III. The interplay between galaxy evolution and the dynamical state of galaxy clusters

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1. Introduction

Galaxy ecology is an attempt to understand the environmental factors that affect galaxy formation and evolution (e.g. Balogh et al. 2004a,b; Wetzel et al. 2012). There is strong evidence for a relationship of galaxy properties and the physical conditions surrounding them (e.g. Martinez et al. 2008). At least three important pieces of information tell us that the environment affects galaxy evolution in clusters. First, the morphology-density relation shows that galaxy morphologies depend on the density (or cluster-centric radius) – the spiral fraction is larger at cluster outskirts than at the center (e.g. Dressler 1980; Whitmore et al. 1993). Furthermore, the fraction of star-forming galaxies decreases with the increasing density of the cluster environment (e.g. Balogh et al. 2004a,b; Kauffmann et al. 2004). Finally, there is a correlation between colors and environment – the fraction of red galaxies decreases toward the outer part of clusters (e.g. Balogh et al. 2000; De Propis et al. 2004). Although these relations are connected, they correspond to independent galaxy observables, and we can understand them as distinct galaxy evolution indicators. Behind them, several physical mechanisms may be present: tidal stripping, mergers, cannibalism, strangulation, ram pressure stripping, galaxy harassment, etc. (see e.g. Mo et al. 2010, for a good description of all these transformation processes).

In particular, the color-radius relation may be crucial for exploring the environmental effects on galaxies. Because the color evolution is mainly completed at low redshifts (e.g. Goto et al. 2004), it would be interesting to relate the red galaxy fraction to the dynamical state of their host clusters. To probe the color-radius relation one needs to consider an important aspect, that is, the very nature of the red galaxies, that is whether they are real passive objects with no (or little) star formation currently taking place (e.g. Strateva et al. 2001; Baldry et al. 2004). Usually, it is assumed that all red galaxies are passive, but this neglects the possible contribution of dusty galaxies to the red sequence, which can be significant in an intermediate environment and for low-to-intermediate stellar masses (e.g. Sánchez-Blázquez et al. 2009).

An additional ingredient for galaxy ecology studies is the role of low-luminosity galaxies. In the hierarchical scenario, they have formed from small peaks in the initial power spectrum (e.g. White & Rees 1978). If this is the case, they are expected to be the building blocks of the whole formation process (e.g. Evstigneeva et al. 2004). We would find them in great numbers, and they would be less clustered than bright galaxies. On the
other hand, some of them may also have formed from tidal debris from galaxy mergers or from galaxies that underwent ram pressure stripping as they fell toward the center of clusters (e.g. Conselice et al. 2002) and, therefore, some of them would be expected at cluster centers (e.g. Trentham 1998; Carrasco et al. 2006). Hence, to determine the spatial distribution and fraction of low-luminosity galaxies in clusters is important for understanding different aspects of galaxy formation and evolution models.

In this work, we present a study of the relation between colors and luminosities of cluster galaxies and the dynamical state of the clusters. Our aim is to describe the interplay between galaxy properties and galaxy cluster evolution. For this purpose, we used 10 721 member galaxies of 183 clusters extracted from the Sloan Digital Sky Survey (SDSS) from a list of NoSOCS and CIRS targets. First, we applied statistical tests to classify the clusters into two categories, Gaussian and non-Gaussian, according to their velocity distribution, which we took as an indicator of their dynamical state. This was made irrespective of the orientation of the velocity ellipsoid is correlated with the large-scale structure and the anisotropic nature of infall into clusters (e.g. White et al. 2010), we assumed that these effects do not severely influence the statistical approach used in this work.

After classifying clusters into Gaussian and non-Gaussian according to their velocity distribution, we used objective criteria to split the galaxies up according to their luminosities, colors, and photometric mean stellar age. This information was finally used to evaluate how galaxies evolve in their host clusters.

The paper is organized as follows: in Sect. 2 we describe our data; in Sect. 3 we present the methods employed to assess the dynamical state of the clusters and to separate the galaxies according to color and luminosity; in Sect. 4 we analyze our results, in Sect. 5 we discuss our findings, and in Sect. 6 we present our conclusion.

2. Data

This work is based on the supplemental version of the Northern Sky Optical Cluster Survey (NoSOCS, Lopes 2003; Lopes et al. 2004). This supplemental version of NoSOCS goes deeper (r = 21 and z ~ 0.5), but covers a smaller region (~2700 square degrees) than the main NoSOCS catalog (Gal et al. 2003, 2009). NoSOCS was created from the digitized version of the Second Palomar Observatory Sky Survey (DPOSS/POSS-II, Djorgovski et al. 2003). The photometric calibration and object classification for DPOSS are described in Gal et al. (2004) and Odewahn et al. (2004), respectively. In the first paper of this series (Lopes et al. 2009a) a subsample of 7414 systems from the NoSOCS supplemental was extracted from the Sloan Digital Sky Survey (SDSS), data release 5 (DR5).

This sample was reduced to 179 low-redshift clusters (z ≤ 0.1) with enough spectra in SDSS (at least three galaxies within 0.50 h⁻¹ Mpc) for spectroscopic redshift determination using the gap technique (Katgert et al. 1996; Lopes 2007). This technique separates groups after the identification of gaps in the redshift distribution larger than a given value. To select members and exclude interlopers, the shifting gapper technique (Fadda et al. 1996) was applied to all galaxies with spectra available within a maximum aperture of 2.50 h⁻¹ Mpc. This method works through the application of the gap technique in radial bins from the cluster center. The bin size is 0.42 h⁻¹ Mpc (0.60 Mpc for h = 0.7) or larger to force the selection of at least 15 galaxies (consistent with Fadda et al. 1996). Galaxies not associated with the main body of the cluster are eliminated. After removing the interlopers, the final sample comprises 127 clusters (out of 179) with at least ten member galaxies within 2.50 h⁻¹ Mpc.

The line-of-sight velocity dispersion (σv) for these clusters was estimated and then a virial analysis was performed. The latter is analogous to the procedure described in Girardi et al. (1998), Popesso et al. (2005, 2007a,b), and Biviano et al. (2006). First, the projected, virial radius (Rvir) is derived and a first estimate of the virial mass is obtained (using Eq. (5) of Girardi et al. 1998). The surface pressure correction is applied to the mass estimate and a Navarro et al. (1997) profile is assumed to obtain estimates of R200, M200, M500 and M1000.

This low-redshift sample was complemented with 56 more massive systems from the cluster infall regions in the SDSS (CIRS) sample (Rines & Diaferio 2006). CIRS is a collection of z ≤ 0.1 X-ray-selected clusters overlapping the SDSS DR4 footprint. In this redshift range, our NoSOCS sample therefore comprises only relatively poor systems. The same cluster parameters as listed above were determined for these 56 CIRS clusters. Hence, the combined NoSOCS plus CIRS sample comprises 183 clusters. The NoSOCS clusters have velocity dispersion estimates of 100 < σv < 700 km s⁻¹, while the CIRS systems cover the range 200 < σv < 900 km s⁻¹ (only 23% of CIRS objects have σv < 400 km s⁻¹). Because from the original CIRS member selection, velocity dispersion and mass estimates are the product of the caustic technique (Rines & Diaferio 2006), CIRS was also used for comparing these properties and for the cluster scaling relations (Lopes et al. 2009a, b). For all the objects in our final we also estimated the sample optical luminosity (Logp), the richness (Ngal), and the X-ray luminosity (Lx) (Lx is obtained with ROSAT All Sky Survey data; see Lopes et al. 2009a, b).

The centroid of each NoSOCS cluster is a luminosity, weighted estimate, which correlates well with the X-ray peak (see Lopes et al. 2006; and more details in Lopes et al. 2004). Lopes et al. (2009b), showed that the scaling relations based only on NoSOCS or CIRS objects agree, although in different mass ranges, which also indicates that the centroid (optical or X-ray) does not create a bias in the cluster parameters (richness, Logp, σv, R200, M200), at least for our sample and analysis. Previous works have also shown a good correlation between optical and X-ray centroids (Adami et al. 1998; Dai et al. 2007; Man & Ebeling 2012). Note that Man & Ebeling (2012) selected disturbed clusters in their search for objects with large offsets between the X-ray emission and the brightest cluster galaxy (BCG). Recently, centroid offsets have also been investigated using the Sunyaev-Zeldovich Effect (SZE, Sehgal et al. 2013) and gravitational lensing (Zitrin et al. 2012). Investigating the offsets between the dark matter (DM) projected center and the BCG, Zitrin et al. (2012) found that some of the offsets are caused by misidentifications of the BCG.

The redshift limit of the sample (z = 0.1) is due to incompleteness in the SDSS spectroscopic survey for higher redshifts, where galaxies fainter than M* + 1 are lacked, which biases the dynamical analysis (see the discussion in Sect. 4.3 of Lopes et al. 2009a). We considered the M* = −20.94 value from Popesso et al. (2006), converted to our cosmology¹. Our galaxy sample consists of 10 721 members from these 183 clusters at z ≤ 0.1.

To compute the absolute magnitudes of each galaxy (in ugriz bands) we considered the following formula: M1 = m1 − DM − kcorr − Qz (z is one of the five SDSS bands we considered),

¹ All quantities with cosmological dependence are computed in the concordance context, defined by Ω_m = 0.3, Ω_Λ = 0.7, and H_0 = 100 h km s⁻¹ Mpc⁻¹, with h = 0.7.
where \( DM \) is the distance modulus (considering the redshift of each galaxy), \( k_{corr} \) is the \( k \)-correction and \( Qz \) (\( Q = -1.4 \); Yee & Lopez-Cruz 1999) is a mild evolutionary correction applied to the magnitudes. The \( k \)-corrections are obtained directly from the SDSS database for every object in each band. Rest-frame colors are also derived for all objects. More details regarding the sample (value of \( M^* \), centroid determination, member selection, virial analysis, \( \sigma_L \), \( L_{opt} \), and \( N_{gals} \) estimates) can be found in Lopes et al. (2009a,b).

3. Methods

3.1. Gaussian and non-Gaussian composite clusters

Our aim is to find a connection between galaxy evolution and the dynamical state of clusters. We started by defining two classes for the galaxy environments according to their velocity distributions: Gaussian velocity distribution and non-Gaussian velocity distribution clusters. Hereafter we refer to them as Gaussian and non-Gaussian clusters for simplicity, which represent the relaxed and less or unrelaxed samples. Although the theoretical line-of-sight velocity distribution expected for galaxy clusters is not exactly Gaussian (e.g. Merrit 1987), phenomenological evidence has suggested for a long time that normality can be assumed for clusters in dynamical equilibrium (e.g. Yahil & Vidal 1977). Hence, distinguishing galaxy clusters according to their velocity distributions may be an objective way to assess their dynamics through the simple use of statistical tests (see e.g. Hou et al. 2009; Ribeiro et al. 2010, 2011).

Differently from our previous works that were only based on the Anderson-Darling (AD) test (usually appropriate for small samples – see Hou et al. 2009), we now used three more normality tests: the Kolmogorov-Smirnov, the Shapiro-Wilk, and the Robust Jarque-Bera test (see Thode 2002, for a comprehensive review on normality tests). We also used the dip test to probe the modality of the velocity distributions: recent works have indicated that multimodal velocity distributions may be very common in galaxy clusters. They probably even correspond to the main cause of non-normality in the velocity distribution in clusters (e.g. Ribeiro et al. 2011; Hou et al. 2012; Einasto et al. 2012a,b; Krause et al. 2013). Therefore, the dip method helps us to better estimate which the intrinsically Gaussian velocity distributed clusters are and which are not. The dip method is based on the cumulative distribution of the variable of interest (Hartigan & Hartigan 1985). The dip statistic is the maximum distance between the cumulative input distribution and the best-fitting unimodal distribution. In some sense, this test is similar to the Kolmogorov-Smirnov test, but the dip test specifically searches for a flat step in the cumulative distribution function, which corresponds to a “dip” in the histogram representation. The dip test has the benefit of being insensitive to the assumption of Gaussianity and is therefore a true test of modality (e.g. Pinkney et al 1996; Muratov & Gnedin 2010).

We defined a non-Gaussian cluster when the dip test rejected unimodality and at least one of the remaining tests rejected normality, taking member galaxies out to 2 \( R_{200} \). For ten clusters with fewer than eight members within this limit, we obtained no reliable results. These clusters were removed from the sample. For the remaining clusters, we found 146 Gaussian (84%) and 27 non-Gaussian (16%) clusters with a total of 9113 galaxies. This proportion is approximately consistent with that found by Ribeiro et al. (2010).

We then built two stacked clusters, Gaussian and non-Gaussian, containing 6478 and 2635 galaxies, respectively. The distances of the galaxies in these composite groups are normalized to the distances to the group centers by \( R_{200} \) and their velocities refer to the cluster median velocities and are scaled by the cluster velocity dispersions

\[
u_i = \frac{v_i - \langle v \rangle_i}{\sigma_f},
\]

where \( i \) and \( j \) are the galaxy and the cluster indices, respectively. The velocity dispersions of the composite clusters, \( \sigma_f \), refer to the dimensionless quantity \( u_i \) (see Ribeiro et al. 2010, 2011).

The virial properties of non-Gaussian clusters were corrected after an iteratively removing galaxies without which the clusters are Gaussian. On average, 15% of the galaxies in non-Gaussian clusters need to be removed in this process. The corrected properties are just those the cluster would have if it consisted only of galaxies consistent with the normal velocity distribution (see Perea et al. 1990; Ribeiro et al. 2011). This correction allows one to approximately compare virial properties of Gaussian and non-Gaussian clusters. After computing the corrected virial properties, we returned the removed galaxies to non-Gaussian clusters for the subsequent photometric analysis of the work.

3.2. Color and luminosity classification

After setting the composite systems, we classified galaxies into blue or red objects. Since the distribution of galaxies in the \( g - r \) versus \( u - g \) color-color diagram is strongly bimodal, we simply classified galaxies above and below the separator developed by Strateva et al. (2001) as red and blue, respectively. Strateva et al. (2001) found that the blue galaxies are dominated by late types (spirals), while the red galaxies are dominated by early types (ellipticals), and that the \( u - r > 2.22 \) color-selection criterion for early types results in a completeness of 98%.

We also classified galaxies according to their luminosities. For this we fitted the absolute magnitude distribution in the \( z \)-band (\( M_z \)) as a Gaussian mixture with \( n \) components. We used the \( z \)-band absolute magnitude as the closest approximation to the galaxy mass among the five SDSS color bands. It is estimated that the variation in the stellar mass-to-light ratio is only a factor of \( \sim 3 \) for galaxies in different ranges of the \( z \)-band absolute magnitude (Kauffmann et al. 2003). In Fig. 1, we see the \( M_z \) histograms and the Gaussian mixture, fitted after using a Bayesian regularization for normal mixture estimation to find the mixture parameters (Fraley & Raftery 2007). The best fit is found for a mixture of three normal distributions. In Fig. 1, we used red vertical lines to mark the intervals for these populations, corresponding to the first quantile of the brightest component and the third quantile of the faintest component. This choice was made to avoid overlaps of the low- and high-luminosity ends with the central and dominant luminosity population.

We considered a loose definition for each luminosity class, calling objects with \( M_z < -22.59 \) the bright population (corresponding to 15% of all galaxies), those with \( M_z > -19.03 \) as the faint population (7% of all galaxies), and objects with intermediate values of \( M_z \) correspond to the intermediate-brightness population of galaxies (78% of all galaxies). Finally, we find that 78% of the bright, 72% of the intermediate-brightness, and 56% of the faint galaxies are in the stacked Gaussian cluster.

4. Analysis

4.1. The red galaxy fraction

To study the connection between galaxy evolution and the dynamical state of clusters, we looked for differences in the galaxy
subsamples according to the cluster dynamical classification, i.e., a Gaussian or non-Gaussian cluster. First, we used the red galaxy fraction (RGF) as an indicator of galaxy evolution in the stacked clusters. We found that red galaxies correspond to 74% of all galaxies. In the stacked Gaussian cluster red galaxies correspond to 76% of the total, while we found a somewhat lower fraction of red galaxies in the stacked non-Gaussian cluster, 70%.

The mean RGF for a sample of field galaxies was estimated for each luminosity population and used for comparison. The field sample, containing 68 375 objects, was constructed as follows. From the whole SDSS DR7 data set, we selected galaxies that are not associated to a group or cluster, considering the cluster catalog from Gal et al. (2009). To be conservative, we defined a galaxy to belong to the field if it is not found within 4.0 Mpc and does not have a redshift offset smaller than 0.06 of any cluster from Gal et al. (2009). Although this definition may include void galaxies in the sample, this should not be a major problem, given that several studies have shown that color bimodality is remarkably similar between void and field galaxies (e.g. Patiri et al. 2006; Hoyle et al. 2012). Finally, we divided the galaxies into the luminosity populations defined in Sect. 3.2, finding 4%, 92%, and 4% of field galaxies in the bright, intermediate and faint populations, respectively.

In Fig. 2, we observe the emergence of the color-radius relation in all cases. The RGF decreases from the center toward the outskirts, with a slight recovering and/or stabilization to the outer radii, when the behavior is approaching the field. In each case we found a significant relationship between the RGF and the clustercentric distance, with a Pearson correlation coefficient ≥0.70 at the 95% confidence level. This result is expected for Gaussian clusters, which are supposed to be virialized. But we found the same behavior for non-Gaussian clusters. This indicates that the color-radius (density) relation is already set for non-Gaussian clusters, suggesting that a strong galaxy evolution happens before the dynamical equilibrium is reached. Since non-Gaussian clusters (as defined in this work) should be multi-modal, our findings suggest that galaxies may have been pre-processed in the individual modes that constitute the clusters (i.e., the subunits we found in their velocity distribution – see Ribeiro et al. 2011), a scenario consistent with that of Zabludoff & Mulchaey (1998), where galaxies were pre-processed in group environments before accretion into large clusters.

We also note in Fig. 2 important differences with respect to the point at which the RGF crosses the line that depicts the mean fraction of red galaxies in the field. Our stacked analysis shows that larger portions of fainter red galaxies are found, on average, in smaller radii. This result is probably related to the fact that the fraction of red galaxies heavily depends on their own stellar mass (e.g. Baldry et al. 2006; Haines et al. 2006). The most massive galaxies have resided within group-sized halos for a longer time (e.g. MacGee et al. 2008), which could lead to a less steep trend for the RGF.

4.2. The stellar population properties

To investigate the stellar population properties of galaxies in Gaussian/non-Gaussian groups, we used the stellar population synthesis code STARLIGHT (Cid Fernandes et al. 2005; Asari et al. 2007). This code fits the observed spectrum with a linear combination of a number of template spectra with known properties. We built a template sample with single stellar population spectra from Bruzual & Charlot (2003) models, using a Chabrier (2003) IMF and the Padova 1994 stellar evolution tracks. Our template sample is composed of 45 spectra with three different metallicities (Z = 0.004, Z = 0.02, or Z = 0.05) and 15 ages ranging from 1 Myr to 13 Gyr. Prior to the fits, we shifted the SDSS galaxy spectra to the restframe and linearly resampled them to 1 Å (the spectra are expressed with fixed resolution in logarithmic, not linear, scale). Our results are expressed in terms of two parameters proposed by Cid Fernandes et al. (2005). The
first is the photometric mean stellar age,
\[
\langle \log t \rangle = \sum_j x_j \log t_j,
\]
(2)
where \(x_j\) is the fractional contribution to the galaxy total flux of the template \(j\), and \(t_j\) is the age of that component (irrespective of its metallicity). The second is a measure of the photometric age dispersion,
\[
\sigma(\log t) = \sqrt{\sum_j x_j (\log t_j - \langle \log t \rangle)^2},
\]
(3)
which is higher for galaxies with extended star formation history and zero for a single burst of age \(t\). Notice that due to the small SDSS fibre size (3 arcsec) the spectra measure the central region of each galaxy, so that the inferred stellar population distribution is not representative of the whole galaxy. However, even if a synthesis result cannot be translated into a direct meaning because of this light sampling bias, we can nevertheless identify average differences of the galaxies in the full sample.

The distribution of the photometric mean stellar age corresponds to a mixture of three components, identified after using the Bayesian regularization for normal mixture estimation (the same procedure we used in Sect. 3.2 to study the luminosity distribution; see Fraley & Raftery 2007). The components present the following mean parameters: \(\log t = 9.90 \pm 0.13\) (for the old component), \(\log t = 8.27 \pm 0.27\) (for the young component) and \(\log t = 9.32 \pm 0.75\) (for what we call here the transition component). Some properties of these components are presented in Table 1. The columns are: (1) the number \(N\) of galaxies; (2) the mean absolute magnitude in the \(z\) band; (3) the mean age in Gyr; (4) the mean \(u - r\) color. These properties indicate that the old component is redder, more luminous and has the lowest photometric age dispersion, on average, showing that this component hosts a more homogeneous stellar population.

Galaxies in the color-age diagram have a clear bimodal distribution in this plane – see Fig. 3 –, as expected for a mixture of blue and red galaxies. The horizontal green dashed line depicts the color separator developed by Strateva et al. (2001), the vertical green dashed line depicts the mean age of the transition component. We used these lines to roughly classify galaxies into passive \((u - r > 2.22\) and \(\log t > 9.32\)) and star-forming objects \((u - r \leq 2.22\) and \(\log t \leq 9.32\)). The blue and red 1-\(\sigma\) ellipses encompass the peaks identified in the color-age space with the MCLUST code, a contributed R package for multivariate normal mixture modeling and model-based clustering\(^2\). It provides functions for parameter estimation via the expectation-maximization (EM) algorithm for normal mixture models with a variety of covariance structures (Fraley & Raftery 2007). The ellipses indicate the central regions of star-forming (blue) and passive (red) galaxies. We found that passive galaxies correspond to 84\% of all red objects (5877 out of 7020). The remaining red galaxies are probably composed of dusty, star-forming galaxies (e.g. Popesso et al. 2007a,b), and were classified in the transition component. Finally, star-forming objects correspond to 93\% of all blue objects (2231 out of 2409).

4.3. Galaxy evolution in the stacked clusters

We now study some properties of the stellar and luminosity populations in the stacked clusters.

4.3.1. \(M_z \times r/r_{200}\)

Figure 4 shows the normalized clustercentric distance of galaxies as a function of their \(z\)-band absolute magnitude. Passive galaxies in Gaussian clusters always have smaller clustercentric distances than star-forming galaxies in both Gaussian and non-Gaussian clusters. For galaxies in the range \(-22.5 < M_z < -20.5\), passive galaxies in Gaussian and non-Gaussian clusters have the same behavior, while galaxies brighter than \(M_z \approx -22.5\) and fainter than \(M_z \approx -20.5\) are more centrally located in Gaussian than in non-Gaussian clusters. The clustercentric distance of passive galaxies brighter than \(M_z \approx -22.5\) is smaller toward brighter magnitudes in Gaussian clusters.

Gaussian clusters seem to have a clear structure: passive galaxies in the virialized region \((r < r_{200})\), and star-forming galaxies inhabiting the outer region \((r \geq r_{200})\). The absence of star-forming galaxies in the center indicates that the environment was able to transform nearly all galaxies into red objects in the innermost regions. In fact, we see in Fig. 4 that the clustercentric distance of star-forming galaxies brighter than \(M_z \approx -19.5\) is systematically smaller toward fainter magnitudes in Gaussian clusters, suggesting that dynamical processes may be providing

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\(^2\) R is a language and environment for statistical computing and graphics. It is a GNU project that is similar to the S language and environment and was developed at Bell Laboratories – R Development Core Team (2011).
both reddening and mass loss as these objects fall into the potential well of the cluster.

The more central distribution of bright and faint passive galaxies in Gaussian clusters can be interpreted as an indicator of dynamical evolution. Luminosity segregation describes the tendency for more luminous/massive galaxies to be located near the cluster center (e.g. Rood et al. 1972; Dressler 1978). This effect is expected from the dynamics of galaxies aggregating in the potential wells of clusters (e.g. Fusco-Femiano & Menci 1998), and thus clusters with luminosity segregation are considered to be more highly evolved than those without this feature. We also see in Fig. 4 that faint passive galaxies show segregation with magnitude and position. If a fraction of these faint galaxies correspond to the result of galaxy-galaxy encounters in the cluster (e.g. Conselice 2002), the presence of faint galaxies in the innermost regions of clusters could be taken as an additional indicator of dynamical evolution.

Finally, we note that the spatial distribution of galaxies in non-Gaussian clusters has some similarity to their counterparts in Gaussian ones, but with certain important differences between them: (i) non-Gaussian clusters do not present luminosity segregation – their brightest galaxies are peripheral; (ii) star-forming galaxies in non-Gaussian clusters show no significant trend with the clustercentric distance; (iii) there are fewer faint galaxies close to the cluster center. These results may be indicating that, regarding the galaxy population, non-Gaussian clusters are less evolved environments than Gaussian clusters.

4.3.2. $M_z \times \sigma_u$

The correlation between the velocity dispersion and the absolute magnitude in the $z$-band of the galaxies is shown in Fig. 5. We call velocity dispersion the dispersion of the galaxy velocities in each bin of absolute magnitude. We confirmed the segregation between passive and star-forming galaxies both in the Gaussian and non-Gaussian stacked clusters: the brightest objects ($M_z < -22.5$) show a lower velocity dispersion, which indicates that they had time to decrease their velocity through dynamical interactions or friction. We also see that passive galaxies in Gaussian clusters have a lower velocity dispersion over the entire luminosity range. This result agrees well with some studies reporting that late-type galaxies have a higher velocity dispersion than early types in nearby clusters (e.g. Moss & Dickens 1977; Sodré et al. 1989; Adami et al. 1998, 2000). This is not true for non-Gaussian clusters, where passive and star-forming galaxies have approximately the same velocity dispersion in the range $-22.5 < M_z < -18.5$. We also note that the brightest star-forming galaxies in Gaussian clusters have a high velocity dispersion and large clustercentric distance, which suggests that these galaxies are falling into the clusters, possibly through radial orbits (e.g. Biviano & Katgert 2004).

From Figs. 4 and 5, we see that bright passive galaxies in Gaussian clusters combine low-velocity dispersion with small clustercentric distance. This kind of segregation with magnitude in velocity and position has been observed in many clusters (e.g. Carlberg et al. 1997; Biviano & Katgert 2004). It can be understood with the model of Menci & Fusco-Femiano (1996), which is a solution of the collisional Boltzmann-Liouville equation, and hence accounts for galaxy collisions and merging processes in the cluster center. However, we also see in Figs. 4 and 5 that the brightest passive galaxies in non-Gaussian clusters combine low velocity dispersion with large clustercentric distance, indicating that these systems are less segregated than Gaussian clusters. Indeed, it has been found that clusters present a gradation of luminosity segregation, from highly segregated to virtually not segregated, and that their different degrees could be a consequence of either the different initial conditions present at the onset of the two-body relaxation phase or the different cluster dynamical stages (e.g. Yepes et al. 1991; Ribeiro et al. 2010). We must also consider that observational evidence for luminosity segregation in distance may be weakened by sub-clustering (Biviano et al. 1992). According to our definition in

**Fig. 4.** Normalized clustercentric distance of galaxies as a function of their $z$-band absolute magnitude. Red circles and magenta diamonds represent passive galaxies in Gaussian and non-Gaussian clusters, respectively. Blue squares and cyan stars represent star-forming galaxies in Gaussian and non-Gaussian clusters, respectively. The vertical dashed lines indicate the separation into luminosity populations.

**Fig. 5.** Velocity dispersions of galaxies as a function of their $z$-band absolute magnitude. Red circles and magenta diamonds represent passive galaxies in Gaussian and non-Gaussian clusters, respectively. Blue squares and cyan stars represent star-forming galaxies in Gaussian and non-Gaussian clusters. The vertical dashed lines indicate the separation into luminosity populations.
Sect. 3.1, non-Gaussian clusters must be multi-modal, which means that the centers of these systems are ill-defined and that galaxy properties may refer more to the individual modes than to the entire cluster. In Fig. 4, we see that both the brightest and the faintest passive galaxies in non-Gaussian clusters are more peripheral than their counterparts in Gaussian clusters. We verified that the ratio of the clustercenteric distance of passive galaxies with respect to the mode center and to the cluster center of non-Gaussian clusters are ∼-0.41, ∼-0.94, and ∼-0.65 for the bright, intermediate, and faint populations, respectively. Thus, in the individual modes, bright passive galaxies are the most centrally located, just like in Gaussian clusters, and segregation in distance is recovered.

These findings agree with the idea of non-Gaussian clusters as a set of subclusters that individually show a degree of dynamical evolution, regarding the galaxy population. At the same time, Gaussian clusters appear to be more evolved systems with strong evidence of segregation, and containing many faint galaxies in the central regions of the clusters. If there is a sufficient number of these faint galaxies, they may steepen the faint end of the luminosity function of galaxies in clusters, as we show below.

4.4. Luminosity function

The results achieved hitherto suggest some important differences between Gaussian and non-Gaussian clusters. We can investigate this point in more detail through the luminosity function of galaxies in our cluster samples. We built the stacked central luminosity functions (LFs), inside a radius of 0.5 \( R_{200} \) from the center, using the Colless (1989) cumulation method. This method consists of a summation of the number counts (corrected for the background contribution) in all magnitude bins of the individual LFs, normalized by the total number of galaxies within the magnitude completeness limit of each cluster (\( M_\text{r} = -19 \) for the NoSOCS sample). All photometric sources classified as galaxies that are located at a maximum projected distance of 10 Mpc to the center of each cluster were retrieved from the SDSS DR7 database. The absolute magnitude \( M_\text{r} \) of each galaxy was obtained by \( M_\text{r} = m_\text{r} - 5 \log D/10 - K \), where \( K \) is the \( K \)-correction and \( D \) is the luminosity distance of the galaxy (in pc). All galaxies in the direction of a given cluster were assigned the same value of \( D \), determined from the cluster redshift; this is certainly not true for the background galaxies, but our results are insensitive to this because the background contribution can be accessed independently from the individual choice of \( D \). The same \( K \)-correction was applied to all galaxies in a given cluster, corresponding to the \( K \)-correction of an elliptical galaxy at the cluster redshift. De Filippis et al. (2011) have also applied this methodology for the NoSOCS sample, and showed that the results are not much different when the individual \( K \)-corrections are determined for all galaxies in the photometric sample. \( K \)-corrections were calculated as in Chilingarian et al. (2010), using the \((g - r)\) colors of elliptical galaxies of Fukugita et al. (1995). The background contribution in the individual LFs was obtained in an area with \( 10 \times 10 \) Mpc and outside a radius of \( 2.0 R_{200} \), where the contribution of cluster galaxies is expected to be very low. Local overdensities were excluded from the background estimation area whenever the local number counts exceeded \( 3\sigma \) from the mean background, calculated in square cells 150 kpc wide. We then rescaled the background number count in each magnitude bin to the area of the central circular region and subtracted it from the number counts in this region.

The resulting LFs for the Gaussian and non-Gaussian composite clusters are shown in Fig. 6. This figure also shows the best-fit Schechter functions (artificially displaced for clarity) obtained by minimization of square residuals. For the non-Gaussian composite cluster, the fit resulted in \( M_\text{r} = -21.31 \pm 0.16 \) and \( \alpha = -0.97 \pm 0.06 \). For the Gaussian composite cluster, a brighter characteristic magnitude \( M_\text{r} = -21.90 \pm 0.14 \) and a steeper faint-end with \( \alpha = -1.14 \pm 0.03 \) were obtained. This result is consistent with the work of Martínez & Zandivarez (2011), and shows that at least a fraction of low-luminosity galaxies is correlated with the environment.

5. Discussion

Our analysis gives some hints for understanding the interplay between galaxy evolution and the dynamical state of galaxy clusters. We verified that Gaussian clusters present at least two important properties expected for dynamically evolved environments: (i) the color-radius relation; and (ii) the luminosity segregation in velocity and position. We have to jointly consider these results to understand what they imply about the interplay between galaxy evolution and the dynamical state of galaxy clusters. First, it is important to note that property (i) was also found in non-Gaussian clusters, reinforcing the idea of a shorter timescale for color evolution than that of the dynamical evolution of the clusters. Goto et al. (2004) showed that color evolution is almost completed by \( z \sim 0.2 \) for a sample of galaxies in SDSS clusters, while Zabludoff & Mulchaey (1998) suggested that galaxies are pre-processed in group environments before accretion into larger clusters. Thus, the color-radius relation is expected for low redshifts, regardless of the dynamical state of the clusters, and hence it cannot be taken as an indicator of galaxy cluster evolution. On the other hand, there is an important difference between Gaussian and non-Gaussian clusters with respect to the property (ii). While segregation in velocity is well defined for passive galaxies in both stacked clusters, segregation in position is less well-defined in non-Gaussian clusters due to the large clustercentric distance of their brightest passive galaxies, a possible consequence of the multimodal nature of non-Gaussian clusters. Hence, considering properties (i) and (ii), our results

![Fig. 6. Cumulative LFs of Gaussian (filled circles) and non-Gaussian (open circles) systems. The best-fit Schechter parameters are also shown.](image-url)
indicate that non-Gaussian clusters are less segregated, because of subclustering, but with color evolution at an advanced stage in the individual modes composing them. At the same time, we found more faint galaxies in Gaussian clusters than in non-Gaussian clusters. Faint galaxies in nearby clusters present a variety in their properties, with significant differences in their spatial and kinematic distributions (e.g. Lisker et al. 2006; Toloba et al. 2009; Paudel et al. 2010). In particular, early-type dwarf galaxies play an important role in understanding galaxy cluster evolution. Since these galaxies have low mass and density, they are more susceptible to interactions with larger galaxies in the cluster environment (e.g. Lisker et al. 2006). Possibly, the number of these galaxies results from the mixture of survival and destruction mechanisms in the cluster environment. Part of them could have a primordial origin and start to be destroyed by tidal stripping as they fall into the clusters. They could also correspond to remnants of galaxy-galaxy encounters (e.g. Dabringhausen & Kroupa 2013). Alternatively, they could correspond to primordial dwarf galaxies that were transported by galaxy groups from the outside to the inside of clusters (e.g. Sánchez-Janssen et al. 2008). This latter possibility favors the idea of non-Gaussian clusters as a crucial step in the evolutionary process of galaxy clusters. They could be made of interacting groups, each one transporting primordial faint galaxies to the center of future more regular clusters. This possibility is consistent with the assumption that the tidal-stripping efficiency is proportional to the ratio of the cluster mass (M) to the galaxy mass (m) (e.g. Kimm et al. 2009). If non-Gaussian clusters correspond to assemblies of galaxy groups with smaller masses, then we have lower M/m values and thus we should expect less tidal stripping in their environments. That is, faint galaxies are expected to survive much longer in the modes of non-Gaussian clusters. At the same time, if part of the faint passive galaxies was already present in non-Gaussian clusters, this means that at least a fraction of these galaxies in Gaussian clusters are formed in the cluster environment — remember that Gaussian clusters present an excess of faint galaxies. Indeed, Fig. 4 shows that faint passive galaxies in Gaussian clusters are more central than their counterparts in non-Gaussian clusters. The mean clustercentric distances are \( r/\langle r_{200}\rangle \approx 0.62 \pm 0.34 \) and \( r/\langle r_{200}\rangle \approx 0.91 \pm 0.23 \). The Kolmogorov–Smirnov test indicates a significant difference between them at the 95% confidence level. This difference in the spatial distribution of these galaxies may be pointing to differences concerning their origin. While slow-motion conditions are more common in low-mass groups, slow galaxy-galaxy interactions and mergers are likely to be rare in virialized clusters (e.g. Ostriker 1980). Galaxies moving at high speeds and in random directions in the center of massive galaxy clusters promote multiple rapid encounters between galaxies, known as galaxy harassment, a possible mechanism underlying the production of faint passive galaxies in Gaussian clusters. Aguerri & González-García (2009) showed that fast galaxy-galaxy interactions are efficient mechanisms to transform late-type galaxies into dwarf galaxies. Thus, the presence of faint galaxies in the central region of Gaussian clusters (and their lower incidence in non-Gaussian clusters) can be taken as a possible indicator of the dynamical state of a galaxy cluster.

A more detailed study of the different types of faint galaxies in Gaussian and non-Gaussian clusters is beyond the scope of the present work. We will investigate this point in a future contribution based on a larger sample.

6. Conclusion

Understanding the process of galaxy cluster formation and evolution is an important step toward refining the details of the structure growth and constraining the evolution of galaxy populations in different environments. The analysis presented in this work is an attempt to link galaxy evolution with the dynamical state of clusters. Our findings suggest a scenario where non-Gaussian clusters represent a previous stage in the life of a galaxy cluster during which two or more galaxy groups merge to eventually form Gaussian clusters. Non-Gaussian clusters are less segregated because of subclustering, but with color evolution already at an advanced stage in the individual modes they are composed of. The modes may also be carrying faint primordial galaxies into the central regions of larger clusters, while the formation of faint galaxies through dynamical interactions probably takes place on a longer timescale, probably achieving the Gaussian phase.

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