

Brown dwarf disks with ALMA: Evidence for truncated dust disks in Ophiuchus

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ABSTRACT

Context. The study of the properties of disks around young brown dwarfs can provide important clues on the formation of these very low-mass objects and on the possibility of forming planetary systems around them. The presence of warm dusty disks around brown dwarfs is well known, based on near- and mid-infrared studies.

Aims. High angular resolution observations of the cold outer disk are limited; we used ALMA to attempt a first survey of young brown dwarfs in the ρ Oph star-forming region.

Methods. All 17 young brown dwarfs in our sample were observed at 890 μm in the continuum at ~ 0.5 angular resolution. The sensitivity of our observations was chosen to detect $\sim 0.5 M_{\oplus}$ of dust.

Results. We detect continuum emission in 11 disks ($\sim 65\%$ of the total), and the estimated mass of dust in the detected disks ranges from ~ 0.5 to $\sim 6 M_{\oplus}$. These disk masses imply that planet formation around brown dwarfs may be relatively rare and that the supra-Jupiter mass companions found around some brown dwarfs are probably the result of a binary system formation. We find evidence that the two brightest disks in ρ Oph have sharp outer edges at $R \lesssim 25$ AU, in contrast to disks around Taurus brown dwarfs. This difference may suggest that the different environment in ρ Oph may lead to significant differences in disk properties. A comparison of the M_{disk}/M_* ratio for brown dwarf and solar-mass systems also shows a possible deficit of mass in brown dwarfs, which could support the evidence for dynamical truncation of disks in the substellar regime. These findings are still tentative and need to be put on firmer grounds by studying the gaseous disks around brown dwarfs and by performing a more systematic and unbiased survey of the disk population around the more massive stars.

Key words. protoplanetary disks – brown dwarfs – stars: formation – submillimeter: planetary systems

1. Introduction

After decades since the discovery of the first young brown dwarf (BDs; Rebolo et al. 1995) and their disks (Comeron et al. 1998; Natta & Testi 2001; Natta et al. 2002), the formation mechanism of very low-mass objects (below $\sim 0.1 M_{\odot}$) is still controversial. Possibilities range from the collapse of a single low-mass core (Hennebelle & Chabrier 2009), as for the more massive T Tauri stars (TTS), to ejection of low-mass protostellar seeds from multiple stellar systems before accretion terminates (Reipurth & Clarke 2001; Bate 2004, 2009) or from fragmenting circumstellar disks (Stamatellos & Whitworth 2009). A solar-mass core in the vicinity of an OB star may be photoeroded to become a very low-mass object by the time of collapse (Hester et al. 1996; Whitworth & Zinnecker 2004). A variety of formation channels may in fact co-exist and their relative importance may change as a function of mass and the environment. All the formation models account for the presence of circumstellar accretion disks around young BDs, but the current generation of numerical models is still unable to reliably predict how much

mass is retained in the small disks around BDs when they are ejected. A solid expectation is that the ratio of the disk mass over the mass of the central object should drop significantly if the ejection process becomes an important formation channel (Stamatellos & Herczeg 2015). A reliable observational estimate of the (possible) variation of this ratio with the mass of the central object would be a critical test that models would have to compare against.

Knowledge of the disk mass is also important to assess the potential of planet formation around BDs, and, in particular the formation of planetesimals and rocky planets. Infrared spectroscopy of young BDs with disks has shown that in several sources dust processing similar to that observed in more massive disks around young stars has taken place in the disks atmospheres (Apai et al. 2004, 2005; Sterzik et al. 2004). Growth to millimeter and centimeters sizes on the disk midplane, similar to what occurs in TTS disks, has been inferred for few BDs observed with ALMA and CARMA (Ricci et al. 2012, 2013, 2014). All this suggests that the initial steps of the core accretion scenario can indeed occur in BD disks, however, theoretical

Table 1. Sample.

Name	α (2000)	δ (2000)	ST	T_{eff} [K]	A_V [mag]	L_* [L_{\odot}]	M_* [M_{\odot}]	Ref.	Other Names
SONYC-RhoOph-8	16:26:18.58	-24:29:51.8	M7	2900	18.8	0.1	0.1	2	CFHTWIR-Oph16
ISO-Oph023	16:26:18.81	-24:26:10.8	M7	2900	9.7	0.04	0.07	1	CRBR 2317.3-1925
ISO-Oph030	16:26:21.53	-24:26:01.4	M7	2900	4.5	0.07	0.1	1	GY92-5
ISO-Oph032	16:26:21.90	-24:44:40.09	M6.5	2935	0.6	0.03	0.07	1	GY92-3
ISO-Oph033	16:26:22.26	-24:24:07.55	M8	2700	7.7	0.005	0.03	1	GY92-11
ISO-Oph035	16:26:22.96	-24:28:46.1	M6	3000	10.7	0.06	0.1	2	GY15, SONYC-RhoOph-5
CRBR 2322.3-1143	16:26:23.81	-24:18:29.0	M6.5	2935	8.6	0.01	0.07	2	
ISO-Oph042	16:26:27.80	-24:26:42.22	M5	3100	6.2	0.03	0.1	3	GY92-37
GY92-202	16:27:05.98	-24:28:36.3	M7	2900	13.0	0.02	0.06	2	
ISO-Oph102	16:27:06.58	-24:41:49.28	M5	3125	2.2	0.047	0.15	1	GY92-204
ISO-Oph138	16:27:26.22	-24:19:23.46	M7.75	2753	16.4	0.1	0.05	2	SONYC-RhoOph-10, CFHTWIR-Oph78
GY92-264	16:27:26.57	-24:25:54.77	M8	2700	2.2	0.023	0.03	4	
ISO-Oph160	16:27:37.42	-24:17:55.34	M7.5	2800	6.1	0.03	0.06	1	
ISO-Oph164	16:27:38.63	-24:38:39.19	M8	2700	5.1	0.05	0.05	1	GY310, ROXN62
GY92-320	16:27:40.84	-24:29:00.8	M7.75	2753	2.4	0.007	0.04	2	CFHTWIR-Oph 96
ISO-Oph176	16:27:46.29	-24:31:41.2	M7.5	2800	6.9	0.06	0.06	1	GY92-350
ISO-Oph193	16:28:12.7	-24:11:36.08	M6	3000	7.4	0.07	0.11	1	B162812-241138

References. References to stellar parameters: 1: Manara et al. (2015); 2: data from Alves de Oliveira et al. (2012) and references therein (see text); 3: data from Muzic et al. (2012) (see text); 4: Liu et al. (2015).

models of grain growth (Pinilla et al. 2013) in low-mass disks encounter very serious difficulties; this challenges current views of how and when grain growth may occur. Payne & Lodato (2007) estimate that the disks around BDs need to be relatively massive, at least a few Jupiter masses, to enable efficient terrestrial planet formation.

Measuring the mass distribution of disks around a significant sample of young BDs is thus essential to shed light on the BD formation mechanisms and to assess their potential to form planetary systems. In this paper we present the first ALMA observations of an unbiased sample of very low-mass objects in the very young star-forming region ρ Oph.

2. The sample

The sample includes 17 spectrally confirmed ρ Oph BDs with infrared excess, which indicates the presence of a circumstellar disk. The sample includes about half of all the substellar objects with infrared excess confirmed to date in ρ Oph (Natta et al. 2002; Testi et al. 2002; Geers et al. 2011; Alves de Oliveira et al. 2012; Mužić et al. 2012). At the time of the proposal (July 2012, Cycle 1), they were all the spectroscopically confirmed Class II BDs in ρ Oph. No selection based on *Herschel* fluxes or pre-existing (sub)mm observations was applied. It should be noted that an object in ρ Oph is considered a BD if it has spectral type of M6 or later. Nonetheless, given the difficulties in estimating spectral types in highly extincted objects, some objects may or may not be included in the published BD samples, depending on the adopted spectral type determination. Recently, the stellar parameters of a subset (eight objects) of our sample have been re-determined using X-Shooter spectra by Manara et al. (2015), who also provide a detailed discussion of the uncertainties. In two cases, the spectral type has been revised to M5, which is just above the BDs threshold. We kept the objects in our analysis, even if strictly speaking they do not meet our original selection criterion.

In spite of the continuing effort to identify and classify new objects, it is important to stress that we are always dealing with

extinction-limited samples, and not with samples complete down to a given mass sensitivity. Moreover, as mentioned above, the determination of photospheric parameters of ρ Oph objects (for any mass) is very uncertain because of the large extinction, young ages, and uncertainties in the evolutionary tracks (see Manara et al. 2015).

Table 1 summarizes the adopted values of the stellar parameters for our sample objects. For those not in Manara et al. (2015), we estimated the luminosity from the spectral type, extinction, and J magnitude provided by Alves de Oliveira et al. (2012) and Mužić et al. (2012), the effective temperature using the spectral type-temperature scale of Luhman et al. (2003), and the mass by comparison with Baraffe et al. (2008) tracks. The objects range in luminosity between ~ 0.01 and $0.1 L_{\odot}$ and between ~ 0.03 and $0.1 M_{\odot}$ in mass.

3. Observations and results

ALMA observed our sources on April 25 and 26, 2014 with 35 and 36 antennas, respectively. We used the ALMA Band 7 receivers tuned to a frequency of ~ 338 GHz, the total effective bandwidth usable for continuum was approximately 6 GHz and the $^{13}\text{CO}(3-2)$ line was covered in one of the spectral windows of the correlator. Titan was used as flux calibrator, while J1626-2951 and J1625-2527 were used as complex gain calibrators in both sessions. The passband calibrator was J1733-1304 for the first session and J1517-2422 for the second session. Standard calibration was performed by the ESO ALMA Regional Centre, the flux density scale is expected to be accurate within 5%. The total time on source for our targets was three minutes for the majority of the sources; the on-source time was six minutes for six objects: SONYC-RhoOph-8, ISO-Oph032, ISO-Oph138, GY92-264, ISO-Oph164, and GY92-320.

Imaging was performed using natural weighting of the visibilities (see Fig. 1). None of the sources were sufficiently bright to attempt self-calibration. In Table 2 we report in Col. 2 the peak flux and rms measured on the images. The full width at half

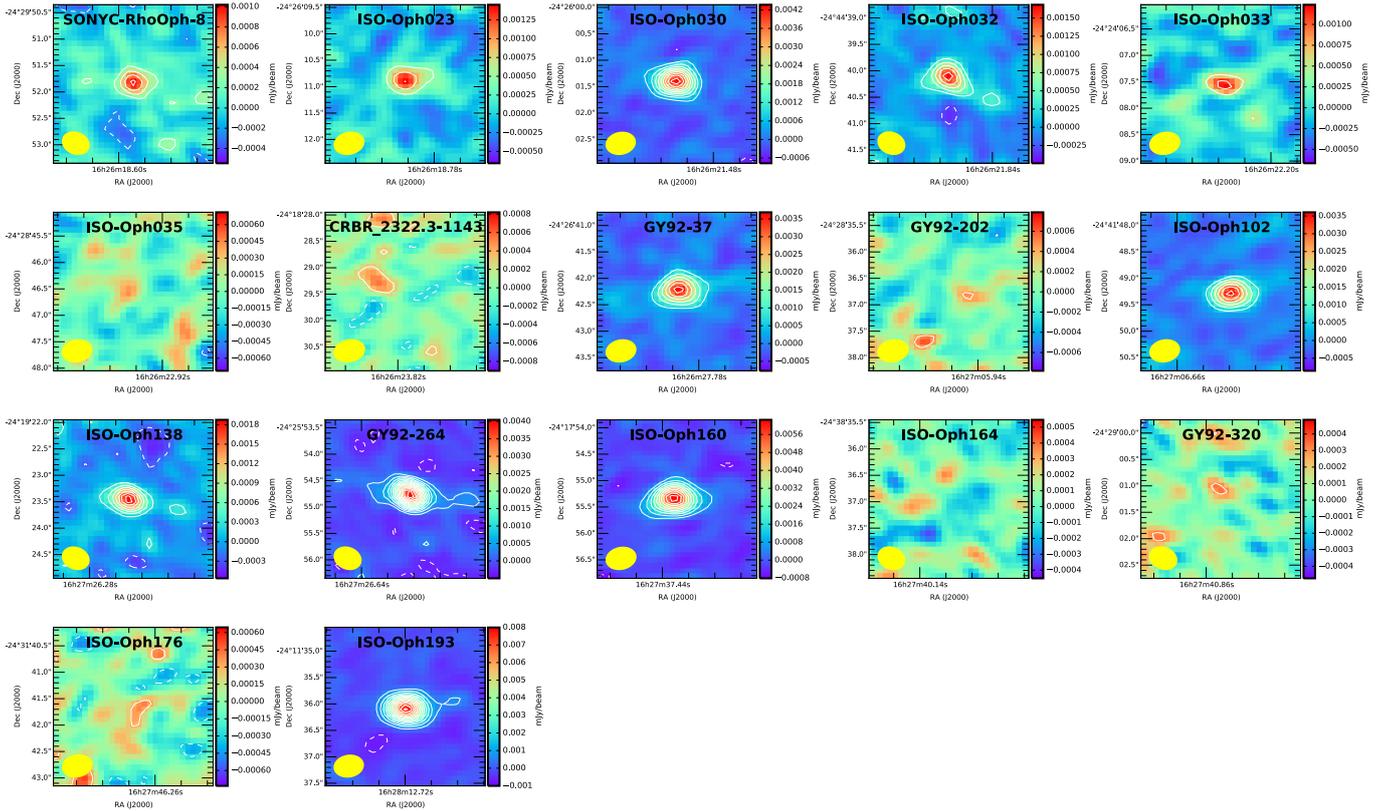


Fig. 1. ALMA Band 7 images of all the observed sources, as labelled in each panel; each panel is $3'' \times 3''$ in size. The synthesized beam full width at half maximum is shown in the lower left corner of each panel; the typical size is $0''.04$. In each panel, contour levels are plot at -3σ (dashed), and every 3σ from 3σ to the maximum.

maximum of the synthesized beam is approximately $0''.5 \times 0''.4$ for all maps. $^{13}\text{CO}(3-2)$ emission was not detected in any of the sources.

The total fluxes reported in Col. 3 of Table 2 for the detected sources are computed using the CASA task `uvmodelfit`: we fitted Gaussian sources to the visibilities of all detected sources except for the three fainter ones, for which we used a point source. The flux upper limits for the non-detected sources correspond to 98% confidence levels and are computed as three times the rms level above the measured flux (assumed null when negative) at the nominal position of the object (see Barenfeld et al. 2016). For three objects the Gaussian fits imply a deconvolved source size with a major axis greater or equal than ~ 0.2 arcsec (see Col. 4 of Table 2).

4. Disk properties

4.1. Disk masses

We determine the mass of dust in the disk from the $890\ \mu\text{m}$ flux using the approximation that the emission is optically thin and isothermal at temperature T ,

$$F_\nu = \frac{1}{D^2} \kappa_\nu B_\nu(T) M_{\text{dust}}, \quad (1)$$

where D is the distance and κ_ν the opacity at the frequency of the observation. This expression has been extensively used in the literature and provides reliable estimates of the product $M_{\text{dust}} \times \kappa_\nu$ from sub-mm and mm fluxes if the emission is optically thin. This is indeed the case for all the BDs studied in

detail so far (see Ricci et al. 2012, 2013, 2014 and Sect. 4.2). In the following, we adopt a dust opacity $\kappa_{890\ \mu\text{m}} = 2\ \text{cm}^2/\text{g}$, as in Ricci et al. (2014), and a temperature that depends on the stellar luminosity as $T = 25 (L_*/L_\odot)^{0.25}$ K (T_A in the following), as suggested by Andrews et al. (2013) in their study of more luminous objects ($L_* \sim 0.1-100 L_\odot$). Recently, the choice of the temperature appropriate to recover the dust mass from a single-wavelength (sub)mm flux in lower-luminosity objects was discussed by van der Plas et al. (2016) and Daemgen et al. (2016). Our motivations for choosing T_A and the uncertainties on M_{dust} due to the uncertainty on T in Eq. (1) (less than a factor 2 in all our objects) are summarized in Appendix A.

Of the 17 ρ Oph BDs observed with ALMA, 11 have a measured dust mass of $0.5-6 M_\oplus$ and 6 have upper limits of $\lesssim 1 M_\oplus$. Assuming a gas-to-dust mass ratio of 100, the total disk mass (gas+dust) is $M_{\text{disk}} \sim 1.5-9 \times 10^{-4} M_\odot$. We do not find more massive disks in our sample and the ratio of the disk-to-star mass is above $\sim 1\%$ only in 4 objects. Our results are more accurate, but they are in broad agreement with the disk masses derived by Alves de Oliveira et al. (2013) from an *Herschel* PACS survey of BDs in ρ Oph. For 12 objects, they were able to determine the disk properties by fitting the observed SEDs with parametric disk models. The mass range they derive is of $0.1-30 M_\oplus$. In particular, when the choice of the mm opacity, which is usually not constrained by the *Herschel* data, is taken into account, masses for 5 of the 6 objects in common agree within a factor of about ± 3 ; in one case (ISO-Oph042, also known as GY92-37) we find a mass a factor of ~ 10 larger, but the uncertainties quoted for this object by Alves de Oliveira et al. (2013) span more than two orders of magnitude (and include our value).

Table 2. Alma data and disk mass.

Name	F_{peak} [mJy/beam]	F_{tot} [mJy]	Size ^a [arcsec]	M_{dust}^b [M_{\oplus}]	M_{disk}^c [$10^{-3} M_{\odot}$]
SONYC-RhoOph-8	1.00 ± 0.08	1.0	<0.2	0.5	0.15
ISO-Oph023	1.30 ± 0.16	1.5	<0.2	1.1	0.33
ISO-Oph030	4.20 ± 0.15	4.8	<0.2	2.7	0.80
ISO-Oph032	1.62 ± 0.1	1.80	<0.2	1.4	0.42
ISO-Oph033	1.2 ± 0.18	1.3	<0.2	2.6	0.77
ISO-Oph035	–	<0.9	–	<0.5	<0.15
CRBR 2322.3-1143	–	<0.6	–	<0.9	<0.27
ISO-Oph042	3.61 ± 0.19	4.2	~0.25	3.5	1.0
GY92-202	–	<0.5	–	<0.5	<0.15
ISO-Oph102	3.66 ± 0.19	3.8	<0.2	2.5	0.75
ISO-Oph138	1.96 ± 0.085	2.0	<0.2	1.0	0.30
GY92-264	3.96 ± 0.09	4.1	<0.2	4.4	1.3
ISO-Oph160	6.13 ± 0.20	7.60	~0.3	6.3	1.9
ISO-Oph164	–	<0.8	–	<0.5	<0.15
GY92-320	–	<0.4	–	<0.7	<0.21
ISO-Oph176	–	<0.5	–	<0.3	<0.09
ISO-Oph193	7.82 ± 0.20	8.7	~0.2	4.8	1.43

Notes. ^(a) Deconvolved major axis; unresolved objects have size <0.2 arcsec. ^(b) Dust mass from the $F_{890 \mu\text{m}}, \kappa_{890 \mu\text{m}} = 2 \text{ cm}^2/\text{g}$; see text for details. ^(c) Total (gas+dust) disk mass computed from M_{dust} assuming a gas = to-dust mass ratio of 100.

4.2. Disk sizes and surface density profile

Table 2 gives in Col. 4 the deconvolved major axis computed assuming a Gaussian source. Of the 11 detected objects, 8 are not resolved with deconvolved radii $\lesssim 24$ AU for the adopted distance $D = 122$ pc. Three objects, ISO-Oph042, ISO-Oph160, and ISO-Oph193, are marginally resolved.

ISO-Oph160 and ISO-Oph193 are detected with a high signal-to-noise ratio (≥ 30), hence we attempted a more careful analysis of the disk structure. Following Tazzari et al. (2016), we performed a fit to the visibilities using a simple two-layer disk model with two different prescriptions for the distribution of the surface density: a power law distribution with a sharp outer radius or an exponential taper, in the following we refer to these two models as truncated power law and exponentially tapered.

In the truncated power law case, $\Sigma(R)$ follows a power law of exponent p out to a radius R_{out} as follows:

$$\Sigma(R) = \Sigma_0 \left(\frac{R}{R_0} \right)^{-p}. \quad (2)$$

For the exponentially tapered, we adopted the parametrization of Guilloteau et al. (2011), i.e.

$$\Sigma(R) = \Sigma_0 \left(\frac{R}{R_0} \right)^{-\gamma} \exp \left[- \left(\frac{R}{R_c} \right)^{2-\gamma} \right], \quad (3)$$

which is a solution of the self-similar evolution of viscous accretion disks (where viscosity increases as R^γ), and is equivalent to other commonly used parametrizations (e.g. Isella et al. 2009). The functional form of $\Sigma(R)$ is defined by three parameters: R_0 and p or, equivalently, R_c and γ , and $\Sigma_0 = \Sigma(R_0 = 10 \text{ AU})$, which is the normalization factor that scales with the disk mass. In all cases we adopt an inner radius of 0.1 AU, as the results do not depend on its exact value.

Once Σ and the stellar parameters are fixed, the disk temperature and the surface brightness at $890 \mu\text{m}$ are computed using the two-layer radiation transfer model (Chiang & Goldreich 1997; Dullemond et al. 2001; Chiang et al. 2001) with flare reduced by a factor 3 to match the typical values of the far-infrared excess observed in BDs (Daemgen et al. 2016). The dust opacity is calculated using Mie theory assuming the same dust composition throughout the disk, given by the following fractional abundances adapted from Pollack et al. (1994): 5.4% astronomical silicates, 20.6% carbonaceous material, 44% water ice, and 30% vacuum (see Trotta et al. 2013, for details). Furthermore, we assume a power law grain size distribution $n(a) \propto a^{-q}$ for $a_{\text{min}} \leq a \leq a_{\text{max}}$, where a is the grain size. In order to model the fact that we expect larger grains in the disk midplane than on the surface (see Testi et al. 2014), we use different prescriptions for the grains in the disk surface ($a_{\text{min}} = 10 \text{ nm}$, $a_{\text{max}} = 1 \mu\text{m}$, and $q = 3.5$) and for the midplane ($a_{\text{min}} = 10 \text{ nm}$, $a_{\text{max}} = 1.4 \mu\text{m}$, and $q = 3$). The midplane dust opacity is $\kappa_{890} = 2 \text{ cm}^2/\text{g}$. The dust-to-gas mass ratio is fixed to 10^{-2} .

The method uses a Bayesian approach and implements an affine-invariant Markov Chain Monte Carlo (MCMC) ensemble sampler (see Tazzari et al. 2016, for a full description). For each model we compute the $890 \mu\text{m}$ synthetic image and we sample its Fourier transform at the (u, v) plane location of the observations. We estimate the Bayesian probability using $\exp(-\chi^2)$ as likelihood with flat priors. In this scheme there are five free parameters, namely the disk mass M_{disk} , the two parameters that define Σ (R_c, γ for the exponentially tapered profile, R_{out}, p for the truncated power law), the inclination, and position angle of the disk on the sky. Two additional nuisance parameters are used for the disk centre position on the sky.

In Figs. 2–4 and in Table 3, we show the results of the fits for our two disks. The probability distributions shown in Fig. 2 illustrate the range of the parameters $\{R_c, \gamma\}$ and $\{R_{\text{out}}, p\}$ derived from our models. The shaded areas correspond to ~68%, ~95%, and ~99% confidence levels. In Fig. 3 we show the real and imaginary part of the visibilities of the two sources and overplot

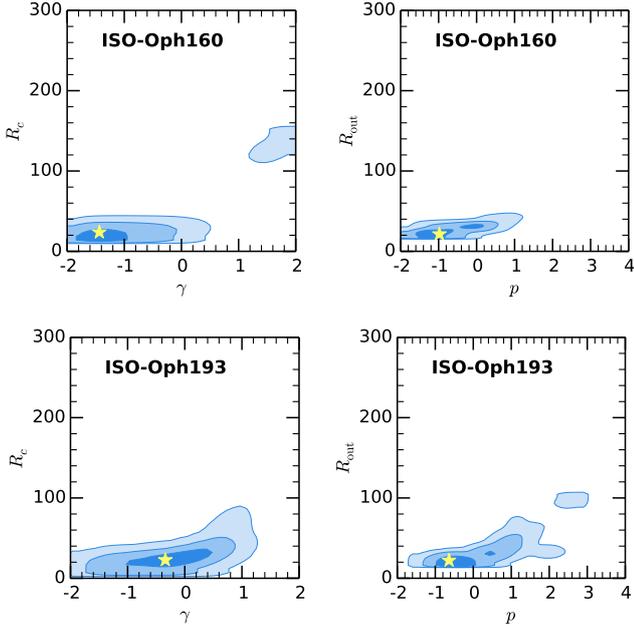


Fig. 2. Two-dimensional distributions of the model parameters $\{R_c, \gamma\}$ (left column) and $\{R_{\text{out}}, p\}$ (right column) for the fits of the disks in ISO-Oph160 (top row) and ISO-Oph193 (bottom row). The different shaded areas correspond to the 1, 2, and 3σ confidence levels (from light to dark blue). The yellow star indicates the values of the parameters for the best-fit models shown in Figs. 3 and 4.

Table 3. Results of the model fits for the parameter sets $\{R_c, \gamma\}$ and $\{R_{\text{out}}, p\}$; see Sect. 4.2 and Appendix B for details.

Name	R_c [AU]	γ	R_{out} [AU]	p
ISO-Oph160	24^{+2}_{-3}	$-1.4^{+0.9}_{-0.2}$	$22.0^{+12}_{-0.4}$	$-1.0^{+1.1}_{-0.4}$
ISO-Oph193	23^{+11}_{-3}	$-0.34^{+0.8}_{-0.7}$	22^{+16}_{-2}	$-0.64^{+1.5}_{-0.02}$
2M0444+2512	49^{+48}_{-11}	$1.4^{+0.5}_{-0.1}$	153^{+100}_{-40}	$2.0^{+0.3}_{-0.2}$
CIDA 1	82^{+8}_{-15}	$0.9^{+0.1}_{-0.1}$	136^{+17}_{-45}	$1.35^{+0.09}_{-0.13}$
CFHT Tau4	>90	$1.0^{+0.2}_{-0.3}$	>90	$1.0^{+0.6}_{-0.1}$

Notes. The 1σ confidence range for each parameter is also shown.

two models, one for the truncated power law $\Sigma(R)$ and one for the exponentially tapered, which are selected as those with the lowest χ^2 . The parameters of these models are indicated with a yellow star in Fig. 2; the minimum normalized χ^2 range is between 1.00 and 1.38. In Fig. 4 we show the observed ALMA images for the two sources (same as Fig. 1), the model images and the residual images computed from the simulated visibilities for the models indicated with a yellow star in Fig. 2 and plotted in Fig. 3. In Table 3 we report the numerical values and uncertainties of (R_c, γ) and (R_{out}, p) for the sources analysed in this paper.

The modelling results suggest that the disks are compact ($R \lesssim 25$ AU), which is also consistent with the small deconvolved sizes (Table 2). The values of γ and p are ≤ 0 and ≤ -0.5 , respectively. This implies that the derived profiles of Σ for ISO-Oph160 and ISO-Oph193 are consistent with a rather flat inner

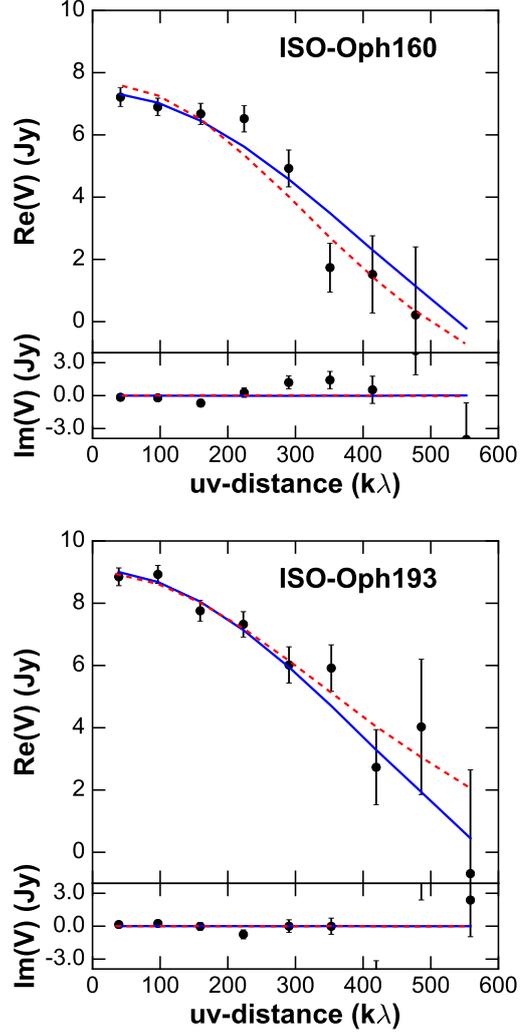


Fig. 3. Real (top subpanel) and imaginary (bottom subpanel) visibilities as a function of baseline length for ISO-Oph160 (top figure) and ISO-Oph193 (bottom figure). The ALMA points were binned to increase the signal-to-noise ratio. The curves show the best-fitting models: the truncated power law Σ model as a solid blue line and the exponentially tapered model as a red dashed line.

region for $R \lesssim 20$ – 25 and a very steep cutoff. They also confirm that the (sub)mm emission is optically thin at all radii. All other disks in our sample are too faint to run this analysis and their small apparent sizes (Table 2) may either be the result of small and sharply truncated disks, as for ISO-Oph160 and ISO-Oph193, or compatible with a decline of Σ and a larger outer radius, as our limited surface brightness sensitivity does not allow us to distinguish between these two cases (see e.g. the discussion in Natta & Testi 2008).

As a cautionary note, we point out that our models have been computed with identical dust properties across the disk (as we have no direct constraint that would allow us to use a different approach). If dust grows, migrates, and eventually has a size distribution that depends on the distance from the star (e.g. Birnstiel et al. 2010), then using identical dust properties throughout the disk may result in deriving a $\Sigma(R)$ profile that is shallower than the true profile (see e.g. the discussion in Banzatti et al. 2011; Trotta et al. 2013).

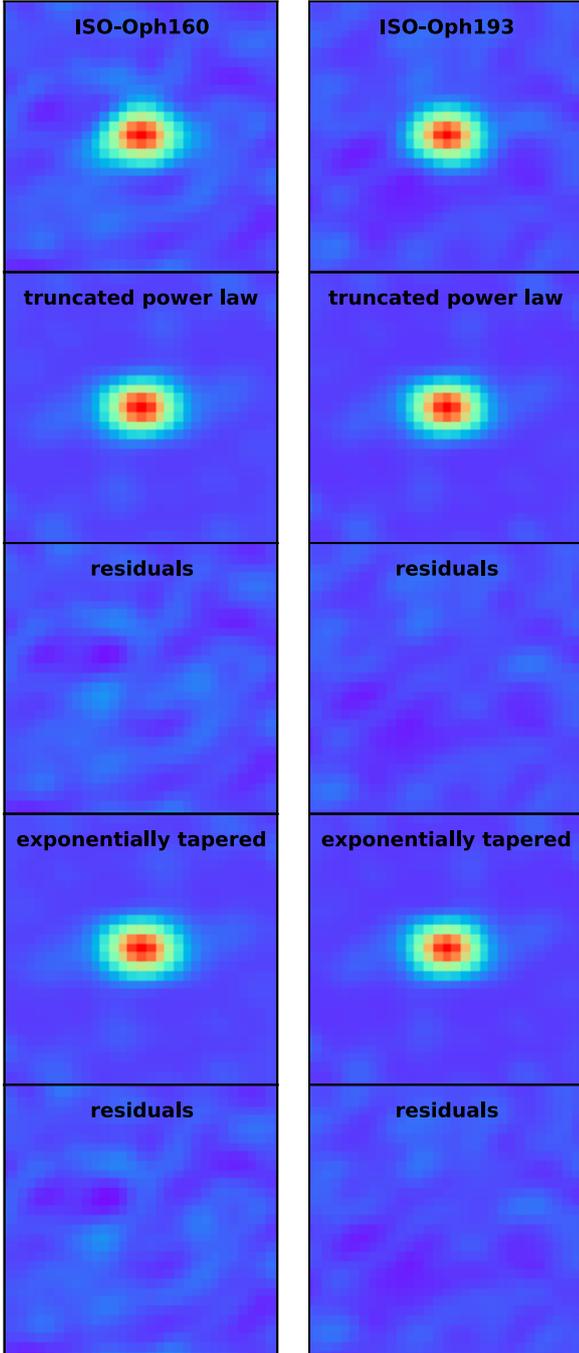


Fig. 4. Comparison between observations and best-fit models for ISO-Oph160 (*left column*) and ISO-Oph193 (*right column*). From top to bottom: observed, model and residual images for the best fit with $\Sigma(R)$ parametrized as a truncated power law; model and residual images for the best fit with the exponentially tapered $\Sigma(R)$. The size of each panel is $3''$ as in Fig. 1.

5. Discussion

5.1. BD disk masses and potential for planet formation

Figure 5 compares the values for disk masses of BDs that we obtained in ρ Oph with disk masses of BDs in the literature derived from (sub)mm fluxes: Upper Sco (van der Plas et al. 2016) and in Taurus (see figure caption for references). For consistency, we recomputed all disk masses using Eq. (1) with the appropriate T_A for each object and $\kappa_{890\ \mu\text{m}} = 2\ \text{cm}^2/\text{g}$. The values of

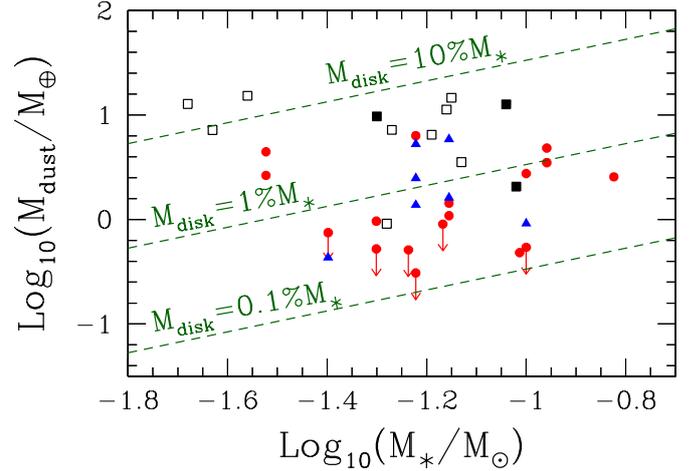


Fig. 5. Disk masses as function of the central object mass M_* . Red dots and arrows are for the ρ Oph sample discussed in this paper. The black squares report the disk masses for BDs in Taurus from the $F_{890\ \mu\text{m}}$ detections: open, single-dish measurements from Andrews & Williams (2005); Broekhoven-Fiene et al. (2014); Mohanty et al. (2013); filled, from ALMA measurements by Ricci et al. (2014). Blue triangles show the values for the 7 BDs in Upper Sco observed with ALMA by van der Plas et al. (2016). For all objects, disk masses have been computed as in ρ Oph, assuming $T = 25 (L_*/L_\odot)^{0.25}$ K, $\kappa_{890\ \mu\text{m}} = 2.0\ \text{cm}^2/\text{g}$.

M_{dust} in the ρ Oph and Upper Sco objects cover a similar range, while several objects in Taurus have $M_{\text{dust}} \sim 10 M_\oplus$. Most Taurus BDs have been observed with single-dish telescopes and, in principle, the large fluxes could be the result of diffuse emission contamination. However, when both single dish and interferometric fluxes are available, they do not differ significantly (see e.g. Andrews & Williams 2007; Ricci et al. 2012, 2014).

The largest ratios M_{disk}/M_* are similar in the three regions, i.e. between 0.01 and 0.1. However, contrary to Taurus and U Sco, ρ Oph has a large number of BD disks with $M_{\text{disk}}/M_* \lesssim 0.1$. This may appear as a surprising result, given that ρ Oph should be the youngest of these regions. This difference is likely a selection effect, which is similar to what was already noted by Natta et al. (2006) for the mass accretion rate distribution. While our ρ Oph sample is unbiased with no pre-selection that could favour more massive disks, this is not the case of the Upper Sco sample (van der Plas et al. 2016).

Overall, the low dust masses shown in Fig. 5 agree with the estimates of disk masses derived from *Herschel* fluxes for a number of BDs in various star-forming regions (Harvey et al. 2012; Alves de Oliveira et al. 2013; Liu et al. 2015a,b). With the bulk of the disk population containing about one Earth mass of solids, the ability of these disks to form planets is obviously questionable. The study by Payne & Lodato (2007) suggests that disks containing a fraction of a Jupiter mass of material (including gas and dust) and surface density profiles that are shallower than $\Sigma \propto R^{-1}$ are very unlikely to form planets at all. If we assume a gas-to-dust ratio by mass of ~ 100 , only the most massive disks in Fig. 5 (those with $M_{\text{dust}} \sim 10 M_\oplus$) will be massive enough to form planets. In addition, if the $\Sigma(R)$ profiles derived in Sect. 4.2 are found to be common in BD disks, the prospects of planet formation in these systems is really grim. Some optimism may be still possible for some of the most massive BD disks in Taurus (see Ricci et al. 2014, and Sect. 5.3), such disks may explain the detection through microlensing of Earth-mass planets around BDs (e.g. Udalski et al. 2015). More massive, supra-Jupiter mass

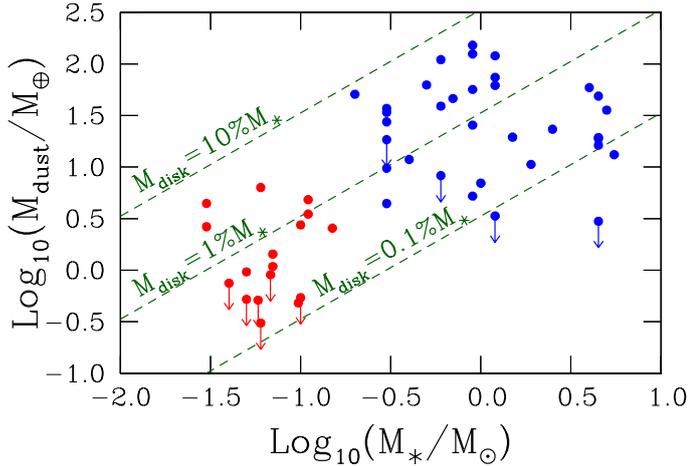


Fig. 6. Dust mass vs. stellar mass for ρ Oph BDs (red) and TTS (blue). The dashed green lines show the dust mass in a disk with 10%, 1%, 0.1% the stellar mass, computed assuming a gas-to-dust mass ratio of 100.

companions (e.g. Chauvin et al. 2004; Joergens & Müller 2007; Todorov et al. 2010; Han et al. 2013) cannot be really considered to be formed in protoplanetary disks with the properties that we observe, and are most likely the result of a binary system formation in the substellar regime.

5.2. Comparison between BDs and TTS disk masses

In Fig. 6 we show the disk mass for the ρ Oph BDs together with the disk mass for the TTS in the same region as a function of the mass of the central object. To compute the disk masses for the TTS sources, we used the $850 \mu\text{m}$ fluxes from Andrews & Williams (2007), calculated the appropriate T_A for each object, and applied Eq. (1) with the same value of $\kappa_{850 \mu\text{m}}$ as for the BDs. This ensures that the same method has been used to compute the masses across the whole range, the choice of using the same dust opacity for all sources is justified by the lack of evidence for a systematic difference in the dust properties in disks as a function of stellar mass in ρ Oph and in other star-forming regions (Ricci et al. 2010, 2012; Testi et al. 2014).

Figure 6 shows that the dust masses in disks around BDs and TTS roughly scale as the mass of the central object. If we correct for a gas-to-dust ratio of 100 by mass, then the disk contains approximately 1% of the mass of the system with a large scatter at any given mass of about one order of magnitude. A number of caveats are in order. Most importantly, the stellar parameters of the ρ Oph TTS are very uncertain, as no systematic study of TTS comparable to that carried out by Manara et al. (2015) for the BDs is available. We estimated L_* and M_* from the spectral types of McClure et al. (2010), assuming that all the stars lie on a 1 Myr isochrone as determined using the theoretical evolutionary tracks of Baraffe et al. (1998). Although this does not affect the classification as TTS, which is based on the spectral type, it affects the exact location on the diagrams and the estimate of the disk-to-star mass ratio. Secondly, the sample of BDs and TTS that have good sub-mm measurements is largely incomplete. The completeness of the BDs sample in this study has been addressed in Sect. 2; the TTS sample limitations are described in Andrews & Williams (2007). In this paper we proceed with the analysis under the assumption that the samples are representative of the properties of the full populations, but this is an assumption that needs to be put on firmer ground with future optical

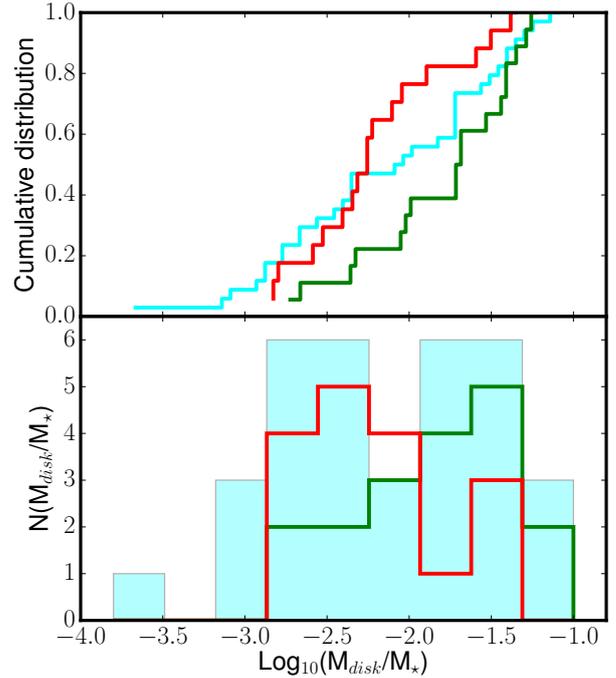


Fig. 7. Cumulative distributions (top) and histogram of the M_{disk}/M_* values for ρ Oph BDs (red), the full TTS sample (cyan), and the subset with $0.2 \leq M_*/M_\odot \leq 1.0$ (green).

and near-infrared spectroscopic studies of the central stars and ALMA surveys of the full populations.

In Fig. 6 there is an apparent paucity of BD disks in the region 1–10% of the mass of the apparent central object compared with TTs. To quantitatively estimate whether there is a real discrepancy between the two samples, we analysed the cumulative distributions of the ratio M_{disk}/M_* for BDs and TTS. In Fig. 7 we show (in the bottom panel) the distributions of the ratio M_{disk}/M_* for the full Andrews & Williams (2007) sample (cyan filled histogram), a subset of that sample with $0.2 \leq M_*/M_\odot \leq 1.0$ (green histogram), and for our BDs sample (red histogram). The top panel of Fig. 7 shows the cumulative distributions for the same samples. The TTS sample contains objects with central mass in the range from $\sim 0.2 M_\odot$ to $\sim 5 M_\odot$. We performed the Anderson-Darling test¹ between these two samples and find $\sim 1.6\%$ probability that the two are drawn from the same parent distribution (for the purpose of this test we treated upper limits as measurements). The major caveat to bear in mind is the fact that the samples may not be fully representative of the full populations and that the methods for deriving the disk and stellar masses in the two samples are not fully identical. Future detailed characterization of, in particular, the TTS population (both the disk and photospheric properties) will allow us to provide a definitive answer as to whether the possible difference we see here is real.

5.3. Comparison with Taurus BD disks structure

The two clearly resolved ρ Oph disks both show a sharp dust disk edge at ~ 20 – 30 AU with a rather flat surface density profile inside it (see Sect 4.2, and Table 5.3). While this second aspect may be due to our assumption that the dust properties do not change with radius, the sharp outer edge of these two disks seems to be a robust result. This finding is in contrast with the

¹ We used the `scipy.stats` python implementation of the test, which follows Scholz & Stephens (1987).

results on BD disks sizes reported by Ricci et al. (2014) for disks in Taurus. To provide a proper comparison, we re-analysed the three BD disks in Taurus using the method outlined in Sect. 4.2. In Table 3 we show the comparison between the values of $\{R_c, \gamma\}$ and $\{R_{\text{out}}, p\}$, which are derived by the two families of models, for the ρ Oph and Taurus BDs (the figures with the model results for Taurus are reported in Appendix B). We confirm and extend the results of the previous study. The truncated power law parameters from our reanalysis are consistent with previous results and, in addition, the exponentially tapered models are also consistent with a decreasing $\Sigma(R)$ and a smooth outer disk edge. This seems to suggest the possibility of an important difference between the two most massive BD disks in ρ Oph and those in Taurus. The Taurus disks have a structure very similar to those of more massive TTS, while the ρ Oph BDs have smaller disks with a sharper outer edge. The dust mass in the disks does not seem to be very different, $\sim 4.8\text{--}6.3 M_{\oplus}$ in Oph and $\sim 2, \sim 10, \text{ and } \sim 15 M_{\oplus}$ for CFHT Tau4, 2M0444+2512 and CIDA 1, respectively.

Both the formation of BDs as ejected embryos (Reipurth & Clarke 2001) and dynamical interactions in a dense star-forming region would predict that disks may be truncated to small radii at some point of the early evolution of the system (Bate 2009, 2012). In all cases it is expected that the gaseous component of the disk viscously re-expands on timescales shorter than ~ 1 Myr or a new outer disk could be accreted from the cloud (Bate 2012; Scicluna et al. 2014). At face value, our numbers are consistent with the results of Bate (2012) models; these models show that the distribution of disk sizes in young dense clusters may be rather small ($\lesssim 10$ AU for 50% of the disks), but with a significant tail that extends to $R \gtrsim 100$ AU. The low density and/or slightly older age of Taurus may naturally explain the larger radii for 2M0444+2512, CIDA 1, and CFHT Tau4.

According to Stamatellos & Whitworth (2009), BDs formed in the disk of a solar-mass star have disks with masses of \lesssim few M_J and radii of 20–50 AU with a small fraction of larger disks. There is no correlation between the BD disk properties and those of the parental star. These disks are likely stripped by the following ejection, and the distribution of properties of the surviving disks is not clearly predicted by models. It is possible that both the ρ Oph and the Taurus BDs can be explained by ejection scenarios. Lacking large observational samples and more detailed theoretical models that describe the properties and evolution of disks after ejection, we cannot really constraint in detail the BDs formation scenario.

Dynamical truncation of the disk radius on timescales longer than the viscous lifetime may be caused by the presence of a companion, which may truncate the circumstellar disk at a radius of $\sim 0.3\text{--}0.5$ of the binary separation and effectively prevent its viscous expansion (Artymowicz & Lubow 1994). There are no reported companions for ISO-Oph160 and ISO-Oph193, but none of the current infrared surveys would be sensitive to close ($\sim 0''.5\text{--}1''.0$), planetary-mass companions. A dedicated measurement would be in order before ruling out this possibility. As a plausibility argument, we note that in our survey we do not find any large and massive disks in ρ Oph that resemble those found in Taurus, and we expect that our unbiased search would have not missed these large, smooth disks.

A sharp edge in the dusty disk, as observed at millimetre wavelengths, can also be the result of a very different process, namely grain evolution. As grains grow, fragment and drift, the large grains, that are responsible for the observed mm emission, decouple from the gas, and concentrate more towards the star. This effect, which is predicted by global disk

evolution models, is also measured in large protoplanetary disks around TTS and Herbig Ae/Be stars (e.g. Birnstiel et al. 2010; Pérez et al. 2012; Tazzari et al. 2016; Testi et al. 2014). Birnstiel & Andrews (2014) have shown that as a result of this process, the large grains surface density, as probed by millimetre observations, shows a sharp decrease at a radius significantly smaller than that of the gaseous disk. The edge of the dusty disk, however, also tends to get smoother with time (on viscous timescales). Similar results are also found when photoevaporation is taken into account (Gorti et al. 2015). Although in this case the difference in size between the gaseous and dusty disk is reduced, the mm-size grains have a sharper outer cutoff than the gas. There is plenty of evidence of grain evolution in BD disks (Apai et al. 2004; Ricci et al. 2012, 2014). In particular, the ISO-Oph102, 2M0444+2512, CIDA 1, and CFHT Tau4, observed with ALMA at two wavelengths by Ricci et al. (2012, 2014) have mm spectral indexes $\sim 2\text{--}2.4$, and an exponent of the mm dust opacity law $\beta \sim 0.2$ that is typical of very large grains. Unfortunately, at present we have no information for the sample of the ρ Oph BDs at other wavelengths, and we do not know if ISO-Oph160 and ISO-Oph193, in particular, have evidence of evolved, large grains. The only ρ Oph object for which this information is available is ISO-Oph102, which shows evidence of evolved grains Ricci et al. (2012) and a very compact continuum (deconvolved half-major axis < 12 AU) and CO($J = 3\text{--}2$) emission (~ 15 AU), which is consistent with the results for the two resolved objects. The Taurus BDs discussed in this paper all have evolved their grains; their dusty disks are large, have smooth edges, and are surrounded by extended gaseous disks, as TTS. If dust evolution occurs in both ρ Oph and Taurus BD disks, then the evolutionary stage or path of the two groups must be different, possibly owing to very different ages, initial disk structures, and/or environmental effects. However, this remains to be proved. On one side, the number of objects studied so far is very small and needs to be significantly increased. On the other, the difference between the two groups is significant at a 2.5σ level only, and ALMA observations with better resolution and sensitivity are in order.

6. Conclusions and summary

Our millimetre observations of disks in ρ Oph BDs provides the first large, homogeneous, and well-characterized sample in a young star-forming region. The sample is unbiased, as it contained all the spectroscopically confirmed Class II BDs at the time of the proposal, with no selection that could favour more massive disks. We detected 11/17 ($\sim 65\%$) objects; the disk masses are $\sim 0.5\text{--}6.3 M_{\oplus}$. For the remaining 6, we set 98% confidence level upper limits at $\sim 0.3\text{--}0.9 M_{\oplus}$. There may be evidence for BDs to have typical values of M_{disk}/M_* that are smaller than in TTS, which possibly supports the idea of a different formation path, but the biases and limited accuracy of the data for the TTS sample do not allow us to reach a firm conclusion. In all cases the emission from the BD disks in ρ Oph appears to be compact with deconvolved major axis $\lesssim 20$ AU. In most cases, however, we are limited by sensitivity in our ability to detect a possible emission from a declining dust surface density in the outer disk. Two objects are resolved, and we performed a detailed analysis to derive their surface density profile. Both objects have a flat surface density and a sharp cutoff at about $\lesssim 25$ AU.

In comparing with model expectations, we conclude that it should be very difficult to effectively form planets in the disks around most BDs. If the disk masses that we measure are typical, then the supra-Jupiter mass companions detected around some

BDs are most likely the result of binary formation rather than bona fide planets formed in protoplanetary disks.

The difference between the ρ Oph BDs studied here with respect to the Taurus BDs studied by Ricci et al. (2014), which have only slightly more massive disks (by factor <3), is striking. The Taurus BD disks are much larger and have a rather smooth edge (see Table 3) that is very similar to TTS disks. It is possible that the ρ Oph environment is responsible, either by giving origin to disks with very different properties or because close encounters between disk systems are much more frequent than in the more diffuse region Taurus. The possibilities that the Taurus BDs had the time to viscously spread-out their disks, or that the two ρ Oph BDs are close binaries cannot be ruled out with the current observational constraints.

Dust evolution (i.e. grain growth) has been confirmed both in the Taurus BDs and in ISO-Oph102, which is one of the BDs in our sample. The combination of growth, fragmentation, and drift can create dust disks that are much smaller than the gaseous disks with relatively sharp edges. However, it is difficult to account for the difference with the Taurus BDs via dust evolution alone.

The results we found with this continuum survey are tantalizing, but clearly need to be put on firmer ground with future ALMA observations. On the one hand, it would be important to compare, with adequate signal to noise and angular resolution, the gaseous and dusty disks for the BDs with and without evidence for disk truncation discussed in Sect. 4.2. On the other hand, it is also necessary to put on firm grounds and for other star-forming regions the possible difference in the $M_{\text{disk}}/M_{\star}$ distributions of TTS and BDs discussed in Sect. 5.3. ALMA is now starting to provide extensive surveys of the protoplanetary disks populations around TTS in various star-forming regions (Ansdell et al. 2016; Barenfeld et al. 2016; Pascucci et al. 2016), and these offer a prime opportunity for a full extension to the substellar domain.

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References

Alves de Oliveira, C., Moraux, E., Bouvier, J., & Bouy, H. 2012, *A&A*, **539**, A151
 Alves de Oliveira, C., Ábrahám, P., Marton, G., et al. 2013, *A&A*, **559**, A126
 Andrews, S. M., & Williams, J. P. 2005, *ApJ*, **631**, 1134
 Andrews, S. M., & Williams, J. P. 2007, *ApJ*, **671**, 1800
 Andrews, S. M., Rosenfeld, K. A., Kraus, A. L., & Wilner, D. J. 2013, *ApJ*, **771**, 129

Ansdell, M., Williams, J. P., van der Marel, N., et al. 2016, *ApJ*, **828**, 46
 Apai, D., Pascucci, I., Sterzik, M. F., et al. 2004, *A&A*, **426**, L53
 Apai, D., Pascucci, I., Bouwman, J., et al. 2005, *Science*, **310**, 834
 Artymowicz, P., & Lubow, S. H. 1994, *ApJ*, **421**, 651
 Banzatti, A., Testi, L., Isella, A., et al. 2011, *A&A*, **525**, A12
 Baraffe, I., Chabrier, G., Allard, F., & Hauschildt, P. H. 1998, *A&A*, **337**, 403
 Baraffe, I., Chabrier, G., & Barman, T. 2008, *A&A*, **482**, 315
 Barenfeld, S. A., Carpenter, J. M., Ricci, L., & Isella, A. 2016, *ApJ*, **827**, 142
 Bate, M. R. 2004, *Ap&SS*, **292**, 297
 Bate, M. R. 2009, *MNRAS*, **392**, 590
 Bate, M. R. 2012, *MNRAS*, **419**, 3115
 Birnstiel, T., & Andrews, S. M. 2014, *ApJ*, **780**, 153
 Birnstiel, T., Dullemond, C. P., & Brauer, F. 2010, *A&A*, **513**, A79
 Broekhoven-Fiene, H., Matthews, B., Duchêne, G., et al. 2014, *ApJ*, **789**, 155
 Chauvin, G., Lagrange, A.-M., Dumas, C., et al. 2004, *A&A*, **425**, L29
 Chiang, E. I., & Goldreich, P. 1997, *ApJ*, **490**, 368
 Chiang, E. I., Joungh, M. K., Creech-Eakman, M. J., et al. 2001, *ApJ*, **547**, 1077
 Comerón, F., Rieke, G. H., Claes, P., Torra, J., & Laureijs, R. J. 1998, *A&A*, **335**, 522
 Daemgen, S., Natta, A., Scholz, A., et al. 2016, *A&A*, in press, DOI: 10.1051/0004-6361/201628431
 Dullemond, C. P., Dominik, C., & Natta, A. 2001, *ApJ*, **560**, 957
 Geers, V., Scholz, A., Jayawardhana, R., et al. 2011, *ApJ*, **726**, 23
 Gorti, U., Hollenbach, D., & Dullemond, C. P. 2015, *ApJ*, **804**, 29
 Guilloteau, S., Dutrey, A., Piétu, V., & Boehler, Y. 2011, *A&A*, **529**, A105
 Han, C., Jung, Y. K., Udalski, A., et al. 2013, *ApJ*, **778**, 38
 Harvey, P. M., Henning, T., Liu, Y., et al. 2012, *ApJ*, **755**, 67
 Hennebelle, P., & Chabrier, G. 2009, *ApJ*, **702**, 1428
 Hester, J. J., Scowen, P. A., Sankrit, R., et al. 1996, *AJ*, **111**, 2349
 Isella, A., Carpenter, J. M., & Sargent, A. I. 2009, *ApJ*, **701**, 260
 Joergens, V., & Müller, A. 2007, *ApJ*, **666**, L113
 Liu, Y., Herczeg, G. J., Gong, M., et al. 2015a, *A&A*, **573**, A63
 Liu, Y., Joergens, V., Bayo, A., Nielbock, M., & Wang, H. 2015b, *A&A*, **582**, A22
 Manara, C. F., Testi, L., Natta, A., & Alcalá, J. M. 2015, *A&A*, **579**, A66
 McClure, M. K., Furlan, E., Manoj, P., et al. 2010, *ApJS*, **188**, 75
 Mohanty, S., Greaves, J., Mortlock, D., et al. 2013, *ApJ*, **773**, 168
 Mužić, K., Scholz, A., Geers, V., Jayawardhana, R., & Tamura, M. 2012, *ApJ*, **744**, 134
 Natta, A., & Testi, L. 2001, *A&A*, **376**, L22
 Natta, A., & Testi, L. 2008, *Ap&SS*, **313**, 113
 Natta, A., Testi, L., Comerón, F., et al. 2002, *A&A*, **393**, 597
 Natta, A., Testi, L., & Randich, S. 2006, *A&A*, **452**, 245
 Pascucci, I., Testi, L., Herczeg, G., et al. 2016, *ApJ*, in press [arXiv:1608.03621]
 Payne, M. J., & Lodato, G. 2007, *MNRAS*, **381**, 1597
 Pérez, L. M., Carpenter, J. M., Chandler, C. J., et al. 2012, *ApJ*, **760**, L17
 Pinilla, P., Birnstiel, T., Benisty, M., et al. 2013, *A&A*, **554**, A95
 Pollack, J. B., Hollenbach, D., Beckwith, S., et al. 1994, *ApJ*, **421**, 615
 Rebolo, R., Zapatero Osorio, M. R., & Martín, E. L. 1995, *Nature*, **377**, 129
 Reipurth, B., & Clarke, C. 2001, *AJ*, **122**, 432
 Ricci, L., Testi, L., Natta, A., & Brooks, K. J. 2010, *A&A*, **521**, A66
 Ricci, L., Testi, L., Natta, A., Scholz, A., & de Gregorio-Monsalvo, I. 2012, *ApJ*, **761**, L20
 Ricci, L., Isella, A., Carpenter, J. M., & Testi, L. 2013, *ApJ*, **764**, L27
 Ricci, L., Testi, L., Natta, A., et al. 2014, *ApJ*, **791**, 20
 Scholz, F.-W., & Stephens, M. A. 1987, **82**, 918
 Scicluna, P., Rosotti, G., Dale, J. E., & Testi, L. 2014, *A&A*, **566**, L3
 Stamatellos, D., & Herczeg, G. J. 2015, *MNRAS*, **449**, 3432
 Stamatellos, D., & Whitworth, A. P. 2009, *MNRAS*, **392**, 413
 Sterzik, M. F., Pascucci, I., Apai, D., van der Blik, N., & Dullemond, C. P. 2004, *A&A*, **427**, 245
 Tazzari, M., Testi, L., Ercolano, B., et al. 2016, *A&A*, **588**, A53
 Testi, L., Natta, A., Oliva, E., et al. 2002, *ApJ*, **571**, L155
 Testi, L., Birnstiel, T., Ricci, L., et al. 2014, *Protostars and Planets VI*, 339
 Todorov, K., Luhman, K. L., & McLeod, K. K. 2010, *ApJ*, **714**, L84
 Trotta, F., Testi, L., Natta, A., Isella, A., & Ricci, L. 2013, *A&A*, **558**, A64
 Udalski, A., Jung, Y. K., Han, C., et al. 2015, *ApJ*, **812**, 47
 van der Plas, G., Ménard, F., Ward-Duong, K., et al. 2016, *ApJ*, **819**, 102
 Whitworth, A. P., & Zinnecker, H. 2004, *A&A*, **427**, 299

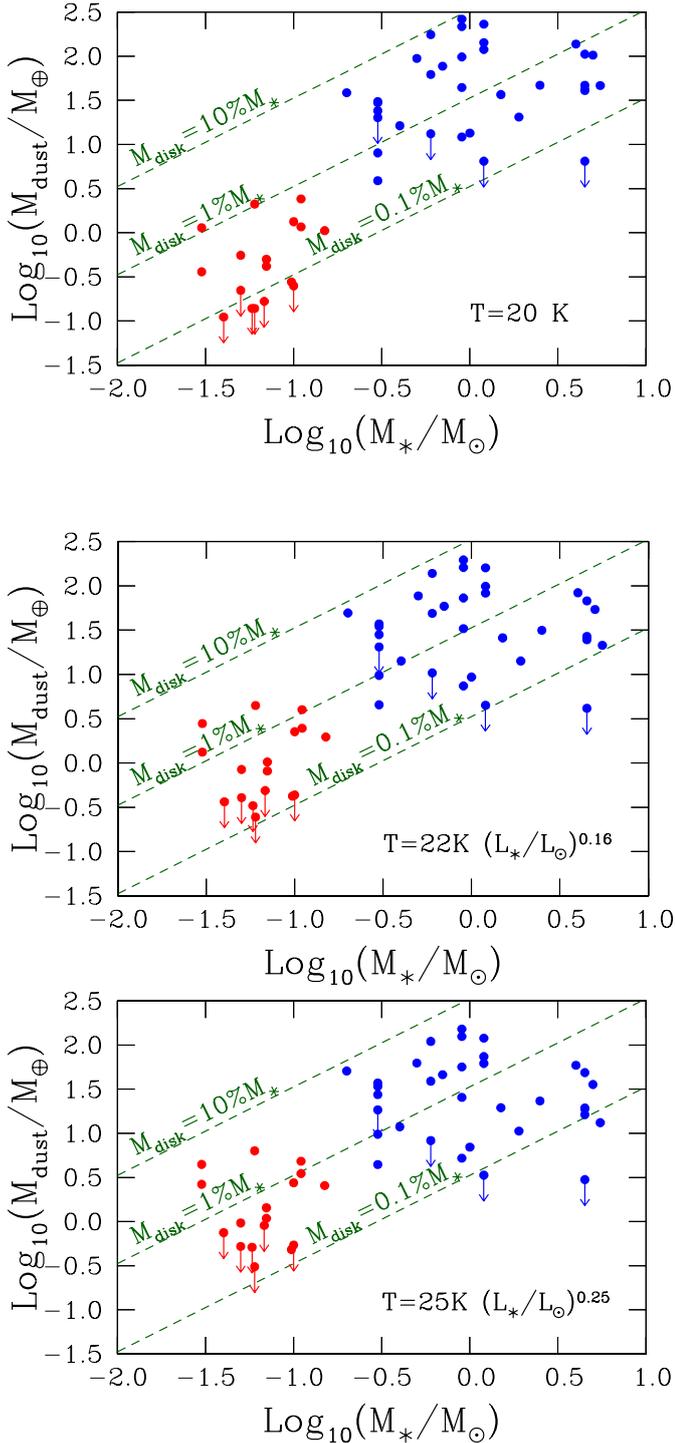


Fig. A.1. Dust mass vs stellar mass for ρ Oph BDs (red) and TTS (blue). The *top panel* shows the results obtained by computing dust masses from Eq. (1) with $T = 20\text{ K}$ for all objects. The *mid panel* when adopting the scaling law of T with L_{*} suggested by van der Plas et al. (2016). The *bottom panel* adopting the scaling law of Andrews et al. (2013), as in Sect. 4.1. The dashed green lines show the dust mass in a disk with 10%, 1%, 0.1% the stellar mass, computed assuming a gas-to-dust mass ratio of 100.

Appendix A: Temperature

The Andrews et al. (2013) scaling law was derived from a grid of disk radiation transfer models over a range $L_{*} \sim 0.1\text{--}100 L_{\odot}$. The choice of the value of T appropriate to recover the dust

mass from the observed (sub)mm flux for very low-mass TTs and BDs was recently discussed by Daemgen et al. (2016), who show that, in addition to L_{*} , the value depends strongly on the degree of disk flaring, and, to a lesser degree, on the disk mass itself and other disk parameters. Using the ratio of the far-infrared flux to the J -band flux, which is a good proxy for the stellar luminosity, these authors find that most objects with *Herschel* far-infrared measurements have ratios that are much lower than the values predicted by fully flared disk models. This is also true also for the BDs in our sample with measured *Herschel* fluxes. Based on the analysis of Daemgen et al. (2016), we conclude that the most appropriate value of the disk averaged temperature for the estimate of the disk mass from the millimetre flux is likely to be a few degrees lower than T_{A} . The error on the disk mass computed with temperature T_{A} , however, is of order $\pm 20\%$, with a systematic trend of underestimating the dust mass in BDs and overestimating it in low-luminosity TTs.

Very recently, van der Plas et al. (2016) have proposed a different scaling law of T with L_{*} ($T_{\text{vdp}} = 22 (L_{*}/L_{\odot})^{0.16}$), using a sample of eight BDs and very low-mass TTs in U Sco with measured ALMA fluxes. They derive the best disk mass from fitting the SEDs at all wavelengths and compare it with the results obtained from the (sub)mm flux only, using T_{A} and their improved prescription. They find that, on average, the masses derived using T_{A} are a factor ~ 3 larger than the result of the SED fits; the discrepancy is significantly reduced when T_{vdp} is used. In practice, for our sample the difference in M_{dust} derived using the two temperature prescriptions is not large; this difference is typically within a factor 1.5 for the majority of objects and ~ 2 for the two lowest luminosity objects, ISO-Oph033 and GY92-320. Given the large number of free parameters and uncertainties, and for an easier comparison with literature results for TTs, in this paper we have used T_{A} to compute dust masses with the caveat that the dust mass in the lowest luminosity objects may be overestimated by a factor of up to 2.

Even if the uncertainty on individual measurements is not very large, the choice of T in Eq. (1) may introduce a systematic trend in the disk mass–stellar mass relation, discussed in Sect. 5.2, because in star-forming regions M_{*} is roughly correlated with L_{*} . In this context, the choice of T_{A} to compute dust masses is the most conservative, i.e. this choice minimizes any existing trend of M_{dust} with M_{*} . Fig. A.1 shows the results for a constant value of $T = 20\text{ K}$, and using T_{vdp} . For $T = \text{const.}$, M_{dust} is $\propto F_{890\ \mu\text{m}}$. One can see that in both cases the difference between the BDs and the TTs is larger than for $T = T_{\text{A}}$.

Appendix B: Model fits to the structure of Taurus BD disks

In this Appendix we present the results of the reanalysis of the Taurus BD disks ALMA $890\ \mu\text{m}$ observations from Ricci et al. (2014). We applied the procedure and parameters as described in Sect. 4.2 to derive comparable results to our modelling of the ρ Oph BDs. The results for the truncated power law fits are consistent with the results presented in Ricci et al. (2014), in addition, we also performed the fits with the exponentially tapered $\Sigma(R)$. The lower values of R_{c} for the exponentially tapered, as compared with R_{out} in the truncated power law case, is consistent with the values of γ in the range 1–1.5. The model results are shown in graphical form in Figs. B.1 and B.2, where we show the two-parameter probability distributions for the pairs $\{R_{\text{c}}, \gamma\}$ and $\{R_{\text{out}}, p\}$ (Fig. B.1), and the comparison between the ALMA observed visibilities and the visibilities of the models with the lowest χ^2 in the chains (Fig. B.2).

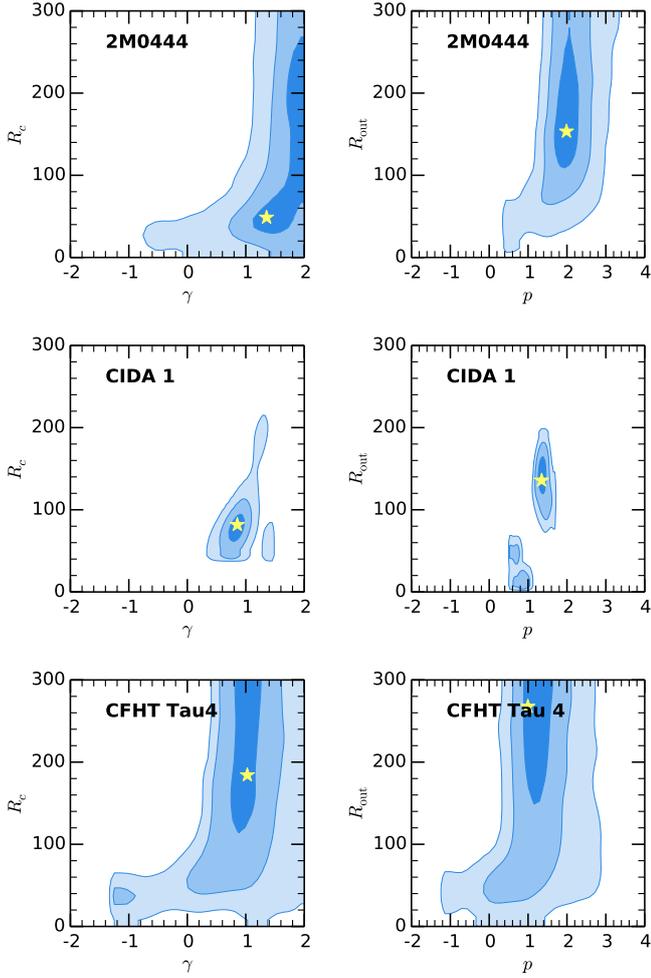


Fig. B.1. Two-dimensional distributions of the model parameters $\{R_c, \gamma\}$ (left column) and $\{R_{out}, p\}$ (right column) for the model fits of the disks in 2M0444+2512 (top row), CIDA 1 (middle row), and CFHT Tau 4 (bottom row). The different shaded areas correspond to the 1, 2 and 3σ confidence levels (from light to dark blue), as in Fig. 2. The yellow stars mark the parameter values for the models plotted in Fig. B.2.

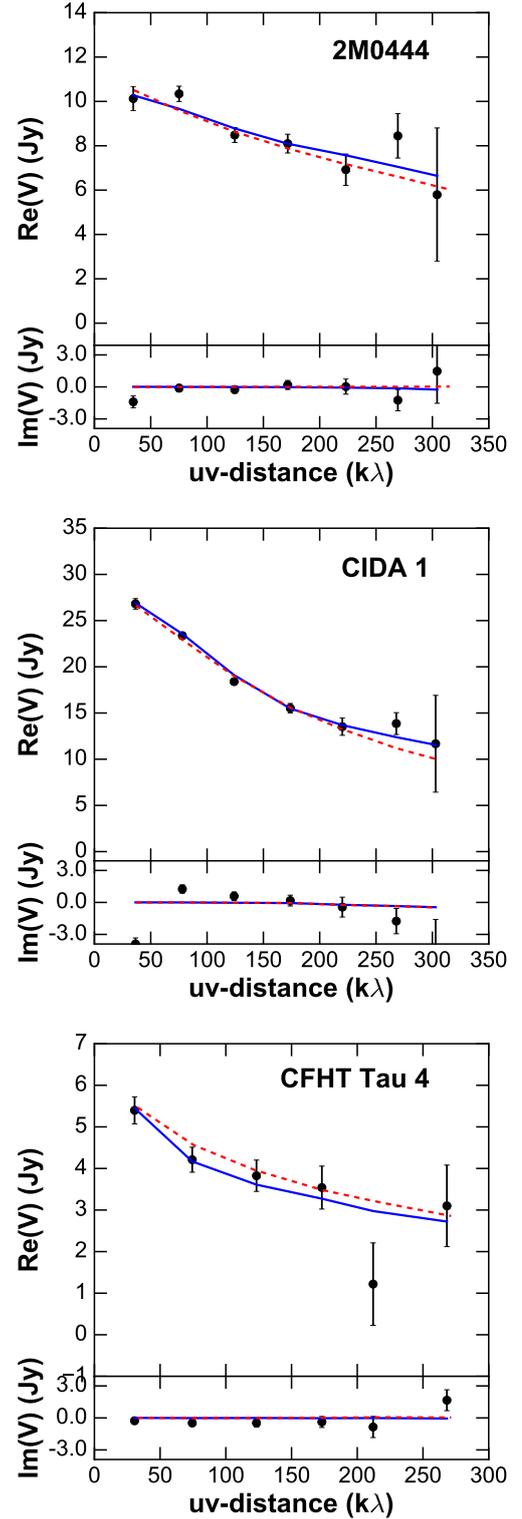


Fig. B.2. Comparison between observed and model visibilities for the model fits of the disks in 2M0444+2512 (top row), CIDA 1 (middle row), and CFHT Tau 4 (bottom row). ALMA data is shown as black circles with errorbars, truncated power law and exponentially tapered models with blue and red lines, respectively, as in Fig. 3.