to be a trend of increasing radiative efficiency \( \eta_r \) towards shorter wavelengths, \( \eta_r \equiv L_{\text{rad}}/E_{\text{rad}} \), where \( f \) is the spectral domain (Lorimer & Kramer 2012).

In the X-ray domain, the scatter of efficiencies is relatively small, and approximately equal to \( \eta_r \approx 10^{-4} \) (Kargaltsev & Pavlov 2007). In case of the pulsar and its wind nebula associated with the DSO, this gives an estimate of the X-ray luminosity \( L_X = \eta_r E_{\text{DSO}} \approx 10^{36} \text{ erg s}^{-1} \), which is, given the uncertainties, comparable to the quiescent X-ray emission of Sgr A*, \( L_{X,\text{Sgr A*}} \approx 10^{33} \text{ erg s}^{-1} \) (Yuan & Narayan 2014), associated with the thermal bremsstrahlung process in the hot plasma surrounding Sgr A*.

Towards the radio domain, the radiative efficiency for rotation-powered pulsars becomes smaller and the scatter is larger, \( \eta_r \approx 10^{-8} - 10^{-5} \), which leads to the values for the pulsar associated with the DSO, \( L_R = \eta_r E_{\text{DSO}} \approx 10^{26} - 10^{31} \text{ erg s}^{-1} \), which is smaller or comparable to the luminosity of Sgr A* in this domain (Yuan & Narayan 2014). In some cases, pulsars are only detected at higher energies and appear to be radio-quiet (e.g. Geminga pulsar; Camilo 2003) under the sensitivity constraints of radio surveys, which either implies that the radio beam is narrow and not directed at the Earth or that radiative efficiencies in the radio domain for some young pulsars are smaller in comparison with X-ray and γ-ray domains.

So far no clear X-ray and radio counterparts of the DSO were detected (Bower et al. 2015; Mossoux et al. 2016; Borkar et al. 2016). However, given the rough estimates above, a high background flux towards Sgr A*, and low angular resolution in the X-ray domain, even young pulsars of a Crab type could be beyond the sensitivity limits of current X-ray and radio instruments. Therefore, weak, infrared excess sources similar to the DSO could be candidates for pulsars and deserve follow-up monitoring with upcoming, high-sensitivity facilities (E-ELT, Square Kilometer Array – SKA).

Given the large orbital velocities of stars and potential stellar remnants in the S cluster with respect to the ambient medium, PWN are expected to be non-spherical and elongated in the direction of the motion. The length-scale of the termination-shock of the pulsar wind is given by the pressure balance as expressed by Eq. (12), where the wind pressure term \( p_w = m_w v_w^2/(4\pi r^2) \) is replaced by \( p_{\text{pwn}} = E_{\text{rad}}/(4\pi r^2) \), which leads to the stand-off distance

\[
R_{\text{pwn}} = \left( \frac{E_{\text{rad}}}{4\pi \rho_0 v_w^2} \right)^{1/2},
\]

where we neglected the thermal term. The relative velocity with respect to the ambient medium can be approximated by the orbital velocity close to the pericentre of the orbit, \( v_\text{rel} \approx v_\text{per} \). Taking \( E_{\text{rad}} = 1.4 \times 10^{38} \text{ erg s}^{-1} \) as estimated for the pulsar potentially associated with the DSO, we calculate the evolution of the stand-off distance according to Eq. (19) during the period of 10 yr before the pericentre passage, see Fig. 15. We see that even for a relatively young PWN with the spin-down energy of the same order as the Crab pulsar, the stand-off distance is comparable or smaller than the diffraction limit of 63 mas, \( R_{\text{pwn}} \leq \theta_\text{min} \), that is the PWN would effectively appear as a point source, mainly due to a large relative velocity close to Sgr A*.

A detailed analysis of the generation of Bry line in the PWN is beyond the scope of this paper. We just note that the source of Bry could be the collisional excitation of hydrogen atoms prior to their ionization in the bow-shock layer, as was similarly suggested by Scoville & Burkert (2013) for a bow shock
associated with a T Tauri star. Specifically, there are several pulsar bow shocks that exhibit Hα emission (Cordes 1996; Brownberger & Romani 2014), and hence Brey line could be produced by the same process. Quantitatively, for three pulsars at kiloparsec distances – B0740-28, B1957+20, B2224+65 (see Table 2 in Chatterjee & Cordes, 2002) – the corresponding Hα luminosities are in the range of $L_{\text{H}\alpha} \approx 6.5 \times 10^{38} - 1.6 \times 10^{39}$ erg s$^{-1}$, that is $L_{\text{H}\alpha} \approx 2 \times 10^{-5} - 4 \times 10^{-6} L_\odot$, which is at least an order of magnitude less than the Brey luminosity of the DSO (Gillessen et al. 2012; Valencia-S. et al. 2015). In general, Chatterjee & Cordes (2002) derive a scaling relation for Hα luminosity of pulsars, $L_{\text{H}\alpha} \propto 4\pi X\dot{E}_\text{rad} v_\gamma$, where $X$ is a fraction of neutral hydrogen. Analogous dependencies are expected for Brey luminosity, under the assumption that the line is produced by the collisional excitation in the pulsar bow shock.

In addition, natal kick velocities during supernova explosions in the clockwise stellar disc could, under a certain configuration, lead to the formation of highly-eccentric orbits similar to that of the DSO; see the analysis of dynamics presented in Paper II. In summary, given the properties of the DSO and that of other NIR-excess sources, one cannot a priori exclude the PWN hypothesis as an explanation of the phenomenon.

5. Discussion

The focus of this paper was on the detailed analysis of the total and polarized continuum emission of the DSO in the NIR domain as explained by an enshrouded pre-main-sequence star model. A detailed analysis of other phenomena associated with the DSO, for example a tentative association with a larger tail/streamer, emission in other domains, and the analysis of the line emission are beyond the scope of this study. However, let us briefly comment on some of these aspects to put the continuum analysis in a larger context. These and other aspects of NIR-excess sources in the Galactic centre will also be examined in detail in upcoming papers of this series.

5.1. DSO/G2 and G1 as parts of a larger gaseous streamer?

It was claimed previously that DSO/G2 is accompanied by an elongated, low-surface-brightness tail that is clearly visible in the position-velocity diagrams (Gillessen et al. 2012, 2013a,b; Pfuhl et al. 2015). A dynamical connection of the DSO/G2 to the tail would favour the “gas-stream-like” scheme: according to this scenario, DSO would be a clump of a more extended filamental structure. However, this clump could still be compact and associated with a star; see also Ballone et al. (2016) for the hydrodynamical model of the “G2+G2t” complex. Indeed, the numerical models of the formation of young stars close to the supermassive black hole suggest that the star formation takes place in infalling gaseous clumps that undergo fragmentation and stretching (Jafali et al. 2014). The occurrence of denser clumps – protostars – embedded in a larger streamer is therefore expected in the earliest stages of the star formation in the strong gravity regime, where tidal forces cannot be neglected.

However, apart from the arguments above, the connection of the DSO to a larger filamentary structure is still disputed observationally, mainly because of a spatial and kinematical offset from the DSO (Eckart et al. 2014; Meyer et al. 2014; Pfiffer et al. 2013); see also Peissker et al. (in prep.). It is plausible that the tail is rather a back/foreground feature associated with the minispiral (Eckart et al. 2014). The denser filament in the south-east direction could be a result of the interaction of the northern and the eastern minispiral arms whose dynamics is consistent with two Keplerian bundles (see Fig. 21 in Zhao et al. 2009; and Fig. 10 in Vollmer & Duschl 2000). Meyer et al. (2014) also claim that while the DSO and the filament have similar radial velocities, there is a significant spatial offset, which is not visible in position-velocity plots of Gillessen et al. (2012, 2013a,b) and Pfuhl et al. (2015), who use an artificial curved slit of a finite width to extract radial velocities, which masks spatial offsets. This also means that the filament can be an artefact as the result of the masking process in the data reduction procedure, which implies that an apparent association of small line-emitting sources that have a spatial offset are grouped together in the position-velocity diagram.

The association of the PWN to a larger filament is also plausible, since it could be a remnant of the material from the supernova explosion, for example in the clockwise disc of massive OB stars. In this sense, the fast-moving pulsar can “catch up” with the expanding shell, as also seems to be the case of Sgr A East remnant and the “Cannonball” pulsar (Zhao et al. 2013).

Pfuhl et al. (2015) also propose a possible dynamical connection between the DSO/G2 object and G1 clump, that is both features could be parts of the same streamer and dynamically related. If this was the case, it could be used for constraining the properties of the accretion flow around Sgr A* (McCourt & Madigan 2016; Madigan et al. 2017), based on the amount of dragging, which is only prominent for core-less clumps. However, the association of these two, reddened sources is still under investigation and should be confirmed/excluded based on continuing monitoring – even if the inclination of both orbits is comparable, the orientation of the orbits in space can be different. Also, G1 object survived the pericentre passage, so it also seems less likely that it is a pure gas cloud (Sitarski et al. 2015). In summary, even if the DSO was associated with or moving through a larger gaseous structure, it would not rule out a young-star or PWN hypothesis presented in this study.

5.2. Core-less cloud models vs. stellar models of the DSO

Following the roadmap in Fig. 2, we will look at a few observables that distinguish the core-less cloud and stellar interpretation of the DSO. A dynamical comparison of the evolution of a
core-less cloud and a stellar model using a simplified test particle model was done in Zajaček et al. (2014). The basic result for an assumed density profile of the ambient medium was that a core-less cloud starts progressively deviating from the Keplerian orbit soon after the pericentre, where the velocity of the cloud as well as the density of the medium are the highest and therefore the non-gravitational acceleration due to a hydrodynamical drag is the largest as well; see also McCourt & Madigan (2016) and Madigan et al. (2017). The star is naturally much less sensitive to the ambient medium because of the smaller ratio of the cross-section to the mass, and follows the original trajectory. Up to now, the DSO does not deviate within uncertainties from the inferred highly-eccentric orbit (Peissker et al., in prep.), which may indicate a stellar nature. However, it could also be argued that the hydrodynamical drag is smaller due to a smaller ambient density than usually assumed in the models of RIAFs.

A stronger argument in favour of a stellar model is the compactness of the source as discussed in detail in Sect. 3. In K and L band continuum, the DSO is fully consistent with a point source (Eckart et al. 2014; Witzel et al. 2014; Shahzamanian et al. 2016). Concerning the analysis of Brr line emission, there are contradictory observational results. While Valencia-S. et al. (2015) detect a single-peak Brr emission at each epoch, both shortly before and after the peribothron passage (see their Fig. 8), which is consistent with a stellar model, Pfuhl et al. (2015), on the other hand, detect both a red-shifted peak and a blue-shifted peak for the same epoch (see their Fig. 15), which indicates the effect of stretching of the gas along the orbit. Despite this observational contradiction, it is difficult to reconcile an apparent compact continuum emission (tracing dust) and a stretched Brr emission (tracing gas) with the gas cloud model, since such a cloud would be expected to consist of a well-mixed gas-dust components. This was interpreted by Witzel et al. (2014) in terms of a binary merger model, which is accompanied by an expanding dusty outflow forming an optically thick photosphere (Pejcha 2014). Since binary mergers contract on a Kelvin-Helmholtz time-scale and are surrounded by a dusty envelope, they share several characteristics with pre-main-sequence stars. Therefore, our dust-enshrouded star model is applicable to this scheme.

In Schartmann et al. (2015), a compact cloud model is presented, where the authors claim that the cloud follows the Keplerian orbit and stays rather compact. However, for the epochs 2005–2015 the full width at half maximum of the normalized Brr emission in their model is clearly above the diffraction limit of 63 mas and reaches as much as 115 mas at the pericentre. Therefore, the cloud should have been clearly resolved at all epochs of the monitoring. In their model, the cloud also undergoes tidal stretching and disruption, with an expected enhancement in accretion as early as 2014

There have been several multi-wavelength observational campaigns that aimed at capturing the signs of the DSO/Sgr A* interaction. The X-ray flux density of Sgr A* was monitored by Chandra X-ray satellite and no increase in the quiescent X-ray emission was detected during 2013–2014 campaign (Haggard et al. 2014), which collected ~900 ks of data. Also, no change in the radio quiescent emission was detected (Bower et al. 2015; Borkar et al. 2016). This implies that the shock associated with the supersonic motion of the DSO was far less strong and bright than the predicted values (Narayan et al. 2012) that exceeded the quiescent level of Sgr A*. It means that either the actual source has a smaller cross-section than the one assumed for synchrotron calculations, \( \sigma \leq 2 \times 10^{27} \text{cm}^2 \) that corresponds to the diameter of \( D \lesssim 34 \text{AU} \) (Bower et al. 2015), or that the ambient medium is rather rarefied even in comparison with the original RIAF models.

Concerning the flaring activity of Sgr A*, there is no statistically significant enhancement detected in both X-ray and infrared bands (Valencia-S. et al. 2015; Mossoux et al. 2016). Based on the analysis of \( \sim 15 \) yr of XMM, Chandra, and Swift data, Ponti et al. (2015) discuss an increase in the rate of bright X-ray flares. However, an alternative and plausible explanation is an effect of the X-ray flare clustering (Haggard 2017) rather than the actual increase in the flaring rate, so the overall statistics does not seem to be affected by the DSO passage (Mossoux et al. 2016).

Nevertheless, it is of interest to estimate the non-thermal synchrotron or potential X-ray bremsstrahlung flux for the stellar model of the DSO. These estimates may also be scaled for different stellar parameters when other stars will pass in the vicinity of Sgr A* and future facilities with the larger sensitivity may detect the corresponding emission.

5.3.1. Bow-shock synchrotron emission

The source of the non-thermal synchrotron emission of the DSO are the electrons accelerated in the bow shock. We apply the theory and the model of Crumley & Kumar (2013) and Sadowski et al. (2013) (based on Rybicki & Lightman 1979) to calculate synchrotron spectra and the light curve of the source. In the left panel of Fig. 16, the spectra are calculated for the epoch of the pericentre passage, when the flux density is the largest across all frequencies. The right panel of Fig. 16 displays the light curve computed for the frequency of 1.4 GHz. For both the spectrum and the light curve, two limiting cases are taken into account:

(i) “plowing” model that assumes that all electrons accelerated in the bow shock radiate in the shock-enhanced magnetic field;

(ii) “local” model that assumes that the electrons accelerated in the shock leave it and radiate in the local, ambient magnetic field.

Two sets of stellar parameters were considered: the mass-loss rate of \( \dot{m}_w = 5 \times 10^{-9} \text{M}_\odot \text{yr}^{-1} \) and the wind velocity of \( v_w = 10 \text{km s}^{-1} \) and \( \dot{m}_w = 10^{-8} \text{M}_\odot \text{yr}^{-1} \), \( v_w = 10 \text{km s}^{-1} \), which are expected for a class 1 pre-main-sequence source (Edwards et al. 2006) with the empirical relation \( \dot{M}_w = 0.001–0.1 \text{M}_\odot \text{yr}^{-1} \) between the accretion rate and the outflow rate. For both parameter sets, the peak flux densities are at least two orders of magnitude smaller than the quiescent radio flux density of Sgr A*, that is the stellar model can naturally explain the non-detection of any enhancement in the flux density due to an expected small bow-shock size at the pericentre. In addition, the values are

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comparable to the radio flux density of the PWN, taking into account the radio efficiencies of $n_R \approx 10^{-6} - 10^{-5}$ and the spin-down luminosity of $E_{\text{rad}} = 1.4 \times 10^{38}$ erg s$^{-1}$. In summary, both stellar models – a dust-enshrouded pre-main-sequence star and a PWN – are expected to have radio flux densities below the quiescent level of Sgr A* , implying only a marginal possibility of detection of any change in the radio flux of Sgr A* and its close vicinity.

5.3.2. X-ray bremsstrahlung

Due to an expected supersonic motion of the DSO close to the pericentre (Zajaček et al. 2016), two layers of shocked stellar wind and ambient gas should form and subsequently mix. The shocked gas is expected to cool down by the thermal bremsstrahlung process (Christie et al. 2016). Here we use order-of-magnitude estimates to calculate the bremsstrahlung luminosity.

First, the ionized medium in the central parsec of the Galactic centre can in principle cause losses to the bremsstrahlung due to the Thomson scattering. We can estimate the optical depth of the scattering using $\tau_T \sim \sigma_T n_e L$, where $\sigma_T = 6.65 \times 10^{-25}$ cm$^2$ is the cross-section for the Thomson scattering, $n_e$ is the electron number density, and $L$ is the length of the part of the line of sight that crosses the hot gas. For an estimate, we take the number density of electrons at the Bondi radius, $n_e(R_B) \approx 130$ cm$^{-3}$ (Baganoff et al. 2003) and the line-of-sight length is set to the Bondi radius, $L = R_B$. Finally, the estimate gives $\tau_T \sim 4.3 \times 10^{-5} \ll 1$ and therefore the Thomson scattering losses can be neglected.

We take the volume emission coefficient per unit frequency band and integrate it over the frequency interval of the X-ray band, $(\nu_1, \nu_2) = (0.04, 0.8) \times 10^{18}$ Hz. For the volume emission coefficient $\epsilon_v$ holds (Lang 1978; Rybicki & Lightman 1979),

$$\epsilon_v d\nu \approx 5.4 \times 10^{-39} Z^2 T_{\text{sh}}^{-1/2} n_e n_i g(\nu, T_{\text{sh}}) \times \exp\left(-\nu / kT_{\text{sh}}\right) d\nu \text{ erg s}^{-1} \text{ cm}^{-3} \text{ Hz}^{-1}, \quad (20)$$

Fig. 16. Left panel: calculated synchrotron spectrum for electrons accelerated in the bow shock. Spectra were calculated for two sets of the mass-loss rate and the terminal wind velocity that are within the range of values expected from the stellar model: $m_w = 5 \times 10^{-9} M_\odot \text{ yr}^{-1}, v_w = 10 \text{ km s}^{-1}$ and $m_w = 10^{-8} M_\odot \text{ yr}^{-1}, v_w = 100 \text{ km s}^{-1}$. Solid lines correspond to the plowing synchrotron model and the dashed lines to the local model. The energy spectrum of accelerated electrons has a power-law index of $p = 2.4$ in accordance with particle-in-cell simulations of Sądowski et al. (2013). The red points are observationally determined values adopted from Davies et al. (1976), Falcke & Markoff (2000), Zhao et al. (2003), and Marrone et al. (2008). The shaded region represents an estimate of the radio flux density of the PWN. Right panel: a synthetic light curve calculated at 1.4 GHz considering for both the plowing (solid lines) and the local model (dashed lines). Two sets of stellar parameters were considered as in the left panel.

where $Z$ is the proton number of participating ions, $n_i$ and $n_e$ are number densities of ions and electrons, respectively, and $T_{\text{sh}}$ is the temperature of the shocked gas. The temperature of the shocked ambient medium for the supersonic motion of the DSO may be estimates as $T_{\text{sh}} = 1.38 \times 10^4 (v_e / 100 \text{ km s}^{-1})^2$ K for an ionized medium (McKee & Hollenbach 1980), which yields $T_{\text{sh}} \approx 10^8 - 10^9$ K for relative velocities of $v_e \sim 10^2 \text{ km s}^{-1}$ close to the pericentre. The shocked stellar wind is colder by about three orders of magnitude (Scoville & Burkert 2013), but denser, so it is likely to contribute more to the overall bremsstrahlung.

The Gaunt factor $g(\nu, T_{\text{sh}})$ may be approximated in the given range ($T_{\text{sh}} = 10^8 - 10^9$ K, $\nu = 10^{18}$ Hz) via (Lang 1978)

$$g(\nu, T_{\text{sh}}) \approx \frac{\sqrt{3}}{\pi} \log\left(4.7 \times 10^{10} T_{\text{sh}} / \nu\right), \quad (21)$$

Fig. 17. Temporal evolution of the X-ray bremsstrahlung signal from two components: shocked wind (black solid line) and shocked ambient medium (blue dashed line). Two vertical lines represent the quiescent emission of Sgr A*, $L[2-10 \text{ keV}] \approx 2 \times 10^{37}$ erg s$^{-1}$ (Haggard 2017), and the estimated PWN signal, assuming the conversion factor of $\eta_X = 10^{-4}$ between the spin-down luminosity and the X-ray luminosity. The stellar parameters were set to $M_w = 10^{-8} M_\odot \text{ yr}^{-1}$ and $v_w = 100 \text{ km s}^{-1}$.
which varies only a little for the considered frequency range. According to Eckart (1983), we set \( \sigma(T, \gamma) = 1.5 \). Using Eq. (20), the bremsstrahlung luminosity can be expressed as,

\[
L_{\text{brems}} \sim 5.4 \times 10^{-39} \times 4\pi \times 1.5 V_{\text{sh}}^2 T_{\text{sh}}^{-1/2} n_{\text{te}}^2 \int_{v_{\text{sh}}}^\infty \exp(-hv/kT_{\text{sh}})dv \text{ erg s}^{-1}.
\]

(22)

The integral \( \int_{v_{\text{sh}}}^\infty \exp(-hv/kT_{\text{sh}})dv \) yields \( 0.63 \times 10^{10} T_{\text{sh}} \) (Eckart 1983). Furthermore, we express the temperature of shocked gas in \( T_{\text{sh}} \equiv (T_{\text{sh}}/10^8 \text{ K}) \) and assume that the shocked gas consists fully of ionized hydrogen and helium, so one can replace the term \( Z^2 n_{\text{te}} \approx 1.55 n_{\text{e}}^2 \). We approximate the volume of the shocked gas by a spherical half-shell with the volume of \( V_{\text{sh}} \sim 2\pi R_{\text{sh}}^2 n_{\text{e}} \), where \( R_{\text{sh}} \) is the ratio of the bow shock thickness to the stand-off radius, Eq. (12). Finally, the bremsstrahlung luminosity becomes

\[
L_{\text{brems}} \sim 6.2 \times 10^{-23} R_{\text{sh}}(t) R_{\text{sh}}(t) n_{\text{e}}^2 T_{\text{sh}}^{7/2} \text{ erg s}^{-1},
\]

(23)

where both the stand-off radius \( R_{\text{sh}}(t) \) and the ratio \( R_{\text{sh}}(t) \) depend on the orbital phase (time) of the DSO (Zajaček et al. 2016; Christie et al. 2016).

We calculate the bremsstrahlung luminosity using Eq. (23) for both shocked layers, ambient and stellar wind layers. The density of the shocked stellar wind is computed using Eq. (15) and we take the temperature of \( T_{\text{sh}} \approx 10^8 \text{ K} \). The shocked ambient medium is denser than the ambient profile, Eq. (13), by about a factor of four and its temperature reaches \( T_{\text{sh}} \approx 10^8 \text{ K} \). For both cases, the stellar mass-loss rate is set to \( \dot{M}_\text{w} = 10^{-8} M_\odot \text{ yr}^{-1} \) and the wind velocity to \( v_{\text{w}} = 100 \text{ km s}^{-1} \). In Fig. 17, we plot the bremsstrahlung light curves for both layers. In case of the shocked wind, the luminosity increases because of the dominant density term — the density in the shocked layer increases towards the pericentre. For the shocked ambient medium, the overall luminosity decreases because of the dominant size term, that is the size of the bow shock decreases. The bremsstrahlung signal from the shocked wind should dominate, but its luminosity is at least three orders of magnitude smaller than the quiescent luminosity of Sgr A*, \( L_{\text{Bry}} \sim 10^{-20} \text{ erg s}^{-1} \) (Haggard 2017). The X-ray flux from the hypothetical PWN is expected to be stronger, at least at the level of the quiescent emission of Sgr A*.

The low level of the X-ray bremsstrahlung emission for a stellar wind shock is not surprising. During the passage of S2 star through the pericentre in 2002, there was no significant increase in the emission of Sgr A* detected (Yuan & Wang 2016). It is worth monitoring the flaring rate during the next passage in early 2018, since some theoretical calculations predict the emission at the level of the quiescent state (Christie et al. 2016).

5.4. Bry emission model for a young star

One of the prominent features of the DSO are the recombinations emission lines, mainly Bry line that is used for monitoring. So far and quite surprisingly, the luminosity of Bry line has remained constant within uncertainties (Gillessen et al. 2013a,b; Valencia-S. et al. 2015). It is not straightforward to explain the plateau of the light curve within the stellar model. In the framework of a photoevaporating and tidally disrupted protoplanetary disc, Murray-Clay & Loeb (2012) predict that the total Bry luminosity at the peribothron should be larger by a factor of five with respect to 2011 epoch. In case Bry recombination line originates due to the collisional ionization in the bow shock, the luminosity should also increase by a factor of a few (Scoville & Burkert 2013; Zajaček et al. 2016).

One of the simplest solutions to the plateau of Bry line is to look for processes that are independent of the distance from Sgr A* and of the velocity of the DSO. Circumstellar outflows and inflows that originate within the tidal radius of the DSO \( r_t \) (see Sect. 3) belong to such processes as was suggested by Valencia-S. et al. (2015). A likely process contributing to Bry emission in class I objects is the accretion of gas from the inner rim of an accretion disc that is truncated by a dipole magnetic field. The inferred large line width of Bry line of the order of \( FWHM_{\text{Bry}} \approx 100 \text{ km s}^{-1} \) (Phifer et al. 2013; Valencia-S. et al. 2015) is consistent with the magnetospheric accretion model (Hartmann et al. 1994; Edwards et al. 1994; Mužerolle et al. 1998), where the disc gas is channelled along magnetic field lines from the truncation radius \( r_t \) onto the stellar surface. The poloidal velocities are close to a free-fall velocity,

\[
e_{\text{pol}} = 618 \left( \frac{M_\ast}{M_\odot} \right)^{1/2} \left( \frac{R_\ast}{R_\odot} \right)^{-1/2} f_T \text{ km s}^{-1},
\]

(24)

where \( f_T = \sqrt{1 - 4 R_\ast/R_t} \) is the truncation factor, correcting the free-fall velocity for the finite truncation radius. Pre-main-sequence stars exhibit a considerable magnetic field with an intensity of \( \sim 1 \text{ kG} \), which truncates an accretion disc at several stellar radii,

\[
\frac{R_T}{R_\ast} \approx 6.5 B_3^{1/2} R_{2,5}^6 M_3^{-2/7} M_1^{1/7},
\]

(25)

where the strength of the dipole magnetic field at the equator of the star \( B_3 \) is in kG, the stellar radius \( R_2,5 \) is in units of \( 2,5 \text{ R}_\odot \), the accretion rate \( M_3 \) is in \( 10^{-8} M_\odot \text{ yr}^{-1} \), and the stellar mass \( M_1 \) is expressed in \( 1 M_\odot \). Using an estimate in Eq. (25), the truncation factor in Eq. (24) is \( f_T = 0.9 \), which leads to \( e_{\text{pol}} \approx 560 \text{ km s}^{-1} \). The line-of-sight velocity of the accreting gas that determines the Doppler broadening of an emerging line depends on the viewing angle of the star-disc system, which is itself variable for any structure bound to the star, for example a bow shock or a disc (see Appendix A for the calculation of the viewing angle).

A stationary accretion can only proceed when the disc truncation radius is inside the corotation radius, which is defined as the distance from the star where the Keplerian angular velocity equals to the rotational angular velocity of the star,

\[
R_{\text{co}} \approx 4.2 M_1^{1/3} P_1^{2/3} R_\odot,
\]

(26)

where \( P_1 \) is the stellar rotational period in units of one day.

For pre-main-sequence stars, a correlation was found between the accretion luminosity \( L_{\text{acc}} \) and the luminosity of Bry emission. The correlation does not have to necessarily imply that Bry is a tracer of accretion (Mendigutía et al. 2015) or that the emission originates within a few stellar radii from the star. We can, however, use the \( L_{\text{acc}} - L_{\text{Bry}} \) correlation to show that a realistic accretion rate can reproduce the observed, approximately constant Bry luminosity of \( L_{\text{Bry}} \approx (1 - 4) \times 10^{-3} L_\odot \) for the DSO (Gillessen et al. 2013a,b; Pfuhl et al. 2015; Valencia-S. et al. 2015). Applying the correlation inferred from a recent fit to several low-mass stars (Alcalá et al. 2014),

\[
\log (L_{\text{acc}}/L_\odot) = 1.16(0.07) \log (L_{\text{Bry}}/L_\odot) + 3.60(0.38),
\]

(27)

The relation for the truncation radius, Eq. (25), gives an upper limit, since the ram gas pressure is larger in the disc geometry than in a spherical approximation that was used for this derivation.
we get the accretion luminosities $L_{\text{acc}} \approx 1.3-6.6 L_\odot$. Hence, the accretion luminosity may be in principle a significant fraction of the continuum emission of the DSO.

Having calculated an order of magnitude of the accretion luminosity allows us to estimate the accretion rate $M_{\text{acc}}$, assuming a certain value for the truncation radius $R_T \approx 5 R_\star$.

$$M_{\text{acc}} \approx \frac{L_{\text{acc}} R_\star}{GM_\star} \left(1 - \frac{R_\star}{R_T}\right)^{-1} \approx 4.1 \times 10^{-8} \left(\frac{L_{\text{acc}}}{L_\odot}\right) \left(\frac{R_\star}{R_\odot}\right) \left(\frac{M_\star}{M_\odot}\right) M_\odot \text{yr}^{-1}.$$ (28)

Given the constraints on the mass and the radius of the DSO based on the bolometric luminosity of $30 L_\odot$ (see Fig. 5), $M_{\text{DSO}} \lesssim 3 M_\odot$ and $R_{\text{DSO}} \lesssim 10 R_\odot$, respectively, the upper limit of the accretion rate is $M_{\text{acc}} \lesssim 10^{-7} M_\odot \text{yr}^{-1}$. The gas accretion in young stellar systems seems to be linked to stellar and circumstellar outflows with the rate of $\dot{M}_w \approx 0.001-0.1 M_{\text{acc}}$ (Edwards et al. 2006).

Hence, the simple model of the accretion described above complements the previous components of the DSO model analysed in Sect. 4, see also Fig. 14 for an illustration. The accretion of gas onto the star and associated outflows can in principle stabilise the light curve of BY emission of the DSO, see Fig. 18. While the emission associated with the bow shock is expected to increase towards the pericentre, the accretion luminosity may stay rather constant since accretion flows are located well inside the circumstellar tidal radius. For a certain set of parameters, the total luminosity can be constant within uncertainties. In Fig. 18, the outflow rate of the star is set to $5 \times 10^{-9} M_\odot \text{yr}^{-1}$ and the terminal wind velocity is $10 \text{ km s}^{-1}$.

6. Summary

The previous analysis of NIR observational data has shown that the NIR-excess source DSO/G2 is a peculiar object in the S-cluster, which was further supported by the detection of a high linear polarization degree of 30% in the NIR $K_s$ band. Taking into account the compact behaviour during the closest passage around the SMBH, we focused on possible compact, stellar models of the fast-moving source. It appears that the SED characteristics of the DSO are reproduced best by either a young, embedded stellar object with a non-spherical dusty enve-lope (consisting of a dusty envelope, bipolar cavities, and a bow shock) or, on the other hand, a compact remnant, specifically a PWN. In both cases, the objects are expected to move supersonically close to Sgr A*.

Given the star-formation potential of the Galactic centre region, we first investigated the scenario of a pre-main-sequence star of class I that is still embedded in dense, optically thick dusty envelope. We found a composite stellar model surrounded by a non-spherical envelope (a star-dusty envelope-bipolar cavities-bow shock) that could reproduce the main characteristics of the continuum emission, including the linear polarization. In the framework of this model, bipolar cavities and the bow shock serve as sites for scattering stellar and dust photons. Furthermore, they increase the overall deviation of the source from the SED syntheses curve, and the bow shock contribution from scattered dust photons, which explains the significant polarized emission in this band. The polarization degree of $\approx 30\%$ is consistent with an optically thick dusty envelope and is comparable to other observed embedded young stellar objects in molecular cloud regions.

Moreover, we also looked at the neutron star model that could explain the SED as well as a high linear polarization degree – more specifically, the DSO would exhibit similar characteristics as a young, Crab-like PWN. Although energetically it would be possible to reproduce the NIR flux densities and the spectral slope, given the non-detection of X-ray or radio counterparts makes this model speculative. On the other hand, our estimates demonstrated that even current NIR facilities could be used to search for candidates of young PWN in the innermost parsec of the Galactic centre in the NIR domain. Such sources would actually manifest themselves as highly polarized, apparent NIR-excess sources, with flux densities comparable to the DSO. Some of the NIR-excess sources observed in the S cluster region could thus be suitable candidates for PWN. The imaging with the current and future NIR instruments can thus complement standard radio searches for young neutron stars in the Galactic centre region, which will allow us to put more constraints on the neutron star population in the innermost parsec. Future monitoring of the DSO and other NIR-excess sources, mainly with the focus on the radiative properties (both continuum and line emission) and the dynamics, will further narrow down the scenarios to explain these intriguing sources in the central arcsecond of the Galactic centre.

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References

Appendix A: Viewing angle of the bow shock

We present the calculation of an expected angle between the symmetry axis of the bow shock structure and the line of sight as a function of time (with respect to the peribothron). In the calculation, we use the orbital elements as derived by Valencia-S. et al. (2015). We use the convention, in which 0 degrees corresponds to the front view of the bow shock, 180 degrees is the view from the tail portion, and 90 degrees corresponds to the side view. We include three possible cases: a negligible motion of the medium, an outflow of 1000 km s$^{-1}$, and an inflow of 1000 km s$^{-1}$, see Fig. A.1.

Fig. A.1. Viewing angle of the bow shock as a function of time for a negligible motion of the medium, an outflow of 1000 km s$^{-1}$, and an inflow of 1000 km s$^{-1}$ (see the key).