The molecular envelope of CRL 618: A new model based on Herschel/HIFI* observations

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Received 25 June 2013 / Accepted 10 September 2013

ABSTRACT

Aims. We study the physical properties and molecular excitation of the different warm gas components found in the protoplanetary nebula CRL 618. The proper study of the nebular structure and its implications on the dynamics and kinematics of the molecular gas are of particular importance for understanding the evolution of these objects.

Methods. We revise our previous Herschel/HIFI observations, which consist of several \(^{12}\)CO and \(^{13}\)CO lines in the far-infrared/sub-mm band in the nebula CRL 618. These data have been re-analyzed in detail by improving calibration, the signal-to-noise-ratio, and baseline subtraction. Due to the high performance of Herschel, it was possible to identify the contributions of the different nebular components to the line profiles. Previous optical imaging and mm-wave interferometric mapping revealed that CRL 618 shows a complex molecular structure composed of a large and diffuse spherical halo, a compact central core, double shells, and a fast bipolar outflow. We have used a spatio-kinematical model to better constrain the temperature, density, and kinematics of the molecular components probed by the improved CO observations.

Results. The \(^{12}\)CO and \(^{13}\)CO \(J = 16–15\), \(J = 10–9\), and \(J = 6–5\) transitions are detected in this source. The line profiles present a composite structure showing spectacular wings in some cases, which become dominant as the energy level increases. Our analysis of the high-energy CO emission with the already known low-energy \(J = 2–1\) and \(J = 1–0\) lines confirms that the high-velocity component, or the fast bipolar outflow, is hotter than previously estimated with a typical temperature of \(\sim 300\) K. This very fast component may then be an example of a very recent acceleration of the gas by shocks that has not yet cooled down. We also find that the dense central core is characterized by a very low expansion velocity, \(\sim 5\) km s\(^{-1}\), and a strong velocity gradient. We conclude that this component is very likely to be the unaltered circumstellar layers that are lost in the last AGB phase, where the ejection velocity is particularly low. The physical properties of the other two nebular components, the diffuse halo and the double empty shell, more or less agrees with the estimations derived in previous models.

Key words. stars: AGB and post-AGB – circumstellar matter – stars: mass-loss – planetary nebulae: individual: CRL 618

1. Introduction

Asymptotic giant branch (AGB) stars are pulsating red giants surrounded by spherical and slowly expanding circumstellar envelopes (CSE) formed by their copious mass loss. In the late AGB phase, the mass loss rate can be as high as \(10^{-4}\)\(M_{\odot}\)yr\(^{-1}\), and most of the stellar atmosphere is removed, exposing the central star. Once the mass loss ceases, the CSE expands and cools, and the effective temperature of the central star increases to ionize the circumstellar material. The CSE with its central AGB star evolves to form a planetary nebula (PN) that surrounds a blue or white dwarf. The transition between these two stages is known as protoplanetary nebula (PPN) or post-AGB phase. During this PPN transition, which is believed to be very short and lasting only about 1000 yr, the nebula experiments dramatically changes in its morphology and its physical and chemical properties.

The PPNe show fast bipolar outflows and slower components that are probably the remnants of the ejected material in the previous AGB phase. The spectacular dynamics usually observed in these objects is thought to be the result from the interaction between the AGB and post-AGB winds. However, the way this process takes place is not well understood yet. The PPNe are the ideal targets for understanding basic and important aspects in the stellar evolution, as are the mass-loss mechanisms during the late AGB and post-AGB phases, and the shaping of PNe. A deep study of PPNe can be approached through multiwavelength observations from the visible or near-infrared ranges, which tend to select the hot and diffuse regions with temperatures \(>1000\) K, to the warm and dense regions, which have a temperature range of \(100\ K \leq T_{k} \leq 1000\) K and are traced by the far-infrared and sub-mm observations, with cooler gas probed by mm-wave molecular lines. Because the various components in PPNe show strong emission in molecular lines, their observation is the best tool to study these nebulae. Thanks to these observations, the dynamics, structure, and physical conditions in several PPNe are well known (e.g. Bujarrabal et al. 2001; Sánchez Contreras et al. 2004).

One of the best sources to study the evolutionary sequence from the AGB to the PN stages is CRL 618. This is a well known PPN that initiated its post-AGB phase about 100 yr ago (Kwok & Bignell 1984) and that is rapidly evolving to form a PN. The atomic and ionized nebula is composed of a compact 0′′2 × 0′′4.
HII region that is visible at cm- and mm-radio continuum wavelengths (Wynn-Williams 1977; Kwok & Bignell 1984; Sánchez Contreras et al. 2004; Nakashima et al. 2007), which is expanding at ~20 km s\(^{-1}\), and of multiple optical lobes (Trammell & Goodrich 2002) with shocked gas that expands with velocities up to ~200 km s\(^{-1}\) (Sánchez Contreras & Sahai 2004). Most of the circumstellar material in this source is still in molecular gas. In their interferometric \(^{13}\)CO \(J = 2–1\) maps, Sánchez Contreras et al. (2004) identified several molecular components in this source: (1) a roughly spherical and extended halo with a mass of 0.05 \(M_\odot\), and that is ~20'' in size that expands at a low velocity of ~17 km s\(^{-1}\), which may be the result of the spherical mass ejection of the central star during the AGB; (2) a fast bipolar outflow with a mass of 0.09 \(M_\odot\), and that is ~3'' in size with velocities that increase with the distance to the central star from ~40 to ~340 km s\(^{-1}\), as explained by the result of the interaction of the AGB and post-AGB winds; (3) a compact and dense central core with a mass of 0.08 \(M_\odot\) and a low expansion velocity of ~12 km s\(^{-1}\), which is believed to be a more recent mass loss episode; and (4) another slow axial component with a mass of 0.04 \(M_\odot\) that is radially expanding at moderate velocities, ~22 km s\(^{-1}\), which may represent the entrained layers of gas between the fast-flow and the slow AGB wind.

The most common molecular lines usually observed in PPNe are the low-\(J\) rotational transitions of \(^{12}\)CO and \(^{13}\)CO (\(J = 2–1\) and \(J = 1–0\)). Thanks to extensive studies of these lines that are performed by means of single-dish observations and interferometric mapping (see for example, Bujarrabal et al. 2001; Castro-Carrizo et al. 2010), important properties of PPNe have been discovered. However, they are not very useful for studying the gas at higher temperatures since these molecular transitions require temperatures of only ~10–20 K to be excited. Because of the crucial role of shocks in the formation and evolution of PPNe, it is particularly important to observe these warmer regions.

A preliminary analysis of the Herschel/HIFI observations in CRL 618 was presented in Bujarrabal et al. (2010). Several \(^{12}\)CO and \(^{13}\)CO lines and emission from other molecules, like CN, HCN or H\(_2\)O, were detected. In this study, the authors made a preliminary nebula model to fit the \(J = 16–15\) \(^{12}\)CO transition, concluding that a theoretical approach including all the CO detections was necessary to better derive the physical properties of the different molecular components found in CRL 618.

We present a new calibration and analysis of several rotational lines of \(^{12}\)CO and \(^{13}\)CO in CRL 618, as previously presented in Bujarrabal et al. (2010). Our improved observational results have been fitted by a nebula model based on the different molecular components known to coexist in the envelope of CRL 618. We also have included the low-\(J\) lines (\(J = 2–1\) and \(J = 1–0\)) of \(^{12}\)CO and \(^{13}\)CO in this study. All the detected CO transitions have been simultaneously modeled, leading to a deeper understanding of the excitation and kinematics of the molecular structures of CRL 618.

### 2. Observations and data calibration

We used the Heterodyne Instrument for the Far Infrared (HIFI) on board the Herschel Space Observatory (Pilbratt et al. 2010) to observe the high excitation transitions (\(J = 16–15\), \(J = 10–9\), and \(J = 6–5\)) of \(^{12}\)CO and \(^{13}\)CO in the PPN CRL 618. These observations are part of the guaranteed time key program HIFISTARS. The preliminary version of these CO data, as published by Bujarrabal et al. (2010, 2012), have been re-analyzed in detail by improving the calibration and the signal-to-noise-ratio.

### Additional lines

Additional molecular lines from other species like H\(_2\)O or HCN were also detected within the observed frequency ranges (for details see Bujarrabal et al. 2010, 2012), but are not discussed here. These HIFI data are combined with the \(J = 2–1\) and \(J = 1–0\) results of \(^{12}\)CO and \(^{13}\)CO, as observed in this source by Bujarrabal et al. (2001) with the IRAM 30 m telescope. Rest frequencies, main-beam temperatures, and calibration uncertainties of the observations are given in Table 1.

The HIFI operates as a DSB (double sideband) receiver. In this mode, the sky frequencies above and below the local oscillator frequency are simultaneously observed. Then, the intermediate frequency (IF) signal is fed into the spectrometer, which was the HIFI wide-band spectrometer (WBS) in our case, an acousto-optical spectrometer that provides simultaneous coverage of the full IF band in the two available orthogonal receivers (H and V).

The data were observed using the dual beam switching (DBS) mode. The HIFI internal mirror chops between the source position and an emission-free position 3'' away. Using this method, the residual standing waves are expected to be minimized. This DBS procedure worked well except for the high frequency bands 7A and 7B and especially in the V receiver, where strong ripples were found.

We processed the data using the standard HIFI pipeline within the HIPE software. A modified version of the level 2 algorithm was used, yielding unaveraged time spectra but with the sub-bands stitched together. All the observed spectra for each sub-band and receiver were checked, and those that showed considerable ripples were removed. Later, the data were exported using the HIPE hiClass tool to CLASS for further inspection, calibration, baseline removal, and final time averaging. When there were no significant differences between the lines detected in the H and V receivers, the data were systematically averaged. Finally, the data originally calibrated in antenna temperature units were converted into main-beam temperatures (\(T_{\text{mb}}\)), using the latest available values for the telescope and beam efficiencies (Roelfsema et al. 2012).

### 3. Line profile results

The presence or absence of different spectral features in the profiles of the observed molecular lines can be used to diagnose the physical properties of the diverse nebular regions found in PPNe. If, in addition, several transitions of the same molecule are simultaneously observed, the overall structure of the PPNe can be studied from the regions where the CO excitation requires temperatures of 10–20 K, which are probed by \(J = 2–1\) and \(J = 1–0\) lines, up to the warm regions with typical excitation temperatures of ~800 K, as in the \(J = 16–15\) transitions.
In Fig. 1, we show the single-dish spectra of the observed $^{12}$CO transitions in CRL 618: $J = 16-15$, 10-9, 6-5, 2-1, and 1-0. The data have been smoothed to obtain a velocity resolution of $\sim 2$ km s$^{-1}$. In general, the profiles present a composite structure with a dominant central component (being the peak in all lines centered at the source systemic velocity, $V_{\text{sys}} = -21$ km s$^{-1}$) and wide wings. From interferometric mapping, we know that the emission from the central component corresponds to an extended ($\sim 20''$) halo expanding at 17 km s$^{-1}$ and that the wings trace a high-velocity ($\sim 250$ km s$^{-1}$) compact bipolar outflow of about 3–4$''$ (Bujarrabal et al. 1988; Neri et al. 1992; Bujarrabal et al. 2001; Sánchez Contreras et al. 2004; Nakashima et al. 2007). We also know that additional nebular components have been found: a central compact core surrounding the HII region, which shows a low velocity expansion and is responsible for the central narrowest peak, and a double elliptical cavity, discovered in the $J = 2-1$ high sensitivity maps made by Sánchez Contreras et al. (2004). As we see in the subsequent sections, the four nebular components are needed and must be included in the nebula model to simultaneously reproduce the observed spectral profiles.

Although the profiles differ significantly, there are common trends that can be seen in Fig. 1. For instance, the halo is the dominant component emitting in the low-$J$ transitions ($J = 2-1$ and $J = 1-0$), whereas the high-velocity wings become progressively dominant as the level energy increases, which are spectacular in the $J = 16-15$ line. Another peculiarity of these $^{12}$CO lines is the absorption features found in the $J = 2-1$ and $J = 1-0$ at velocities $[-60, -40$ km s$^{-1}]$. This has been seen in other molecular lines like HCN ($J = 1-0$) or HCO$^+ (J = 1-0)$ (Neri et al. 1992; Pardo et al. 2004; Sánchez Contreras & Sahai 2004). These blueshifted features appear as a result of the continuum absorption and line self-absorption by cooler gas that is located in the outer envelope of CRL 618. The absorption components are also observed in $^{13}$CO, as mainly seen in the $J = 1-0$. Again, there is a blueshifted feature at velocities $[-64, -52$ km s$^{-1}]$ that is believed to arise from the outer envelope of CRL 618, and another redshifted absorption component visible at $[0-10$ km s$^{-1}]$, which, as seen in the HCO$^+$ data, may not come from CRL 618, since it coincides with the velocity of the foreground gas of the Taurus dark cloud complex (3.5 km s$^{-1}$) (Cernicharo et al. 1989).
We also note that the central component of the profiles becomes significantly narrower in high-$J$ transitions. This is due to the low velocity of the central dense core of the nebula, where we can expect a high excitation.

Another common characteristic of the CO profiles is the clear asymmetries found in the spectral profiles. For instance, the HIFI $^{13}$CO spectra show a high-velocity blue wing that is more intense than the red one, which may be due to real asymmetries in the nebula. Also, the fast increase in the wing/core ratio with the energy of the levels shows that the temperature of the fast outflow may be higher than the values reported in previous model fittings of the nebula (see next section). In the $^{12}$CO data, especially in the HIFI spectra, we also note that the subtraction of the baselines is less accurate because of either the difficulty in selecting the “complete” emission of the corresponding line or the contamination due to emission from other molecules (Bujarrabal et al. 2012). In other cases as in the $J = 16–15$ $^{13}$CO line, the baseline substraction is not accurate enough due to the lack of spectral coverage in the observed frequency settings and the possible presence of standing waves, which are often conspicuous at these high frequencies.

The $^{13}$CO data show a core/ratio increase with $J$ but present weaker wings. The $^{13}$CO/$^{12}$CO ratio is also much lower than 1, meaning that the $^{13}$CO lines are optically thin. This idea is supported by the morphology of the line profiles. The profiles of the low-$J$ $^{13}$CO lines (Fig. 1) are not typically parabolic as those found in optically thick emission (see $^{12}$CO in Fig. 1) but show the complex kinematics of the inner parts of the envelope, which result in profiles with a flat-topped line with spikes. As in the $^{12}$CO lines, there are also asymmetries in $^{13}$CO; for instance, the red-shifted region of the bipolar outflow is stronger and reaches up to $V \sim 40\ km\ s^{-1}$ in the $J = 6–5$ and more clearly in the $J = 2–1$ profile.

A general description of the nebula model, a more detailed analysis and comparison between the CO observed line profiles, and the results of the model fitting are given in the subsequent sections.

### 4. The nebula model

We have used a numerical code that calculates the excitation and emissivity of the $^{12}$CO and $^{13}$CO rotational transitions throughout the various nebula components. The code uses the LVG approximation to calculate the level populations of CO in a large number of points in the nebula. The corresponding positions are defined by the distance of each point to the nebula symmetry axis and to its equator. Then, the derived populations are used to calculate the emission and absorption coefficients to solve the standard radiative transfer equation and to determine the brightness distribution along a high number of lines of sight. Finally, the resulting brightness is convolved with the telescope beam (IRAM 30 m or HIFI; see Table I), which is described by a Gaussian function, to obtain the line profiles in units of main beam temperature ($T_{mb}$). This allow us to compare the model predictions with our HIFI observations.

The LVG approximation can be used to calculate the excitation of a molecule when there is a sufficient velocity gradient in the molecular cloud under study. Points separated a certain distance do not interact radiatively, and therefore only the local physical properties become relevant, which results in a considerable simplification of the calculations. In our case, this theoretical approach is fully satisfied, since CRL 618 is known to present high-velocity gradients. We note that this formalism yields a good approximation to the excitation state, even in cases when the large velocity gradient requirement is scarcely satisfied (Bujarrabal & Alcolea 2013). In this paper, the authors present a wide discussion of the validity of this LVG approximation for a variety of conditions and conclude that the calculations of the molecular excitation of CO are still accurate even in cases where the gradient of the velocity is low, which is not very dependent on the theoretical treatment of the radiative transfer. With this in mind, we have used the proper velocity gradient ($\epsilon = \frac{\Delta V}{\Delta d}$) for each molecular component. For the dense core, ellipses, and outflow, $\epsilon = 1$, and for the outer halo, $\epsilon = 0.1$. In either case, we have checked that the calculations are consistent even if we assume $\epsilon = 1$ for the halo.

We have developed a new code that is based on Bujarrabal et al. (1997) but with significant improvements. Our theoretical model performs more complex calculations of the excitation of both molecules. $^{12}$CO and $^{13}$CO. Since we are fitting the low-$J$ transitions and the high-$J$ lines, which are characterized by high radiative probabilities, we cannot assume that the energy levels are populated under LTE in that case, and therefore require the LVG approximation. To solve the statistical equilibrium equations, we have taken the collisional coefficients from the Leiden Atomic and Molecular Database (Schöier et al. 2005; Yang et al. 2010). In our calculations, we have used collisions with ortho- and para-H$_2$, for which we have adopted an abundance ratio of 3.

As an additional test, we have performed calculations considering the rotational levels within the $\nu = 1$ vibrationally excited state and the effects of their presence in the populations of the $\nu = 0$ levels. In these calculations, we have considered $\Delta \nu = 1$ collisional and radiative transitions and the IR emission at 4.7 $\mu$m (the wavelength of the $\Delta \nu = 1$ transitions) of CRL 618, assuming that it comes from a small region in the center of the nebula. In all cases, these effects were found to be negligible, so we conclude that further refinement of the treatment of the pumping via vibrational states is not necessary.

The molecular structure of the nebula is based on the one proposed by SC04. Some general assumptions in our nebula model include (see Table 2 and discussions in SC04) (1) a distance to the source of 900 pc; (2) an inclination of the source with respect to the plane of the sky of 32°; (3) a local dispersal velocity of 2 km s$^{-1}$; (4) relative abundances of $X(^{12}$CO) = 3 $\times$ 10$^{-4}$ and $X(^{13}$CO) = 1.2 $\times$ 10$^{-5}$; and (5) symmetry with respect to the nebula axis and equatorial plane. For the central HII region, we have used the same parameters as SC04: an angular size of 8 $\times$ 4 $\times$ 10$^{15}$ cm and a brightness temperature of 350 K, which have been derived from their 1 mm radio-continuum interferometer maps. We assumed that the free-free brightness varies with the frequency as $\sim 1/\nu^2$. This is usually adopted for optically thin continuum emission in mm- and submm-waves. In all calculations, we find that the predicted line profiles depend slightly on the assumed HII region properties. At higher frequencies (~690 GHz, 1150 GHz, and 1800 GHz), we have also considered the contribution of the dust continuum, which is known to be dominant (Wyrowski et al. 2003; Lee et al. 2013). To avoid extra parameters, we assumed that the dust brightness distribution is compact and similar to that of the free-free continuum, except for the observed values of the total flux. In any case, we find that the dust emission has a negligible effect in the excitation and profiles of these high-frequency CO lines. We have also assumed that the molecular abundance within the HII region is very low.

The geometrical parameters, velocity field, temperature law, and density distribution of the different molecular components used in the CRL 618 model are summarized in Table 2. As mentioned, we have followed SC04 in the general description of
Table 2. Molecular components of the model for CRL 618.

<table>
<thead>
<tr>
<th>Nebula component</th>
<th>Size (cm)</th>
<th>Radial velocity $V_{\text{exp}}$ (km s$^{-1}$)</th>
<th>Temperature $T$ (K)</th>
<th>Density $\rho$ (cm$^{-3}$)</th>
<th>Mass $M$ ($M_\odot$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Halo</td>
<td>$R_{\text{in}} = 1.6 \times 10^{16}$</td>
<td>$7 + 10 [1 - (R_{\text{out}} / r)]^{1/2}$</td>
<td>$115 (10^{16} / r) + 5$</td>
<td>$1.2 \times 10^6 (10^{16} / r)^2$</td>
<td>0.24</td>
</tr>
<tr>
<td></td>
<td>$R_{\text{out}} = 10^{17}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ellipses</td>
<td>$M = \text{major axis} = 8.4 \times 10^{16}$</td>
<td>$10 [1 + (h / M)]$</td>
<td>$80$</td>
<td>$[1.1-1.05 (h/M)]10^6$</td>
<td>0.04</td>
</tr>
<tr>
<td></td>
<td>$\text{minor axis} = 4 \times 10^{16}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$\text{thickness} = 2.6 \times 10^{15}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$\text{center} = \pm 4.2 \times 10^{16}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Fast outflow</td>
<td>$R_{\text{in}} = 0.9 \times 10^{16}$</td>
<td>$45 + 255 (h - 10^{16}) / (h_{\text{out}} - 10^{16})$</td>
<td>$300 (10^{16} / h) + 5$</td>
<td>$5.5 \times 10^6 (10^{16} / h)^2$</td>
<td>0.07</td>
</tr>
<tr>
<td></td>
<td>$h_{\text{out}} = 2.8 \times 10^{16}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$\text{center} = 7 (r / R_{\text{out}})$</td>
<td>$45 [1 + (h - 10^{16}) / (10^{16})]$</td>
<td>$300 (10^{16} / h) + 5$</td>
<td>$5.5 \times 10^6 (10^{16} / h)^2$</td>
<td>0.07</td>
</tr>
<tr>
<td>Dense core</td>
<td>$R_{\text{in}} = 1.6 \times 10^{16}$</td>
<td>$7 (r / R_{\text{out}})$</td>
<td>$120$</td>
<td>$2.7 \times 10^6 (10^{16} / r)^3$</td>
<td>0.05</td>
</tr>
</tbody>
</table>

Notes. $r$ is the radial distance to the central star. $h$ is the distance to the equator. (a) and (b) are the values for the cylindrical and conical regions of the high-velocity outflow.

As mentioned, we have followed the model made by SC04 by using a similar nebular structure. We have introduced moderate variations in the geometry and velocity field and more substantial changes in the temperature and density laws, which characterize the different nebular components that allow a better fit of the observed high-$J$ CO profiles. In particular, the main differences, when compared to SC04, are found in two components: the high-velocity outflow and the dense central core. Of course, we must keep in mind that we are analyzing molecular lines that require different excitation conditions (for example, the lowest and highest rotational transitions which are separated by more than 700 K) and therefore, are tracing distinct regions of the nebula, which lead to a more accurate determination of physical parameters like the density and temperature than in SC04.

In general, the predictions from our code using this nebula structure satisfactorily reproduce the observed CO profiles as we discuss in the next section.

5. Discussion

As mentioned, we have followed the model made by SC04 by using a similar nebular structure. We have introduced moderate variations in the geometry and velocity field and more substantial changes in the temperature and density laws, which characterize the different nebular components that allow a better fit of the observed high-$J$ CO profiles. In particular, the main differences, when compared to SC04, are found in two components: the high-velocity outflow and the dense central core. Of course, we must keep in mind that we are analyzing molecular lines that require different excitation conditions (for example, the lowest and highest rotational transitions which are separated by more than 700 K) and therefore, are tracing distinct regions of the nebula, which lead to a more accurate determination of physical parameters like the density and temperature than in SC04.

We have compared our observational data with the predictions of the model summarized in Sect. 4. We have derived the best nebula model by fitting the observed CO profiles (see Table 2). Our results are shown in Fig. 1. We can see that our
predictions for the best nebula model adequately reproduce the observed spectral profiles for both molecules, $^{12}$CO and $^{13}$CO, in CRL 618. To get to this satisfactory fitting, we have used the same nebular structure and identical physical conditions of those used by SC04 as a first step. With this approach, we were able to reproduce the $J = 1\rightarrow0$ and $J = 2\rightarrow1$ lines but not the high excitation ones. To do the latter, we needed to change the physical parameters of the different components. The general properties of the halo and the double cavity are not changed significantly (see Table 1 in SC04 and our Table 2). For instance, we have introduced a small velocity gradient of the gas in the extended halo from 7 up to 16 km s$^{-1}$, which is almost the same value derived in SC04. The temperature law is similar with the halo slightly being hotter. The density distribution is similar too, although the inner regions of the halo are denser than in SC04.

On the other hand, the double empty cavity that extends along the nebula axis (named ellipses in Table 2) also shows a maximum velocity of 20 km s$^{-1}$, and temperature and density laws that are compatible to those used in SC04. The ellipses in this case are cooler and less dense. This result confirms the predictions made in Bujarrabal et al. (2010). As we can see, the small differences in these two nebular components must be included in the model to simultaneously fit the low-$J$ emissions (which mainly comes from the halo) and the emission from the ellipses which, although its contribution to the profile is not very important as shown by the observations, is seen in both the $J = 10\rightarrow9$ and $J = 6\rightarrow5$ spectra of $^{13}$CO and $^{12}$CO and in the $J = 16\rightarrow15$ $^{12}$CO line.

In contrast, the physical conditions and properties of the other two components, the bipolar outflow and the compact central component, have been revised more substantially in our model. We discuss these changes below.

1. The high-velocity bipolar outflow: a first approach to model the high CO emission was performed by Bujarrabal et al. (2010). These authors made a preliminary fitting of the $J = 16\rightarrow15$ $^{12}$CO line observed in CRL 618. The main conclusion they found was that the excitation conditions to reproduce the intensity measured in the outflow were underestimated – a result that we have confirmed in our model predictions. In particular, the velocity and density distributions do not differ much from the original model but the temperature laws have changed. In the entire outflow we have used the same temperature law (see Table 2): the temperature decreases with the distance to the star, being $\sim300$ K at a typical distance of $r = 10^{15}$ cm. This relatively high temperature is needed to reproduce the evident contribution of the outflow to the central observed features (see $J = 16\rightarrow15$, 10–9, 6–5 in Fig. 1) and the high-velocity wings seen in the different high frequency spectral profiles. Our estimation of the temperature in the outflow of CRL 618 is higher than the values typically derived in other PPNe, which are usually lower: ~ 100 K in CRL 2688 (Cox et al. 2000; Bujarrabal et al. 2012) and ~ 60 K in Frosty Leo (Castro-Carrizo et al. 2005) and IRAS 17436+5003 (Bujarrabal et al. 2012). However, these values are consistent with the derived averaged density and time, since the acceleration of the outflow gas took place (Bujarrabal et al. 2012). Using the velocity gradient and size of the outflow in Table 2, we derive a kinematic age of the outflow in CRL 618 of ~70 yr in the inner regions or close to the central star and ~30 yr in the outermost regions. The gas in the outflow of CRL 618 is then an example of the very recent acceleration and heating of the passage of shocks that is still cooling down.

We note that the observed asymmetry between the red and the blue line wings is not reproduced in our calculations. In general, the blue wing is more intense than the red one in the high-$J$ transitions, while the red wing is stronger in the low-$J$ lines, particularly for $^{13}$CO. As mentioned in Sect. 3, opacity effects in opaque lines can yield weaker blue wings, due to absorption by outer cooler layers approaching the observer. This phenomenon, which is widely observed in molecular lines, cannot explain the empirical features in our case, which must be due to actual asymmetries of the nebular properties with respect to the equator. We think that our observations reveal the presence of slightly higher temperatures in the approaching gas, which could explain the intense high-$J$ blue wings, and a higher mass in the receding gas, which would be responsible for the stronger red wing found in low-$J$ $^{13}$CO lines. However, our model cannot account for these features, since we assume symmetry with respect to the equator for simplicity, and therefore the calculations always give an average of the emission of both wings.

2. The central core: this component was proposed by SC04 to explain the compact and intense emission found in their two central channels at $V = [–18, –24$ km s$^{-1}]$. In the $J = 16\rightarrow15$, 10–9 transitions of $^{12}$CO and $^{13}$CO, it is clear from Fig. 1 that there is a central feature that is actually emitting at the velocities seen by SC04. To properly fit the low-CO emission and the high-CO, we have to introduce again small differences to the physical laws used in SC04. For instance, the fitting is improved if the velocity of this component is decreased to typical values of $\sim7$ km s$^{-1}$ while keeping its strong gradient to reproduce the triangular shape observed in the profiles. In addition, a constant temperature of 120 K and a less dense gas in the core are needed to fit the profiles satisfactorily (see Figs. 1 and 2, and Table 2).

Other assumptions in our model concern the relative abundances of $^{12}$CO and $^{13}$CO. We have used an abundance ratio, $^{13}$CO/$^{12}$CO, equal to 25. This ratio agrees with the values derived in C-rich circumstellar AGB envelopes and PPNe (see Kahane et al. 1992; Bujarrabal et al. 1994, 2001, 2010). We have also assumed that both values are constant throughout the nebula.

Using our best possible model for CRL 618, we derive a total molecular mass of $M \sim 0.4 M_\odot$. Most of the calculated mass is contained in the halo and in the bipolar outflow with values of 0.24 $M_\odot$ and 0.07 $M_\odot$, respectively. The mass of the dense core is 0.05 $M_\odot$; the ellipses are less massive with a mass of 0.04 $M_\odot$. The kinetic energy and total momentum of the nebula are $9.1 \times 10^{45}$ erg and $1.9 \times 10^{39}$ g cm s$^{-1}$. The outflow carries most of the momentum, with a value of $1.0 \times 10^{39}$ g cm s$^{-1}$. These values are compatible with the known previous estimations of the masses and linear moments by Bujarrabal et al. (2001) and SC04, when we consider the differences in the methods and/or parameters used. In the first case, the authors used a simple nebula model, a distance of 1700 pc (instead of 900 pc), and a very low rotational temperature (15 K for the outflow and 25 K in the slow component) when compared to our derived mean values (~300 K and ~100 K, respectively). In SC04, the masses of the core and outflow, and hence the momentums, are larger than our values. This difference is explained due to the coefficients of the density laws assumed in the two components. Our coefficients in the density laws are lower than those derived in SC04. There is also another difference with SC04: We have used a higher abundance of $^{12}$CO. This means that we expect lower densities throughout the nebula for similar line intensities, since there are more molecules emitting at the different frequencies. Finally, if we compare the momentum of the outflow with what can be supplied by the radiation pressure ($-3.5 \times 10^{34}$ g cm s$^{-1}$ yr$^{-1}$), this is a result that does not depend on the assumed distance, we obtain $P/(L/c) \sim 0.3 \times 10^{3}$ yr. This high value is comparable to the one given by SC04 (~10$^5$ yr),
which, as explained by the authors, confirms that radiation pressure cannot drive the observed bipolar outflows seen in CRL 618.

In general, the observed spectral profiles are well reproduced by our model. We find that the errors in the intensities derived from the fitg range between 15 and 20%, except for the $^{13}$CO $J = 16–15$ line where the error in the determination of the total flux is 50%. These scale factors are then comparable to the errors measured in the amplitude calibration of the processed data (see Table 1), except for the $^{13}$CO $J = 16–15$ where the detection is within the observing limits.

The nebular structure and velocity field are independent of the physical conditions used in the different components, since they have been determined directly from the available data. The determination of the temperature and density is usually more uncertain because it depends on the individual properties of each molecular component, where the opacity of the CO emission changes across the nebula. As mentioned previously, a proper study of those parameters also requires the observations of high excitation lines, and therefore, we have been able to derive reliable values of the temperature and density throughout the molecular envelope thanks to our Herschel observations.

6. Conclusions

We present observations of the FIR/sub-mm molecular lines of $^{12}$CO and $^{13}$CO using Herschel/HIFI in the protoplanetary nebula CRL 618. The $J = 16-10$, 10-9, and 6-5 lines of both isotopomers have been detected. We have improved the reduction and, particularly, the calibration of these observational data, which were previously reported.

We have used a nebula model that calculates the excitation of the CO transitions through the molecular components of the nebula. The model includes accurate calculations of the molecular excitation and radiative transfer in a complex structure. Our theoretical approach also allows a good determination of the temperature thanks to our modeling of the high excitation transitions. For the first time, a spatio-kinematical model has been used to fit all the observed low- and high-excitation CO lines simultaneously, and therefore, we have been able to better constrain and study relevant parameters like the density and temperature across the nebula. The main conclusions derived from this study are the following:

1. We confirm the several molecular components previously identified in CRL 618: a spherical halo, a dense core, a double empty shell, and a high-velocity outflow. The overall properties of the halo and the double shell do not differ significantly from previous studies. The halo, which is probably the remnant of the AGB circumstellar envelope, contributes to the line profiles mainly in the low-$J$ CO transitions. The double empty shell, on the other hand, extends along the nebula axis and its contribution is less important at high-$J$ emission. In contrast, the compact central core and the high-velocity bipolar outflow are the dominant components at higher excitations.

2. To obtain the best possible fit to the low-$J$ and particularly the high-$J$ CO profiles, we have found that important changes in the physical conditions in the bipolar outflow and core must be considered:

- The fast bipolar outflow, which axially expands from $\sim 45$ to $300 \text{ km s}^{-1}$ with a typical density of $5.5 \times 10^3 \text{ cm}^{-3}$, is characterized by a relatively higher temperature than previously estimated; the temperature decreases with the distance to the central star, being $\sim 300 \text{ K}$ at a typical distance of $10^{16} \text{ cm}$. This temperature is needed to explain the high-velocity wings seen in the spectral profiles, which become dominant when the energy level increases and which are spectacular in the $J = 16–15$ $^{12}$CO line. This temperature for the fast gas is also higher than what is found in PPNe. Therefore, the outflow in CRL 618 may be the result of very recent acceleration of shocked gas that has not cooled down.

- The molecular emission arising from the compact central core is clearly observed in the low- and high-$J$ transitions. The core emission is the narrow central feature seen in the high-$J$ line profiles. Therefore, its temperature is higher, and its expansion velocity is lower than estimated. In particular, the temperature has been increased to 120 K, and the radial expansion velocity has been decreased to typical values of $\sim 5 \text{ km s}^{-1}$, while keeping its strong gradient. This molecular component may then represent the ejected material from the central star during the ultimate AGB phase, at around 500 yr, where AGB stars experience a higher mass-loss rate and, at the same time, a drop in the expansion velocity.

Acknowledgements. The authors acknowledge the useful comments of the referee, which helped to improve the paper.

References