Multiwavelength active-optics Shack-Hartmann sensor for monitoring seeing and turbulence outer scale

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ABSTRACT

Context. Real-time seeing and outer-scale estimation at the location of the focus of a telescope is fundamental for predicting the adaptive-optics system’s dimensioning and performance, as well as for the operational aspects of instruments.

Aims. This study attempts to take advantage of multiwavelength long-exposure images to instantaneously and simultaneously derive the turbulence outer scale and seeing from the full width at half maximum (FWHM) of seeing-limited images taken at the focus of a telescope. These atmospheric parameters are commonly measured in most observatories by different methods located away from the telescope platform, thus differing from the effective estimates at the focus of a telescope, mainly because of differences in pointing orientation, height above the ground, or local seeing bias (dome contribution).

Methods. Long-exposure images can either be provided directly by any multiwavelength scientific imager or spectrograph or, alternatively from a modified active-optics Shack-Hartmann sensor (AOSH). From measuring the AOSH sensor spot point spread function FWHMs at different wavelengths, one can estimate the instantaneous outer scale in addition to seeing.

Results. Multipwavelength long-exposure images provide access to accurate estimates of $r_0$ and $L_0$ by adequate means as long as precise FWHMs can be obtained. Although AOSH sensors are specified to measure not spot sizes but slopes, real-time $r_0$, and $L_0$ measurements from spot FWHMs can be obtained at the critical location where they are needed with major advantages over scientific instrument images: insensitivity to the telescope field stabilization, and continuous availability.

Conclusions. Assuming an alternative optical design that allows simultaneous multiwavelength images, the AOSH sensor benefits from all the advantages of real-time seeing and outer scale monitoring. With the substantial interest in the design of extremely large telescopes, such a system could be of considerable importance.

Key words. atmospheric effects – instrumentation: adaptive optics – site testing – methods: numerical

1. Introduction

Atmospheric seeing is commonly measured by the differential image motion monitor (DIMM, Sarazin & Roddier 1990) in most observatories, or by means of alternative seeing monitors, e.g., Generalized Seeing Monitor (GSM, Ziad et al. 2000), Multi-Aperture Scintillation Sensor (MASS, Kornilov & Tokovinin 2001). Since it is localized away from the telescope platform, the DIMM delivers a seeing estimate that can differ significantly from the effective seeing as seen at a telescope focus because of pointing orientation and/or differences in height above the ground, or local seeing bias (dome contribution). The effect of the two last will substantially expand in the next generation of telescopes: the extremely large telescopes (ELTs).

Evaluating the seeing is paramount for selecting astronomical sites and/or following their temporal evolution. Likewise, its estimation is fundamental for dimensioning adaptive optics (AO) systems and their performance predications. In this context, the outer scale of the turbulence, related as the distance over which the spatial power spectral density of phase distortions deviates from the pure $5/3$ power law at low frequencies (associated with the Kolmogorov-Obukhov turbulence model), plays a significant role in AO systems. In particular, the power in the lowest Zernike aberration modes (e.g., tip and tilt) is strongly affected, and the knowledge of reliable estimate of $L_0$ is of considerable importance in the future area of the ELTs. As a consequence, knowledge of both seeing and $L_0$ virtually drive instrument designs or operational aspects at a telescope, and more emphasis is put on developing accurate real-time seeing and outer scale monitors at the focus of a telescope.

For this purpose, various flavors of images can be used at the critical location of the telescope focus: (1) scientific instrument images; (2) guide-probe images; and (3) active-optics Shack-Hartmann images. At the VLT (the Very Large Telescope at the ESO Paranal observatory), focal planes are equipped with an arm used for acquiring of a natural guide star. The light from this star is then split between a guide probe for an accurate tracking of the sky, and a Shack-Hartmann wavefront sensor used by the active-optics to control the shape of the primary mirror. In this context, estimating the seeing from the full width at half maximum (FWHM) of a PSF strongly relies on the exposure time that must be long enough so that the turbulence has been averaged (ensuring that all representations of the wavefront spatial scales have passed through the pupil). This depends on telescope diameter and turbulence velocity, though it is commonly admitted that 30 s is the proper average of the turbulence and that significant FWHM biases would otherwise be introduced. Since the guide probe has exposure times that are no longer than 50 millisecond, it cannot be used as a seeing/outer scale monitor. The active-optics Shack-Hartmann (AOSH) sensor includes all the advantage of real-time monitoring of these turbulence parameters. While most of the instruments are affected...
by observational bias (unavailability for a wide range of seeing conditions) and are affected by the telescope field stabilization. AOSH delivers continuous real-time images of long-exposure-spot PSFs (typically 45 s) at the same location as do scientific instruments. AOSH images simultaneously provide various data: slopes, intensities, and spot sizes. When short exposures are used, the information provided by both slopes and intensities (i.e., scintillation) can be used to retrieve $Cn^2$ profile using correlations of these data from two separated stars (Robert et al. 2011; Voyez et al. 2013). When long exposures are used, it is feasible to retrieve the atmospheric seeing in the line of sight from the spot sizes in the sub-apertures, with the advantage of being insensitive to the telescope field stabilization (Martinez et al. 2012). While in most observatories the trend is to compare instrument image quality to DIMM or telescope guide camera FWHM measurements of the seeing in order to estimate $L_0$ (e.g., Floyd et al. 2010), in this paper, we propose to use the AOSH sensor system of the telescope as a turbulence monitor to provide accurate seeing estimation directly at the telescope focus, with the additional measurement of the instantaneous turbulence outer scale $L_0$ through multilengthscale exposures. For this purpose, an alternative optical configuration of the AOSH system is proposed, and the accuracy of seeing and $L_0$ estimation is analyzed through extensive simulations.

2. Analytical treatment

2.1. Long-exposure seeing-limited PSF

The theoretical expression of a long-exposure seeing-limited PSF can be described through the Fourier transform (FT) of its optical transfer function (OTF). The OTF is obtained by multiplying the telescope OTF, denoted $T_0(f)$, by the atmospheric OTF:

$$T(f) = \exp\left[-0.5D_0(\lambda f)\right],$$

(1)

where $f$ is the angular spatial frequency, $\lambda$ the imaging wavelength, and $D_0(f)$ the phase structure function (Goodman 1985; Roddier 1981). Equation (1) is appropriate to any turbulence spectrum and any telescope diameter.

The standard theory based on the Kolmogorov-Obukhov model (Tatarskii 1961) provides the analytic expression for the phase structure function and is expressed by

$$D_0(r) = 6.88 \left(\frac{r}{r_0}\right)^{5/3}.$$  

(2)

This theory describes the shape of the atmospheric long-exposure PSF by a single parameter, the Fried’s coherence radius $r_0$ (Fried 1966), and the long-exposure OTF is expressed as

$$T(f) = T_0(f) \times \exp\left[-3.44(\lambda f r_0)^{5/3}\right].$$  

(3)

In the case of a large ideal telescope with diameter $D \gg r_0$, the diffraction term $T_0$ can be neglected. However, it is commonly accepted that Eq. (3) assumes non-realistic behavior of the low-frequency content of the turbulence model phase spectrum, and it is firmly established that the phase spectrum deviates from the power law at low frequencies (Ziad et al. 2000; Tokovinin et al. 2007). This behavior is described in a first order by an additional parameter, the outer scale $L_0$. This additional parameter is introduced by the Von Kármán ($vK$) turbulence model (e.g., Tatarskii 1961; Ziad et al. 2000), and the mathematical definition of $L_0$ is given by

$$W_0(f) = 0.0229 \left(\frac{r_0}{\lambda}\right)^{5/3} \left(\frac{f^2 + L_0^{-2}}{1 + L_0^{-2}}\right)^{-11/6},$$

(4)

where $W_0(f)$ represents the phase distortions. In this context, the Kolmogorov-Obukhov model corresponds to $L_0 = \infty$, and in the $vK$ model $r_0$ describes the high-frequency asymptotic behavior of the spectrum. Physically, $L_0$ is related to the largest size of perturbations, and corresponds to a reduction in the low-frequency content of the phase perturbation spectrum. Nonetheless, the $vK$ is not a verified model. It is established that the phase spectrum does deviate from a power law, and existing experimental data on $L_0$ are interpreted in this sense. The value of $L_0$ does not depend on wavelength, and typical values are on the order of 20 m with a scatter that can be as large as a few hundred meters (Ziad et al. 2000; Tokovinin et al. 2007).

In the $vK$ model, the expression for the phase structure function ($D_0$) with finite outer scale $L_0$ can be found in Tatarskii (1961) or Tokovinin (2002):

$$D_0(r) = \frac{\Gamma(11/6)}{2^{11/6} \pi^{5/3}} \left[2^{2/3} \left(\frac{6}{5}\right)^{5/6} \left(\frac{r}{L_0}\right)^{-5/3}\right] \times \left[2^{-1/6} \Gamma \left(\frac{5}{6}\right) - \frac{2\pi r}{L_0} K_{5/6} \left(\frac{2\pi r}{L_0}\right)\right].$$

(5)

where $K_{5/6}(x)$ is the modified Bessel function of the third kind, and $\Gamma(x)$ is the gamma function. Putting the $vK$ phase structure function into Eq. (3), we obtain the atmospheric long-exposure OTF expression, which now depends on both $r_0$ and $L_0$. While it is understood that for finite $L_0$, Eq. (3) does not go to zero at high spatial frequencies (the FT of $T_0(f)$ formally does not exist), but when $r_0 \ll L_0$, it can be neglected.

2.2. Seeing, outer scale, and FWHM

The Kolmogorov-Obukhov model predicts dependence of the PSF FWHM on wavelength $\lambda$ and $r_0$:

$$\varepsilon_0 = 0.976 \frac{\lambda}{r_0}.$$  

(6)

However, because the outer scale of turbulence $L_0$ describes the low-frequency behavior of the turbulence model phase spectrum, it plays a significant role in the image FWHM at the focus of a telescope. The image FWHM is different, and the difference can be as much as 30% to 40% in the near-infrared, from the atmospheric seeing that can be measured by dedicated seeing monitors, such as the DIMM (Sarazin & Roddier 1990).

The seeing measured by the DIMM is sensitive to small-scale wavefront distortions, and thus provides estimates that are almost independent of the outer scale of the turbulence $L_0$. The dependence of atmospheric long-exposure resolution on $L_0$ is efficiently predicted by a simple approximate formula (Eq. (7)) introduced by Tokovinin (2002) and confirmed by means of extensive simulations (Martinez et al. 2010b,a), where it is emphasized that the effect of finite $L_0$ is independent of the telescope diameter. The validity of Eq. (7) has been established in an $L_0/r_0 > 20$ and $L_0/D \leq 500$ domain (Martinez et al. 2010b), where $D$ is the telescope diameter (the treatment of the diffraction failed for small telescope diameters, $D < 1$m). As a consequence, long-exposure seeing-limited PSF FWHM ($\varepsilon_{vK}$) are directly related to $\varepsilon_0$ (or alternatively $r_0$) and $L_0$ as

$$\varepsilon_{vK} \approx \varepsilon_0 \sqrt{1 - 2.183(r_0/L_0)^{0.536}}.$$  

(7)

Deducing the atmospheric seeing $\varepsilon_0$ from the FWHM of a long-exposure, seeing-limited PSF at the focus of a telescope requires the correction implied by Eq. (7) with either the knowledge of $L_0$ (simultaneously measured by any means) or the correction by an
a priori $L_0$ value selected from a long-term monitoring of the observational site (usually the median value is retained, e.g., $L_0 = 22$ m at Paranal), prior to airmass and wavelength correction. It is trivial to see that these two parameters ($\varepsilon_0$, or alternatively $r_0$, and $L_0$) cannot be simultaneously deduced from a single long-exposure seeing-limited PSF FWHM (i.e., a single wavelength exposure provide a unique FWHM estimate, while two parameters are undetermined).

2.3. Multiwavelength FWHMs

A straightforward way to solve the indetermination is to consider a multiwavelength FWHM measurement. In the following, and for the sake of generality, $n$ measurements will be assumed, while only two are required to resolve the current problem. In the context of $n$-wavelength, long-exposure seeing-limited PSF FWHM measurements, Eq. (7) can be formalized as

$$
\varepsilon_{\nu K}(\lambda_n) \approx \varepsilon_0 \left(\frac{\lambda_0}{\lambda_n}\right)^{1/5} \times \left[1 - 2.183 \left(\frac{0.976 \times \lambda_0}{\varepsilon_0 \left(\frac{\lambda_0}{\lambda_n}\right)^{1/5} L_0}\right)^{0.356}\right],
$$

where $\lambda_n$ is the wavelength of the exposure considered, $\lambda_0$ is the wavelength of 500 nm, adopted as standard for seeing computation, and $r_0$ has been replaced by $\varepsilon_0$ using Eq. (6). Equation (8) now provides $n$ different $\varepsilon_{\nu K}$ estimations, for two unknown parameters ($\varepsilon_0$ and $L_0$) and can be simplified as:

$$
\varepsilon_{\nu K}(\lambda_n) = A_n^{2/5} \times (\varepsilon_0)^2 - 2.183 \times A_n^{0.328} \times B^{0.356} \times \left(\frac{\varepsilon_0}{L_0}\right)^{1.644},
$$

where $A_n = \lambda_0/\lambda_n$ and $B = 0.976 \times \lambda_0$. Finally, a simple expression can be obtained:

$$
\varepsilon_{\nu K}(\lambda_n) = A_n^{2/5} \times \varepsilon_0^2 - 2.183 \times A_n^{0.328} \times B^{0.356} \times V,
$$

where $U$ and $V$ are equal to $\varepsilon_0^2$ and $\varepsilon_0^{1.644}/r_0^{0.356}$, respectively. A numerical resolution of the system solving for $U$ and $V$ where $n = 2$ can be trivially achieved with a standard singular value decomposition method.

3. Numerical simulations

The schematic representation of the modified AOSH sensor considered to provide two-wavelength images is presented in Fig. 1. It is based on the standard principle of the AOSH except that at a focal plane downstream of the Shack-Hartmann lenslet array, the light from the telescope pupil is focused at the tip of a roof prism, which splits the light into two parts. These two separated beams propagate through different spectral filters. Finally, the incoming light of these two optical arms is dissected by individual lenslet arrays, which then focus the light onto the detector array. The lenslet array creates a number of separated focal spots of light on the detector. As part of the telescope active-optics system, such a system has the advantage of delivering continuously spot images (unaffected by observational bias in contrast to scientific instruments). Retrieving atmospheric seeing $\varepsilon_0$ (at 500 nm) from the FWHM of a unique (single-wavelength) long-exposure seeing-limited PSF image requires the correction implied by Eq. (7) (prior to airmass and wavelength correction). I remind the reader that it even concerns the case of small-size ($d$) AOSH subapertures, where $L_0 \gg d$, and the examination of the $L_0$ influence was also treated (Martinez et al. 2012). Accurate seeing estimation by means of a dedicated algorithm and upon adequate calibration is demonstrated in Martinez et al. (2012). The following sections explain the details of the simulations involved in the study.

3.1. Atmospheric turbulence

The atmospheric turbulence is simulated with hundreds to thousands of uncorrelated phase screens of dimension $4096 \times 4096$ pixels (i.e., 60 m width) to allow long-exposure images ($>30$ s) upon atmospheric conditions. The principle of the generation of a phase screen is based on the standard Fourier approach, where randomized white noise maps are colored in the Fourier space by the turbulence power-spectral-density (PSD) function, and the inverse Fourier transform of an outcome corresponds to a phase screen realization. The validity of the atmospheric turbulence statistic has been verified on the simulated phase screens: the value of the outer scale ($L_0$), Fried parameter ($r_0$), and seeing of the phase screens has been confirmed by

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**Fig. 1.** Principle of the two-wavelength active-optics Shack-Hartmann sensor.
sor spots has been proposed by Tokovinin et al. (2007) and de x-

The algorithm used to extract the FWHM from the AOSH sen-

3.3. Extraction of the FWHM

Simulations are based on a di fff

In Fig. 2, we show an example of the simulated AOSH image

Fig. 2. Simulated AOSH image based on the VLT AOSH geometry.

decomposition on the Zernike polynomials and variance mea-

surements over the uncorrelated phase screens. In addition, the

validity of the long-exposure AOSH image has been verified.

In Fig. 2, we show an example of the simulated AOSH image

(based on the ESO VLT AOSH configuration).

3.2. Shack-Hartmann model

Simulations are based on a diffractive Shack-Hartmann model

that reproduces the VLT AOSH geometry, mimicking the

24 subapertures across the pupil diameter of the VLT active-

optics, with 22 pixels per subaperture, and 0.305” pixel scale

(d = D/24 = 0.338 m). The validity of the AOSH model has

been verified through several aspects, such as the plate scale,

spot sizes, slope measurements, and phase reconstruction. The

AOSH paradigm is presented in Fig. 2. Background estimation

is performed on a corner of the image without spots, and hot

pixels are set to the background. The cleanest and unvignetted

spots are selected in each frame for the analysis. These ex-

tracted spots are oversampled by a factor two, recentered and

averaged. The averaging reduces the influence of potential lo-

cal CCD defects, though these are not included in the simu-

lation. In practice, the averaged spot is based on hundreds of

selected spots. More than 400 spots over 526 available are usu-

ally selected for the analysis. The multiwavelength AOSH sim-

ulator provides four images at four different wavelengths (0.5,

0.55, 0.6, and 0.65 μm), while only two are used and analyzed

(0.5 and 0.55 μm). The choice of the wavelength values used in

simulation is arbitrary, and its optimization is beyond the scope

of the present study. While an optimal combination can cer-

tainly be found by considering system and telescope operational

aspects (e.g., photon noise, bandpasses, subsystem characteris-

tics, and pertaining constraints, etc.), once the wavelengths are

known and corresponding FWHMs correctly estimated, seeing

and outer scale are accurately retrieved regardless of the wave-

length combination selected.

3.3. Extraction of the FWHM

The algorithm used to extract the FWHM from the AOSH sen-

sor spots has been proposed by Tokovinin et al. (2007) and ex-

tensively analyzed in Martinez et al. (2012). It is based on the

long-exposure spot PSF profile defined in Eq. (3). The modu-

lus of the long-exposure optical transfer function of the averaged

spot is calculated and normalized. It is then divided by the square

subaperture diffraction-limited transfer function $T_0(f)$:

$$T_0(f) = (1 - [\lambda f_x/d]) \times (1 - [\lambda f_y/d]).$$  (11)

In the case of a large ideal telescope with diameter $D \gg r_0$, the
diffraction term $T_0$ of Eq. (3) can be neglected, while in the

case of AOSH subapertures of size $d$, it cannot ($d \approx r_0$). At this

case the cut of the $T(f)$ along each axis can be extracted and

fitted to the exponential part of Eq. (3) to derive a single parame-

ter $r_0$, or equivalently, Fourier-transformed to derive the FWHM

of the resulting spot PSF profile using a two-dimensional ellipti-
	ical Gaussian (a Moffat or a 10th-order polynomial fit can be

selected instead). The orientation of the long and small axes

of $T(f)$ is found by fitting it with a two-dimensional elliptical

Gaussian.

3.4. Solving $\epsilon_0$ and $L_0$ from FWHMs

Various methods for solving a set of $n$ linear equations in $n$

unknowns are available, such as least squares fitting or LU

(lower/upper) decomposition. In practice, the standard LU de-

composition has been successfully used to solve our square sys-

tem of linear equations. The programming language is IDL using

the linear algebra library package LAPACK.

4. Results and discussion

4.1. General results

The series of tests conducted to determine the ability of a multi-

wavelength AOSH sensor to sort out seeing and turbulence outer

scale values are twofold: (1) under a specific simulated seeing

condition (0.83”, ESO Paranal observatory median seeing value

as measured by the DIMM at 6 meters height from the ground),

several turbulence outer scale conditions are simulated, and sim-

ulated/estimated parameters can be compared; (2) for a particu-

lar generated turbulence outer scale value, several seeing condi-

tions (ranging from 0.6 to 1.8”) were simulated. Estimated

and simulated parameters were then again compared. This lat-

est test was repeated for two outer scale values (22 and 30 m,

where 22 m is the Paranal observatory median value).

At this stage, two aspects should be pointed out, both related

to the sampling issue. (1) Higher outer scale values than 30 m

cannot in principle be considered because the simulated atmo-

spheric phase screens are physically limited to 60 m width. It

was indeed observed that above roughly 40 m phase screen sides,

the outer scale estimation failed to be accurate. (2) There is a

catch in matching the simulated AOSH sensor to the one of the

VLT: the pixel scale is crude (0.305”), while only two are used and analyzed

(0.5 and 0.55 μm). This has been pointed out in Martinez et al. (2012): seeing estimates under 0.6” failed to be accurate, while probably seeing values above 0.6” are still affected to a certain extent by the effect of undersampling. This point will be discussed further in the Sect. 4.3, where the AOSH geometry is modified (by simulating AOSH sensor with various subapertures configurations but identical telescope pupil footprint in pixel, in order to increase or decrease the pixel sampling, e.g., $6 \times 6, 9 \times 9, 18 \times 18, 24 \times 24$, and $48 \times 48$ subapertures).

Table 1 summarizes the results obtained under various turbu-

lence outer scale values coupled with 0.83” seeing conditions.

Both seeing and outer scale values are estimated well from the

AOSH images. The seeing is accurate at a 10⁻² level, while the

outer scale is fairly estimated with a maximum error margin
of two meters. Table 2 presents the results under various seeing conditions with two outer scale values (22 and 30 m). For the 22 m outer scale set of data, the mean value of the estimated outer scale is 24.5 m with a standard deviation of 7.9 m, while for the 30 m outer scale set of data, the mean value is 28.7 m with a standard deviation of 5.7 m. In all cases, the seeing estimate is fairly good, accurate at a few 10⁻² level. In addition, from Table 2 it is observable that the better the seeing, the worse the outer scale estimates. Increasing the seeing estimate accuracy is therefore fundamental for increasing the accuracy of the outer scale estimation. This is likely due to the outcome of the pixel scale problem, which directly affects the accuracy of the FWHM estimates. This point is addressed in the next section.

4.2. Sensitivity analysis

Precise FWHM estimation from the spot images is mandatory to deliver accurate seeing and outer scale monitoring with the AOSH sensor. This is a major concern for the outer scale estimation more than for the seeing itself. This is observable in Fig. 3 where the impact of a differential error on the calculation of the two FWHMs is appraised. The evaluation of the FWHMs from spot images is not perfect, and some errors are committed during the calculation for various reasons: internal system aberrations, spot under or poor sampling, insufficient signal-to-noise, etc. However, it is likely that this unavoidable amount of error involved in this estimation will apply almost similarly for both wavelength measurements, and the impact on the seeing and outer scale estimates will therefore be small because the errors committed at the two wavelengths will roughly compensate for each other. As a result, only the differential error between the two wavelengths matters. This is precisely what is addressed in the following. Using Eqs. (7) and (10) makes it straightforward to compute the seeing and outer scale values knowing the theoretically corresponding FWHMs at 0.5 and 0.55 μm. The test was done for a 0.83″ seeing and various outer scale values by introducing a small error in the theoretical FWHM at 0.5 μm. The FWHM computed at 0.55 μm is left unaffected. The impact of this error on the resolution of the multiwavelength system (Eq. (10)) is then plotted in Fig. 3, where the impact on the seeing estimate (left) and outer scale estimate (right) are shown.

The impact is not significant for the seeing evaluation, but is for the outer scale. The seeing estimation is mainly affected for low outer scale values (<30 m) and the evolution almost stabilizes for high outer scale values (>100 m). The impact on the outer scale estimate behaves in opposite way. Low outer scale values are less sensitive to FWHM error than high ones. The departure from the expected value (a dashed black line, i.e., with no error) can be significant, and degrades further with the outer scale. While a reasonable differential error in the estimation of the two-wavelength FWHMs has little impact on the seeing estimation, the impact on the outer scale can be considerable. This raises the importance of either developing a dedicated and accurate algorithm to precisely evaluate FWHMs from AOSH sensor spots upon adequate calibration (Martinez et al. 2012) or developing an optimized optical design for the multiwavelength AOSH sensor struggled for high sampling of the spots on the detector.

4.3. Subaperture sampling

The sampling effect is analyzed by modifying the AOSH pattern. While the footprint in pixel of the lenslet array is left unmodified, the number of subapertures is varying to allow changing.
Table 3. Effect of the subaperture sampling on the measured FWHM.

<table>
<thead>
<tr>
<th>AOSH geometry [sub-apertures]</th>
<th>Pixel sampling [&quot;]</th>
<th>Measured FWHM [&quot;]</th>
</tr>
</thead>
<tbody>
<tr>
<td>48 x 48</td>
<td>0.610</td>
<td>0.700</td>
</tr>
<tr>
<td>24 x 24</td>
<td>0.305</td>
<td>0.615</td>
</tr>
<tr>
<td>18 x 18</td>
<td>0.228</td>
<td>0.573</td>
</tr>
<tr>
<td>9 x 9</td>
<td>0.114</td>
<td>0.520</td>
</tr>
<tr>
<td>6 x 6</td>
<td>0.076</td>
<td>0.508</td>
</tr>
</tbody>
</table>

Notes. Seeing is 0.6" and L0 is 22 m. The theoretical FWHM is equal to 0.470" and 0.455" at 0.5 μm and 0.55 μm respectively.

the number of pixels per subaperture. Various configurations are tested (from 6 x 6 to 48 x 48 subapertures), where the FWHMs can be compared to predictions by Eq. (7). The results presented in Table 3 are unambiguous: the higher the sampling, the more accurate the FWHM. Subaperture sampling can only be calibrated but to a certain extent, and the effect is not linear with the seeing. Poor subaperture sampling calibration will not be as efficient as for a mild situation. This is a key aspect in the AOSH parameter space to consider when designing a multiwavelength AOSH system.

5. Conclusion

Although AOSH sensors are specified to measure slopes not spot sizes, the principle of the multiwavelength AOSH sensor was demonstrated and emerges as a potential efficient system for real-time seeing and instantaneous monitoring of turbulence outer scale. It offers direct access to important turbulence parameters at the precise location where we need them (at the focus of the telescope). Multiwavelength AOSH delivers long-exposure PSFs without being affected by any observational bias in contrast to scientific instruments and with being insensitive to the telescope field stabilization.

In addition, the AOSH design as proposed has the advantage of permitting calibration of the internal aberrations present in the system/telescope downstream of the roof prism. It precludes their contribution to the spot FWHMs. The present study shows that accurate estimates of seeing and turbulence outer scale can reasonably be achieved with current systems, while the reliability of such a system can easily be increased with a better sampling of the spot PSFs. Assuming an alternative optical design that allows simultaneous multiwavelength images, the AOSH sensor is a good candidate for monitoring seeing and outer scale, especially in the vicinity of the ELT area.

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