Scattering of small bodies by planets: a potential origin for exozodiacal dust?

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Received 12 July 2012 / Accepted 20 September 2012

ABSTRACT

High levels of exozodiacal dust are observed around a growing number of main sequence stars. The origin of such dust is not clear, given that it has a short lifetime against both collisions and radiative forces. Even a collisional cascade with km-sized parent bodies, as suggested to explain outer debris discs, cannot survive sufficiently long. In this work we investigate whether the observed exozodiacal dust could originate from an outer planetesimal belt. We investigate the scattering processes in stable planetary systems to determine whether sufficient material could be scattered inwards in order to retain the exozodiacal dust at its currently observed levels. We use N-body simulations to investigate the efficiency of this scattering and its dependence on the architecture of the planetary system. The results of these simulations can be used to assess the ability of hypothetical chains of planets to produce exozodi in observed systems. We find that for older (>100 Myr) stars with exozodiacal dust, a massive, large radii (>20 AU) outer belt and a chain of tightly packed, low-mass planets would be required to retain the dust at its currently observed levels. This brings into question how many, if any, real systems possess such a contrived architecture and are therefore capable of scattering at sufficiently high rates to retain exozodi dust on long timescales.

Key words. methods: numerical – comets: general – planets and satellites: dynamical evolution and stability – zodiacal dust – planet-disk interactions – circumstellar matter

1. Introduction

Excess emission in the far-infrared or sub-mm, associated with cold, dusty debris discs is regularly observed around hundreds of main sequence stars (see Wyatt 2008 for a review). There are now a growing number of stars with similar emission, but in the mid-infrared from material at higher temperatures. These observations have been associated with dust very close to the star, reminiscent of the solar system’s exozodiacal cloud. There are now several dozen such sources discovered either using near or mid-infrared, interferometric observations with, for example, FLUOR/CHARA (e.g. Absil et al. 2006, 2008), IONIC/IOTA (e.g. Delfrère et al. 2011), MIDI/VISIR (e.g. Smith et al. 2009b), or using their mid-infrared spectra with Spitzer (Olofsson et al. 2012; Lisse et al. 2012, 2009). Such sources have been compared to the solar system’s exozodiacal cloud, but in general are several orders of magnitude brighter, for example η Corvi is 1250 ± 260 times brighter than the solar system’s exozodiacal dust cloud at 10 μm (Millan-Gabet et al. 2011). These observations can be modelled to determine estimates on the geometry, mass, position and grain properties. A well studied example is the 450 Myr old A-star Vega (Absil et al. 2006, 2008; Delfrère et al. 2011), where the best fit model found using Bayesian statistics to assess a grid of models, suggests that the emission is dominated by small grains (<1 μm) in a 10^{-9} M_⊕ ring between ~0.1–0.3 AU (Delfrère et al. 2011). More detailed compositional information can be determined for the handful of brighter sources detected by their Spitzer spectra in the mid-infrared, for example Olofsson et al. (2012); Lisse et al. (2012), amongst others.

Once the potential alternative of a stellar companion is ruled out for the interferometric observations, the only explanation for this excess emission is emission from high levels of small dust grains. Such small grains, however, have a short lifetime, both against collisional processes (years) and radiative forces (years). If the observed discs are to survive for longer than year timescales, the small grains must be replenished. In outer debris discs, the observed small grains are thought to be continuously replenished in a steady-state collisional cascade from a population of unseen, large parent bodies. However, models for such collisional evolution (e.g. Wyatt & Dent 2002; Wyatt et al. 1999, 2007b; Stark & Kuchner 2009; Krivov et al. 2008; Löhne et al. 2008, amongst others), find that close to the star, the planetesimal belt required to supply the observed levels of small dust must be so dense that even kilometer sized parent bodies are rapidly destroyed by collisions (Wyatt et al. 2007a). Thus, it is not possible for the observed small grains to be replenished by an insitu steady-state collisional cascade on long timescales (hundreds of years at 1 AU). The suggestion has been made that the dust could be resupplied in a steady state collisional cascade if the population of bodies were on highly eccentric (e > 0.99) orbits (Wyatt et al. 2010). The origin of such a configuration is, however, difficult to conceive. Therefore, in general another explanation for the origin of the observed small dust is required, in particular for the older systems with exozodi.

Many suggestions have been made in the literature to explain these exozodi. The young systems (∼10–20 Myr) with hot dust are easier to explain and it seems probable that we are witnessing increased collision rates due to terrestrial planet formation (Smith et al. 2009a, 2012; Kenyon & Bromley 2004), whereas
for the older systems, the observations are more puzzling. An obvious origin for the material is further out in the planetary system where it can survive on longer timescales (e.g. Smith et al. 2009b; Lisse et al. 2012; Absil et al. 2006). With the growing number of detections of planets and/or planetesimal belts, it seems that outer planetary systems are common. In fact some of the observed exozodis also have detections for outer planetesimal belts (e.g. Fomalhaut Absil et al. 2009; Acke et al. 2012, η Corvi Smith et al. 2009b; Wyatt et al. 2005, amongst many others). It remains, however, to be determined how this material is transported inwards and whether we are observing a transient or steady-state phenomena.

Recent dynamical modelling of our solar system’s exozodiacal dust cloud found good evidence that much of the observed dust originates from Jupiter Family Comets, scattered inwards from the Kuiper belt. Once inside Jupiter’s orbit the dust’s evolution is dominated by radiative forces, Poynting-Robertson-drag from the Kuiper belt. Once inside Jupiter’s orbit the dust’s evolution is dominated by radiative forces, Poynting-Robertson-drag is most influential in low luminosity systems, for example, it has been suggested to model observations of warm dust around Epsilon Eridani (Reidemeister et al. 2011). Scattering can occur both in a stable planetary system, such as the Jupiter Family Comets in our solar system, and at increased rates after a dynamical instability, such as the solar system’s Late Heavy Bombardment. Evidence that we may be observing the aftermath of a collision between two large bodies exists from the presence of impact processed silica in the spectra of the hot dust (Lisse et al. 2012, 2009). Models of collisions between large bodies, such as the earth-moon forming collision, show that high levels of dust are produced (Jackson & Wyatt 2012). Such collisions are by nature rare, in particular their probability decreases with the system age and thus, their probability must be compared to the growing numbers of systems with exozodiacal dust, in particular, the number of old (greater than Gyr) systems (e.g. τ Ceti, di Folco et al. 2007).

In this work we investigate whether sufficient material can be scattered inwards from an outer planetesimal belt, in a stable planetary system, to resupply an exozodi, or whether it is necessary to invoke further explanations. We consider the simple scenario where there are (several) planet(s) interior to an outer planetesimal belt and use N-body simulations to determine how efficiently they scatter material inwards from the outer belt. To assess the feasibility of this scenario, these efficiencies must be compared with observations of inner and outer belts. We start by discussing the details of our simulations in Sect. 2. Section 3 presents the illustrative example of single planet systems, which is expanded upon in Sect. 4 with simulations to determine the scattering efficiencies in multi-planet systems. The implications of our results and their limitations are then discussed in Sect. 5, before conclusions are formed in Sect. 6.

2. Our simulations

The main purpose of this work is to investigate the rates at which material can be scattered from an outer planetesimal belt into the inner planetary system, with the view that it could contribute to the observed exozodiacal dust. This is necessarily dependant on the architecture of the planetary system; that is the orbits and masses of the planets, and the radial location and masses of the planetesimal belt and exozodi. We aim to constrain the planetary system architecture required in order to scatter material inwards at sufficient rates to produce the observed exozodiacal dust. We anticipate a high dependence of the scattering rates on the system architecture, thus, we hypothesis that the diversity of observed systems could potentially be explained by a diversity of planetary system architectures. For simplicity, we limit ourselves in this work to the scenario of an outer planetesimal belt.

In order to assess the validity of this hypothesis, we use N-body simulations to determine the efficiency of scattering in planetary systems of different architectures. Given the huge diversity of planetary systems found by current observations, it is necessary to limit our parameter exploration to a tiny region of the available parameter space, which is chosen such that the simulations can be used to make further deductions regarding the remaining parameter space. Our simulations determine the rate at which material is scattered inwards as a function of the total mass of material in the outer belt, that is the total mass in all bodies between small μm grains and km-sized bodies. The mass of the outer planetesimal belt can be determined, albeit in a model dependent manner, from observations of outer debris discs. For systems where an outer belt is not detected, this merely places an upper limit on the mass that could be hidden in an outer belt in this system. Using these masses it is possible to assess whether this hypothesis can be applied to real planetary systems with both outer planetesimal belts and exozodi. This requires a knowledge of the rate at which material needs to be supplied in order to sustain the observed levels of exozodiacal dust.

Observations of exozodiacal dust can be used, again in a model dependent manner, to determine a mass for the observed dust. It is clear that the observed dust is so small (μm) that it has a short lifetime, either against collisions or radiative forces, although the exact lifetime is difficult to calculate. Multiple epoch observations, separated by longer than the lifetime of the small dust, of a handful of systems (e.g. Ciardi et al. 2001; Absil et al. 2006, 2008; Defrère et al. 2011), do not find significant variation in the observed fluxes. Therefore, it seems reasonable to make the assumption in this work that the small dust should be retained at its currently observed rates. It is, however, not clear whether this small dust is resupplied directly, or via collisions between somewhat larger (maybe only mm sized) grains also orbiting in the disc. In order to avoid a complicated discussion of the collisional evolution of material in the exozodi, we decide to make the base-line assumption that at least the currently observed mass of dust must be supplied to the exozodi, on the lifetime of this small dust. In general, this is likely to be (significantly) lower than the rate at which material with the size distribution of the outer belt (where the mass is dominated by large km sized bodies) needs to be scattered inwards, since it ignores the inefficient conversion of this material to small dust (discussed further in Sect. 5). However, if stable outer planetary systems cannot even scatter material inwards at this rate, then it is highly unlikely that they are capable of replenishing the exozodi. As our fiducial example we take the Vega system, where a best fit model finds 10^{-9} M_{⊙} in between 0.2 μm and 1 mm grains, with an estimated lifetime of 1yr (Defrère et al. 2011). Thus, to retain Vega at its currently observed levels, the exozodi must be resupplied at a rate of at least 10^{-9} M_{⊙}/yr, although uncertainties in these values should be taken into account in the assessment of our simulations.

2.1. The scattering process

In this work our focus is on the fate of planetesimals that are scattered during the planet’s sculpting of the planetesimal belt.
Of particular interest are those particles that are scattered into the inner planetary systems at late times, as these have the potential to replenish an exozodi.

The scattering of planetesimals by planets is a subject that has been investigated in much detail in the literature (e.g. Raymond et al. 2009; Quillen & Holman 2000; Beust & Morbidelli 1996; Boley et al. 2012; Bonsor & Wyatt 2012; Debes et al. 2012). Planets are often invoked to sculpt the inner edges of debris discs (e.g. Quillen & Faber 2006; Chiang et al. 2009; Bonsor et al. 2011). A planet placed at the edge of a disc of planetesimals, as shown in Fig. 1, will scatter particles that are close to it. These particles lie in a zone directly surrounding the planet, whose size can be estimated analytically by considering the overlap of mean motion resonances, given by (Wisdom 1980):

$$\delta a_{\text{chaos}} = C \mu^{3/7} a_{\text{pl}},$$

where $\mu = \frac{M_p}{M_\star}$, the planet mass and $C$ is a constant, with various values between $C \approx 1.3$ (Wisdom 1980), $C \approx 1.5$ (Duncan et al. 1989; Quillen & Faber 2006) to $C = 2$ (Chiang et al. 2009) in the literature. In this work, we use the value $C = 2$, as we find this is a good fit to our simulations (see Fig. 1). Almost all particles in the planet’s chaotic zone will be scattered, given sufficiently long timescales, however, some particles outside of this zone will also be scattered by the planet.

Although simulations such as Quillen & Faber (2006) show that planets generally clear their chaotic zone on less than 10,000 orbital periods, the effects of this clearing can continue on significantly longer timescales. Even in our own solar system, after Gyr of evolution, there is evidence of Kuiper belt objects scattered by Neptune, for example, Jupiter Family Comets or Neptune’s scattered disc. The best way to understand some of these processes is to consider a very simple example.

In Fig. 1, we present the results of a simulation in which a 1 $M_{\text{Nep}}$ planet was placed on a circular orbit at 2 AU, with an initially “cold” ($e < 0.1$ and $I < 10^4$) planetesimal belt, extending from 2 to 3 AU. Particles that start inside of the chaotic zone, and close to its edge, are scattered by the planet onto orbits of higher eccentricity, in general at either constant pericentre or apocentre. The scattering timescale is proportional to distance from the planet, thus the chaotic zone is cleared from inside outwards. In the left-hand panel, it is clear that after 10,000 yrs of simulation, the chaotic zone is still being cleared; all particles initially in the inner regions have been scattered, whilst there are still some particles on unperturbed orbits in the outer regions of the chaotic zone. On the other hand, as shown in the right-hand panel, after 1 Myr of simulation, the full chaotic zone has been cleared. Particles are scattered onto orbits at constant pericentre ($q$) or constant apocentre ($Q$), thus lie between the dotted lines $q \sim q_\text{pl}$ and $q \sim q_\text{pl} - \delta a_{\text{chaos}}$ or $Q \sim q_\text{pl}$ and $Q \sim q_\text{pl} + \delta a_{\text{chaos}}$.

![Fig. 1](image1.png)

![Fig. 2](image2.png)
orbit at 2 AU, as a function of the time at which particles reach $r_{\text{Rodi}} = 1$ AU with increasing initial semi-major axis. This was anticipated, as the planet scatters particles close to it more quickly. This trend is, however, very smeared out, in a way that would not be the case if we merely plotted the time at which the particles were initially scattered. This is because once particles have been scattered a few times by the planet, their further scattering looses its dependence on the particle’s initial orbit. Given that most particles are scattered many times before they end up inside $r_{\text{Rodi}}$, the trend in Fig. 2 is somewhat blurred.

Critically, Fig. 2 shows that the scattering rates, even at late times, can be influenced by particles that start on orbits very close to the planet. This is unfortunate since it is not clear whether or not particles are expected on such orbits after planet formation. As discussed in further detail in Sect. 3.3, the end conditions of planet formation are not well constrained. It is, however, clear that planets clear a zone directly surrounding them, although there are no precise constraints on the size of this zone, which may well differ between terrestrial planet and gas giant formation. It is not the purpose of this work to investigate the end conditions of planet formation, nor to rely greatly upon their formation. It is not the purpose of this work to investigate the which may well differ.

Fig. 3. Diagram to illustrate the set-up of our simulations. The large circle represents the planet, at $a_{\text{pl}}$. The real belt, at late times, is shown by the thick line between $r_{\text{belt,in}} = a_{\text{pl}} + \delta a_{\text{chaos}}$ to $r_{\text{belt,out}} = a_{\text{max}}$. To simulate this belt we need only consider test particles that start between $a_{\text{min}} = a_{\text{pl}} + \delta a_{\text{chaos}}$ and $a_{\text{max}} = a_{\text{pl}} + 2\delta a_{\text{chaos}}$, represented by the dotted, thick line.

2.2. Details of the simulations

Our simulations are run using the RMVS3 integrator as part of the SWIFT package (Levison & Duncan 1994). This has an adaptive timestep. We consider planetary systems that have an outer planetesimal belt, running from $r_{\text{belt,in}}$ to $r_{\text{belt,out}}$, and a total mass of $M_{\text{belt}}$ in all bodies (between the blow-out size, $D_{\text{bl}}$ and a maximum size, $D_{\text{max}}$, as in Eq. (5)). The planets are on circular, coplanar orbits, interior to this outer belt. We consider that the outer planet, orbiting with a semi-major axis of $a_{\text{pl}}$, has sculpted the inner edge of the outer belt (see for example Fig. 1).

The outer planet is therefore placed interior to the outer belt’s inner edge by its chaotic zone (Eq. (1)), i.e. $a_{\text{pl}} + 2\delta a_{\text{chaos}}$. For our initial simulations we only consider a single planet, whilst later in this work (Sect. 4) we consider chains of several equal mass planets, of mass $M_{\text{pl}}$, separated equally in units of their mutual Hill’s radii, given by (e.g. Raymond et al. 2009; Chambers et al. 1996)

$$R_{\text{Hill}} = \left(\frac{a_1 + a_2}{2}\right)^{1/3} \left(\frac{M_1 + M_2}{3M_*}\right)^{1/3},$$

where $a_1$ and $a_2$, $M_1$ and $M_2$ are the semi-major axes and masses of the two planets.

Our outer planetesimal belt is composed of $N$ test particles, whose initial semi-major axes are randomly selected between $a_{\text{min}}$ and $a_{\text{max}}$, initial eccentricities between 0 and $e_{\text{max}} = 0.1$, initial inclinations between 0 and $i_{\text{max}} = 10^\circ$, and whose initial longitude of ascending node, argument of pericentre and mean anomalies are between 0 and $2\pi$. Although we consider our simulations representative of a belt between $r_{\text{belt,in}}$ and $r_{\text{belt,out}}$, it is not necessary to simulate particles covering the full belt (i.e. $a_{\text{min}} = r_{\text{belt,in}}$ and $a_{\text{max}} = r_{\text{belt,out}}$). Initial test simulations (see Fig. 2) found that a single planet has little to no influence on particles outside of twice the width of its chaotic zone. Thus, to reduce computing time, we fix $e_{\text{max}}$ at $a_{\text{pl}} + 2\delta a_{\text{chaos}}$. As will be discussed in further detail in Sect. 3.3, the planet will already have cleared a zone surrounding it during its formation. The exact size of this zone is not well constrained and particles close to the planet are scattered on average on shorter timescales, therefore we arbitrarily fix $a_{\text{min}}$ at $a_{\text{pl}} + \delta a_{\text{chaos}}$, although the dependence of our simulations on this value should be noted.

The results of our simulations are scaled to the full belt of width $r_{\text{belt,in}}$ to $r_{\text{belt,out}}$. Care must be taken when referring to the mass of the outer belt. In this work we refer to the total mass of the outer belt as the total mass in a belt between $r_{\text{belt,in}} = a_{\text{pl}} + \delta a_{\text{chaos}}$ and $r_{\text{belt,out}} = a_{\text{max}}$, except for in the examples where the outer belt radial extent is known from observations. This outer radius for the belt is an entirely arbitrary choice, and our results can be readily scaled to any value. It, however, enables a comparison between examples with different outer planet masses to be readily made.

The details of the set-up used in our simulations are shown in Fig. 3 and all the important parameters are listed in Table 1. In order to avoid unnecessary computing, we consider that particles have left the planetary system if their eccentricity increases above 1 or they are scattered outside of $r_{\text{max}}$, which we take as 10 AU in the one planet simulations and 1000 AU in the multi-planet simulations.

To determine the rate at which material is scattered inwards, we track the rate at which particles are scattered inside of $r_{\text{Rodi}}$, the nominal location of the exozodi, which we generally take to be 1 AU. Given the necessity to limit the number of test particles in our simulations, we consider that each test particle represents a fraction of the mass in the outer belt, contained in a suitable number of particles that reflect the size distribution of the outer belt. The fraction of the outer belt mass represented by each test particle is assigned based on the particles initial semi-major axis, assuming a mass surface density of the belt given by $\Sigma(r)dr \propto r^{-\alpha}dr$, where $\alpha = 1$, and that $a \sim r$ (valid for the low initial particle eccentricities used here). Given the potential difference between the simulated belt and the actual belt (see
2.3. The survival timescale of massive outer belts

As can be logically expected, and as will be quantitatively investigated in our study, the scattering of bodies from an outer belt to an exozodi is facilitated for massive outer belts. There is, however, a theoretical limit as to how massive such a belt can be, imposed by its collisional evolution. This concept of a maximum possible belt mass for a given system’s age is a very important constraint when discussing our results. It is therefore important to introduce it before presenting and discussing our simulations.

Debris discs are collisional system in which larger bodies are continuously collisionally ground down to smaller bodies and the smallest bodies are removed by radiation pressure. Thus, over time the total mass in the disc is depleted. Care must be taken in referring to the total disc mass, which here refers to the total mass of all bodies in the collisional cascade, extending from the observed small dust grains (μm) to km sized bodies. There may be larger bodies that are not yet in collisional equilibrium, it is however, impossible to obtain any information about such bodies from the observations and we therefore choose to disregard them in this work. Models for the collisional evolution of such discs from Wyatt et al. (1999, 2007a,b); Wyatt (2003) find that there exists a maximum total disc mass that can survive against collisions on long timescales. This maximum mass as a function of the disc radius, r, is given by (Wyatt et al. 2007a):

\[ M_{\text{max}}(r) = 5.2 \times 10^{-13} M_{\odot} \times \left( \frac{\rho}{\text{kg m}^{-3}} \right) \left( \frac{r}{\text{AU}} \right)^{13/3} \left( \frac{dr}{r} \right) \left( Q_D/\text{J kg}^{-1} \right)^{5/6} (D_{\text{max}}/\text{km}) \left( M_c/M_\odot \right)^{-4/3} \left( e \right)^{-5/3} (t/\text{Myr})^{-1}, \]

where \( \rho \) is the bulk density of the bodies, \( r \) the central radius of the belt of width \( dr \), \( Q_D \) the dispersal threshold, \( D_{\text{max}} \) the size of the largest body in the outer disc.

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Table 1. A list of the parameters used in this work.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Nominal value in this work</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \Delta )</td>
<td></td>
<td>The separation of the planets, in units of their mutual Hill’s radii</td>
</tr>
<tr>
<td>( \delta a_{\text{chaos}} )</td>
<td></td>
<td>The radial extent of the chaotic zone in units of the planet’s semi-major axis</td>
</tr>
<tr>
<td>( \rho )</td>
<td>2700 kg m(^{-3})</td>
<td>The density of the individual particles in the outer belt</td>
</tr>
<tr>
<td>( a_i )</td>
<td></td>
<td>The initial semi-major axis of a particle, before it is scattered by a planet</td>
</tr>
<tr>
<td>( a_p )</td>
<td></td>
<td>The planet’s semi-major axis</td>
</tr>
<tr>
<td>( a_{\text{pl}} )</td>
<td>( r_{\text{belt,in}} - \delta a_{\text{chaos}} )</td>
<td>The outer planet’s semi-major axis</td>
</tr>
<tr>
<td>( a_{\text{min}} )</td>
<td>( a_{\text{pl}} + \frac{dr}{r_{\text{belt,in}}} )</td>
<td>The minimum initial semi-major axis of test particles in this simulations</td>
</tr>
<tr>
<td>( a_{\text{max}} )</td>
<td>( a_{\text{pl}} + 2\delta a_{\text{chaos}} )</td>
<td>The maximum initial semi-major axis of test particles in this simulations</td>
</tr>
<tr>
<td>( \delta a_{\text{belt}} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( D_{\text{max}} )</td>
<td>60 km</td>
<td>The size of the largest body in the outer disc</td>
</tr>
<tr>
<td>( d_r )</td>
<td></td>
<td>The width of the outer belt</td>
</tr>
<tr>
<td>( \varepsilon_{\text{max}} )</td>
<td>( \frac{d_r}{r} = 2 )</td>
<td>The maximum initial eccentricity of test particles in this simulations</td>
</tr>
<tr>
<td>( \varepsilon_i )</td>
<td></td>
<td>The eccentricity of a particle before it is scattered by the planet</td>
</tr>
<tr>
<td>( F_{\text{disc}} )</td>
<td></td>
<td>The disc flux</td>
</tr>
<tr>
<td>( F_{\text{disc}} )</td>
<td></td>
<td>The stellar flux</td>
</tr>
<tr>
<td>( (e) )</td>
<td>0.05</td>
<td>The average eccentricity of particles in the outer belt</td>
</tr>
<tr>
<td>( L_{\text{belt}} )</td>
<td>10(^{10})</td>
<td>The maximum initial inclination of test particles in this simulations</td>
</tr>
<tr>
<td>( M_{\text{belt}} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( M_{\text{dis}} )</td>
<td></td>
<td>The minimum mass of a planetesimal belt such that it can be detected</td>
</tr>
<tr>
<td>( M_{\text{max}} )</td>
<td></td>
<td>The maximum mass of a collisionally evolving planetesimal belt</td>
</tr>
<tr>
<td>( M_{\text{part}} )</td>
<td></td>
<td>The fraction of the total outer belt mass assigned to each test particle</td>
</tr>
<tr>
<td>( M_{\text{pl}} )</td>
<td></td>
<td>The planet mass</td>
</tr>
<tr>
<td>( N_{\text{pp}} )</td>
<td></td>
<td>The number of particles used in the simulation</td>
</tr>
<tr>
<td>( Q_D )</td>
<td>150 J kg(^{-1})</td>
<td>The dispersal threshold</td>
</tr>
<tr>
<td>( q_{\text{min}} )</td>
<td></td>
<td>The maximum pericentre of a particle, with a Tisserand parameter of ( T_i ), scattered by a single planet on a circular orbit</td>
</tr>
<tr>
<td>( R_\odot )</td>
<td></td>
<td>Hill’s radii</td>
</tr>
<tr>
<td>( r )</td>
<td></td>
<td>The central radius of the outer belt</td>
</tr>
<tr>
<td>( r_{\text{belt,in}} )</td>
<td>( a_{\text{pl}} + \delta a_{\text{chaos}} )</td>
<td>The inner radius of the outer belt</td>
</tr>
<tr>
<td>( r_{\text{belt,out}} )</td>
<td>( a_{\text{max}} - a_{\text{min}} )</td>
<td>The outer radius of the outer belt</td>
</tr>
<tr>
<td>( r_{\text{exozodi}} )</td>
<td></td>
<td>The position of the exozodi, or the inner radial limit within which most scattered material will go on to produce an exozodi</td>
</tr>
<tr>
<td>( r_{\text{max}} )</td>
<td>10 or 100 AU</td>
<td>The distance outside of which particles are considered removed from the simulations</td>
</tr>
<tr>
<td>( r_{\text{min}} )</td>
<td></td>
<td>The minimum radius of a planetesimal belt in order that a given mass of material can survive against collisions for the age of the system</td>
</tr>
<tr>
<td>( r_{\text{belt,min}} )</td>
<td></td>
<td>The minimum radius required by a planetesimal belt such that it can scatter material inwards at a sufficiently high rate to retain the observed levels of exozodiacal dust</td>
</tr>
<tr>
<td>( T_i )</td>
<td></td>
<td>The initial value of the Tisserand parameter</td>
</tr>
</tbody>
</table>

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Fig. 3), each particle is assigned a fraction of the total mass in the belt, extending between \( r_{\text{belt,in}} \) and \( r_{\text{belt,out}} \):

\[
m_{\text{part}} = \left( \frac{1}{N_{\text{pp}}} \right) \left( \frac{r_{\text{belt,out}} - r_{\text{belt,in}}}{a_{\text{max}} - a_{\text{min}}} \right),
\]

where \( N_{\text{pp}} \) is the number of test particles placed between \( a_{\text{min}} \) and \( a_{\text{max}} \) at \( t = 0 \). Using this formulation, this rate can readily be scaled to an outer belt of a different width (i.e. with a different \( r_{\text{belt,out}} \)). The rate at which material is scattered inwards is then calculated from the fraction of the belt mass assigned to each particle divided by the time between adjacent collisions.
the largest body in the disc, $m$, the stellar mass, $\langle e \rangle$ is the average eccentricity of particles in the disc, assumed to be constant and $t$ is the age of the system, or strictly the time after the disc was stirred. Written in this form, it was assumed that the disc contains a Dohnanyi size distribution of bodies (Dohnanyi 1969), with a power index of $\frac{2}{3}$ (Tanaka et al. 1996) between the smallest size body that is not blown out of the system by radiation pressure and the significantly larger maximum size for bodies in the disc, $D_{\text{max}}$. The mass is dominated by the largest bodies. It also assumes that particles can be catastrophically destroyed by particles significantly smaller than themselves, that the disc is thin (of width $dr$) and does not spread radially.

This maximum mass is a strong function of the disc radius. We can use it to determine the minimum radius of a planetesimal belt in which a particular mass can survive against collisions, up to a given age. Thus, the minimum radius at which a disc of mass, $M_{\text{disc}}$, can survive is

$$r_{\text{min}} = 6.8 \times 10^2 \text{ AU} \times$$

$$\times \left( \frac{M_{\text{disc}}}{M_{\odot}} \right)^{3/13} \left( \frac{M_{\odot}}{M_{\text{disc}}} \right)^{4/13} \langle e \rangle^{5/13} \left( \frac{t}{\text{Myr}} \right)^{3/13} \left( \frac{D_{\text{max}}}{\text{km}} \right)^{-3/13} \left( \frac{\rho}{\text{kg m}^{-3}} \right)^{-3/13} \left( \frac{Q_T}{J \text{kg}^{-1}} \right)^{-5/26}.$$  

This minimum radius is particularly interesting because it enables us to place a radial limit on the position of an outer belt if sufficient mass is to survive for a given age. This minimum radius is plotted in Fig. 4 as a function of time. Formally this is the time since the collisional velocities in the disc reached high enough values to be catastrophic and the system was stirred, which we assume to be approximately equal to the age of the system. We take fiducial values for the model parameters that come from fitting observations of debris discs around main sequence A stars (Wyatt et al. 2007b). Thus, the maximum body is $D_{\text{max}} = 60$ km, eccentricity $\langle e \rangle = 0.05$, the density $\rho = 2700$ kg m$^{-3}$ and the width $\frac{2}{3}$ = 0.5. In order to allow some of these parameters to be easily varied, the time is plotted multiplied by a factor involving the stellar mass and the ratio of the disc mass to the maximum diameter particle is fixed, rather than the exact disc mass. Planetesimal belts in steady state can exist above and to the left of the minimum lines plotted.

Figure 4 confirms our earlier assertion that exozodi cannot be supplied by a steady-state collisional cascade of massive, unseen, parent bodies orbiting at their radial location. Consider the example of Vega, where the best fit to the observations of the exozodi find $1.9 \times 10^{-3} M_{\odot}$ of material, in 0.2 μm to 1 mm sized bodies (Defrère et al. 2011). If this material were to be supplied in a steady-state size collisional cascade from unseen bodies extending up to $D_{\text{max}} = 60$ km in size, at the same radial location (i.e. inside of 1 AU), an absolute minimum on the total disc mass required would be $10^{-3} M_{\odot}$. Figure 4 clearly shows that such a mass of material cannot survive at 1 AU for longer than ~30 Myr, less than 10% the age of Vega. However, such a mass (and significantly more) can survive for 455 Myr age of Vega (Yoon et al. 2010), in a belt outside of 60 AU (the observed debris disc radius, Müller et al. 2010).

3. One planet

The simplest possible planetary system is one containing an outer planetesimal belt and a single interior planet on a circular orbit. Although possibly not a likely structure for many real planetary systems, this provides a simple to understand, illustrative example of the scattering processes that occur in more complicated multi-planet systems, which we defer to later in this work. We investigate the rate at which particles are scattered to the position of the exozodi. However, a single planet is not capable of scattering particles infinitely far and therefore it is useful to firstly consider analytically the position of the planet relative to the outer belt and the exozodi.

3.1. An analytical limit on the maximum semi-major axis of the planet

If particles scattered by a planet are to produce an exozodi, the planet must be capable of scattering them sufficiently far in, to $r_{\text{rad}}$. If we consider planets on circular orbits, the conservation of the Tisserand parameter places an analytical limit on how far a planet can scatter a particle (Bonsor & Wyatt 2012). This can be expressed as a minimum allowed pericentre for the particle’s orbit, given by (Eq. (3) of Bonsor & Wyatt 2012)

$$q_{\text{min}}(T_i) = a_i - T_i^2 + 2T_i + 4 - 4\sqrt{3 - T_i} + \frac{i}{T_i - 8},$$

where $T_i$ is the initial value of the Tisserand parameter, for a particle with semi-major axis, $a_i$, eccentricity, $e_i$ and inclination, $I_i$ (Eq. (3) of Bonsor & Wyatt 2012). This limit is only strictly valid for low mass planets on circular orbits, where long range interactions are rare. It, however, provides a good approximation to the behaviour even of Jupiter mass planets on mildly eccentric orbits, although there may be a small flux of particles scattered inside of this minimum pericentre.

This minimum pericentre can be used to determine whether or not a particular configuration of planet and planetesimal belt can scatter any material to the position of the exozodi, $r_{\text{rad}}$. For a single planet it provides a limit on the maximum semi-major axis of the planet. This depends on the initial orbital parameters (Tisserand parameter value) of the particles before they are scattered by the planet and is determined by equating $q_{\text{min}}(T_i) = r_{\text{rad}}$. This maximum semi-major axis is plotted in Fig. 5 as a function of the particle’s Tisserand parameter value.

Although note the factor of $(2.1 M_{\odot})^{4/3}$ necessary in Fig. 4 to account for the mass of Vega (Yoon et al. 2010).
Fig. 5. Analytical limit on the maximum semi-major axis of a planet, if it is to be able to scatter particles as far inwards as the position of the exozodi at $r_{\text{odi}}$, as a function of the particle’s initial eccentricity. This is calculated using Eq. (6), and the particle’s initial eccentricity is a proxy for the Tisserand parameter value, as described in Sect. 3.1. This limit only strictly exists for planets on circular orbits and vanishes for $e_i > 0.46$ (or $T_i < 2$), or for very low eccentricity particles that do not cross the planet’s orbit ($e_i > 0.04$ or $T_i < 3$).

Fig. 6. Comparing the rate at which particles are scattered inwards by Neptune, Saturn and Jupiter-mass planets on circular orbits at 2 AU. The details of the simulations can be found in Table 2. Higher mass planets scatter more material inwards, but lower mass planets continue to scatter material inwards on longer timescales.

except that the particle’s initial eccentricity is used as a proxy for its value of the Tisserand parameter. This means assuming values for the particle’s initial inclination of $I_i \approx 2e_i$, and initial semi-major axis of $a_i = a_{pl} + \delta a_{\text{chaos}}(1 \ M_{\text{Neptune}})$, which places the particle initially at the edge of the planet’s chaotic zone. In this plot, we consider a Neptune mass planet, although the dependence on the planet mass of the results is negligible. In terms of our single planet simulations, given that we start particles in a fairly cold belt, with $e_{\text{max}} = 0.1$, Fig. 5 shows that the planet must be inside of $a_{pl} < 2.2$ AU if it is to scatter such particles in as far as an exozodi at $r_{\text{odi}} = 1$ AU.

This analysis can also be applied to the inner planet of a chain of multiple planets, as considered later in this work (Sect. 4). In this case, the particle’s inclinations and eccentricity will have been excited by the exterior planets before it reaches the inner planet. For example all particles with $e_i \sim 0.2$ by the time they reach the inner planet, can be scattered as far as 1 AU by a planet at 5 AU.

3.2. Dependence on the planet mass

Given the analytical limit on the ability of a planet outside of 2.2 AU on a circular, planar orbit to scatter particles inside of $r_{\text{odi}} = 1$ AU, we consider the fiducial example of different mass planets on circular orbits at $a_{pl} = 2$ AU. The simulations are set-up in the manner described in Sect. 2.2 and the rate at which material is scattered inside of $r_{\text{odi}} = a_{pl} = 1$ AU is tracked, as a function of the total mass of a belt spanning between $r_{\text{belt, in}} = a_{pl} + \delta a_{\text{chaos}}$ and $r_{\text{belt, out}} = a_{pl} + 3$ AU. Each cross on the plot in Fig. 6 represents an individual test particle in our simulations, at the time at which it reached $r_{\text{odi}}$.

An analytical understanding of the dependence of scattering process on planet mass can be found by considering the variance in the size of the chaotic zone (Eq. (1)) with planet mass. Thus, an increase in the total amount of material scattered with planet mass is anticipated. Generic arguments tell us that higher mass planets scatter on shorter timescales. Thus, a significantly increased rate of scattering, at least at early times, is anticipated. This can be seen in Fig. 6. Although the high mass planets are good at scattering particles inwards at high rates on short timescales, on longer timescales, low mass planets are better suited to scattering particles inwards at lower rates.

3.3. Dependence on the initial conditions of the simulation

The precise outcome of $N$-body simulations depends on the exact initial conditions used. In our case, the initial orbital parameters of the planetesimals in the outer belt can affect the ability of planets to scatter them inwards. Ideally the initial conditions for our simulations would be those found at the end of planet formation process. It is, however, not fully clear what these are. There are many uncertainties in our understanding of the planet formation process and its outcomes, and it is not the purpose of this work to investigate these. We therefore choose to consider an idealised scenario in which the planets are fully formed at the start of our simulations, and the planetesimal belt is situated outside of their orbits.

As planets form they accrete material from their direct surroundings. Thus, a deficit of planetesimals very close to the planet would be expected at the end of planet formation. However, we do not anticipate that the planet fully clears its chaotic zone, given that our initial simulations (Fig. 1) showed...
that some particles in the outer regions of the chaotic zone were only scattered after 10,000\,T_{pl}, i.e. longer than expected timescales for planet formation. As discussed in Sect. 2.2, we therefore did not include any particles between \( a_{\text{pl}} \) and \( a_{\text{min}} = a_{\text{pl}} + \frac{a_{\text{chaos}}}{2} \) in our simulations. Figure 7 shows the the range of change that could be anticipated in our scattering rates, if we have either under or over estimated \( a_{\text{lim}} \). At the late times of interest, even the maximum possible change is less than an order of magnitude.

In order to reduce the necessary computation time, we also limited the initial semi-major axis range of test particles to less than \( a_{\text{max}} = a_{\text{pl}} + 2\,a_{\text{chaos}} \). Figure 7 shows that this does not alter the results more than the statistical variation between individual simulations. For multi-planet systems, there is the potential that three-body resonances or secular terms may affect particles much further out in the disc, however, test simulations found this not to be significant (Sect. 5).

Arguably the most significant initial condition for our simulations is the initial excitation of the disc. Planet formation models suggest that planetesimals should initially have very low eccentricities and inclinations, damped by the gas disc. For this reason we choose to restrict our initial eccentricities and inclinations, damped by the gas disc. For this parameter, and the limit this provides on how far particles can be scattered inside of \( r_{\text{chaos}} \), in our simulations. Figure 7 shows that this does not alter the results more than the statistical variation between individual simulations. For multi-planet systems, there is the potential that three-body resonances or secular terms may affect particles much further out in the disc, however, test simulations found this not to be significant (Sect. 5).

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Fig. 7. Change in the scattering rates with the width of the simulated belt, i.e. \( a_{\text{max}} \) and \( a_{\text{lim}} \), for a 1 \( M_{\text{Neptune}} \) planet at 2 AU, as described in Table 2. The crosses represent individual scattering events, whilst the dotted lines are straight line fits to the data. There is a negligible difference between scattering rates when \( a_{\text{max}} \) is increased (green and black points), however, a decrease in \( a_{\text{max}} \) causes a slight increase in the scattering rates, even at late times (red or blue crosses compared to black or green).

4. Multi-planet systems

A more realistic planetary system is one in which there are multiple planets and the outer planetesimal belt is significantly further from the star. There is good evidence for the prevalence of multi-planet systems with a wealth of different architectures\(^3\). The full parameter space is clearly too large to investigate in this work, even if we restrict ourselves to \( N_{\text{pl}} \) planets on circular orbits, in the same plane, interior to a planetesimal belt. For simplicity, we therefore focus on the example of a chain of equal mass planets, separated equally in units of their mutual Hill’s radii. This system should be considered a representative system, from which it is possible to better understand the scattering processes and the way that they apply to other systems.

The simulations are set-up in the same manner as described in Sect. 2. We place the outer belt at \( r_{\text{belt,in}} = 62 \) AU, to match with the observations of the outer belt in the Vega system (Müller et al. 2010), although we anticipate that our simulations can be scaled to a limited range of different belt radii. In the same manner as for the single planet system, the outer planet is placed such that it sculpts the inner edge of the outer belt, at \( a_{\text{belt,in}} = r_{\text{belt,in}} - \delta a_{\text{chaos}} \). Equal mass planets are then placed interior to this, separated by \( \Delta R_{\text{Hill}} \). In order to ensure that the planetary systems considered actually scatter material inside of \( r_{\text{chaos}} = 1 \) AU, we consider the conservation of the Tisserand parameter, and the limit this provides on how far particles can be scattered by a planet (Eq. (6)). This time, we anticipate that the scattering by multiple outer planets excites the particles eccentricities and inclinations before they are scattered by the interior planet. Therefore, we place a limit on the interior planet such that all particles with \( e > 0.2 \) can be scattered inside of \( r_{\text{chaos}} = 1 \) AU. This implies that the planet should be at 5 AU. Therefore we “fill” our planetary system with planets equally spaced in terms of their Hill’s radii down to \( a_{\text{fill,in}} = 5 \) AU. The number of planets required to “fill” the planetary system ranges between 3 and 10 (as can be seen in Table 3). A choice of a larger value for \( a_{\text{fill,in}} \) could reduce the number of particles scattered inside of \( r_{\text{chaos}} \) to zero. It is therefore worth noting that our simulations are more representative of the maximum, than minimum scattering rates.

\(^3\) 162/580 multi-planet systems according to exoplanets.org on 18 June 2012.
scribed in Sect. 3), the rate at which particles are scattered inside of $r$ of

The simulations presented in this section are for very specific systems find a huge variety of planet masses and separations. Nonetheless, the results from these simulations can be used to make useful conclusions about the scattering rates in more realistic planetary systems. Firstly, having understood the broad dependences of the scattering rates on planet separation and mass, we are able to conclude that the highest scattering rates, at late times, occur for tightly packed, low-mass planets. Thus, our simulations with chains of Neptune mass planets separated by 8 $R_H$ are representative of some of the highest possible scattering rates after millions of years of evolution, beaten only by chains of lower mass planets, packed even closer to the stability limit. We therefore consider that our simulations are broadly representative of an approximate upper limit on the scattering rates possible in any planetary system, although, it is worth noting, as will be discussed in Sect. 5, that we may have missed a few systems.

### 4.1. Application of these results to any system

The simulations presented in this section are for very specific planetary systems, with strict constraints on its architecture. This was necessary in order for the current investigation to be feasible. Clearly, these do not mimic many, if any, real planetary systems. In fact, the current observations of multi-planet systems find a huge variety of planet masses and separations. Nonetheless, the results from these simulations can be used to make useful conclusions about the scattering rates in more realistic planetary systems. Firstly, having understood the broad dependences of the scattering rates on planet separation and mass, we are able to conclude that the highest scattering rates, at late times, occur for tightly packed, low-mass planets. Thus, our simulations with chains of Neptune mass planets separated by 8 $R_H$ are representative of some of the highest possible scattering rates after millions of years of evolution, beaten only by chains of lower mass planets, packed even closer to the stability limit. We therefore consider that our simulations are broadly representative of an approximate upper limit on the scattering rates possible in any planetary system, although, it is worth noting, as will be discussed in Sect. 5, that we may have missed a few systems.
with very specific architectures that enhance the rates still further. Secondly, the results presented here can be scaled, such that the scattering rates in a system of a known architecture can be estimated. In this manner the scattering rates in a real planetary system, with planets on known orbits, could be estimated.

In this work, we investigated the change in the scattering rates between chains of equal mass planets, evenly spaced in units of their Hill’s radii (ΔR_H), with different planet masses (M_p) and separations (Δ). To do this we fixed the stellar mass (M_*) and the radial location of the outer belt, (r_{belt,out}, r_{belt,in}), the radial location of the exozodi (r_{rodi}) and a parameter that we term a_{fill}, that specifies the number of planets, by providing an inner radial limit on their possible orbits. Real planetary systems are unlikely to have the values used for these parameters. We therefore discuss the effects of changing the different parameters on the scattering rate, in such a way that we can understand and anticipate the behaviour in any planetary system.

Firstly considering planetary systems of the form described in this section, with equally separated, equal mass planets, the scattering rates that we calculated (i.e. shown in Fig. 9), can be applied almost exactly to another system in which the orbital timescales of the planets/planetesimals are different. In other words, systems where the radial location of the outer belt or the stellar mass is changed. In this manner the results of our simulations can be applied to planetary systems with outer planetesimal belts at any location, with the assumption that the radial location of the exozodi scales with the radial location of the outer belt. If the radial location of the outer belt is scaled by a factor, f, then the same scattering rates can be applied to the system by scaling the time axis by a factor of f^{1/2}. Similarly, for stars of different stellar mass, there is a small change in the scattering timescales that can be found by scaling the time axis by a factor M_*^{1/2}.

There are three other parameters that can affect the scattering rates; the width of the outer belt (r_{belt,out}), the location of the exozodi (r_{rodi}) and the innermost planet’s semi-major axis, a_{inj}. The width of the outer belt is in essence unimportant, as long as it is greater than the planet’s chaotic zone. It will however change the values for both the total outer belt mass, and the fraction of it, that is scattered inwards, in a manner that can be readily calculated using Eq. (3).

The location of the exozodi (r_{rodi}) is crucial. Scattering rates generally scale with r_{rodi}, unless r_{rodi} is too small that no (or very few) particles can be scattered sufficiently far inwards (see discussion of the analytical limit in Sect. 3.1). Changing the location of the exozodi produces differences in the scattering rate of the same order of magnitude as the difference caused by changing the planet separation (Δ).

On the other hand, the value of the parameter a_{fill} used here, was chosen to ensure that particles are scattered to the location of the exozodi, r_{rodi}. In a real planetary system, the innermost planet could take any position, and the scattering rates will depend critically on this position. Test simulations find that scattering rates do not vary significantly with a_{fill}, or equivalently the position of the innermost planet, so long as the planet separation does not increase. This only applies if a_{fill} is not decreased so much that the inner planet is within a Hill’s radius of the exozodi, or increased so much that particles can no longer be scattered from a_{fill} to r_{rodi}. For the example system used in this work with q_{belt,out} = 62, a_{rodi} analysis of our simulations found that particles are generally excited up to eccentricities of around e ∼ 0.3 before being scattering by the planet. Thus, using Fig. 5 we anticipate that increasing a_{fill} up to 10 AU, does not significantly alter the scattering rates. We verified this with test simulations. In other words, taking the example of the chain of 4 Jupiter mass planets separated by 8R_H, the innermost planet is not required in order to retain the scattering rates at the calculated values. However, if a_{fill} were to be increased beyond 15 AU, no particles would be scattered inwards. It is therefore easy to design a planetary system in which the scattering rates tend to zero, by applying Fig. 5 to that system.

Now, we consider the broad outcomes of these results and their applicability to any planetary system. In general, the results presented in this work only further our understanding of planetary systems with a single, outer planetesimal belt and planets on circular, co-planar orbits, interior to the belt. Let us first consider chains of planets of non-equal mass. The outer planet controls the amount, and the rate, at which material is scattered into the inner planetary system. Thus, the outer planet dominates the scattering rates, whilst the inner planets modify these rates slightly by controlling how long it takes for particles to be passed inwards to the exozodi. This timescale depends on the mass of the planets. The best way to illustrate this is to consider the simple example of a chain of Neptune mass planets, that ordinarly scatter a small amount of material inside of r_{rodi} on long timescales (see Fig. 9). If all but the outer planet were replaced with higher mass (e.g. ∼1M_J) planets, whilst retaining the same separation in Hill’s radii, then material would continue to be scattered out of the outer belt on the same timescales, but would be passed from the outer belt to r_{rodi} more swiftly. Therefore, the rate of scattering of material inside of r_{rodi} would fall off more steeply with time. If the interior planets were of lower mass than the outer planets, they could do the inverse and cause a bottleneck, delaying the scattering process.

Now, all that remains in order to be able to apply our results to any planetary system, is a consideration of the effect of changing the separation of the planets. Although our simulations clearly show that more widely spaced systems scatter at somewhat lower rates, as discussed in Sect. 4, the effect on the scattering rates is not as significant as that caused by changing the planet mass. The separation of the planets can, however, be increased so much, that a gap in the planetary system is produced, over which very few particles are scattered. The separation at which this occurs can be estimated by considering when the planets are so widely separated that q_{min}(T_i) < a_{inj} - ΔR_H, or referring to Bonsor & Wyatt (2012) for a more detailed calculation.

To take an example, for a chain of Jupiter mass planets, if any pair of planets were separated by more than 20R_H, very few particles could be passed between them.

To summarise, the arguments presented here can be used to calculate exactly the scattering rates in planetary systems that follow the mould of our example and to estimate the broad behaviour in any other planetary system.

4.2. The collisional evolution of the outer planetesimal belt

The outer planetesimal belt is a collisionally evolving system, like any debris disc. We have not taken the collisional evolution of the disc mass into account in our calculation of the rate at which material is scattered inwards, shown in, for example, Fig. 9. Each individual data point in this plot was calculated by assigning each test particle a fraction of the total outer belt mass at the instant it was scattered inwards. Of course, if the disc is collisionally evolving, the total outer belt mass could potentially be different for each particle. Taking this into account, the new version of Fig. 9, would have an even steeper fall off with time. For practical purposes, the data in Fig. 9 will generally be used.
to assess the total outer belt mass required in order to obtain an observed scattering rate. This should be close to the disc’s current mass, because in the general the timescales for the collisional evolution are not significantly faster than the scattering timescales.

If we make the assumption that material must be scattered inwards at a rate of at least $10^{-9} M_\oplus/yr$ to resupply an exozodis, the simulations shown in Fig. 9 can be used to determine the minimum mass required for the outer belt at 62 AU. It is important to consider whether or not such a mass can survive against collisions, at the given radial location, for the age of the system. This can be done analytically, for example using the models of Wyatt et al. (2007a) and Eq. (5). In fact, given that the results of our simulations can be readily scaled to systems with outer belts at different radial locations (as discussed in Sect. 4.1), the minimum mass required can be determined for belts at a variety of different radii. This scaling necessarily assumes that the location of the exozodi scales with the outer belt. The best way to illustrate this is to take the scattering rates, $R_s$, calculated and shown in Fig. 9. The disc mass required to produce these scattering rates, by an outer belt at any (reasonable) radial location, $\rho_{\text{belt, in}}$ (i.e. scaling the rates of Fig. 9 with the orbital timescales), is given by

$$M_{\text{disc}} = \left(\frac{R_s/M_\oplus}{10^{-9}/M_\oplus\text{yr}^{-1}}\right) \left(\frac{\rho_{\text{belt, in}}}{62 \text{ AU}}\right)^{3/2} \frac{1}{M_\oplus}. \quad (7)$$

We now have a requirement on the minimum mass needed in an outer belt, at a range of radial locations, if the outer belt is to supply material scattered inwards at a rate of at least $10^{-9} M_\oplus/yr$. Contrasting this with the collisional evolution of the disc, it is possible to determine which of these discs can survive against collisions for the age of the system. In other words a minimum limit on the radius required for the outer belt can be placed. This limit is shown in Fig. 10. Given the assumptions, this means that an outer belt that resupplies an exozodi must lie beyond the radial limit shown in Fig. 10. Each cross in this plot is taken from the simulations shown in Fig. 9, where the minimum mass required in the disc is calculated for a range of radial locations using Eq. (7) and the minimum possible radial location determined by substituting these masses into Eq. (6), to obtain:

$$\rho_{\text{belt, min}} = K^{26/17} \left(\frac{r^2 (R_s/M_\oplus \text{yr}^{-1})^2}{(10^{-9}/M_\oplus \text{yr}^{-1})^2 (62 \text{ AU})^3}\right)^{3/17} \text{AU} \quad (8)$$

$$K = \frac{6.8 \times 10^2 (M_\ast/M_\odot)^{4/13} (e)^{5/13}}{(D_{\text{max}}/\text{km})^{3/13} (\mu/\text{kg m}^{-3})^{3/13} (\rho^{1/3} D_\Omega/\text{J kg}^{-1})^{5/26}}.$$

This makes the assumption that the belt width is small and takes the values for the parameters listed in Sect. 2.3. Figure 10 clearly shows that because relatively massive planetesimal belts are required to scatter material inwards at the required rates, the belt must be reasonably far from the star in order that such a mass can survive against collisions for the typical ages of exozodi systems. This of course assumes that the collisional evolution of the belt commenced very early in the star’s evolution and that all bodies in the disc are involved in this collisional evolution. It also assumes that the belt width is small and fixed at $\Phi = 0.5$, that the location of the exozodi scales with the radial location of the outer belt and that a scattering rate of $10^{-9} M_\oplus/yr$ is reasonable requirement to retain the observed dust levels in an exozodi. In this case, Fig. 10 shows that in order for an outer planetesimal belt to scatter dust inwards at this level for longer than 100 Myr, it must be outside of ~20 AU, otherwise insufficient mass can survive against collisions. This is an important conclusion because many observed debris discs are inside of this radius.

### 4.3. The detectability of the outer belt

Our simulations can be used to place limits on the required masses and radial locations of an outer planetesimal belt, in order that it could potentially scatter material inwards at sufficiently high rates to retain the currently observed levels of dust in exozodi. These limits can be compared with our ability to detect such discs.

Taking our simulations for chains of multiple equal mass planets, shown in Fig. 9, we calculate the minimum disc mass required to scatter material inwards at a fiducial rate of $10^{-9} M_\oplus/yr$, at an age of 100 Myr. This is the total mass, in bodies of all sizes, in a disc between $\rho_{\text{belt, in}} = \rho_{\text{p}} + \delta\rho_{\text{chaos}}$ and $\rho_{\text{belt, out}} = 3\rho_{\text{min}}$. As discussed in Sect. 4.1 the scattering rates, and thus the minimum required disc mass, can be scaled to outer belts at any radial location, although only with the assumption that the position of the exozodi, $\rho_{\text{rad}}$, scales in a similar manner. Thus, every point in Fig. 9 can be considered to represent the scattering rate after 100 Myr in a belt at a different radial location. The radial location and minimum required masses for the outer belts to scatter material inwards at rates higher than $10^{-9} M_\oplus/yr$ are shown by the blue crosses in Fig. 11, for a chain of 1 $M_{\text{Sat}}$ planets separated by 8R_\ast. This is the simulation with the largest detectable parameter space of any of our simulations. This plot reiterates the fact that massive, large radii planetesimal belts are the most adept at scattering material inwards.

Some constraints on the existence of the discs outlined in Fig. 11 can be made by considering their collisional evolution. As discussed in Sect. 2.3, only belts below a maximum mass, can survive at a given radial location for a given age. This maximum mass is plotted by the dotted line in Fig. 11, calculated using Eq. (5), taking the parameters of Wyatt et al. (2007b), listed in Sect. 2.3.

The next question to consider is which of these discs could be detectable. One way to detect a debris disc is by an infrared excess, for example at 70 μm. For this plot, we consider Spitzer’s detections limits, as Spitzer surveys of debris discs are...
The number of systems with detected exozodi is limited, only a handful of the detected systems also have outer planetesimal belts and there are very few planet detections. For these reasons, we decide to focus here on two example systems, both of which have resolved outer belts, and detailed modelling of the inner exozodi. Neither of the systems have any evidence for planetary companions. The two example systems were chosen to contrast. Vega is a 450 Myr old A star, whilst η Corvi is an older (Gyr), sun-like star, with an extremely large infrared excess. We apply the simulations presented in this work, to these systems, in order to determine the possible scattering rates that could occur, if we make the hypothesis that chains of planets orbit between the inner and outer dust discs. We then compare these scattering rates with observations of the exozodi and outer belt, and assess the feasibility of such scattering to solve the conundrum of the high levels of exozodiacal dust observed.

4.4.1. Vega

Vega’s outer belt was the first debris disc to be detected (Aumann et al. 1984) and has since been observed many times at a variety of different wavelengths. The exact properties derived from observations of the outer belt vary in the literature, but here we consider the best fit model of Müller et al. (2010), that takes observations from the near-infrared through to sub-mm wavelengths into account. Their best fit model finds a dust belt between 62 and 120 AU, with 5.09 $M_\odot$ of dust and a total mass of 46.7 $M_\odot$, which collisionally evolved from an initial mass of 55.9 $M_\odot$. Fitting of isochrones finds an age of 455 ± 13 Myr and a mass of 2.157 ± 0.017 $M_\odot$ (Yoon et al. 2010). Exozodiacal dust was detected around Vega by Absil et al. (2006) and again by Defrère et al. (2011). The best-fit to the observations finds a mass of 10$^{-9}$ $M_\odot$ in small dust grains between 0.2 μm and 1 mm in size (Defrère et al. 2011). A collisional timescale of ~1 yr is derived. This suggests that if the disc is to be retained at its current levels it needs to be replenished at a rate of at least 10$^{-9}$ $M_\odot$/yr.

The scattering rates determined in our multi-planet simulations described in Sect. 4 and shown in Fig. 9 can be applied to Vega. Without any limits on planetary companions less than several Jupiter mass (e.g. Hinkley et al. 2007; Itoh et al. 2006), we are free to hypothesise the existence of any inner planetary system. If Vega is really orbited by as yet undetected planets, they may or may not resemble the chains of multi-planet systems considered in this work. However, by considering the hypothesis that there are chains of equal mass planets, interior to Vega’s outer planetesimal belt, we are able to place an estimate on the maximum rates that planets could possibly scatter material inwards.

The position of the outer belt was already chosen to fit with that of the outer belt in the Vega system. Thus, in order to apply the results of these simulations to Vega, it is only necessary to scale the scattering times by a factor of $\frac{1}{\sqrt{2 \text{AU}}}$ ≈ 0.68 in order to account for the increased stellar mass. These results now represent systems with chains of equal mass planets still separated by $\Delta = 8 R_H$ or $15 R_H$, but with increased masses of $2 M_{\text{Neg}}, 2 M_{\text{sat}}$ or $2 M_I$. This is detailed in Table 3. In Fig. 12 we calculate the total mass in the outer belt if these chains of equal mass planets were to scatter material in to the position of the exozodi, which we take to be 1 AU, at the required rate of 10$^{-9}$ $M_\odot$/yr. This is the minimum required mass in the outer belt, assuming a constant surface density of $\Sigma(r)dr \propto r^{-2}dr$, between 62 and 120 AU.
its model dependence should be noted. Mid-infrared and sub-mm suggest that it has both a cold and a $\eta$ extremely high infrared excess. Observations of Smith et al. (2009b) and Lisse et al. (2012) of Müller et al. (2010). No error bars are quoted on the mass, however, its model dependence should be noted.

Figure 12 clearly shows that by the age of Vega (455 ± 13 Myr) a very massive outer belt is required in order to sustain the high levels of dust observed. In general the required masses are higher than the observationally derived mass for the belt (shown by the diamond), or even the pre-collisional evolution initial mass of 55.5 $M_\oplus$ (Müller et al. 2010). Given that the plotted values assume that all material scattered inwards is converted to the observed small dust grains and thus are likely to underestimate the belt mass required, this places doubt on the ability of Vega’s outer belt to replenish the exozodi. Such a conclusion, should, however, be viewed in the light of the large uncertainties, in particular on the rate at which Vega’s exozodi needs to be replenished. A small decrease from the currently used value of $10^{-9}$ $M_\odot$/yr, would mean that a chain of low mass planets could readily scatter material at the required rates. Another possibility is that the scattering process in Vega started less than 455 Myr ago and therefore that the scattering rates are higher at the current epoch. To summarise, the uncertainties on the values of various parameters are sufficiently large that these simulations by no means rule out steady-state scattering by a chain of planets to replenish Vega’s exozodi, however, the evidence presented in favour of such scattering requires the existence of many closely spaced, terrestrial to Saturn mass planets, orbiting between the two belts.

4.4.2. $\eta$ Corvi

$\eta$ Corvi as a significantly older (1.4 ± 0.3 Gyr) system, with an extremely high infrared excess. Observations of $\eta$ Corvi in the mid-infrared and sub-mm suggest that it has both a cold and a warm component (Smith et al. 2009b; Chen et al. 2006; Wyatt et al. 2005). Both Smith et al. (2009b) and Lisse et al. (2012) find that the warm component is inside of 3.5 AU and Lisse et al. (2012) find that it can be explained by $9 \times 10^{18}$ kg $\sim 10^{-7}$ $M_\oplus$ of dust in particles between 0.1 and 100 $\mu$m in size, with a lifetime of 3–6 yrs against collisions. This suggests that this dust needs to be replenished at a rate of $10^{-6}$ $M_\odot$/yr in order to retain the current observed levels. Sub-mm observations of the outer belt, modelled in Wyatt et al. (2005) find a radius of 150 ± 20 AU and a mass of ~20 $M_\oplus$.

Again the scattering rates shown in Fig. 9 can be applied to $\eta$ Corvi, hypothesising the existence of chains of equal mass planets orbiting interior to the outer belt. Again, the planetary system of $\eta$ Corvi may differ radically from such chains of equal mass planets, nonetheless, such systems provide a useful upper limit on the possible scattering rates. In this case, the scattering rates determined in Fig. 9 apply at times greater by a factor $(130 \text{ AU})^{3/2}(1.4 \text{ AU})^{1/2} \sim 2.57$, to account for the difference in belt radius and stellar mass. The scattering rates now apply to chains of planets with slightly higher masses, scaled upwards by a factor of 1.4, as detailed in Table 3. The scattering rates now apply to a system with an exozodi at 2 AU, slightly inside the observed position of less than 3.5 AU, however, this could only potentially cause a small change in the calculated scattering rates.

The level of excess observed in this system, and therefore the replenishment rate required, is significantly higher than for Vega’s exozodi. This means that the minimum required outer belt mass to replenish the exozodi at $10^{-6}$ $M_\odot$/yr, shown in Fig. 13, are ridiculously high. This is clear evidence that the warm dust observed in $\eta$ Corvi is at levels far too high for it to be resupplied by the scattering of material inwards from the observed outer planetesimal belt by a chain of stable planets. Another explanation is required for this system.

5. Discussion

In this work we have considered some example planetary systems in order to investigate the hypothesis that high levels of exozodiacal dust observed in some planetary systems could be retained by material scattered inwards from an outer planetesimal belt. We used $N$-body simulations to determine the scattering rates from chains of equal mass planets, on circular, co-planar orbits, interior to an outer planetesimal belt. These were used to assess the validity of this hypothesis by comparison with observations. We used our simulations to outline the properties (mass and radius) of debris discs that are capable of scattering material inwards at sufficiently high rates, which were then compared with our ability to detect such discs and whether the masses are
consistent with collisional evolution. In general, this is highly dependent on the properties of individual systems and thus, the most definitive conclusions can only be made by comparison with observed systems, as was done here for Vega and τ Corvi. We now discuss some of the uncertainties that should be taken into account when considering the results presented in this work.

5.1. Uncertainties

The biggest uncertainty in these comparisons is the determination of the rate at which the exozodi must be supplied with material in order to retain the observed levels of exozodiacal dust. This is calculated from a fairly uncertain mass of dust in the exozodi, combined with an even more uncertain timescale on which this mass is supplied. This is calculated from a fairly uncertain mass of dust in the exozodi, combined with an even more uncertain timescale on which this mass is supplied. The best fit to the observed levels of exozodiacal dust is calculated from a fairly uncertain mass of dust in the exozodi, combined with an even more uncertain timescale on which this mass is supplied.

Thébault et al. (2003; Thébault & Augereau 2007; Krivov et al. 2006; Löhné et al. 2008) finds that the ratio of the total mass of the disc to the observed dust mass calculated using realistic size distributions does not differ significantly from simplistic estimates made using the size distribution from a steady state collisional cascade (n(D) ∝ D^(-3/2), Dohnanyi 1969, with a power index of α, Tanaka et al. 1996). Thus, the calculated values for the mass should not vary too dramatically. The biggest uncertainty is in the size of the largest body in the collisional cascade, which can alter the calculated mass significantly. It is also possible that larger bodies exist that are not yet in collisional equilibrium. These could contribute to the scattering process, but only in a stochastic manner. Given our total lack of information regarding such bodies, it seems unreasonable to invoke their contribution to the scattering rates, although, evidence exists in some systems that such stochastic collisions may produce the observed exozodi (Lisse et al. 2009, 2012).

The second biggest uncertainty in our calculations regards the conversion of the bodies scattered inwards from the outer belt, with a size distribution reflecting that of the outer belt, to the observed small dust. In order to obtain maximum possible scattering rates, we considered that this process is 100% efficient. There are three main processes by which larger bodies are converted to small dust, collisions, evaporation or spontaneous disruption. Marboeuf et al. (in prep.) investigated in detail the evaporation of comets as a potential mechanism to produce exozodiacal dust. They find that it is reasonably efficient in high luminosity systems, with a maximum possible efficiency that reflects the dust/ice ratio in the comets (generally about 1, so 50% efficient). Dust may also be produced as larger bodies are ground down by collisions, or cometary bodies may spontaneously disrupt, as suggested as an explanation for the solar system’s zodiacal cloud (Nesvorný et al. 2010). None of these processes will be 100% efficient at converting large bodies to the observed small grains. In this work, we merely note that where outer belt masses have been calculated, these are very much minimum values, rather than attempting to make any conclusions regarding the conversion of the scattered bodies to the observed small dust.

There are then several uncertainties based on the initial conditions used in our simulations, which were discussed in detail in Sect. 3.3. It is, however, worth reiterating a dependence of our results, on the fact that planetesimals remain on orbits such that they can be scattered by the planet, at the end of planet formation. Should this prove not to be the case, whether due to planetary migration, or an inaccurate estimation of the parameter that we used to characterise this clearing, our scattering rates will only decrease. Again, reiterating the fact that the outer planetesimal belt masses determined by our simulations are very much minimum values. We also assumed that all planets were fully formed at t = 0, which of course is not generally true, particularly for terrestrial mass planets. During terrestrial planet formation, the scattering processes are likely to be similar to those seen in our simulations, albeit controlled by the somewhat smaller planetary core. Thus, we do not anticipate that our results would be significantly altered if planet formation was only completed some time after t = 0.

Of potential concern is how representative our example systems are of the full range of real planetary systems. Such well ordered planetary systems are unlikely to be found (often) in nature. In particular, it is unlikely that planet formation would have been equally efficient throughout any planetary system. They should, however, be representative of the range of scattering rates possible from the full range of real planetary systems, as a function of time. This hypothesis is supported by test simulations of two further planetary systems, with random architectures, which were found to scatter material inwards at rates that lie neatly within the range of scattering rates found for our example systems. As discussed, for example in Sects. 4.1 or 4, it is easy to design planetary systems with “blockages” where the scattering rates tend to zero. However, given our understanding of the dependence of the scattering rates on the planet masses and separations (see discussion in Sect. 4.1), we anticipate that very few systems can scatter material inwards after millions of years of evolution, at rates higher than those outlined here for a chain of tightly packed Neptune mass planets (given constraints on the outer belt mass, stellar mass, age etc.). It is, however, still possible that a few very specific architectures exist where the scattering rates are enhanced beyond those seen in our simulations, for example due to resonant interactions. Alternatively systems with eccentric planets or planetesimals may prove to scatter material inwards at higher rates, although test simulations suggest that they can only do so on short timescales.

There are two other potential contributors to the scattering rates, that we have ignored so far. Both contribute at such low levels that we feel justified in leaving them out of our calculated rates. The first is particles that started on orbits between the planets. If the planets are sufficiently widely separated, it may be that some material was left orbiting between the planets, rather than being accreted onto the planets. In general such planetesimals are scattered on short timescales, however, if the separation of the planets is larger than their dynamical influence, i.e. ΔR_{H} > ΔR_{chaos}, planetesimals may remain on stable orbits between the planets, even on long timescales. The scattering
process for such planetesimals is very similar to that for the outer planet in our simulations, except on shorter timescales, given the shorter orbital periods. Thus, at late times the contribution of such particles is likely to be small. The only question therefore is whether such belts of planetesimals, or indeed planetesimals in the process of being scattered inwards, may be detectable.

The second potential contribution is from particles that started far outside of the outer planet’s chaotic zone and are scattered on long timescales. In a multi-planet system, the dynamics are more complicated and there are a range of secular and multi-body resonances that can influence particles in the belt. These have been shown to provide a small flux of material into Neptune’s chaotic zone in our solar system (e.g. Duncan et al. 1995; Holman & Wisdom 1993; Levison & Duncan 1997; Emel’yanenko et al. 2004; Morbidelli 1997). This contribution cannot be significant as in our simulations to test this effect with a particle density of 50 particles per AU, not a single particle, that started outside of $a_{\min} = a_{p1} + 2\Delta a_{\max}$ and inside of 100 AU, was scattered inwards, although there was evidence of the effect of the inner planets on the outer regions of the belt.

5.2. Comparison with real planetary systems

All of the potential uncertainties discussed in the preceding section need to be taken into account when comparing the results of our simulations with observed exozodi. In Fig. 11 we determined the mass and radius required for the outer belt, such that it can scatter material to the location of the exozodi at a sufficiently high rate. These requirements could change significantly, for example, if our estimate on the rate at which material needs to be scattered inwards was wrong, or the conversion of the scattered large bodies to small dust is inefficient. Changes of several orders of magnitude are already seen between the example systems considered here. Given a diversity of planetary systems, this would naturally result in a diverse population of exozodi, that could help to explain the range of exozodi detections and non-detections found so far. These uncertainties render insignificant the possible differences in the scattering rates caused by the unrealistic assumption that the radial location of the exozodi scales with that of the outer belt.

A general conclusion from Fig. 11 is that the longer lifetimes and scattering timescales of large radii outer belts are required to sustain high scattering rates on long timescales. Unfortunately the population of large radii debris discs is the least well constrained, although sub-mm instruments such as ALMA and SCUBA2 may shed light on this in the near future. For a more detailed comparison, we considered two example systems, Vega (Sect. 4.4.1) and Corvi (Sect. 4.4.2). For Corvi, the mass of observed outer belt is orders of magnitude too low to retain the exozodi at its currently observed levels and it therefore seems more likely that there is another explanation for this system. For Vega, the replenishment of the exozodi by a chain of planets seems unlikely, but given the uncertainties discussed above, it is not ruled out, although very specific constraints on the system would be required.

Our $N$-body simulations necessarily only consider a very limited range of all possible planetary system architectures. We consider these to be a fair representation of the range of scattering rates possible in any arbitrary planetary system, and discussed their application to any planetary system in detail in Sect. 4.1. However, it still remains possible that we have missed some very specific architecture involving unequally spaced planetesimals of different masses, potentially on eccentric or inclined orbits, that is significantly more efficient at scattering material, for example where secular or mean motion resonances enhance the scattering rates. However, within the limitations of reasonable computing timescales, a full investigation was not possible in this work.

5.3. Application to unstable systems

The results presented in this work find high scattering rates for the first thousands or millions of years of a system’s evolution, but much lower rates in stable planetary systems after hundreds of millions of years. However, there is a potential way to get high, albeit temporary, scattering rates in such older mature systems. This could happen if the empty chaotic region surrounding a planet is refilled with fresh material. A way to achieve this is if the planet is displaced from its current orbit by a dynamical instability and scattered into a planetesimal belt, or if it migrates into such a planetesimal belt at late times. Such processes could restart the scattering processes and significantly increase the scattering rates. From our simulations, we can estimate that the scattering rates could remain high, even for thousands to millions of years after such an event. However, this is only an estimate because we did not consider any test particles closer to the planet than $a_{\min} = a_{p1} + \Delta a_{\max}$ and if the chaotic zone were refilled with planetesimals after an instability, it is likely that the planetesimal belt will be cold. Further detailed work is required to investigate this hypothesis.

6. Conclusions

In this work we have considered the conundrum that high levels of exozodiacal dust are observed in some systems, despite it being clear that such small dust has very short lifetimes against collisions or radiative forces. We considered the hypothesis that the exozodiacal dust could be replenished by material from an outer belt, scattered inwards by planets. We presented $N$-body simulations that calculate the efficiency of scattering by a chain of equal mass planets, in a way that can be applied to a wide range of different planetary systems, irrespective of whether or not exozodiacal dust has been detected. The outer planet scatters planetesimals as it sculpts the inner edge of the planetesimal belt. Particles are cleared from the chaotic zone on relatively short timescales, but these particles may continue to be scattered multiple times by the planet, evolving at constant pericentre or apocentre, until they are scattered sufficiently far inwards that they are passed onto an interior planet or ejected. In this manner particles can be passed along a chain of planets and may only reach the location of the exozodi, some after hundreds of millions of years.

Our simulations show that it is possible for this scattering to be at a sufficiently high rate that it could retain the currently observed levels of exozodiacal dust. This, however, places very stringent constraints on the architecture of the planetary system, namely that it contain a chain of closely spaced, low-mass planets orbiting interior to a massive, large radii outer planetesimal belt. Without a complete census of the architecture of planetary systems and/or detailed statistics about the exozodi population, it is difficult to make definitive conclusions about the proportion of systems in which this scenario could apply. We considered in detail two systems with observed outer belts and exozodi, and we hypothesise that there may be as yet undetected planets orbiting between the observed exozodi and outer belt. We find that for Corvi, an old, sun-like star with very high levels of infrared excess, that the exozodi cannot be retained at its current levels, on
Gyr timescales, with this process, whereas for Vega a very contrived architecture would be required for the planetary system to retain the levels of exozodiacal dust observed around Vega.

In general, in this work we show that material is scattered into the inner systems of many planetary systems, at rates that depend on the architecture of the planetary system, but are in general low, particularly after hundreds of millions of years. We put this forward as an explanation for the observations of high levels of exozodiacal dust, but find that sufficient material is only scattered inwards in systems with very contrived architectures. An alternative solution for, particularly the older planetary systems with exozodiacal dust, could be that we are observing these systems in the aftermath, albeit the long aftermath, of a dynamical instability that led to a planet being scattered into the outer belt.

Acknowledgements. We thank Dimitri Veras, Hervé Beust, Virginie Faramaz, Jérémy Lébreton, Julien Vanderportal, Quentin Kral and Olivier Absil for discussions that contributed to this work. We acknowledge the support of the ANR-2010 BLAN-0505-01 (EXOZODI). Computations presented in this paper were performed at the Service Commun de Calcul Intensif de l’Observatoire de Grenoble (SCCI) on the super-computer funded by Agence Nationale pour la Recherche under contracts ANR-07-BLAN-0221, ANR-2010-JCJC-0504-01 and ANR-2010-JCJC-0501-01.

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