

Hot subdwarf stars in close-up view

III. Metal abundances of subdwarf B stars[★]

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ABSTRACT

Context. Hot subdwarf B stars (sdBs) are considered to be core helium-burning stars with very thin hydrogen envelopes situated on or near the extreme horizontal branch. The formation of sdBs is still unclear as well as the chemical composition of their atmospheres. The observed helium depletion is attributed to atmospheric diffusion. Metal abundances have been determined for about a dozen sdBs only resulting in puzzling patterns with enrichment of heavy metals and depletion of lighter ones.

Aims. We present a detailed metal abundance analysis of 106 sdBs.

Methods. From high resolution spectra we measured elemental abundances of up to 24 different ions per star. A semi-automatic analysis pipeline was developed to calculate and fit LTE models to a standard set of spectral lines.

Results. A general trend of enrichment was found with increasing temperature for most of the heavier elements. The lighter elements like carbon, oxygen, and nitrogen are depleted and less affected by temperature. Although there is considerable scatter from star to star, the general abundance patterns in most sdBs are similar. State-of-the-art diffusion models predict such patterns and are in qualitative agreement with our results. However, the highest enrichments measured cannot be explained with these models. Peculiar line shapes of the strongest metal lines in some stars indicate vertical stratification to be present in the atmospheres. Such effects are not accounted for in current diffusion models and may be responsible for some of the yet unexplained abundance anomalies.

Key words. stars: atmospheres – subdwarfs

1. Introduction

Subluminous B (sdB) stars are considered to be core helium-burning stars with very thin hydrogen envelopes and masses around $0.5 M_{\odot}$ (Heber et al. 1986; Heber 2009). The formation of these objects is still unclear. SdB stars can only be formed, if the progenitor loses its envelope almost entirely after passing the red-giant stage and the remaining hydrogen-rich envelope has not retained enough mass to sustain a hydrogen-burning shell. The star cannot ascend the asymptotic giant branch, but remains on the extreme horizontal branch (EHB) until the core helium-burning stops and eventually evolves to become a white dwarf. The reason for this very high mass loss near the core helium flash is still unclear. Several single star and close binary scenarios are currently under discussion (see Han et al. 2002, 2003; Yi 2008, and references therein). Close binary evolution is a promising option, because the envelope can be lost through common envelope ejection or stable Roche lobe overflow. An alternative way of forming a single sdB is the merger of two helium white dwarfs (Webbink 1984; Iben & Tutukov 1984).

The abundance anomalies of hot subdwarf stars are very important to understand the physical properties of hot stellar atmospheres. Sargent & Searle (1966) discovered the helium deficiency of sdB stars for the first time. This finding seemed to be at variance with the big-bang theory of nucleosynthesis. Greenstein, Truran & Cameron (1974) suggested that diffusion

in the hot atmosphere of sdBs could cause the helium deficiency. Peculiar metal abundances were first reported by Baschek et al. (1972) for HD 4539. While some metals show solar abundances, others are depleted or even enriched.

Studies of optical spectra remained scarce. Heber et al. (1999, 2000) analysed high resolution spectra of four pulsating sdB stars taken with *Keck/HIRES*. Napiwotzki et al. (2001) and Telting et al. (2008) derived metal abundances of the sdB binary HE 1047–0436 and the hybrid sdB pulsator Balloon 090100001 from optical spectra, respectively. Finally, Edelmann et al. (1999, 2001), Przybilla et al. (2006) as well as Pereira & Jeffery (2008) published some preliminary results of their analysis of high resolution spectra.

Hot stars display a much larger number of spectral lines in the ultraviolet (UV) than in the optical. With the advent of the IUE satellite it became possible to determine abundances of C, N and Si from strong UV resonance lines for nine sdB stars (Lamontagne et al. 1987 and references therein). Lines of heavier metal have been analysed from IUE spectra of two stars (Baschek et al. 1982a,b). The most detailed analysis of UV spectra has been carried out by O’Toole & Heber (2006) based on spectra obtained with STIS onboard *Hubble* Space Telescope (HST). The FUSE satellite opened up the far UV (FUV) regime for abundance studies. Many sdBs have been observed, but only some have been analysed (Fontaine et al. 2006; Chayer et al. 2006; Blanchette et al. 2008; Pereira & Jeffery 2008).

Due to their faintness, quantitative analyses of hot subdwarfs in globular clusters (GCs) are restricted to low-resolution

[★] Tables A.1–A.3 are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/549/A110>

spectroscopy. Therefore constraints can only be put on the helium abundances and the analysis of metal abundances remains coarse (Heber et al. 1986; Moni Bidin et al. 2007; Moehler et al. 2007; Brown et al. 2011).

The blue horizontal branch (BHB) stars are the cooler siblings of the EHB stars ($T_{\text{eff}} < 20\,000$ K; for a review see Behr 2003a). Their chemical composition is of interest especially in GC research. Since the morphology of the HB in GCs still remains unclear, different explanations for the shape of and the apparent gaps along the HB have been proposed. In GCs all stars belong to the same population and should therefore have similar primordial chemical compositions.

Glaspey et al. (1989) were the first to discover a significant change of chemical abundances as function of the position on the HB. While a BHB star with $T_{\text{eff}} \approx 10\,000$ K in NGC 6752 showed helium and iron abundances similar to the cluster composition (which is usually derived from abundance studies of red giants), a hotter one ($T_{\text{eff}} \approx 16\,000$ K) turned out to show depletion of helium and strong enrichment of iron. Further abundance studies of BHB stars in several GCs revealed a general pattern (Moehler et al. 1999; Behr et al. 2003a; Fabbian et al. 2005; Pace et al. 2006), which can also be observed in field BHB stars (Behr et al. 2003b; For & Sneden 2010). Stars cooler than about 11 500 K show the typical abundances of their parent population, while stars hotter than that are in general depleted in helium and strongly enriched in iron and other heavy elements like titanium or chromium. Lighter elements like magnesium and silicon on the other hand have normal abundances.

Diffusion processes in the stellar atmosphere are responsible for this effect. Michaud et al. (1989) predicted such abundance patterns even before the anomalies were observed. Caloi (1999) explained the sharp transition between the two abundance patterns as disappearance of subsurface convection layers at a critical temperature. Modelling BHB stars Sweigart (1997b) indeed found that thin convective layers below the surface driven by hydrogen ionisation should exist and move closer to the surface, as soon as the temperature increases. At about 12 000 K the convection zone reaches the surface and the outer layer of the star becomes fully radiative. Since convection is very efficient in mixing the envelope, diffusion processes cannot set in below this limit. In hotter stars with radiative atmospheres helium is expected to diffuse downward, since its mean molecular weight is higher than the one of hydrogen. Heavier elements on the other hand present sufficiently large cross sections to the outgoing radiation field and experience radiative accelerations greater than gravity. Hence these elements become enriched in the atmosphere. If the radiative acceleration almost equals gravity, the diffusion timescales get very long and the element is not significantly affected by diffusion. Michaud et al. (2008) modelled these effects and reproduced for the first time the observed abundance patterns of BHB stars.

Atmospheric diffusion processes have also been invoked to explain abundance peculiarities in a wide range of stars including white dwarfs, luminous blue variables, low mass halo stars, Ap and Am stars, and HgMn stars (see Vauclair & Vauclair 1982, for a review). For sdB stars the first theoretical diffusion models met with little success only (e.g. Michaud et al. 1983). Since then several attempts have been made to model the atmospheres of sdBs (Bergeron et al. 1988; Michaud et al. 1989; Fontaine & Chayer 1997; Ohl et al. 2000; Unglaub & Bues 2001). Radiative levitation and mass loss caused by stellar winds (Vink & Cassisi 2002) have been invoked to counteract the gravitational settling as well as extra mixing at the surface (Michaud et al. 2011; Hu et al. 2011).

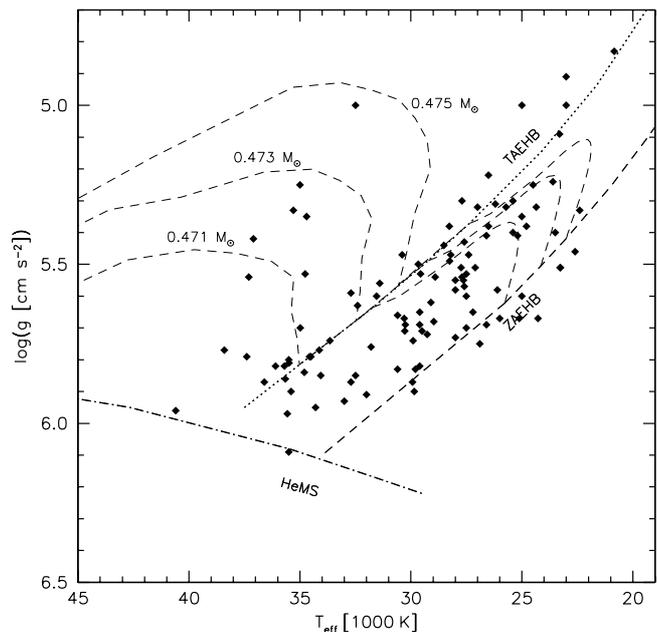


Fig. 1. Surface gravity is plotted against effective temperature. The diamonds mark the programme stars from our sample. Zero age extreme horizontal branch (ZAEHB) and terminal age extreme horizontal branch (TAEHB) are plotted as well as the helium main sequence (HeMS). Tracks for canonical EHB stars are taken from Dorman et al. (1993). The sample covers the whole parameter range on the EHB and also subdwarfs that already evolved away from the EHB.

Here we present a metal abundance analysis of 106 sdB stars, by far the largest sample to date. Previous papers of this series dealt with the rotational properties of sdB binaries (Geier et al. 2010, Paper I) and the rotational properties of single sdBs (Geier & Heber 2012, Paper II).

In Sect. 2 the dataset is described. Section 3 introduces the semi-automatic analysis pipeline used to measure elemental abundances. In Sect. 4 our results are compared with the literature and systematic uncertainties are discussed. The metal abundances, general trends as well as details for individual elements, are presented in Sect. 5. The abundance patterns of different sdB sub-populations (e.g. pulsators vs. non-pulsators) are discussed in Sects. 6–8, while Sect. 9 contains a comparison of our results with the abundance patterns on the BHB. State-of-the-art diffusion models are compared to our results in Sect. 10. Remaining abundance anomalies and peculiar shapes of metal lines are discussed in (Sect. 11). Finally, conclusions are drawn in Sect. 12.

2. Sample of sdBs with high resolution spectra

We selected a large sample of 106 sdB stars for which high resolution spectroscopy ($R = 20\,000$ – $48\,000$) suitable for the analysis of weak and sharp metal lines is available. Observations and data reduction are described in Lisker et al. (2005), Geier et al. (2012) and the Papers I and II of this series.

Our sample contains 38 radial velocity (RV) variable systems in close binary systems. The remaining 68 are apparently single stars. Eleven sdBs in our sample are known pulsators. Four of them belong to the class of short-period pulsators (V361 Hya, sdBV_r), seven are long-period pulsators (V1093 Her, sdBV_s). Our programme stars cover the entire parameter range in the $T_{\text{eff}} - \log g$ -diagram (see Fig. 1).

3. Semi-automatic abundance analysis

To derive the metal abundances we compared the observed spectra with synthetic line profiles. Metal line-blanketed LTE (local thermodynamic equilibrium) model atmospheres (Heber et al. 2000) were computed for the atmospheric parameters given in Lisker et al. (2005), Geier et al. (2012) and Papers I and II using the LINFOR Program (developed by Holweger, Steffen and Steenbock at Kiel university, modified by Lemke 1997).

A standard set of lines was chosen taking several criteria into account. First of all the lines had to be strong enough to be detectable in noisy spectra. Blends with lines of different ions were not used. Only line blends of the same ion could be handled because only one abundance was fitted to individual lines or multiplets. We selected a set of 182 metal lines from 24 different ions (see Table 1) and used atomic data from the lists of Kurucz (1992), Wiese et al. (1996), Ekberg (1993), and Hirata & Horaguchi (1995). For carbon, nitrogen, oxygen and silicon, the NIST database was used to obtain state-of-the-art atomic data.

A simultaneous fit of elemental abundance, projected rotational velocity ($v_{\text{rot}} \sin i$) and RV was then performed for each identified line using the FITSB2 routine (Napiwotzki et al. 2004). Inappropriate lines were neglected. This rejection procedure included several criteria. Equivalent width and depth of the fitted line was measured and compared to the noise level to distinguish between lines and noise features. The resulting individual RV had to be low, because all spectra were corrected to zero RV before. Otherwise the lines were considered as misidentifications or noise features. Then the fit quality given by the χ^2 had to be comparable to the average value to sort out lines contaminated by blends or artifacts caused by cosmic rays. Mean value and standard deviation were calculated from all abundance measurements of each ion. Because not all lines were present or suitable for fits in each star, the number of fitted lines differs. Upper limits were calculated by comparing the depth of the rotationally broadened synthetic spectral lines with the noise level. If only one line was found suitable for determining the abundance, the upper limits derived for the other lines of the same element where compared to this abundance. Only consistent results (within the error margins) were considered reliable, lowering the probability of misidentifications.

The accuracy of our results is limited by the quality of the spectra. Figure 2 shows two examples of spectra with highly different quality. The errors given in Table A.1 are the standard deviations of the individual line measurements. Numerical experiments were carried out to quantify the impact of noise on the result (see Paper I). We therefore regard 0.3 dex as typical statistical uncertainty of our abundance analysis. Some lines have peculiar profiles (see Sect. 11), which cannot be matched with the synthetic models. However, the equivalent widths are similar to the models and the abundance determination should therefore be correct to within ± 0.5 dex.

4. Comparison with literature and systematic uncertainties

Important sources of systematic errors are discussed in Przybilla et al. (2006) and references therein. Enhanced metal abundances can cause significant line blanketing (e.g. O'Toole & Heber 2006; Geier et al. 2007), which can affect the temperature-pressure stratification of the atmosphere and therefore the atmospheric parameter determination. However, these parameters are used to construct the model spectra for measuring the metal abundances. Some lines are much more sensitive to a change in

Table 1. Standard line list.

Ion	λ [Å]	Ion	λ [Å]	Ion	λ [Å]
Ne II	3694.212	V III	4274.417	S II	4815.552
Ne II	3713.080	Ti III	4281.555	Si III	4828.951
Si III	3796.124	S III	4284.979		4829.030
	3796.203	Fe III	4286.091		4829.111
Si III	3806.562		4286.128	Ar II	4879.863
	3806.700		4286.164	O II	4890.858
O II	3850.799	V III	4294.919	O II	4906.833
	3851.033	O II	4303.615	O II	4941.069
O II	3911.959		4303.833	O II	4943.003
	3912.107	Fe III	4304.748	N II	4994.353
C II	3920.681		4304.767		4994.360
O II	3945.038	O II	4342.009		4994.370
N II	3994.997	O II	4349.426	N II	5001.134
N II	4035.081	O II	4351.262	O II	5001.474
N II	4041.310	Fe III	4352.577	N II	5005.150
N II	4043.532	Fe III	4371.337	N II	5007.328
C III	4056.061	V III	4383.391	Sc III	5032.072
P III	4059.312	Ne II	4391.991	Fe III	5063.421
O II	4060.526	O II	4414.905	Si III	5091.250
Sc III	4061.210	O II	4416.974		5091.364
O II	4069.623	Fe III	4419.596		5091.455
	4069.886	Mg II	4481.126		5091.543
O II	4072.157		4481.325	Fe III	5127.387
P III	4080.089	O II	4452.375		5127.631
N II	4082.270	Al III	4528.945	C II	5132.947
Si IV	4088.862		4529.189		5133.281
O II	4097.258	N II	4530.410	C II	5143.495
Si IV	4116.104	Si III	4552.622	C II	5145.165
O II	4119.215	Si III	4567.840	C II	5151.085
Fe III	4122.780	Si III	4574.757	Fe III	5156.111
K II	4134.723	O II	4590.972	N II	5175.896
Fe III	4137.764	O II	4596.175	N II	5179.521
Fe III	4139.350	C II	4618.559	Fe III	5193.909
Al III	4149.913		4619.249	S II	5212.267
	4149.968	N II	4630.539		5212.620
	4150.173	N III	4634.126	Fe III	5235.658
C III	4162.877	N III	4640.644	Fe III	5276.476
Fe III	4164.731	O II	4641.810	Fe III	5282.297
	4164.916	C III	4647.418		5282.579
Fe III	4166.840	O II	4649.134	Fe III	5299.926
N II	4171.595	C III	4650.246	Fe III	5302.602
S II	4174.265		4651.016	S II	5320.723
N II	4176.195		4651.473	C II	5342.376
K II	4186.162	Si IV	4654.312	S II	5345.712
O II	4189.789	O II	4661.633		5346.084
N III	4195.760	O II	4676.235	Ti IV	5398.930
Ti III	4207.491	N II	4678.135	S II	5432.797
Ti III	4215.525	N II	4694.642	Ti IV	5492.512
Fe III	4222.271	O II	4699.003	N II	5535.346
Ca III	4233.713		4699.220	S II	5606.151
	4233.736	O II	4701.184	N II	5679.558
N II	4236.927		4701.708	N II	5686.213
	4237.047	O II	4703.163	N II	5710.766
Ca III	4240.742	O II	4705.352	Si III	5739.734
N II	4241.755	Si III	4716.654	Fe III	5833.938
	4241.786	Ar II	4735.906	N II	5893.147
S III	4253.589	C II	4737.966	N II	5931.782
K II	4263.447	C II	4744.766	N II	5941.654
C II	4267.001	C II	4747.279	Fe III	6032.604
	4267.261	Ar II	4806.021	N II	6167.755
V III	4268.183	Si III	4813.333		

the atmospheric parameters than others. Especially for the heavier elements there is a severe lack of adequate atomic data, which may introduce systematic shifts of the derived abundances.

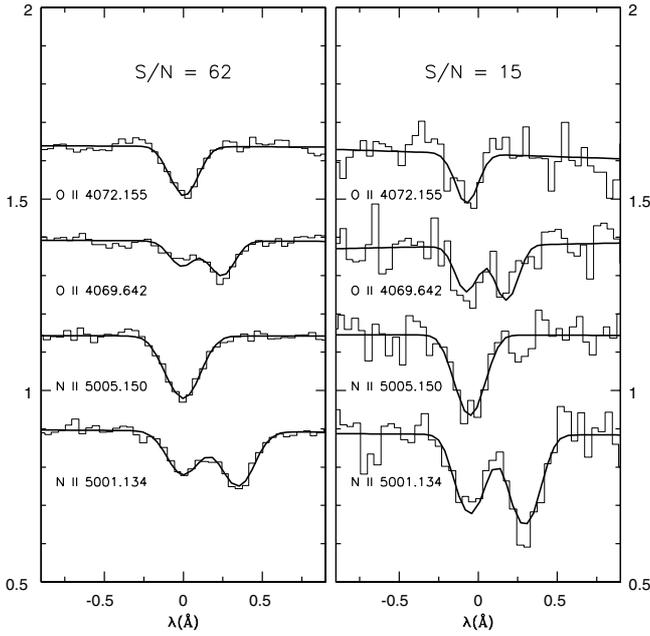


Fig. 2. Example fits of common oxygen and nitrogen lines for two spectra with different quality. Although the fit quality deteriorates, it is still possible to fit models with reasonable equivalent widths.

NLTE (non-local thermodynamic equilibrium) effects which are neglected in this analysis become important especially at higher temperatures. But not all lines are equally affected by NLTE effects. In detailed analyses of main sequence B stars, some lines were found to behave well in LTE, while others can deviate in abundance by orders of magnitude when NLTE effects are taken into account (Nieva & Przybilla 2008). Finally, microturbulence may lead to systematic trends in the abundances derived from single lines dependent on the line-strength. Due to the limited number of lines used in this study, it is not possible to measure this effect directly. However, more detailed analyses of a few stars in literature showed that in most cases microturbulence in sdB atmospheres is either negligible or small (e.g. Heber et al. 2000; Edelmann 2003; Przybilla et al. 2006).

To check whether the abundances determined with the pipeline approach are consistent with those derived by more detailed studies, we compared our results with independent determinations from literature. While we restrict ourselves to a limited set of pre-selected metal lines, other studies usually use all suitable lines in the spectra. The latter approach is more challenging and time consuming.

Metal abundances of HD 4539, PG 1710+490, PG 1627+027, PG 1716+426, PHL 457 and PG 0101+039 have been determined by Fontaine et al. (2006) and Blanchette et al. (2008) using FUV-spectra obtained with the FUSE satellite. O’Toole & Heber (2006) performed a detail analysis of UV-spectra obtained with the HST/STIS spectrograph for Feige 48, CD-24°731 and CPD-64°481. Optical high-resolution spectra were used to determine the abundances of PG 1101+249 (Feige 36, Edelmann et al. 1999), HE 1047-0436 (Napiwotzki et al. 2001), TONS 183 (Pereira & Jeffery 2008), KPD 2109+440, PG 1219+534 (Heber et al. 2000), HD 205805 and Feige 49 (Przybilla et al. 2006).

Figure 3 shows the differences of our abundances and the results from literature. Despite different wavelength ranges of the spectra, different atomic data and different methods to calculate the models (LTE or NLTE) the average scatter (± 0.2 dex) is consistent with our estimate of the statistical uncertainties. In

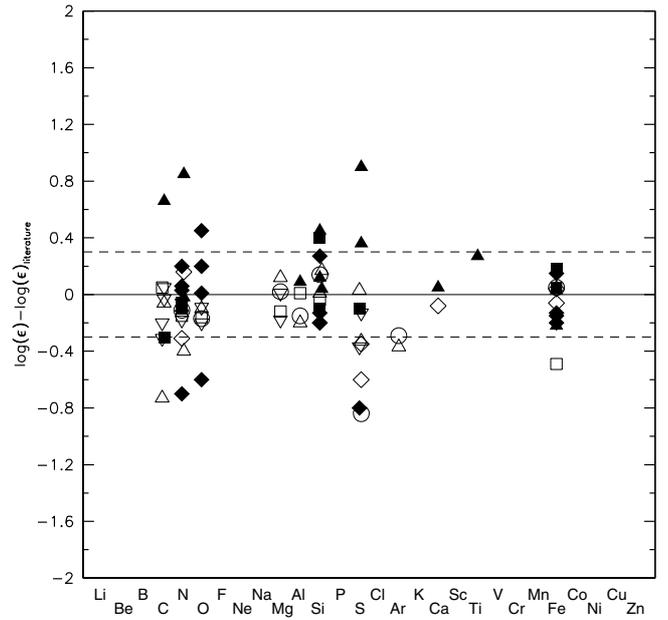


Fig. 3. Residuals between the metal abundances determined here and from literature are plotted against the chemical elements. Filled symbols mark results derived from UV-spectroscopy (squares, Fontaine et al. 2006; diamonds, Blanchette et al. 2008; triangles, O’Toole & Heber 2006), open symbols results derived from optical high-resolution spectra (circles, Edelmann et al. 1999; upward triangles, Napiwotzki et al. 2001; squares, Pereira & Jeffery 2008; diamonds, Heber et al. 2000; downward triangles, Przybilla et al. 2006). The dashed horizontal lines mark our statistical uncertainty estimate (± 0.3 dex).

conclusion, the metal abundances determined using the pipeline method are in general consistent with the ones determined by more detailed approaches.

However, in a few cases the differences between our results and the results from literature are more significant (>0.5 dex). The same holds for the ionisation equilibria of some elements, which are very sensitive to the atmospheric parameters, especially the effective temperature. In most cases such mismatches can be explained and a few of them are discussed now.

The abundances of C II and C III differ by more than 0.6 dex in some stars (CPD-64°481, HE 1047-0436) while the abundances of other elements in different ionisation stages are consistent within the error margins. Since the C II/C III abundances given in literature (Napiwotzki et al. 2001; O’Toole & Heber 2006) do not show such high deviations, we conclude that the limited number of lines used in our study leads to those systematic shifts. Especially the C II lines at 4267 Å are known to be very sensitive to NLTE effects (Nieva & Przybilla 2008). In a pilot study, Przybilla et al. (2006) derived the carbon abundance from the C II and C III lines of HD 205805 using LTE and NLTE models. The mismatch of 0.43 dex using the LTE approach consistent with our results could be significantly reduced to 0.17 dex using NLTE models. However, the similar difference between the abundances derived from C II and C III lines in the hotter sdB Feige 49, which is measured here as well, could not be reduced in this way.

The most significant differences in the carbon ionisation equilibrium are seen in HE 0101-2707 (0.9 dex) and HS 2033+0821 (1.2 dex), where the abundances derived from the C III lines are much higher than the ones derived from the C II lines. The most likely explanation for these mismatches are peculiarities in the line profiles discussed in Sect. 11.

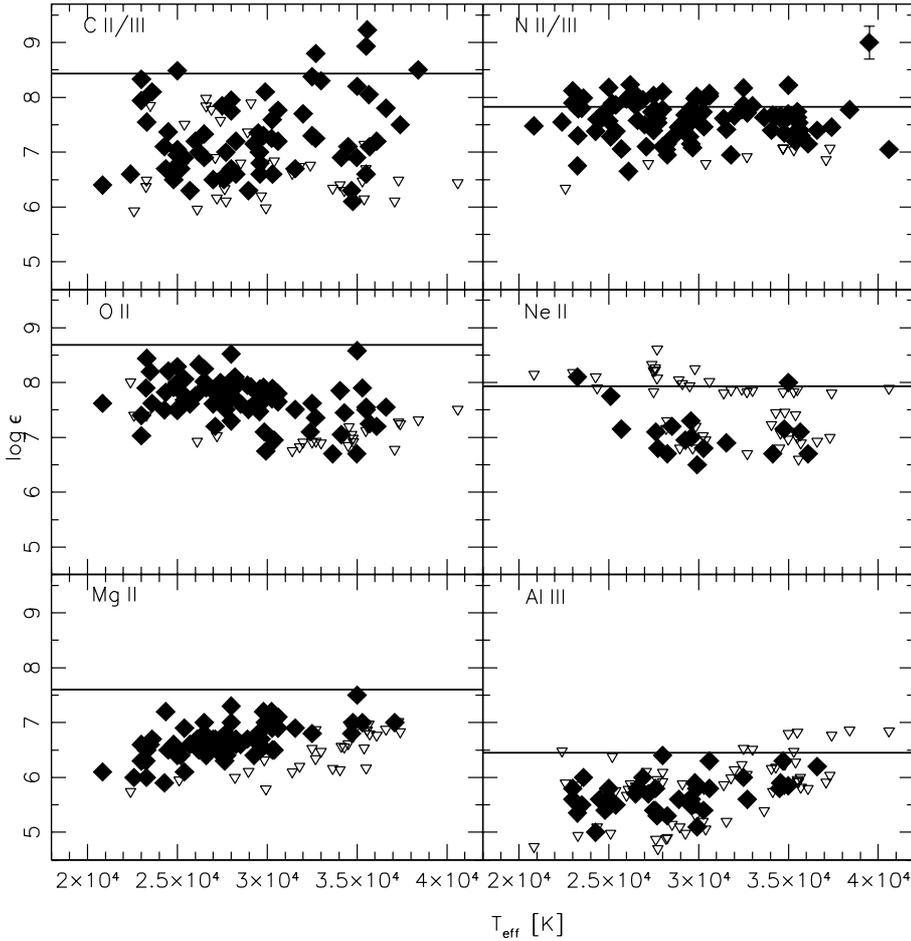


Fig. 4. Elemental abundances from carbon to aluminium plotted against effective temperature. If two ionisation stages are present, the average abundance is given. The filled diamonds mark measured abundances while the open triangles mark upper limits. Typical error bars are given in the upper right corner. The solid horizontal lines mark solar abundances (Asplund et al. 2009).

The abundances derived from N II/N III lines, Si III/Si IV lines and S II/S III lines agree within the given error margins for most stars where both ionisation stages are present. Although the abundances of Ti III and Ti IV agree within the given error margins in most stars, in some cases the difference can be as high as 1.4 dex. NLTE effects or insufficient atomic data are the most likely reasons for these discrepancies.

5. Metal abundances

Metal abundances of all stars are given in Table A.1 and are plotted against effective temperature in Figs. 4–6. Atmospheric parameters and helium abundances are published in Lisker et al. (2005), Geier et al. (2012) and Paper I, the projected rotational velocities in Papers I and II.

5.1. Carbon

The observed C abundances derived from C II/III lines scatter from -2.5 dex subsolar to solar (solar abundance 8.43 dex). Three sdBs with $T_{\text{eff}} > 32\,000$ K show supersolar abundances up to more than $+1.0$ dex.

5.2. Nitrogen and oxygen

The N II abundances (solar abundance 7.83 dex) range from -1.0 dex to $+0.5$ dex and do not show any trend with temperature. The O II abundances (solar abundance 8.69 dex) range from -2.0 dex to solar. At a temperature of $\approx 30\,000$ K the average abundance is shifted by -0.5 with respect to the cooler stars in the sample.

5.3. Neon and magnesium

The Ne II abundance scatters from -1.5 dex to $+0.1$ dex (solar abundance 7.93 dex). A slight trend can be seen with temperature in the magnesium abundance (solar abundance 7.60 dex), which ranges from -1.5 dex to -0.2 dex.

5.4. Aluminium and silicon

A slight trend with temperature is present in the Al III abundance (solar abundance 6.45 dex). Aluminium is enriched from -1.5 dex to 0.0 dex. The abundances from Si III as well as from Si IV (solar abundance 7.51 dex) show a large scatter between -2.0 dex and 0.0 dex w. r. t. solar. Subdwarfs with strong silicon lines are present in the same temperature range as sdBs where only low upper limits can be given. At temperatures higher than $\approx 35\,000$ K the mean silicon abundance drops by about -1.0 dex.

5.5. Phosphorus and sulfur

A trend with temperature is present in the P III abundance (solar abundance 5.41 dex). Phosphorus is enriched starting at a temperature of $T_{\text{eff}} > 28\,000$ K from -0.5 dex to $+1.0$ dex. The two stars HE 2307–0340 and HE 0539–4246 with temperatures of $\approx 23\,000$ K show lines at a wavelength of P III 4080.089 Å. Although no possible blends were found in line lists, these lines may be misidentifications since the derived abundances (5.90 dex) seem to be too high to fit in the overall trend. The S II and especially S III abundances (solar abundance 7.12 dex) scatter between -1.5 dex and $+1.0$ dex.

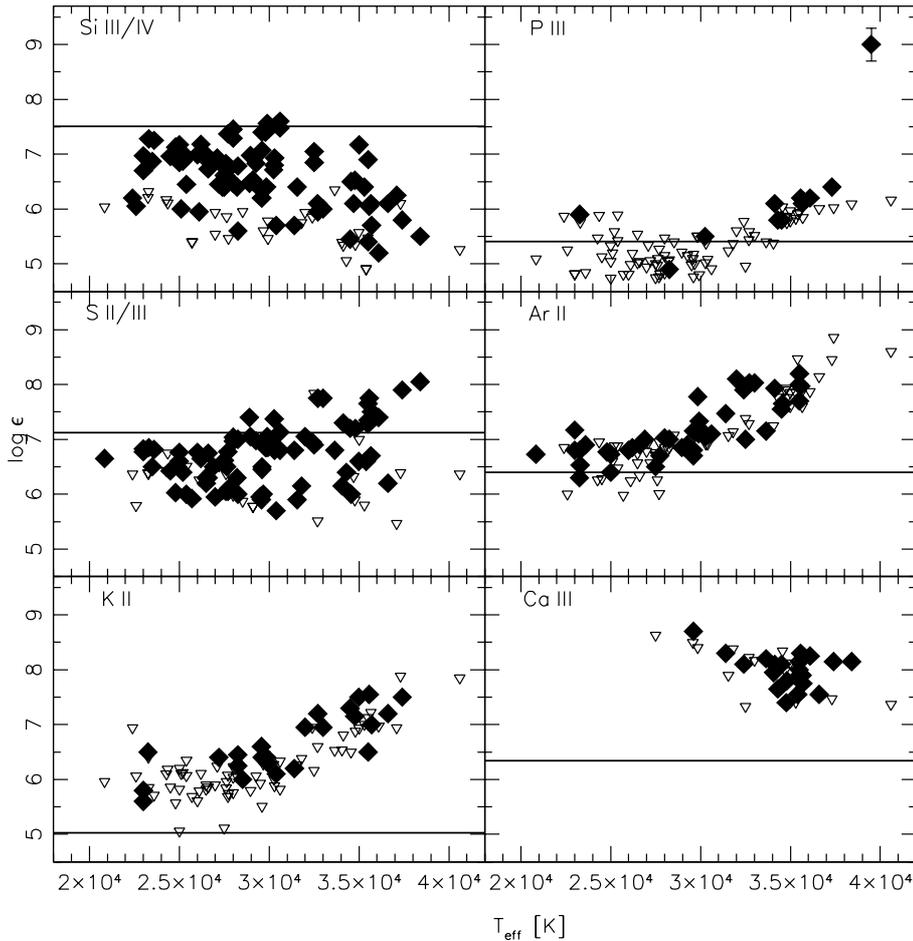


Fig. 5. Elemental abundances from silicon to calcium plotted against effective temperature (see Fig. 4).

5.6. Argon, potassium, and calcium

The Ar abundance increases with temperature from solar to +1.8 dex (solar abundance 6.40 dex). This trend has not been reported in prior analyses. Potassium has not been discovered in sdB atmospheres so far (solar abundance 5.03 dex). Similar to argon, the K abundance increases with temperature from +0.7 dex to +3.0 dex. Ca III (solar abundance 6.34 dex) is present at temperatures higher than $T_{\text{eff}} > 29\,000$ K. The abundances scatter from +1.0 dex to +2.5 dex. Ca II was not included in our analysis because the most prominent lines are usually blended with interstellar lines.

5.7. Scandium, titanium, vanadium and chromium

Sc III (solar abundance 3.15 dex) is strongly enriched and its abundance increases with temperature from +2.0 dex to +4.0 dex. Ti III (solar abundance 4.95 dex) is enriched and scatters from +1.0 dex to +3.0 dex. V III (solar abundance 3.93 dex) is highly enriched independent of the temperature ranging from +2.0 dex to almost +4.0 dex. The Cr III abundance (solar abundance 5.64 dex) increases with temperature from +0.0 dex to +2.0 dex.

5.8. Iron, cobalt and zinc

The Fe III abundance (solar abundance 7.50 dex) is constant ranging from -0.7 dex to $+0.5$ dex. For cobalt (solar abundance 4.99 dex) and zinc (solar abundance 4.56 dex) only upper limits could be given (zinc is not shown in Fig. 6 because upper limits could be derived from a single line only). These limits allow

high enrichments of these elements up to +2.0 dex, which is consistent with the results from UV-spectroscopy (O'Toole & Heber 2006; Chayer et al. 2006; Blanchette et al. 2008).

6. Abundance patterns of sdB sub-populations

Besides apparently single sdB stars our sample contains several pulsating sdBs and RV-variable systems in close binaries. These stars may have formed differently or – in the case of the pulsating sdBs – may be in a distinct evolutionary phase. It is instructive to compare the metal abundance patterns of these sub-populations and search for differences, which may help to clarify these issues.

Our sample contains 38 RV-variable sdBs in single-lined, close spectroscopic binary systems. Aznar Cuadrado & Jeffery (2002) argued that the helium content in such close binary sdBs may be higher than in single stars, because tidal effects might lead to mixing in the stellar atmosphere. According to this scenario, the metal abundances should be affected as well. However, we showed that the helium content in sdB atmospheres is not affected in this way (Geier et al. 2012).

There is also no significant difference between the metal abundance patterns of sdBs in close binaries and apparently single stars. In conclusion, moderate tidal influence of close companions does not change the abundances in sdB atmospheres. In the most extreme cases, where the sdB has been spun up to very high rotational velocities of the order of 100 km s^{-1} (e.g. KPD 1930+2752, Geier et al. 2007; EC 22081–1916, Geier et al. 2011a), it was not yet possible to determine the metal abundances, because the broadening of the spectral lines is too strong. Such objects may still show peculiar abundance patterns.

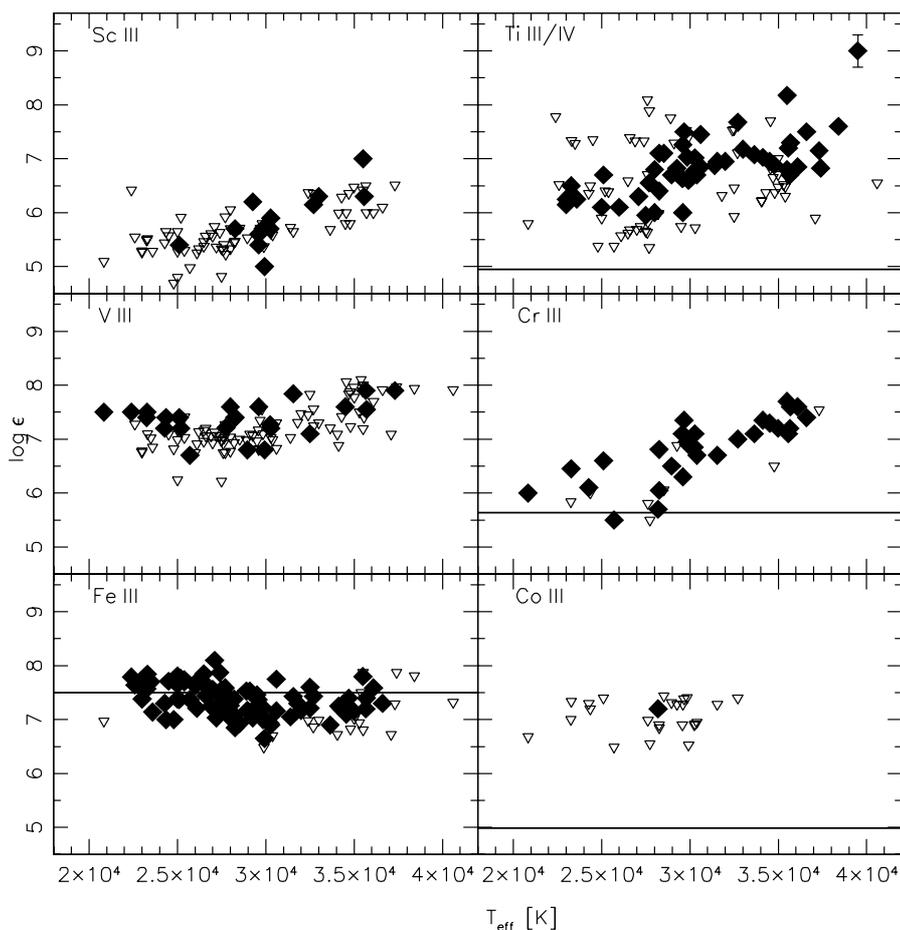


Fig. 6. Elemental abundances from scandium to cobalt plotted against effective temperature (see Fig. 4). In the case of scandium and vanadium the solar abundances are lower than 4.5 dex (see text).

Since the driving mechanism of pulsations in sdB stars is thought to be an enrichment of iron in the outer layers of the star (Charpinet et al. 1997), the metal abundances of pulsating sdBs have been determined to search for peculiarities. However, the abundance patterns of pulsating sdBs turned out to be the same as the ones of non-pulsating comparison stars with similar atmospheric parameters (Heber et al. 2000; O’Toole & Heber 2006; Blanchette et al. 2008).

Our sample includes the short-period pulsators Feige 48 (Koen et al. 1998), KPD 2109+440 (Billères et al. 1998), PG 1219+534 (O’Donoghue et al. 1999) and HE 0230–4323 (Kilkenny et al. 2010) as well as the long-period pulsators PG 1627+017 (Green et al. 2003), LB 1516 (Koen et al. 2010), JL 82 (Koen 2009), PHL 44 (Kilkenny et al. 2007), PHL 457 (Blanchette et al. 2008), PG 1716+426 (Green et al. 2003) and PG 0101+039 (Randall et al. 2005). Consistent with the results of Heber et al. (2000), O’Toole & Heber (2006) and Blanchette et al. (2008) no differences have been found in the metal abundance patterns of these stars with respect to the rest of the sample.

7. Helium and metal abundances

Edelmann et al. (2003) discovered a correlation between the effective temperatures of sdB stars and their helium abundances. Hotter sdB stars tend to show higher enrichments of helium in some cases reaching or even exceeding the solar abundance. However, the scatter in helium abundance is high and two distinct sequences appear in the $T_{\text{eff}} - \log y$ -diagram. These results have been confirmed by Geier et al. (2012). About 75% of the field sdB population belongs to the upper sequence, while $\approx 25\%$ form the lower sequence, which is offset by about 2 dex.

It is instructive to compare the metal abundances of sdBs belonging to the two helium sequences (see Fig. 7). Most species are not significantly affected by the difference in helium abundance. For nitrogen, oxygen, iron and all other metals not shown in Fig. 7 there are no obvious differences between the two subsamples. The silicon abundances of the helium-poor stars seem to be somewhat lower than for the helium-rich ones. However, this impression is most likely created by the different sizes of the samples.

In contrast, significant differences are visible for the carbon and sulfur abundances. All sdBs on the lower helium sequence have carbon abundances of -1.0 or less with respect to the solar value, while the stars with more helium show a large scatter in carbon abundance up to supersolar values. The sulfur abundances behave in a similar way. While the helium-poor sample shows subsolar abundances, sulfur can be enriched to supersolar values in the helium-rich sample.

8. Other trends

It has been noted by several authors (e.g. Lamontagne et al. 1985, 1987; O’Toole & Heber 2006) that the silicon abundance in sdB stars appears to drop sharply at $T_{\text{eff}} > 32\,000$ K. Fractionated winds have been invoked to explain this strange observation (Ungraub 2008). The aluminium abundance were proposed to behave in a similar way. As can be clearly seen in Figs. 4 and 5, this assumption has to be dropped. Silicon as well as aluminium are present all over the temperature range of sdBs.

O’Toole & Heber (2006) also reported a possible anti-correlation between iron and the other heavy elements. In our sample no such trend is visible for the Ti and Ca abundances.

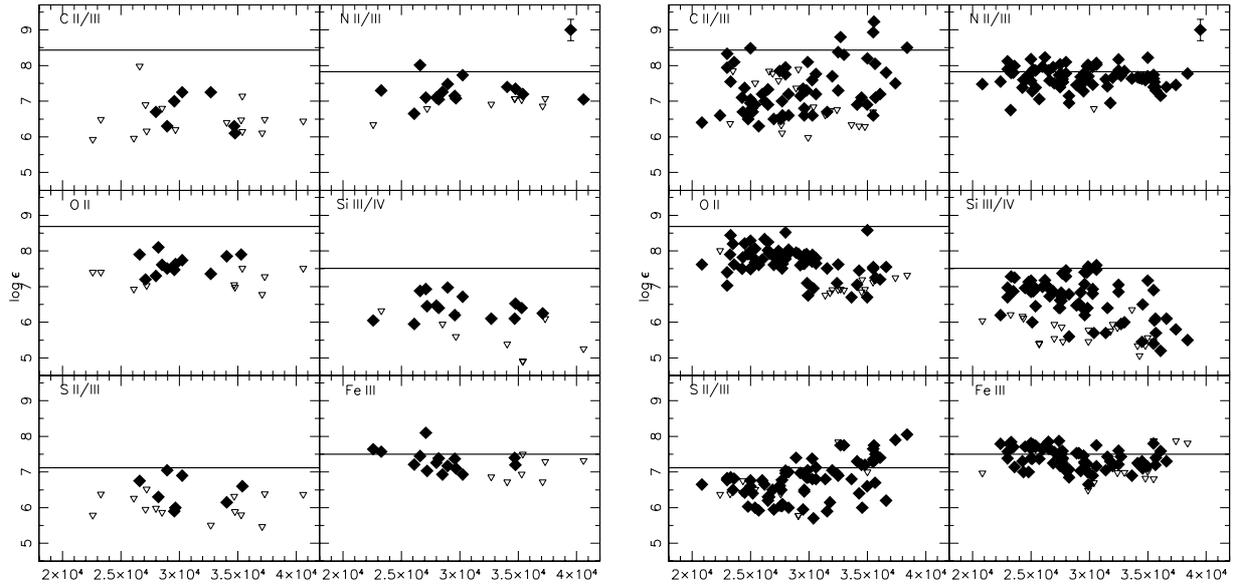


Fig. 7. Abundances of selected elements plotted against effective temperature (see Fig. 4). *Left panel:* only sdBs belonging to the lower He-sequence are plotted. *Right panel:* only sdBs belonging to the upper He-sequence are plotted.

Looking at high resolution spectra of a sample of sdBs it is striking that most of them show a lot of metal lines, while some don't show any metal lines at all. At first instance one could argue, that there exist two different populations of sdBs with different metallicities. Heber & Edlmann (2004) discovered three hot sdBs showing lots of metal lines (e.g. PG 0909+276). They were subsequently named “super-metal-rich” sdBs because their metal abundances seemed to be exceptionally high.

Our results provide a natural explanation for this effect, since such an enrichment is found to be quite normal for sdBs in the high temperature range. All stars with no metal lines are lying at the hot end of the EHB with temperatures higher than $T_{\text{eff}} > 33\,000$ K. Although they show no lines, the derived upper limits are consistent with the abundance measurements of hot sdBs with metal lines. At these temperatures the optical lines are becoming so weak that they are only observable in high signal to noise ratio (S/N) spectra. The effect can be seen in Fig. 4, where the oxygen and magnesium abundance measurements partly turn into upper limit estimates at high temperatures. Spectra of slightly poorer quality appear to be metal free, but they are not. This selection effect illustrates the limitation of optical spectroscopy for metal abundance analyses in hot stars. Therefore UV spectra are needed to study the strong metal lines of higher ionisation stages in hotter sdO/B or sdO stars.

9. Extreme horizontal branch versus blue horizontal branch

Quantitative spectral analyses of BHB stars have been published by Behr et al. (2003a,b), Fabbian et al. (2005) and Pace et al. (2006) and it is worthwhile to compare them to our results for EHB stars. In Fig. 8 the abundances of iron and titanium are plotted against effective temperature. Abundances of all BHB stars are plotted together, although they are derived from stars coming from very different populations. Eight different GCs as well as field stars are put together here¹. At first glance this makes

¹ The gap in temperature between the BHB and EHB stars is a known, but yet unexplained feature, which is also observed in two-colour diagrams of field blue halo stars and GCs (Newell 1973; Geier et al. 2011b, and references therein).

absolutely no sense, because stars from different chemical environments should have different abundances. This would result in a scattered plot from which no relevant information could be derived.

However, Fig. 8 proves that this is not the case. Although there is a high scatter in the iron abundance at low temperatures, all stars hotter than about 11 500 K end up at almost solar abundance with a significantly lower scatter (Fig. 8, upper panel). As soon as diffusion sets in, the atmospheres of stars from different populations become similar regardless of the primordial abundances. The distribution of sdBs now shows that the iron abundance remains indeed saturated at this value up to temperatures of 40 000 K. This plot clearly illustrates that the abundance of iron in EHB and the hottest BHB stars is not “solar” for reasons of star formation and stellar evolution. This abundance reflects the surface concentration of iron caused by an interplay of gravitational settling and radiative levitation, which becomes saturated in stars hotter than 11 500 K, and is just by chance “solar”. This result is in perfect agreement with diffusion models (Michaud et al. 2008, 2011).

A similar behaviour is predicted by Michaud et al. (2008) for the titanium abundance. In BHB stars only a rise of the titanium abundance can be observed, which is more continuous than in the case of iron. Adding the sdBs one can see that the abundance becomes saturated at an effective temperature of about 30 000 K and an abundance of roughly 100 times solar (Fig. 8, lower panel). This behaviour proves in a most convincing way, that heavy elements in EHB and hot BHB stars are enriched by radiative levitation.

10. Diffusion at work along the horizontal branch

The metal abundances of the sdBs in our sample show a pattern, which could not be seen that clearly before. While the light elements carbon, nitrogen, oxygen and neon are not affected by higher temperatures, most heavier elements from aluminium to chromium become enriched in hotter atmospheres, the high scatters in the silicon and sulfur abundance being interesting exceptions. Iron, on the other hand, becomes saturated at solar abundance in HB star atmospheres as soon as the effective

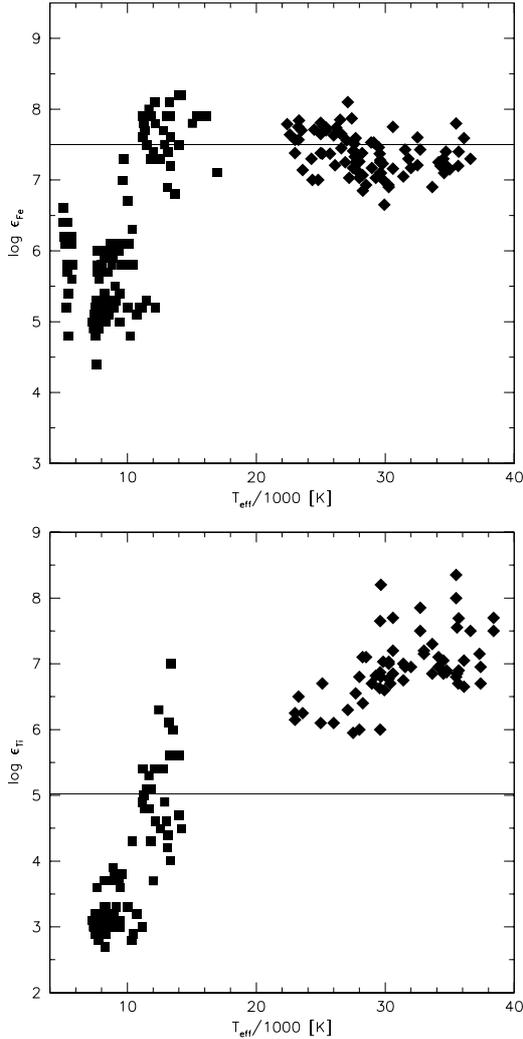


Fig. 8. *Left panel:* iron abundance is plotted against effective temperature. The filled diamonds mark the results from the sdBs. The filled rectangles mark the combined results for BHB stars from seven GCs and the field (Behr et al. 2003a,b; Fabbian et al. 2005). *Right panel:* titanium abundance is plotted against effective temperature. The filled diamonds mark the results from the sdBs. The filled rectangles mark the combined results for BHB stars from eight GCs and the field (Behr et al. 2003a,b; Fabbian et al. 2005; Pace et al. 2006).

temperature exceeds 11 500 K. Consistent with that the hotter sdB stars all have “solar” iron abundances.

These results are in reasonable agreement with theoretical calculations performed by Michaud et al. (2008, 2011). The authors calculated full evolutionary models, including the effects of diffusion and radiative acceleration for different primordial metallicities. The evolution on the HB was followed for the first 32 Myr, which is about one third of the typical lifetime of core helium-burning stars. Their calculations of the abundance anomalies only depend on the mass mixed by turbulence at the surface. Other effects like mass-loss via stellar winds have not been taken into account. Michaud et al. (2011) used the observed iron abundances in sdB stars mostly taken from a preliminary version of the dataset presented here to fix the mixed surface mass to $\approx 10^{-7} M_{\odot}$.

The time evolution of the surface abundances was then calculated for the elements C, N, O, Ne, Mg, Al, Si, P, S, Ar, K, Ca, Ti, Cr and Fe. To compare our measurements with these curves, we can restrict ourselves to models with solar metallicity on the

main sequence (Michaud et al. 2011). Since the sdBs in our sample are rather bright field stars, we can assume that most of them originate from the Galactic thin disc with only minor contributions from the thick disc or the halo (e.g. Altmann & de Boer 2000).

In general, the models of Michaud et al. (2011) match the observations quite well. The predicted enrichments or depletions are mostly of the same order as the observations. This is the first time that the complete abundance patterns of sdB stars could be modelled in a quantitative way. However, the models do neither predict the highly supersolar enrichments of C, S, P, K and Ar with temperature nor the large scatter in the C, Si and S abundances.

Both the high enrichments and the large scatter of certain abundances may partly be caused by age effects. Michaud et al. (2011) pointed out that their evolutionary calculations only cover a part of the lifetime on the EHB. There are no clear correlations between the metal abundances and the ages of the stars derived from their position in the $T_{\text{eff}} - \log g$ -diagram. However, such a trend may be washed out by the uncertainties in the atmospheric parameters and the abundances. Furthermore, mass loss via stellar winds, which was not accounted for, might play a role as well (e.g. Unglaub 2008, and references therein). However, a closer inspection of the data makes an alternative explanation more likely.

11. Peculiar line profiles and stratification

While the enrichments of P, K, Ar (and maybe also S at the hot end) follow a general trend with temperature, which seems to be an indicator of radiative levitation, the supersolar enrichment of some stars in C is hard to explain in this framework, because the other light elements N, O, Ne and Al are depleted with respect to their solar abundances.

Since carbon enrichment is also common in the helium-rich sdBs (Ahmad & Jeffery 2003; Naslim et al. 2010) and sdOs (Ströer et al. 2007; Hirsch & Heber 2009) and the helium abundances of hot sdBs with carbon enrichment are among the highest in our sample, a connection seems to be likely. Alternative formation scenarios like the late hot flasher (Sweigart 1997b; Lanz et al. 2004) do indeed predict an enrichment of helium and carbon.

In the case of helium enrichment prior to the subdwarf stage Groth et al. (1985) predict a broad subsurface convection zone, which should be able to mix nuclear processed material in the atmosphere and therefore counteract gravitational settling. Of course, this mechanism would have to ensure the enrichment of He and C without destroying the general abundance pattern caused by diffusion, which might require some finetuning. Diffusion might also lead to a slow transformation of He-rich subdwarfs into He-deficient ones (Miller Bertolami et al. 2008). The discovery of sdBs with intermediate He abundances right in between the normal sdBs and the He-rich ones may be consistent with such a scenario (Ahmad et al. 2007; Naslim et al. 2011; Naslim et al. 2012).

However, we found observational evidence that yet another unaccounted effect may be responsible for the most extreme chemical peculiarities in sdB atmospheres. Looking at the spectra of our sample in detail, the shape of the strongest metal lines in some stars (CPD-64°481, EC 03591-3232, EC 05479-5818, Feige 38, HD 205805, HE 0101-2707, PG 0133+144, PG 1303+097, PG 1710+490, PG 1743+477) was found to be peculiar (see Fig. 9). The lines are too sharp to be fitted with synthetic models even if the rotational broadening is set to zero.

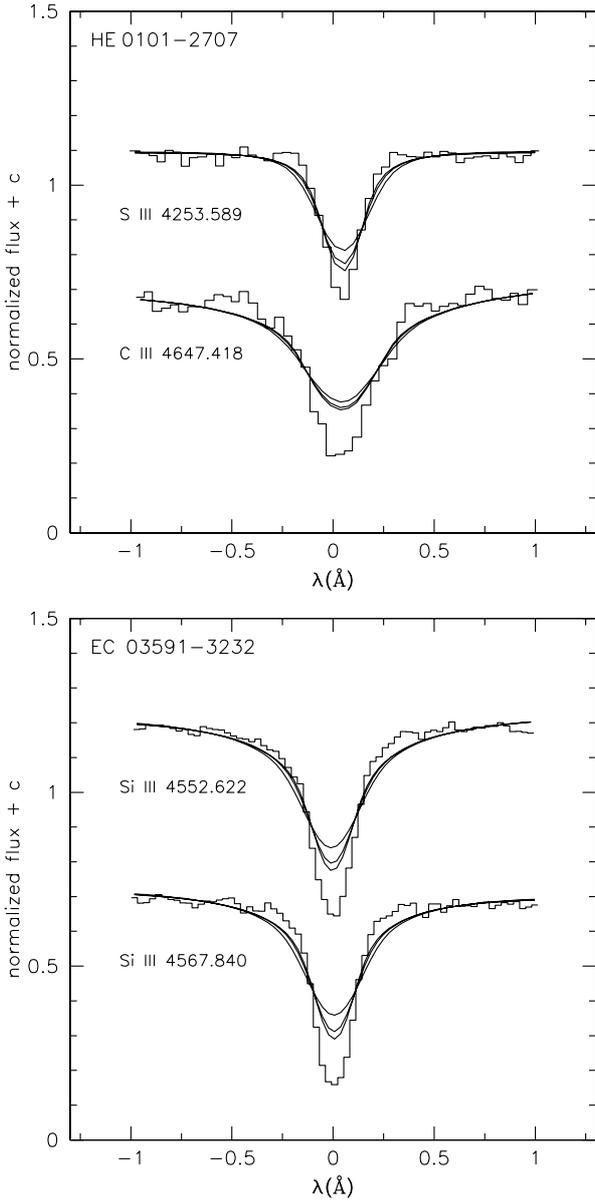


Fig. 9. *Upper panel:* fits of models with different rotational broadening (solid lines, 0, 5, 10 km s⁻¹ respectively) to an S III and a C III line (solid histograms) of HE 0101–2707. *Lower panel:* similar fits of models to Si III-lines of EC 03591–3232. It can be clearly seen that the synthetic line profiles do not match the observed ones at all. Examples for normal fits to metal lines are given in Fig. 2.

Especially the line wings are much too weak with respect to the depths of the cores. NLTE effects cannot cause such line shapes and the weaker metal lines don't show similar profiles.

Using five spectra of Feige 38 taken within a timespan of 1.8 yr we checked whether the shape of the peculiar lines changes. The lines do not show any significant differences in depth and shape. Time dependent effects like star spots can therefore be excluded.

The most significant peculiarities are seen in the strongest Si III lines of EC 03591–3232 (see Fig. 9, lower panel), PG 0133+114, Feige 38 and PG 1710+490. Most remarkably all of these stars belong to the rare class of sdBs that also show an enrichment in ³He (Geier et al. 2012).

Michaud et al. (2011) pointed out that additional element separation may occur in the stellar atmosphere between the bottom of the mixed mass ($\approx 10^{-7} M_{\odot}$) and the surface. Such effects

are not included in their models. The ³He anomaly observed in sdB stars with temperatures around 30 000 K is not predicted by the model of Michaud et al. (2011) either and should therefore not be present in the mixed zone. Nevertheless, it is clear that the settling of almost all ⁴He must be caused by diffusion, which can then only happen in the outermost atmosphere.

Diffusion in the photosphere should lead to vertical stratification of the metal abundances. Observational evidence for such a stratification of Fe in the atmospheres of BHB stars has been found (Khalack et al. 2007, 2010; LeBlanc et al. 2009, 2010). How is the shape of the spectral lines affected by vertical stratification? If radiative levitation leads to an abundance gradient in the atmosphere, the wings of a spectral line should become weaker, because of less absorption at the bottom of the atmosphere. This not only explains the peculiar shape of the lines, but also the fact that the weak lines are not affected. Those lines originate from deeper layers, where the gradient is less pronounced. Together with the ³He anomaly the peculiar line shapes provide evidence for diffusion processes above the mixed zone in the atmospheres of sdBs.

Such effects may also provide a reasonable explanation for the high scatter of the C, Si and S abundances as well as mismatches in the ionisation equilibria (see Sect. 4), since peculiar line shapes have also been found for strong C III and S III lines in the spectra of hot sdBs (e.g. HE 0101–2707, see Fig. 9). Given that these peculiarities are only detectable in the most extreme cases or in data of high quality, stratification may be rather common in sdB atmospheres. It is therefore possible that the highest enrichments not predicted by the models of Michaud et al. (2011) are caused by radiative levitation in the stellar atmosphere rather than the mixed zone beneath. Of course, this hypothesis needs to be tested further.

12. Conclusion

A combination of diffusion both in a mixed zone close to the surface and in the stellar atmosphere on top of it seem to be sufficient to explain most of the results presented here. However, different formation scenarios, which lead to different amounts of helium in the atmosphere may still leave some imprint on the final abundance patterns. The connection between sdBs with hydrogen-rich atmospheres, He-sdBs and intermediate objects remains as unclear as the reason for the differences in the abundance patterns of the two distinct helium populations (see Sect. 7). Our lack of understanding the details of diffusion in sdBs is very well illustrated by the extremely peculiar intermediate He-sdB LS IV–14°116, whose atmosphere is highly enriched in strontium, yttrium and zirconium (Naslim et al. 2011). The reason for this is unclear and the very well detected spectral lines of these elements are not present in any of the sdBs of our sample.

Furthermore, as pointed out by Hu et al. (2011), the physical mechanism necessary to mix the surface in the way needed to reproduce the observed abundances is still unknown. Mass loss through stellar winds may play a role, but Hu et al. (2011) also showed that the mass loss rates must be lower than $\approx 10^{-15} M_{\odot} \text{ yr}^{-1}$ to allow sdBs to pulsate. Since the abundance patterns of sdB pulsators do not differ from the ones of stable sdBs, one would expect similar mass loss rates. But even very weak and fractionated winds might affect the atmospheric abundances (Ungraub 2008).

Although in most cases unstratified photospheres reproduce the observed line profiles well, the discovery of spectral lines with peculiar shapes possibly caused by vertical stratification might pose a new challenge for atmospheric models of sdB stars.

Besides NLTE effects (Przybilla et al. 2006) and enhanced line blanketing by metals enriched due to diffusion (O'Toole & Heber 2006), next generation models might have to take vertical stratification into account. Especially the strong resonance lines in the UV should be affected and due to crowding and blending in this region such effects might not be obvious.

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