Bulges and discs in the local Universe. Linking the galaxy structure to star formation activity

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ABSTRACT

We use a sample built on the SDSS DR7 catalogue and the bulge-disc decomposition of Simard et al. (2011, ApJS, 196, 11) to study how the bulge and disc components contribute to the parent galaxy’s star formation activity, by determining its position in the star formation rate (SFR) – stellar mass ($M_*$) plane at 0.02 < z < 0.1 and around the main sequence (MS) of star-forming galaxies. For this purpose, we use the bulge and disc colours as proxy for their SFRs, while the total galaxy SFR comes from H$_\alpha$ or $D_{21}$ H$_\alpha$. We study the mean galaxy bulge-total mass ratio ($B/T$) as a function of the residual from the MS ($\Delta_{\text{MS}}$) and find that the $B/T-\Delta_{\text{MS}}$ relation exhibits a parabola-like shape with the peak of the MS corresponding to the lowest $B/T$s at any stellar mass. The lower and upper envelope of the MS are populated by galaxies with similar $B/T$, velocity dispersion and concentration ($R_90/R_{50}$) values. The mean values of such distributions indicate that the majority of the galaxies are characterised by classical bulges and not pseudo-bulges. Bulges above the MS are characterised by blue colours or, when red, by a high level of dust obscuration, thus indicating that in both cases they are actively star forming. When on the MS or below it, bulges are mostly red and dead. At stellar masses above $10^{10.5} M_\odot$, bulges on the MS or in the green valley tend to be significantly redder than their counterparts in the quiescence region, despite similar levels of dust obscuration. This could be explained with different age or metallicity content, suggesting different evolutionary paths for bulges on the MS and green valley with respect to those in the quiescence region. The disc $g-r$ colour anti-correlates at any mass with the distance from the MS, getting redder when approaching the MS lower envelope and the quiescence region. The anti-correlation flattens as a function of the stellar mass, likely due to a higher level of dust obscuration in massive SF galaxies. We conclude that the position of a galaxy in the Log SFR – Log $M_*$ plane depends on the star formation activity of its components: above the MS both bulge and disc are actively star forming. The nuclear activity is the first to be suppressed, moving the galaxies on the MS. Once the disc stops forming stars as well, the galaxy moves below the MS and eventually to the quiescence region. This is confirmed by a significant percentage (≈45%) of passive galaxies with a secure two component morphology, coexisting with a population of pure spheroidals. Our findings are qualitatively in agreement with the compaction-depletion scenario, in which subsequent phases of gas inflow in the centre of a galaxy and depletion due to high star formation activity move the galaxy across the MS before the final quenching episode takes place.

Key words. galaxies: evolution – galaxies: bulges – galaxies: star formation – galaxies: structure – galaxies: spiral

1. Introduction

The main sequence (MS) of star-forming galaxies (SFGs) is a linear relation between the star formation rate (SFR) of a galaxy and its stellar mass ($M_*$). This relation is close to linear, with a small scatter (0.2–0.3 dex) over a wide stellar mass range (e.g., Brinchmann et al. 2004; Noeske et al. 2007a,b; Daddi et al. 2007; Elbaz et al. 2007; Salim et al. 2007; Whitaker et al. 2012; Speagle et al. 2014; Pannella et al. 2015). It has also been shown that, while the slope of the relation remains ~1 up to $z \sim 2$, the normalisation changes drastically with redshift, where the SFR of galaxies at $z \sim 2$ is almost 20 times larger than that of galaxies at $z \sim 0$. (e.g., Schreiber et al. 2015). The physical processes that cause this decrease in SF activity are generally grouped under the term quenching, a topic at the core of galaxy evolution studies.

Quenching works by prohibiting SF in a galaxy and by acting on the cold gas reservoir. Processes that expel cold gas from galaxies, such as galactic winds driven by supernovae and massive stars are efficient in dark matter (DM) haloes with $M < 10^{12} M_\odot$ (e.g. Dekel & Silk 1986; Efstathiou 2000). Above this mass threshold, more powerful outflows are required to counter the deeper DM halo potential well. In such haloes, accreting central BHs can quench star formation by either heating the gas in the disc (quasar mode; Hopkins et al. 2006a,b; Dunn et al. 2010; Feruglio et al. 2010; Fabian 2012; Cicone et al. 2014), or mechanically removing the gas from the inner regions through powerful radio jets (radio mode; Croton et al. 2006; Bower et al. 2006, 2008; De Lucia et al. 2006; McNamara & Nulsen 2007; Vogelsberger et al. 2013; Di Matteo et al. 2005; Ciotti et al. 2007; Cattaneo et al. 2009). Besides ejecting the gas, the effects of quenching can also be caused by a lack of cold gas supply. In DM halos with $M > 10^{12} M_\odot$, the transition from cold to hot accretion (Dekel & Birnboim 2006) would prohibit further SF (Cen 2014). On the other hand, Martig et al. (2009) propose morphological quenching where the growth of central mass concentration, i.e. a massive bulge, could simply stabilise a gas disc against fragmentation, thus preventing SF without affecting the cold gas reservoir in the galaxy. It has also been proposed that quenching could be a combination of all these processes. For example, using their cosmological zoom-in simulations, Zolotov et al. (2015) show that quenching of high redshift SFGs is preceded by a compaction phase that creates the so-called blue nuggets: SFGs morphologically similar to quiescent ones. This
compaction phase is caused by strong inflows to the centre due to minor mergers and/or counter-rotating gas and violent disc instabilities. The availability of dense cold gas in the centre results in a high SF and consequent stellar/supernova and/or AGN feedback causing quenching. Tacchella et al. (2015) propose that episodes of compaction, quenching and replenishment are responsible for the position of a galaxy in a ±0.3 dex region around the MS. The final quenching happens when the replenishment time is longer than the depletion time (i.e. in massive haloes, or at low redshifts) and results in a passive galaxy.

Observational evidence in favour of this scenario increased in the past years. The SFGs at $z \gtrsim 2$ characterised by the largest central gas densities seem to have spheroidal morphologies similar to the one of passive galaxies at the same redshift (Wuyts et al. 2011; Barro et al. 2014; Patel et al. 2013; Stefanon et al. 2013; Williams et al. 2013), but are significantly different from other SFGs (with lower central gas densities), which at $z \gtrsim 2$ are mostly irregular and clumpy (Elmegreen et al. 2004; Genzel et al. 2008; Guo et al. 2015b). At low redshift, less massive SFGs are mainly pure discs, while more massive SFGs are characterised by a bulge plus disc structure (Wuyts et al. 2012; Bruce et al. 2012, 2014; Lang et al. 2014). Wuyts et al. (2011) analyse the dependence of galaxy structure (size and Sérsic index) on the position of the galaxies with respect to the MS ridge at $z=0–2$. They find that the Sérsic index tends to be roughly the same, $n \sim 1$, within $3\sigma$ from the MS, i.e., there is no significant gradient of $n$ across the MS. They observe an increase of $n$ only in the starburst region. While Cheung et al. (2012) confirm that the Sérsic index most sharply discriminates between the red sequence and the blue cloud, they also find a large number of blue outliers ($\approx 40\%$) in their $n > 2.3$ galaxy sample at $z = 0.65$. Concurrently, using a sample of local galaxies Guo et al. (2015a) report that bulges/bars are responsible for the large dispersion of the specific SFR (sSFR), but only for massive SFGs. These recent results imply that a significant percentage of SFGs must have a bulge plus disc morphology. Under the assumption that the star formation activity is confined in the disc, Abramson et al. (2014) show that defining the sSFR with respect to the disc mass rather than the total galaxy mass decreases (and sometimes erases) the dependence of sSFR on stellar mass. This suggests that the slope of the sSFR − $M_*$ relation reflects the increase of the bulge prominence with stellar mass, and also points towards the importance of treating galaxies as multicomponent systems.

The aim of this paper is to study the relation between galaxies structural parameters and location with respect to the MS in the local Universe. The choice of performing this study on a local galaxy sample is dictated by the fact that the Sloan Digital Sky Survey (SDSS; Strauss et al. 2002) provides the required statistics to dissect the MS brick by brick to study the nature of its scatter as a function of the galaxy morphology with high accuracy. In addition, the availability of accurate morphological classification and bulge/disc decomposition (Simard et al. 2011) of the SDSS galaxies allows us to study the role and interconnection of the individual galaxy components. This is the first paper of a series, which follows the evolution of the relation of the galaxy structural parameter and scatter across the MS in the $0–2.0$ redshift window.

The paper is organised as follows. In Sect. 1 we describe our dataset. In Sect. 2 we analyse the reliability of the morphological classification and colours of the bulge and disc in individual galaxies. In Sect. 3 we present our results and in Sect. 4 we present our discussion and conclusions. Throughout the study, the following cosmology is assumed: $H_0 = 70.0 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_m = 0.3$ and $\Omega_{\Lambda} = 0.7$.

2. Dataset

In this paper we make use of the catalogues derived from the SDSS-DR7 database (Abazajian et al. 2009) and in particular the following quantities: SFRs, stellar masses, stellar velocity dispersion, and properties derived from bulge/disc decomposition of galaxies. We now briefly summarise how these were derived and provide references to the original papers for details.

2.1. SFRs, stellar masses, and velocity dispersion

SFRs and $M_*$ are taken from the MPA/JHU DR7 catalogues (Kauffmann et al. 2003; Brinchmann et al. 2004; Salim et al. 2007). In particular, we use the total, aperture corrected, stellar mass computed from the total ModelMag photometry that is less sensitive to emission line contamination. SFRs come from emission line modelling using the grid of $\sim 2 \times 10^5$ models of Charlot & Longhetti (2001), where dust corrections are mainly based on the $H\alpha/H\beta$ ratio. The stellar aperture velocity dispersion $\sigma_{ap}$ (computed from stars) and mean signal-to-noise ratio (S/N) per pixel are taken from the MPA/JHU gal_info catalogue, while values of the $H\alpha$ and $H\beta$ fluxes and their $S/N$s are from the MPA/JHU gal_line catalogue.

2.2. The bulge/disc decomposition catalogue

Galaxy structural parameters are taken from the bulge/disc decomposition of the Simard et al. (2011) catalogue (S11 hereafter). In S11, the GIM2D code (Simard et al. 2002) has been applied to the $g$ and $r$ filter images of 1 123 718 SDSS DR7 galaxies to obtain a two-dimensional bulge-disc decomposition convolved with the point-spread function. The simultaneous fit of the $g$ and $r$ images makes the decomposition robust against spurious effects. S11 provide structural parameters for three different fitting models: 1) a pure Sérsic; 2) an exponential disc plus De Vaucouleurs bulge; and 3) an exponential disc plus free Sérsic bulge model. In this work, we use the catalogue obtained from the exponential disc plus De Vaucouleurs bulge model as the F statistics reveal that SDSS images are not good enough to efficiently compute the Sérsic index of the bulge and its structural parameters (see S11 for details). We use the bulge-total ratio ($B/T$) computed from the r-band image and the magnitudes of the bulge and disc components, that are given as rest-frame, extinction, and $K$ corrected. Extinction values are taken from the SDSS pipeline, while $K$ correction was computed using version 4.2 of k-correct Blanton & Roweis (2007). We use the criterion $P_{PS} < 0.32$ (as suggested by S11) to select robust subsamples of genuine bulge plus disc systems, where $P_{PS}$ is the probability that a two-component model is not statistically needed to fit the galaxy image.

2.3. The galaxy sample

We construct the master catalogue from the MPA-JHU SFR and $M_*$ catalogue, after removing duplicates and objects with no SFR or $M_*$ estimates, and cross-correlate it with the S11 catalogue. Less than 2% of galaxies do not have a SFR or a stellar mass estimate because of low quality photometric or spectroscopic data. In the cross-correlation between the master and the S11 catalogues, only 8% of galaxies are lost owing to minor
differences in the selection criteria applied in S11. To limit our analysis to a local volume galaxy sample with relatively high spectroscopic completeness, we select galaxies that satisfy the following criteria: $0.02 < z < 0.1$, $\log M_\star \geq 9.0 \, M_\odot$, no AGN as identified in the MPA-JHU catalogue, and a good estimate of $z$ and SFR.

Our selection criteria lead to a final galaxy sample of 265,000 galaxies, $S_{\text{ALL}}$. In the bottom panel of Fig. 1 we show how galaxies in our $S_{\text{ALL}}$ sample populate the Log SFR – Log $M_\star$ plane. In the upper panels we show the distribution of the SFR of galaxies in three bins of stellar mass to better visualise the typical bimodal distribution and its dependency on stellar mass. The thick solid line and error bars in the bottom panel of Fig. 1 indicate the position of the MS of SFGs and its $1\sigma$ scatter, respectively. Following the example of Renzini & Peng (2015), the MS and its scatter are computed as the mode and dispersion of the SFR distribution in several stellar mass bins. We divide the sample in stellar mass bins of 0.2 dex in the range $9.0 \leq \log (M_\star/M_\odot) \leq 11.0$. In each bin, we fit with a Gaussian to the right side of SFR distribution (see, as an example, the red fits in the upper panels of Fig. 1), to avoid shift in the peak value caused by the green valley population. We did not compute the MS values for masses $M_\star > 10^{11} \, M_\odot$ since in this range the distribution is significantly non–Gaussian (Erfanianfar et al. 2016; Whitaker et al. 2012) and cannot be easily disentangled from the tail of the quiescent distribution. The mean ($\mu$) and sigma ($\sigma$) values of the Gaussian fit are used as MS and scatter in the midpoint of each stellar mass bin and are summarised in Table 1.

Table 1. Main sequence SFRs (first column) and dispersion values (second column) in bins of stellar mass, in log $(M/M_\odot)$ (third column).

<table>
<thead>
<tr>
<th>Log SFR$<em>{\text{MS}}$ [M$</em>\odot$ yr$^{-1}$]</th>
<th>$\sigma_{\text{MS}}$ [M$_\odot$ yr$^{-1}$]</th>
<th>Log $M_\star$ [M$_\odot$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>$-0.48$</td>
<td>$0.24$</td>
<td>$9.0:9.2$</td>
</tr>
<tr>
<td>$-0.34$</td>
<td>$0.25$</td>
<td>$9.2:9.4$</td>
</tr>
<tr>
<td>$-0.21$</td>
<td>$0.29$</td>
<td>$9.4:9.6$</td>
</tr>
<tr>
<td>$-0.07$</td>
<td>$0.26$</td>
<td>$9.6:9.8$</td>
</tr>
<tr>
<td>$0.06$</td>
<td>$0.23$</td>
<td>$9.8:10.0$</td>
</tr>
<tr>
<td>$0.16$</td>
<td>$0.22$</td>
<td>$10.0:10.2$</td>
</tr>
<tr>
<td>$0.26$</td>
<td>$0.25$</td>
<td>$10.2:10.4$</td>
</tr>
<tr>
<td>$0.36$</td>
<td>$0.28$</td>
<td>$10.4:10.6$</td>
</tr>
<tr>
<td>$0.47$</td>
<td>$0.31$</td>
<td>$10.6:10.8$</td>
</tr>
<tr>
<td>$0.50$</td>
<td>$0.37$</td>
<td>$10.8:11.0$</td>
</tr>
</tbody>
</table>
To check for biases introduced by our selection criteria, we study the completeness of our spectroscopic $S_{\text{ALL}}$ sample in the Log $SFR$–Log $M_*$ plane, by comparing it with the parent photometric sample drawn from the SDSS DR7 in the same region, redshift, and stellar mass range ($S_{\text{phot}}$). The stellar masses for $S_{\text{phot}}$ galaxies without spectroscopic data are derived from the $\z$ band absolute magnitude, $M_*$, using the best-fit Log $M_*$–$M_*$ relation obtained for $S_{\text{ALL}}$ (Log($M_*/M_\odot$) = $(-0.42 \pm 0.1)M_\odot + 1.3(\pm0.2)$). On the other hand, obtaining a measure of the SFR without spectroscopic data is not trivial. We verified that the five SDSS broadbands are insufficient to retrieve a reliable measure of the SFR through the SED fitting technique. Also, the addition of the GALEX UV bands does not help in obtaining a reliable dust correction. Indeed, the scatter between the SFR derived in this manner and the SFR derived from the dust-corrected H$\alpha$ emission of the MPA-JHU catalogue exceeds 0.5 dex. To overcome this issue we use the rest-frame $(g - r)$ galaxy colour as a proxy for star formation activity.

The left panel of Fig. 2 shows the $(g - r)$–Log $M_*$ plane with respect to $S_{\text{phot}}$. The completeness in each bin is estimated as the percentage of $S_{\text{phot}}$ galaxies that are also in the $S_{\text{ALL}}$ sample in the same bin. Completeness is below 50% for $10^{8.0} < M_*/M_\odot < 10^{10.0} M_\odot$. In this stellar mass range it is larger for blue, SFGs than for passive, redder galaxies because of the presence of strong emission lines. For $M_*>10^{10.0} M_\odot$, the completeness is larger for redder galaxies, most likely owing to the strong stellar continuum. To obtain the completeness in the Log $SFR$–Log $M_*$ plane we proceed as follows. For every galaxy we get the completeness value by its $(g - r)$ colour and stellar mass (left panel). We then compute the completeness in a given bin of the Log $SFR$–Log $M_*$ as the average completeness over all galaxies in that bin. The result is shown in the right panel of Fig. 2. Completeness varies between 5% and ~20% for galaxies with $M_* < 10^{9.5} M_\odot$, where it is larger for blue, SFGs owing to the presence of strong emission lines. For stellar masses in $10^{8.5-10.0} M_\odot$, the completeness of the spectroscopic catalogue reaches 40% on the MS and in its upper envelope, while it decreases to 20% for passive galaxies. For galaxies with $M_* > 10^{10} M_\odot$, completeness is always higher than 60%, reaches values of ~80% on the MS, and is even larger in the passive region with $M_* \sim 10^{10.5 - 11.0} M_\odot$, where galaxies are characterised by a strong continuum.

2.4. Bulge/disc decomposition reliability: comparison with BUDDA and Galaxy Zoo

To check the reliability of the S11 $B/T$ classification, we compare it with different morphological classifications, in particular, BUDDA (de Souza et al. 2004, Bulge/disc Decomposition Analysis) and Galaxy Zoo (Lintott et al. 2008). Both classifications take the presence of bars into account. Thus, this comparison is particularly interesting to understand how the presence of a bar can bias the S11 $B/T$ estimate.

BUDDA is a FORTRAN code that performs multicomponent decomposition of galaxies. Bulges are fitted with Sérsic profiles and discs are fitted with exponentials. Unlike in GIM2D, in addition to bulge and disc, bars are also modelled with a Sérsic profile. We make use of the public catalogue of structural parameters presented in Gadotti (2009, G09 hereafter), where the BUDDA code has been applied to a sample of 946 spectroscopically confirmed, nearly face-on galaxies, in the range $0.02 \leq z \leq 0.07$ and $M_* > 10^{10} M_\odot$. The final sample of G09 is clean and optimal for bulge/disc decomposition as the quality of each image has been inspected by eye and the redshift range is low. The S11 and G09 catalogues have 910 galaxies in common (correlation radius $r = 3''$). We compare the $B/T$ ratios of S11 ($B/T_{\text{GIM2D}}$) with the G09 values ($B/T_{\text{BUDDA}}$). Both $B/T$ values have been computed from the $r$-band images. Results are shown in Fig. 3. The red stars are the median values of the whole sample in bins of 0.1 in $B/T$ and the errors are computed as the standard deviation in each bin. We find an overall agreement between the two methods at least below $B/T \sim 0.6$. GIM2D tends to find slightly higher $B/T$s with respect to BUDDA. The blue triangles indicate the subsample of galaxies that are classified as “barred” in BUDDA, while the black circles indicate the “unbarred” subsample. A very good agreement in $B/T_{\text{BUDDA}}$ and $B/T_{\text{GIM2D}}$ is found for unbarred galaxies, while for barred galaxies, GIM2D

Fig. 2. Completeness in the $(g - r)$–Log $M_*$ plane (left panel) and Log SFR–Log $M_*$ plane (right panel) of the spectroscopic $S_{\text{ALL}}$ sample with respect to the parent photometric $S_{\text{phot}}$ sample.
tends to estimate higher values of the $B/T$ of almost double at $B/T < 0.1$ and 20–30% higher at larger $B/T$s. Despite this, the overall effect is not dramatic as $B/T_{GIM2D}$ for the whole sample (red stars) does not increase more than 25% because of the inclusion of barred galaxies. This is because of their relatively low percentage, ~30%. Above the $B/T \sim 0.6$ threshold, $B/T_{GIM2D}$ tends to flatten to an average value of ~0.7. This is consistent with the tendency of GIM2D to find an overabundance of small discs in spheroidal galaxies, as pointed out in S11.

We compare GIM2D with the second release of Galaxy Zoo (Lintott et al. 2008), which is a project aimed at classifying “bye-eye” the morphology of galaxies in the SDSS Main Galaxy Sample (Strauss et al. 2002). The catalogue provides morphological classification only for ~50% of the parent photometric sample drawn from the SDSS. The remaining half of the galaxy sample is classified with uncertain morphology. In the second release (GZ2; Willett et al. 2013) ellipticals are classified as round, cigar-like, or in-between. Spirals are classified in four classes as a function of the bulge prominence: Sa if they have dominant bulge, Sb for obvious bulges, Sc if the bulge is just noticeable, and Sd if there is no bulge. In addition, spirals are also divided into barred and not-barred categories. Since edge-on spirals have separate morphological classes in GZ2, we restrict this analysis to galaxies that, in S11, have a disc inclination angle that is smaller than 70° (where $i = 90^\circ$ for an edge-on disc). In Fig. 4, we show the $B/T$ distribution of each subcategory, which are identified using the $gz2class$ final classification in GZ2.1 The GZ2 ellipticals, which are considered as a whole regardless of the shape, are characterised by a $B/T$ distribution peaking at $B/T \sim 1$ and with a second peak at $B/T \sim 0.6$. We also observe a third, much less significant peak at $B/T$ of 0. Approximately 60% of GZ2 ellipticals with $B/T < 0.8$ have $P_{PS} \leq 0.32$, thus making the disc component statistically significant. These galaxies could be S0 galaxies that are visually misclassified as ellipticals (Willett et al. 2013; Huertas-Company et al. 2011). Not surprisingly, for GZ2 Sa galaxies, i.e. consistent with an intermediate morphology template (bulge-dominated spiral), the $B/T$ distribution is wide with three peaks, at $B/T$ of ~0.5, and 1, respectively. However, we point out that Sa galaxies account only for less than ~1% of the GZ2 sample. For Sb, Sc, and Sd the $B/T$ distributions reveal a very good agreement between GZ2 and GIM2D classification. Also, it is clear from Fig. 4 that the presence of a bar (red dashed line histograms) results in an overestimate of the GIM2D $B/T$, in particular for Sc and Sd galaxies.

We point out that neither G09 or GZ2 catalogues are suitable for our analysis. While BUDDA does not provide the required statistics, in GZ2, the visual classification is available only for half of the parent galaxy subsample drawn from the SDSS, leading to a high level of incompleteness. Only S11 simultaneously provides the required statistics and completeness.

The drawback of using S11 is the uncertainty of bulge/disc decomposition at relatively high values of $B/T$. Indeed, the comparison with BUDDA and GZ2 shows that S11 find an overabundance of double component systems among galaxies that are classified as pure spheroidal by BUDDA and by the visual classification. Cheung et al. (2013) suggest that among galaxies with $B/T > 0.5$ only those with $P_{PS} \leq 0.32$ have a reliable the bulge/disc decomposition. However, such a drastic cut would imply selecting only half of the S11 sample at $B/T > 0.5$, leading to significant selection effects in our analysis. To overcome this problem, we adopt the following approach. When measuring the mean $B/T$ in the Log SFR – Log $M_*$ plane, we use a weighted mean, where the weights are based on the errors provided by the

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1 Alternatively, a similar comparison can be carried out using the vote fractions instead of the $gz2class$ parameter, but this leads to a decrease in the number of sources for the comparison, especially in the case of intermediate-morphology galaxies.
S11 catalogue for $B/T$. Including this error in the weighted mean allows us to take into account the uncertainty due to low S/N and resolution issues. This approach also allows us to propagate the uncertainty of the morphological classification throughout our analysis. As an alternative approach, and to verify the robustness of our results, we create a reference sample ($S_{eq}$) in which we keep the $B/T$ as given by S11 for all galaxies with $P_{PS} \leq 0.32$. Instead, galaxies that have $P_{PS} > 0.32$ are considered as pure disks ($B/T = 0$) when $B/T \leq 0.5$ or as pure spheroids ($B/T = 1$) when $B/T > 0.5$. The results based on $S_{eq}$ are shown for comparison in Appendix A. When analysing the colours of the individual components in the Log SFR–Log $M_*$ plane, we use a sample with a robust double component classification by imposing the cut at $P_{PS} < 0.32$.

3. Results

In the following sections, we study the galaxy $B/T$ and bulge/disc colours in the Log SFR–Log $M_*$ plane. The purpose of this analysis is to better understand the drivers of the MS scatter, and the main differences in galaxy properties between SF and passive galaxies.

3.1. The $B/T$ across the Log SFR–Log $M_*$ plane

In Fig. 5 we show the distribution of the $B/T$ values for $S_{ALL}$ in the Log SFR–Log $M_*$ plane (left panel). Each bin is colour-coded according to the weighted average of the $B/T$s in that bin. The width of each bin is 0.2 in both Log $M_*$ and Log SFR to account for the average errors with a minimum of 20 galaxies per bin. The white solid line is the MS and the error bars show the dispersion around it (Table 1).

Figure 5 confirms the result already obtained by Wuyts et al. (2011): the MS is populated mainly by disc-dominated galaxies and the quiescent region by bulge-dominated systems. Intermediate $B/T$ values are found in the green valley and the upper envelope of the MS. We also confirm previous results that the mean $B/T$ on the MS increases as a function of the stellar mass, going from 0.16 at $10.2 < \log M_* < 10.4$, to 0.21 at $10.4 < \log M_* < 10.6$, 0.26 at $10.6 < \log M_* < 10.8$, and 0.32 at $10.8 < \log M_* < 11.0$. This implies that the MS above $\log M_* = 10.2$ begins to be populated by double-component galaxies, which is consistent with previous findings (Lang et al. 2014; Bluck et al. 2014; Erfanianfar et al. 2016). When approaching the quiescence region at $\gtrsim 1$ dex below the MS, the $B/T$ further increases to reach an average value between $0.6–0.7$ for galaxies with $\log M_* > 9.6$. For less massive galaxies, the average $B/T$ in the passive region is in the range $0.3–0.5$. However, this is the region most affected by completeness issues as shown in Fig. 2. Thus, it is very likely that a strong selection effect in favour of emission line galaxies is biasing the mean value of the $B/T$ in the weighted mean.

A deeper insight is obtained from a careful analysis of the relation between the residuals around the MS, $\Delta_{MS} = \log SFR_{MS} – \log SFR_{gal}$ (where $SFR_{MS}$ is the SFR on the MS and $SFR_{gal}$ is the galaxy SFR), and the mean $B/T$ in different stellar mass bins as shown in the right panel of Fig. 5. Contrary to Wuyts et al. (2011), who find a roughly constant value of the Sérsic index $n \sim 1$ around the MS, we observe that the $B/T-\Delta_{MS}$ relation exhibits a parabola-like shape within $3\sigma$ from the MS with the MS coinciding with the lowest $B/T$s at any stellar mass. In contrast to previous results (Wuyts et al. 2011; Cheung et al. 2012), we find that star-forming galaxies with a bulge-dominated morphology are not outliers in the diagram but are just populating the upper envelope tail of the MS. To further investigate how galaxies with different morphologies populate the plane, we study the distribution in the entire stellar mass range of the $B/T$ for galaxies above the MS ($>2\sigma$), within the MS ($\pm 2\sigma$), in the lower envelope of the MS (2–3\sigma below) and in the passive region (3\sigma below). As shown in Fig. 6, the MS (black line) is dominated by pure disc galaxies, in which $\sim 60\%$ of the population have $B/T < 0.2$. The large error associated with MS galaxies with $B/T \lesssim 0.2$ reflects the increase of the $B/T$ along the MS. In the upper envelope of the MS (blue stars), disc galaxies make up only $\sim 30\%$ of the entire galaxy sample, favouring a population of intermediate $B/T$s. Similarly, $\sim 35\%$ of galaxies are pure discs in the lower envelope of the MS. Galaxies in the lower
and upper envelopes of the MS share the same distribution of galaxy B/T. Among passive galaxies (red triangles), $\approx 70\%$ have $B/T \leq 0.8$. As discussed earlier, this fraction is contaminated by true spheroidal galaxies for which GIM2D finds a spurious disc. Nevertheless, there is a significant population of passive galaxies with a secure bulge plus disc morphology, as $\approx 45\%$ of all passive galaxies have $B/T < 0.8$ and $P_{PS} < 0.32$. Also, the fraction of passive galaxies with $B/T < 0.2$ is negligible, indicating that passive pure discs, if at all present, are outliers of the galaxy population.

These trends of $B/T$ in the Log SFR–Log $M_*$ are also confirmed using the S$_{ap}$ sample (see Appendix A). As an additional test, we repeat the analysis by limiting the sample to galaxies with high S/N photometric data and secure S11 classification, by selecting galaxies with a disc scale length larger than 2 arcsec to avoid resolution issues (as in Cheung et al. 2013). All the tests confirm the results presented in Fig. 5.

3.2. The effect of bars

In Sect. 2.4 we conclude that S11 and G09 show good agreement for $B/T < 0.6$ and that the presence of a bar leads to an overestimation of the S11 $B/T$ of $10\%$–$25\%$. However, the gradient observed from the peak of the MS towards the upper and lower envelopes of the relation leads to an increase of the mean $B/T$ by a factor $\sim 1.5$, depending on the stellar mass bin. Thus, the increase of the mean $B/T$ across the MS is much larger than the overestimation of the $B/T$ due to the bars. Nevertheless, the bars could be preferentially located in certain regions of the Log SFR – Log $M_*$ plane, thus affecting the average $B/T$ value of that region.

To check this, we perform the same analysis as in Fig. 5 on the G09 sample (see left panel of Fig. 7). We observe a $\sim 25\%$ milder increase of the mean $B/T$ along the MS with respect to the result of Fig. 5 (mean $B/T$ value of 0.13, 0.19, and 0.23 at stellar masses of $10^{10.5}$–$10^{11.0}$, $10^{10.4}$–$10^{10.8}$, and $10^{10.8}$–$10^{11.2}$ $M_{\odot}$, respectively), which is consistent with the overall effect of overestimation of the S11 $B/T$ from the inclusion of barred galaxies. Because of the relatively small size of the G09 sample, the upper and lower envelopes of the MS are poorly populated. Thus, we limit the analysis of the mean $B/T$ as a function of the distance from the MS to two stellar mass bins, above and below the median mass of the sample ($10^{10.25}$ $M_{\odot}$). We perform the analysis for the whole G09 sample and for the “unbarred” G09 sample (deprived of barred galaxies). The right panel of Fig. 7 shows the mean $B/T$ as a function of $\Delta_{MS}$ for the two G09 samples in comparison with the mean relation obtained in the same stellar mass bins in S11. The error bars are estimated via bootstrapping technique. We find a perfect match of all relations in the MS region. This indicates that bars do not play a crucial role in the gradient of $B/T$ across the MS. Only in the quiescence region, as expected, the S11 relation shows lower mean $B/T$ with respect to G09 because of the underestimation of S11 $B/T$ for spheroidal galaxies (Fig. 3). In addition the barred galaxy sample of G09 shows that the $B/T$–$\Delta_{MS}$ for barred galaxies exhibits the same parabola-like shape. Thus, barred galaxies follow the same trend. This suggests that the presence of a bar on average plays a second order effect with respect to the galaxy morphology.

3.3. Velocity dispersion in the Log SFR–Log $M_*$ plane

To investigate the similarities and differences of the bulgy galaxy population in the upper and lower limit of the MS, we use the bulge velocity dispersion, $\sigma$, and the SDSS concentration parameter, $R_{90}/R_{50}$. The parameters $\sigma$ and $R_{90}/R_{50}$ are often used to discriminate between classical and pseudo-bulges (see e.g. G09). Classical bulges resemble spheroidal galaxies for their colours and scaling relations. Pseudo-bulges are, instead, outliers in the Kormendy relation (Kormendy 1977, G09). They tend to be blue and with low velocity dispersion with a Sérsic index close to $\sim 2$.

To retrieve the bulge velocity dispersion, we use the estimate of the stellar velocity dispersion provided by the MPA-MJU catalogue, which is measured by fitting the stellar absorption features of the SDSS galaxy spectra. The aperture velocity dispersion, $\sigma_{ap}$, is computed inside the SDSS fibre, characterised by a 3 arcsec diameter. Such an aperture samples different galaxy parts as a function of redshift, galaxy size, and morphology. In order to sample the bulge alone, we select galaxies with $B/T \geq 0.5$ and galaxies with $R_{PS} \leq 0.32$ if $B/T < 0.5$. In order to exclude contamination by disc rotation, we limit our analysis to nearly face-on galaxies, with disc inclination $i < 30^\circ$.

Given the spectral resolution of the SDSS spectrograph and typical S/N values, velocity dispersion estimates smaller than $\sim 70$ km s$^{-1}$ are not reliable. Thus, to all galaxies with $\sigma_{ap} < 70$ km s$^{-1}$, we assign a fixed upper limit of $\sigma_{ap} > 70$ km s$^{-1}$ with an error of $\pm 70$ km s$^{-1}$ to be used for the weight calculation in the weighted mean. We also exclude galaxies with $\sigma_{ap} > 420$ km s$^{-1}$ (as the SDSS template spectra are convolved to a maximum sigma of 420 km s$^{-1}$) and with low S/N continuum ($<3$). We

\footnote{The disc inclination angle is $0^\circ$ for face-on galaxies and $90^\circ$ for edge-on galaxies.}
apply the aperture correction of Jorgensen et al. (1995) to $\sigma_{ap}$ to compute $\sigma_e$: the velocity dispersion within the effective radii of the galaxy, $r_e$ (that we take from SDSS database). In the redshift range considered here, the average aperture correction is $\sim$14%.

Figure 8 shows the distribution of galaxies in the Log SFR – Log $M_*$ plane colour-coded as a function of the average $\sigma_e$ in each bin. The error bars in Fig. 8 are estimated via a bootstrapping analysis. The behaviour of $\sigma_e$ across and along the MS is qualitatively similar to the $B/T$ ratio. At a fixed stellar mass, $\sigma_e$ has its minimum on the MS, increases towards the upper and lower envelopes of the MS, and reaches its maximum in the quiescence region. Also, the velocity dispersion of MS galaxies increases for increasing stellar mass along the MS, resembling the $B/T$ behaviour. We point out that the exclusion of
pure-disc galaxies, which populate the core of the MS, naturally leads to a flatter parabola-like shape for the \( \sigma_c - \Delta_{\text{MS}} \) distribution as a function of the mass.

The same trend in Fig. 8 is also observed for the concentration parameter, which is one of the most reliable discriminant (G09) between bulges and pseudo-bulges at given B/T (see Appendix B). In the lower and upper envelopes of the MS the mean value of \( R_{b0}/R_{s0} \approx 2.5 \) is consistent with the mean for classical bulges with low values of D4000, as estimated in the same mass range by G09 (see Fig. 20 of G09). Low values of the D4000 index would indicate a relatively young age of the stellar population. Values of \( R_{b0}/R_{s0} \approx 2 \), which are consistent with pseudo-bulges, are found only in the core of the MS. In the quiescence region, the mean \( R_{b0}/R_{s0} \approx 3 \) is consistent with classical bulges with high values of D4000, i.e. older stellar populations. Thus, we conclude that lower and upper envelopes of the MS share the same B/T, bulge velocity dispersion, and concentration parameter distributions. Both are populated by intermediate morphology galaxies with classical bulges. The similarity of these distributions could suggest that the scatter around the MS is characterised by different evolutionary stages of the same galaxy population, while the MS itself is mainly populated by pure disc galaxies.

### 3.4. Bulge and disc colours in the Log SFR – Log \( M_\star \) plane

The SDSS spectroscopic dataset does not provide any spatial information. Thus to understand whether there is a connection between the SF activity of the individual galaxy components (bulge and disc) and the star formation of the galaxy as a whole, we use the colour of bulges and discs as a proxy of their SFR, while the total SFR of the galaxy is taken from Brinchmann et al. (2004).

For this purpose we limit this analysis to the \( S_{\text{ALL}} \) sample with secure double morphological component, applying the cut at \( P_{\text{PS}} \leq 0.32 \).

In Fig. 9 we show the \((g - r)\) colour of the galaxy (upper left panels), disc (upper central panels), and bulge (upper right panels) in the Log SFR – Log \( M_\star \) plane. The upper panels are colour-coded as a function of the galaxy or galaxy component colour. The colour in each bin is obtained with a weighted mean. The bottom panels show the dependence of the mean colour of the whole galaxy (left panel), disc (central panel) and bulge (right panel) on the distance from the MS.

The galaxy and disc colours follow similar trends where at any stellar mass bin, they anti-correlate with the distance from the MS, getting progressively bluer from the quiescence region to the upper envelope of the MS. The anti-correlation is steeper for the whole galaxy colour than for the disc component. In both cases, the relation flattens progressively towards highest stellar mass bin. The bulge colour shows a different behaviour instead. Up to \( \sim 10^{10} \ M_\odot \), the bulge colour also anti-correlates with the distance from the MS, getting bluer from the passive region to the upper envelope of the MS. In this stellar mass range bulges above the MS are as blue as their discs. However, above \( \sim 10^{10} \ M_\odot \), the relation reverses with the bulge colour getting redder from the passive region up to the MS. After reaching its reddest value, the bulge turns slightly bluer towards the upper envelope of the MS. However, the bulge colour is always redder than the disc even in the upper envelope of the MS. For \( M > 10^{11} \ M_\odot \), bulges are always characterised by red colours independent of their position on the Log SFR – Log \( M_\star \) plane.

In order to check the bias from dust obscuration, we analyse the average Balmer decrement computed for galaxies with \( S/N > 8 \) in both H\( \alpha \) and H\( \beta \) (Fig. 10). Dust obscuration is
not significant for galaxies with stellar masses below $10^{10} \, M_\odot$. Hence the trends in colours reflect a trend in SF activity. Very massive ($\gtrsim 10^{10.5} \, M_\odot$) SFGs in the upper MS envelope exhibit the highest values of Balmer decrement, pointing to a very high level of dust obscuration. This, in turn, would suggest that the flattening of the colour gradients across the MS at increasing stellar mass in all panels of Fig. 9 could be due to an increasing level of dust obscuration towards the upper envelope of the MS.

We also point out that above $10^{10.5} \, M_\odot$, the very red colour of bulges in the green valley and on the MS cannot be explained by a large level of dust obscuration due to the low average Balmer decrement. We conclude that the bulges in massive MS and green valley galaxies are intrinsically redder than their counterparts in the passive region. This implies that such bulges might be older or more metal rich with respect to bulges in the passive region. In any case, this suggests different evolutionary paths for bulges on the MS, and in the passive region.

The observed trends of the bulge and disc colours at fixed stellar mass with the distance from the MS are also preserved when considering all galaxies in $S_{\text{ALL}}$ with $0.2 \leq B/T \leq 0.8$.

4. Discussion and conclusions

We used the bulge-disc decomposition of Simard et al. (2011) to study the link between the structural parameters of galaxies and their location in the $\log SFR - \log M_\star$ plane. We use the colour of bulges and discs to understand how these individual components influence the evolution of the galaxy as a whole. Our sample is drawn from the spectroscopic sample of SDSS DR7, in the redshift range $0.02 < z < 0.1$ and $M_\star > 10^9 \, M_\odot$, and the main findings are as follows:

- The MS of SFGs is populated by galaxies that, at every stellar mass, have the lowest $B/T$s. At low stellar masses, $M_\star < 10^{10.2} \, M_\odot$, MS galaxies are pure discs, while the prominence of the bulge component increases with increasing stellar mass for more massive galaxies.

- The upper and lower envelopes of the MS are populated by galaxies characterised by intermediate $B/T$s. This is robust against different decompositions and independent of the modelling of the bar component.

- Bulges in the upper envelope of the MS are characterised by blue colours at low stellar masses, or red colours and large dust obscuration at high stellar masses. This is consistent with high SF activity in the central region of the galaxy.

- The study of the mean bulge velocity dispersion and galaxy concentration parameter indicates that galaxies populating the upper and lower envelopes of the MS are structurally similar. The values of the concentration parameter, in particular, suggest that these galaxies are characterised by classical bulges rather than pseudo-bulges.

- In the low mass regime, $M_\star < 10^{10} \, M_\odot$, disc and bulge colours show a similar behaviour at fixed stellar mass, becoming progressively redder from the upper envelope of the MS to the passive region. Nevertheless, the reddening of the bulge component is steeper than for discs. Discs and bulges become bluer for $M_\star > 10^{10} \, M_\odot$ when going form the MS towards its upper envelope, despite a less pronounced total variation of colours. The trend of the bulge colour reverses in the lower envelope of the MS, where bulges are redder than in the passive region.

- The population of passive galaxies is largely made of genuine bulge plus disc systems (at least 45%).

Our results point to a tight link between the distribution of galaxies around the MS and their structural parameters. Contrary to Wuyts et al. (2011) and Cheung et al. (2012), we find that blue bulgy SFGs are not outliers in the distribution of galaxies on the MS. They occupy the upper tail of the MS distribution, leading to a progressive increase in $B/T$ above the MS. In particular, Wuyts et al. (2011) find that the galaxy Sérsic index remains $\sim 1$ in the region of the MS. We find, instead, that the MS location corresponds to the lowest value of the $B/T$ at any mass. This could be due to the inability of a single Sérsic model (used in Wuyts et al. 2011) to capture small bulges in disc-dominated galaxies. In agreement with previous results, we find a large percentage of bulge-dominated systems in the high-mass SF region, where the MS scatter tends to increase (i.e. Lang et al. 2014; Whitaker et al. 2014; Erfanianfar et al. 2016). However, the $B/T - \Delta_{\text{MS}}$ relation at fixed stellar mass holds in the stellar mass range $10^9 - 10^{11} \, M_\odot$, and seems to flatten when the MS itself tends to disappear. We also investigate how the presence of a bar influences the scatter around the MS. Overall we conclude that bars do not affect the scatter of the MS or the $B/T - \Delta_{\text{MS}}$ relation. In fact, this relation holds for both the unbarred and barred GO9 subsamples. This suggests, partly in disagreement with the findings of Guo et al. (2015a), that the predominance of the bulge in a galaxy is intrinsically related to the location of a galaxy around the MS, and this is true at any stellar mass independent of the presence of a bar. Nevertheless, we do not exclude the possibility that a large percentage of bars among very massive SFGs can contribute to an increase in the scatter of the MS, as suggested by Guo et al. (2015a).

Our study shows that the location of galaxies in the $\log SFR - \log M_\star$ plane and, in particular, with respect to the MS of SFGs, is determined by the combined activity (or inactivity) of the individual galaxy components. This was previously suggested by Abramson et al. (2014), who have pointed out that the MS becomes roughly linear if one assumes that the SF activity takes place only in the disc rather than in the entire galaxy. However, our results suggest otherwise. The effect of
normalising the SF activity to the disc mass leads to a completely different scatter of the sSFR – $M_\star$ relation. Here we present the vertical dotted line. Here Fig. 11. B/T ratio, as a function of the distance from the MS, represented by the vertical dotted line. Here $\Delta_{\text{MS}}$ was computed from the sSFR normalised to $M_{\text{disc}}$. Different bins of stellar mass are indicated with different colours.

In Fig. 11, we show the relation between B/T and distance from the MS computed as the difference between the sSFR$_{\text{disc}}$ of galaxies and sSFR$_{\text{disc}}$ of galaxies in the MS. This is carried out for galaxies that are pure discs or have a secure bulge plus disc structure. The B/T trends in Fig. 11 are similar to those in Fig. 5; there is a steep increase of the mean $B/T$ in the upper envelope of the MS due to the displacement of bulgy SFGs above the sSFR$_{\text{disc}}$–$M_\star$ relation. We underline that the $B/T$ in the passive region is lower than that observed in Fig. 5, as here pure spheroidal galaxies are excluded from the sample. We find that the overall effect of neglecting the SF activity of the bulge component is to increase the scatter of the sSFR – $M_\star$ relation.

It has been proposed that minor mergers or violent disc instabilities could favour the flow of cold gas from the disc towards the galaxy centre and, thus, cause an overall compaction of the system. The high SF activity in the centre would lead to a compact, bulgy, star-forming object (Dekel & Burkert 2013; Zolotov et al. 2015). Tacchella et al. (2015) study the evolution of galaxies in this scenario using zoom-in simulations and they find that galaxies at high redshift undergo subsequent phases of compaction and depletion of the gas reservoir, which ultimately leads to quenching. The compaction phase causes high SF in the central region of galaxies, and hence could favour bulge growth. Thus, $M_\text{gal}$ is then followed by $M_\text{bulge}$, then by $M_\text{disc}$, and finally by $M_\star$ exhaustion. Such subsequent phases can move a galaxy across the MS: towards the upper envelope during compaction and towards the lower envelope during depletion. Complete quiescence can be reached once the bulge reaches a given mass threshold corresponding to no more inflows in massive halos or AGN feedback. Our findings on the $B/T$ in the Log $SFR$–Log $M_\star$ plane and bulge/disc colours can be related to such a scenario and are also consistent with the observed gradient of molecular and atomic gas fraction across the MS, as seen by Saintonge et al. (2016).

Integral field spectroscopy surveys, such as MaNGA (Bundy et al. 2015) and CALIFA (Sánchez et al. 2012), will greatly advance our understanding of the evolution of individual galaxy components, and how they impact the galaxy as a whole. This will help us draw a better picture of the quenching mechanism, and understand the CSFH at any epoch.

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References
Appendix A: Results with $S_{\text{ref}}$ sample

Here we show the result of the analysis of the mean $B/T$ in the Log $SFR$–Log $M_*$ plane for the $S_{\text{ref}}$ sample. We recall that the $S_{\text{ref}}$ sample is built from the $S_{\text{all}}$ sample by keeping the $B/T$ as given by S11 for all galaxies with $P_{PS} \leq 0.32$, while the remaining galaxies are considered pure discs if they have $B/T \leq 0.5$ or pure spheroidals if they have $B/T > 0.5$. We show the results in Fig. A.1. The trends of the $B/T$ in the Log $SFR$–Log $M_*$ plane are remarkably consistent with those of Fig. 5 for the $S_{\text{ALL}}$ sample. We still observe the minimum of the $B/T$ distribution for galaxies that, at each stellar mass bin, are located on the MS. As expected, the increase of the $B/T$ in the passive region is more significant for $S_{\text{ref}}$ than for the $S_{\text{ALL}}$, as only the ~50% of galaxies with $B/T > 0.5$ have $P_{PS} \leq 0.32$. This confirms that our results are robust against the S11 decomposition.

Fig. A.1. Same as Fig. 5, but for $S_{\text{ref}}$ sample of galaxies. Left panel: Log $SFR$–Log $M_*$ plane colour–coded according to the weighted average $B/T$ in the bin. The white line represents the location of the MS of SFGs, and the error bars show its dispersion. Right panel: $B/T$ ratio as a function of $\Delta_{\text{MS}}$ (distance from the MS) in different stellar mass bins.
Appendix B: Concentration in the Log SFR – Log $M_\star$ plane: $R_{90}/R_{50}$

We show here the behaviour of the concentration index ($R_{90}/R_{50}$) in the Log SFR – Log $M_\star$ plane in the $S_{\text{ALL}}$ sample. The values of $R_{50}$ and $R_{90}$ are taken from the SDSS DR7 catalogues. Figure B.1 shows that the concentration index is minimum on the MS, and it increases both towards larger and smaller SFRs. Bulges in the upper and lower envelopes of the MS are characterised by an average $R_{90}/R_{50} \approx 2.5$ which, according to G09, is the typical concentration index of classical bulges with low values of D4000, which suggests a young age (see Fig. 20 of G09). Classical bulges in the passive region have, on average, a $R_{90}/R_{50}$ of 3, typical of bulges with high values of D4000 suggesting an old stellar population. Pseudobulges are characterised by $R_{90}/R_{50} \approx 2.0$. We conclude that the upper and lower envelopes of the MS are populated by bulgy galaxies with classical bulges with a relatively young population.

![Figure B.1](image-url)

**Fig. B.1.** *Left panel:* Log SFR – Log $M_\star$ plane colour-coded as a function of the weighted average of the $R_{90}/R_{50}$ ratio. The white line represents the location of the MS of SFGs, and the error bars its dispersion. *Right panel:* $R_{90}/R_{50}$ ratio as a function of the distance from the MS ($\Delta \text{MS}$) in different stellar mass bins.