A new infrared Fabry-Pérot-based radial-velocity-reference module for the SPIRou radial-velocity spectrograph

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Received 28 October 2016 / Accepted 30 January 2017

ABSTRACT

Context. The field of exoplanet research is moving towards the detection and characterization of habitable planets. These exo-Earths can be easily found around low-mass stars by using either photometric transit or radial-velocity (RV) techniques. In the latter case the gain is twofold because the signal induced by the planet of a given mass is higher due to the more favourable planet-star mass ratio and because the habitable zone lies closer to the star. However, late-type stars emit mainly in the infrared (IR) wavelength range, which calls for IR instruments.

Aims. SPIRou is a stable RV IR spectrograph addressing these ambitious scientific objectives. As with any other spectrograph, calibration and drift monitoring is fundamental to achieve high precision. However, the IR domain suffers from a lack of suitable reference spectral sources. Our goal was to build, test and finally operate a Fabry-Pérot-based RV-reference module able to provide the needed spectral information over the full wavelength range of SPIRou.

Methods. We adapted the existing HARPS Fabry-Pérot calibrator for operation in the IR domain. After manufacturing and assembly, we characterized the FP RV-module in the laboratory before delivering it to the SPIRou integration site. In particular, we measured finesse, transmittance, and spectral flux of the system.

Results. The measured finesse value of $F = 12.8$ corresponds perfectly to the theoretical value. The total transmittance at peak is of the order of 0.5%, mainly limited by fibre-connectors and interfaces. Nevertheless, the provided flux is in line with the requirements set by the SPIRou instrument. Although we could test the stability of the system, we estimated it by comparing the SPIRou Fabry-Pérot with the already operating HARPS system and demonstrated a stability of better than 1 m s$^{-1}$ during a night.

Conclusions. Once installed on SPIRou, we will test the full spectral characteristics and stability of the RV-reference module. The goal will be to prove that the line position and shape stability of all lines is better than 0.3 m s$^{-1}$ between two calibration sequences (typically 24 h), such that the RV-reference module can be used to monitor instrumental drifts. In principle, the system is also intrinsically stable over longer time scales such that it can also be used for calibration purposes.

Key words. instrumentation: spectrographs – instrumentation: interferometers – techniques: radial velocities – telescopes

1. Introduction

SPIRou is a near-infrared (NIR) spectro-polarimeter and velocimeter that is soon to be offered as a new-generation instrument on the Canada-France-Hawaii Telescope (CFHT; Delfosse et al. 2013). Its main goals are a) the search and characterization of habitable exo-planets orbiting low-mass and very-low mass stars by using high-precision radial-velocity (RV) measurements and b) the study of the impact of magnetic fields in star and planet formation by means of spectro-polarimetry. SPIRou is presently being integrated in Toulouse and will be transferred to the CFHT in 2017. Operations are planned to start end of 2017.

The radial-velocity method is employed to determine the Doppler shifts of absorption lines in the host star’s spectrum. M dwarfs present the opportunity to discover potential habitable planets due the larger radial-velocity signature induced by the planet on the lower-mass star (Udry et al. 2007). Also, the habitable zone (HZ) of an M star lies much closer in than that of a solar-type star, which again leads to a higher radial-velocity signal compared to a solar-type star. However, because M-dwarfs emit most of their flux in the infrared wavelength domain (Reiners et al. 2010), a radial-velocity instrument has to operate at infrared wavelengths, to make best use of the stellar light.

The wavelength range, resolution and the design of SPIRou, as well as its stability, have been optimized to search for habitable planets around M stars. The expected RV amplitude induced by a two Earth-mass planet in the HZ of an M5 dwarf, for instance, is of the order of 1.7 m s$^{-1}$ (Barnes et al. 2011). To achieve sufficiently significant detection, a measurement precision, and thus instrumental precision, of the order or better than 1 m s$^{-1}$ is required. It is well known that such a precision can only be achieved if both the spectral calibration and the instrumental drift are controlled to the same level. Both wavelength calibration and drift measurements, make use of spectral references that fix the necessary wavelength scale. The RV-observable corresponds to the measurement of the central wavelength of a spectral line that has to be referred to a known laboratory standard. Unlike the visible case, for which multiple wavelength calibration sources exist, such as spectral lamps, iodine cells, and lately also laser frequency combs (LFC; Ycas et al. 2012; Schwab et al. 2015) and Fabry-Pérots étalons (Reiners et al. 2014), in the infrared wavelength domain we are lacking suitable references sources.
The precision limitations in the calibration of radial velocity measurements play a key-role, especially when targeting the ambitious cases listed above. For these kind of investigations, an ultra-stable, broadband, bright, flexible and reliable wavelength calibrator is required.

To ensure optimal accuracy and precision, the spectrum of the ideal calibrator must have the following main characteristics:

- Many unresolved narrow lines.
- Coverage of the full spectral range.
- Known (or calibrated) line position.
- Line stability.
- No blending.
- Homogeneous peak flux.

In recent years, we developed a Fabry-Pérot calibration system with the aforementioned characteristics (Wildi et al. 2010) for the visible wavelength range. The first system, currently in use on the HARPS spectrograph, has performed well and has completely replaced the ThAr spectral lamp for instrumental drift measurement purposes. However, its lens-based optical design was not compatible with an infrared version. Therefore, we redesigned the system using an all-reflective solution. Two systems of the new design have been manufactured and are currently in operation on the TNG/HARPS-N and EULER/CORALIE spectrographs. Both systems have demonstrated stability of better than 1 m s\(^{-1}\) during an observing night that allowed us to use them systematically for the simultaneous reference measurement (Pepe et al. 2004). Based on this second design, we have manufactured and tested a similar system for SPIRou. The only element that needed to be adapted was the étalon itself in terms of material and coatings.

In the next section we will describe the basic working principles of the Fabry-Pérot based RV-reference module for SPIRou. In Sect. 3 we will describe the opto-mechanical design and the rationale that led us to the final parameter choice. In Sect. 4, we present the laboratory measurement set-up and the results obtained. In the final sections, we will also describe some of the particular aspects of RV precision and we will provide an outlook on possible future developments.

### 2. Theory of the plano-plano Fabry-Pérot étalons

A plano-plano Fabry-Pérot étalon (FP) consists of two flat parallel mirrors separated by an optical gap \(d\). The inner surface of each mirror is coated with a partially reflecting coating and the outer surface has an anti-reflection coating. The medium between the mirrors is transparent and has a refractive index of \(n\).

The FP is illuminated with a parallel light beam of divergence \(\Phi\). The light is partially reflected and transmitted by both mirrors producing interference in both reflection and transmission as shown in Fig. 1 (excerpt from Field guide to spectroscopy of Ball 2006). The transmission function of the étalon, taking into account the losses due to unavoidable absorption and scattering, is given by:

\[
T(\lambda) = \frac{1}{1 + (2FR/\pi)^2 \sin^2 \frac{\lambda}{2d}}.
\]

This function reaches a transmission maximum every time the phase \(\frac{\pi}{2}\) is an integral multiple of \(\pi\), namely,

\[
2nd \cos \theta = m\lambda.
\]

The distance between two successive maxima, also called the free spectral range (FSR), is defined by:

\[
FSR = \frac{\lambda^2}{2nd \cos \theta}.
\]

Figure 2 shows the theoretical transmission function of a Fabry-Pérot étalon with finesse \(F_R = 13\) at 1540 nm wavelength and FSR of \(~0.09\) nm. In this example we chose normal incidence (\(\theta = 0\)) and vacuum operation (\(n = 1\)). Transmission maxima are then reached for each wavelength \(\lambda_m = 2d/m\) and the free spectral range simplifies to \(FSR = \lambda^2/2d\).

The finesse \(F\) of a Fabry-Pérot étalon is defined as the ratio of the FSR to the full-width at half maximum (FWHM) of the transmission peak \(F = \frac{FSR}{FWHM}\). The functional analysis leads to \(FWHM = \frac{\lambda}{2F}\) leading to \(F = \frac{FSR}{FWHM}\).

We previously assumed a perfect étalon. In reality, any étalon will show errors such as surface errors and non-parallelism of the mirror. In order to take into account all these contributions, we can replace the reflective finesse \(F_R\) by an effective finesse \(F_e\) of the étalon, which can be expressed as:

\[
\frac{1}{F_e} = \frac{1}{F_R} + \frac{1}{F_D} + \frac{1}{F_p} + \frac{1}{F_\phi}
\]

where \(F_R\) is the reflectivity finesse, \(F_D\) is the defect finesse, and \(F_p\) is the parallelism finesse. An approximation of the finesse is represented by \(F_p\). This is produced by the divergence finesse of the illuminating entrance slit, which in turn produces a beam divergence of the quasi-parallel beam through the étalon. In the simulations we will present in the following sections, we replaced the divergence finesse by an integration over the field positions of the slit, to compute a realistic transmission function of the étalon in the case of a large entrance slit.

Using the effective finesse and the definition of the resolving power \(RP\), we computed:

\[
RP := \frac{\lambda}{\Delta \lambda} = \frac{\lambda}{FWHM} = \frac{\lambda}{\lambda/(mF_e)} = mF_e.
\]
3. Infrared Fabry-Pérot radial-velocity-reference module for SPIRou

The Fabry-Pérot RV-reference module for SPIRou has the purpose of providing a large number of ultra-stable lines in the wavelength range of the spectrograph, that allow to measure the instrumental drift during the night (or, in other terms, on the time scale between two calibrations). From the general characteristics of an ideal calibration source described in the introduction, we derived the requirements for the SPIRou RV-reference module as follows:

- The calibration source must cover the full wavelength range of SPIRou, i.e. from 980 nm to 2350 nm.
- The lines must not be resolved by the SPIRou spectrograph, since otherwise information is lost, respectively we do not take full advantage of the spectral resolution of the instrument.
- The line separation must be minimum two and maximum four the full width at maximum (FWHMs) of the spectrograph instrumental-profile (IP), in order to maximize the information content and avoid blends.
- The line position and shape stability of all lines must be better than 0.3 m s\(^{-1}\) during a night and on the time scale in between two calibrations (typically 24 h).
- The lines must be equidistant and the position of all lines defined by a limited number of system parameters.
- The relative intensity of any neighboring lines must be stable at 10\% over any time scale.
- The dynamic range of line intensities must be smaller than a factor 2 over one echelle order and a within a factor five over the full spectrum.

3.1. Spectral characteristics

Assuming the aforementioned hypothesis, we were able to design the Fabry-Pérot RV-reference module’s spectral characteristics. First, we took into account the resolution of the spectrograph \(R_S\). To optimize the spectral content, we need to make the line spacing as small as possible but also ensure that on the blue side, where it is minimal, it remains larger than \(3 \cdot \text{FWHM}\). This led us to the first condition:

\[
FSR_B \geq 3 \cdot \frac{\lambda_B}{R_S}
\]  

### Table 1. SPIRou’s main parameters and derived étalon parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Variable</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>SPIRou start wavelength</td>
<td>(\lambda_B)</td>
<td>980 nm</td>
</tr>
<tr>
<td>SPIRou end wavelength</td>
<td>(\lambda_B)</td>
<td>2350 nm</td>
</tr>
<tr>
<td>SPIRou resolving power</td>
<td>(R_S)</td>
<td>75 000</td>
</tr>
<tr>
<td>Étalon finesse</td>
<td>(F)</td>
<td>10.8</td>
</tr>
<tr>
<td>Étalon gap</td>
<td>(d)</td>
<td>12.250 mm</td>
</tr>
</tbody>
</table>

In the case of vacuum operation and perpendicular incidence, Eq. (3) simplifies to

\[
2 \cdot d = m \cdot \lambda.
\]  

Combining this equation with the inequality in Eq. (7), we obtained for the étalon gap:

\[
FSR_B = \frac{\lambda_B}{m} \geq 3 \cdot \frac{\lambda_B}{R_S}.
\]  

If we set the gap to exactly match the minimum FSR, we obtained the value:

\[
d = \frac{\lambda_B}{6} \cdot \frac{R_S}{\lambda_B}.
\]  

On the other hand, the lines of the étalon, at constant finesse, are larger on the red side of the spectrum. Therefore, we had to ensure that they remain narrower than the IP in this area of the spectrum. Our choice was to under-resolve the FP lines by a factor of two to three and not less, such that unnecessary flux loss is avoided. This choice drove the second condition:

\[
\text{FWHM} \leq \frac{2}{3} \cdot \frac{\lambda_B}{R_S}.
\]

Using the definition of the finesse \(F = FSR/\text{FWHM}\) and combining it with Eq. (11), we obtained for the finesse:

\[
F \geq \frac{2 \cdot d \cdot 3 \cdot R_S}{m^2 \cdot 2 \cdot \lambda_B} = \frac{3 \cdot d \cdot R_S \lambda_B^2}{4 \cdot d \cdot \lambda_B} = \frac{3 \cdot R_S \lambda_B}{4 \cdot d}.
\]

Choosing the lowest possible finesse and by substituting the gap \(d\), we obtained for the finesse:

\[
F = \frac{3 \cdot R_S \lambda_B}{4D} = \frac{9 \lambda_B}{2 \lambda_B}.
\]

To summarize, the spectrograph’s spectral range and resolution, together with the general requirements for the RV-module described in the previous section, defined the Fabry-Pérot parameters summarized in Table 1.

To achieve a reflectivity-limited effective finesse of about \(F = 11\), we distributed the various finesse components of Eq. (5) as shown in Table 2. As mentioned above, our starting choice was to determine the effective finesse by allocating a value of

<table>
<thead>
<tr>
<th>Finesse</th>
<th>Budget</th>
<th>Formula</th>
<th>Req.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Reflectivity</td>
<td>13</td>
<td>(F_R = \pi \sqrt{R/(1 - R)})</td>
<td>(R = 80%)</td>
</tr>
<tr>
<td>Divergence</td>
<td>28</td>
<td>(F_R = 4 \cdot \lambda / (\Phi^2 \cdot d))</td>
<td>(\Phi = 2) mrad</td>
</tr>
<tr>
<td>Parallelism</td>
<td>40</td>
<td>(F_R = \lambda / (2 \cdot \Delta))</td>
<td>(\Delta = 4.5) nm</td>
</tr>
<tr>
<td>Defect</td>
<td>40</td>
<td>(F_R = \lambda / (\sqrt{2} \cdot \delta))</td>
<td>(\delta = 6.7) nm</td>
</tr>
<tr>
<td>Effective</td>
<td>10.88</td>
<td></td>
<td>Eq. (5)</td>
</tr>
</tbody>
</table>
$F_R = 13$ to the reflectivity finesse. The remainder of the budget was almost completely used up by the divergence finesse, to maximize the fibre diameter and minimize the physical size of the étalon. The remaining finesse values were set much higher to keep $F_R$ in budget.

Once the finesse values have been frozen, they define minimum requirements to the opto-mechanics of the étalon. The finite divergence forces a trade-off between fibre size, the focal length of the collimator, and clear aperture of the étalon. In principle, at fixed divergence value, the physical dimensions of the assembly are minimized when the smallest fibre is selected. However, this implies a loss of flux inversely proportional to the fibre size if an incoherent (extended) light source is used. To maximize the flux while still using an incoherent source, we decided to go for the source with the highest possible surface brightness. The choice fell on the Laser-Driven Light Source (LDLS) EQ-99 FC by Energetiq that is composed of a high-temperature plasma bulb $T = 10{,}000$ K (Fig. 3, excerpt from LDLS EQ-99 handbook) heated by a high-power diode laser. The light output perfectly matches that of an ordinary step-index fibre of 200 μm that can directly be used to feed our FP assembly. The numerical aperture $NA = 0.20$ and the practical wish to keep the system compact, led us to fix the focal length of the collimator to 100 mm and the clear aperture of the étalon to 40 mm. The parallelism defect $\Delta < 4.5$ nm translated into $10^{-6}$ rad or 0.2 arcsec. Finally, the value for the surface defects of $\delta = 6.7$ nm required the mirrors to be manufactured with at least $1/50$ in wave-front error.

### 3.2. Sensitivity of finesse and radial-velocity stability to alignment and fibre diameter

Up to now we have considered the transmission function of the étalon to be given by Eq. (2). Defects, non-parallelism and finite divergence were taken into account by computing an effective finesse that was corrected for the various contributions. Although this approach is satisfactory for the defects and non-parallelism of the mirrors, it is incomplete for the finite divergence. The finite divergence (or fibre diameter) not only introduces a loss of finesse but also a shift in wavelength of the transmitted peaks. Furthermore, a non-uniform light distribution across the fibre exit produces a change in the shape of the transmitted peak. The resulting transmission function can be simply understood as the sum of the individual transmission functions from every field point (or, in other words, over each ray arising from the different points across the fibre tip) that will cross the étalon with slightly different incidence angles $\theta$.

We simulated the transmission function for different fibre diameters and as a function of the de-centring of the fibre from the optical axis, to understand how sensitive the finesse and the peak wavelength are as a function of these parameters. For the analysis, we needed to consider that the fibre is spatially extended and the deviation of each ray from the parallel beam is:

$$\theta = \arctan \left( \frac{x}{f} \right)$$  \hspace{1cm} (14)

where $x$ is the distance from the fibre centre and $f = 100$ mm is the focal length of the collimator (parabolic mirror). The angle $\theta$ by which the beam crosses the étalon depends on the position of the fibre of entrance.

To obtain the total transmittance spectrum, we need to compute the integral over the surface of the fibre. For the simulations we assume circular fibres and uniform illumination, and we perform the integral in polar coordinates. The total transmittance can then be written as:

$$T(\lambda) = \left( \int_0^R \rho \mathrm{d}\rho \int_0^{2\pi} \frac{1}{1 + (2 \cdot F_{eff}/\pi)^2 \cdot \sin^2(\theta/2)} \mathrm{d}\theta \right)/A$$  \hspace{1cm} (15)

where $R$ is the radius of the fibre and $\delta = 4\pi nd \cos \theta / \lambda$, as defined earlier. The integral is divided by the surface $A$ of the fibre tip to re-normalize the peak transmittance.

In case of a de-centring $\Delta$ of the fibre with respect to the optical axis of the system, the angle of incidence $\theta$ becomes:

$$\theta = \arctan \left( \sqrt{(\rho \cos \varphi + \Delta)^2 + (\rho \sin \varphi)^2} / f \right)$$  \hspace{1cm} (16)

where, without loss of generality, we have assumed the fibre to be de-centred along the $x$-axis only.

It is easily understood that, if the fibre has infinitely small diameter, all the the rays will cross the Fabry-Pérot with $\theta = 0$, such that we end up with the known Airy function. For the general case of a finite fibre diameter, we performed a numerical integral to obtain the transmittance as a function of the diameter of the fibre $D$ and $\Delta$. 

Fig. 3. Spectral power produced by the LDLS. The original plot, which is an excerpt from LDLS EQ-99 handbook, was manually digitized.

Fig. 4. Simulated transmittance of a Fabry-Pérot for fibre diameters of 200, 500, and 900 μm, assuming the fibre is centred on the optical axis and a focal length of the collimator $f = 100$ mm.
Figure 4 shows the transmittance as a function of fibre size for a system with focal length \( f = 100 \) mm. As expected, for small fibres the peak transmittance is close to 1 and the effective finesse is equal to the reflective finesse. For larger fibres, the transmission at the peak decreases and the width increases, which is equivalent to a reduction of the effective finesse. Simultaneously, the peak wavelength shifts towards a shorter wavelength, which reflects the fact that the number of rays having an incidence angle \( \theta > 0 \) has increased. Interestingly, the peaks remain symmetric, even for very large fibres, which is due to the fact that we have assumed uniform illumination and a circular fibre. This assumption is justified by the fact that the primary source we are using has a larger étendue than the fibre. The fibre is over-filled by the source and uniformly illuminated. In the real system, we are using an octagonal fibre that has even better scrambling properties and produces increased illumination uniformity (Chazelas et al. 2010).

Figure 5 shows the results of the simulation as a function of the fibre de-centring, in which we fixed the fibre diameter to the chosen value of \( D = 200 \) \( \mu \)m. In this case we also observe a reduction of finesse and a blue-shift of the peaks with increasing de-centring. It is interesting to note, however, that when combining a finite fibre size with de-centring, the peaks become asymmetric.

The results for the finesse are summarized in Fig. 6. The plot shows the evolution of the finesse as a function of fibre diameter (left hand) and of the fibre de-centring (right hand). To be more general, we have expressed both, the fibre diameter and de-centring, in terms of angular values \( \Delta \theta = D/f \) and \( \theta = \Delta f / f \), respectively. In the case of a small fibre diameter or small de-centring, the value for the effective finesse approaches the nominal value of \( F_E = 13 \). It is important to note that the effective finesse remains larger than \( F_E = 11 \) for a fibre diameter up to \( \Delta \theta = 0.0035 \) (\( D = 350 \) \( \mu \)m), which perfectly justifies our choice for a 200 \( \mu \)m diameter. However, the plot as a function of de-centring also tells us that, if we want to ensure the required effective finesse, the fibre must be centered to better that \( \theta = 0.0015 \) (\( \Delta = 150 \) \( \mu \)m) for the optical axis of the system.

As mentioned before, the peak wavelength shifts towards the blue when increasing the fibre diameter or de-centring the fibre. When the Fabry-Pérot is used for absolute wavelength calibration, the position of the peaks must be known. Even more critical is that, when used as a RV-reference (to measure the instrumental drift between two calibration sequences), we have to make sure that the transmission peaks remain stable in wavelength. Their dependence on fibre diameter and centring will set the requirements on the focus and centring stability of our optical system.

For this reason, we have expressed the wavelength shift in terms of “radial-velocity” in the unit of [m s\(^{-1}\)]. The conversion from wavelength to speed is obtained by the relation:

\[
\Delta v = \frac{\Delta \lambda}{c}.
\]

Figure 7 presents the shift of the transmission peak as a function of similarly to Fig. 6 fibre diameter \( \Delta \theta = D/f \) and de-centring \( \theta = \Delta f / f \). It can be seen that even a small change introduces shifts of several hundreds or even thousands of m s\(^{-1}\). However, there is no reason besides thermo-mechanical instabilities for the fibre diameter or the de-centring to change with time. To better evaluate the calibration sensitivity to these parameters, we chose to presents the derivative of these curves (Fig. 8). Since the curve has a parabolic shape (as can be understood from the fact that \( \cos \theta \sim \theta^2 \) for small angles \( \theta \)), its derivative is nothing more than a slope. The left-hand plot simply shows us that, the larger the fibre, the more sensitive the system is to a de-focus, and, from the right-hand plot, the same conclusion can be drawn for the de-centring. Given the chosen fibre size (2 \( \mu \)rad), we derive that the radial velocity will change by 300 m s\(^{-1}\) m rad\(^{-1}\). In physical terms for our system, this is 3 m s\(^{-1}\) micron\(^{-1}\) (relating to the change in fibre size). In terms of de-centring, the sensitivity will
3.3.1. Alignment precision

The analysis above shows that the RV-sensitivity of the étalon to opto-mechanical mechanical misalignment increases with de-centring. A perfectly-aligned system would not be sensitive to motions of the fibre, for example due to thermal or gravity effects, but even for slight misalignment our system could become unstable at radial velocities beyond 30 cm s\(^{-1}\). Assuming that we can align the fibre by auto-collimation to better than one-twentieth of its diameter, that is to 10 \(\mu\)m and using the results presented in Fig. 8, we obtain a sensitivity of 30 m s\(^{-1}\) mrad\(^{-1}\) (0.3 m s\(^{-1}\) micron\(^{-1}\)). In other words, the fibre position must be stable to within one micron of the focal plane of the collimator and the angular alignment of the étalon with the collimators must not change by more than 0.01 mrad.

3.3.2. Pressure stability

For an air-spaced étalon like SPIRou’s, any pressure change will induce a change in the optical gap and thus in the wavelength of the transmitted peaks. For this reason we made the choice to operate the RV-reference module in a vacuum (see Fig. 9). To establish whether the system must be pumped continuously or not, we have to compute the drift of the system arising from pressure changes that have occurred since the last wavelength calibration of the spectrograph, which taking place at the start of the night. In other words, pressure changes in the Fabry-Pérot system must not induced line-position changes larger than the required RV-precision. Given the requirement for the RV-precision of 30 cm s\(^{-1}\) during an observing night (typically 12 h) and using Eqs. (3) and (17), we computed that the refractive index \(\Delta n/n\) must not change by more than \(10^{-9}\) in relative terms. Using the approximation for the air index \(n_{\text{air}} = 1 = 0.00027 \cdot p/p_{\text{am}}\), where \(p_{\text{am}}\) is the average ambient pressure at sea level, we computed that the pressure \(p\) inside the vacuum tank must not change by more than \(3.7 \times 10^{-3}\) mbar in 12 h or \(7.4 \times 10^{-3}\) mbar day\(^{-1}\).

3.3.3. Operating pressure

An aspect which is frequently forgotten, is that pressure does not only depend on air leaks but on the volume of the air contained in the vacuum tank. External ambient pressure changes due to meteorological effects affect the volume of our vacuum tank due to the variation in pressure differences between outside and inside. Consequently, the index of the residual air inside the vacuum tank will vary and degrade the calibration system. The sensitivity to atmospheric pressure changes depends on the air pressure (or density) inside the vacuum tank. We must therefore understand at which (maximum) pressure we must operate the RV-reference module to avoid effects larger than 30 cm s\(^{-1}\).

Bear in mind Boyle’s law \(p \cdot V = \text{const.}\), defining \(V_0\) as the initial volume, and defining \(p_0\) the initial pressure inside the vacuum tank, the refractive index \(n\) of the residual air can be written as:

\[
 n - 1 = \frac{p}{p_{\text{Atm}}} \cdot (n_{\text{Atm}} - 1) = \frac{V_0}{V} \cdot \frac{p_0}{p_{\text{Atm}}} \cdot (n_{\text{Atm}} - 1)
\]

where \((n_{\text{Atm}} - 1) \approx 2.7 \times 10^{-4}\) corresponds to the refractive index of standard air at atmospheric pressure \(p_{\text{Atm}}\), and \(p\) and \(V\) are the actual pressure and volume inside the vacuum tank.

The derivative of the refractive index \(n\) with respect to the change of the external pressure \(p_{\text{out}}\) can then be written as:

\[
 \frac{dn}{dp_{\text{out}}} = \frac{dn}{dV} \cdot \frac{dV}{dp_{\text{out}}} = \beta \cdot \frac{p_0}{p_{\text{Atm}}} \cdot (n_{\text{Atm}} - 1)
\]

where \(\beta := -\frac{dV}{dp_{\text{out}}}\) is the relative volume change of the vacuum tank as a function of changes in external pressure (at constant internal pressure).

By means of a finite element analysis of the vacuum tank (the following sections detail the design description), we computed \(\beta \sim 10^{-5}\) mbar\(^{-1}\). This value allows us to determine the maximum operational pressure to avoid change in the radial velocity of the RV-reference module larger than the specified 30 cm s\(^{-1}\). If we consider that ambient pressure variations hardly exceed 10 mbar night\(^{-1}\) at 2500 m altitude (e.g. at the La Silla and Paranal Observatories), we derive an upper limit for the operation pressure of \(p_0 < 30\) mbar. In practical terms, and given the maximum allowed pressure-rise rate of \(dp/dt = 7.4 \times 10^{-3}\) mbar day\(^{-1}\) determined in the previous section, it is sufficient to evacuate the RV-reference module once every 10 yrs in the worst case.

3.3.4. Temperature stability

We considered two effects induced by temperature variations. The first is the thermal stability of the optical gap that is essentially given by CTE of the spacers. The spacer material is from Corning ULE and thus the CTE is guaranteed to be lower than 2 \(\times \) 10\(^{-8}\) Kelvin\(^{-1}\). This translates into a radial-velocity sensitivity of about 6.7 m s\(^{-1}\) K\(^{-1}\). Again applying the radial-velocity stability requirement, we derive a temperature stability requirement for the RV-reference module of better than 0.05 K.

The second temperature effect may produce focal-length changes of the collimator that would result in a “de-focus” of the entrance fibre and an apparent increase of fibre diameter \(D\). As we will describe in Sect. 3.4, the Fabry-Pérot assembly of

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Fig. 8. Radial velocity sensitivity to fibre-size change for a centred fibre (left) and to de-centring for a fixed fibre size of \(D = 200\ \mu m\) (right). The blue line marks the limit area we are interested in. For 2 mrad fibre size, the RV will change by \(300\ \text{m s}^{-1}\) (3 m s\(^{-1}\) micron\(^{-1}\)) for a centred fibre. In the case of de-centring, it changes by \(600\ \text{m s}^{-1}\) (6 m s\(^{-1}\) micron\(^{-1}\)).
our RV-reference module is made of aluminium (also Fig. 9). Considering the focal length of \( f = 100 \text{ mm} \) and the coefficient of linear thermal expansion for aluminium as \( CTE_{Al} = 2.3 \times 10^{-5} \text{ K}^{-1} \), we computed an absolute focal length change of \( df/dT = 2.3 \mu m \text{ K}^{-1} \). Because the F-number of the fibre exit (or collimator) is F/2.5, we obtained an increase of apparent diameter \( dD/dT \approx 1 \mu m \text{ K}^{-1} \). From the plot in Fig. 8 we can then derive that, for a fibre of 200 \( \mu m \) diameter, the radial velocity would change by \( \Delta v \sim 3 \text{ m/s K}^{-1} \). In order to comply with the radial-velocity requirements, we have to keep the temperature of the system stable to 0.1 K.

From the analysis above, we conclude that it is sufficient to control the temperature of the RV-reference module to a level of 0.05 K even when using aluminium for its structure. This kind of temperature stability is easily achieved with commercial components. Nevertheless, we made a particular effort to design the opto-mechanical system in the most symmetric and stable way, and to thermally isolate the critical parts inside the vacuum from the vacuum tank. Therefore operating in a vacuum will further improve the thermal stability.

### 3.4. Design of the SPIRou radial-velocity-reference module

The RV-reference module designed for SPIRou (Fig. 9) is derived from a concept that was successfully developed for HARPS and the visible wavelength range (Wildi et al. 2010). The design was later made more modular and adapted for the infrared wavelength range by replacing lenses with mirrors. This was successfully applied firstly to the HARPS-N and CORALIE modules and was later essentially copied for SPIRou.

The system conceptually consists of a Fabry-Perot étalon filter illuminated in white light to produce a set of equally-spaced (in frequency) emission lines of uniform intensity across a wide wavelength range. For the illumination we use a laser-driven light source (LDDS by Energetix) that essentially produces a black-body emission of 10000 K. Although at visible wavelengths the surface brightness of this sort of source is considerably higher than a standard halogen source of about 3000 K, the brightness difference at wavelengths above 1 \( \mu m \) is much lower and almost negligible. For our system we nevertheless decided to use an LDDS with a 200 \( \mu m \) fibre output that perfectly matches the étendue of the étalon. The LDDS light is fed to the RV-reference module through an octagonal fluoride fibre of 300 \( \mu m \) core diameter and 2 m in length, whereas the RV-reference module output fibre, which collects the light from the module and brings it to the spectrograph, is of 600 \( \mu m \) core diameter and 4 m length.

A vacuum tank contains the fibre-fed Fabry-Pérot opto-mechanical system (Fig. 10). The pressure is initially pumped to \( 10^{-4} \text{ mbar} \) or less, but eventually the valve is closed. More important than the actual pressure value is the pressure rise rate which must comply with the previously mentioned requirements. The temperature is controlled using heating-resistor foils glued around the vacuum tank. Two precise silicon-diode temperature sensors (one on the vacuum tank for the control and the other close to the étalon for monitoring) and a Lakeshore 331 device close the temperature-control loop to better than 5 mK rms. The whole system is isolated and packed inside a box to avoid heat exchange with the laboratory environment.

The optical system is placed in the vacuum vessel and fixed to the top flange in only 3 points, using thermally insulating material to minimize thermal conduction from outside. The collimating and focusing optics comprise identical protected silver-coated parabolas with a focal length of 100 mm. Parabolic mirrors were selected because they result in low aberrations and guarantee that the line profile stays symmetric.

The light enters the vacuum tank through an octagonal silica fibre purchased from CERAMOPTEC (OPTRAN WF). Its diameter is 200 \( \mu m \) in accordance to the derived finesse requirements. The octagonal shape was chosen to ensure a very uniform and thus stable illumination of the étalon (Chazelas et al. 2012). This is important to minimize possible illumination effects at the source level, such as PSF changes and variations of the illumination spot position or its angular distribution.

The connectorized fibre is mounted on a spider and illuminates, on its axis, a parabolic mirror of 50 mm clear aperture. Given the 100 mm focal length of the mirror, the F/2.5 beam of the fibre produces a collimated beam of 40 mm diameter. The back-reflected beam is partially obstructed by the fibre and its spider, but we preferred to accept some light losses for the
Fig. 11. Picture of the SPIRou Fabry-Pérot étalon.

Fig. 12. Transmission (left) and reflectance (right) of an étalon mirror.

sake of symmetry. The beam crosses the étalon before being re-focused by a second on-axis parabola on the output fibre, that is mounted in exactly the same way as the collimation part.

The output fibre inside the vacuum tank is circular and its diameter is 600 µm. A larger fibre was chosen in order make alignment easier, collect all the light, and eventually increase the stability of the system. Being located after the étalon, the diameter of this fibre has no influence on the resulting finesse.

The Fabry-Pérot étalon used in SPIRou is shown in Fig. 11. Its physical diameter is of 60 mm while the clear aperture is 50 mm. The two mirrors are made of Suprasil. They were polished and coated by the company Thin Films Physics, Switzerland. The surface flatness is of the order of λ/100. The coating reflectivity of R = 80% + 2% over the 980–2350 nm range was designed to match the reflectivity-finesse requirements (Fig. 12). Both mirrors were anti-reflection (AR) coated on the external face. Nevertheless, a wedge was introduced between the two faces of each mirror to avoid possible parasitic interference with the external faces. The two mirrors are separated by a set of three high-precision Corning ULE (Ultra Low Expansion material – CTE < 2 × 10⁻⁶ K) spacers produced by sls-optics, UK. The étalon was finally assembled using dry optical contacting by ICOS, UK.

4. Laboratory test

4.1. Test goals

We characterized the RV-reference module in the laboratory with respect to its basic parameters. It turned out to be quite a demanding task to measure the high-resolution transmission function because of the high spectral resolution of the étalon itself. To sufficiently sample the line profile we would have needed a spectrograph or spectrometer of resolving power $R > 500,000$ that only a Fourier-Transform-Spectroscopy (FTS) can deliver. We decided to restrict ourselves to a tunable laser wavelength for this measurement. Once spectral performances are demonstrated at one wavelength, and knowing the étalon gap and the broad-band reflectivity, the performances can be determined also at other wavelength. Nevertheless, we have separately determined the broad-band transmittance and the flux delivered by the system. Also, we have measured the pressure and temperature stability to verify that the system complies with the technical requirements.

4.2. Measurements and results

4.2.1. Finesse

Figure 13 shows the set-up used for characterizing our étalon. We used a temperature-controlled DFB laser diode at 1540 nm as a tunable laser. The centre wavelength has a temperature coefficient of 0.095 nm K⁻¹. We used this characteristic to scan the transmittance of the Fabry-Pérot as a function of wavelength. The source’s spectral width (FWHM ≈ 2 MHz) is narrow enough to probe the line profile of our étalon (FWHM ≈ 1 GHz). The flux was measured at the output of the system by an indium-gallium-arsenide (InGaAs) photodiode.

Figure 14 shows the measured transmittance curve $T(\lambda)$ of the RV-reference module. The finesse can be estimated by dividing the free-spectral range (distance between two neighbouring peaks) by the FWHM of a single line. Alternatively, we fitted the obtained curve by a theoretical transmission function (green curve in Fig. 14) leaving the $FSR$ and the effective finesse $FSR_E$ as free parameters. The so obtained values are $F_{SR} \approx 12.76$ and $FSR = \Delta \lambda = \lambda^2 / 2\pi D \approx 0.09$ nm, both perfectly in line with the design values. The finesse is actually slightly higher than expected because of an actual coating reflectivity of about 81–82% instead of the specified 80%. Finally, we would like to note the exact match of the fitted curve with the measured data, which demonstrates that we have all the effects which could influence the line symmetry, such as the divergence finesse, well under control.
4.2.2. Transmittance and flux

We measured the spectral power and transmittance of the system in the 950–1700 nm range directly with a laboratory Optical Spectrum Analyzer (OSA). Figure 15 shows the corresponding set-up. Figure 16 shows the set-up for the 1600–2400 nm spectral range, for which we employed a small optical bench with selectable band-pass filters to measure the optical power and transmittance in four discrete bands by means of a NIR photodiode.

The power was estimated using the internal calibrations and conversion factors of the OSA and the photodiode. The measurements should therefore not be considered to be of great accuracy but to provide a coarse estimate of the spectral-power density produced by the RV-reference module as a whole. Figure 17 shows the spectral flux produced by the RV-reference module as a function of wavelength. We originally observed a discrepancy of about a factor of 4.5 at 1625 nm where we have overlapping measurements on the two set-ups. We approximately measured the same factor when using an halogen lamp instead of the LDLS to light-feed the module (Fig. 18). This factor can be explained by the bad match of the fibre diameter used to feed the OSA and the photodiode. The measured Fabry-Pérot transmittance as a function of wavelength (blue dots) and fitted theoretical curve (green line). On the bottom the residuals to the fit are shown.

In interesting to note that the flux above 1000 nm produced by feeding the module with the two lamps (Figs. 17 and 18), the LDLS or the halogen lamp, is not significantly different despite the very different temperature of the lamps. This is expected by the black-body emission law. For cost considerations, we therefore used a halogen lamp in the final RV-reference module layout.

In the latter case we simply connected together the input and output fibre of the module. The corresponding measurements for flux and transmittance in the four bands are summarized in Table 3. The last column indicates the transmission of the RV-reference module at the peak $T_{FP}$ of the Fabry-Pérot line, and has been computed by multiplying the average (broadband) transmittance of the system by the finesse of the Fabry-Pérot.

4.2.3. Pressure and temperature stability

As explained in Sects. 3.3.3 and 3.3.4 the RV-reference module must be operated in a vacuum well below 30 mbar and the pressure raise rate must be lower than $7.4 \times 10^{-3}$ mbar.
After evacuating the vacuum tank and doing a leak test to ensure the absence of vacuum leak, we performed a pressure test as shown in Fig. 19. The residual out-gassing rate is $7.2 \times 10^{-3}$ mbar day$^{-1}$, just within the specification. Experience shows that out-gassing decreases as a function of time to a level much better than the required value.

We tested the temperature stability in a similar way. Figure 20 shows the diagram of the set-up for temperature monitoring.

We used a LakeShore 331 temperature controller with a set-point set at 25°C. The temperature control loop is closed on the sensor, which is bonded to the vacuum vessel’s inside wall. A second sensor monitors the temperature of the opto-mechanical structure in proximity of the Fabry-Pérot étalon. Figure 21 shows the temperature of both sensors after turning on the temperature controller.

The temperature of the vacuum tank stabilizes after less than one hour with a dispersion of $\sigma_T = 1.2$ mK, while the sensor close to the étalon reaches a stable temperature after about 40 h with a slightly higher dispersion of $\sigma_T = 2.1$ mK. This can be explained by the fact that the test was performed in a laboratory with no temperature control at all and thus night-to-day temperature variations of several degrees. Even under these conditions the temperature stability of our RV-reference module is well within specification.

5. Radial velocity performance

5.1. Photon noise

By analogy with the HARPS-N Fabry-Pérot we know that the centroid of a single emission line featuring 100 000 $e^-$ per line can be determined with a photon-noise limited precision $\sigma$ of better than 2 m s$^{-1}$. SPIRou will be using a Hawaii 4RG detector
with lower dynamical range than typical CCD detector. If we assume a conservative line flux of only $25 000 \, e^-/\text{per exposure}$, given the fact that the present étalon will produce about $14 280$ lines in the spectral range of SPIROU, we will obtain a global precision of the drift measurement of

$$
\sigma_{\text{total}} = \frac{\sigma_{100,000} \times \sqrt{100,000/25,000}}{\sqrt{14 280}} = 0.034 \, \text{m/s}.
$$

(20)

This value is significantly lower than the aimed precision of $0.3 \, \text{m/s}$ for SPIROU, and therefore compliant with the requirements.

5.2. Radial velocity stability

Radial-velocity stability measurements could however not be performed, because they would have required a spectral reference at least as stable as the RV-reference module is supposed to be. We therefore decided to postpone these measurements until they can be performed on SPIROU itself, where it will be possible to compare our module directly with a Uranium hollow-cathode lamp.

Nevertheless, we can refer to stability measurements of an identical system (besides the étalon coatings because they are optimized for the visible) made with HARPS-N (Wildi et al. 2011). Doing this, we demonstrated that the short-term RV-dispersion obtained using the Fabry-Pérot system is better than that measured using the ThAr hollow-cathode lamp. Typical dispersion values are of the order of $0.1$ to $0.2 \, \text{m/s}$ on time scales from hours to a day. This is again perfectly in line with the specified RV-stability requirement. Given the almost identical design of these two systems, we have plausible reason to expect similar performances on the SPIROU RV-reference module.

5.3. Modal noise

Several studies have demonstrated that the finite number of modes in a wave guide such as a fibres, may introduce noise in excess to pure photon noise. For instance, the modal noise limits the signal-to-noise ratio (S/N) (McCoy & Ramsey 2011) measured in the continuum of the measured spectrum. This modal noise increases with wavelength because of the fewer modes in the fibre and it may therefore represent a limit to the NIR radial-velocity precision budget. We therefore analyze the situation for the SPIROU RV-reference module. The number of excited modes in a uniformly-illuminated fibre is inversely proportional to the wavelength and is given by the formula (McCoy & Ramsey 2011)

$$
M = \frac{1}{2} \left( \frac{\pi \cdot d \cdot NA}{\lambda} \right)^2,
$$

(21)

where $d$ is the fibre core diameter, $\lambda$ is the light’s wavelength, and $NA$ is the fibre’s numerical aperture. In the wavelength domain of SPIROU and for the chosen fibre, we have $M = 9941$ at $980 \, \text{nm}$ and $M = 1741$ at $2350 \, \text{nm}$. At first glance it appears that at short wavelengths there are enough modes for our Fabry-Pérot system because we expect to obtain an S/N at continuum of the order of the square root of the number of modes

$$
\left( \frac{S}{N} \right)_{\text{limit}} \sim M^{0.784}
$$

(Baudrand & Walker 2001) meaning about $100$ on the blue end of the spectrum. On the red end of the spectrum the mode-limited S/N ratio decreases to about $30$, which is even below what we expect to be the limit to reach a precision of $1 \, \text{m/s}$.

Let us take HARPS-N as the reference instrument. The Fabry-Pérot spectrum recorded by HARPS-N includes approximately $20,000$ lines with average $S/N = 187 \, \text{pixel}$ and global photonic error on the drift measurement $\sigma_{\text{RV}} = 0.044 \, \text{m/s}$. In SPIROU the number of lines is approximately $14,000$. Assuming a similar S/N per line, and by analogy with HARPS-N, we estimate that the global photonic error on the drift measurement will be of the order of $\sigma_{\text{RV}} = 0.062 \, \text{m/s}$.

Assuming an effective $S/N = 100 \, \text{pixel}$ and $S/N = 30 \, \text{pixel}$ at the two extreme ends of the spectral range of SPIROU, we computed the effective measurement error values (see Table 4). Given these values, we see that the modal noise contribution to the error budget is $0.38 \, \text{m/s}$ even in the worst case, and for the average of the spectral range it is better than the $0.3 \, \text{m/s}$ requirement of SPIROU.

6. Conclusions

In this paper we present the design of a new infrared Fabry-Pérot RV-reference module for SPIROU and we describe its key properties and spectral characteristics in detail. The primary objectives were to build, test and finally operate a Fabry-Pérot-based RV-reference module able to provide the needed spectral information over the full wavelength range of SPIROU to measure instrumental drift to a precision of $30 \, \text{cm/s}$. It must be remarked that we followed a quite strict top-down approach: 1) after establishing the requirements set by SPIROU we 2) converted them into requirements for the RV-reference module; 3) verified the assumption by analysis and simulations; 4) designed and manufactured the module according to the choices we made; and finally 5) tested the key performances in the laboratory. The obtained performances, at least those which could be verified in the laboratory, are compliant with the requirements. Only the RV-stability requirements had to be postponed to a later stage when the SPIROU spectrograph will be ready for system tests. Nevertheless, we know by analogy with the HARPS-N RV-reference module, that we can expect an RV-stability well below $1 \, \text{m/s}$. In summary, we demonstrate that the SPIROU reference
module can replace any cathode spectral lamp or absorption cell for drift measurements at relatively moderate costs.

Our module also provides equally-spaced spectral lines of uniform intensity over an extremely wide spectral range, which could greatly help in measuring the detector geometry. Although the étalon does not have the intrinsic accuracy provided by an atomic transition and the mirror coatings may introduce slow variations of the phase (and thus cause group-delay dispersion, as per Wildi et al. 2011), it should be remembered that the line separation and position is perfectly smooth and continuous in wavelength. This information can be used to improve the wavelength solution, in particular to determine the higher-order terms of the polynomials used to describe the pixel-to-wavelength relationship, which are badly constrained by the sparse lines of hollow-cathode lamps only. In the absence of commercial and affordable laser-frequency combs that cover the entire spectral range, we are currently investigating and implementing a combined use of hollow-cathode lamps and Fabry-Pérot calibration. The former provides the accuracy (or global wavelength “zero point”), whereas the latter provides the detector geometry and the pixel-to-pixel and intra-pixel responses. In fact, we are also considering the possibility of varying the line position of the Fabry-Pérot by changing the (low) pressure inside the vacuum tank, to “scan” and characterize the response of every detector pixel individually.

We can conclude that the presented RV-reference module for SPIRou is able to measure instrumental drifts at the required precision level and can replace the performance-limited hollow-cathode lamps and absorption cells with respect to this goal. Furthermore, we identify possible developments of the module and significant potential to convert it into a calibration source, which could turn the Fabry-Pérot-based light source into a cost-effective alternative to laser-frequency combs, at least in the short and mid term.

Acknowledgements. This work was supported by the Swiss National Science Foundation (SNSF) grants Nos. 200021-140649, 200020-152721 and 200020-166227. The authors acknowledge its financial support.

References
McCoy, K., & Ramsey, L. 2011, in Advanced Maui Optical and Space Surveillance Technologies Conference, E69