From dense hot Jupiter to low-density Neptune: The discovery of WASP-127b, WASP-136b, and WASP-138b[★]

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ABSTRACT

We report three newly discovered exoplanets from the SuperWASP survey. WASP-127b is a heavily inflated super-Neptune of mass $0.18 \pm 0.02 M_J$ and radius $1.37 \pm 0.04 R_J$. This is one of the least massive planets discovered by the WASP project. It orbits a bright host star ($V_{\text{mag}} = 10.16$) of spectral type G5 with a period of 4.17 days. WASP-127b is a low-density planet that has an extended atmosphere with a scale height of 2500 ± 400 km, making it an ideal candidate for transmission spectroscopy. WASP-136b and WASP-138b are both hot Jupiters with mass and radii of $1.51 \pm 0.08 M_J$ and $1.38 \pm 0.16 R_J$, and $1.22 \pm 0.08 M_J$ and $1.09 \pm 0.05 R_J$, respectively. WASP-136b is in a 5.22-day orbit around an F9 subgiant star with a mass of $1.41 \pm 0.07 M_{\odot}$ and a radius of $2.21 \pm 0.22 R_{\odot}$. The discovery of WASP-136b could help constrain the characteristics of the giant planet population around evolved stars. WASP-138b orbits an F7 star with a period of 3.63 days. Its radius agrees with theoretical values from standard models, suggesting the presence of a heavy element core with a mass of $\sim 10 M_{\oplus}$. The discovery of these new planets helps in exploring the diverse compositional range of short-period planets, and will aid our understanding of the physical characteristics of both gas giants and low-density planets.

Key words. planetary systems – stars: individual: WASP-127 – techniques: radial velocities – techniques: photometric – stars: individual: WASP-136 – stars: individual: WASP-138

1. Introduction

Over 3000 exoplanets have been discovered as of 2016 July¹. The space-based mission *Kepler* (Borucki et al. 2010) and its

[★] Radial velocity and photometry tables are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via

<http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/599/A3>

¹ <http://exoplanetarchive.ipac.caltech.edu/>

successor K2 (Howell et al. 2014) have discovered a large number of transiting planets. The results show that small Earth- and Neptune-sized planets are common around solar-like stars (Borucki et al. 2011). The *Kepler* discoveries have provided a large sample of planetary systems that are very useful for statistical studies of planetary populations (e.g. Fressin et al. 2013; Dressing & Charbonneau 2013; Petigura et al. 2013). However, most of the *Kepler* planets orbit very faint stars, for which it is quite difficult to obtain precise radial velocity (RV)

measurements that are necessary to constrain planetary masses. On the other hand, ground-based systematic surveys (e.g. HATNet: Bakos et al. 2002; SuperWASP: Pollacco et al. 2006; KELT: Pepper et al. 2007; QES: Alsubai et al. 2013; HATSouth: Bakos et al. (2013); NGTS: Wheatley 2013) usually provide a large number of candidates around stars that are sufficiently bright to enable measuring their RVs, from which strong observational constraints for theoretical studies can be obtained. The upcoming space mission, TESS (Ricker et al. 2015), will target main-sequence dwarf stars that are brighter than 13th magnitude and could yield over 1000 planets smaller than Neptune. In addition, all-sky surveys such as MASCARA (Snellen et al. 2012), Evryscope, (Law et al. 2015) and Fly’s Eye Camera (Pál et al. 2016) will also be able to provide planet candidates around bright stars for detailed characterisation.

Precise measurements and analysis of these systems reveals that planets with similar masses can have very different radii, resulting in very unique physical characteristics. For example, Jupiter-mass planets can range in radii from $0.775 R_J$ (WASP-59b Hébrard et al. 2013) to $1.932 R_J$ (WASP-17b Anderson et al. 2010; Southworth et al. 2012). A growing number of short-period sub-Saturn and super-Neptune mass planets such as WASP-39b ($M_p = 0.28 M_J$; Faedi et al. 2011), HAT-P-11b ($M_p = 0.081 M_J$; Bakos et al. 2010), and HAT-P-26b ($M_p = 0.059 M_J$; Hartman et al. 2011) were also found. Many of these planets were found to have radii larger than predicted from standard coreless models (e.g. Fortney et al. 2007). Some theories suggest that the planet radius is correlated with the equilibrium temperature. For example, strong stellar irradiation could heat up the planet, inflating its radius (Guillot et al. 1996). The planetary interior could also be tidally heated as the orbit circularises (Bodenheimer et al. 2001, 2003). An enhanced atmospheric opacity can hinder the cooling process of the planet such that the planet radius can remain larger for longer (Burrows et al. 2007). The interaction between stellar wind and the magnetic field of the planet can lead to Ohmic heating, which could also influence the temperature of the planet (Batygin et al. 2011). Low-density planets with extended atmospheres orbiting bright host stars are ideal targets for transmission spectroscopy, which can further reveal the composition of planets.

We present here the discovery of three new planets, WASP-127b, WASP-136b, and WASP-138b, discovered by the SuperWASP survey. Section 2 summarises the observations from the WASP detection, follow-up photometry, and spectroscopic data of each of the planets. In Sect. 3, we describe our analysis and present the derived results of the system parameters. Lastly, we discuss the system characteristics and how evolution theories could explain the existence of these planets in Sect. 4.

2. Observations

2.1. SuperWASP

The SuperWASP-North facility is situated at the Observatorio del Roque de los Muchachos in La Palma, Canary Islands, and the SuperWASP-South facility is located at the Sutherland Station of the South African Astronomical Observatory. Both cameras consist of an array of 8 Canon 200 mm, f/1.8 telephoto lenses that are linked to e2v CCDs of 2048×2048 pixels each. The cameras in each of the facilities provide a total field of view of 8×64 square degrees and a pixel scale of $13.7''$ (Pollacco et al. 2006).

WASP data were observed with an exposure time of 30 s and an average cadence of 8–10 min. The data were reduced

with the pipeline as described in Pollacco et al. (2006). The box least-squares fit (Kovács et al. 2002) and the SysRem detrending algorithm (Tamuz et al. 2005) were used to analyse light curves from multiple seasons to determine planetary transit signals and provide system parameters for the candidates (Collier Cameron et al. 2006).

WASP-127 was observed between 2006 July 03 and 2014 June 13. A total number of 87 349 photometric data points were taken. The number of transits and in-transit data depends on the camera used and the season in which the star was observed. In the best season, 57 transits were observed with 1084 in-transit data points. There were always more than 500 in-transit data points obtained in all seasons, with more than 6 transits observed. WASP-136 was observed between 2006 December 29 and 2014 December 06. A total number of 97 827 photometric data points were taken. In the best season, 44 transits were observed with 2253 in-transit data points. Except for a few seasons, there were always more than 500 in-transit data points, with more than 7 transits observed. WASP-138 was observed between 2008 April 02 and 2012 December 20. A total number of 39 381 photometric data points were taken. In the best season, 58 transits were observed with 1077 in-transit data points. There were always more than 87 in-transit data points, with more than 7 transits observed.

Each set of data was analysed with the transit search algorithm (Collier Cameron et al. 2007) and was flagged as planetary candidates for follow-up observations. The algorithm revealed that WASP-127 has a periodicity of $P = 4.18$ days, transit duration of $T_{14} \approx 3.6$ h, and a depth of ~ 5.8 mmag. WASP-136 showed a period of $P = 5.22$ days, transit duration of $T_{14} \approx 5.2$ h, and a depth of ~ 2.9 mmag. The transit signal of WASP-138 showed a period of $P = 3.6$ days, transit duration of $T_{14} \approx 4.1$ h, and a depth of ~ 8.2 mmag. Subsequent follow-up photometry and spectroscopy were obtained to confirm the existence of the planets and to characterise their physical parameters.

2.2. Spectroscopic follow-up

We have obtained spectra of WASP-127, WASP-136, and WASP-138 with the SOPHIE and CORALIE spectrographs. SOPHIE is mounted on the 1.93 m telescope (Bouchy et al. 2009) on the Observatoire de Haute-Provence (OHP) and CORALIE is mounted on the 1.2 m Euler-Swiss telescope (Queloz et al. 2000; Pepe et al. 2002) in La Silla, Chile. We obtained the SOPHIE observations in high-efficiency mode ($R = 40\,000$), while CORALIE observations were made with an instrumental resolution of $R = 55\,000$.

A total of 28 spectral measurements of WASP-127 were taken between 2013 April 18 and 2015 April 9 using CORALIE. Six of the measurements were obtained after the instrumental upgrade in November 2014, which led to an offset of the zero point of the instrument, hence they will be treated as if they were from different instruments in our analysis. In addition, 13 SOPHIE measurements of WASP-127 were obtained between 2013 April 18 and 2014 December 31. Twenty-three CORALIE spectra of WASP-136 were obtained from 2014 June 24 to 2014 October 28. Between 2014 October 20 and 2015 January 25, 10 SOPHIE and 10 CORALIE measurements were made for WASP-138. All SOPHIE and CORALIE data were reduced with their respective standard reduction pipelines. The data were calibrated against radial velocity (RV) standards, yielding absolute RV measurements (Baranne et al. 1996). We computed the RV of each system with a weighted cross-correlation method as described in Baranne et al. (1996) and Pepe et al. (2002). Figures 1

Table 1. Photometric properties of WASP-127, WASP-136, and WASP-138.

Parameter	WASP-127	WASP-136	WASP-138
Identifier	1SWASP J104214.08–035006.3	1SWASP J000118.17–085534.6	1SWASP J024633.37–002750.0
RA(J2000)	10:42:14.08	00:01:18.17	02:46:33.37
Dec(J2000)	−03:50:06.3	−08:55:34.6	−00:27:50.0
<i>B</i>	10.79	10.39	12.28
<i>V</i>	10.15	9.98	11.81
<i>R</i>	9.74	9.71	11.40
<i>H</i>	8.74	8.79	10.54
<i>K</i>	8.64	8.81	10.49

Fig. 1. *Upper panel:* phase-folded radial velocity of WASP-127 as a function of the orbital phase with best-fit RV curve (from the analysis with only the CORALIE RVs) plotted as a black solid line. CORALIE data observed before the instrumental upgrade are denoted by red circles, while data taken after the upgrade are denoted by blue triangles. *Lower panel:* residuals from the RV fit as a function of orbital phase. **Fig. 2.** Same as Fig. 1 with SOPHIE data included as black open squares. The best-fit RV curve is obtained from our solution with both CORALIE and SOPHIE RVs.

and 2 show the phase-folded RV measurements of WASP-127 from two different analyses (see Sect. 3.2). Similar RV plots of WASP-136 and WASP-138 are shown in Figs. 3 and 4, respectively. All CORALIE data observed before the instrumental upgrade are represented by red circles, and blue triangles are data obtained after the upgrade. SOPHIE measurements are denoted by open black squares.

WASP-127 has a visual companion located 41'' away. We inspected the line bisector and searched for asymmetry in the stellar line profiles that may have arisen through stellar activity or a blended binary system (Queloz et al. 2001). Figure 5 shows the bisector velocity span (V_{span}) as a function of RV. No correlation is seen between V_{span} and RV, supporting the detection of a genuine planetary signal. Similar results were found for WASP-136 and WASP-138, where no correlation is seen between V_{span} and RV.

2.3. Photometric follow-up

Multiple follow-up photometry was taken for the three stars to place better constraints on the system parameters. The photometry was obtained with EulerCam at the 1.2 m *Euler-Swiss* telescopes (Lendl et al. 2012) and TRAPPIST (Jehin et al. 2011; Gillon et al. 2011), which are situated at ESO La Silla Observatory in Chile, the RISE camera on the Liverpool Telescope at the Observatorio del Roque de los Muchachos on La Palma (Steele et al. 2008) and the Zeiss 1.23 m telescope

Fig. 3. *Upper panel:* phase-folded radial velocity of WASP-136, measured by CORALIE (red circles), as a function of the orbital phase with the best-fit RV curve plotted as a black solid line. *Lower panel:* residuals from the RV fit as a function of orbital phase.

at the German-Spanish Astronomical Center at Calar Alto in Spain. The summary of our follow-up photometric observations is given in Table 2, and the phase-folded light curves are shown in Figs. 8–10, along with their best-fit transit models derived from our analysis in Sect. 3.2.

TRAPPIST: WASP-127 and WASP-136 were both observed with the 0.6 m TRANSiting Planets and PlanetesImals Small

Fig. 4. Upper panel: phase-folded radial velocity of WASP-138 as a function of the orbital phase with the best-fit RV curve plotted as a black solid line. CORALIE data are denoted by red circles and SOPHIE data are represented by black open squares. Lower panel: residuals from the RV fit as a function of orbital phase.

Fig. 5. Radial velocity bisector span of WASP-127 as a function of the relative radial velocity. CORALIE data before and after the instrumental upgrade are represented by red circles and blue triangles, respectively. SOPHIE data are denoted by open black squares. The grey dashed line shows the linear best fit to the data.

Telescope (TRAPPIST) robotic telescope. The telescope is equipped with a thermoelectrically cooled $2k \times 2k$ CCD camera, which has a pixel scale of $0.65''$ that translates into a $22' \times 22'$ field of view. For details of TRAPPIST, see [Gillon et al. \(2011\)](#) and [Jehin et al. \(2011\)](#).

A partial transit of WASP-127b was observed on 2014 March 18 through a Sloan- z' filter (effective wavelength $=896.3 \pm 0.8$ nm) with an exposure time of 9 s. The same filter was used to observe a partial transit of WASP-136b on 2014 November 24 (effective wavelength $=895.0 \pm 0.6$ nm), but with an exposure time of 7 s. Throughout the observations, the telescope was kept in focus and the positions of the stars on the detector were retained on the same few pixels, thanks to a software guiding system that regularly derives an astrometric solution for the images and sends pointing corrections to the mount when needed. The observation of WASP-136 was made towards the

Fig. 6. Radial velocity bisector span of WASP-136 as a function of the relative radial velocity. The grey dashed line shows the linear best fit to the data.

Fig. 7. Radial velocity bisector span of WASP-138 as a function of the relative radial velocity. CORALIE data are denoted by red circles and SOPHIE data are represented by open black squares. The grey dashed line shows the linear best fit to the data.

Table 2. Photometry observation of WASP-127, WASP-136, and WASP-138.

Planet	Date	Instrument	Filter	Comment
WASP-127b	18/03/2014	TRAPPIST	z	partial transit
	28/04/2014	EulerCam	Gunn r	partial transit
	13/02/2016	LT RISE	$V + R$	full transit
	18/04/2016	Zeiss 1.23 m	Cousins- I	full transit
WASP-136b	21/08/2014	EulerCam	z	partial transit
	24/11/2014	TRAPPIST	z	partial transit
	21/08/2015	EulerCam	z	full transit
WASP-138b	17/12/2015	EulerCam	NGTS	partial transit

end of night. Therefore the increase in airmass is reflected in the uncertainties of the photometry.

Data were reduced as described in [Gillon et al. \(2013\)](#). After a standard pre-reduction (bias, dark, and flat-field correction), the stellar fluxes were extracted from the images using

IRAF/DAOPHOT² (Stetson 1987). For each light curve, we tested several sets of reduction parameters and chose the one giving the most precise photometry for the stars of similar brightness as the target. After a careful selection of reference stars, the transit light curves were finally obtained using differential photometry.

EulerCam: we observed one full transit of WASP-127, one partial and one full transit of WASP-136, and one full transit of WASP-138 with EulerCam (Lendl et al. 2012). The full transit of WASP-127 was observed on 2014 April 28 with a Gunn *r* filter. The telescope was defocused throughout the observation with a FWHM of between 1.6 and 2.5 arcsec. A circular aperture of radius 4.7 arcsec was used along with one reference star for the extraction of the light curve.

A partial and a full transit of WASP-136 were obtained on 2014 August 21 and 2015 August 21, respectively. Both observations were taken using a Gunn *z* filter and an exposure time of 50 s. The telescope was substantially defocused throughout both nights. The FWHM of the first night was between 1.5 and 2.3 arcsec. A circular aperture of radius 2.7 arcsec and four reference stars were used for photometry extraction. The FWHM of the second night was between 1.9 and 3.0 arcsec. We used a circular aperture of radius 4.5 arcsec along with five reference stars for the photometry reduction.

The observation of WASP-138 was carried out on 2015 December 17 with an NGTS filter (with a custom wavelength of 550–900 nm) and exposure times of between 50 and 85 s. The telescope was substantially defocused and the FWHM was between 1.3 and 2.5 arcsec. A photometric aperture of 5.6 arcsec radius was used to extract the fluxes, and one reference star was used to generate the relative light curve. See Lendl et al. (2012) for further details on EulerCam and its data reduction procedures.

RISE: a full transit of WASP-127 was observed with RISE (Steele et al. 2008). The camera is equipped with a back-illuminated frame-transfer CCD of 1024 × 1024 pixels. A *V* + *R* filter (a custom filter constructed from 3 mm OG515 + 2 mm KG3, with a bandwidth of 500–900 nm) and a 2 × 2 binning of the detector were used for the observation, resulting in a pixel scale of 1.08 arcsec/pixel. We used an exposure time of 1.5 s and defocused the telescope by 0.5 mm for all the observations. Images were automatically bias, dark, and flat corrected by the RISE pipeline. We selected four comparison stars for data reduction. The data were reduced with the standard IRAF apphot routines using a 1.4 pixels (4.86 arcsec) aperture. We attribute the increased scatter around mid-transit to thin clouds (see Fig. 8).

ZEISS: the Zeiss 1.23 m telescope has a focal length of 9857.1 mm and is equipped with the DLR-MKIII camera, which has 4k × 4k pixels of size 15 micron. The plate scale is 0.32 arcsec/pixel and the field of view is 21.5 × 21.5 arcmin. It has previously been successfully used to follow-up many planetary transits (e.g. Mancini et al. 2015). The telescope was defocused and the exposure time was adjusted several times during the night in a range of between 65 and 105 s.

The guiding camera did not operate correctly on the night of our observations, and the usual precision was not achieved. The CCD was windowed to decrease the readout time and therefore sped up the cadence of the observations. The night was not photometric, and several clouds disturbed the observations. The

Fig. 8. Photometry follow-up of WASP-127 observed from EulerCam (red), TRAPPIST (green), RISE (magenta) and Zeiss (cyan). The data are phase-folded with the ephemeris from our analysis. The light curves are assigned an arbitrary offset from the zero magnitude and are binned to a 2-min cadence for clarity. The best-fit transit model from Mandel & Agol (2002) is plotted as a black solid line, and the residuals of the fit are plotted directly below the light curves.

data were reduced using a revised version of the DEFOT code (Southworth et al. 2014). In brief, the scientific images were calibrated and the photometry was extracted by the standard aperture-photometry technique. The resulting light curve was normalised to zero magnitude by fitting a straight line to the out-of-transit data.

3. Results

3.1. Stellar parameters

The CORALIE spectra of the individual host stars were co-added to produce spectra for analysis using the methods

² IRAF is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.

Fig. 9. Photometry follow-up of WASP-136 observed from EulerCam (red) and TRAPPIST (green). The data are phase-folded with the ephemeris from our analysis. The light curves are assigned an arbitrary offset from the zero magnitude and are binned to a 2-min cadence for clarity. The best-fit transit model from Mandel & Agol (2002) is plotted as a black solid line, and the residuals of the fit are plotted directly below the light curves.

described in Doyle et al. (2013). The $H\alpha$ line was used to estimate the effective temperature (T_{eff}), and the Na I D and Mg I b lines were used as diagnostics of the surface gravity ($\log g$). The iron abundances were determined from equivalent-width measurements of several clean and unblended Fe I lines and are given relative to the solar value presented in Asplund et al. (2009). The quoted abundance errors include that given by the uncertainties in T_{eff} and $\log g$, in addition to the scatter due to measurement and atomic data uncertainties. The projected rotation velocities ($v \sin i$) were determined by fitting the profiles of the Fe I lines after convolving with the CORALIE instrumental resolution ($R = 55\,000$) and macroturbulent velocities adopted from the calibration of Doyle et al. (2014). The result of our spectral analysis is listed in Table 3.

Fig. 10. Photometry follow-up of WASP-138 observed from EulerCam (red). The data are phase-folded with the ephemeris from our analysis. The EulerCAM light curve is assigned an arbitrary offset from the zero magnitude for clarity. The best-fit transit model from Mandel & Agol (2002) is plotted as a black solid line, and the residuals of the fit are plotted directly below the light curves.

Table 3. Stellar parameters of WASP-127, WASP-136, and WASP-138 obtained from spectral analysis.

Parameter	WASP-127	WASP-136	WASP-138
T_{eff} (K)	5750 ± 100	6250 ± 100	6300 ± 100
$\log g$	3.9 ± 0.1	3.9 ± 0.1	4.1 ± 0.1
$v \sin i$ (km s $^{-1}$)	0.3 ± 0.2	13.1 ± 0.8	7.7 ± 1.1
[Fe/H]	-0.18 ± 0.06	-0.18 ± 0.10	-0.09 ± 0.10
$\log A(\text{Li})$	1.97 ± 0.09	2.50 ± 0.08	2.20 ± 0.08
Mass ($M_{\odot}$)	1.31 ± 0.05	1.38 ± 0.08	1.20 ± 0.03
Radius ($R_{\odot}$)	1.33 ± 0.03	2.07 ± 0.24	1.43 ± 0.02
Sp. type	G5	F5	F9
Distance (pc)	102 ± 12	164 ± 18	308 ± 51

We used the open-source BAGEMASS³ code (Maxted et al. 2015a) to estimate the masses and ages of the three stars. The stellar mass and age were derived by calculating the stellar model grid of a single star using the GARSTEC stellar evolution code (Weiss & Schlattl 2008). A Bayesian method was then applied to sample the probability distribution of the posterior mass and age. The result of our stellar mass and age analysis is shown in Table 4. The probability distribution along with the best-fit stellar evolutionary tracks and isochrones are plotted in Fig. 11.

³ <https://sourceforge.net/projects/bagemass/>

Table 4. Stellar mass and age estimates of WASP-127, WASP-136, and WASP-138 from BAGEMASS.

Star	Mass [$M_{\odot}$]	τ_{iso} [Gyr]	τ_{gyro} [Gyr]
WASP-127	0.93 ± 0.04	11.41 ± 1.80	$v \sin i$ too low
WASP-136	1.29 ± 0.08	3.62 ± 0.70	$>1.3^{+1.2}_{-0.6}$
WASP-138	1.17 ± 0.06	3.44 ± 0.93	$>2.7^{+2.5}_{-1.3}$

Notes. The isochronal ages are presented in the τ_{iso} column and the gyrochronological ages are presented in the τ_{gyro} column.

WASP-136 is an F-type star with an age estimated to be 3.62 ± 0.70 Gyr. It also has a surface gravity of $\log g = 3.9 \pm 0.1$. This implies that WASP-136 is a subgiant star that is evolving off the main sequence. We also applied the relation from Barnes (2007) to derive the gyrochronological ages (τ_{gyro}) of WASP-136 and WASP-138. From the stellar rotation period calculated from the measured $v \sin i$ and radius, the estimated τ_{gyro} of WASP-136 and WASP-138 are $1.3^{+1.2}_{-0.6}$ Gyr and $2.7^{+2.5}_{-1.3}$ Gyr, respectively. The $v \sin i$ value of WASP-127 is too low for a sensible estimate. The $v \sin i$ values give upper limits on the rotation periods, hence the τ_{gyro} can only provide a lower limit here. There are discrepancies between the isochronal ages and τ_{gyro} of WASP-136 and WASP-138, which may have arisen as a result of tidal interactions. In gyrochronology, the rate of stellar surface rotation is used to determine the stellar age. However, currently available gyrochronology models do not predict the observed rotation rate of older stars. Evolved stars exist whose rotation rate is spun up by the tidal forces of the planets, which causes τ_{gyro} to appear significantly lower than the isochronal ages (Maxted et al. 2015b; van Saders et al. 2016). This suggests that τ_{gyro} is a less suitable way of estimating the stellar age. We searched for rotational modulation of the WASP photometry using the method of Maxted et al. (2011). No rotational modulation was found above 2 mmag, suggesting that the host stars are inactive.

3.2. System parameters from MCMC analysis

The Markov chain Monte Carlo (MCMC) method was used to derive the system parameters. We simultaneously analysed the WASP photometry, the follow-up photometry, and CORALIE and SOPHIE RV measurements. The details of our method are described in Collier Cameron et al. (2007) and Pollacco et al. (2008). In summary, the transit light curves were modelled with analytical functions from Mandel & Agol (2002), and the stellar limb-darkening was accounted for using the non-linear four-component model of Claret (2000, 2004). We also applied a linear decorrelation to remove systematic trends in our photometry. The parameters used in our MCMC analysis are the mid-transit epoch T_0 , the period P , the planet-to-stellar-size ratio (a proxy for the transit depth) ΔF , the transit duration T_{14} , the impact parameter b , the stellar metallicity $[\text{Fe}/\text{H}]$, the stellar effective temperature T_{eff} , the stellar reflex velocity K_1 , and the Lagrangian elements $\sqrt{e} \cos(\omega)$ and $\sqrt{e} \sin(\omega)$ (where e is the eccentricity and ω is the longitude of periastron). These values were randomly perturbed at each step of the burn-in phase and the minimum χ^2 of the model was calculated. The Metropolis-Hastings method (Metropolis et al. 1953; Hastings 1970) was applied to derive the best-fit solution to the set of parameters, and the median of the posterior distribution was used as the final solution along with the 1σ uncertainties. The result of our MCMC analysis is

Fig. 11. Stellar mass and age analysis of WASP-127 (upper panel), WASP-136 (middle panel) and WASP-138 (lower panel) using BAGEMASS. The dotted black line is the ZAMS. The solid blue line is the mass evolutionary track, and the blue dashed tracks on either side are for the 1σ error of the mass. The solid orange line is the stellar age isochrone and the orange dashed lines represents the 1σ error. The density of MCMC samples is shown in the colour scale of the plotted posterior distribution.

presented in Table 6 and the best-fit RV curves and the best-fit transit light curves are presented in Figs. 1–4 and Figs. 8–10, respectively.

WASP-127: we imposed a main-sequence mass-radius constraint in the MCMC analysis of WASP-127. However, the constraint offers a solution where the posterior stellar parameters do not agree with our spectral analysis as described in Sect. 3.1. We therefore relaxed the main-sequence constraint for our analysis. The solution does not give convincing evidence of an eccentric

Table 5. WASP-127 parameters from the MCMC analysis.

Parameter (unit)	Solution without SOPHIE	Solution with SOPHIE
P (d)	4.178062 ± 0.000002	4.178062 ± 0.000002
T_0 (BJD)	$2\,457\,248.74131 \pm 0.000160$	$2\,457\,248.74126 \pm 0.000184$
$\Delta F = R_{\text{pl}}^2/R_*^2$	0.01037 ± 0.00015	0.01050 ± 0.00017
T_{14} (d)	0.1795 ± 0.0007	0.1802 ± 0.0009
b	$0.15^{+0.09}_{-0.11}$	$0.25^{+0.08}_{-0.16}$
i ($^\circ$)	$88.7^{+0.8}_{-0.6}$	$88.1^{+1.2}_{-0.7}$
M_* ($M_\odot$)	1.08 ± 0.03	1.08 ± 0.03
R_* ($R_\odot$)	1.39 ± 0.03	1.42 ± 0.05
$\log g_*$ (cgs)	4.18 ± 0.01	4.17 ± 0.02
ρ_* ($\rho_\odot$)	0.404 ± 0.015	0.380 ± 0.031
T_{eff} (K)	5620 ± 85	5639 ± 90
M_{pl} (M_J)	0.18 ± 0.02	0.16 ± 0.02
R_{pl} (R_J)	1.37 ± 0.04	1.41 ± 0.06
$\log g_{\text{pl}}$ (cgs)	2.33 ± 0.06	2.25 ± 0.7
ρ_{pl} (ρ_J)	$0.068^{+0.010}_{-0.010}$	$0.055^{+0.011}_{-0.009}$
a (au)	0.0520 ± 0.0005	0.0522 ± 0.0005
$T_{\text{pl},A=0}$ (K)	1400 ± 24	1417 ± 32

Notes. The solutions are derived with and without SOPHIE RV data to test for the effect of the RV dispersion. The resulting RV fits show a 1σ agreement between the two solutions.

orbit ($\chi^2_{\text{circ}} = 37.2$ and $\chi^2_{\text{ecc}} = 37.3$), and a circular orbit is adopted.

Both CORALIE and SOPHIE RV measurements show some dispersion from the fit. However, CORALIE RVs suggest an in-phase variation. Initial analysis with both sets of data suggests a planet with a much lower mass that is unlikely to be detected by both spectrographs. We therefore increased the size of the error bars of the SOPHIE RVs by a multiplication factor of 2, to cause the reduced chi-square statistics (χ^2_{reduced}) to converge to unity. The solution using the original weighting of the SOPHIE RVs has a χ^2_{reduced} value of 1.31. When the weighting of the SOPHIE RVs is decreased, the χ^2_{reduced} becomes 0.91. We decided to look for a best-fit solution with the latter case because the fit was improved.

We explored the solutions with and without the set of SOPHIE RV measurements. For the case using only the CORALIE RVs, the best-fit reflex radial velocity value is $21.4 \pm 2.8 \text{ ms}^{-1}$. The solution using both the CORALIE and SOPHIE RVs gives a best-fit reflex radial velocity of $18.7 \pm 2.7 \text{ ms}^{-1}$. The two solutions give a 1σ agreement in the reflex radial velocity, and Table 5 shows the solutions from both analyses. We attribute the dispersion of the residuals to the very low mass of the planet, which is challenging for the spectrographs to detect. Higher precision follow-up RV measurements is recommended in the future to accurately determine the mass of the planet.

WASP-136: as expected from a subgiant star, a main-sequence mass-radius constraint gives an unrealistic solution for the stellar metallicity and the effective temperature. We used the χ^2 statistics to test for the goodness of fit of our model. There is no evidence supporting an eccentric orbit ($\chi^2_{\text{circ}} = 46.6$ and $\chi^2_{\text{ecc}} = 43.5$), hence we adopt the circular orbit and relaxed the main-sequence constraint.

WASP-138: using all the follow-up photometry and RV measurements, we find that imposing a main-sequence constraint has an insignificant effect on the solution. There is no evidence suggesting an eccentric orbit ($\chi^2_{\text{circ}} = 11.2$ and $\chi^2_{\text{ecc}} = 10.4$). We

Table 6. System parameters of WASP-136 and WASP-138 from the MCMC analysis.

Parameter (unit)	WASP-136b	WASP-138b
P (d)	5.215357 ± 0.000006	3.634433 ± 0.000005
T_0 (BJD)	$2\,456\,776.90615 \pm 0.00109$	$2\,457\,326.62183 \pm 0.000319$
$\Delta F = R_{\text{pl}}^2/R_*^2$	0.00411 ± 0.00015	0.00683 ± 0.00013
T_{14} (d)	0.2272 ± 0.0033	0.1572 ± 0.0012
b	$0.59^{+0.08}_{-0.14}$	$0.19^{0.12}_{0.15}$
i ($^\circ$)	$84.7^{+1.6}_{-1.3}$	$88.5^{+0.9}_{-1.2}$
M_* ($M_\odot$)	1.41 ± 0.07	1.22 ± 0.05
R_* ($R_\odot$)	2.21 ± 0.22	1.36 ± 0.05
$\log g_*$ (cgs)	3.90 ± 0.06	4.25 ± 0.02
ρ_* ($\rho_\odot$)	0.132 ± 0.030	0.488 ± 0.044
T_{eff} (K)	6260 ± 100	6272 ± 96
M_{pl} (M_J)	1.51 ± 0.08	1.22 ± 0.08
R_{pl} (R_J)	1.38 ± 0.16	1.09 ± 0.05
$\log g_{\text{pl}}$ (cgs)	3.26 ± 0.09	3.36 ± 0.04
ρ_{pl} (ρ_J)	$0.581^{+0.230}_{-0.148}$	$0.92^{+0.097}_{-0.146}$
a (au)	0.0661 ± 0.0012	0.0494 ± 0.0007
$T_{\text{pl},A=0}$ (K)	1742 ± 82	1590 ± 31

therefore adopt the solution with a circular orbit with no main-sequence constraint.

4. Discussion and conclusion

4.1. WASP-127b

From our best-fit MCMC solution, we obtain a planet with a mass of $0.18 \pm 0.02 M_J$ and a radius of $1.37 \pm 0.04 R_J$ ($M_{\text{pl}} = 0.16 \pm 0.02 M_J$ and $R_{\text{pl}} = 1.41 \pm 0.06 R_J$ for the case where RVs from both CORALIE and SOPHIE were included for analysis). This means that WASP-127b has a density of $0.07^{+0.01}_{-0.01} \rho_J$, making it one of the lowest density planets ever discovered. It is also the planet with the second lowest mass discovered by WASP, only more massive than WASP-139b (Hellier et al. 2017).

Compared to the standard coreless model of Fortney et al. (2007), WASP-127b is over 30% larger than expected for a planet with an orbit at 0.045 au around a 4.5 Gyr solar-type star. From Sect. 3.1, WASP-127 is estimated to be much older than the Sun. Hence the theoretical radius of the planet should be even smaller. The anomalously large radius of WASP-127b could be explained by several inflation mechanisms. One such mechanism is tidal heating (Bodenheimer et al. 2001, 2003), where the planetary interior receives heat energy as the orbit circularises. As with many short-period gas giants, the orbit of WASP-127b may have shrunk and migrated to its current position through planet-planet scattering (Ford & Rasio 2008) or Kozai mechanism (Fabrycky & Tremaine 2007; Kozai 1962; Lidov 1962). The planetary orbit may also have been tidally circularised during the migration process, which results in rapid transfer of energy to its interior, inflating the radius of the planet. This energy transfer process occurs rapidly at the early stages of the evolution history of the system, hence it is unclear how efficient this way of heating up the planetary interior is for such an old system. On the other hand, the atmosphere of WASP-127b could have an enhanced opacity resulting from enhanced metallicity (Burrows et al. 2007). This can delay the cooling effect and maintain the inflated radius for a longer time. Batygin et al. (2011) suggested that the Ohmic heating

mechanism could account for the large planetary radii. The interaction between the planetary magnetic field and the flow of ionised atmospheric heavy elements could induce an electromotive force. This reaction can drive electrical currents throughout the planet and lead to inflation as the planet heats up. The Ohmic dissipation, however, is limited by the depth of the dissipation. The Huang & Cumming (2012) model suggests that the convective zone boundary will move deeper if Ohmic dissipation occurs outside the convection zone, which in turn will slow down the efficiency of the planet cooling process. Recently, Lopez & Fortney (2016) have suggested that a planet whose radius was inflated through internal heating could re-inflate again as its host star moves towards the RGB phase because of increased irradiation. Their studies also showed that re-inflation of a planet is most likely for low-mass and short-period planets. WASP-127 is estimated to have a main-sequence lifetime of approximately $t_{\text{MS}} = t_{\odot}(M/M_{\odot})^{-2.5} \approx 8$ Gyr, where $t_{\odot}$ is the solar main-sequence lifetime, $M_{\odot}$ is the solar mass and M is the stellar mass. WASP-127 has an isochronal age of 11.41 ± 1.80 Gyr, implying that the star is at the end of the main-sequence phase. Therefore, WASP-127b may be undergoing a phase of re-inflation as its host star enters the subgiant branch.

WASP-127b is a highly inflated planet that shares many similarities with a number of low-density planets such as WASP-39b (Faedi et al. 2011), WASP-113b (Barros et al. 2016), HAT-P-8b (Bayliss et al. 2015), HAT-P-11b (Bakos et al. 2010), HAT-P-47b, and HAT-P-48b (Bakos et al. 2016). Assuming it has an atmosphere identical to that of Jupiter ($\mu = 2.2u$, where the atomic mass unit is $u = 1.66 \times 10^{-27}$ kg), its scale height would be $H \approx 2500 \pm 400$ km. WASP-127b also orbits a bright G-type star of $V_{\text{mag}} = 10.172$, making it an excellent candidate for transmission spectroscopy. Figure 12 shows the planetary mass as a function of the orbital period. WASP-127b falls into the short-period Neptune desert (Mazeh et al. 2016), a region between Jovian and super-Earth planets with a lack of detected planets. The presence of such a region indicates the existence of two unique types of short-period planets, hot Jupiters and super-Earths, which have very different formation and evolution mechanisms. It also suggests that short-period planets with intermediate masses are likely to be destroyed.

4.2. WASP-136b

WASP-136b is an inflated hot-Jupiter transiting a bright F5 host star ($V_{\text{mag}} = 9.928$). The best-fit MCMC solution of the system gives a planetary mass of $1.51 \pm 0.08 M_{\text{J}}$ and a radius of $1.38 \pm 0.16 R_{\text{J}}$ which yields a planet density of $0.58^{+0.23}_{-0.15} \rho_{\text{J}}$. The estimated main-sequence lifetime of WASP-136 is approximately $t_{\text{MS}} \approx 4$ Gyr. In Sect. 3.1 we estimated the isochronal age of WASP-136 to be $\sim 3.6 \pm 0.7$ Gyr. This suggests that WASP-136 is at the end of the main-sequence phase. The density and surface gravity of WASP-136 implies that the star is a subgiant, which is consistent with the age estimate. The radius of WASP-136b is approximately 25% larger than predicted from the planet evolution model of Fortney et al. (2007) for a coreless planet. Like many bloated hot-Jupiters (WASP-54b: Faedi et al. 2013; WASP-78b and WASP-79b: Smalley et al. 2012; WASP-142b: Hellier et al. 2017), WASP-136b receives a stronger irradiation from its F-type host star compared to a G-type, which can lead to a more inflated planet. Similar to EPIC 211351816.01 (Grunblatt et al. 2016), the inflation mechanism of WASP-136b could follow the class I model from Lopez & Fortney (2016), where WASP-136b might be heated up through the deposit of some of the incident stellar irradiation into the planetary interior.

Fig. 12. Planetary mass against orbital period plot. Exoplanet data are taken from the NASA Exoplanet Archive (<http://exoplanetarchive.ipac.caltech.edu/>) and are plotted as grey dots. WASP-127b, WASP-136b, and WASP-138b are represented by green, red, and cyan circles, respectively. The black dashed lines are the upper and lower boundaries of the Neptune desert as defined by Mazeh et al. (2016). WASP-127b falls in this Neptune desert between Jovian and super-Earth planets.

Consequently, when the host of WASP-136b enters the subgiant branch, the planet could receive an increased stellar irradiation that will lead to re-inflation of the planet radius.

The existence of short-period hot Jupiters around subgiant stars is rare. The lack of giant planets at short orbital distances may be a consequence of tidal disruption (Schlaufman & Winn 2013). A planet residing inside the synchronous orbit could experience strong tidal forces and spiral inwards towards the star. When the planet eventually reaches the Roche limit, the tidal force becomes stronger than the planet's gravitational force, and the planet will be tidally disrupted. WASP-136b has an orbital distance of 0.0661 au and is approximately 46 times the Roche limit. We followed the derivation of Matsumura et al. (2010) and estimated that WASP-136b has a remaining lifetime of ~ 0.683 Gyr. Furthermore, during the post-main-sequence phase, the stellar radius expands and will eventually lead to the engulfment of the planet (Villaver & Livio 2009).

4.3. WASP-138b

Our best-fit solution gives a system with a planetary mass and radius of $1.22 \pm 0.08 M_{\text{J}}$ and $1.09 \pm 0.05 R_{\text{J}}$. The density of WASP-138b is $0.92^{+0.10}_{-0.15} \rho_{\text{J}}$. It orbits around an F9 star with a metallicity of $[\text{Fe}/\text{H}] = -0.09$ dex, slightly more metal-poor than the Sun. WASP-138b is a hot Jupiter that has similar characteristics to many short-period gas giants with a period of ~ 3 days, for example, WASP-35b (Enoch et al. 2011) and WASP-141b (Hellier et al. 2017). With an isochronal age of 3.4 ± 0.9 Gyr, the planet evolution model of Fortney et al. (2007) suggests that WASP-138b has a core mass of $\sim 10 M_{\oplus}$ of heavy elements.

Many interesting large short-period exoplanets are being discovered by ground-based surveys. Discoveries such as that of WASP-127b will provide exceptional targets for future missions such as JWST and for further characterisation. With the diverse range of exoplanets, it is important to understand the mass-radius relation and distinguish the mechanisms responsible for each

distinct class of planet. This will ultimately help our understanding of the dynamics of planetary systems.

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