Detection and measurement of micrometeoroids with LISA Pathfinder

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ABSTRACT

The Solar System contains a population of dust and small particles originating from asteroids, comets, and other bodies. These particles have been studied using a number of techniques ranging from in-situ satellite detectors to analysis of lunar microcraters to ground-based observations of Zodiacal light. In this paper, we describe an approach for using the LISA Pathfinder (LPF) mission as an instrument to detect and characterize the dynamics of dust particles in the vicinity of Earth-Sun L1. Launched on Dec. 3rd, 2015, LPF is a dedicated technology demonstrator mission that will validate several key technologies for a future space-based gravitational-wave observatory. The primary science instrument aboard LPF is a precision accelerometer which we show will be capable of sensing discrete momentum impulses as small as $4 \times 10^{-8}$ N s. We then estimate the rate of such impulses resulting from impacts of micrometeoroids based on standard models of the micrometeoroid environment in the inner solar system. We find that LPF may detect dozens to hundreds of individual events corresponding to impacts of particles with masses $>10^{-9}$ g during LPF’s roughly six-month science operations phase in a 5 $\times$ 10$^5$ km by 8 $\times$ 10$^5$ km Lissajous orbit around L1. In addition, we estimate the ability of LPF to characterize individual impacts by measuring quantities such as total momentum transferred, direction of impact, and location of impact on the spacecraft. Information on flux and direction provided by LPF may provide insight as to the nature and origin of the individual impact and help constrain models of the interplanetary dust complex in general. Additionally, this direct in situ measurement of micrometeoroid impacts will be valuable to designers of future spacecraft targeting the environment around L1.

Key words. meteorites, meteors, meteoroids – instrumentation: miscellaneous

1. Introduction

Our current understanding of the interplanetary dust complex is informed by a number of measurement techniques including photographic and visual meteors (Halliday et al. 1984; Hawkes 2007; Trigo-Rodríguez et al. 2008), radio meteors, atmospheric collections (Flynn 1994), observation of Zodiacal light in thermal (Krick et al. 2012) and visual (Levasseur-Regourd & Dumont 1980) wavelengths, in-situ penetration and ionization detectors (Weidenschilling 1978; Zhang & Kessler 1995), and analysis of microcraters in lunar samples (Allison & McDonnell 1982).

Additionally, NASA’s Stardust mission (Hörz et al. 2006) and ESA’s Rosetta mission (Rotundi et al. 2015) have made in situ measurements of the dust environments near the comets Wild 2 and 67/Churyumov-Gerasimenko respectively. The combined picture from all of these techniques, each with varying ability to detect and characterize various sub-populations of the dust complex, is used to constrain theoretical models that account for the sources, sinks, and dynamics of the dust complex.

The LISA Pathfinder (LPF) mission (Armano et al. 2015), is a technology demonstration mission dedicated to validating several key technologies for a future space-based observatory (Bender & Danzmann 1998; Jennrich 2011) of astrophysical gravitational waves (Einstein 1918; Bondi et al. 1959). Led by the European Space Agency with contributions from NASA and a number of European research institutions, LPF consists of a single spacecraft operating in a 5 $\times$ 10$^5$ km by 8 $\times$ 10$^5$ km Lissajous orbit around the first Sun-Earth (L1) lagrange point. LPF was launched on December 3rd, 2015 and will begin science operations in early 2016 and continue for approximately six months with a possible extension of an additional six months. In this paper, we outline an approach for using LPF as an instrument to detect and characterize interplanetary dust in the vicinity of L1. This technique does not require any modification to the hardware or operations of LPF and may provide an important new source of information to constrain models of the dust complex.

The outline of the paper is as follows. In Sect. 2 we describe the working principle of the LPF instrument and its application as a dust detection instrument. In Sect. 3 we make a simple estimate for the detection threshold of LPF as a function of transferred momentum using a simplified 1D model. In Sect. 4 we estimate the rates of events above this threshold and the total number of likely events during the LPF mission. In Sect. 5 we estimate the precision with which LPF will measure parameters of individual impacts such as momentum transferred and direction of impact. In Sect. 6, we summarize our results and outline likely avenues for refining the estimates made here.

2. Overview of technique

Inside the LPF are two inertial sensor units each containing a test mass comprised of a 46 mm cube of Au-Pt alloy with a mass...
of 1.96 kg. During launch and cruise, these test masses are mechanically supported by a lock mechanism, which is retracted prior to beginning science operations leaving the test masses freely-falling inside the inertial sensors with no mechanical contacts. Each inertial sensor unit measures the position and attitude of its respective test mass relative to the LPF spacecraft in all six rigid-body kinematic degrees-of-freedom (DoFs) using a capacitive sensing system. The inertial sensor unit can apply forces and torques to the test mass via electrostatic actuation. Additional information is provided by a laser interferometer that measures a three of DoFs (position, tip, and tilt) with higher precision and a star tracker which measures the three angular DoFs of the spacecraft relative to a background inertial reference frame. A control system converts the position and attitude measurements from the two inertial sensors, the interferometer, and the star tracker into force and torque commands that are applied to the test masses and the spacecraft, the latter being actuated using a microthruster system.

The main purpose of the control system is to reduce external force disturbances on the test masses; low-disturbance reference masses are a key technology for LISA-like instruments. A byproduct of this effort is an exquisite measurement of external force disturbances on the LPF spacecraft either through the residual motion between the spacecraft and the test masses or in the applied control forces and torques. One such source of external force disturbance is an impulse generated by an impact of a micrometeoroid or dust particle. In the following sections, we estimate the detection threshold and rate for such impact events.

3. Detection threshold

The momentum transferred to the LPF spacecraft by an individual micrometeoroid impact will combine with stochastic disturbances on the spacecraft from a number of sources such as Solar radiation pressure, outgassing, and noise from the microthruster system. The measured momentum transfer will also be effected by noise in the position sensing system and force disturbances on the test masses. To simplify our estimate of the threshold at which LPF can detect an individual impact, we consider a simplified one-dimensional model in a linear DoF. We adopt the maximum-likelihood formalism, where the signal-to-noise ratio (S/N) of an event is defined using a noise-weighted inner-product:

\[ \rho^2 = \langle F|F \rangle, \]

where \( \rho \) is the S/N, \( F \) is the “waveform” of the force on the spacecraft resulting from the impact and \( \langle \ldots | \ldots \rangle \) denotes the noise-weighted inner product defined as:

\[ \langle a|b \rangle \equiv 4\pi \int_{-\infty}^{\infty} \frac{\delta(t) \delta^*(f)}{S_n(f)} df, \]

where \( \delta(t) \) denotes Fourier-domain signals and \( S_n(f) \) is the one-sided power-spectral density of the equivalent force noise on the spacecraft. Given a waveform \( F \) and an estimate of the noise characterized by \( S_n(f) \), the S/N can be calculated using (2) and (1). An S/N threshold for detection, typically set around 5–10 to optimize the balance between high detection efficiency and low false alarm probability (Lehmann & Romano 2008), can be used to determine whether an individual event is likely to be observed.

While the error budget developed for LPF contains dozens of individual effects that contribute equivalent force noise to the test masses and spacecraft, there are two effects that dominate force noise on the spacecraft in the measurement band 0.1 mHz \( \leq f \leq 100 \) mHz. The first is the noise of the microthruster system itself, which is characterized by a flat power spectral density with a level of

\[ S_n \approx 10^{-16} \text{N}^2/\text{Hz}. \]

This provides us with a waveform parametrized by two parameters, total momentum transferred \( P \) and impact time \( \tau \). Using the expression for \( \tilde{F}(f) \) in (7) and a generic total equivalent force noise of the form \( S_n(f) = S_0 + S_a f^4 \), the formula for S/N in (1) can be used to determine the S/N as a function of \( P \):

\[ \rho = \frac{P}{P_c}, \]

\[ P_c = \frac{1}{\sqrt{2\pi}} (4S_0 S_a^3)^{1/8} \]

\[ \text{where } S_0 \] is the one-sided power-spectral density at a level of 1 mHz by the equivalent force noise of the inertial sensor. The inertia sensor noise is characterized by a flat displacement amplitude spectral density at a level of \( \sim 2 \) mHz. This can be converted to an equivalent force noise on the spacecraft by multiplying by the spacecraft mass (\( M = 422 \) kg) and taking two time derivatives. The resulting power spectral density of this equivalent spacecraft force noise from the inertial sensor is given by

\[ S = \left( \frac{2 \times 10^{-9} \text{m/Hz}^{1/2}}{f} \right)^2 \cdot \frac{M}{2\pi f^2} \cdot \frac{M}{2\pi f^2} \]

\[ = 1.1 \times 10^{-9} \cdot f^4 \text{N}^2/\text{Hz}. \]

The individual and combined components of the spacecraft equivalent force noise are shown in Fig. 1.

An impact by a micrometeoroid is modeled as an impulsive force occurring at time \( \tau \) and imparting a total momentum \( P \) over a characteristic timescale \( \Delta \). This can be written in the time and frequency domains respectively as:

\[ F(t) = \frac{P}{\Delta} \left[ \Theta(t-\tau) - \Theta(t-\tau-\Delta) \right], \]

\[ \tilde{F}(f) = \frac{Psinc(f\Delta)e^{-2\pi if\Delta/2}}{1 - f^2/\pi^2}. \]

where \( \Theta(t) \) is the Heaviside step function, and \( sinc(x) \equiv \sin(x)/\pi x \) is the normalized sine cardinal function. One would generally expect that the characteristic impulse times for micrometeoroids would be small compared to the standard sampling rate for LPF data of 1 Hz. In this limit,

\[ \lim_{\Lambda \to 0} F(t) = P \cdot \rho \cdot e^{-2\pi if\tau}. \]

This provides us with a waveform parameterized by two parameters, total momentum transferred \( P \) and impact time \( \tau \). Using the expression for \( \tilde{F}(f) \) in (7) and a generic total equivalent force noise of the form \( S_n(f) = S_0 + S_a f^4 \), the formula for S/N in (1) can be used to determine the S/N as a function of \( P \):

\[ \rho = \frac{P}{P_c}, \]

\[ P_c = \frac{1}{\sqrt{2\pi}} (4S_0 S_a^3)^{1/8} \]
where \( P_c \) is the characteristic threshold momentum. For the case described above of \( S_0 = 10^{-16} \text{N}^2/\text{Hz} \) and \( S = 1.1 \times 10^{-9} \text{N}^2/\text{Hz} \), the characteristic momentum \( P_c \approx 3.6 \times 10^{-8} \text{N} \). For an event to be detected with \( \rho \geq 8 \), the total momentum must be \( P \geq 8P_c \approx 2.9 \times 10^{-7} \text{N} \). For detection with LPF, the mass distribution of the micrometeoroids in the inner Solar system is derived primarily from the collisional processing of asteroids and comets. The particles making up this population are mostly small, with a size distribution that is not well known. The LPF spacecraft is likely to encounter. The MEM takes as input a state vector describing the orbit of a spacecraft and returns the total flux and velocity distribution of impacts for particles having a mass \( m \geq 10^{-6} \text{g} \). Because the MEM concentrates on these higher-mass events, which are more rare, it is not by itself useful in determining the number of the events likely to be detected by LPF. However, we can use the MEM to provide an improved estimate of the distribution of impact velocities under the assumption that this distribution is roughly constant as we extend to lower masses. Using a representative state vector for the LPF science orbit provided by ESA, the MEM was used to produce the velocity distribution in Fig. 3. The MEM results are reasonably well fit by a normal distribution with a mean velocity of \( \bar{v} = 21.4 \text{ km s}^{-1} \) and a standard deviation of \( \sigma_v = 9.7 \text{ km s}^{-1} \).

Combining the mass flux from the Grün model and the velocity distribution from Fig. 3 produces the impact flux as a function of particle momentum in Fig. 4. Note that for a threshold momentum of \( 8P_c = 1.7 \times 10^{-5} \text{N} \), the predicted event rate assuming a 3 m² area is approximately 3 \times 10^2 events per year, about 2.5 times higher than the simple prediction in (10). This increase is due to detections of the high-velocity tail of the lighter particles, which are more numerous.

An improved treatment of the event rate would include a geometrical model for the LPF spacecraft and its orientation as well as any correlations between impact mass and impact velocity.
### Table 1. Envisioned meteoroid streams contributing to the meteoroid flux in the L1 Lagrange point, and listed from their January to December appearance periods.

<table>
<thead>
<tr>
<th>Meteoroid stream</th>
<th>Parent Body</th>
<th>Type</th>
<th>$e$</th>
<th>q (AU)</th>
<th>$v_g$ (km s$^{-1}$)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Quadrantids</td>
<td>2003 EH1</td>
<td>Ann. show and dust trails</td>
<td>0.989</td>
<td>0.141</td>
<td>41</td>
<td>Jenniskens (2006)</td>
</tr>
<tr>
<td>April Lyrids</td>
<td>C/1861 G1 Thatcher</td>
<td>Ann. show and dust trails</td>
<td>0.921</td>
<td>0.921</td>
<td>47</td>
<td>Jenniskens (2006)</td>
</tr>
<tr>
<td>Eta Aquariids</td>
<td>1P/ Halley</td>
<td>Ann. show and dust trails</td>
<td>0.968</td>
<td>0.662</td>
<td>67</td>
<td>Christou et al. (2008)</td>
</tr>
<tr>
<td>Tau Herculis</td>
<td>73P/Schwassmann -Wachmann 3</td>
<td>Dust trail: May 31, 2017 event produced by trail</td>
<td>?</td>
<td>0.97</td>
<td>15</td>
<td>Jenniskens (2006) (Table 6g)</td>
</tr>
<tr>
<td>Perseids</td>
<td>109P/ Swift-Tuttle</td>
<td>Ann. Show; and dust trail</td>
<td>Aug 11, 2016</td>
<td>0.951</td>
<td>0.948</td>
<td>60</td>
</tr>
<tr>
<td>Kappa Cygnids</td>
<td>Unknown</td>
<td>Ann. show</td>
<td>0.763</td>
<td>0.980</td>
<td>23</td>
<td>Jenniskens (2006)</td>
</tr>
<tr>
<td>Taurids</td>
<td>2P/ Encke</td>
<td>Ann. show</td>
<td>0.833</td>
<td>0.35</td>
<td>28</td>
<td>Jenniskens (2006)</td>
</tr>
<tr>
<td>Leonids</td>
<td>55P/Tempel-Tuttle</td>
<td>Ann. show and dust trails</td>
<td>0.918</td>
<td>0.985</td>
<td>72</td>
<td>Jenniskens (2006)</td>
</tr>
<tr>
<td>Geminids</td>
<td>3200 Phaeton</td>
<td>Ann. show</td>
<td>0.898</td>
<td>0.141</td>
<td>34</td>
<td>Jenniskens (2006)</td>
</tr>
<tr>
<td>Ursids</td>
<td>8P/ Tuttle</td>
<td>Ann. Show; and dust trail</td>
<td>Dec 22nd, 2016 event produced by young filament (outwards towards Earth orbit)</td>
<td>0.961</td>
<td>0.947</td>
<td>33</td>
</tr>
</tbody>
</table>

**Notes.** The listed streams are probably contributing with old meteoroids forming the annual shower plus some punctual encounters with young dust trails (the year indicated for each trail corresponds with the year of perihelion in which it was created). Known dust trail events are listed, indicating in bold the most favorable ones. Eccentricity ($e$) and perihelion distance (q) are also given from Jopek et al. (2003, 2010). $v_g$ indicates the geocentric velocity relative to the Earth which roughly corresponds to the impact velocity.

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**Fig. 4.** Flux of LPF particle impacts with transferred momenta $P \geq P_0$ estimated using the Grün model mass flux in Fig. 2 and the fit to the MEM-derived velocity distribution in Fig. 3.

In addition to the “average” micrometeorite flux estimated using the Grün and MEM models, LPF may also experience episodic increases in flux when LPF’s orbit intersects asteroidal dust trails or cometary meteoroid showers. In principle, any evolved meteoroid stream on Earth having a significant cross section is a potential generator of dust in the L1 environment because the stream cross section increases over time and their meteoroids cross the Earth’s orbit and its surroundings. The most famous annual showers like the Geminids or the Perseids have activity periods on Earth of a week or even more, so they are extended enough to be contributing to L1 (assuming that their activity periods provide a reasonable diameter for the meteoroid stream cross sections). Table 1 compiles our first-guess meteoroid streams contributing significantly to increase the meteoroid flux around the L1 Lagrange point, but the list is not exhaustive. Some old annual showers like the Lyrids, Perseids, Kappa Cygnids or Ursids have perihelion distances close to the L1 Lagrange point and are potential, but probably weak, meteoroid contributors. Obviously, the casual occurrence of dense dust trails is also possible from some periodic comets like e.g. 55P/Tempel-Tuttle that generate the Leonid storms Beech et al. (1999), but they are not expected trail to cross the Earth up to 2033 due to planetary perturbations Jenniskens (2006). Consequently, Table 1 shows that the most favorable dust trail
encounter to be detected by LPF is the August 11, 2016 Perseid event produced by the 1862 dust trail of comet 109P/Swift-Tuttle Jenniskens (2006). Another good chance of detecting a high meteoroid flux associated with a dust trail, if LPF operations are finally extended up to mid-2017, could be that associated with comet 73P/Schwasmann-Wachmann 3 (see Tau Herculis in Table 1).

5. Parameter estimation

A key feature of LPF as a micrometeoroid instrument is its ability to estimate certain dynamical parameters for each detection. For example, each LPF test mass will measure the transferred linear momentum from the impact in three orthogonal directions. The error of in the estimate of each of these momentum components will be $\sim r^{-1}$ where $r$ is the S/N defined in (8). Under the assumption that the error in each momentum component is independent, the two angles describing the impact direction will be measured with errors of roughly

$$\sigma_{\phi} \sim \sigma_{\theta} \sim \sqrt{3} r^{-1}. \quad (11)$$

For example, an event with $r = 10$ will have typical errors in the impact angles of 0.17 rad $\approx 10^\circ$. Knowledge of the direction of the impact combined with an ephemeris for LPF will allow reconstruction of the impactor’s orbit, a key piece of information for distinguishing different populations of micrometeoroids. For example, it may be possible to measure an excess of impacts coming from a particular direction that could be associated with a known comet. This would allow the velocity of the impact to be inferred from the ephemerides of LPF and the comet which would in turn allow an estimate of the mass of each impacting particle from the measured momentum transfer.

LPF will also measure three components of the angular momentum transferred to the spacecraft. To estimate the noise floor for angular DoF, we follow a similar procedure to the analysis in Sect. 3. The angular sensing noise of the LPF inertial sensor units is characterized by a flat spectrum with an amplitude spectral density of $\sim 200 \text{nrad/Hz}^{1/2}$. This can be converted into an equivalent torque noise by multiplying by the spacecraft moment of inertia $\sim 200 \text{kgm}^2$ and taking two time derivatives. The resulting power spectral density of the equivalent torque noise is

$$S_{\text{Nas}} \approx \left[ \left( 2 \times 10^{-7} \text{rad/Hz}^{1/2} \right) \cdot I \cdot (2\pi f)^2 \right]^2 = 2.5 \times 10^{-6} \cdot f^4 N^2 \cdot m^2 \cdot Hz^5. \quad (12)$$

The equivalent torque noise of the micropropulsion system can be estimated by multiplying the force noise by a characteristic “lever-arm” corresponding to the perpendicular distance between the spacecraft center of mass and a line along the thrust vector passing through the thruster mounting point. A rough estimate of this value is 0.5 m based on the physical dimensions of the LPF spacecraft. This gives an equivalent torque noise of $S_{\text{Nth}} \approx 2.5 \times 10^{-17} N^2 \cdot m^2 / \text{Hz}^2$. Figure 5 shows the power spectral density of the total equivalent torque noise for this simplified model.

The characteristic angular momentum for LPF can then be computed using (8) with $S_{\theta} = 2.5 \times 10^{-17} \text{N}^2 \cdot m^2 / \text{Hz}^2$ and $S_{\phi} = 2.5 \times 10^{-6} \cdot f^4 N^2 \cdot m^2 / \text{Hz}^5$. The result is $L_c = 5.6 \times 10^{-8} \text{N} \cdot \text{m}$. The typical errors on impact location can then be estimated as

$$\sigma_r = r^{-1} \frac{L_c}{P_c} = r^{-1} 1.6 \text{ m} \quad (13)$$

A $\rho = 10$ event would have typical localization errors of $\sim 16 \text{ cm}$. A more detailed reconstruction of the impact location would include a mechanical model of the spacecraft and might improve the impact localization somewhat. While the impact location is not as useful a measurement for studying the micrometeoroid population as the total momentum or impact direction, it may be of interest to LPF’s operations team.

6. Discussion

The next logical step in this research effort is to refine the estimates made here, taking advantage of the detailed information available about the LPF spacecraft and additional nuances of the known or modeled micrometeoroid environment. Examples of improvements in the LPF model might include proper modeling of the noise and noise correlations in the inertial sensor and thruster subsystems, including the second inertial sensor as a quasi-independent sensor, and an improved rate estimate including a geometrical model of the LPF spacecraft and its orientation during the science operations.

Modifications to the micrometeoroid flux model might include recent radar data (Janches et al. 2015) that indicate a bimodal distribution of velocities in which the fraction of high-velocity meteoroids peaking at 50–60 km s$^{-1}$. If such a high-velocity population exists in the vicinity of L1, it would extend LPF’s detection capability to lower mass particles and further boost the detection rate. Similarly, micrometeoroids coming from high-eccentricity cometary orbits collide at higher velocity than the asteroidal one, so the momentum transferred will be higher and the threshold for mass detection will be lower. We think that such capability to compute the flux from the cometary source and its possible fine-structure associated with the disintegration of periodic comets may also be of interest.

In addition to improving estimates of detection thresholds, event rates, and parameter estimation capabilities, an analysis pipeline could be developed that would detect and characterize events from a stream of LPF science data. Techniques that have already been developed for the analysis of data from ground- and space-based gravitational wave detectors would likely be applicable to this problem.

7. Conclusion

We have outlined a concept for using the LPF spacecraft as an instrument for studying the micrometeoroid environment in the vicinity of Earth-Sun L1 and made rough estimates of the
detection threshold, event rates, and errors with which physical parameters are likely to be measured. These estimates suggest that LPF should be capable of detecting dozens to hundreds of individual events during its operational lifetime and will measure their individual momenta, impact directions, and impact locations with interesting precision.

LPF represents a unique and novel opportunity to make in-situ measurements of the micrometeoroid environment in the vicinity of L1, a region for which no in-situ measurements exist. Such measurements can be used to constrain models of the micrometeoroid population in the inner solar system and will complement existing measurements using other techniques. Our proposed method requires no modification to LPF’s hardware or operations, it simply requires a dedicated analysis of the data that will be collected as part of normal science operations.

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References

Christou, A. A., Vaubaillon, J., & Withers, P. 2008, Earth Moon and Planets, 102, 125
Einstein, A. 1918, Sitzungsberichte der Königlich Preussischen Akademie der Wissenschaften (Berlin), Seite 154-167, 154
Flyn, G. J. 1994, Planetary and Space Science, 42, 1151
Halliday, I., Blackwell, A. T., & Griffin, A. A. 1984, Science, 223, 1405
Hawkes, R. 2007, Earth, Moon, and Planets, 101, 93
Hörz, F., Bastien, R., Börg, J., et al. 2006, Science, 314, 1716
Jenrich, O. 2011, LISA: Unveiling a hidden Universe
McNamara, H., Jones, J., Kauffman, B., et al. 2004, Earth, Moon, and Planets, 95, 123