Photospheric activity, rotation, and magnetic interaction in LHS 6343 A

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ABSTRACT

Context. The Kepler mission has recently discovered a brown dwarf companion transiting one member of the M4V+M5V visual binary system LHS 6343 AB with an orbital period of 12.71 days.

Aims. The particular interest of this transiting system lies in the synchronicity between the transits of the brown dwarf C component and the main modulation observed in the light curve, which is assumed to be caused by rotating starspots on the A component. We model the activity of this star by deriving maps of the active regions that allow us to study stellar rotation and the possible interaction with the brown dwarf companion.

Methods. An average transit profile was derived, and the photometric perturbations due to spots occulted during transits are removed to derive more precise transit parameters. We applied a maximum entropy spot model to fit the out-of-transit optical modulation as observed by Kepler during an uninterrupted interval of ~500 days. It assumes that stellar active regions consist of cool spots and bright faculae whose visibility is modulated by stellar rotation.

Results. Thanks to the extended photometric time series, we refine the determination of the transit parameters and find evidence of spots that are occulted by the brown dwarf during its transits. The modelling of the out-of-transit light curve of LHS 6343 A reveals several starspots rotating with a slightly longer period than the orbital period of the brown dwarf, i.e., 13.13 ± 0.02 days. No signature attributable to differential rotation is observed. We find evidence of a persistent active longitude on the M dwarf preceding the sub-companion point by ~100° and lasting for at least ~500 days. This can be relevant for understanding how magnetic interaction works in low-mass binary and star-planet systems.

Key words. stars: magnetic field – stars: late-type – stars: activity – stars: rotation – binaries: eclipsing – brown dwarfs

1. Introduction

Kepler is a photometric space mission devoted to searching for planets by the method of transits and asteroseismology. The recently released public data contain a large amount of information useful for characterizing stellar pulsations and modulations caused by starspots in solar-like and low-mass stars.

M-type stars are particularly interesting targets in exoplanet searches since Earth-like planets in their habitable zones are expected to lie within the detection capabilities of some of the currently working instruments. However, the effects of magnetic activity in these stars may sometimes mask or even mimic the signal of a transiting exoplanet (e.g., Bonomo & Lanza 2008; Barnes et al. 2011). High-precision photometry from space offers the opportunity to study the signature of spots and faculae during large uninterrupted intervals of time, so it represents the best way to improve our knowledge of activity patterns in low-mass stars in order to further optimize exoplanet searches.

Among the M-type stars observed by Kepler, a particularly interesting object is LHS 6343 AB, a visual binary system consisting of an M4V and an M5V star at a projected distance of ~40.2 AU. Johnson et al. (2011) report the discovery of a brown dwarf companion (LHS 6343 C) with a mass of 62.7 ± 2.4 M⊕ transiting component A of the system every 12.7138 days. The primary star, LHS 6343 A, shows almost no evidence of chromospheric activity and presents a modulation of very low amplitude in the Kepler optical light curve (see Sects. 2 and 3.1). The modulation remains stable for more than 500 days and has a period of 12.71 ± 0.28 days, which is synchronized with the orbital motion of the companion. The large separation between the A and C components makes tidal interaction particularly weak in this system. Some other known synchronous systems are CoRoT-3 (Deleuil et al. 2008; Triaud et al. 2009), CoRoT-4 (Lanza et al. 2009b), and τ Bootis (Catala et al. 2007; Walker et al. 2008; Donati et al. 2008), although in the last two cases the star is orbited by a massive planet, not by a brown dwarf (BD). Since they are F-type dwarf stars, it has been suggested that the close-in brown dwarf or the planets may have synchronized their thin outer convective envelopes during the main-sequence lifetimes of the systems (Donati et al. 2008).

In this work we study the photospheric activity of LHS 6343 A by applying the spot modelling approach already used for other objects, such as CoRoT-4 (Lanza et al. 2009b) or CoRoT-6 (Lanza et al. 2011). This allows us to map the
longitudinal distribution and evolution of spots in a reference frame co-rotating with the companion orbital period. As we discuss in Sect. 4.2, we find an overall migration of the spot pattern, indicating a rotation period of $13.137 \pm 0.011$ days for LHS 6343 A, and a persistently active longitude, locked at a phase difference of $\sim 100^\circ$ from the sub-companion point. Starspots are systematically enhanced when they approach and cross that longitude during their migration. This leads us to discuss possible magnetic interactions between LHS 6343 A and its brown dwarf companion (cf. Sect. 5).

2. Observations

About 156 000 targets are being continuously monitored by the Kepler space telescope in a $10^\circ \times 10^\circ$ field near the constellations of Lyra and Cygnus (Koch et al. 2010; Borucki et al. 2010). Photometry is continuously acquired for time intervals up to $\sim 90$ days, called “quarters” in Kepler jargon, after which a re-orientation of the spacecraft is required to keep the solar arrays pointed toward the Sun. This maneuver implies a rotation of the field of view on the focal plane making the image of a given star to fall on a different CCD. As a consequence, a jump appears in the raw time series at the end of each quarter. Kepler acquires photometry with a so-called long-term cadence of $\sim 30$ min, except for a subset of selected targets for which the exposure is reduced to about one minute. Long-cadence data have been made publicly available as part of the first quarters data release (Q0–Q6) and their reduction is described in Jenkins et al. (2010a,b).

LHS 6343 (KIC 010002261) has been observed by Kepler during all the first six quarters. The time series contains a total of 22 976 data points with $\sim 30$ min cadence and a mean relative precision of $7 \times 10^{-5}$, ranging from May 2009 to September 2010. Both A and B components of the system, separated by $0^\prime.55$ (Johnson et al. 2011), are contained inside the Kepler photometric mask used to measure the flux from the target. Its aperture is optimized by the Kepler pipeline for each individual target. Note that since the image scale is $3^\prime.98$ per pixel it is not possible to measure separately the fluxes coming from the A and B components even redefining the photometric mask.

Cotrending basis vectors were applied to the raw data using PyKE pipeline reduction software$^1$ to correct systematic trends, which are mainly related to the pointing jitter of the satellite, detector instabilities and environment variations (Murphy 2012). These are optimized tasks to reduce Kepler Simple Aperture Photometry (SAP) data$^2$ as they account for the position of the specific target on the detector plane to correct for systematics. From two to four vectors were used for each quarter to remove the main trends from the raw data (see Fig. 1). A low-order ($\leq 4$)

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$^1$ http://kepler.go.arc.nasa.gov/PyKE.shtml

$^2$ The SAP light curve is a pixel summation time-series of all calibrated flux falling within the optimal aperture.
polyharmonic filtering was then applied to the resulting data for each quarter because some residual trends still remained followed by discontinuities between quarters. These are due to the change of the target position on the focal plane following each re-orientation of the spacecraft at the end of each quarter. Raw SAP data and detrended light curves are shown in Fig. 1. As a consequence of this data reduction process, the general trends disappeared, as well as jumps of the photometry between quarters. On the other hand, any possible intrinsic long-term variability of the object (≥50 days) has also been removed. The use of low-order polynomials to detrend each quarter series of data ensures that the frequency and amplitude of any variability with a timescale comparable with the companion orbital period is preserved. The presence of a number of gaps in the data prevents us from using other detrending methods such as Fourier filtering.

The out-of-transit light curve was cleaned by applying a moving box-car median 3σ-clipping filter to identify and remove outliers. Then it was rebinned with a regular 120 min sampling to reduce the computation load for the spot modelling. This is allowed because variations related to spot activity have timescales of the order of one day or longer. The average standard error of the binned observations is \( \sim 5.0 \times 10^{-3} \) in relative flux units. Transits were removed assuming the ephemeris of Johnson et al. (2011). The resulting light curve consists of 5716 data points ranging from BJD 2 454 953.569 to BJD 2 455 462.163, i.e., with a duration of 508,593 days.

Studying the photometric variability of LHS 6343, we note that the light curve exhibits a periodic modulation with a low amplitude (\( \sim 10^{-3} \) in relative flux units, resulting in a signal-to-noise ratio around 15−20) that remains stable throughout all the time series. The minima of the modulation are separated by a nearly constant phase interval from the transits of the BD companion, as can be seen in the lower panel of Fig. 1, which also shows the long-term coherence of the modulation. This suggests that component A is responsible for the observed variability. A first analysis of the out-of-transit light curve was performed through a Lomb-Scargle periodogram, finding only one significant period of 12.71 ± 0.28 days, thus confirming the synchronicity with the LHS 6343 C orbital period (see Fig. 2). The other peaks seen in the periodogram correspond to the harmonics of the main periodicity and have heights similar to that of the main peak because the signal is quasi-periodic, but not exactly sinusoidal in shape. A sinusoidal fit to the light curve with the above period was performed to estimate the phase lag, showing that the light minima precede the mid-transits by 98° in phase. The phased light curve obtained with all the Q0–Q6 data is presented in Fig. 3 with overplotted a sinusoidal best fit, showing the difference in phase between the minima of the photometric modulation and the transits.

For further analysis and spot modelling, we assume that all the observed variability is caused by LHS 6343 A. This is also supported by the fact that the system is estimated to be older than 1−2 Gyr from the very low observed chromospheric activity, and most likely near 5 Gyr from brown dwarf mass and radius relations (Johnson et al. 2011; Baraffe et al. 1998). Therefore, the rotation period of the isolated component LHS 6343 B is expected to be longer than that of the observed modulation (Barnes 2003, 2007).

Since both A and B components of the system fall within the Kepler photometric aperture, it is necessary to correct for the flux contribution from star B before performing any modelling on the light curve. Johnson et al. (2011) use the measured \( B−V \) colours and \( V \) magnitudes to estimate the relative magnitudes of the stars in the Kepler bandpass, obtaining \( \Delta k_F = 0.74 \pm 0.10 \). This yields a flux ratio of 1.97 ± 0.19 between star A and B. By assuming that all the modulation comes from star A, we use this value to correct for the dilution of the flux produced by the component B. This hypothesis is valid if the amplitude \( \Delta F_B \) of the variability of component B satisfies the relationship:

\[
\frac{\Delta F_B}{F_A + F_B} \ll \frac{\Delta F_A}{F_A + F_B},
\]

where \( \Delta F_A \) is the variability of component A and \( F_A + F_B \) the total flux of the system. Given the above flux ratio, this implies:

\[
\frac{\Delta F_B}{F_B} \ll (1.97 \pm 0.19) \frac{\Delta F_A}{F_A}.
\]
In other words, the relative amplitude of the variability of LHS 6343 B must be much lower than twice that of the A component to ensure that our analysis is consistent. This seems to be reasonable in view of the motivations given above.

3. Light curve modelling

3.1. Transit modelling

Although Johnson et al. (2011) present a transit light curve analysis, recomputing the system parameters considering the currently available dataset is justified, since the more extended Q0–Q6 transit photometry reveals several features related to spot occultations that would cause a bias in the computation of the transit depth if not properly accounted for. Specifically, when the transiting BD occults a dark feature on the disc of the A component, a relative flux increase appears along the light curve leading to a reduced relative depth of the transit (cf., e.g., Ballerini et al. 2012).

For modelling the transits, we retained the original Kepler time cadence of ~29.4 min without applying the 3σ-clipping filter to the time series. Our fitting procedure for the phased transit photometry is based on the Mandel & Agol (2002) analytic model and is performed by using the Transit Analysis Package (Gazak et al. 2012), a graphic user-interface IDL tool. This combines a Markov chain Monte Carlo (MCMC) technique to fit light curves and a wavelet-based likelihood function (Carter & Winn 2009), which is used to compute parameter uncertainties. The model light curve is resampled and rebinned according to the Kepler long-cadence (~29.4 min) data sampling to avoid systematic deviations, in particular during the ingress and egress phases (Kipping 2010). The orbital period is fixed to 12.71382 days (Johnson et al. 2011), and the adjusted parameters are the inclination $i$, the ratio of the companion and primary radii $a/R_A$, the scaled semimajor axis $(a/R_A)$, and the time of mid-transit $T_0$. Limb darkening is treated by adopting a quadratic approximation, and the coefficients are interpolated for the specific LHS 6343 A stellar parameters from the tabulated values of Claret & Bloemen (2011). An attempt to derive the limb-darkening coefficients from the data fitting while fixing the rest of the parameters has resulted in unphysical values, probably due to a complex brightness profile and the presence of active regions. Both $u_1$ and $u_2$ have therefore been fixed to the values obtained from the tables. In most cases, the low impact of the limb darkening on the shape of the transit – note its almost flat-bottomed profile – and the existing degeneracy with other parameters, such as the inclination, makes this a better approach than obtaining the coefficients from transit modelling.

The eccentricity and argument of periastron are given by Johnson et al. (2011). A low value of the eccentricity ($e \approx 0.05$) may still affect the transit modelling by increasing its duration by ~5% when the argument of periastron is changed from $\omega = 0^\circ$ to $\omega = 180^\circ$ (cf. Perryman 2011). Indeed, there is a certain probability that the eccentricity is zero because the value is within two standard deviations from zero (assuming a Gaussian distribution of the parameter). Moreover, the eccentricity is a definite positive quantity so any orbital fit to a radial velocity time series with some degree of noise tends to give a non-zero value for this parameter even if the orbit is perfectly circular (cf., e.g., Husnoo et al. 2012). The eccentricity is expected to be zero in our system, which is close to synchronization, but a possible excitation by perturbations caused by the distant B companion cannot be excluded in the absence of a specific study. However, a transit analysis with the assumption of a circular orbit was also performed and obtained no significant change in the parameter values.

A first modelling of the transit was performed by using a Levenberg-Marquardt algorithm, and a three-sigma clipping filter was applied to the positive residuals of this fit to identify and remove the data points affected by occulted spots. Then, an MCMC fitting algorithm was applied and the resulting posterior parameter probability distribution was obtained from the combination of ten chains. Several extra runs were performed by fixing each of the parameters in turn to check the consistency of the results and find possible systematic errors that were added to the final uncertainties. The error on the stellar flux ratio (see Sect. 2) was also accounted for in the presented uncertainties. The presence of surface brightness inhomogeneities, associated with stellar activity, makes it especially difficult to accurately model the transit with our long-cadence data because the induced perturbations are often unresolved. This produces an increase in the intransit residuals. The results are presented in Table 1 and the fit displayed in Fig. 4. The posterior probability density functions

<p>| Table 1. Parameters obtained from the transit light curve modelling of LHS 6343 A. |
|---------------------------------|-----------------|</p>
<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Radius ratio ($R_C/R_A$)</td>
<td>0.221 ± 0.002</td>
</tr>
<tr>
<td>Semimajor axis $(a/R_A)$</td>
<td>45.5 ± 0.4</td>
</tr>
<tr>
<td>Orbit inclination ($i$)</td>
<td>89.60 ± 0.04</td>
</tr>
<tr>
<td>Impact parameter ($b$)</td>
<td>0.30 ± 0.03</td>
</tr>
<tr>
<td>Mid transit (BJD-2 454 957.0)</td>
<td>0.2174 ± 0.0001</td>
</tr>
<tr>
<td>Linear limb darkening ($u_1,A$)</td>
<td>0.457</td>
</tr>
<tr>
<td>Quadratic limb darkening ($u_2,A$)</td>
<td>0.374^a</td>
</tr>
<tr>
<td>Eccentricity</td>
<td>0.056 ± 0.032</td>
</tr>
<tr>
<td>Argument of periastron, $\omega$ (deg)</td>
<td>-23 ± 56°</td>
</tr>
<tr>
<td>Mean stellar density, $\rho_A$ ($\rho_\odot$)</td>
<td>6.8 ± 0.4</td>
</tr>
</tbody>
</table>

Notes. | (a) Uncertainties correspond to 85.1% confidence interval from MCMC fitting plus the contribution of systematic errors. | (b) Fixed values obtained from Claret & Bloemen (2011). | (c) Fixed values obtained from Johnson et al. (2011). |

![Fig. 4. Upper panel: Kepler LHS 6343 transit photometry from Q0–Q6 (black dots) and the best fit model obtained as described in Sect. 3.1 (red line); crosses indicate data corresponding to spot occultations during the transits. They are not used for modelling the transit. Lower panel: the residuals of the transit best fit (black dots) and the points corresponding to spot occultations (crosses) vs. the time elapsed from mid-transit.](image-url)
of the parameters obtained by the MCMC modelling are shown in Fig. 5 assuming uniform priors.

Our mean transit profile, derived from 41 observed transits of LHS 6343 C after removing the spot perturbations, has a better sampling of the ingress and egress intervals allowing us to reduce the uncertainties on the parameters in comparison with the previous determination by Johnson et al. (2011). Specifically, we find a slightly lower value for the relative radius and a higher value for the inclination, although both are within two standard deviations of their previous values, respectively. That we find a very similar result for $R_C/R_A$ essentially means that spot occultations did not occur or at least were not significant for the five transit events present in the data analysed by Johnson et al. (2011). On the other hand, the results for the relative orbital semimajor axis $a/R_A$ are in close agreement. Also the mean stellar density as computed from the transit parameters (e.g., Seager & Mallén-Ornelas 2003) is consistent with the mass and radius parameters in Table 2, adopted from Johnson et al. (2011).

Some systematic trends are observed in the residuals, almost symmetrically placed around the second and third contacts. They could be due to a complex brightness profile along the occulted chord on the stellar disc. In other words, a quadratic limb-darkening law could not be a good approximation for this very late-type star. Short-cadence data should be used to investigate these systematic deviations further along individual transits.

The occultation of the stellar disc by the BD companion during the transits can be used to resolve the fine structure of the spot pattern and study its evolution (e.g., Silva-Valio et al. 2010; Silva-Valio & Lanza 2011). From the phase-folded data shown in Fig. 4, we find evidence of occulted spots that seem to primarily appear close to mid-transit. This could mean that some active regions are associated with the sub-companion point. Therefore, short-cadence data for LHS 6343 would be particularly interesting for further study. This would also help for constraining the projected obliquity and confirm the quasi-synchronicity of the system (cf., e.g., Sanchís-Ojeda et al. 2011; Sanchís-Ojeda & Winn 2011).

Transit residuals are analysed to look for variability in the transit depth. One of the effects producing such a variability could be a change in the third light contributed by the component B. We find that transit residuals are dominated by noise and do not show any modulation or trend, thus confirming that star B is not active enough to produce a detectable variability and is probably rotating with a much longer period than star A. However, since some scatter in the transit depth may be caused also by active regions in star A that are not occulted during transit, it is difficult to use this result to put a strong constraint on the variability of LHS 6343 B.

3.2. Spot modelling

The reconstruction of the surface brightness distribution from the rotational modulation of the stellar flux is an ill-posed problem, because the variation in the flux vs. rotational phase contains information only on the distribution of the brightness inhomogeneities vs. longitude. The integration over the stellar disc effectively cancels any latitudinal information, particularly when the inclination of the rotation axis along the line of sight is close to 90°, as is assumed in the present case (see Sect. 3.3 and Lanza et al. 2009a). Therefore, we need to include a priori information...
in the light curve inversion process to obtain a unique and stable map. This is done by computing a maximum entropy (ME) map, which has been proven to successfully reproduce active region distributions and area variations in the case of the Sun (cf. Lanza et al. 2007).

Our approach has been compared with other spot modelling methods by Mosser et al. (2009) and Huber et al. (2010) and with the maps obtained by spot occultations during the planetary transits in the CoRoT-2 system by Silva-Valio & Lanza (2011). To model the high-precision space-borne photometry of ε Eri and K1 Ceti obtained by MOST (the Microvariability and Oscillation of STar satellite), Croll (2006), Croll et al. (2006), and Walker et al. (2007) have developed a sophisticated approach based on a few circular spots. They use simulated annealing and tempering techniques to explore the multi-dimensional model parameter space and Markov chain Monte Carlo methods to assess the parameter uncertainties. The main limitation of these models is that the reduced \( \chi^2 \) values of their best fits are significantly greater than the unity. This indicates that the model assumptions, in particular the consideration of only two or three fixed spots, are too simplified to reproduce the true stellar variability down to the level of precision of space-borne photometry.

A similar approach has been applied in the case of the Kepler light curves by Frasca et al. (2011) and Fröhlich et al. (2012) by considering several spots whose areas evolve with time. Although these models allow a convincing determination of the model parameters and their uncertainties, they require a huge amount of computation and their best fits often show systematic deviations suggesting that the spot pattern is more complex than can be described with several circular, non-overlapping starspots. Therefore, we prefer to use a continuous distribution for the spotted area and a regularization approach to find a unique and stable solution.

An important advantage of the ME regularization is that the multi-dimensional parameter space of the objective function to be minimized (cf. Eq. (6)) has a smoother landscape than the \( \chi^2 \) landscape of a multi-spot model, thanks to the addition of the configurational entropy term (the function \( S \) defined below; cf. the analogous problem of image restoration in Bryan & Skilling 1980). This effectively reduces the problems associated with the presence of several \( \chi^2 \) relative minima falling in widely separated regions of the parameter space (cf. Croll et al. 2006; Walker et al. 2007). Moreover, we effectively average over many degrees of freedom by only considering the distribution of the spotted area vs. the stellar longitude, which is the only information that can be directly extracted from our unidimensional time series. Therefore, the basic role of our regularization is that of smoothing the distribution of the spot filling factor versus longitude, thus reducing the impact of the noise on the light curve inversion process.

In our model, the star is subdivided into 200 surface elements, namely 200 squares of side 18°, with each element containing unperturbed photosphere, dark spots, and facular areas. The fraction of an element covered by dark spots is indicated by the filling factor \( f \), the fractional area of the faculae is \( Qf \), and the fractional area of the unperturbed photosphere is \( 1 - (Q + 1)f \). The contribution to the stellar flux coming from the \( k \)th surface element at the time \( t_j \), where \( j = 1, ..., N \) is an index numbering the \( N \) points along the light curve, is given by

\[
\Delta F_{kj} = I_0(\mu_k) \left\{ 1 - (Q + 1)f_k + c_f f_k + Qf_k[1 + c_l(1 - \mu_k)]n_k(\mu_k), \right. 
\]

where \( I_0 \) is the specific intensity in the continuum of the unperturbed photosphere at the isophotal wavelength of the observations; \( c_f \) and \( c_l \) are the spot and facular contrasts, respectively (cf. Lanza et al. 2004); \( n_k \) is the area of the \( k \)th surface element, and \( w(\mu_k) = \{ 1 \text{ if } \mu_k \geq 0 \}, \quad 0 \text{ if } \mu_k < 0 \) is its visibility; and

\[
\mu_k = \cos \psi_k = \sin i \sin \theta_c \cos[\ell_k + \Omega(t_j - t_0)] + \cos i \cos \theta_c, \quad \psi_k \quad (5)
\]

is the cosine of the angle \( \psi_k \) between the normal to the surface element and the direction of the observer, with \( i \) being the inclination of the stellar rotation axis along the line of sight; \( \theta_c \) the colatitude and \( \ell_k \) the longitude of the \( k \)th surface element; \( \Omega \) denotes the angular velocity of rotation of the star (\( \Omega = 2\pi/P_{rot} \), with \( P_{rot} \) the stellar rotation period), and \( t_0 \) the initial time. The specific intensity in the continuum varies according to a quadratic limb-darkening law, as adopted by Lanza et al. (2003) for the case of the Sun, viz. \( I_0 \propto a_p + b_p\mu + c_p\mu^2 \). The stellar flux computed at the time \( t_j \) is then \( F(t_j) = \sum_k \Delta F_{kj} \).

To warrant a relative precision of the order of \( 10^{-5} \) in the computation of the flux \( F \), each surface element is further subdivided into \( 1'' \times 1'' \)-elements, and their contributions, calculated according to Eq. (3), are summed up at each given time to compute the contribution of the \( 18'' \times 18'' \) surface element to which they belong.

We fit the light curve by varying the value of \( f \) over the surface of the star, while \( Q \) is held constant. Even fixing the rotation period, the inclination, and the spot and facular contrasts (see Lanza et al. 2007, for details), the model has 200 free parameters and suffers from non-uniqueness and instability. To find a unique and stable spot map, we apply ME regularization by minimizing a functional \( Z \), which is a linear combination of the \( \chi^2 \) and the entropy functional \( S \); i.e.,

\[
Z = \chi^2(f) - \lambda S(f), \quad (6)
\]

where \( f \) is the vector of the filling factors of the surface elements, \( \lambda > 0 \) a Lagrangian multiplier determining the trade-off between light curve fitting and regularization. The expression for \( S \) is given in Lanza et al. (1998). The entropy functional \( S \) attains its maximum value when the star is free of spots. Therefore, by increasing the Lagrangian multiplier \( \lambda \), we increase the weight of \( S \) in the model, and the area of the spots is progressively reduced. This gives rise to systematically negative residuals between the observations and the best-fit model when \( \lambda > 0 \). The optimal value of \( \lambda \) depends on the information content of the light curve, which in turn depends on the ratio of the amplitude of its rotational modulation to the average error of its points. In the case of LHS 6343 A, the amplitude of the rotational modulation is \( \sim 0.001 \), while the average error of the points is \( \sim 5 \times 10^{-5} \) in relative flux units, giving a signal-to-noise ratio of \( \sim 20 \). The significant impact of the noise on the light curve makes the regularization a critical process, and a different criterion than that applied for CoRoT-2 (see Lanza et al. 2009a) or CoRoT-6 (see Lanza et al. 2011) must be adopted, because in those cases the signal-to-noise ratio was \( > 100 \). For the present case, we increase the regularization until we obtain \( \lambda_{ent} = 2.5 \), where \( \lambda_{ent} \) is the mean of the residuals of the regularized light curve, and \( \beta_0 \equiv \sigma_0 \sqrt{N} \) is the standard error of the residuals of the unregularized light curve (i.e., obtained with \( \lambda = 0 \)), defined as the ratio of their standard deviation \( \sigma_0 \) to the square root of the number of data points \( N \) in each individual segment.
of duration $\Delta t_f$ fitted by our model (see below). The parameter $\beta \geq 1$ depends on the information content of the light curve and is unity when the signal-to-noise ratio is of the order of 100 or greater. In our case, we determine the optimal value of $\beta$ after posteriori, by increasing $\Delta$ until the small random spots associated with the noise are strongly smoothed, while the deviation of the regularized model from the data points is still acceptable (see Sect. 4.1 and Appendix A for the effects of varying $\beta$ on the solution).

In the case of the Sun, by assuming a fixed distribution of the filling factor, it is possible to obtain a good fit of the irradiance changes only for a limited time interval $\Delta t_f$, not exceeding 14 days, which is the lifetime of the largest sunspot groups dominating the irradiance variation. In the case of other active stars, the value of $\Delta t_f$ must be determined from the observations themselves, looking for the longest time interval that allows a good fit with the applied model (see Sect. 3.3).

The optimal values of the spot and facular contrasts and of the facular-to-spotted area ratio $Q$ in stellar active regions are unknown a priori. In our model the facular contrast $c_f$ and the parameter $Q$ enter as the product $c_fQ$, so we can fix $c_f$ and vary $Q$, estimating its best value by minimizing the $\chi^2$ of the model, as shown in Sect. 3.3. Since there are many free parameters in the ME model is large, for this specific application we make use of the model of Lanza et al. (2003), which fits the light curve by assuming only three active regions to model the rotational modulation of the flux plus a uniformly distributed background to account for the variations in the mean light level. This procedure is the same as used to fix the value of $Q$ in the cases of CoRoT-2, CoRoT-4, CoRoT-7, and CoRoT-6 (cf. Lanza et al. 2009a, 2010, 2011).

We assume an inclination of the rotation axis of LHS 6343 A of $i = 90^\circ$ in most of our models (see Sect. 3.3), coming from the results of the transit modelling (see Sect. 3.1). Such a high inclination implies that negligible information on the spot latitude can be extracted from the rotational modulation of the flux, so that the ME regularization virtually puts all the spots around the subobserver latitude (i.e., $\approx 0^\circ$) to minimize their area and maximize the entropy. Therefore, we are limited to mapping only the distribution of the active regions vs. longitude, which can be done with a resolution better than $\sim 50^\circ$ (cf. Lanza et al. 2007, 2009a). Our ignorance of the true facular contribution may lead to systematic errors in the active region longitudes derived by our model because faculae produce an increase in the flux when they are close to the limb, leading to a systematic shift of the longitudes of the active regions used to reproduce the observed flux modulation, as discussed by Lanza et al. (2007) for the case of the Sun and illustrated by Lanza et al. (2009a, cf. Figs. 4 and 5) for CoRoT-2.

Given the dependence of our modelling approach on several parameters, we present a detailed discussion of their impact on our results in Appendix A.

### 3.3. Model parameters

The fundamental stellar parameters are taken from Johnson et al. (2011) and are listed in Table 2. A quadratic limb-darkening law is adopted for the stellar photosphere, viz., $I(\mu) = a_p + b_p\mu + c_p\mu^2$, where the coefficients $a_p$, $b_p$, and $c_p$ have been obtained for $T_{\text{eff}} \approx 3130$ K, $\log g = 4.85$ [cgs], and solar abundances from the theoretical values computed by Claret & Bloemen (2011) from Phoenix model atmospheres.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Ref.</th>
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<tbody>
<tr>
<td>Star mass ($M_\star$)</td>
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<tr>
<td>Star radius ($R_\star$)</td>
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<td>$T_{\text{eff}}$ (K)</td>
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<tr>
<td>$\log g$ (cm s$^{-2}$)</td>
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<tr>
<td>$c_p$</td>
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<td>$P_{\text{rot}}$ (days)</td>
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<tr>
<td>$\epsilon$</td>
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</tr>
<tr>
<td>Inclination (deg)</td>
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</tr>
<tr>
<td>$c_f$</td>
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</tr>
<tr>
<td>$c_t$</td>
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</tr>
<tr>
<td>$Q$</td>
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</tr>
<tr>
<td>$\Delta t_f$ (days)</td>
<td>8.769</td>
</tr>
</tbody>
</table>

### References

CB11: Claret & Bloemen (2011); He12: present work; J11: Johnson et al. (2011); L04: Lanza et al. (2004).

The rotation period for modelling the spotted photosphere was fixed to the companion orbital period. This assumption comes from the periodogram analysis giving $P_{\text{rot}} = 12.71 \pm 0.28$ days (see Fig. 2), which indicates that the system is close to synchronization. As we see in Sect. 4.2, any deviation of stellar rotation from synchronization will appear on the ME map as a longitude drift of the active regions versus time.

The rotation period of 12.71 days is used to compute the polar flattening of the star due to the centrifugal potential in the Roche approximation, yielding a relative difference between the equatorial and the polar radii $\epsilon$ of $6.09 \times 10^{-6}$. The effect of this flattening on the modulation caused by spots is negligible. The relative difference in flux for a $\sim 2\%$ spot coverage would be less than $10^{-5}$ as a consequence of the gravity darkening in the equatorial regions of the star.

Owing to the lack of a measurement of the Rossiter-McLaughlin effect or precise $v \sin i$ data, the inclination of the stellar axis of LHS 6343 A cannot be constrained. The limit on $v \sin i < 2$ km s$^{-1}$ given by Johnson et al. (2011) does not help because the above rotation period and the radius yield an equatorial rotation velocity of $\sim 1.5$ km s$^{-1}$. Nevertheless, we assume that the system is spin-orbit aligned; that is, its inclination is assumed to be equal to that of the orbit of the BD companion, i.e., $89.60 \pm 0.04$. The inclination of the stellar spin axis along the line of sight is of primary concern for characterizing the geometry of the stellar rotation for modelling the out-of-transit light modulation. If we had been interested in also modelling the occultations of starspots during transits, the sky-projected angle between the stellar spin and the orbital angular momentum would have been required, too (e.g., Sanchis-Ojeda et al. 2012).

The maximum time interval $\Delta t_f$ that our model can accurately fit with a fixed distribution of active regions has been determined by means of a series of tests dividing the total interval, $T = 508.5936$ days, into $N_t$ equal segments, i.e., $\Delta t_f = T/N_t$. The simple three-spot model of Lanza et al. (2003) has been applied to fit the individual intervals to reduce the number of free parameters. The optimal $N_t$ is given by the minimum value that allows us a good fit to the light curve as measured by the $\chi^2$ statistics. For $N_t < 58$, the quality of the fit starts to degrade significantly, so we adopt this as the optimal number of segments, giving $\Delta t_f = 8.769$ days (cf. Appendix A). In any case, $\Delta t_f > P_{\text{rot}}/2$ is required to adequately sample the light...
modulation produced by a rotating active region, providing us with information on its longitude and area. On the other hand, a too long $\Delta t$ would result in a low time resolution of our model, so that starspot evolution and migration would be more difficult to trace.

The spot temperature contrast is estimated by the correlation found in Fig. 7 of Berdyugina (2005) that shows that the contrast decreases with decreasing stellar effective temperature. Thus, we adopt a spot temperature deficit of $\Delta T_\text{S} = -250$ K for LHS 6343 A and compute the spot’s intensity contrast considering blackbody emission for the spots and the photosphere in the Kepler passband, yielding $c_s = 0.536$. This is not a critical parameter because a variation in $c_s$ will only cause a change in the overall spot filling factor, but will not affect either spot longitudes or their time evolution, as discussed in detail by Lanza et al. (2009a). The facular contrast is assumed to be solar-like with $c_f = 0.115$ (Lanza et al. 2004).

The ratio $Q$ between the facular and the spotted areas in active regions is estimated by means of the three-spot model introduced by Lanza et al. (2003) simultaneously with the optimal value of $\Delta t$. Both the flux increase due to the facular component when an active region is close to the limb and the flux decrease due to its spots when that region transits across the central meridian of the disc are modelled by this approach, allowing us to derive the optimal value of $Q$, if the signal-to-noise ratio of the data is high enough.

In Fig. 6 we plot the ratio $\chi^2_\min/\chi^2_\text{true}$ of the total $\chi^2$ of the composite best fit of the entire time series to its minimum value vs. the parameter $Q$, i.e., the ratio of the facular area to the cool spot area in active regions. The horizontal dashed line indicates the 95% confidence level for $\chi^2/\chi^2_\text{true}$. This does not put any significant constraint on the interval of acceptable $Q$ values owing to the low signal-to-noise ratio of the data.

4. Results

4.1. Light curve model

The composite best fit obtained with the ME regularization and $Q = 8.0$ is shown in Fig. 7 (upper panel) together with the residuals (lower panel). From a best fit without regularization ($\lambda = 0$) applied to the whole time series ($Q0$–$Q6$), we obtain a mean $\mu_{\text{res}} = 8.308 \times 10^{-9}$ and a standard deviation of the residuals $\sigma_0 = 6.778 \times 10^{-5}$ in relative flux units, which is slightly higher than the standard error of the mean points. This can be due to short time scale fluctuations that cannot be fitted with our approach that reproduces variations on a timescale comparable to $\Delta t$ or longer. On average, we have $N \sim 98$ data points per fitted subset $\Delta t$.

The Lagrangian multipliers $\lambda$ for the regularized ME models are iteratively adjusted until the mean of the residuals $\mu_{\text{reg}} = -1.365 \times 10^{-5} \approx -\beta(\sigma_0/\sqrt{N})$, where $\beta = 2$ is established as the optimal value that still leads to an acceptable fit while reducing the information content of the spot maps as much as possible, i.e., maximizing the entropy. A lower value of $\beta$ improves the fit slightly over small sections of the light curve, but introduces several small spots that change from one time interval to the next without any clear regularity. On the other hand, by selecting $\beta = 2$, we obtain smoother maps with concentrated groups of spots that evolve regularly from one $\Delta t$ interval to the next, which indicates that we are properly modelling the overall distribution of the active regions on the star. A higher level of regularization ($\beta > 2$) gives unacceptably larger, systematically negative residuals because the maximum entropy criterion reduces the spotted area too much. At the same time, it concentrates the spots into isolated groups, and a pattern with three active regions equally spaced in longitude (i.e., with $\approx 120^\circ$ gaps) begins to appear. This pattern still shows the general migration of the multiple spots appearing in the maps with the optimal regularization (see Sect. 4.2), but it is clearly an artefact of the over-regularization, due to the limited signal-to-noise level of our data that favours a reproduction of the light variations by a decreasing number of spots when the regularization is increased (cf. Appendix A).

In either case, the low signal-to-noise ratio of our data requires a relatively strong regularization, and as a consequence, misfits sometimes appear at the matching points between time intervals. Therefore, by decreasing $\Delta t$, the overall quality of the best fit is not increased in our case. Nevertheless, looking at the residuals of our regularized composite best fit, we see a generally good reproduction of the light variations without systematics that could be attributed to sizable active regions evolving on timescales significantly shorter than $\Delta t$. We notice that the noise level increases after BJD 2 455 276 (corresponding to BJD-2 454 833 = 443 in Fig. 7), which coincides with the beginning of quarter Q5 and returns to the previous level after BJD 2 455 371 (BJD-2 454 833 = 538), i.e., at the beginning of quarter Q6. This is a consequence of the rotation of the focal plane of the Kepler telescope between successive quarters, which makes the target be measured on a different CCD.

4.2. Distribution of active regions and stellar rotation

The distribution of the spot filling factor $f$ versus longitude and time is plotted in Fig. 8 for our ME model with $Q = 8.0$ adopting a reference frame rotating with the orbital period of the BD companion, i.e., 12.7138 days. The origin of the longitude frame corresponds to the subobserver point at the beginning of the Kepler time series (i.e. BJD 2 454 953.569) and the longitude increases in the same direction as the stellar rotation and the orbital motion of the companion. The subcompanion longitude is fixed at $\sim 257^\circ$ in this reference frame.

Several individual active regions can be identified from the map in Fig. 8 showing lifetimes around 15–20 days. Three
dotted lines have been drawn connecting the longitudes with higher filling factors to trace the overall migration of the spots. They identify three long-lived active longitudes that migrate backwards at the same constant rate. This indicates that the rotation of the star is somewhat slower than that of our reference frame following the orbital motion of the BD companion. The similarity of the migration rates among the three active longitudes suggests that either the spot latitudes are confined to a thin belt or the star has no detectable differential rotation.

By considering the longitudes of the relative maxima of the spot covering factor in Fig. 8, a linear fit is performed to find the relative rotation rates associated with the steady migration of the three main starspots. The results are listed in Table 3 for two models having a different facular-to-spotted area ratio $Q$. By assuming a significant facular contribution ($Q = 8.0$), a mean rotation period of $13.137 \pm 0.011$ days is obtained. This is a significantly slower rotation than the companion orbital motion, showing that the system is slightly out of synchronism. The stellar rotation, as traced by starspots, appears to be rigid since there is no significant difference between the highest and the lowest migration rates. The migration rates for a spot model assuming only dark spots ($Q = 0$) are also reported in Table 3, because the longitudes of the spots derived from the maximum entropy modelling may depend on the value of $Q$ (Lanza et al. 2007, 2009a). Nevertheless, very similar results are obtained, thus confirming that the presence of faculae is not actually required to adequately fit the low signal-to-noise photometry of LHS 6343 A (cf. Sect. 3.3). In the case of no faculae, a virtually identical mean rotation period of $13.129 \pm 0.015$ days is obtained from the migration of the spots.

An intriguing phenomenon seen in Fig. 8 is that the spot filling factor shows a persistent relative minimum in the longitude range between $\approx 100^\circ$ and $\approx 250^\circ$, while it has a relative maximum between $\approx 250^\circ$ and $\approx 450^\circ$. In other words, the filling factor appears to be systematically enhanced when the migrating starspots approach and cross a longitude leading the subcompanion longitude by $\approx 100^\circ$ in our reference frame. Since the passage of that longitude across the centre of the stellar disc precedes
that of the BD companion, this agrees with the light curve that shows a relative light minimum ~3.5 days before each transit. This modulation has persisted for more than 500 days, as far as the *Kepler* data currently cover.

This enhancement of the spot filling factor is highlighted in Fig. 9, where the spot coverage factor integrated over the time is plotted vs. longitude in bins of 72°. A wide maximum is evident around ~350°, meaning that activity tends to be concentrated in a region preceding the subcompanion longitude. This agrees closely with what can be seen in Fig. 1, and especially in the phase-folded light curve (Fig. 3). Moreover, this explains the results obtained by the Lomb-Scargle periodogram (Fig. 2) because only the frequency of the main modulation associated with this activity enhancement, phased to the companion C, is detected by that method. On the other hand, ME modelling allows us to map individual starspots and follow their migration across the longitude where they show an enhancement. Unfortunately, no information on the spot latitudes can be derived with our models, so we cannot establish whether the enhancement of activity at this longitude is produced in a sin-
The possibility that magnetic interactions in star-planet systems lead to an enhancement of stellar activity was initially suggested by Cuntz et al. (2000) and Cuntz & Shkolnik (2002). Some evidence has been found in several star-planet systems from the modulation of chromospheric activity indexes in phase with the orbit of the planet rather than with the rotation period of the star (Shkolnik et al. 2005). For HD 179949, HD 189733, and τ Boo, an enhancement of the flux variability has been observed preceding the subplanetary planetary period by ~70° during several observing campaigns (Shkolnik et al. 2008).

In the case of LHS 6343 A, where the companion is a low-mass BD object, the available data are photometric, so the activity modulation is observed in the photosphere. Here, a phase lead of 98° between the transits and the photometric minima is observed (see Sects. 2 and 4.2). The effect peaks once per orbit, thus suggesting a magnetic interaction because two relative maxima per orbit are expected in the case of a tidal interaction due to the symmetry of the tidal bulge. Moreover, the relative amplitude of the flux modulation due to the ellipsoidal deformations of LHS 6343 A does not exceed ~5 × 10^{-5} owing to the large separation of the A and C components (Pfähl et al. 2008). Even considering an orbit with an eccentricity of 0.1, the difference in the ellipsoidal light variation between the periastron and apostron does not exceed ~3 × 10^{-5} in relative flux units. Therefore, the observed flux modulation with a relative amplitude of ~10^{-3}, phased to the orbital motion of the BD, cannot be attributed to the tidal distortion of the primary star.

Similar cases of photospheric active regions rotating in phase with a close-in massive planet have been reported for τ Boo (Walker et al. 2008) and CoRoT-4 (Lanza et al. 2009b). In the former case, a photospheric active region producing a signature of the order of one millimag was observed in different seasons with the MOST satellite. The feature was sometimes dark, sometimes bright, and was associated with phase with the persistent chromospheric hot spot discussed above. In the case of CoRoT-4, a preferential longitude for spot appearance was found within ~40°–50° from the subcompanion point. The rotation of both stars is close to synchronization as in the case of LHS 6343 A. Although τ Boo and CoRoT-4 are F-type stars, the same mechanism could be at work in all three cases.

Several models have been proposed to account for the features of the magnetic interaction between stars and close-in planets. They can be extended to the case of a close BD companion as in LHS 6343 AC. The models of McIntyre et al. (2006), Preuss et al. (2006), and Lanza (2008) have focussed on interpreting the phase lag between the planet and the maximum visibility of the chromospheric hot spot by adopting different hypotheses, e.g., a tilted potential stellar magnetic field, a finite propagation time of the magnetic perturbation along the field lines from the planet to the star, or a non-potential twisted field in the stellar corona. They are generally capable of accounting for the phase lag observed in the case of a chromospheric hot spot, but cannot account for an enhancement of the photospheric activity. As shown by the numerical MHD simulations of Cohen et al. 2009, 2011a,b, when the planetary magnetosphere is inside or in touch with the stellar Alfvén surface, a remarkable interaction between the stellar and the planetary fields occurs, and the energy released in the magnetic reconnection can be transferred down to the stellar chromosphere and photosphere. This can account for a localized enhancement of the flux, i.e., a local brightening as in large solar flares that have a white-light photospheric counterpart to their chromospheric and coronal emission. However, the appearance of dark spots associated with a close-by companion requires a different mechanism. Lanza (2008, 2011) have conjectured that the perturbation of the coronal field and the triggering of flaring activity in the corona may increase the loss rate of magnetic helicity through coronal mass ejections (cf. also Lanza 2012) leading to a perturbation of the stellar dynamo. As reviewed by, e.g., Brandenburg et al. (2012), the operation of the dynamo in late-type stars implies a mechanism that can get rid of the magnetic helicity that is continuously pumped into the small field scales, otherwise the dynamo is rapidly quenched by magnetohydrodynamic effects. In the Sun, coronal mass ejections associated with large flares are regarded as a viable mechanism for accomplishing this goal, therefore an enhancement of flaring activity in stars with close-in companions may help the operation of the dynamo. Since the perturbation moves in phase with the planet, the associated loss of magnetic helicity is non-axisymmetric and may lead to a modulation of the α effect of the stellar dynamo in phase with the motion of the companion (see Lanza 2008, 2011, for details). In systems that are close to synchronization, the modulation can be particularly effective thanks to the slow relative motion of the companion in the reference frame rotating with the star that increases the duration of the interaction between a stellar coronal structure and the magnetic field of the orbiting body. The phase lag between the starspots and the companion may be explained by adopting a twisted magnetic field interconnecting the spots with the orbiting BD as discussed in Lanza (2008).

An alternative explanation taking into account the destabilizing effects of the tidal perturbation on the magnetic flux tubes inside the red dwarf star cannot of course be excluded. In this scenario, the persistent active longitude would correspond to the periastron passage of the BD companion with the phase lag of ~98° being the angular distance of that point from the mid-transit. Recent works suggesting a possible gravitational perturbation of the planets on the solar dynamo may give support to this conjecture (cf., e.g., Abreu et al. 2012, and references therein).

6. Conclusions

Considering 508 days of Kepler photometry of the visual system LHS 6343, we have computed a new best fit to the mean photometric transit profile of the C brown dwarf component across the disc of the A component. We essentially confirm the transit parameters found by Johnson et al. (2011) and reduce their uncertainties. A maximum entropy spot model was applied to the Kepler light curve of LHS 6343 to derive maps of the longitudinal distribution of the active regions on the A component, assumed to be responsible for the out-of-transit modulation of the flux. While including faculae is not found to be critical for obtaining an acceptable fit to the light modulation, an optimal fit of the light curve is found for a facular-to-spotted area ratio around Q = 8.0.

Our maps show several active regions with a slower rotation rate (P_{rot} = 13.14 ± 0.02 days) than the BD orbital period (P_{orb} = 12.71 days), implying that the AC system is quasi-synchronized. Owing to the limited signal-to-noise ratio of the data and the fast evolution of the active regions that have lifetimes of 1520 days, it is not possible to detect any differential rotation signature. On the other hand, the starspot covering factor is observed to be systematically enhanced when the spots cross a longitude leading the substellar point by ~100°. This effect is also detected in the photometric time series as a modulation with the orbital period of the BD showing minima ~3.5 days before each transit. That this active longitude persists for more than ~500 days provides evidence that the BD companion does affect...
the photospheric activity of its host somewhat. We conjecture that a magnetic interaction between the coronal field of the M dwarf and the BD may produce a modulation of the stellar dynamo leading to an increase in activity modulated in phase with the orbital motion (see Sect. 5).

A monitoring of the system through measurements of the modulation of the chromospheric lines (e.g., Hα or Ca II H&K) and coronal X-ray emission would be very helpful, because a detection of a hot spot in the upper stellar atmosphere with the same phase lag as the detected photospheric active longitude would indicate interactions through magnetic field reconnection, thus supporting the conjectured mechanism.

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Appendix A: Influence of the adopted model parameters on the spot maps

A.1. Time resolution (Δt) and amount of regularization (β)

In Sect. 3.3 we discussed the method applied to determining the maximum time interval Δt that our model can accurately fit when considering a fixed distribution of three active regions (Lanza et al. 2003). This corresponds to the time resolution of our model, since we assume that active regions do not evolve on timescales shorter than Δt. The total interval T was divided to Nf segments so that Δt = T/Nf. The optimal Nf was found to be 58 from the best fit of the three-spot model, as measured from the χ^2 statistics.

Three cases corresponding to different lengths of the time interval Δt are presented in Fig. A.1, where the ratio χ^2/χ^2_min is plotted vs. Q, the facular-to-spotted area ratio; χ^2 is the chi square of the composite best fit to the total time series; and χ^2_min is the minimum χ^2 obtained for Nf = 58 and Q = 8.0. The corresponding spot model is discussed in the text. Here we explore the case with Nf = 50 and perform an ME analysis with the corresponding time interval, i.e., Δt = 10.1719 days, to investigate the effect of a different Δt on our results. The same approach as described in Sect. 4.1 was considered, and regularized ME models were iteratively adjusted until β = 2. The isocontour map of the distribution of the spot filling factor vs. time and longitude is presented in Fig. A.2. It is remarkably similar to the one presented in Fig. 8 and the phased activity enhancement around ~350° is still visible, although the migration of the starspots and their changes on short timescales are less evident. Therefore, a longer time interval limits the possibility of accurately measuring spots’ migration and estimate their lifetimes.

In a second test, we chose the same time interval as in Sect. 4, i.e., Nf = 58, to explore the effects of a different amount of regularization on the ME spot maps. In Fig. A.3, we present a spot map obtained with a lower regularization (β = 1). At that point, the large starspots appearing in Fig. 8 are resolved into several smaller spots. This fine structure changes vs. the time without any clear regularity, as expected for an artefact due to overfitting the noise present in the data.

Finally, we plot the distribution of the filling factor obtained with β = 3 in Fig. A.4. The effects of the overregularization described in Sect. 4.1 can be seen as a tendency for the appearance of larger and smoother spot groups that include previously resolved starspots. Three main groups separated by approximately 120° in longitude generally appear, showing the same backwards migration as with β = 2, the optimal value adopted for the regularization. The residuals of the composite best fit to the light curve (not shown) show larger systematic deviations than in the cases with β = 1 or β = 2, again a sign of overregularization.

A.2. Inclination of the stellar spin axis

The inclination of the stellar spin is assumed to be equal to that of the orbit of the BD companion in our analysis, i.e. i = 89.60. An isotropic orientation of the stellar spin axis has its mode at i = 90° (Herrero et al. 2012), so it is reasonable to choose a value close to this, given that there is no a priori information to constrain the parameter.

The tidal timescale for the alignment of the stellar spin and the orbital angular momentum are comparable, in the case of LHS 6343 A, to the synchronization timescale that is estimated to be ≈7.5 Gyr. Given a probable age of the system between 1 and 5 Gyr, we cannot be sure that the obliquity has been damped by tides, unless we assume that most of the damping occurred during the pre-main-sequence phase when the tidal interaction was stronger due to a larger R_A (cf. Sect. 5). Therefore, we adopt a prudential approach and explore different cases in which the system is out of spin-orbit alignment.

We adopt the same parameters as in Sect. 4.1 and compute a regularized ME best fit of the light curve with β = 2, fixing the stellar inclination to i = 60° and i = 45°. The resulting spot maps are plotted in Figs. A.5 and A.6, respectively. We may expect that the latitudinal distribution of the spots are remarkably different, especially for i = 45°. On the other hand, the plotted distributions of the filling factor vs. longitude and time are

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Fig. A.1. Ratio of the χ^2 of the three-spot model fit to the minimum value for Nf = 58 (χ^2_min) vs. the parameter Q, i.e., the ratio of the facular area to the cool spot area in active regions. Solution series for three different values of the time interval Δt = T/Nf are shown.

Fig. A.2. As in Fig. 8, but adopting a longer time interval Δt = 10.1719 days.
Fig. A.3. As in Fig. 8, but performing an ME regularization with $\beta = 1$.

Fig. A.4. As in Fig. 8, but performing an ME regularization with $\beta = 3$.

Fig. A.5. As in Fig. 8, but adopting a stellar inclination of $i = 60^\circ$.

Fig. A.6. As in Fig. 8, but adopting a stellar inclination of $i = 45^\circ$.

Similar to what is computed with $i = 89.60^\circ$. Also the evolution and migration of the active regions are similar to that case. Only some details appear to be critically dependent on the adopted inclination.

The results of the tests described in this Appendix confirms that by averaging the ME spot maps over latitude, we can effectively remove most of the degeneracy present in the light curve inversion process.