A whole sky study of quasars known population starting from the LQAC-2 compiled catalogue

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Received 12 December 2013 / Accepted 22 February 2014

ABSTRACT

Context. Thanks to huge surveys, such as the Sloan Digital Sky Survey (SDSS), the last decade has shown a dramatic increase in the number of known quasars. In the second release of the general compiled catalogue Large Quasar Astrometric Catalogue (LQAC), 187 504 objects are recorded.

Aims. From this catalogue, we carry out statistical studies dealing with several topics: the astrometric accuracy of the quasars, their spatial location, the distribution of the distance to the closest neighbour, the identification of binary quasars, the completeness of catalogues at a given magnitude and the estimation of the number of quasars expected to be detected by the astrometric space mission *Gaia*.

Methods. We analyse the astrometric improvements brought by the LQAC-2 in terms of equatorial coordinates off-sets. We plot the bi-dimensional spatial distribution of the LQAC-2 quasars according to their equatorial, galactic, and ecliptic coordinates, thus exploring the anisotropy of the distribution. We compare the observed distribution of closest neighbours with the theoretical values based on a Poisson distribution. Moreover, we perform a comparison between two catalogues, the SDSS and the 2dF inside a huge common field. By extrapolating to the whole sky we deduce the number of quasars that will be detected by *Gaia*.

Results. We show how the equatorial, ecliptic, and galactic distribution of recorded quasars is strongly affected by the galactic extinction as well as by the deficiency of detections in the southern hemisphere. In homogenous zones covered by the SDSS survey we identify a significant excess of closest neighbours at short angular distances, with respect to the theoretical estimation, which is caused by the presence of binary quasars. Moreover, we detail the incompleteness of systematic survey catalogues at any magnitude threshold, when comparing two huge surveys such as the SDSS and 2dF. Following this study we deduce the number of quasars detected by *Gaia* under a given magnitude threshold. For $V = 20$, this number should be at least 1 million objects.

Key words. quasars: general – catalogs – astrometry

1. Introduction

In the recent years, the number of recorded quasars has significantly increased. It reached 151 217 objects in the last and thirteenth. release of the Véron-Cetty & Véron (2010) compilation (when adding BL LAC objects and Seyfert 1 galaxies to true QSO's), and 187 504 objects in the second release of the Large Quasar Astrometric Catalogue (LQAC-2) constructed by Souchay et al. (2012). A priori, the distribution of the objects already detected is far from homogeneous in the whole celestial sphere because of the variety of original surveys involved in these compiled catalogues with inhomogeneous sky coverage and magnitude thresholds. Nevertheless, a catalogue like the LQAC-2 gives the opportunity to carry out some statistical studies of the recorded quasar population in the whole sky as well as in some well delimited and homogeneous areas. It also helps to estimate the level of incompleteness of the available data as well as the inhomogeneities in the sky distribution of the objects recorded so far. This is the main purpose of this paper.

We carry out our study starting from the LQAC-2 compiled catalogue. Recall that one of its main objectives was to recompute the equatorial coordinates of the quasars of the compilation from algorithms leading to an optimized accuracy of the positions of the objects. These algorithms were exactly those used in the construction of the Large Quasar Reference Frame (LQRF) by Andrei et al. (2009). In addition, the LQAC-2 contains

extended multi-bands photometry, radiofluxes, redshifts, a new calculation of the absolute magnitudes in two bands (b and i), and finally a morphological characterization of the quasars from three estimators (skewness, roundness, and normalness).

2. Astrometric improvement

One of the main aims of the LQAC, and more specifically of its second release the LQAC-2, was to recalculate the equatorial coordinates of the quasars compiled in the various catalogues included in the compilation in a more accurate manner. Of course, we could exclude from this re-calculation the catalogues of radio quasars observed with the Very-Long-Baseline Interferometry (VLBI) technique, which give positions of the objects at the level of milliarcseconds. These include the 3414 quasars of the International Celestial Reference Frame (ICRF2, Ma et al. 2009; Bobholtz et al. 2010), 5198 from the Very Long Baseline Array (VLBA), 1858 from the Very Large Array (VLA, Claussen 2006) and 2118 from Jodrell Bank-VLA Astrometric Survey (JVAS). Notice that the positional off-set between the radio VLBI centre and the photocentre of these quasars is subject to particular recent investigations (Orosz & Frey 2013; Zacharias & Zacharias 2014). These objects with optimal astrometric quality at radio wavelengths represent only a small part of the LQAC-2. The four catalogues concerned gather no more than 5717 quasars with respect to the 187 504 quasars of the whole LQAC-2, that is

Fig. 1. Histogram of the off-sets between the quasars' right ascension given in the original catalogue and those re-calculated through the LQRF algorithm.

Fig. 2. Histogram of the off-sets between the quasars' declination given in the original catalogue and those re-calculated through the LQRF algorithm.

to say, a mere 3.05%. Thus, although the objects concerned are fundamental in terms of astrometric standards and references, their relative proportion is very small.

2.1. Recomputation of equatorial coordinates from the LQRF

Except in the case of the specific VLBI sample mentioned above, the positions of the objects found in the original catalogues belonging to the compilation are subject to a lack of accuracy, sometimes at the level of a few tenths of arcsecond or even a few arcseconds (Souchay et al. 2009), which explains the necessity of a recomputation of their equatorial coordinates. This was done through the intermediary of the algorithms taken to construct the LQRF (Andrei et al. 2009). They consist in homogenizing astrometry and reaching the milliarcsecond alignment with the ICRF. In these algorithms, the quasars are found, when available, in the very large optical surveys as the USNO B1.0 (Monet et al. 2003), the GSC2.3 (Lasker et al. 2008), and the Sloan Digital Sky Survey (SDSS). The positions were then placed onto the UCAC-2 based reference frame (Zacharias et al. 2004). A final step consisted in using spherical harmonics to fit the coordinates with the ICRF2. All this recomputation procedure was possible only for the quasars which could offer a counterpart in one or more of the various surveys used in the algorithm above. This concerns 159 700 objects, i.e., 85.17% of the whole sample of 187 504 quasars in the LQAC-2.

To get a clear insight as to the differences brought by the recomputation of coordinates we show in Figs. 1 and 2, respectively, the histograms of the off-sets in right ascension and declination, between the quasar coordinates given in their original catalogue and those recalculated through the LQRF algorithm. We note that both histograms present the same Gaussian profile accompanied by a small asymmetry, with a slightly sharper aspect in declination (Fig. 2) than in right ascension (Fig. 1). We took the factor $\cos \delta$ into account to evaluate the real angular offset in right ascension. The asymmetries mentioned above lead to a relative global bias towards negative values in $\alpha \cos \delta$ and positive ones in δ . Indeed, the mean values for both samples are respectively $\alpha \cos \delta = -0''.0109$ and $\bar{\delta} = 0''.0168$, respectively, whereas the standard deviations are $\sigma_{\alpha \cos \delta} = 0''.188$ and $\sigma_{\delta} = 0''.197$. The rather large amplitude of these two last values

Table 1. Difference of coordinates of quasars per V magnitude range, between the original catalogues of the LQAC-2 and the re-calculated values from the LQRF (Andrei et al. 2009).

V magnitude	Nb. QSO's	$\alpha \cos \delta$	$\bar{\delta}$	$\sigma_{\alpha \cos \delta}$	σ_{δ}
$14 < V < 15$	294	-0.022	-0.011	0.324	0.349
$15 < V < 16$	551	-0.026	0.021	0.256	0.256
$16 < V < 17$	1777	-0.010	0.015	0.196	0.230
$17 < V < 18$	9179	-0.013	0.013	0.172	0.195
$18 < V < 19$	45148	-0.019	0.001	0.133	0.145
$19 < V < 20$	21062	-0.004	0.008	0.169	0.185
$20 < V < 21$	7262	0.001	0.023	0.214	0.220
$21 < V < 22$	5394	0.002	0.011	0.174	0.174
$22 < V < 23$	169	-0.019	0.017	0.355	0.351

Notes. Mean values $\alpha \cos \delta$ and $\bar{\delta}$ and standard deviations $\sigma_{\alpha \cos \delta}$ and σ_{δ} . Unit = $1''$.

attests to the generally poor astrometric quality of some of the original catalogues involved in the LQAC-2 compilation and justifies the necessity to recalculate them in the LQRF. We note that they are of their order is the same as the positional uncertainty of the UCAC-2 astrometric catalogue (Zacharias et al. 2004).

In a next paper, we plan to focus the present analysis on the sub-set of the 3414 objects of the ICRF2. It will be interesting, in particular, to check if the recalculated equatorial coordinates at optical wavelengths become closer to the ICRF2 coordinates obtained by VLBI than the original ones. Two supplementary remarks must be added: first a high proportion of ICRF2 objects have no optical counterpart either because of their faintness or because they have not been surveyed so far. Second, there is no insurance that optical photocentre of ICRF2 quasars correspond to the same position as that determined from VLBI. This is subject to recent investigations (Orosz & Frey 2013).

2.2. Study of the magnitude dependence

As a supplementary study linked with astrometric performance, we investigated the magnitude dependent systematic errors on the quasars' positions. To this aim, we selected all the quasars with an estimation of the V magnitude, which represents a sample of 91 183 objects (48.63% of the whole LQAC-2). In Table 1, we list the mean values $\alpha \cos \delta$ and $\bar{\delta}$ as well as the standard

Table 2. Difference of coordinates of quasars per g magnitude range, between the original catalogues of the LQAC-2 and the re-calculated values from the LQRF (Andrei et al. 2009).

g magnitude	Nb. QSO's	$\alpha \cos \delta$	$\bar{\delta}$	$\sigma_{\Delta \alpha \cos \delta}$	$\sigma_{\Delta \delta}$
$14 < g < 15$	12	0.029	0.023	0.208	0.120
$15 < g < 16$	84	-0.024	-0.015	0.095	0.084
$16 < g < 17$	701	-0.014	-0.015	0.095	0.095
$17 < g < 18$	5098	-0.020	-0.012	0.087	0.085
$18 < g < 19$	29 897	-0.021	-0.009	0.089	0.083
$19 < g < 20$	48 621	-0.017	-0.005	0.092	0.085
$20 < g < 21$	23 665	-0.008	0.005	0.104	0.096
$21 < g < 22$	8644	-0.004	0.005	0.104	0.092
$22 < g < 23$	812	-0.014	-0.001	0.115	0.095
$23 < g < 24$	222	-0.022	-0.006	0.117	0.112
$24 < g < 25$	147	-0.043	-0.006	0.115	0.143

Notes. Mean values $\alpha \cos \delta$ and $\bar{\delta}$ and standard deviations $\sigma_{\alpha \cos \delta}$ and σ_{δ} . Unit = $1''$.

deviations $\sigma_{\alpha \times \cos \delta}$ and σ_{δ} of the differences of coordinates between those given by the original catalogues of the LQAC-2 and those based on the improved values given by the LQRF recalculation, for each V magnitude bin. The results for the standard deviations are plotted in Fig. 3 both in right ascension and declination. We can observe a very clear correlation between the values of $\sigma_{\alpha \times \cos \delta}$ and σ_{δ} , with a minimum at $\sigma_{\alpha \times \cos \delta} = 0''.133$ and $\sigma_{\delta} = 0''.145$ both for $18 < V < 19$. The standard deviation is generally slightly smaller in declination than in right ascension. Moreover, the general feature of the curves is in good agreement with typical astrometric reductions, for which the best results in terms of accuracy are obtained for intermediary values of magnitude. This is explained by saturation problems for the brightest objects and insufficient S/N ratio for the faintest ones, both phenomena leading to larger position errors.

We have carried out exactly the same kind of study but with respect to the g magnitude instead of the V magnitude. This concerns 118 048 quasars, which represent 62.96% of the whole LQAC-2. Our results are presented in Table 2 and plotted in Fig. 4. Here the values of the standard deviation σ_{δ} are always slightly smaller than $\sigma_{\alpha \times \cos \delta}$ excepted for one magnitude bin considered, with a minimum at $\sigma_{\alpha \times \cos \delta} = 0''.0873$ for $17 < g < 18$ and $\sigma_{\delta} = 0''.0829$ for $18 < g < 19$. All these values, below $0''.1$, are significantly smaller than in the case of the precedent study by taking into account V magnitudes. This can be explained by the following reason: quasars recorded with a V magnitude come from a large set of individual catalogues, already compiled by Véron-Cetty & Véron (2010) for most of them. They are characterized by poor astrometric quality, whereas quasars recorded with a g magnitude come mainly from the SDSS catalogue (DR8 release) with homogenous and rather accurate astrometry. This explains that the agreement with the LQRF optimized values of coordinates is much better. The astrometric quality in g band is stabilized at small values for a wide range of the g magnitude ($15 < g < 24$) (Fig. 4), whereas this stability is not present in V magnitude (Fig. 3).

To complete our astrometric analysis, we plot the same kinds of histograms as for the global set of LQAC-2 quasars of Figs. 1 and 2 with the sub-sets of quasars selected above, that is to say, the 90 880 objects with V magnitude available (Figs. 5 and 6) and 118 048 objects with g magnitude available (Figs. 7 and 8). The sharpness of the histograms in the latter case with respect to the former shows up obviously, both in right ascension (Figs. 5 and 7) and in declination (Figs. 6 and 8). This

Fig. 3. Standard deviation between the quasar coordinates given in the original catalogue and those re-calculated through the LQRF algorithm, with respect to V magnitude. Right ascension (upper curve) and declination (lower one). The dashed line indicates the normalized number of quasars. **Fig. 4.** Standard deviation between the quasar coordinates given in the original catalogue and those re-calculated through the LQRF algorithm, with respect to g magnitude. Right ascension (upper curve) and declination (lower one). The dashed curve indicates the normalized number of quasars.

sharpness is concretized by the corresponding values of the standard deviations: $\sigma_{\Delta \alpha \times \cos \delta} = 0''.095$ in g with respect to $\sigma_{\Delta \alpha \times \cos \delta} = 0''.160$ in V ; $\sigma_{\Delta \delta} = 0''.088$ in g with respect to $\sigma_{\Delta \delta} = 0''.173$ in V . Concerning the mean value of the coordinates off-sets, we note in both cases a negative bias in right ascension with $\alpha \cos \delta = -0''.0154$ in g and $\alpha \cos \delta = -0''.0120$ in V ; The bias is close to zero with $\bar{\delta} = -0''.003$ in g and $\bar{\delta} = 0''.006$ in V for the declination.

3. The whole sky lack of homogeneity in the distribution of recorded quasars

Two main reasons lead to the lack of uniformity of the surface distribution of the quasars already discovered and recorded on the celestial sphere. The first one must be considered as an observational defect: it comes from the fact that each survey participating in a compiled catalogue, such as the LQAC-2 (Souhay et al. 2012), is more or less dense and complete at a given

Fig. 5. Histogram of off-sets in right ascension between the quasar coordinate given in the original catalogue and the one recalculated through the LQRF algorithm. The quasars considered are restricted to those that present an estimation of V magnitude.

Fig. 7. Histogram of off-sets in right ascension between the quasar coordinate given in the original catalogue and the one re-calculated through the LQRF algorithm. The quasars considered are restricted to those that present an estimation of g magnitude.

Fig. 6. Histogram of off-sets in declination between the quasar coordinate given in the original catalogue and the one re-calculated through the LQRF algorithm. The quasars considered are restricted to those that present an estimation of V magnitude.

Fig. 8. Histogram of off-sets in declination between the quasar coordinate given in the original catalogue and the one re-calculated through the LQRF algorithm. The quasars considered are restricted to those that present an estimation of g magnitude.

threshold of magnitude and covers a limited and generally relatively small area in the sky. Therefore the combination of the catalogues involved is naturally a source of large inhomogeneities in terms of surface density on the celestial sphere, including depletion zones for which no systematic or extended survey has been achieved so far.

The second reason is physical. It arises from the galactic extinction, which is all the more important that we consider fields close to the galactic plane, that is to say, with small absolute values of the galactic latitude. In the following, we study, with the help of histograms, the variations of surface density of the recorded quasars in the LQAC-2, with respect to galactic, equatorial, and ecliptic coordinates.

3.1. Galactic coordinates distribution

In Figs. 9 and 10 we show the histograms of the population distribution of the LQAC-2 quasars as a function of the galactic longitude l and the galactic latitude b , respectively. The horizontal

line in Fig. 9 and the rounded one in Fig. 10 show the features that should be followed by these histograms in the ideal case of a uniform surface distribution. The impact of the galactic extinction on the drastic decrease of the number of objects for low absolute values of b is clearly seen in Fig. 10. For $-10^\circ < b < +10^\circ$, the number of recorded quasars is around 1000 objects per bin whereas it should reach approximately more than 16 times this value in the case of a homogeneous distribution. We must emphasize that this ratio should be even much larger if we only take the optical sources into account and exclude the radio emitting sources that are poorly affected by the galactic extinction. The ratio of the number of quasars in the northern galactic hemisphere to those in the southern hemisphere, which is equal to 2.614, is largely explained by the discrepancy between the surveys in the respective hemispheres, also noticed for the equatorial coordinates, as will be pointed out in the following.

Fig. 9. Histogram of the quasar population with respect to galactic longitude. The straight line represents the shape the histogram should have in the case of a homogeneous distribution.

Fig. 11. Histogram of the quasar population with respect to right ascension. The straight line represents the shape the histogram should have in the case of a homogeneous distribution.

Fig. 10. Histogram of the quasar population with respect to galactic latitude. The curved line represents the shape the histogram should have in the case of a homogeneous distribution.

Fig. 12. Histogram of the quasar population with respect to declination. The curved line represents the shape the histogram should have in the case of a homogeneous distribution.

3.2. Equatorial coordinates distribution

A dense and homogeneous space distribution of the equatorial coordinates of quasars is desirable for a reference frame. Indeed, quasars play the fundamental role as quasi-inertial reference objects, as has been demonstrated in the construction of the ICRF (Ma et al. 1998) and its up-dated version the ICRF-2 (Ma et al. 2009) built from observations carried out with the VLBI technique at radio wavelengths. With the event of the *Gaia* astrometric space mission launched December 19 2013 from the Guyana Space Center, optical observations are expected to be the key for the construction of a very dense and accurate celestial reference frame at optical wavelengths in the near future, maybe at the end of the decade. For this purpose, a rather uniform distribution in the celestial sphere in terms of equatorial coordinates is greatly recommended.

Although *Gaia* should considerably improve both surface density and uniformity of recorded quasars, it is instructive to study these topics with the present available sample. Thus, this sub-section is devoted to the analysis of the present quasars distribution inside the LQAC-2 compiled catalogue with respect to the equatorial coordinates. In Figs. 11 and 12, we show the

histograms of the distribution of quasars of the LQAC-2 in right ascension and declination, respectively, with 10° (40^m) bins. In declination (Fig. 12), there is a general depletion of quasars in the southern hemisphere and in opposite a large excedentary count in the northern hemisphere, with respect to a uniform distribution represented by the rounded curve. This is obviously because, by far, the largest survey, the SDSS, which contains 67.51% of the total sample of the LQAC-2 (187 504 quasars), is concentrated in the northern hemisphere. Only 14 176 objects among the 126 577 ones representing the whole SDSS population belong to the southern hemisphere, that is to say a mere 11.20%. If we consider the whole LQAC-2 catalogue, the counts are 51 887 (27.67%) and 135 617 quasars (72.33%) respectively in the southern and northern hemispheres. Here two gaps appear neatly in right ascension (Fig. 11) centred around 90° and 290° , respectively, with no explanation other than the lack of uniformity of surveys.

3.3. Ecliptic coordinates distribution

The ecliptic band ($-30^\circ < \beta < +30^\circ$) being the privilegiate zone in which the overwhelming majority of moving objects (planets,

Fig. 13. Histogram of the quasar population with respect to ecliptic longitude. The straight line represents the shape the histogram should have in the case of a homogeneous distribution.

Fig. 14. Histogram of the quasar population with respect to ecliptic latitude. The curved line represents the shape the histogram should have in the case of a homogeneous distribution.

asteroids, etc.) are detected and monitored, it also looks interesting to investigate the surface density of quasars through this band. Indeed, we can expect that, in the near future, following the *Gaia* mission output data, a large number of astrometric reductions of these moving bodies will be carried out directly from quasars instead of stars, on the condition that the sky surface density of the former objects is large enough. This issue has already been studied by Souchay et al. (2007) when searching for the cases of close approaches between quasars and Jupiter with possible applications to the *Gaia* mission. An underlying purpose in that particular study of the biggest planet was to estimate theoretically the relativistic deflection of light due to its gravitation.

In Figs. 13 and 14, we present the histograms of a number of LQAC-2 objects with respect to their ecliptic longitude and ecliptic latitude. As mentioned in the preceding subsection for equatorial coordinates, and because of the small inclination ($23^\circ 27'$) of the ecliptic with respect to the celestial equator, we observe (Fig. 14) a dramatic excess of quasars in the part corresponding to positive ecliptic latitudes with respect to negative ones, which is essentially a consequence of a much extended coverage of sky observations in the northern hemisphere. Here also the two gaps in ecliptic longitude appear clearly in Fig. 13, correlated with those already observed in right ascension (Fig. 11).

4. Distance to the nearest neighbour: statistical analysis

In the case of a compiled catalogue, such as the LQAC-2, the distance to the nearest neighbour, or by extension to the k th neighbour is a fundamental parameter that should naturally obey some statistical law in the case of a uniform distribution. A general theoretical overview of the topic can be found in a *Gaia* DPAC Technical Note by Mignard (2008). In the following, we recapitulate the main steps of the theory to confront it with the real quasars sample of the LQAC-2.

4.1. Theoretical calculations and expected results

When supposing a point Q of the celestial sphere located at the centre of a circular area $S = \pi r^2$, let ρ be the surface density,

so that $\lambda = \rho S$ represent the mean number of sources expected in S . In a homogeneous sources repartition, the probability $P(k)$ that there are exactly k points, ($k = 0, 1, 2, \dots$) in S is given by a Poisson distribution:

$$P(k) = \frac{\lambda^k}{k!} e^{-\lambda}. \quad (1)$$

As a consequence, the probability that no source is found in S is:

$$P(0) = e^{-\lambda}. \quad (2)$$

Thus, the probability that at least one source is present inside S , that is to say, that the distance d to the nearest neighbour is smaller than r , is:

$$P(d < r) = 1 - e^{-\lambda} = 1 - e^{-\rho \pi r^2}. \quad (3)$$

From this last equation, we get by derivation the probability density function (PDF) for the angular variable r :

$$f(r) = \frac{r}{\sigma^2} e^{-\frac{r^2}{2\sigma^2}}. \quad (4)$$

Where σ can be introduced as a characteristic distance, that is to say the average distance to find the nearest neighbour:

$$\sigma = \frac{1}{(2\pi\rho)^{\frac{1}{2}}}. \quad (5)$$

These theoretical calculations can be extended to the search for the k th nearest neighbour (Mignard 2008). Then the smallest distance corresponds to the nearest neighbour, the second smallest to the second nearest neighbour, etc. until the k th distance. The corresponding formula for PDF of the k th nearest neighbour, can be written:

$$f_k(d < r) = \frac{1}{2^{k-1}(k-1)!\sigma} \left(\frac{r}{\sigma}\right)^{2k-1} e^{-\frac{r^2}{2\sigma^2}}. \quad (6)$$

In the following, we only deal with the study of the nearest neighbour, concerning the LQAC-2.

Fig. 15. Histogram of the number of quasars with respect to their distance to the nearest neighbour in the whole LQAC-2 catalogue. The line shows the shape the histogram should have according to the theory, if uniform distribution is assumed.

4.2. Comparison with the all-sky LQAC-2 catalogue and a large SDSS survey field

In this sub-section, we confront the theoretical results presented above with real samples of quasars. At first, we take the whole LQAC-2 quasars population, containing 187 504 objects distributed in the whole celestial sphere. This concerns an all-sky surface area of 41 253 square degrees, which gives a density $\rho = 4.545$ sources per square degree. Using (3), the probability that the distance between a quasar and its nearest neighbour is located between two consecutive radii values r_1 and r_2 is:

$$P(r_1 < d < r_2) = e^{-\rho\pi r_1^2} - e^{-\rho\pi r_2^2}. \quad (7)$$

Multiplying this probability by the total number of quasars in the sample considered, we can compare our theoretical expectation with the histogram of the number of sources with respect to the value of the closest distance. This comparison is shown in Fig. 15. We observe that the theoretical curve corresponding to a typical Rayleigh distribution does not fit the results at all. This can be easily understood as the consequence of a lack of homogeneity of the sample in the celestial sphere. Because of the high density of quasars due essentially to the SDSS survey in some area covering roughly 1/3 of the sky, the peak for the largest number of quasars is reached near $d = 200''$ whereas its theoretical value is close to $d = 700''$. We observe a drastic depletion of quasars for values of the angular distance in the interval $600'' < d < 2000''$, which is clearly attributable to the fact that when we exclude the large and dense surveys participating in the present known quasar population, the quasars surface density is excessively small in some zones of the celestial sphere.

To avoid this artefact because of the lack of uniformity and to find a better agreement with theoretical expectations, we must carry out our study in a limited and homogeneous area of the sky, that is to say, with a relatively constant surface density. We naturally choose a zone of the LQAC-2 covered by the SDSS, but also containing objects from other catalogues. It is limited by the following conditions: $8^{\text{h}}40^{\text{m}} < \alpha < 16^{\text{h}}$ and $5^\circ < \delta < 55^\circ$. Indeed, in this new case, the histogram presented in Fig. 16 fits the theoretical estimation well: the real distribution of the sample with respect to the distance of the nearest neighbour is in good agreement with the theoretical curve, and it peaks for a value in accordance with the characteristic distance of $\sigma = 375''$.

Fig. 16. Histogram of the number of quasars with respect to their distance to the nearest neighbour in a specific zone of the LQAC-2 with homogenous surface density. The line shows the shape the histogram should have according to the theory, if uniform distribution is assumed.

Nevertheless, with a meticulous and more detailed inspection, we note that the correspondence between our sample and the theory is not perfect: there is a small O–C discrepancy characterized by an excedent of the true distribution of quasars for nearly all the values of $d < \sigma$ and a significant deficiency of the number of quasars for the values of distance $\sigma < d < 800''$. This can be attributable to an effect of the remaining imperfection in homogeneity of the quasars distribution in the area selected, because we took catalogues other than the sole SDSS into account.

A more careful and deeper analysis of the small discrepancy mentioned above could be performed by investigating the density variations inside sub-zones of the sample. These densities could have different causes such as a real inhomogeneity in the quasar's distribution, biases due to observational climatic conditions (seeing), or declination effects. This analysis is out the scope of this paper. Here we simply want to emphasize the good correlation between the histogram of the distribution with the basic theoretical distribution law.

4.3. Uncertainties for quasars pairing at short angular distance

Following the study above, we take a particular here care to the excedent of quasars characterized by short angular distances to the nearest neighbour, i.e., with small values of d . Figure 17 represents a zoom of the histogram in Fig. 16 for $0^\circ < d < 200''$. We note a significant excess of quasars in the histogram at very small distance ($d < 30''$) with respect to the theoretical curve. This deserves specific attention because this excess should have different origins. Indeed, admitting that the theoretical curve represents cases of hazardous coincidence between two quasars in nearly the same line of sight, the excedent should be explained by two kinds of external cases. First, it should come from the presence of double listings in the LQAC-2 catalogue, that is to say, of a single object which, by a failed cross-identification, has been recorded twice with different coordinates. Second, it should have a physical origin and cosmological relevance: we are in presence either of a true case of binary quasars, linked by gravitational interaction, or of gravitational lensing of a single quasar reproduced twice.

The redshift related to the two objects is expected to be roughly the same, whether a double listing or a true binary. Thus,

Fig. 17. Zoom at the shortest distances d of the histogram in Fig. 16. The line shows the shape the histogram should have according to the theory.

Fig. 19. Position of couples quasar/nearest neighbour in a bi-dimensional (z_1, z_2) graph in the case of quasars with an angular separation between 10 arcsec and 20 arcsec.

Fig. 18. Position of couples quasar/nearest neighbour in a bi-dimensional (z_1, z_2) graph in the case of quasars with an angular separation shorter than 10 arcsec.

Fig. 20. Position of couples quasar/nearest neighbour in a bi-dimensional (z_1, z_2) graph in the case of quasars with an angular separation between 20 arcsec and 30 arcsec.

the redshift comparison is not suitable to separate the two external cases above. But such a comparison can, at least, differentiate couples of quasars in excess from those predicted by the theory, as we explained above, for which a significant z difference between two paired quasars a priori validates the thesis of the presence of two real coincident objects with no physical interaction.

In Fig. 18, we represent in a bi-dimensional (z_1, z_2) graph the couple of quasars for which $d < 10''$. The redshift of a quasar considered is z_1 and z_2 the nearest neighbour's redshift. Frequently, a point has a symmetric with respect to the first diagonal, because, most of the time, the first quasar in a couple quasar/nearest neighbour is also the nearest neighbour of the second one (but not all the time, we will see an example in Table 4). A zone is delimited by two parallel lines following this condition: the number of points (z_1, z_2) inside this zone is equal to the excess of couples of quasars from theoretical expectations, and so the number of points (z_1, z_2) outside this zone represents the expected cases of hazardous coincidences, in other words, quasars close to each other but with no equal redshift.

The same process is applied to the next bins in the histogram, that is to say, $10'' < d < 20''$ in Fig. 19 and $20'' < d < 30''$ in

Fig. 20. The results can be considered as convincing if and only if the zone between the two parallels is restricted to the first diagonal and its surroundings. As we can see in Figs. 19 and 20, we cannot separate the two parallel lines with naked eye, which is because quasars in the zone delimited by these two lines have a difference in redshift of less than 0.1. So the excess can be explained by physical couples of quasars or double listings. In Fig. 18, we remark that the two lines are far away from the other and the ends of the zone reach a difference in redshift of close to 1. In conclusion, for $10'' < d < 30''$, the excess estimated between the theory and the real sample of the LQAC-2 can be explained by physical pairs of quasars (or single quasar seen under gravitational lensing) and double listings, but at the closest distance ($d < 10''$) physical quasars and double listings are not enough to explain an excess. This contradicting result is difficult to interpretate.

4.4. Identification and confirmation of binary quasars

In the continuity of the study above, the search for binary quasars looks like an interesting by-product of huge surveys. For instance, Hennawi et al. (2006) presented a sample of 221 quasar

pairs, over the redshift range $0.5 < z < 3.0$, discovered from an extensive follow-up campaign to find companions around the SDSS and 2dF QSO surveys. In particular, this sample includes 26 new binary quasars with separation $\theta < 10''$, which corresponds to proper transverse separation $R_{\text{prop}} < 50 h^{-1}$ kpc.

Following our investigation above we wanted to characterize real binary quasars. To that end, we identify the pairs of quasars with a redshift difference smaller than $\Delta z_0 * \sqrt{2}$, where Δz_0 is an arbitrary threshold. The factor $\sqrt{2}$ comes from the fact that we work with the distance to the first diagonal of a couple (z_1, z_2) given by the expression $d = |z_1 - z_2|/\sqrt{2}$. In our study, we adopt $\Delta z_0 = 0.02$, which looks reasonable when considering the precision of redshift determination (Souhay et al. 2009).

So, as double listings and true double quasars present the same redshift at this level, the only possibility to make an adequate differentiation between these two categories consists in searching deep field images of these objects. We decided to rely on SDSS images, when available, at the following site: <http://cas.sdss.org/astro/en/tools/search/IQS.asp>. Our selection for the search and validation of binary quasars leads to a set of 289 pairs based on the following constraints: their angular distance must be $d < 30''$ and their off-set Δz with respect to the line $z_1 = z_2$ should be less than $\Delta z_0 = 0.02$. For this global set we found 159 real binary quasars (with three of them doubtful), i.e., with same redshift and two photocentres, and 35 double listings (with five of them doubtful), for which there is only one photocentre visible on the frame. Nevertheless, in this last case we cannot exclude the possibility that we are in the presence of a real binary quasar for which one of the photocentres is out of detection from the DSS image database. At last, 97 pairs could not be accessible to the DSS data and are still waiting for further observational investigation. The fact that double listings exist at an angular distance of several arcseconds is not surprising. Some original quasars catalogues belonging to the LQAC-2 compilation present a poor positional accuracy at this level. They are not concerned by the analysis presented in Sect. 2.1 for they were not identified by the LQRF algorithm because of their poor astrometry.

We recognize that the present study constitutes a preliminary effort in the identification of binary quasars. Some point can be deepened, for example the definition of the limit of redshift difference between two quasars to consider them as binary quasars. Nevertheless, we think that this kind of analysis should be deepened at least to evaluate the proportion of binaries objects among the total sample of known quasars statistically.

An important remark, from a private communication (Mignard 2013) based on personal investigations, was that the probability that a quasar undergoes a gravitational lensing should be about 1/1000. So it looks legitimate to require further analysis and to understand at what extent our set of binary quasars should or should not be the consequence of these lensings. We observe that the number of binary quasars we found (159) corresponds to a little less than one thousandth of all the 187 504 quasars in the LQAC-2 catalogue. In fact, the possibility that quasars clustering at short angular distances ($2'' < \Delta\theta < 10''$) are due to gravitational lensing has been abundantly investigated for more than a decade, with the conclusion that the expected number of quasars lensed by groups and clusters is too small to account for all the controversial pairs (Oguri & Keeton 2004; Hennawi et al. 2007). The plausible explanation is that the controversial pairs are real binaries rather than lenses (Schneider 1993; Kochanek et al. 1999; Mortlock et al. 1999). Djorgovski et al. (1991) as well as Hewett et al. (1998) similarly

Table 3. Binary quasars of the LQAC-2 with the highest redshifts.

Quasar 1/2	z_1	z_2	θ''	U_1	U_2	Ref.
LQAC_169+013_002/003	3.029	3.009	21.24	21.6	20.0	E/M
Lqac_172+007_009/010	2.654	2.668	10.60	18.1	–	B/I
Lqac_019+031_003/004	2.640	2.624	11.22	19.6	21.6	M/E
Lqac_246+026_017/018	2.605	2.605	6.32	19.7	–	E/I
Lqac_329+000_016/017	2.550	2.545	20.81	21.3	20.5	E/E
Lqac_249+026_006/007	2.540	2.540	9.20	21.5	–	M/I
Lqac_246+026_014/016	2.526	2.522	19.03	–	17.8	I/E
Lqac_041-001_012/013	2.459	2.465	4.44	21.1	20.8	E/E
Lqac_187+011_009/010	2.458	2.458	16.59	–	–	I/M

Notes. Letters in the last column are LQAC-2 flags indicating original catalogues: B = VLBA, E = SDSS, I = Hewitt and Burbidge, M = Véron-Cetty & Véron compilation. The parameters z_1 and z_2 are redshift of both quasars, U_1 and U_2 their magnitude in the U band.

Table 4. Binary quasars with the lowest redshifts (two of them form a triplet).

Quasar 1/2	z_1	z_2	θ''	U_1	U_2	Ref.
Lqac_195+029_005/006	0.024	0.023	19.44	16.2	–	M/M
Lqac_204+048_006/007	0.028	0.028	8.42	14.3	17.5	M/E
Lqac_209+018_002/003	0.051	0.051	2.45	–	14.9	M/M
Lqac_357+002_005/006	0.053	0.053	3.71	–	–	M/M
Lqac_159+047_009/010	0.064	0.063	14.20	–	–	M/M
Lqac_223+047_010/011	0.070	0.070	16.68	–	–	M/M
Lqac_223+047_011/012	0.070	0.070	7.25	–	–	M/M
Lqac_146+042_004/005	0.074	0.075	21.27	17.6	18.8	E/M
Lqac_154+046_006/007	0.080	0.079	4.57	–	–	M/M

Notes. Letters in the last column are LQAC-2 flags indicating original catalogues: E = SDSS, M = Véron-Cetty & Véron compilation. The parameters z_1 and z_2 are redshift of both quasars, U_1 and U_2 their magnitude in the U band.

claimed that this interpretation implied a factor 100 more binary quasars over what is expected from extrapolating the quasar correlation function power law down to co-moving scales smaller than $100 h^{-1}$ kpc. The first work interpreted this fact as the enhancement of quasar activity during merger events. The estimation of the factor above was done before the advent of very dense surveys as the 2dF and the SDSS, and should be re-calculated by taking their statistics into account.

4.5. Examples of interesting binary quasars

This sub-section is devoted to a sub-sample of physical binary quasars with exceptional characteristics coming from the total LQAC-2 compilation. They should present some interest because of their uncommon properties. We have carefully checked the binary status of all of them via the DSS imaging database. In Tables 3 and 4, we show quasar binaries with the highest and lowest redshift value, respectively, whereas, in Table 5, we show binaries whose one of the component is among the brightest ones in U band. Finally, in Table 6, we selected binaries with the smallest angular separation. In all these tables, for the sake of concision, the quasars are referenced from their LQAC number instead of their equatorial coordinates. Moreover, we give all the relevant information when it is available: the angular separation r , the redshift z , and the U magnitude. For each binary component we mention the LQAC-2 flag indicating the

Table 5. Binary quasars with the brightest magnitude U for one of their components.

Quasar 1/2	U_1	U_2	θ''	z_1	z_2	Ref.
Lqac_204+048_006/007	14.3	17.5	8.424	0.028	0.028	M/E
Lqac_209+018_002/003	–	14.9	2.450	0.051	0.051	M/M
Lqac_195+029_005/006	16.2	–	19.444	0.024	0.023	M/M
Lqac_209+025_001/002	21.5	16.3	3.665	0.164	0.164	E/E
Lqac_137+000_025/026	20.3	16.9	14.978	1.887	1.873	E/E
Lqac_144+054_009/010	17.1	–	16.400	0.102	0.100	M/I
Lqac_184+050_007/008	19.6	17.2	9.012	1.456	1.457	E/E
Lqac_205+005_008/009	–	17.3	20.293	0.266	0.266	I/E
Lqac_126+003_006/007	17.3	–	2.777	0.506	0.506	A/I

Notes. Letters in the last column are LQAC-2 flags indicating original catalogues: A = ICRF2, E = SDSS, I = Hewitt and Burbidge, M = Véron-Cetty & Véron compilation. The parameters z_1 and z_2 are redshift of both quasars, U_1 and U_2 their magnitude in the U band.

Table 6. Binary quasars with the smallest separation.

Quasar 1/2	θ''	z_1	z_2	U_1	U_2	Ref.
Lqac_250+031_012/013	2.132	0.587	0.586	19.6	–	E/M
Lqac_238+046_013/014	2.377	0.136	0.135	–	–	M/M
Lqac_209+018_002/003	2.450	0.051	0.051	–	14.9	M/M
Lqac_247+037_006/007	2.452	0.923	0.922	18.9	19.4	M/E
Lqac_181+043_009/010	2.608	1.789	1.791	18.3	18.7	M/E
Lqac_126+003_006/007	2.777	0.506	0.506	17.3	–	A/I
Lqac_242+028_012/013	2.810	0.170	0.170	19.7	20.8	M/E
Lqac_052-000_030/031	2.890	0.610	0.609	24.5	19.5	E/E
Lqac_123+040_002/003	2.953	0.188	0.189	22.3	18.3	E/E

Notes. Letters in the last column are LQAC-2 flags indicating original catalogues: A = ICRF2, E = SDSS, I = Hewitt and Burbidge, M = Véron-Cetty & Véron compilation. The parameters z_1 and z_2 are redshift of both quasars, U_1 and U_2 their magnitude in the U band.

original catalogue from which it has been picked up (Souhay et al. 2012). In all our tables we limited our search for binaries within a maximum separation $\theta = 30''$.

Some interesting remarks can be driven from these subsamples. First, in Table 3, where we list the binary quasars with the highest redshift, we find a pair with $z > 3$ despite the fact that the population in this area is relatively very small as will be shown in Sect. 5.4. The following very distant binaries have a redshift around $z = 2.5$. On the other hand, in the case of binaries with the smallest redshifts (see Table 4), the values of these redshifts are $z < 0.1$. As could be expected some of the binaries with brightest component in Table 5 are also included in Table 4 with the lowest redshift. But some quasars do not follow this rule, as in the case of Lqac_137+000_026 with a redshift of 1.873 despite a relatively bright component at $U = 16.9$, making it the fifth brightest binary.

In Table 6, we observe that the nine closest binaries have an angular separation between $2''$ and $3''$. As a complement we present in Table 7 the complete list of the 159 binary quasars that we have clearly identified from DSS imaging, with a separation angle θ between $2''$ and $30''$. The objects are arranged in order of increasing θ . The U magnitudes of the two components are indicated (when available) as well as their redshift, the flag of the catalogues in which each component can be found, and a number indicating the sequential number in terms of increasing magnitude U of the brightest component and decreasing value of z . We think that this extended list will be profitable for further

purpose, for instance dissociating the cases of true binaries from those of gravitational lensing by specific spectral characterization. In many cases the SDSS survey (flag “E”) has identified only one of the two components despite their relative proximity.

5. Cross-identification and cross analysis of two surveys in high density fields: SDSS and 2dF

A particular and interesting study concerns the inter-comparison between two independent dense catalogues on a common explored sky area. Some important issues can be addressed from it. For instance, for the selected area, we can investigate, at a given magnitude threshold, the number of quasars common in the two surveys as well as those detected in only one survey. Thus, we can evaluate the level of completeness of the respective catalogues, which could be dependent on the method of detection of the objects.

Two catalogues are particularly suitable for our study, because they are both relatively very dense and contain a rather extended common surveyed sky area: the Sloan Digital Sky Survey (SDSS, Adelman-McCarthy et al. 2007) and the 2-degree Field Quasar Redshift Survey (2dF, Croom et al. 2004). After describing the properties of these surveys as well as their specific underlying method of detection of quasars, we show the results of the analysis coming from their cross-identification.

5.1. The characteristics of the SDSS and the 2dF surveys

The Sloan Digital Sky Survey, generally referred as SDSS, results from observations performed with a dedicated 2.5 m telescope at Apache Point (New Mexico, USA). The pre-selection of the quasars is based on analysis the u, g, r, i, z photometric database of the catalogue and on the analysis of the colour indexes ($u - g, g - r, r - i, i - z$) which are significantly different from normal stars. Once a candidate has been detected, its spectrum is obtained and the detection of broad emission lines, characteristic of a quasar, is validated from an automated analysis pipeline. A specific software detects absorption and emission lines, and fits a Gaussian function to each line profile. The SDSS criteria to qualify an object as a quasar is that at least one line must have a full-width at half maximum (FWHM) broader than 1000 km s^{-1} . Moreover, an additional condition is that the object must be intrinsically brighter than $M_i = -22$.

Similar to the SDSS, the 2-degree Field (2dF) Quasar Redshift Survey, quoted as 2QZ (Croom et al. 2004) is based on a pre-selection of quasar candidates using well defined criteria on three u, b, r colours (instead of five for the SDSS). Nevertheless, the support is fundamentally different for it consists of automated measurements of UKST photographic plates. As in the case of the SDSS, a spectroscopic follow-up of the candidate quasars is completed, using a χ^2 minimization technique to fit the spectrum to a number of quasars, galaxies, and stellar templates.

5.2. Cross-identification between the two surveys in a large common field

In order to estimate the relative completeness of the two surveys above and to identify the differences between them concerning information on the quasars taken individually, we choose a fully explored common sky area. It corresponds to an area delimited by the following equatorial coordinates intervals: $11^{\text{h}}40^{\text{m}} < \alpha < 14^{\text{h}}$ and $-2^\circ < \delta < +2^\circ$.

Table 7. Binary quasars with the shortest separation, between 0'' and 30''.

Quasar 1/2	U_1	U_2	θ	z_1	z_2	Catalog ref 1	Catalog ref 2	Position when sorted by U	Position when sorted by z
LQAC_250+031_012/013	19.63	0.0	2.1322	0.587	0.586	---E---KLM	-----M	96	112
LQAC_238+046_013/014	0.0	0.0	2.3773	0.136	0.135	-----M	-----M	143	144
LQAC_209+018_002/003	0.0	14.91	2.4501	0.051	0.051	-----M	-----M	2	157
LQAC_247+037_006/007	18.92	19.4	2.4523	0.923	0.922	-----M	---E---K-M	49	101
LQAC_181+043_009/010	18.26	18.65	2.6083	1.789	1.791	-----M	---E---M	30	59
LQAC_126+003_006/007	17.33	0.0	2.7771	0.506	0.506	ABCD----J--M	-----I-KL-	9	120
LQAC_242+028_012/013	19.66	20.84	2.8096	0.17	0.17	-----M	---E---J--M	100	139
LQAC_052-000_030/031	24.52	19.53	2.8899	0.61	0.609	---E-----	---E---KL-	88	107
LQAC_123+040_002/003	22.26	18.3	2.9534	0.188	0.189	---E-----	---E---JKLM	31	137
LQAC_179+012_006/007	19.53	19.82	3.3223	0.596	0.596	-----M	-----M	87	109
LQAC_188+068_007/008	19.05	19.45	3.3991	1.529	1.514	-----M	-----M	55	84
LQAC_209+025_001/002	21.51	16.3	3.6647	0.164	0.164	---E-----	---E---JKLM	4	140
LQAC_357+002_005/006	0.0	0.0	3.7166	0.053	0.053	-----M	-----M	144	156
LQAC_195+051_005/006	20.09	19.74	3.7278	1.686	1.684	-----M	-----M	109	69
LQAC_249+026_004/005	20.21	19.65	3.7585	1.961	1.965	-----M	---E---KLM	99	43
LQAC_149+054_014/015	19.83	19.52	3.892	1.956	1.954	-----M	-----M	86	44
LQAC_232+053_012/013	20.1	19.99	3.9819	1.531	1.533	-----M	-----M	118	82
LQAC_216+007_007/008	20.2	19.59	4.0379	1.312	1.309	-----M	-----M	93	95
LQAC_258+032_005/006	18.25	24.63	4.124	0.102	0.101	---E---JKLM	---E---J--	29	147
LQAC_226+029_013/014	20.15	19.7	4.255	0.875	0.862	-----M	-----M	104	103
LQAC_181+014_004/005	19.93	19.75	4.2621	1.801	1.8	-----M	-----M	110	57
LQAC_194+012_014/015	19.45	19.56	4.3662	2.18	2.189	-----M	-----M	79	17
LQAC_041-001_012/013	21.07	20.77	4.4356	2.459	2.465	---E---KLM	---E---LM	135	8
LQAC_151+041_005/006	18.03	19.15	4.445	1.734	1.738	-----M	---E---LM	23	62
LQAC_151+041_005/006	18.03	19.15	4.445	1.734	1.738	-----M	---E---LM	22	63
LQAC_154+046_006/007	0.0	0.0	4.5715	0.08	0.079	-----M	-----M	145	151
LQAC_248+026_024/025	0.0	19.49	4.598	2.1	2.086	-----IJKL-	---E---K-M	84	30
LQAC_193+008_005/006	18.8	17.44	4.6132	0.44	0.439	-----M	---E---JKLM	13	123
LQAC_325+000_050/051	21.67	22.09	4.8306	2.152	2.14	-----G---K-M	-----G---K-M	141	22
LQAC_218-001_007/008	20.71	17.91	5.0177	2.082	2.082	-----M	---E---IJKLM	18	32
LQAC_224+054_011/012	20.36	20.28	5.204	1.913	1.912	-----M	-----M	125	47
LQAC_206+038_002/003	0.0	18.32	5.2872	1.533	1.538	-----IJK--	---E---KLM	32	80
LQAC_221+021_012/013	0.0	18.45	5.4503	1.4	1.395	-----IJKL-	---E---KLM	39	88
LQAC_333+013_012/013	19.9	19.64	5.6612	1.995	2.002	-----M	-----M	97	39
LQAC_200+030_004/005	18.87	19.65	5.7624	1.595	1.596	---E---KLM	-----M	47	75
LQAC_186+056_006/007	20.25	19.15	6.0586	2.39	2.379	-----M	-----M	62	10
LQAC_212+039_003/004	19.62	20.22	6.3113	2.078	2.083	-----M	-----M	94	33
LQAC_246+026_017/018	19.72	0.0	6.325	2.605	2.605	---E---K-M	-----IJKL-	106	4
LQAC_171+046_012/013	19.41	0.0	6.3712	0.106	0.106	-----M	-----M	77	146
LQAC_350+008_002/003	0.0	0.0	6.6457	2.09	2.09	ABCD----KLM	-----IJKL-	146	31
LQAC_357+000_012/013	20.06	19.2	7.0195	2.147	2.159	-----I-KLM	---E---KLM	64	20
LQAC_164-000_024/025	19.87	20.1	7.2296	2.132	2.128	----FG--KLM	-----M	114	23
LQAC_223+047_011/012	0.0	0.0	7.2474	0.07	0.07	-----M	-----M	147	154
LQAC_269+023_001/002	0.0	0.0	7.3022	1.721	1.721	ABCD----J--M	-----I-KL-	148	67
LQAC_250+039_007/008	20.09	0.0	7.4091	0.539	0.54	---E---KLM	-----I-K--	122	118
LQAC_345-000_006/007	21.64	20.41	7.6698	1.896	1.885	-----G-----	---E-G---KLM	128	49
LQAC_157+039_001/002	19.25	20.19	7.8861	1.895	1.885	-----M	-----M	67	50
LQAC_128+011_005/006	0.0	19.41	8.0646	0.589	0.588	-----IJKL-	---E---KLM	76	111
LQAC_322-006_003/004	19.08	19.24	8.2125	2.065	2.062	-----M	-----M	56	34
LQAC_204+048_006/007	14.25	17.45	8.4238	0.028	0.028	-----M	---E---J--M	1	158
LQAC_184+050_007/008	19.6	17.15	9.0124	1.456	1.457	---E---KLM	---E---JKLM	7	86
LQAC_249+026_006/007	21.53	0.0	9.2052	2.54	2.54	-----M	-----I-KL-	140	6
LQAC_116+043_008/009	19.72	19.97	9.2084	0.501	0.501	---E---KLM	---E---KLM	105	121
LQAC_206+026_009/010	19.61	19.46	9.225	2.03	2.03	-----I-KLM	-----I-KLM	80	38
LQAC_343+013_013/014	0.0	0.0	9.2484	0.543	0.543	-----M	-----IJKL-	149	116
LQAC_253+026_011/012	18.92	18.39	9.6202	1.904	1.899	---E---JKL-	---E---KL-	37	48
LQAC_199+000_014/015	20.57	18.8	10.054	0.138	0.138	-----M	-----M	44	141
LQAC_200+045_001/002	18.16	0.0	10.436	0.109	0.11	---E---JKLM	-----M	25	145
LQAC_172+007_009/010	18.05	0.0	10.603	2.654	2.668	-B-E---JKLM	-----IJK--	24	2

Notes. Letters in the last column are LQAC-2 flags indicating original catalogues: A = ICRF2, B = VLBA, C = VLA, D = JVAS, E = SDSS, F = 2dF, G = 2dF-SDSS LRG and QSO Survey, H = FIRST, I = Hewitt and Burbidge, J = 2MASS, K = GSC2.3, L = B1.0, M = Véron-Cetty & Véron. The parameters z_1 and z_2 are redshift of both quasars, U_1 and U_2 their magnitude in the U band.

Table 7. continued.

Quasar 1/2	U_1	U_2	θ	z_1	z_2	Catalog ref 1	Catalog ref 2	Position when sorted by U	Position when sorted by z
LQAC_248+033_013/014	0.0	18.7	10.745	1.85	1.87	-----IJKL -	---E----KLM	42	54
LQAC_151+041_003/005	19.02	18.03	10.752	1.734	1.734	-----M	-----M	21	65
LQAC_151+041_003/005	19.02	18.03	10.752	1.734	1.734	-----M	-----M	20	66
LQAC_171+003_009/010	23.92	17.38	10.857	0.561	0.545	---E-----	---E---JKL -	10	114
LQAC_154+038_010/011	0.0	17.4	11.172	0.38	0.386	-----I-K -	---E---H-JKLM	11	125
LQAC_019+031_003/004	19.57	21.62	11.218	2.64	2.624	-----M	---E----KLM	90	3
LQAC_122+031_018/019	19.74	21.43	11.303	1.3	1.301	---E----KL -	---E----KL -	108	96
LQAC_151+041_004/006	20.01	19.15	11.525	1.734	1.738	-----M	---E----LM	61	61
LQAC_172+024_001/002	18.33	18.44	11.583	1.607	1.6	---E---JKL -	-----M	33	74
LQAC_238+004_003/004	19.55	19.14	11.682	1.564	1.565	---E---KL -	---E---KL -	60	77
LQAC_238+004_003/004	19.55	19.14	11.682	1.564	1.565	---E---KL -	---E---KL -	59	78
LQAC_197+029_019/020	0.0	20.38	11.739	1.71	1.71	-----IJKL -	-----M	127	68
LQAC_204+000_044/045	21.31	21.28	11.778	2.309	2.294	-----G---KLM	-----G---K-M	139	14
LQAC_196+031_001/002	19.02	0.0	11.910	1.291	1.289	---E---KLM	-----IJKL -	54	97
LQAC_237+018_003/004	19.28	17.84	11.927	1.442	1.442	-----M	-----I-KL -	17	87
LQAC_149+069_009/010	19.78	0.0	12.011	2.04	2.033	-----M	-----IJKL -	111	37
LQAC_241+028_004/005	0.0	20.29	12.138	1.8	1.8	-----IJKL -	-----M	126	58
LQAC_340+000_010/011	18.76	0.0	12.873	2.1	2.1	-----M	-----IJKL -	43	29
LQAC_149+003_014/015	20.47	0.0	12.921	0.091	0.09	---E---JKL -	-----M	129	149
LQAC_348+000_069/070	20.51	21.72	12.960	1.35	1.354	-----M	---E-G---KL -	132	91
LQAC_013+000_025/026	21.31	20.57	13.250	1.737	1.734	-----M	---E-G---KL -	134	64
LQAC_187+007_015/016	0.0	18.37	13.515	1.878	1.882	-----I-K -	---E---KLM	34	52
LQAC_237+011_009/010	0.0	19.69	13.588	2.15	2.15	-----I-KL -	-----M	102	21
LQAC_150+002_235/236	0.0	0.0	13.646	0.358	0.358	-----M	-----M	150	127
LQAC_159+047_009/010	0.0	0.0	14.200	0.064	0.063	-----M	-----M	151	155
LQAC_210+012_005/006	19.68	19.82	14.544	2.053	2.068	-----M	-----M	101	35
LQAC_013-009_008/009	20.17	18.38	14.630	2.11	2.125	-----M	---E---JKL -	35	26
LQAC_184+030_008/009	17.94	23.77	14.857	0.363	0.362	---E---JKLM	---E---KL -	19	126
LQAC_126+023_004/005	19.2	18.91	14.953	0.535	0.536	---E---JKLM	---E---KLM	48	119
LQAC_137+000_025/026	20.31	16.88	14.978	1.887	1.873	---E---KL -	---E---JKL -	5	53
LQAC_248+041_004/005	0.0	19.11	15.038	0.136	0.138	-----M	---E---JKLM	58	143
LQAC_204-000_100/102	0.0	19.35	15.144	1.808	1.818	-----I-KL -	---F---KLM	72	56
LQAC_259+025_004/005	19.31	20.36	15.238	2.17	2.172	-----M	---E---KL -	70	19
LQAC_149+049_008/009	19.3	0.0	15.401	0.241	0.234	---E---JKLM	-----M	68	136
LQAC_204+027_012/013	19.34	0.0	15.657	1.95	1.95	-----M	-----IJKL -	71	45
LQAC_003+000_002/003	21.64	21.14	15.938	1.633	1.641	---E---KLM	---E---KLM	138	70
LQAC_335+012_002/003	20.22	19.4	15.956	2.003	1.987	-----M	-----M	75	40
LQAC_334+021_002/003	0.0	0.0	16.196	0.0	0.02	-B-----JKL -	-----M	152	160
LQAC_144+054_009/010	17.09	0.0	16.400	0.102	0.1	-----M	-----IJKL -	6	148
LQAC_207+000_057/058	19.47	20.75	16.492	1.836	1.836	---EFG---KL -	---G---K-M	82	55
LQAC_187+011_009/010	0.0	0.0	16.591	2.458	2.458	-----I-KL -	-----M	153	9
LQAC_223+047_010/011	0.0	0.0	16.678	0.07	0.07	-----M	-----M	154	153
LQAC_203+026_014/015	19.65	0.0	16.820	1.556	1.556	-----M	-----IJKL -	98	79
LQAC_212+052_014/016	0.0	22.7	16.924	0.467	0.462	-----M	-C-----M	142	122
LQAC_141+029_011/012	18.71	18.59	17.458	0.697	0.705	---E---KLM	-----M	40	106
LQAC_193+001_009/010	18.96	19.25	17.572	2.041	2.051	-----M	---E---KL -	50	36
LQAC_152+004_012/013	19.59	20.28	17.685	1.51	1.508	-----M	---E---KL -	92	85
LQAC_126+009_015/016	19.48	0.0	17.702	0.26	0.26	---E---JKLM	-----M	83	131
LQAC_053-007_003/004	19.96	19.59	18.191	2.112	2.102	-----M	-----M	91	28
LQAC_355-000_068/069	0.0	18.18	18.306	1.366	1.369	-----IJKL -	---E---JKLM	26	90
LQAC_148+060_014/015	20.67	19.98	18.653	0.717	0.72	---E---KLM	-----M	116	105
LQAC_131+027_011/012	19.16	19.79	18.679	2.114	2.119	-----M	---E---KLM	63	27
LQAC_315+016_001/002	0.0	0.0	18.708	2.12	2.12	-----I-KL -	-----M	156	24
LQAC_315+016_001/002	0.0	0.0	18.708	2.12	2.12	-----I-KL -	-----M	155	25
LQAC_205+028_009/010	0.0	19.63	18.847	0.78	0.78	-----IJKL -	-----M	95	104
LQAC_044+000_065/001	20.42	19.73	18.951	0.893	0.892	---E---KL -	-----M	107	102
LQAC_246+026_014/016	0.0	17.8	19.029	2.526	2.522	-----IJKL -	---E---H-JKLM	16	7
LQAC_240+018_015/016	0.0	0.0	19.228	2.31	2.31	-----I-KL -	-----M	157	13
LQAC_195+029_005/006	16.18	0.0	19.443	0.024	0.023	-----M	-----M	3	159
LQAC_259+060_010/011	21.67	20.49	19.712	0.242	0.234	-----M	-----M	131	135
LQAC_030+000_027/028	20.0	20.34	20.082	2.293	2.299	-----M	---E---KLM	119	15
LQAC_213+000_017/018	19.25	21.62	20.093	0.565	0.539	---E---KL -	---G---K-M	66	115
LQAC_205+005_008/009	0.0	17.28	20.292	0.266	0.266	-----I-KL -	---E---JKLM	8	130

Table 7. continued.

Quasar 1/2	U_1	U_2	θ	z_1	z_2	Catalog ref 1	Catalog ref 2	Position when sorted by U	Position when sorted by z
LQAC_250+039_028/030	0.0	19.96	20.649	0.594	0.591	-----IJKL -	---E-----KLM	115	110
LQAC_329+000_016/017	21.28	20.52	20.809	2.55	2.545	---E-----K-M	---E-----KLM	133	5
LQAC_150+046_004/005	0.0	20.07	20.937	0.08	0.086	-----M	---E----JKLM	121	150
LQAC_179+028_004/005	18.25	21.97	20.999	0.349	0.327	---E----JKL -	---E-----KL -	28	128
LQAC_169+013_002/003	21.59	20.02	21.242	3.029	3.009	---E-----KL -	-----M	120	1
LQAC_146+042_004/005	17.56	18.78	21.268	0.074	0.075	---E----JKLM	-----M	15	152
LQAC_318+006_004/005	0.0	0.0	21.304	0.398	0.398	-----IJKL -	-----M	158	124
LQAC_134+051_001/003	18.97	20.1	21.714	0.543	0.543	---E----JKL -	---E-----KLM	51	117
LQAC_228+025_004/005	0.0	19.31	21.745	1.966	1.977	-----IJKL -	---E-----KLM	69	42
LQAC_153+009_006/007	19.99	20.13	21.878	2.291	2.292	-----M	---E-----KL -	117	16
LQAC_230+056_004/005	19.86	20.03	22.059	1.58	1.57	---E-----KL -	---E-----KL -	113	76
LQAC_194+000_020/021	17.42	18.94	22.175	1.26	1.284	---E--IJKLM	---F----KLM	12	98
LQAC_250+039_019/020	0.0	19.81	22.842	2.381	2.382	-----IJKL -	---E-----KL -	112	11
LQAC_185+046_010/012	0.0	0.0	22.940	0.185	0.185	-----M	-----M	159	138
LQAC_167+066_002/003	20.6	20.2	23.070	0.137	0.137	-----M	-----M	123	142
LQAC_180+000_016/017	19.06	18.39	23.219	1.367	1.37	AB--EF---KLM	-----I-KL -	36	89
LQAC_132+037_002/003	18.22	0.0	23.355	0.307	0.307	---E----JKLM	-----I-KL -	27	129
LQAC_009-000_046/048	21.8	20.91	23.408	1.786	1.783	-----G---KLM	-----G---K-M	136	60
LQAC_131+044_019/020	21.1	0.0	23.775	1.1	1.1	-----M	-----IJKL -	137	100
LQAC_203-000_049/050	20.27	21.04	23.844	0.608	0.611	-----G---LM	-----G---KLM	124	108
LQAC_202+031_012/013	0.0	17.46	23.917	0.241	0.242	-----IJKL -	---E----JKLM	14	134
LQAC_195+027_009/011	18.45	0.0	24.087	0.242	0.243	---E----JKLM	-----I-K--	38	133
LQAC_144+033_040/041	19.7	21.33	24.173	1.535	1.53	---E-----KL -	---E-----KL -	103	81
LQAC_136+000_002/003	19.36	20.17	24.346	1.615	1.643	---E-----KL -	---E-----KL -	73	73
LQAC_143+033_020/021	20.37	19.45	24.484	1.634	1.631	---E-----KL -	---E-----KL -	78	72
LQAC_166+000_057/059	19.27	18.99	24.675	1.879	1.882	---EF---KL -	---FG---KLM	52	51
LQAC_147+049_008/009	0.0	18.85	24.747	1.223	1.251	-----I-K--	---E-----KLM	46	99
LQAC_240+049_003/004	23.18	18.65	25.461	0.244	0.246	---E----JKLM	---E----JKLM	41	132
LQAC_201-000_010/011	20.48	21.41	25.816	1.34	1.358	-----G---KLM	-----G---KLM	130	92
LQAC_144+049_004/005	0.0	19.21	26.902	1.321	1.315	-----IJKL -	---E-----KLM	65	94
LQAC_208+000_042/043	22.04	18.85	26.908	1.633	1.64	-----G---K-M	---F----KLM	45	71
LQAC_161+034_009/010	0.0	19.52	26.962	2.347	2.355	-----IJKL -	---E----JKLM	85	12
LQAC_173+008_005/006	19.4	19.76	27.101	1.526	1.524	---E-----KL -	---E-----KL -	74	83
LQAC_170+013_010/011	0.0	19.54	28.262	1.94	1.947	-----IJKL -	---E-----KLM	89	46
LQAC_176-001_026/027	19.0	20.21	28.612	1.972	1.977	---F----KLM	---F----KLM	53	41
LQAC_178-000_010/011	19.66	19.09	29.188	0.554	0.552	---F----KLM	---E-----KL -	57	113
LQAC_246+026_019/020	0.0	0.0	29.349	2.183	2.183	-----IJKL -	-----M	160	18
LQAC_044-000_029/030	20.28	19.47	29.464	1.321	1.318	---E-----KLM	---E---I-KLM	81	93

This area, shown in Fig. 21 contains 4326 quasars among the 23 660 included in the 2dF catalogue, that is to say, 18.28% of the sample, and 1731 quasars among the 126 577 of the SDSS (8th release), which corresponds to 1.36%. A cross-identification in the area above leads to a surprising result: this area totals 5157 quasars present in at least one of the two surveys, but with only 900 objects belonging to the two catalogues (17.55%), 831 only to the SDSS (16.20%) and 3426 only to the 2dF (6682%).

Moreover, to the set of 5157 quasars mentioned above we must add 2563 quasars belonging neither to the SDSS nor the 2dF to the set of 5157 quasars mentioned above. They are present in the selected area and included in the LQAC-2. Half of them come from various sub-catalogues already compiled by Véron-Cetty & Véron (2010). The other half comes essentially from a specific investigation of the common area by da Angela et al. (2008). Thus, the total number of quasars discovered in the area amounts to 7720 objects. With respect to this total number, the percentages above are significantly reduced: no more than 22.42% of objects have been detected by the SDSS, 55.14% by the 2dF and only 11.65% by both surveys. Last, a substantial

percentage of 33.20% of objects have not been detected in at least one of the two main surveys.

This means that the SDSS, which is the most ambitious quasar survey ever produced, and which gives an essential part of its objects to the LQAC-2 (67.51%), misses a majority of them (roughly about 3/4) in a given explored area. This fact should not be attributable to the limiting magnitude of detection of the SDSS survey, which is much larger than in other surveys, as will be detailed below. In comparison, the 2dF, which concerns a rather limited area of the sky, can be considered as a particularly meticulous and efficient survey, with roughly 2.5 more quasar detections for a same explored area. In conclusion, we can assert that these two surveys leave a significant large quantity of discoveries to be made, not only in the southern hemisphere, which has been poorly investigated so far, but also in the northern hemisphere, even for areas already explored.

5.3. Photometric comparative analysis

To deepen the comparative study between the two catalogues and to understand the reasons of the relatively poor number of

Fig. 21. Mapping of quasars present both in catalogues SDSS and 2dF. The area is restricted to the common area of those two catalogs and presented in equatorial coordinates.

Fig. 22. Histogram of quasars in the common area of the SDSS and the 2dF with respect to their R magnitude. We present quasars in different curves, depending on if they are common to both catalogues, and therefore depending on which catalogue the value of the magnitude comes from, or if they are present in only one catalogue.

common quasars better, we have performed a photometric analysis of the objects present in both of them. In Figs. 22 and 23, we present the histograms, with respect to respectively the R and U magnitudes, of the objects detected in at least one of the two surveys. In particular, we separate the cases for which the quasar is common to the two catalogues or not and, for cross-identified quasars, we indicate where the value of R or U magnitude comes from. The U and R magnitudes coming from the SDSS and 2dF do not exactly refer to the same nominal wavelengths and bandwidths. In the case of the SDSS (Gunn et al. 1998), the U band (noted u) corresponds to $\lambda_{\text{eff}} = 0.3549 \mu\text{m}$ and a $FWHM = 0.0560 \mu\text{m}$ whereas information cannot be extracted easily concerning the 2dF survey (Croom et al. 2004; Lewis et al. 2002).

In the R band (Fig. 22), we can observe that the peak of common quasars ranges between $18 < R < 19$, whereas the overwhelming majority of quasars detected by the sole 2dF corresponds to $19 < R < 21$. The relative number of quasars detected per magnitude bin is comparatively much more contrasted for the 2dF than for the SDSS. Thus, we remark that

Fig. 23. Histogram of quasars in the common area of the SDSS and the 2dF with respect to their U magnitude. We present quasars in different curves, depending on if they are common to both catalogues, and therefore depending on which catalogue the value of the magnitude comes from, or if they are present in only one catalogue.

the number of objects detected by the 2dF alone is nearly the same as the number of objects detected by the SDSS alone for $18 < R < 19$, whereas this number is roughly seven times larger for the following bin ($19 < R < 20$) and even ten times larger for $20 < R < 21$. Last the origin of the R magnitude estimation (SDSS or 2dF) does not influence significantly the histogram for quasars common to the two catalogues. The parameter $R = 22$ represents roughly the limit of the detection (Fig. 22).

In the U band (Fig. 23) the origin of the magnitude value significantly influences the statistics for common quasars. When U (in fact u) is taken from the SDSS, the peak number of common identifications arises for $19 < u < 20$ whereas it corresponds to $18 < U < 19$ when it is taken from the 2dF. Here the very large majority of detections by the 2dF alone occurs for $18 < U < 21$, with a very neat peak for the central bin, for which the number of detections is more than 10 times the corresponding one by the SDSS alone. This ratio falls to slightly greater than 3 for the following bin ($20 < R < 21$). In comparison, for the SDSS, the magnitude interval for a significant number of detections is much bigger, ranging between $u = 17$ and $u = 25$. Finally, the number of quasars present in 2dF but not in the SDSS as well as in contrast the number of quasars present in SDSS but not in 2dF peak at the same R or U magnitude bin ($19 < R$ or $U < 20$). From all these results we can conclude that the relatively small number of cross-identifications between the two surveys is explained in a large part by different detection sensitivities with respect to magnitude intervals.

5.4. Redshift comparative analysis

To complete our study, and to fully benefit from the presence of the common 2dF-SDSS selected area, we focus on the redshift of quasars present or missing in both surveys. The histograms of the number of quasars with respect to their redshift are presented in Figs. 24 and 25, respectively, for the SDSS and for the 2dF. For the sake of comparison, we also present in each figure the histogram of quasars common to the two surveys as well as the histogram of the total sample of recorded quasars in the explored area. Some important remarks can be pointed out. First, for very low redshifts ($z < 0.2$), the contribution of both large surveys is very small with respect to that of other catalogues. This is

Fig. 24. Histogram of the number of SDSS quasars with respect to z . In red, proportion of quasars common to the SDSS and 2dF surveys; in blue, quasars only in SDSS catalogue; in grey, quasars missing from SDSS and 2dF.

Fig. 25. Histogram of the number of 2dF quasars with respect to z . In red, proportion of quasars common to the SDSS and 2dF surveys; in green, quasars only in 2dF catalogue; in grey, quasars missing from SDSS and 2dF.

certainly due to selection effects, wherein the photometric filtering algorithms lead to particularly efficient selection of candidate quasars, in both surveys, for sufficiently large values of z .

Second, all the histograms present a leading peak around $z = 1.5$. By combining the QSO sample from the 2dF-SDSS luminous red galaxy (LRG) and QSO survey, da Angela et al. (2008) remarked on and deeply investigated the clustering of $z \approx 1.5$ QSO's, deducing some cosmological consequences from appropriate correlation functions.

Third, the histogram for quasars only detected by the SDSS is rather flat with a short peak for a small redshift value (at $z = 0.3$), which can again be explained by a selection effect. At last, the cut-off limit for z in the 2dF survey as well as for the other surveys, except the SDSS, is around $z = 3$, whereas for this last catalogue a significant number of quasars is found up to $z = 5$. Detections of objects with $5 < z < 7$ are not represented because of their very small relative number. Whatever is considered to be the z interval, the number of quasars detected by the SDSS alone (24) is slightly bigger than the number of quasars in common, whereas it is several times larger in the case of the 2dF (Fig. 25).

Fig. 26. Value of the standard deviation of $z_{\text{SDSS}} - z_{\text{2dF}}$ for quasars common to SDSS and 2dF surveys.

Another instructive topic related to the common selected area concerns the comparison of the values of the redshifts for the cross-identified quasars in both surveys. This gives clear and direct information on the external accuracy of the z determination and its dependency on the value of z itself. In Fig. 26, we show the standard deviation between the determinations of z done by each survey, with respect to each 0.1 interval of z . We can notice that the difference is smaller than 0.04 excepted for two intervals for which the number of objects is particularly high, i.e., $1.5 < z < 1.6$ and $1.8 < z < 1.9$, respectively. Finally, the quality of determination is much better for $z < 1$ with an uncertainty smaller than 0.02, than for $z > 1$, where it is generally larger than this last value.

6. An estimation of the whole set of quasars N_{Gaia} detectable by the space probe *Gaia*

The results shown in the preceding section should help us to make a rough evaluation of the total number of quasars N_{Gaia} that could be detected by the space astrometric mission *Gaia*. To understand the method of detection of quasars by the probe we can refer to Mignard (2002): the major problem will be the recognition among many point-like sources, as stars. Several indicators will help make the decision, such as the absence of parallax, the negligible proper motion, the short term variability and, before all, the spectral signature summarized by a set of colour indices. Indeed, the combination of the broadband and medium band filters will permit a photometric identification of quasars from virtually any type of star. In particular, the decontamination from white dwarfs, a traditional contaminant in colour selected quasars will be resolved from medium band colours thanks to a good sensitivity to the $\text{Ly}\alpha$ line. In the following, we accept the principle that from these criteria that the quasars as selected by *Gaia* will be the same kinds of objects as those compiled in the LQAC-2.

As the detection of quasars by the satellite will be possible under the magnitude threshold $V = 20$ (Mignard 2002), N_{Gaia} could be determined from the following principle: first, we estimate the total number of quasars with $V < 20$ in the dense area considered in the last section, common to the SDSS and 2dF surveys. Second, we simply extrapolate this number to the whole sky. Third, we take the galactic extinction into account, which significantly diminishes the value of N_{Gaia} . This way of computation is rather straightforward once we have solve two

Fig. 27. Numbers n_V and n_U of quasars found at a given magnitude threshold in a dense selected sky area, respectively in V and U bands. The thin curve indicates the ratio n_U/n_V . (This ratio is multiplied by 1000.)

Fig. 28. Percentage of quasars found at a given magnitude threshold in a dense selected sky area, in V and U bands, respectively, with respect to the total number of quasars detected. The dashed vertical line corresponds to the GAIA cut-off in V band.

difficulties. First, we have V magnitudes for only 3775 quasars in the selected area, which constitutes no more than 48.90% of the total population of 7720 recorded objects, whereas the U magnitude has been evaluated for a large majority of 7662 objects, that is to say, 99.25% of the sample. Second, it is difficult to evaluate the ratio $\rho_{G.E.}$ of the number of quasars non-visible because of the galactic extinction, which concerns a band of galactic latitude included roughly inside the interval $-20^\circ < b < +20^\circ$ (Fig. 10).

We can remedy the first difficulty by adopting the following procedure: for the 3749 quasars of the selected area having both a V and a u magnitude we calculate at a given magnitude m (and more particularly for $m = 20$) the ratio of quasars with $V < m$ to the number of quasars with $u < m$. The results are shown in Fig. 27 for each integer value of the magnitude between $m = 15$ and $m = 23$.

We study the value of the ratio in a magnitude range that concerns us particularly, around the *Gaia* V magnitude cut-off, between 19.0 and 20.5. This ratio, always bigger than 1, is

Fig. 29. Number of expected quasars detected by the GAIA satellite during its mission, according to four values of the percentage of quasars missed because of the galactic extinction missing ratio $\rho_{G.E.} = 0, 0.1, 0.2, 0.3$.

slightly decreasing with the magnitude. It takes the maximum value 1.583 for $V = u = 19.0$, and the minimum value 1.113 for $V = u = 20.4$. Then, we extrapolate this ratio to the total sample of 7720 quasars detected in the area. This gives us an estimation of the total number of quasars visible at a given V magnitude threshold. At the magnitude value $m = 20.0$, the ratio V/u of quasars visible below this threshold is 1.140. Supposing that the sample of 4283 quasars (55.9%) detected in the area and characterized by $u < 20.0$ represents the complete estimation, we deduce that approximately 4882 quasars should be visible at $V < 20.0$ for the same area, which corresponds to 63.7% of our sample. By adopting the same process we could deduce the ratio of quasars visible in the field at various magnitude thresholds from $18 < u < 20.5$ and $19 < V < 20.5$. The results are presented in Fig. 28 with the real percentages for u and the extrapolated ones for V , with respect to the total sample.

Now we can evaluate, in absence of galactic extinction, what should be the total number of quasars N_t with $V < 20$. Our test area above was extended along $\pm 2^\circ$ in declination north and south of the celestial equator, and 35° in right ascension, which results in a sky surface coverage of 140 square degrees. That constitutes 0.33096% of the total celestial sphere surface. By simple extrapolation, this leads to a total estimation of $N_t = 4882/0.0033096 = 1\,475\,290$ quasars with $V < 20$ for the total celestial sphere. The same kind of calculation can be carried out at any other magnitude threshold.

As we have already explained above, the second difficulty to evaluate N_{Gaia} consists in evaluating the ratio $\rho_{G.E.}$ of quasars that are not visible because of the presence of galactic extinction, with the relationship: $N_{Gaia} = N_t \times (1 - \rho_{G.E.})$. The effect of the galactic extinction on the apparent magnitude of quasars can be computed locally as was the case in the LQAC-2 when estimating at the same time their absolute magnitude M_B in the blue band and in the infrared band M_i (Souhay et al. 2012). For that purpose, the reddening value $E(B - V)$ in magnitude was based on the galactic extinction map of Schlegel et al. (1998). Nevertheless, it is difficult to extrapolate the magnitude algorithm for the whole sky, in particular because of the absence of an accurate extinction map for some areas of the celestial sphere close to the galactic plane.

Basically, a total impenetrable and isolated screen extended on galactic latitude $-20^\circ < b < +20^\circ$ would lead to

$\rho_{G.E.} = 0.342$. We expect that the real value of $\rho_{G.E.}$ is lower than this last value. In Fig. 29, we show the number of quasars that should be detected at a given V magnitude threshold, for four different percentages (0%, 10%, 20%, 30%) of quasars lost for detection due to the galactic extinction, that is to say, for $\rho_{G.E.} = 0.0, 0.1, 0.2, 0.3$. We observe that even by adopting a 30% loss, our estimation of quasars brighter than $V = 20.0$ accessible to detection by *Gaia* is slightly bigger than 1 million. This corresponds roughly to twice the number currently mentioned in the frame of the preparation of the *Gaia* mission (Mignard 2011). This number significantly decrease when taking the possible lack of detection at the magnitude limit $V = 20$ into account because of an insufficient signal/noise ratio for some colours of the photometry. With a detection limit at $V = 19$, it should reach approximatively 500 000 quasars.

7. Conclusion

The construction of a compiled catalogue of all the recorded quasars, such as the LQAC-2, represented a unique opportunity to perform various studies on the whole known quasar population. This was the purpose of this paper, in which we carried out several kinds of analysis.

First, we evaluated the improvement due to the recalculation of the quasars equatorial coordinates through the LQRF algorithms set up by Andrei et al. (2009), with respect to the coordinates initially given by the original catalogues taken into account in the compilation. In particular, we have pointed out the magnitude dependence of the quality of these astrometric determinations.

Second, we have shown in some detail the dramatic lack of uniformity of the whole sky quasar distribution, in terms of galactic, equatorial, and ecliptic coordinates. In all case, we have compared this distribution with an ideal uniform one, thus clearly showing the depleted areas for which observational efforts could be done towards a better coverage. Obviously, the galactic extinction will constitute an unavoidable obstacle for this aim at low absolute galactic latitudes.

Third, we have performed a meticulous analysis on the statistical distribution of the nearest neighbour, both for the overall LQAC-2 quasar population and for a specific limited area of the sky, homogeneous in terms of surface density. We have shown that in the second case the distribution of quasars with respect to the distance of the nearest neighbour is in very good agreement with theoretical modelling, in contrast with the first case, characterizing an important heterogeneity of the sample. This study on the distance of the nearest neighbours enabled us to detect the cases of pairs with very small angular distances, which could be interpreted with three different categories: pairs of quasars in the same line-of-sight, but without any link together, real binary quasars which should in consequence offer the same redshift, at last double listings, i.e., single quasars which by error have been recorded twice with different equatorial coordinates. We have compared the number of quasars of the first category (close position but significant difference of redshifts) with theoretical expectations, thus showing a good agreement, excepted for angular distance smaller than $10''$. Then we have analysed DSS optical images, when available, to separate the quasars belonging to the second and third category. From this study, we extracted a set of 159 objects clearly identified and confirmed by the DSS as binary

quasars, from which we have isolated and listed a subset of those with exceptional characteristics (smallest angular distance, lowest and highest redshifts, lowest U magnitude for one of the components).

Fourth, we have compared the data given by the two densest surveys, the SDSS and the 2dF, in a common area. This comparative study enabled us to understand the degree of completeness of these surveys under their respective magnitude threshold as well as their relative number of quasars detected at a given R or U magnitude interval. Globally, we showed that 4326 objects were detected by the 2dF while only 1731 ones were detected by the SDSS, that is a ratio roughly 2.5 compared with the first catalogue. Moreover, only 900 objects were found in both surveys, whereas 2563 supplementary quasars of the LQAC-2 are not found in at least one of the two surveys. The study shows globally that 2dF quasars are concentrated in small magnitude intervals with a neat peak at $19 < R/U < 20$, whereas SDSS detections are regularly displayed along magnitude intervals $17 < r < 22$ and $17 < u < 23$.

Finally, on the basis of the preceding study we extrapolated the counting results to evaluate the whole sky number of quasars that could be observed by the up-coming *Gaia* space mission. We arrived at the conclusion that by adopting the same surface density as in the common area above and even by considering a 30% miss of quasars due to galactic extinction, a little more than 1 million objects could be detected by the probe with a $V = 20$ cut-off.

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