

# Fragmentation in the massive star-forming region IRAS 19410+2336<sup>★,★★</sup>

J. A. Rodón<sup>1</sup>, H. Beuther<sup>2</sup>, and P. Schilke<sup>3</sup>

<sup>1</sup> European Southern Observatory, Alonso de Córdova 3107, Vitacura, 19001 Casilla, Santiago 19, Chile  
e-mail: jrodon@eso.org

<sup>2</sup> Max-Planck-Institut für Astronomie, Königstuhl 17, 69117 Heidelberg, Germany

<sup>3</sup> I. Physikalisches Institut, Universität zu Köln, Zùlpicherstr. 77, 50937 Köln, Germany

Received 27 July 2009 / Accepted 12 June 2012

## ABSTRACT

**Context.** The core mass functions (CMFs) of low-mass star-forming regions are found to resemble the shape of the initial mass function (IMF). A similar result is observed for the dust clumps in high-mass star-forming regions, although on spatial scales of clusters that do not resolve the substructure that is found in these massive clumps. The region IRAS 19410+2336 is one exception, having been observed on spatial scales on the order of  $\sim 2500$  AU, which are sufficient to resolve the clump substructure into individual cores. **Aims.** We investigate the protostellar content of IRAS 19410+2336 at high spatial resolution at 1.4 mm, determining the temperature structure of the region and deriving its CMF.

**Methods.** The massive star-forming region IRAS 19410+2336 was mapped with the PdBI (BCD configurations) at 1.4 mm and 3 mm in the continuum and several transitions of formaldehyde ( $\text{H}_2\text{CO}$ ) and methyl cyanide ( $\text{CH}_3\text{CN}$ ). The  $\text{H}_2\text{CO}$  transitions were also observed with the IRAM 30 m Telescope.

**Results.** We detect 26 continuum sources at 1.4 mm with a spatial resolution as low as  $\sim 2200$  AU, several of them with counterparts at near- and mid-infrared wavelengths, distributed in two (proto)clusters. With the PdBI  $\text{CH}_3\text{CN}$  and PdBI/IRAM 30 m  $\text{H}_2\text{CO}$  emission, we derive the temperature structure of the region, ranging from 35 K to 90 K. Using these temperatures, we calculate the core masses of the detected sources, ranging from  $\sim 0.7 M_\odot$  to  $\sim 8 M_\odot$ . These masses are strongly affected by the spatial filtering of the interferometer, which removes a common envelope with  $\sim 90\%$  of the single-dish flux. Considering only the detected dense cores and accounting for binning effects as well as cumulative distributions, we derive a CMF, with a power-law index  $\beta = -2.3 \pm 0.2$ . We resolve the Jeans length of the (proto)clusters by one order of magnitude, and only find a small velocity dispersion between the different subsources.

**Conclusions.** Since we cannot unambiguously differentiate between protostellar and prestellar cores, the derived CMF is not prestellar. Furthermore, because of the large fraction of missing flux, we cannot establish a firm link between the CMF and the IMF. This implies that future high-mass CMF studies will need to complement the interferometer continuum data with the short spacing information, a task suitable for ALMA. We note that the method of extracting temperatures using  $\text{H}_2\text{CO}$  lines becomes less applicable when reaching the dense core scales of the interferometric observations because most of the  $\text{H}_2\text{CO}$  appears to originate in the envelope structure.

**Key words.** stars: formation – instrumentation: high angular resolution – instrumentation: interferometers – ISM: individual objects: IRAS 19410+2336

## 1. Introduction

Our understanding of the structure of the cold, dense interstellar medium (ISM) in star-forming regions has improved in the past few years. In these regions, the ISM exhibits a clumpy, often filamentary structure with density maxima at the sites of star formation. To represent this structure quantitatively, we use the core mass function (CMF). In this paper, we refer to “core” as the small (diameter  $D \sim 0.01$  pc), dense condensation that will form individual stars or small multiple systems, while with “clump” we denote structures that may form (proto)clusters and therefore be more massive and larger than cores. In this sense, cores may be considered as a subset of clumps.

Sub-mm observations of low-mass star-forming regions such as Serpens (e.g., Testi & Sargent 1998), Orion B

(e.g., Motte et al. 2001), Aquila (e.g., Könyves et al. 2010), and  $\rho$  Oph (e.g., Motte et al. 1998), as well as near-infrared (NIR) extinction maps (e.g., Alves et al. 2007), show that their CMFs resemble the shape and intrinsic mass scale of the stellar initial mass function (IMF; e.g., Salpeter 1955; Kroupa 2002). This suggests that these dense cores are the immediate precursors of stars, and that by applying a more or less constant core-to-star mass conversion efficiency we can obtain the IMF from the CMF.

In the case of massive star-forming (MSF) regions, we have, for example, the analysis of Reid & Wilson (2006). They gathered the published masses of the MSF regions M8 (e.g., Tothill et al. 2002), M17 (e.g., Reid & Wilson 2006), NGC 7538 (e.g., Reid & Wilson 2005), W43 (e.g., Motte et al. 2003), and RCW 106 (e.g., Mookerjee et al. 2004), tracing spatial scales of clumps that correspond to (proto)clusters rather than to individual cores, and tested the fit of several functional forms for their clump mass functions. They found that in those cases, the best fit was obtained by a double power law that for the high-mass end had a mean power-law exponent consistent with the Salpeter IMF. This would again imply that by an almost one-to-one mass

\* Based on observations carried out with the IRAM Plateau de Bure Interferometer and the IRAM 30 m Telescope. IRAM is supported by INSU/CNRS (France), MPG (Germany), and IGN (Spain):

\*\* Data cubes in FITS format are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/545/A51>

conversion efficiency the IMF could be obtained from the clump mass function, as in the case for low-mass star-forming regions. A similar analysis were conducted by e.g., Shirley et al. (2003) and Beltrán et al. (2006). Furthermore, a reinterpretation by Chabrier & Hennebelle (2010) of a study by Smith et al. (2009) of the relationship between the CMF and the IMF suggests that there is a tight correlation between the two. Once more, this implies that the IMF is defined by the CMF in the early stages of evolution.

However, this one-to-one relationship may not hold as, for example, some clumps must fragment to produce the observed quantity of multiple stellar systems (Goodwin et al. 2007). The relatively large distances ( $\geq 2$  kpc) of most of the known MSF regions require a spatial resolution of about  $1''$  to resolve the clumps into cores with sizes below  $\sim 0.1$  pc. That resolution in the (sub)mm regime is only achievable with the interferometric technique. So far, only a few MSF regions have been observed in the (sub)mm with spatial resolutions good enough to resolve individual cores (e.g., Bontemps et al. 2010; Fontani et al. 2009; Rodón et al. 2008; Rathborne et al. 2008; Beuther et al. 2006), and for only one source, IRAS 19410+2336, has it been possible to determine a CMF (Beuther & Schilke 2004).

The young MSF region IRAS 19410+2336 is at a distance of 2.16 kpc (Xu et al. 2009) and has an integrated bolometric luminosity of about  $10^4 L_{\odot}$ . It is a very active star-forming site, with sources detected from X-rays down to radio wavelengths. It has  $\text{H}_2\text{O}$  and  $\text{CH}_3\text{OH}$  maser emission (Sridharan et al. 2002; Beuther et al. 2002d) and X-ray sources (Beuther et al. 2002a), indicating that there is ongoing formation of intermediate-to-high mass stars. The region is embedded within a cluster of over 800 components detected at NIR wavelengths (Martín-Hernández et al. 2008; Qiu et al. 2008), and it has a rich and energetic outflow component with multiple outflows detected in CO (Beuther et al. 2002c, 2003). Beuther et al. (2002b) found that the large-scale mm emission shows two massive gas clumps roughly aligned in a north-south direction that splits into several subsources with increasing spatial resolution (Beuther & Schilke 2004).

With their studies of the mm continuum at high spatial resolution, Beuther & Schilke (2004) were able to derive the mass function of IRAS 19410+2336, resulting in a Salpeter-like distribution. However, the strongest caveat in the derivation of that mass function was that a uniform dust temperature was used in the calculation of the masses. Although they argue that the dust temperature distribution should not vary strongly, they also warn that changes in the temperature of the cores would result in a somewhat flatter slope.

We have revisited IRAS 19410+2336 by observing its mm continuum at high-spatial resolution and obtaining molecular-line emission of known temperature tracers, to determine via several methods its temperature structure and in the end derive a more robust mass function.

## 2. Observations

### 2.1. Interferometric

We observed the two protostellar clusters of IRAS 19410+2336 with the PdBI in the *B* (Feb.-2005), *C* (Dec.-2004/Mar.-2005), and *D* (Apr.-2005) configurations, comprising baselines from 20 m to 330 m. This translates into projected baselines ranging from  $\sim 7$  k $\lambda$  to  $\sim 120$  k $\lambda$  at 3 mm and from  $\sim 15$  k $\lambda$  to  $\sim 240$  k $\lambda$  at 1.4 mm. The phase centers were set at RA(J2000) =  $19^{\text{h}}43^{\text{m}}10.7^{\text{s}}$ ; Dec(J2000) =  $23^{\circ}44'58.4''$  for the

**Table 1.** Observed molecular transitions and rms of the respective maps.

Transition	$\nu$ (GHz)	Spectral Resol. (MHz)	$E_{\text{up}}$ (K)	rms <sup>a</sup> (mJy beam <sup>-1</sup> )	
				North	South
$\text{CH}_3\text{CN} (6_0-5_0)$	110.383	0.18	18.5	10	17
$\text{CH}_3\text{CN} (6_1-5_1)$	110.381	0.18	25.7	10	17
$\text{CH}_3\text{CN} (6_2-5_2)$	110.375	0.18	47.1	10	14
$\text{CH}_3\text{CN} (6_3-5_3)$	110.364	0.18	82.9	10	14
$\text{H}_2\text{CO} (3_{0,3}-2_{0,2})^b$	218.222	0.36	21.0	29	36
$\text{H}_2\text{CO} (3_{2,2}-2_{2,1})^b$	218.476	0.36	68.1	19	30
$\text{H}_2\text{CO} (3_{2,1}-2_{2,0})$	218.760	0.36	68.1	23	34

**Notes.** (a) For a spectral resolution of  $0.5 \text{ km s}^{-1}$ ; (b) rms values obtained after combining 30 m and PdBI data.

“northern” (proto)cluster and at RA(J2000) =  $19^{\text{h}}43^{\text{m}}11.2^{\text{s}}$ ; Dec(J2000) =  $23^{\circ}44'03.2''$  for the “southern” (proto)cluster. The continuum was mapped at 3 mm and 1.4 mm.

The 3 mm receiver was tuned in the upper sideband and the 1.4 mm receiver in the lower sideband. With this spectral setup, we observed the  $\text{H}_2\text{CO}$  and  $\text{CH}_3\text{CN}$  transitions described in Table 1 with a maximum spectral resolution of  $0.5 \text{ km s}^{-1}$ , adopting a systemic velocity  $V_{\text{LSR}} = 22.4 \text{ km s}^{-1}$  (Ridge & Moore 2001; Tieftrunk et al. 1998).

The phase and amplitude calibrators were 1923+210 and 2023+336 and the flux calibrators were 3C 273, 2200+420, 1749+096 and 1741-038, adopting for the calibration the flux values from the SMA flux monitoring of these quasars<sup>1</sup>. The data were calibrated with CLIC and then imaged with MAPPING, which are both part of the GILDAS package<sup>2</sup>. The spectra were processed with CLASS90, which is also from the GILDAS package.

After imaging and deconvolution, the resulting synthesized beams for the continuum data are  $1.2'' \times 0.8''$  at 1.4 mm and  $2.2'' \times 1.6''$  at 3 mm. At the given distance of 2.2 kpc, this means a spatial resolution of  $\sim 2200$  AU and  $\sim 4200$  AU, respectively. The continuum data for the northern (proto)cluster have rms noise levels of  $\sigma \sim 0.8 \text{ mJy beam}^{-1}$  and  $\sigma \sim 0.4 \text{ mJy beam}^{-1}$  at 1.4 mm and 3 mm, respectively, while in the southern (proto)cluster the rms noise levels are  $\sigma \sim 1.0 \text{ mJy beam}^{-1}$  and  $\sigma \sim 0.4 \text{ mJy beam}^{-1}$  at 1.4 mm and 3 mm, respectively. For the line data, the synthesized beams and noise levels are detailed in Table 1.

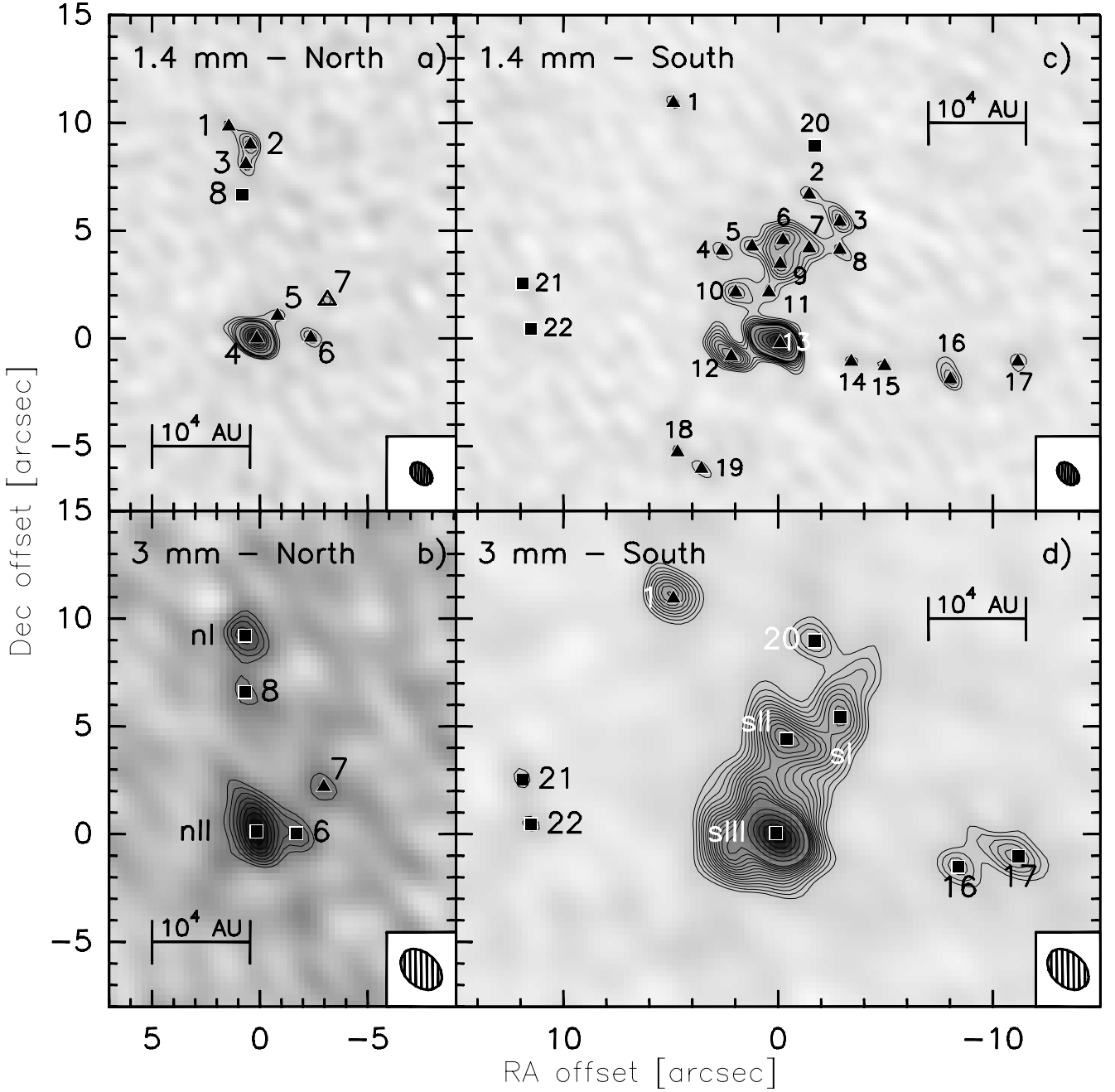
### 2.2. Short spacings

We obtained IRAM 30 m observations of  $\text{H}_2\text{CO} (3_{0,3}-2_{0,2})$  and  $\text{H}_2\text{CO} (3_{2,2}-2_{2,1})$  towards IRAS 19410+2336 in November 2007, which were taken in the on-the-fly mode with both HERA heterodyne receivers tuned at 218.222 GHz. For the backend, we used the VESPA correlator, assigning 2 of its spectral bands to each HERA receiver, with a channel spacing of 320 kHz and a bandwidth of 80 MHz, resulting in a spectral resolution of  $0.5 \text{ km s}^{-1}$  at 218 GHz.

The data were processed with CLASS90. The single-dish uv-data were combined with the interferometric uv-data using MAPPING. After imaging and deconvolution we obtained a synthesized beam of  $1.6'' \times 1.0''$  for the combined data. The rms levels of the combined data are shown in Table 1.

<sup>1</sup> <http://sma1.sma.hawaii.edu/callist/callist.html>

<sup>2</sup> <http://www.iram.fr/IRAMFR/GILDAS>



**Fig. 1.** Continuum maps of IRAS 19410+2336 obtained with the PdBI. In the *top* row are the 1.4 mm maps of the northern (panel **a**) and southern (panel **c**) (proto)clusters. Similarly, in the *bottom* row are the 3 mm maps of the northern and southern (proto)clusters in panels **b**) and **d**), respectively. The contouring starts at the  $4\sigma$  level in all the panels. Contours in panel **a**) increase in  $1\sigma$  steps up to  $8\sigma$  and in  $4\sigma$  steps afterwards, in panel **b**) in  $4\sigma$  steps, in panel **c**) in  $1\sigma$  steps up to  $11\sigma$ , and in  $4\sigma$  steps afterwards, and in panel **d**) in  $1\sigma$  steps up to  $16\sigma$  and in  $4\sigma$  steps afterwards. See Table 2 for the  $\sigma$  values. The triangles mark the position of the sources detected at 1.4 mm, while the squares are the sources detected at 3 mm. A square appearing in a 1.4 mm map indicates a source that is only detected at 3 mm. Similarly, a triangle in a 3 mm map signals a source detected at the same position in a 1.4 mm map.

### 3. Results

#### 3.1. Millimetric continuum

We established a detection threshold of  $4\sigma$  in our 1.4 mm continuum maps, corresponding to  $\sim 4 \text{ mJy beam}^{-1}$ ,  $M \sim 1 M_{\odot}$ <sup>3</sup>, and  $N(\text{H}_2) \sim 6 \times 10^{23} \text{ cm}^{-2}$  in the southern (proto)cluster, and  $\sim 3.2 \text{ mJy beam}^{-1}$ ,  $M \sim 0.8 M_{\odot}$ , and  $N(\text{H}_2) \sim 4.5 \times 10^{23} \text{ cm}^{-2}$  in the northern (proto)cluster. In the latter, we detect 7 sources, while in the former there are 19 sources detected. Figure 1 shows

the 1.4 mm and 3 mm continuum maps for both (proto)clusters, with the 26 sources detected at 1.4 mm marked with triangles and the two sources only detected at 3 mm marked with squares.

The properties of the sources are summarized in Table 2. Columns 2 and 3 give their absolute positions, the measured peak flux intensity and integrated flux density are given in Cols. 4 and 5, respectively. For the unresolved sources, their angular size is typically smaller than the synthesized beam at the respective wavelength.

Because the brightness temperature at 1.4 mm of the corresponding Planck function for the strongest source in the region

<sup>3</sup> For  $T_k \sim 40 \text{ K}$  (see Sects. 3.1 and 4.1.2 for more details).

**Table 2.** Properties of the continuum mm sources in IRAS 19410+2336.

Source	RA (J2000)	Dec (J2000)	$I_\nu$ (mJy beam <sup>-1</sup> )	$S_\nu$ (mJy)	$T_k^a$ (K)	Mass ( $M_\odot$ )	$N(\text{H}_2)$ ( $10^{23}$ cm <sup>-2</sup> )	$A_\nu$ ( $10^3$ mag)	Flags
1.4 mm with a $1.2'' \times 0.8''$ beam									
1-s ...	19 43 11.553	23 44 14.15	4.8	...	35	1.5	8.2	0.9	<i>u</i>
2-s ...	19 43 11.093	23 44 09.90	5.7	...	35	1.7	9.6	1.0	<i>u</i>
3-s ...	19 43 10.989	23 44 08.64	8.1	8.3	35	2.5	14	1.5	
4-s ...	19 43 11.387	23 44 07.29	5.3	...	35	1.6	9.0	1.0	<i>u</i>
5-s ...	19 43 11.286	23 44 07.49	6.2	...	35	1.9	10	1.1	<i>u</i>
6-s ...	19 43 11.182	23 44 07.78	1.1	16	35	4.9	19	2.0	
7-s ...	19 43 11.093	23 44 07.41	7.6	7.7	35	2.4	13	1.4	
8-s ...	19 43 10.989	23 44 07.33	5.6	...	35	1.7	9.4	1.0	<i>u</i>
9-s ...	19 43 11.191	23 44 06.68	1.0	14	35	4.3	17	1.8	
10-s ...	19 43 11.342	23 44 05.37	7.2	11	35	3.4	12	1.3	
11-s ...	19 43 11.229	23 44 05.37	5.6	...	35	1.7	9.5	1.0	<i>u</i>
12-s ...	19 43 11.357	23 44 02.39	1.3	24	45	5.5	17	1.8	
13-s ...	19 43 11.191	23 44 03.00	4.2	75	90	8.1	25	2.7	
14-s ...	19 43 10.950	23 44 02.15	4.6	...	35	1.4	7.8	0.8	<i>u</i>
15-s ...	19 43 10.837	23 44 01.94	4.8	...	35	1.5	8.1	0.9	<i>u</i>
16-s ...	19 43 10.614	23 44 01.33	7.3	...	35	2.2	13	1.4	<i>u</i>
17-s ...	19 43 10.385	23 44 02.15	5.1	...	35	1.6	8.7	1.0	<i>u</i>
18-s ...	19 43 11.539	23 43 57.94	4.6	...	35	1.4	7.8	0.8	<i>u</i>
19-s ...	19 43 11.458	23 44 57.17	5.3	...	35	1.6	9.0	1.0	<i>u</i>
1-n ...	19 43 10.801	23 45 08.26	3.4	...	35	1.0	5.8	0.6	<i>u</i>
2-n ...	19 43 10.728	23 45 07.41	6.1	...	35	1.9	11	1.0	<i>u</i>
3-n ...	19 43 10.743	23 45 06.51	4.5	...	35	1.4	7.6	0.8	<i>u</i>
4-n ...	19 43 10.706	23 44 58.42	2.7	32	60	5.3	25	2.7	
5-n ...	19 43 10.636	23 44 59.48	3.6	...	50	0.7	4.1	0.4	<i>u</i>
6-n ...	19 43 10.524	23 44 58.45	4.7	...	35	1.4	7.9	0.8	<i>u</i>
7-n ...	19 43 10.469	23 45 00.2	3.6	...	35	1.1	6.1	0.6	<i>u</i>
3 mm with a $2.2'' \times 1.6''$ beam									
1-s ...	19 43 11.558	23 44 14.41	5.1	...	40	19.9	32	3.4	<i>u</i>
20-s ...	19 43 11.073	23 44 12.23	3.1	...	40	12.1	19	2.1	<i>u, n</i>
c3mm-sI ...	19 43 10.986	23 44 08.67	4.8	6.7	40	26.2	29	3.1	c(2, 3, 8-s)
c3mm-sII ...	19 43 11.170	23 44 07.64	6.6	13	40	50.8	40	4.2	c(5, 6, 7, 9-s)
c3mm-sIII ...	19 43 11.206	23 44 03.29	17.7	48	40	187.5	102	10.8	c(10, 11, 12, 13-s)
16-s ...	19 43 10.587	23 44 01.71	2.9	...	40	11.2	18	1.9	<i>u</i>
17-s ...	19 43 10.382	23 44 02.20	3.5	3.9	40	15.2	22	2.3	
21-s ...	19 43 12.066	23 44 05.76	2.0	...	40	7.9	12	1.3	<i>u, n</i>
22-s ...	19 43 12.037	23 44 03.68	2.0	...	40	7.7	12	1.3	<i>u, n</i>
c3mm-nI ...	19 43 10.746	23 45 07.63	3.2	...	40	12.7	20	2.1	<i>u, c(1, 2, 3-n)</i>
8-n ...	19 43 10.746	23 45 05.01	1.9	...	40	7.5	12	1.2	<i>u, n</i>
c3mm-nII ...	19 43 10.707	23 44 58.54	5.1	7.4	40	29.0	31	3.3	c(4, 5-n)
6-n ...	19 43 10.573	23 44 58.47	2.6	...	40	10.2	16	1.7	<i>u</i>
7-n ...	19 43 10.480	23 45 00.61	2.2	...	40	8.5	13	1.4	<i>u</i>

**Notes.** The last column indicates unresolved cores (*u*) and detections at 3 mm without a 1.4 mm counterpart (*n*). The c(X, Y, Z) flag indicates that the source is the unresolved combination of sources X, Y, and Z. If the source is unresolved, its mass in Col. 7 is calculated with the peak intensity value of Col. 4. <sup>(a)</sup> Derived from the H<sub>2</sub>CO emission, the 3 mm temperatures are the average in the region (see Sect. 4.1.2). The values for the 1.4 mm cores are the same as in Table 3, and are repeated here just for reading convenience.

is about 2 K, merely ~2% of the typical hot core temperatures being ~100 K, we were able to assume that the emission comes from optically thin dust and thus calculate the masses and column densities with the approach outlined by Hildebrand (1983) and adapted by Beuther et al. (2002b, 2005). We adopted a distance of 2.2 kpc, and used a grain emissivity index  $\beta = 2$ , corresponding to a dust opacity per unit mass of  $\kappa_{1.4\text{mm}} \sim 0.3$  and  $\kappa_{3\text{mm}} \sim 0.08$  cm<sup>2</sup> g<sup>-1</sup> for a median grain size  $a = 0.1$   $\mu\text{m}$ , a grain

mass density  $\rho = 3$  g cm<sup>-3</sup>, and a gas-to-dust ratio of 186 (Draine et al. 2007).

The selected value of  $\beta = 2$  for the grain emissivity index is the value assumed by Beuther & Schilke (2004; see also Beuther et al. 2005) and the typical value found for the ISM dust (e.g., Hildebrand 1983; Ossenkopf & Henning 1994; Rodmann et al. 2006). Generally,  $\beta$  is thought to range from 1 to 2. When an IR-to-mm SED is available, as is the case now with *Herschel*



results, authors have found  $\beta$  values in that range and even higher. Examples are  $\beta \sim 1.2$  and  $1.5$  in Rathborne et al. (2008), or  $\beta \sim 1.7$ – $3.3$  in Anderson et al. (2010) and  $\beta \sim 1.0$ – $1.8$  in Rodón et al. (2010). For IRAS 19410+2336, there is no data available to directly calculate the dust opacity index. Therefore, in this work we adopted  $\beta = 2$ .

In contrast to the bolometer observations of the single dish data (see below), the interferometric continuum data are produced from the line-free part of the spectrum, therefore line contribution to the emission is negligible. Potential contribution from free-free emission is insignificant as well, since the flux at cm wavelengths is on the 1 mJy level and towards only the central source in the south, with no emission being detected from the other sources (Beuther et al. 2003). Therefore, we can safely assume that the mm continuum from which the masses are calculated is not severely contaminated by free-free emission.

The calculated masses and  $H_2$  column densities are in Cols. 7 and 8 of Table 2, respectively. For their calculation, we assumed the temperatures shown in Col. 11 of Table 3. These temperatures were determined from the measured  $H_2CO$  line ratios, following the procedure explained and discussed in Sect. 4.2. The visual extinctions in Col. 9 were calculated assuming  $A_v = N(H_2)/0.94 \times 10^{21}$  (Frerking et al. 1982).

The masses obtained are strongly affected by the spatial filtering inherent to interferometers. While varying dust properties may account for some of the discrepancy between the masses calculated at 1.4 mm and 3 mm, the spatial filtering is most likely the main cause. Comparison with single-dish continuum observations of IRAS 19410+2336 at 1.2 mm acquired with the IRAM 30 m Telescope (Beuther et al. 2002b) shows that in our 1.4 mm continuum map of the southern (proto)cluster we are recovering only  $\sim 6\%$  of the flux estimated with single dish observations. On the other hand, at 3 mm we recover a relatively larger amount of the single dish flux,  $\sim 37\%$ . This demonstrates that a large fraction of the mass is contained in extended structures, which we filter out.

The different percentage of flux filtered out in each wavelength band can be explained in the same way as the large (up to a factor  $\sim 10$ ) difference between the calculated masses at 1.4 mm and 3 mm. Both wavelengths were observed at the same time with the same interferometer configurations meaning that although the ground baselines are the same, the uv coverage measured in units of wavelength ( $k\lambda$ ) at 3 mm is more compact than at 1.4 mm, therefore traces more extended components in the region.

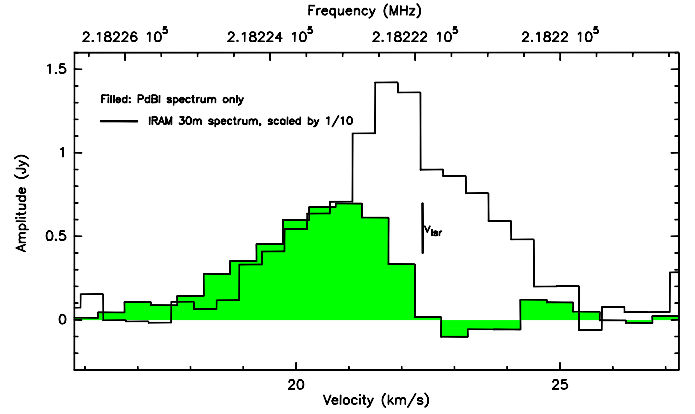
In the following, we assume that the missing flux is smoothly distributed and affects all cores in the same way. This assumption has one important caveat when deriving a CMF at high-spatial resolution, which is described in more detail in Sect. 5.4.

### 3.2. Formaldehyde

To estimate the temperature structure of IRAS 19410+2336, we observed three  $H_2CO$  transitions known to be usable as a gas thermometer (e.g., Mangum & Wootten 1993, see Sect. 4.2).

Since the PdBI data are clearly affected by missing short spacings (an example of this is shown in Fig. 2), the region was also observed with the IRAM 30 m telescope. Figure 3 shows the integrated intensity maps of the combined PdBI+IRAM 30 m data.

Of the three detected  $H_2CO$  lines,  $H_2CO(3_{0,3}-2_{0,2})$  and  $H_2CO(3_{2,2}-2_{2,1})$  are the ones with the highest signal-to-noise ratio. According to Mangum & Wootten (1993), these two transitions are enough to determine temperatures, therefore we did



**Fig. 2.** Comparison of the interferometer (PdBI, filled) and single-dish (IRAM 30 m, solid line)  $H_2CO(3_{0,3}-2_{0,2})$  line emission towards IRAS 19410+2336. Clearly seen is the “self-absorption”-like feature in the PdBI emission, denoting the missing flux coming from more extended spatial-scales and filtered out by the interferometer. The single-dish spectrum has been scaled down for comparison by a factor of ten.

not use the third detected transition,  $H_2CO(3_{2,1}-2_{2,0})$ , for the temperature analysis.

Both  $H_2CO(3_{0,3}-2_{0,2})$  and  $H_2CO(3_{2,2}-2_{2,1})$  have their strongest emission towards the brightest mm source detected in the continuum in both the north and south (proto)clusters. The secondary peaks in all the maps are in the same spatial region as the continuum emission, although there is no spatial correlation between the secondary peaks in the  $H_2CO$  and dust emission. This prevents us from obtaining a temperature for each individual core.

There is an emission feature seen in the northern cluster in both  $H_2CO(3_{0,3}-2_{0,2})$  and  $H_2CO(3_{2,2}-2_{2,1})$  transitions  $\sim 4''$  southeast of the main peak, which is marked with a star in the upper panels of Fig. 3. The feature is at rest velocity, and we detect continuum emission at neither 1.4 mm nor 3 mm at that position.

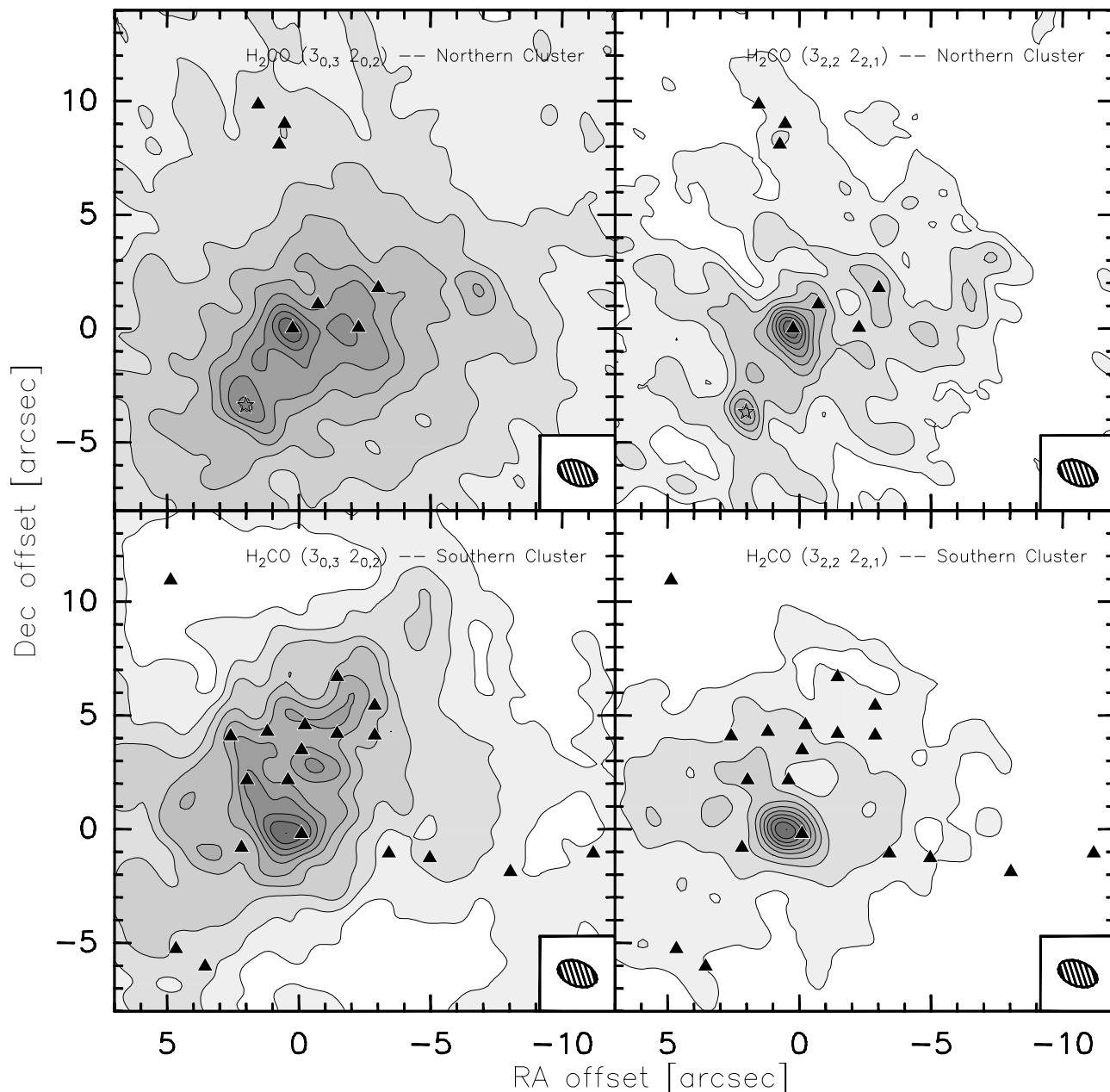
The first-moment maps of the combined PdBI+30 m data (see Fig. 4) show only a small velocity dispersion of  $\sim 1 \text{ km s}^{-1}$  in both (proto)clusters for the observed  $H_2CO$  lines. Similarly, the second-moment maps show no strong variation over the (proto)clusters.

### 3.3. Methyl cyanide

We observed the  $K = 0$ – $3$  components of the  $CH_3CN(6_K-5_K)$  ladder, which are a useful thermometer of the dense gas (e.g., Loren & Mundy 1984; Zhang et al. 1998). We detected  $CH_3CN$  emission only towards sources 13-s, 6/7/9-s and 4-n. Figure 5 shows the  $CH_3CN$  spectra toward these three positions.

The  $K = 0$  and  $K = 1$  components were detected at the three positions, and towards 13-s we also detected the  $K = 2$  and  $K = 3$  components. Since this is the only position at which these transitions are seen, this implies that 13-s is the warmest in the region. In addition, there is a tentative detection of the  $K = 2$  component towards 4-n.

Unlike in the case of the  $H_2CO$  transitions,  $CH_3CN$  is a dense gas tracer, which is barely affected by the missing short-spacings.



**Fig. 3.** Combined PdBI and IRAM30 m integrated emission of  $\text{H}_2\text{CO}$  towards IRAS 19410+2336. In the *left panels* are the  $\text{H}_2\text{CO}(3_{0,3}-2_{0,2})$  transition in the northern (*upper panel*) and southern (*lower panel*) (proto)clusters, and in the *right panels* of the image are the  $\text{H}_2\text{CO}(3_{2,2}-2_{2,1})$  transition. The contour levels are in 10% steps of the peak integrated intensity for each map. The triangles mark the 1.4 mm sources detected, and the  $1.6'' \times 1''$  beam appears in the lower-right corner of each panel.

## 4. Deriving the core mass function

### 4.1. Temperature determination

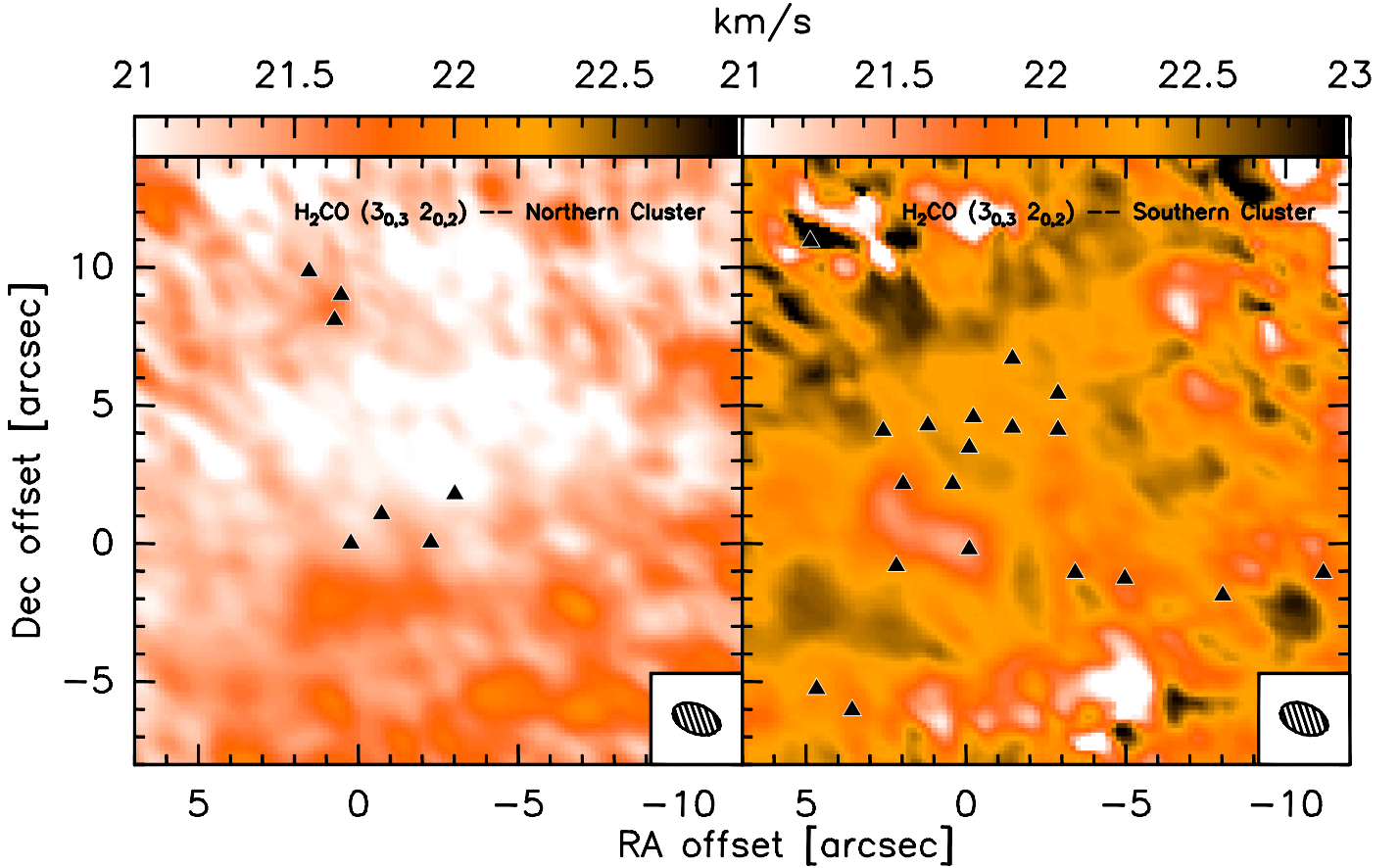
One of the major caveats of [Beuther & Schilke \(2004\)](#) in deriving a CMF for IRAS 19410+2336 was the assumption of a uniform temperature for both the north and south (proto)clusters when deriving the masses of the cores. In this work, we tried to derive a temperature structure for the two subclusters to obtain more accurate core masses, hence a more reliable CMF.

In this section, we describe the process used to determine the temperature of the detected cores. However, we note that we assumed that the kinetic temperatures derived from a combined PdBI+30 m molecular-line analysis correspond to the dust temperatures of the PdBI continuum peaks. As discussed further in

Sect. 5.4 this is not ideal, but is one of the limitations that we still have to face when working with high-spatial resolution mm observations. While combining single-dish and interferometer line data is relatively easy, the vastly different continuum bandpasses of interferometers and single-dish bolometers make the combination of continuum data extremely difficult.

#### 4.1.1. Applying $\text{H}_2\text{CO}$ line ratios

Formaldehyde ( $\text{H}_2\text{CO}$ ), one of the first polyatomic molecules discovered in space, has proven its usefulness in deriving the physical properties of the interstellar gas (e.g., [Mangum & Wootten 1993](#); [Jansen et al. 1994, 1995](#); [Mühle et al. 2007](#); [Watanabe & Mitchell 2008](#)). In particular,  $\text{H}_2\text{CO}$  allows one to



**Fig. 4.** Combined PdBI and IRAM 30 m first-moment maps of  $\text{H}_2\text{CO}(3_{0,3}-2_{0,2})$  towards IRAS 19410+2336 for the northern (*left panel*) and southern (*right panel*) (proto)clusters. The triangles mark the continuum sources detected, and the beam appears in the lower-right corner of each panel. There is no signature of a strong velocity dispersion.

estimate the kinetic temperature and the spatial density of star-forming regions.

Because  $\text{H}_2\text{CO}$  is almost a symmetric rotor ( $\kappa = -0.96$ ), transitions between energy levels with different  $K$  are only collisionally excited. Therefore, the comparison between the level populations from different  $K$  components with the same  $\Delta J = 1$  transition gives a measure of the kinetic temperature of the medium (Mangum & Wootten 1993).

In this work, we used the line intensity ratios of the  $\text{H}_2\text{CO}(3_{0,3}-2_{0,2})$  and  $\text{H}_2\text{CO}(3_{2,2}-2_{2,1})$  transitions, with energies  $E_{\text{up}} \sim 21$  K and  $E_{\text{up}} \sim 68$  K, respectively. These transitions meet the criteria previously mentioned and are only  $\sim 254$  MHz apart, therefore they could be observed within the same spectral setup of the PdBI receivers and the HERA heterodyne receiver. In this way, possible instrumental uncertainties, such as telescope efficiency as a function of wavelength or receiver and pointing instabilities, can be disregarded and one can obtain line ratios that are unaffected by instrumental effects.

Since there is only a poor spatial correlation between the combined  $\text{H}_2\text{CO}$  and continuum emission, we cannot extract a temperature for each individual core but only a temperature structure of the (proto)clusters as a whole. For only the brightest continuum cores was it possible to associate the  $\text{H}_2\text{CO}$  with the dust emission. Their spectra are shown in Fig. 6.

Having this temperature information in hand is already an improvement on the assumption of a single temperature for all cores.

#### 4.1.2. Large velocity gradient modeling

We extracted spectra towards the positions of each of the 26 sources detected at 1.4 mm and processed them with CLASS90, the obtained line parameters being listed in Table 3. Once we had obtained the  $R = \text{H}_2\text{CO}(3_{0,3}-2_{0,2})/\text{H}_2\text{CO}(3_{2,2}-2_{2,1})$  line ratios, we compared them with large velocity gradient (LVG) model predictions of the behavior of  $R$  as a function of molecular hydrogen density  $n(\text{H}_2)$ , formaldehyde column density  $N(\text{H}_2\text{CO})$ , and kinetic temperature  $T_k$ .

The  $\text{H}_2$  density could be estimated from our data. With the continuum emission measured towards the positions of the different sources, we estimated a beam-averaged  $\text{H}_2$  column density  $N(\text{H}_2)$  ranging from  $\sim 5 \times 10^{23} \text{ cm}^{-2}$  to  $\sim 6 \times 10^{24} \text{ cm}^{-2}$  with a mean value of  $\sim 10^{24} \text{ cm}^{-2}$ . For this calculation, we assumed a priori a uniform temperature of  $T_k = 46$  K (Beuther & Schilke 2004).

Considering spherical symmetry for the (proto)clusters, at the given distance of 2.2 kpc and when  $\theta$  is the angular diameter of the (proto)cluster, the relationship

$$n(\text{H}_2) = 1.5 \times 10^{-16} \text{ cm}^{-3} \left[ \frac{N(\text{H}_2)}{\text{cm}^{-2}} \right] \left[ \frac{\text{kpc}}{d} \right] \left[ \frac{\text{arcsec}}{\theta} \right] \quad (1)$$

gives an average value  $n(\text{H}_2) \sim 10^7 \text{ cm}^{-3}$  for each (proto)cluster. For the calculation, we adopted an approximate size of  $\theta \sim 9''$  for the protoclusters, which encompasses the extension of the main 1.4 mm emission. This translates to a size of  $\sim 20\,000$  AU at 2.2 kpc.

**Table 3.** H<sub>2</sub>CO line parameters for the detected cores.

Source	H <sub>2</sub> CO (3 <sub>0,3</sub> -2 <sub>0,2</sub> )				H <sub>2</sub> CO (3 <sub>2,2</sub> -2 <sub>2,1</sub> )				Ratio	T <sub>k</sub> <sup>c</sup> (K)
	T <sub>b</sub> (K)	∫ T <sub>b</sub> dv (K km s <sup>-1</sup> )	v <sub>c</sub> (km s <sup>-1</sup> )	Width (km s <sup>-1</sup> )	T <sub>b</sub> (K)	∫ T <sub>b</sub> dv (K km s <sup>-1</sup> )	v <sub>c</sub> (km s <sup>-1</sup> )	Width (km s <sup>-1</sup> )		
1-s <sup>a</sup>	...	...	...	...	0.4 ± 0.2	1 ± 0.4	20.4 ± 0.6	2.7 ± 1.2	...	35
2-s	14.7 ± 0.5	45.7 ± 0.8	22.2 ± 0.1	3.0 ± 0.1	1.7 ± 0.3	4.5 ± 0.8	21.7 ± 0.2	2.5 ± 0.6	8.5	35
3-s	13.6 ± 0.5	40.8 ± 0.9	22.3 ± 0.1	2.8 ± 0.1	1.9 ± 0.4	3.5 ± 0.4	21.3 ± 0.1	1.7 ± 0.3	7.0	35
4-s	17.1 ± 0.8	51.8 ± 0.8	22.3 ± 0.1	2.8 ± 0.1	3.0 ± 0.3	7.4 ± 0.7	21.9 ± 0.1	2.3 ± 0.3	5.8	35
5-s	17.5 ± 0.7	54.4 ± 0.8	22.3 ± 0.1	2.9 ± 0.1	2.7 ± 0.2	7.4 ± 0.8	21.5 ± 0.1	2.6 ± 0.4	6.5	35
6-s	18.0 ± 0.9	56.3 ± 1.1	22.2 ± 0.1	2.9 ± 0.1	1.8 ± 0.4	6.8 ± 0.8	21.4 ± 0.2	3.5 ± 0.6	9.8	35
7-s	18.1 ± 0.7	54.6 ± 0.8	22.2 ± 0.1	2.8 ± 0.1	2.3 ± 0.2	5.9 ± 0.8	21.0 ± 0.2	2.4 ± 0.4	7.8	35
8-s	12.4 ± 0.4	39.0 ± 0.9	22.3 ± 0.1	3.0 ± 0.1	1.8 ± 0.3	4.1 ± 0.4	20.9 ± 0.1	2.2 ± 0.2	7.0	35
9-s	20.5 ± 1.1	62.7 ± 0.6	22.2 ± 0.1	2.9 ± 0.1	2.6 ± 0.5	7.3 ± 0.5	21.6 ± 0.1	2.6 ± 0.2	7.7	35
10-s	18.4 ± 1.3	61.2 ± 1.3	22.3 ± 0.1	3.1 ± 0.1	2.7 ± 0.4	9.3 ± 1.2	21.5 ± 0.2	3.2 ± 0.5	6.8	35
11-s	19.2 ± 0.7	58.3 ± 1.0	22.1 ± 0.1	2.8 ± 0.1	3.0 ± 0.5	8.4 ± 0.9	21.3 ± 0.1	2.6 ± 0.3	6.5	35
12-s	12.8 ± 0.6	38.7 ± 0.6	22.1 ± 0.1	2.8 ± 0.1	2.6 ± 0.4	8.0 ± 1.1	21.3 ± 0.2	2.9 ± 0.5	4.9	45
13-s	14.9 ± 1.0	83.5 ± 0.8	21.6 ± 0.1	3.8 ± 0.1	4.8 ± 0.5	21.7 ± 0.8	20.8 ± 0.1	3.0 ± 0.1	3.1	90
14-s	5.8 ± 0.2	13.3 ± 0.7	22.1 ± 0.1	2.1 ± 0.1	1.7 ± 0.5	5.1 ± 0.8	21.2 ± 0.2	2.9 ± 0.6	3.5	35
15-s	6.5 ± 0.7	21.6 ± 1.1	22.3 ± 0.1	3.1 ± 0.2	1.8 ± 0.1	...	21.4 ± 0.1	unresolved	3.6	35
16-s	3.5 ± 0.2	8.6 ± 0.8	22.2 ± 0.1	2.3 ± 0.3	0.8 ± 0.1	...	21.3 ± 0.2	unresolved	4.2	35
17-s	4.1 ± 0.3	10.8 ± 0.7	22.4 ± 0.1	2.5 ± 0.2	1.8 ± 0.1	...	22.2 ± 0.1	unresolved	2.3	35
18-s	8.4 ± 0.7	25.3 ± 0.9	22.4 ± 0.1	2.8 ± 0.1	3.1 ± 0.1	...	21.5 ± 0.1	unresolved	2.7	35
19-s	8.0 ± 0.6	21.6 ± 0.8	22.4 ± 0.1	2.5 ± 0.1	1.0 ± 0.3	3.1 ± 0.5	22.0 ± 0.3	2.8 ± 0.5	7.9	35
1-n	0.8 ± 0.3	3.3 ± 0.7	21.3 ± 0.5	4.0 ± 1.1	0.2 ± 0.1	2.3 ± 0.9	23.9 ± 1.8	9.3 ± 3.5	3.4	35
2-n	1.4 ± 0.2	4.2 ± 0.6	21.1 ± 0.2	3.0 ± 0.6	0.8 ± 0.1	1.3 ± 0.6	20.7 ± 0.3	1.6 ± 1.1	1.7	35
3-n	1.4 ± 0.1	5.1 ± 0.7	21.3 ± 0.2	3.4 ± 0.6	0.5 ± 0.3	2.5 ± 0.9	22.8 ± 0.9	4.9 ± 2.1	2.9	35
4-n	7.8 ± 0.7	35.6 ± 1.1	21.0 ± 0.1	4.3 ± 0.2	2.7 ± 0.4	12.2 ± 1.2	20.5 ± 0.2	4.2 ± 0.5	2.9	60
5-n	5.4 ± 0.2	13.6 ± 0.9	21.2 ± 0.1	2.4 ± 0.2	1.8 ± 0.3	6.0 ± 1.0	20.2 ± 0.2	3.2 ± 0.7	3.0	50
6-n	6.8 ± 0.2	20.2 ± 0.9	21.3 ± 0.1	2.8 ± 0.1	1.4 ± 0.1	3.4 ± 0.8	20.7 ± 0.3	2.3 ± 0.7	4.9	35
7-n	5.6 ± 0.7	16.4 ± 1.3	20.6 ± 0.1	2.7 ± 0.3	1.4 ± 0.3	5.9 ± 0.7	20.5 ± 0.2	4.1 ± 0.6	4.2	35

**Notes.** <sup>(a)</sup> No detection in H<sub>2</sub>CO (3<sub>0,3</sub>-2<sub>0,2</sub>). <sup>(b)</sup> Obtained with a 3'' beam to avoid the optically thick regime. <sup>(c)</sup> From the LVG analysis in Sect. 4.1.2.

In contrast to  $n(\text{H}_2)$ , we cannot directly measure the value of  $N(\text{H}_2\text{CO})$  from our data. Values for the H<sub>2</sub>CO abundance relative to H<sub>2</sub> are reported to be in the range of  $X(\text{H}_2\text{CO}) \sim 10^{-9}-10^{-12}$ , for  $n(\text{H}_2) \sim 10^{4-6} \text{ cm}^{-3}$  (e.g., Wootten et al. 1978; Mundy et al. 1987; Carey et al. 1998; van der Tak et al. 2000), therefore calculations of an average  $N(\text{H}_2\text{CO})$  assuming an  $X(\text{H}_2\text{CO})$  value from the literature would introduce a high degree of uncertainty.

To constrain the value of  $N(\text{H}_2\text{CO})$ , we performed a least-squares minimization of the H<sub>2</sub>CO (3<sub>0,3</sub>-2<sub>0,2</sub>) and H<sub>2</sub>CO (3<sub>2,2</sub>-2<sub>2,1</sub>) line intensities as a function of  $n(\text{H}_2)$  and  $N(\text{H}_2\text{CO})$  for 13-s, the strongest source in the region. Assuming  $T_k = 100 \text{ K}$  (typical for hot cores), we obtain  $N(\text{H}_2\text{CO}) \sim 10^{14.5 \pm 0.1} \text{ cm}^{-2}$  and  $n(\text{H}_2) \sim 10^{6.4 \pm 1.0} \text{ cm}^{-3}$ , for our best solution. This density agrees to within  $1\sigma$  with the previously calculated  $n(\text{H}_2) \sim 10^7 \text{ cm}^{-3}$ , while the column density value can be considered as an upper limit since it was derived for the brightest source, with the highest H<sub>2</sub> column density.

We now compare the LVG model predictions of the behavior of the ratio  $R$  as a function of  $N(\text{H}_2\text{CO})$  and  $T_k$  for  $n(\text{H}_2) \sim 10^7 \text{ cm}^{-3}$  with the observed  $R$  values. Figure 7 shows the comparison. The dotted black contours are the modeled  $R$  values from 1 to 10 in  $R = 1$  steps, while the solid red contours are the observed  $R$  for the sources 3-s, 12-s, 13-s, and 19-s (for viewing simplicity, we only plot a few sources here). The vertical

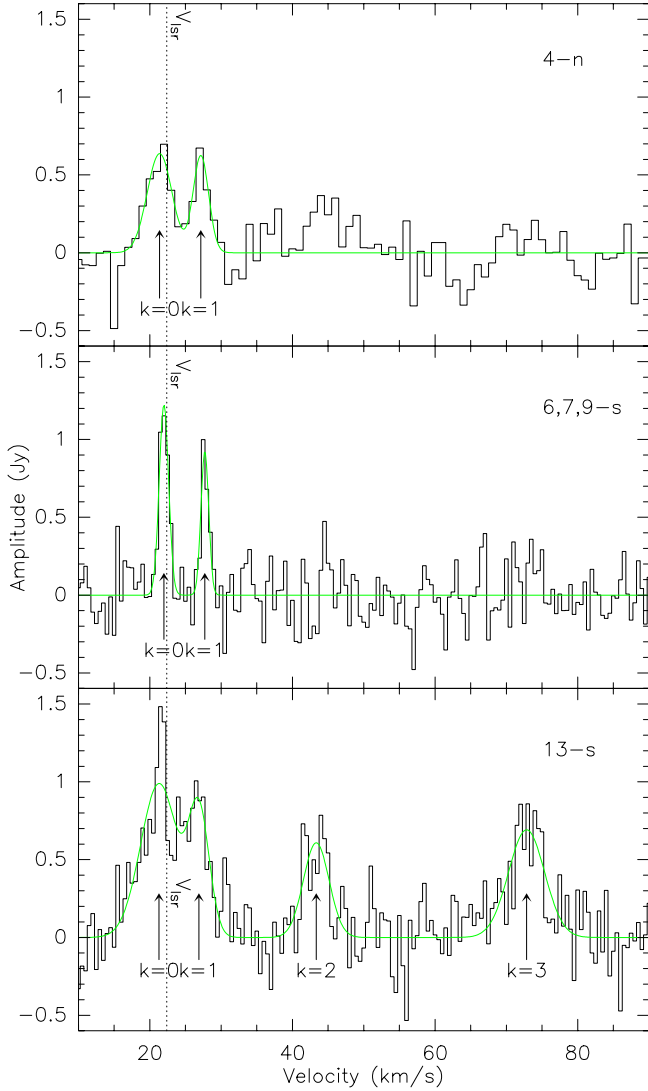
gray dotted line mark the previously obtained upper limit value of  $\log N(\text{H}_2\text{CO}) \sim 14.5$

For  $n(\text{H}_2) \sim 10^7 \text{ cm}^{-3}$ , the calculated upper limit  $N(\text{H}_2\text{CO})$  puts the cores close to the optically thin/thick regime turnover. This turnover is hinted at in the behavior of the contour lines in Fig. 7, and is located at  $N(\text{H}_2\text{CO}) \sim 10^{15} \text{ cm}^{-2}$ . At higher values, the temperature is no longer sensitive to the column density, which indicates the onset of the optically thick regime. Another means of (qualitatively) estimating the optical depth is by comparing the kinetic temperature  $T_k$  with the brightness temperature  $T_b$ . We found that  $T_b$  is systematically lower than  $T_k$  (see Table 3), therefore if we assume beam-filling the medium is optically thin.

Near to the turnover, the uncertainty in the temperature becomes larger, and in this case we see that it is approximately  $\sim 15 \text{ K}$ . To derive this value, we considered the uncertainty of  $\sigma \sim 0.2$  dex in the derivation of  $N(\text{H}_2\text{CO})$ . Shifting our upper value for  $N(\text{H}_2\text{CO})$  by that amount, the derived temperature varies by  $\sim 15 \text{ K}$  for 13-s, which is the brightest source. This can be seen in Fig. 7, where it can also be noted that this effect is smaller for the sources with lower column densities.

As noted before, there is only a poor correlation between the continuum cores and the H<sub>2</sub>CO peaks (except for the main sources). Therefore, on the basis of their continuum fluxes and relative locations in the (proto)cluster, we separated the cores

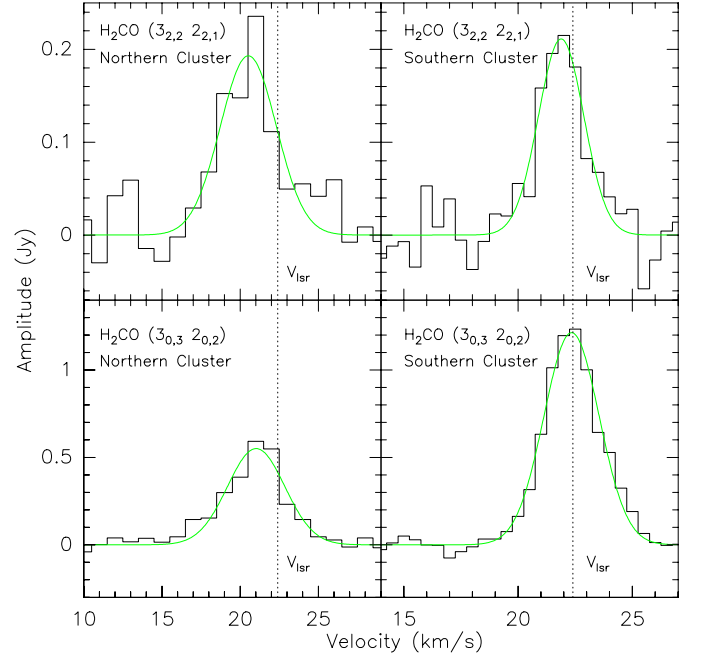




**Fig. 5.** Observed  $\text{CH}_3\text{CN}$  spectra towards sources 13-s, 6,7,9-s, and 4-n. The detected  $K$ -components are marked with arrows in each case, and the rest velocity with a dotted line. The green solid line is the best Gaussian fit to the lines, obtained with CLASS, and the resulting line parameters are in Table 4. Only for 13-s were the four  $K$ -components detected, indicating a warmer environment.

into several groups. For each of these groups, an average value of  $T_k$  was determined based on the values obtained for each of the sources within the group. Column 11 of Table 3 contains the kinetic temperature values assigned to each group, which are used to determine the masses and values of  $N(\text{H}_2)$  for the cores shown in Table 2, and to build the mass distribution to fit the CMF.

The majority of cores appear to be relatively cold, with a temperature of  $\sim 35$  K. Only cores 12-s, 13-s, 4-n, and 5-n have higher temperatures, up to  $\sim 90$  K in the case of 13-s. This indicates that these cores harbor a protostar. In the cases of 13-s and 4-n, there are reported NIR counterparts (see Sect. 5.2). The average temperature value for the whole region is  $\sim 40 \pm 15$  K, in agreement with the  $T_k \sim 46$  K derived from IRAS far-infrared observations (Beuther & Schilke 2004). Consequently, we found that the mean  $N(\text{H}_2)$  does not deviate significantly from the value adopted at the beginning despite the changes introduced by the different temperature values (see Table 2), since that column density was calculated based on the IRAS-based temperature.



**Fig. 6.**  $\text{H}_2\text{CO}$  spectra of the main sources in each (proto)cluster of IRAS 19410+2336. In the upper row are the  $\text{H}_2\text{CO}$  ( $3_{2,2}-2_{2,1}$ ) spectra for sources 4-n (left panel) and 13-s (right panel), and similarly in the bottom row are the  $\text{H}_2\text{CO}$  ( $3_{0,3}-2_{0,2}$ ) spectra for those two sources. A Gaussian profile was fit to each spectrum, and is shown by a green solid line. The dotted line marks the rest velocity adopted for the observations.

#### 4.1.3. The $\text{CH}_3\text{CN}$ k-ladder spectra

Methyl cyanide ( $\text{CH}_3\text{CN}$ ) is a dense gas ( $n \gtrsim 10^5 \text{ cm}^{-3}$ ) tracer and can also be used as a temperature determinant. As described previously in Sect. 3.3, we only detect  $\text{CH}_3\text{CN}$  towards 3 positions, although only for source 13-s do we detect enough  $k$ -components to derive a temperature, and to that source we applied the analysis described in this section. In the other two cases, we only detected the first two  $k$ -components, indicating that these are cold objects.

Two methods were used. We first compared the  $\text{CH}_3\text{CN}$  spectra with LTE model spectra produced with XCLASS (Schilke et al. 1999), a superset of CLASS of the GILDAS package, obtaining a temperature of  $\sim 80 \pm 40$  K for 13-s (see Fig. 8). Second, we also produced a rotational diagram to derive the gas temperature (see e.g., Loren & Mundy 1984; Zhang et al. 1998).

For the rotational diagram, we followed the method outlined in Appendix B of Zhang et al. (1998). Basically, we assumed LTE and optically thin emission, then the level populations became directly proportional to the line intensities of the  $k$ -components and could be translated into a single temperature via the Boltzmann equation. With these assumptions, we derived the following equation (adapted from Eq. (B6) of Zhang et al. 1998) for the relation between the level populations  $N_{J,K}$  and the gas temperature  $T_{\text{rot}}$

$$\ln \frac{N_{J,K}}{g_{J,K}} \propto -\frac{E_{J,K}}{k} \frac{1}{T_{\text{rot}}}, \quad (2)$$

where  $g_{J,K}$  and  $k$  are the statistical weight of the  $(J, K)$  level and the Boltzmann constant, respectively. Studies by Wilner et al. (1994) show that  $T_{\text{rot}}$  derived with this formulation agrees with those obtained with LVG calculations.

**Table 4.** CH<sub>3</sub>CN line parameters and LTE column densities.

Source	Line	$\int T_b dv$ (K km s <sup>-1</sup> )	$\sigma$	$v_c$ (km s <sup>-1</sup> )	$\sigma$	Width (km s <sup>-1</sup> )	$\sigma$	$T_b$ (K)	$\sigma$	$\log N_k$ (cm <sup>-2</sup> )	$\sigma$
13-s	$k = 0$	6.4	1.0	21.3	0.4	6.1	1.1	1.0	0.2	12.1	0.2
	$k = 1$	2.9	0.9	20.0	0.3	3.4	0.9	0.8	0.2	11.8	0.3
	$k = 2$	2.7	0.4	20.2	0.3	4.2	0.7	0.6	0.2	11.8	0.1
	$k = 3$	4.4	0.6	19.8	0.3	6.0	1.2	0.7	0.2	12.1	0.1
6,7,9-s	$k = 0$	2.0	0.2	22.0	0.1	1.6	0.2	1.2	0.1	11.6	0.1
	$k = 1$	1.3	0.2	20.9	0.1	1.3	0.3	0.9	0.1	11.4	0.2
4-n	$k = 0$	2.78	0.02	21.4	0.4	4.1	0.8	0.6	0.1	11.77	0.01
	$k = 1$	1.71	0.01	20.3	0.3	2.6	0.7	0.6	0.1	11.57	0.01

The level population for the upper  $k$ -level can be obtained from the integrated intensity of the corresponding line. The line parameters obtained from the Gaussian fit of the spectra shown in Fig. 5, and the calculated  $N_{J,K}$  for each level are given in Table 4. The resulting rotational diagram is shown in Fig. 9, along with the least-squares fit to all the  $k$ -components using Eq. (2), obtaining the value  $T_{\text{rot}} \sim 100 \pm 60$  K for 13-s.

From the plot, it can be seen that the fit does not represent the physical picture well. Explanations of this may be that the assumption of optically thin emission is incorrect, thus the model applied is unsuitable, or that we have mapped a hot and small core with a colder extended envelope, thus presenting two different temperature regimes.

Despite the crude fit, this value agrees very well with the  $T_k$  obtained from the H<sub>2</sub>CO LVG model and also with the value obtained from the XCLASS model.

#### 4.2. The differential core mass function

Combining the data from both (proto)clusters, we derive a differential CMF  $\Delta N/\Delta M$ , with the number of cores  $\Delta N$  per mass bin  $\Delta M$ .

One of the strongest caveats (see Sect. 5.4) that we faced when deriving the CMF was the relatively small number of cores detected. Because of that, a continuous linear binning in mass was not possible. We instead performed a logarithmic binning to more clearly represent and analyze the data, meaning that the fixed-width mass bins were defined on a logarithmic axis

$$\Delta M = \log M_k - \log M_{k-1} = B, \quad (3)$$

where  $B$  is the constant bin width. Therefore, the  $k$ -th mass was defined as  $M_k = 10^{kB}$ . This binning scheme was discussed in greater detail by Maíz Apellániz & Úbeda (2005).

A priori, we do have no preferred value of  $B$ , thus we derived a mass spectrum for different bin widths, with  $B$  ranging from 0.001 to 1 in 0.001 steps. Not all the CMFs obtained with this method were fitted. To obtain meaningful results, we established the following criteria to be satisfied for a CMF to be fitted:

- only one bin at most may contain a single core;
- there must be at least four non-empty bins after the incompleteness threshold.

We fit a powerlaw of the form  $\Delta N/\Delta M \propto M^\beta$  to the CMFs satisfying those two criteria, obtaining a  $\beta_B$  index value corresponding to a given  $B$ . The final value  $\beta$  is the weighted mean of all

the  $\beta_B$  indices with  $\sigma \leq 0.4$  and a coefficient of correlation<sup>4</sup>  $r^2 \geq 0.9$ . The different values of  $\beta_B$  satisfying these conditions are consistently lower than  $\sim -2$ , and have a weighted average and formal error of  $\beta = -2.3 \pm 0.2$  (see Rodón 2009, for a more detailed description of this method).

We see then that our results for the CMF slope are steeper than the  $\sim -1.6$  found for the clump mass functions (e.g., Stutzki & Guesten 1990; Kramer et al. 1998), which were obtained from CO emission maps for structures of sizes on the order of  $\sim 0.1$  pc. Going to at least a one order of magnitude higher spatial resolution, we found that the slope of the mass function is consistently steeper, indicating that there has been further fragmentation on smaller spatial scales.

For reference, Fig. 10 shows an example of the CMFs we obtained, in this case corresponding to  $B = 0.214$  and having a power-law index  $\beta = 2.3 \pm 0.2$ . A turnover in the distribution at the bin centered on  $\sim 1.4 M_\odot$  can be seen, containing masses above  $\sim 1 M_\odot$ . It appears in all the derived CMFs at about the same position, and since it matches our detection threshold, it is likely caused by the low-mass incompleteness of our sample rather than a physical feature. In all of the cases, we fit our mass distributions for masses higher than the turnover.

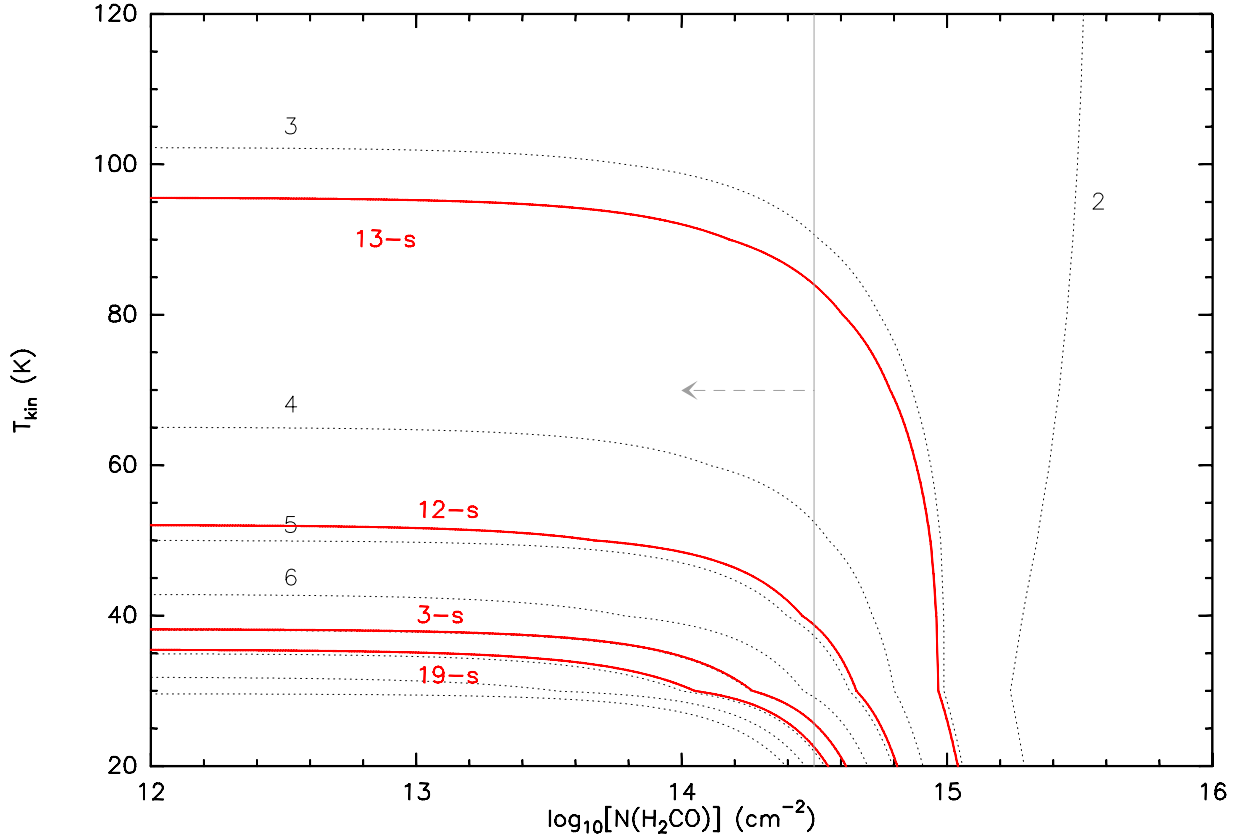
The incompleteness comes from both the sensitivity limit and the crowding in the region. The sensitivity limit was addressed in Sect. 3.1; it corresponds to a lower completeness limit of  $\sim 1 M_\odot$ . We found that the effect of crowding cannot be properly quantified with our data. Nevertheless, in (sub)mm studies the turnover in the mass distribution and the incompleteness of the sample tend to occur at the same position (see Kirk et al. 2006, and references therein), therefore we assume that our sample is completeness-limited for masses below  $\sim 1 M_\odot$ .

Although we filtered out considerable fractions of flux (Sect. 3.1) on large spatial scales, this filtering likely affected all observations in the same way. Although we cannot draw conclusions about the absolute masses of the cores, it is expected that their relative masses are correct.

##### 4.2.1. The cumulative mass function

Using the differential CMF in a small-number sample has the disadvantage that it is sensitive to the arbitrariness of binning, as we have shown in the previous section and led to the analysis described there. On the other hand, a cumulative CMF is free from

<sup>4</sup> This coefficient is defined as  $r^2 = 1 - \frac{SS_{\text{err}}}{SS_{\text{tot}}}$ , where  $SS_{\text{err}}$  is the sum of squared errors or residual sum of squares, and  $SS_{\text{tot}}$  is the total sum of squares. By this definition,  $r^2$  ranges between 0 and 1. A value of 1 means a perfect fit to the data (e.g., Draper 1998).



**Fig. 7.** Behavior of the  $R = \text{H}_2\text{CO}(3_{0,3}-2_{0,2})/\text{H}_2\text{CO}(3_{2,2}-2_{2,1})$  integrated intensity ratio. The dotted contours represent the  $R$  values from the LVG model for  $n(\text{H}_2) \sim 10^7 \text{ cm}^{-3}$  (see Sect. 4.1.2) and go from 2 to 10 in unit steps. The red solid contours are the observed  $R$  values, plotted here for cores 3-s, 12-s, 13-s, and 19-s for viewing simplicity. The vertical gray dotted line is the  $N(\text{H}_2\text{CO})$  upper limit value obtained with the LVG model. The effect of the optically thin/thick turnover is also seen, which introduces the largest uncertainty in the  $T_k$  estimation.

any problems associated with the binning, and is more suitable for small-number samples.

With our treatment of the CMF described in the previous section, we took into account the arbitrariness of the binning. However, for comparison and further analysis we also derived a cumulative CMF for our sample. Since our differential CMF above  $\sim 1 M_\odot$  could be fit by a single power-law of the form

$$\frac{\Delta N}{\Delta M} \propto M^\beta, \quad (4)$$

then the cumulative CMF is

$$N(>M) \propto -\frac{1}{1+\beta} M^{1+\beta} \quad (5)$$

for  $\beta < -1$ . According to Reid & Wilson (2006), when using the cumulative CMF one should take into account the upper mass cutoff  $M_{\text{max}}$  of the sample, regardless of whether it is a real cutoff or the result of finite sampling. In that case, the cumulative CMF takes the form

$$N(>M) \propto \begin{cases} \frac{1}{1+\beta} (M_{\text{max}}^{1+\beta} - M^{1+\beta}), & M < M_{\text{max}} \\ 0, & M \geq M_{\text{max}}, \end{cases} \quad (6)$$

for  $\beta < -1$ . However, they also state that a “steep power law” ( $\beta = -2.5$ ) will overwhelm the effect that the upper mass cutoff introduces into the fitting. From the differential CMF, we see that we are close to that “steep power law” limit, so we adopt

both analytical forms given in Eqs. (5) and (6) for the cumulative CMF.

Figure 11 shows the cumulative CMF for masses above  $1 M_\odot$ . As stated before, we fit both the analytical expressions given in Eqs. (5) and (6). The results are  $\beta = -2.4 \pm 0.1$  and  $\beta = -2.2 \pm 0.1$ , respectively, with the  $\sigma$  values resulting from the fitting algorithm. These results are comparable, showing that for a steep power law the inclusion of  $M_{\text{max}}$  in the definition of the cumulative CMF does not significantly affect the result (Reid & Wilson 2006). Since both results are similar, we adopt their average value of  $\beta = -2.3 \pm 0.2$ .

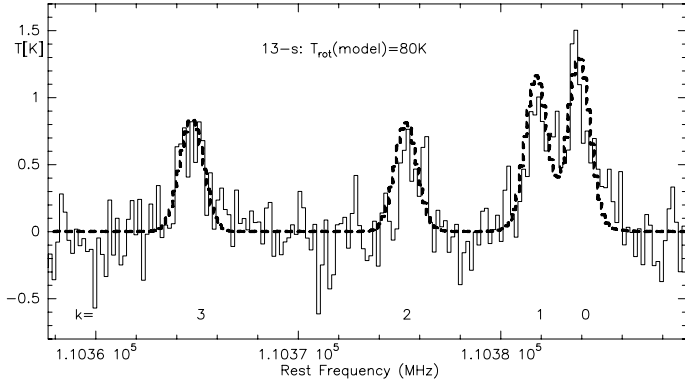
The cumulative CMF shows that the lower-mass objects dominate the fit. This is already visible in the differential CMF, but is clearer in the cumulative CMF. This is because the lower-mass bins are more populated. We see that of the 25 cores with masses above  $1 M_\odot$  only 6 are more massive than  $2.5 M_\odot$ , therefore the lower-mass bins have more statistical weight in the fitting.

There is also an inflection in the distribution starting at  $\sim 4 M_\odot$ . It is unclear whether this is a real physical feature of the distribution or a product of the uncertainty in its derivation. We discuss this in further detail in Sect. 5.5.

## 5. Discussion

### 5.1. Comparison with Beuther & Schilke (2004)

Beuther & Schilke (2004) detected 24 mm sources at 1.3 mm, 12 in each northern and southern cluster, with a detection threshold of  $3\sigma \sim 9 \text{ mJy beam}^{-1}$ . Owing to our higher sensitivity, we



**Fig. 8.** XCLASS (dashed line) fit to the observed  $\text{CH}_3\text{CN}$  spectrum towards source 13-s.

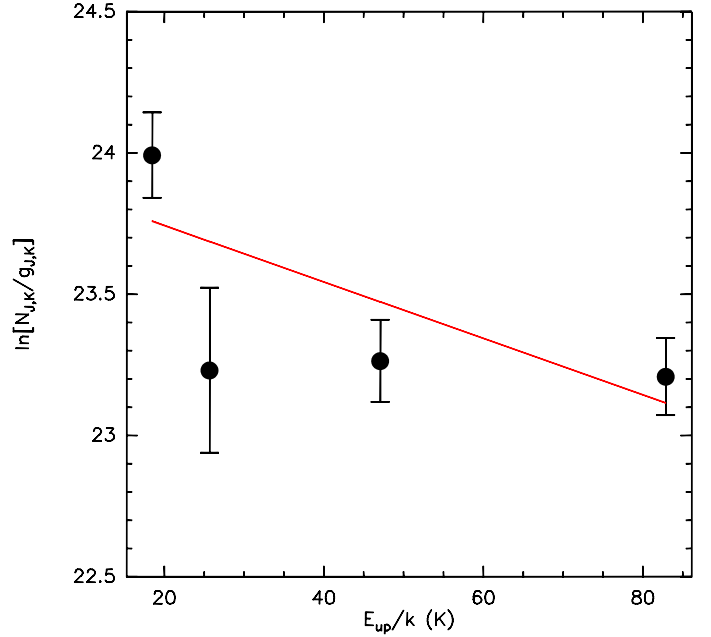
adopted a detection threshold of  $4\sigma \sim 4 \text{ mJy beam}^{-1}$  at 1.4 mm finding 26 cores, 19 in the southern cluster and 7 in the northern (proto)cluster. Despite the slight difference in the total number, the general 1.4 mm high-resolution cluster structure shown in [Beuther & Schilke \(2004\)](#) is recovered.

This highlights the general mapping difficulties with interferometers having only a small number of antennas close to the detection limit. For example, in contrast to expectations, formal  $3\sigma$  limits in such maps are not as reliable as one may expect. Therefore, here we raised the threshold to  $4\sigma$ . With its many antennas, ALMA will help to overcome these problems.

From the analysis described in Sect. 4.2, we obtain a power-law CMF for IRAS 19410+2336 with an index  $\beta = -2.3 \pm 0.2$ , in agreement with the previous result of [Beuther & Schilke \(2004\)](#). The new result is more reliable than the previous one since with the new data presented here for IRAS 19410+2336, we were able to estimate a temperature structure for the (proto)clusters. This is despite the limitations described in Sects. 4.1.2 and 5.4, which allow us to obtain a more accurate value for the core masses and thus avoid the previous caveat of assigning a uniform temperature to the whole region.

Nevertheless, this similarity between the CMF indices would imply that there is no strong dependence on the temperature structure. If we calculate the cumulative CMF of our region, but assume a uniform temperature  $T = 35 \text{ K}$ , the new index is  $\beta = -2.3 \pm 0.1$ . In the same way, if  $T = 40 \text{ K}$  then  $\beta = -2.6 \pm 0.2$ . Both values are indistinguishable within the errors from our main result. This feature is in part related to the temperature regime. The functional dependence of the mass with the temperature implies that if we were to vary the latter from 10 K to 20 K, the mass would change by about a factor of 3. However, going to higher temperatures, the variation in mass is less pronounced. For example, a change from 40 K to 50 K implies a change in mass of less than a factor 1.5, decreasing with increasing temperatures. Our other uncertainties in the temperature and mass calculations have more weight than this effect. Nevertheless, this suggests that a detailed temperature structure plays a more significant role in the determination of the mass functions of true pre-stellar regions, because of their intrinsic lower temperatures. The calculation of the mass function of a star-forming region before its members become stars is key in determining how the parental cloud further fragments, and whether the IMF is set at the fragmentation stage or is a later result of additional dynamical processes (e.g., competitive accretion, mergers, etc.).

The calculation of the power-law index was done by taking into account the arbitrariness of the binning at the moment of



**Fig. 9.** Rotational diagram of the observed  $K$ -levels of  $\text{CH}_3\text{CN}(J = 6 \rightarrow 5)$  towards source 13-s. The solid line is the best fit of Eq. (2), corresponding to a rotational temperature of  $100 \pm 60 \text{ K}$ , in agreement with the kinetic temperature obtained with the LVG modeling of the  $\text{H}_2\text{CO}$  line emission.

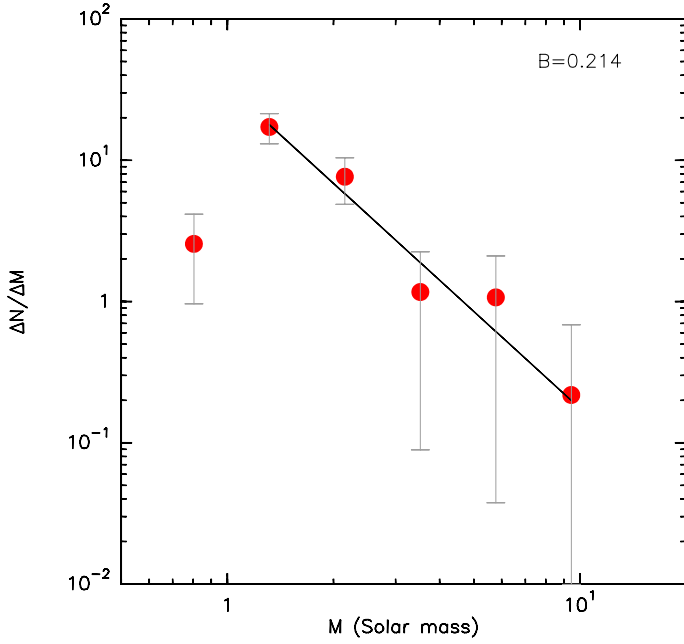
deriving a differential CMF. In addition, the cumulative CMF was taken into account in the analysis.

In the case of the cumulative CMF, the result obtained from it matches the result from the differential CMF. Although the former is more well-suited than the latter for the analysis of a small-number sample, in this case we observe that the fit to the cumulative CMF closely represents the lower-mass end of the distribution but not the higher-mass end. However, a slight 10 K increase in temperature in the higher-mass end, which is within the uncertainty in the temperature determination, flattens the inflection seen starting at  $\sim 4 M_\odot$ , obtaining also a better fitting of the distribution while not introducing substantial modifications to the fitted parameters.

## 5.2. Continuum sources

In the southern (proto)cluster, there are NIR and mid-infrared (MIR) counterparts detected for several of our mm sources. [Martín-Hernández et al. \(2008\)](#) and [Qiu et al. \(2008\)](#) detected in the position of 13-s a bright source in the  $K_s$  filter and the  $3.6 \mu\text{m}$ ,  $4.5 \mu\text{m}$ ,  $5.8 \mu\text{m}$ , and  $8.0 \mu\text{m}$  *Spitzer*/IRAC bands. [Martín-Hernández et al. \(2008\)](#) suggest that the detected NIR and MIR emission is either leaking through an outflow-created cavity (see [Beuther et al. 2003](#)), or that the cavity itself is radiating the emission, based on their estimation that the visual extinction at that position should be very large and thus should have no detectable NIR or even MIR emission. We confirmed their estimation, finding that the visual extinction for 13-s is  $A_v \sim 2700$  (see Table 2). Source 13-s is in an early stage of evolution, according to its NIR excess and the presence of  $\text{H}_2\text{O}$  and Class II  $\text{CH}_3\text{OH}$  masers ([Beuther et al. 2002d](#)), although the detection of a VLA 3.6 cm source at its position ([Sridharan et al. 2002](#)), suggests that there is a recently ignited protostar that has already formed





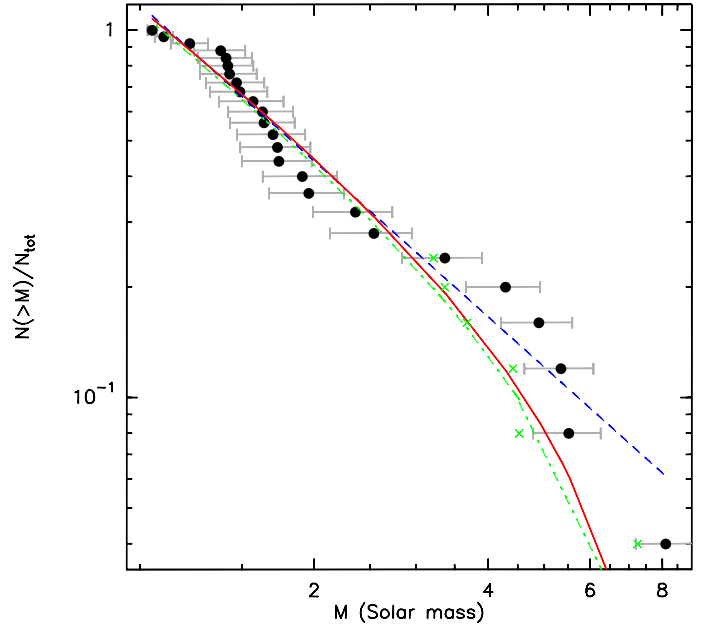
**Fig. 10.** Example of the CMFs obtained, corresponding to  $B = 0.214$  for core masses above  $1.4 M_{\odot}$ . The solid line is the best fit of Eq. (4) with a power-law index  $\beta = -2.3 \pm 0.2$ .

an ultracompact or hypercompact HII region, the detected radio emission being consistent with an ionizing B2 V star (Martín-Hernández et al. 2008; Qiu et al. 2008; Panagia 1973).

In Fig. 2 of Martín-Hernández et al. (2008), MIR emission is also seen at the position of the “subcluster” centered on sources 6-s, 7-s, and 9-s (source mm2 in their work and in Beuther et al. 2003). There is no detected cm counterpart at that position, suggesting that either none of the sources have ignited or the ionized HII region is still too small, hence the free-free emission is confined and undetectable. These sources might therefore be at an even earlier stage of evolution as 13-s, the equivalent of a Class 0 low-mass protostar, heating their circumstellar dust enough to be detected at MIR wavelengths.

Source nr76 of Martín-Hernández et al. (2008) is located less than  $1.5''$  from source 1-s. However, nr76 is detected in the  $J$ ,  $H$ , and  $K_s$  bands and not in any of the *Spitzer* bands, while 1-s is marginally detected at 1.4 mm and is resolved at 3 mm. The lack of emission from nr76 in the *Spitzer* bands, its reliable detection in the  $K_s$  band, and that it is a relatively strong source at 3 mm, make us believe that nr76 is not the counterpart of 1-s, but a separate source, appearing nearby owing to a projection effect. The case is also similar for source nr71. It is located at  $\sim 1.5''$  from 20-s, and although nr71 displays strong MIR emission, we only detect source 20-s at 3 mm and not at 1.4 mm. We therefore believe that this is another case of spatial projection.

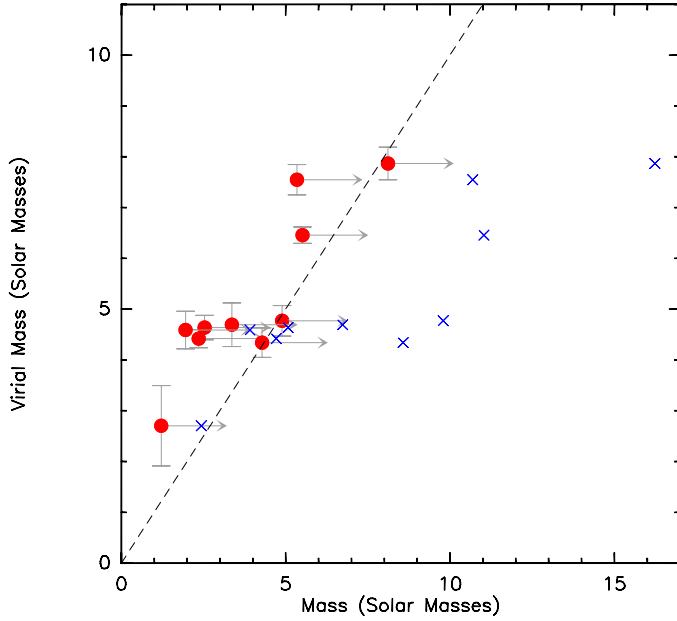
This would be expected, since IRAS 19410+2336 is embedded in a cluster of young stellar objects (YSOs). Martín-Hernández et al. (2008) detected 116 NIR/MIR sources in a  $\sim 75'' \times 75''$  region centered on IRAS 19410+2336, while Qiu et al. (2008) detected 46 YSOs ranging from Class 0 to Class II protostars within a radius of  $\sim 2$  pc, in addition to detecting over 800 NIR sources in that region. That there are already low-mass stars in the outskirts of IRAS 19410+2336 while high-mass stars continue to form supports the hypothesis that the low-mass stars form before their high-mass counterparts (e.g., Kumar et al. 2006).



**Fig. 11.** Cumulative CMF of IRAS 19410+2336 for core masses above  $1 M_{\odot}$ . The solid red line and the dashed blue line represent the best fits of Eq. (6) with a power-law index  $\beta = -2.2 \pm 0.1$  and Eq. (5) with  $\beta = -2.4 \pm 0.1$ , respectively. The green crosses represent a slight increase of 10 K in the higher-mass end, and the green dash-dotted line is the corresponding new fit of Eq. (6) (see Sect. 5.1). We note the flattening of the “bump” in the distribution, while the slope of the fit remains practically unchanged. In all cases, we have normalized  $N(>M)$  by the total number of cores  $N_{\text{tot}}$ .

In the northern (proto)cluster there are also identified NIR and MIR counterparts. Qiu et al. (2008) found five-band *Spitzer*/IRAC and 2MASS  $H$  and  $K_s$  emission towards 4-n, as well as *Spitzer*/IRAC  $3.6 \mu\text{m}$ ,  $4.5 \mu\text{m}$ ,  $5.8 \mu\text{m}$ , and  $8.0 \mu\text{m}$  emission towards 1/2/3-n. Source 4-n is likely at an early stage of evolution, although it is probably the most evolved source in the northern (proto)cluster. It is undetected at cm wavelengths, therefore has either not yet ignited its protostar or has an ionized region that is still too small where the free-free emission is trapped and thus not yet detectable. The other NIR/MIR detection in the (proto)cluster is towards sources 1/2/3-n, whose NIR/MIR fluxes are lower than that of 4-n, while their respective 1.4 mm masses are similar. This would indicate that 4-n is in a more advanced evolutionary stage than 1/2/3-n.

With a luminosity of  $\sim 10^4 L_{\odot}$ , IRAS 19410+2336 is a high-mass star-forming region, but the (proto)stellar content in its core is unknown because of high obscuration. Since it shows cm emission, it most likely already has a (proto)stellar component that ionizes an ultra- or even a hypercompact HII region. While it is impossible to directly measure the masses of the (proto)stars with mm data (see Sect. 3.1), it is possible to estimate the masses of the circumstellar structure. Our shortest baseline of 20 m at the given distance of 2.2 kpc corresponds to a spatial scale of  $\sim 38\,000$  AU at 1.4 mm, therefore any structure larger than this was not detected. The low masses that we then calculated from the 1.4 mm data can be attributed to a circumstellar structure, while the surrounding envelope likely contributes to the higher masses derived from the 3 mm data.



**Fig. 12.** Comparison between the virial masses and gas masses of the resolved cores in IRAS 19410+2336. Virial masses are unaffected by the interferometric flux filtering, which do affect the gas masses. The red dots are the actual values obtained, while the blue crosses represent the relationship if we take into account  $\sim 10\%$  of the flux filtered out by the interferometer. This is a hint of the care that must be taken when interpreting interferometric flux values.

### 5.3. Virial and Jeans analysis

The large uncertainty that the flux filtering introduces into the mass calculations can be seen when comparing the gas masses with the virial masses. The former were calculated from the interferometric continuum emission that is affected by the flux filtering, while the latter were calculated using the combined interferometric and single-dish  $\text{H}_2\text{CO}$  data, with the short-spacings correcting the effect introduced by the flux filtering. The virial and gas masses for the resolved cores in IRAS 19410+2336 are compared in Fig. 12. At first glance, the cores do not appear to be collapsing, although the gas masses derived from the continuum are lower than the virial masses because of the missing flux discussed previously. If we shift the gas masses higher by a factor of 2, taking into account only  $\sim 10\%$  of the missing flux, we see that within the uncertainty in the virial masses now all the resolved cores are likely to be collapsing.

The relative distances between neighboring cores within each (proto)cluster have a range several thousands of AU. These are similar and below the (proto)cluster's Jeans length  $\lambda_J \sim 25\,000$  AU, calculated from the equation

$$\lambda_J = 0.19 \text{ pc} \left( \frac{T}{10 \text{ K}} \right)^{1/2} \left( \frac{n(\text{H}_2)}{10^4 \text{ cm}^{-3}} \right)^{-1/2} \quad (7)$$

for an average  $n(\text{H}_2) \sim 10^5 \text{ cm}^{-3}$  and an average  $T_k \sim 40 \text{ K}$  for the whole large-scale clumps (see Sect. 4.1.2; [Stahler & Palla 2005](#)). Our resolution of  $\sim 1''$  at 1.4 mm corresponds to a spatial scale of  $\sim 2200 \text{ AU}$ , which clearly resolves the Jeans length of the region. We thus resolve the fragmentation of the clump-scale (proto)clusters far below their Jeans length. This cannot be said in the case of the cores, for which our resolution is above the Jeans length of the individual cores, in the 700–1200 AU range.

We resolve the Jeans length of the clumps by one order of magnitude, almost reaching the Jeans length of the individual cores, therefore we can safely assume that we mapped the direct progenitors of single stars or multiple systems at most (as in the case of the Trapezium in Orion, see e.g., [Rodón et al. 2008](#)). From the  $\text{H}_2\text{CO}$  data, we see that there is only a small signature of velocity dispersion (see Fig. 4), which would imply that the (proto)clusters are in a stage of weak dynamical evolution.

## 5.4. Considerations

### 5.4.1. Masses from (sub)mm interferometry

All interferometer observations underestimate the masses detected because of the incomplete sampling of the uv-plane. However, this filtering is not necessarily constant throughout the observed region. For instance, the single-dish observations map the cores as well as their envelope. This gas and dust reservoir is not necessarily gravitationally bound to the cores in its totality, thus only a fraction of it will be accreted by the cores during their evolution. Theory and observations cannot yet estimate how much this fraction is, and in addition, we are insensitive to the mass that is already in either (proto)stars or small, optically thick cores. Therefore, the underestimation factor we calculated for the masses is an upper-limit value, obtained in the simple approximation that all the mass detected with single-dish observations is uniformly distributed and contributes to each core in the same way.

Furthermore, the cores might not draw uniformly from the envelope during their accretion phase. The competitive accretion model (e.g., [Bonnell et al. 2004, 2007](#); [Peters et al. 2010](#)), for example, tells us that the most massive cores will accrete more from the envelope than lower-mass cores, and that it cannot be determined to which (proto)star(s) some parts of the envelope are going to contribute. It also claims that there may be the problem that the mass reservoir of each (proto)star is not a well-defined concept. This has then to be added to the problem of the spatial filtering from the interferometer.

All considered, we believe that the core masses we have determined are the best values that can be obtained with the currently available instruments and techniques. New studies with ALMA will certainly provide significant improvements in this field.

### 5.4.2. The nature of the CMF

In an ideal case, the CMF should be calculated with only the pre-stellar (starless) cores because if there were already a protostar, the gas mass accreted onto would not be negligible compared with its initial core mass. However, in the high-mass case the starless phase is very short-lived if it exists at all (see e.g. [Motte et al. 2007](#)). In addition, some of the MSF theories propose that non-prestellar cores would not affect the resulting CMF ([Clark et al. 2008](#), see Sect. 5.5 for more details).

We can assume a relationship of the mass function (MF) in a given region to its CMF as  $\text{CMF} = f(M) * \text{MF}$ , where  $f(M)$  is the fraction we are able to observe. If  $f(M) = \text{const.}$ , then our data are a fair representation of the CMF. If it increases with mass, for example because a larger fraction is resolved out for higher-mass cores, then the slope of the MF we measure is steeper than the true CMF. If it instead decreases with mass, because a larger fraction is resolved out for low-mass cores, the slope measured will be shallower than the true CMF. The shape

of this  $f(M)$  could be estimated by synthetically “observing” model CMFs. However, this is beyond the scope of this paper.

Even without flux losses, unresolved substructure and projection effects complicate the picture even more.

Taking into account all of these caveats, we consider that using a protostellar CMF similar to the one derived in this work is the best approach we can currently follow for a MSF region, though care has to be taken when comparing this CMF with the IMF. With its much better uv-coverage and means to measure the complete flux, ALMA will significantly improve our technical capabilities to study the CMF in detail.

### 5.5. The CMF of IRAS 19410+2336

Most of the studies that trace core scales ( $\sim 0.01$  pc) are OF low-mass star forming regions, since the distances involved are of a few hundred parsecs and therefore it is possible to recover such spatial scales with single-dish telescopes. Some examples are Motte et al. (1998) and Johnstone et al. (2000), who from single-dish sub-mm observations of the  $\rho$  Ophiuchi region derived in each case a mass function that resembles the IMF. A similar result was obtained by Könyves et al. (2010) with *Herschel* observations (i.e., in the far-IR spectrum) of the Aquila rift (see also André et al. 2010). Extending to a few solar-like masses, there are for example the works of Johnstone et al. (2006) and Nutter & Ward-Thompson (2007) on Orion. In these cases, which are also based on single-dish sub-mm observations, they recover a mass function similar to the IMF.

The mass functions of MSF regions have indeed been derived in many previous studies, although most of them with single-dish telescopes that due to the distances involved of more than  $\sim 2$  kpc, can only recover scales on the order of 0.1 pc. According to the criteria that we follow this corresponds to clump scales, i.e., structures that may form (proto)clusters and neither a single star nor small multiple system. These results correspond to mass spectra with indices  $\beta$  between  $\sim -1.2$  and  $\sim -3$  (e.g. Kramer et al. 1998; Kerton et al. 2001; Tothill et al. 2002; Shirley et al. 2003; Mookerjee et al. 2004; Reid & Wilson 2005, 2006; Beltrán et al. 2006; Muñoz et al. 2007; Ikeda & Kitamura 2011)

The case of IRAS 19410+2336 is, to our knowledge, the only one where a high-mass star forming region that could be mapped down to core scales presented enough fragmentation to derive a CMF. For a MSF region, a mass function on similar spatial scales was derived by Reid & Wilson (2005) for NGC 7538. Their smaller condensations have an average size of  $\sim 0.06$  pc, which is in-between clumps and cores. They derived a mass function with a power-law index  $\beta = -2.0 \pm 0.3$ , which despite being comparable with the stellar IMF, is also halfway between the clump mass function value of  $-1.6$  and the CMF value of  $-2.3$  found in low-mass star forming regions and in this work for a MSF region.

Remarkably, IRAS 19410+2336 is a very rare object in containing more than 10 cores when resolved down to a spatial scale of several thousand AU. Similar high-spatial resolution (sub)mm observations of MSF regions typically resolve only a few cores. For example, interferometric PdBI and SMA mm mappings of the MSF regions W3 IRS 5, IRAS 06058+2138, IRAS 06061+2151, IRAS 05345+3157, and AFGL961 resolve cores down to spatial scales of between  $\sim 750$  AU and  $\sim 5000$  AU, recovering in all cases fewer than 10 cores in each region (Fontani et al. 2009; Williams et al. 2009; Rodón et al. 2008; Rodón 2009). These regions are similar in distance and luminosity to IRAS 19410+2336, and although the gas mass

varies, even the regions more massive than IRAS 19410+2336 show much less fragmentation on similar spatial scales. More recently, there is the work of Bontemps et al. (2010) in the Cygnus X region. They resolved 5 clumps down to spatial scales similar to the ones we obtained, recovering 23 fragments in total, from which they estimated 9 are probable high-mass protostars. Although the total number of cores is similar to this work, each clump fragments to “only” 7 cores or less.

It is unclear why IRAS 19410+2336 is highly fragmented. This could be because it is in a different evolutionary stage, having a different chemical composition or even owing to perturbation and/or a different formation processes. Whatever the case, this apparent lack of fragmentation is preventing the derivation of a CMF for other individual MSF regions, highlighting the rarity of IRAS 19410+2336.

In general, observations of low-mass star-forming regions suggest that the IMF of low-mass stars is determined at early evolutionary stages (e.g., Testi & Sargent 1998; Motte et al. 1998, 2001; Alves et al. 2007; Könyves et al. 2010; see varying suggestions e.g., Goodwin & Kouwenhoven 2009). This is not so clear in the case of MSF regions, because dynamical processes like competitive accretion and merging of less massive protostars can shape the IMF at later evolutionary stages (e.g., Bonnell et al. 2004, 2007; Bonnell & Bate 2006).

A similarity between the CMF of a MSF region and the IMF would suggest that the structure and conditions within the molecular cloud could determine the IMF. This is essentially what was found by Chabrier & Hennebelle (2010) in a statistical study of the relationship between the CMF and the IMF. They found that, contrary to the original interpretation of Smith et al. (2009), both functions are correlated, and they argue that the IMF would then be defined in the early stages of evolution, being only slightly modified by environmental effects. The IMF and the CMF would also be similar if the relationship between the cores and the stars forming from them were one-to-one or nearly one-to-one. This kind of relationship is supported by theoretical models explaining the shape of the high-mass end of the IMF (e.g., Scalo et al. 1998; Padoan & Nordlund 2002), and by the apparently constant star-formation efficiency suggested both by theory and observations (Matzner & McKee 2000; Alves et al. 2007).

In the Clark et al. (2008) picture of competitive accretion, the shape of the IMF is also independent of when competitive accretion is halted. This would suggest that the IMF is set early on in the evolution of the clump, and therefore having non-prestellar cores at the moment of deriving a CMF would not affect the final results.

Taking into account the caveats discussed in Sect. 5.4, our derived power-law index  $\beta$  is similar to the high-mass end of the Salpeter IMF, and one would then be tempted to do a direct comparison between them. However, the CMF we derive is not completely pre-stellar, since we cannot confidently extract all the (proto)stellar sources. This means that our CMF is “contaminated” with sources that might already have been considered when calculating the local IMF in the region. Thus, we cannot draw solid conclusions about the likeness of the CMF of MSF regions and the IMF until the former can be derived with only pre-stellar cores.

Even then, caution must be taken when doing a direct comparison between the CMF and the IMF. Numerical simulations show that although the overall shape of the IMF in the low-mass to intermediate-mass regime is insensitive to a particular choice of core evolution scenarios, further turbulent fragmentation of



the cores may change the high-mass slope of the IMF (Swift & Williams 2008).

## 6. Conclusions

We have resolved the two clumps of the MSF region IRAS 19410+2336 into 26 cores at 1.4 mm, with a spatial resolution of  $\sim 2200$  AU. This resolves the Jeans length of the clumps, and the relative distances between the cores are similar or smaller than the Jeans length corresponding to individual cores. In addition, the cores show only a marginal signature of velocity dispersion, implying that the (proto)clusters are not in a strong dynamical evolution.

The approach of calculating temperatures using  $\text{H}_2\text{CO}$  lines might not be suitable for studies of such high-spatial resolution and density as the one presented here. We have found that the  $\text{H}_2\text{CO}$  and the continuum emission only correlate for the brightest source in each (proto)cluster and not for the fainter sources, therefore preventing the derivation of the temperature of each single core. However, we have been able to derive a temperature structure for the (proto)clusters as a whole.

The temperature structure of IRAS 19410+2336 was determined from its  $\text{H}_2\text{CO}$  and  $\text{CH}_3\text{CN}$  emission allowing the estimation of a CMF. Taking into account the arbitrariness of the mass binning when deriving a mass function, we found a CMF index  $\beta = -2.3 \pm 0.2$  for core masses above  $\sim 1.4 M_\odot$ , confirming the previous results of Beuther & Schilke (2004) with increased confidence levels.

It was impossible to determine with enough confidence the evolutionary stage of all the sources detected (i.e. pre-, proto-, or stellar sources). Because of this, the CMF we have derived is not a fully pre-stellar one, and therefore cannot be considered as a true predecessor of the stellar IMF, but a step in-between a pre-stellar CMF and the IMF. An additional important caveat is the difficulty in combining continuum single-dish and interferometer data because of the vastly different bandpasses. This induces missing flux problems that severely affect the mass estimates.

To the present day, mapping of the CMF has been done mostly in low-mass star forming regions. We have shown and discussed the caveats that involve such a study in MSF regions, which in turn explains the rarity of such studies so far. Mapping a MSF region down to  $\sim 0.01$  pc scales requires an angular resolution on the order of one arc-second for the closest regions, and tenths of arc-second if we go to larger distances. At (sub)mm wavelengths, this can only be achieved with interferometry. The interferometers operating at the moment normally achieve  $\sim 1''$  resolution, but it is not common for yet higher resolution to be reached. Sensitivity can also become an issue, and interferometers naturally filter out a large part of the incoming flux. When fully operational, ALMA will improve significantly on these observational limitations. Despite the difficulties and assumptions that have to be made owing to these limitations, the study of the CMF of high-mass star forming regions has great usefulness for the study of the origin of the IMF. It has already been seen that for low-mass stars, the IMF and the CMF are indistinguishable, suggesting that there is a kind of relationship between them. This relation is yet unknown for high-mass stars and therefore needs to be addressed, both theoretically and observationally.

*Acknowledgements.* J.A.R. and H.B. acknowledge support by the *Deutsche Forschungsgemeinschaft*, DFG project number BE 2578. J.A.R. also acknowledges support from the *International Max-Planck Research School for Astronomy and Cosmic Physics* at the University of Heidelberg.

## References

- Alves, J., Lombardi, M., & Lada, C. J. 2007, *A&A*, 462, L17  
 Anderson, L. D., Zavagno, A., Rodón, J. A., et al. 2010, *A&A*, 518, L99  
 André, P., Men'shchikov, A., Bontemps, S., et al. 2010, *A&A*, 518, L102  
 Beltrán, M. T., Brand, J., Cesaroni, R., et al. 2006, *A&A*, 447, 221  
 Beuther, H., & Schilke, P. 2004, *Science*, 303, 1167  
 Beuther, H., Kerp, J., Preibisch, T., Stanke, T., & Schilke, P. 2002a, *A&A*, 395, 169  
 Beuther, H., Schilke, P., Menten, K. M., et al. 2002b, *ApJ*, 566, 945  
 Beuther, H., Schilke, P., Sridharan, T. K., et al. 2002c, *A&A*, 383, 892  
 Beuther, H., Walsh, A., Schilke, P., et al. 2002d, *A&A*, 390, 289  
 Beuther, H., Schilke, P., & Stanke, T. 2003, *A&A*, 408, 601  
 Beuther, H., Schilke, P., Menten, K. M., et al. 2005, *ApJ*, 633, 535  
 Beuther, H., Zhang, Q., Sridharan, T. K., Lee, C.-F., & Zapata, L. A. 2006, *A&A*, 454, 221  
 Bonnell, I. A., & Bate, M. R. 2006, *MNRAS*, 370, 488  
 Bonnell, I. A., Vine, S. G., & Bate, M. R. 2004, *MNRAS*, 349, 735  
 Bonnell, I. A., Larson, R. B., & Zinnecker, H. 2007, in *Protostars and Planets V*, eds. B. Reipurth, D. Jewitt, & K. Keil, 149  
 Bontemps, S., Motte, F., Csengeri, T., & Schneider, N. 2010, *A&A*, 524, A18  
 Carey, S. J., Clark, F. O., Egan, M. P., et al. 1998, *ApJ*, 508, 721  
 Chabrier, G., & Hennebelle, P. 2010, *ApJ*, 725, L79  
 Clark, P. C., Bonnell, I. A., & Klessen, R. S. 2008, *MNRAS*, 386, 3  
 Draine, B. T., Dale, D. A., Bendo, G., et al. 2007, *ApJ*, 663, 866  
 Draper, N. R. 1998, *Applied regression analysis*  
 Fontani, F., Zhang, Q., Caselli, P., & Bourke, T. L. 2009, *A&A*, 499, 233  
 Frerking, M. A., Langer, W. D., & Wilson, R. W. 1982, *ApJ*, 262, 590  
 Goodwin, S. P., & Kouwenhoven, M. B. N. 2009, *MNRAS*, 397, L36  
 Goodwin, S. P., Kroupa, P., Goodman, A., & Burkert, A. 2007, in *Protostars and Planets V*, eds. B. Reipurth, D. Jewitt, & K. Keil, 133  
 Hildebrand, R. H. 1983, *QJRAS*, 24, 267  
 Ikeda, N., & Kitamura, Y. 2011, *ApJ*, 732, 101  
 Jansen, D. J., van Dishoeck, E. F., & Black, J. H. 1994, *A&A*, 282, 605  
 Jansen, D. J., van Dishoeck, E. F., Black, J. H., Spaans, M., & Sossin, C. 1995, *A&A*, 302, 223  
 Johnstone, D., Wilson, C. D., Moriarty-Schieven, G., et al. 2000, *ApJ*, 545, 327  
 Johnstone, D., Matthews, H., & Mitchell, G. F. 2006, *ApJ*, 639, 259  
 Kerton, C. R., Martin, P. G., Johnstone, D., & Ballantyne, D. R. 2001, *ApJ*, 552, 601  
 Kirk, H., Johnstone, D., & Di Francesco, J. 2006, *ApJ*, 646, 1009  
 Könyves, V., André, P., Men'shchikov, A., et al. 2010, *A&A*, 518, L106  
 Kramer, C., Stutzki, J., Rohrig, R., & Corneliussen, U. 1998, *A&A*, 329, 249  
 Kroupa, P. 2002, *Science*, 295, 82  
 Kumar, M. S. N., Keto, E., & Clerkin, E. 2006, *A&A*, 449, 1033  
 Loren, R. B., & Mundy, L. G. 1984, *ApJ*, 286, 232  
 Maíz Apellániz, J., & Úbeda, L. 2005, *ApJ*, 629, 873  
 Mangum, J. G., & Wootten, A. 1993, *ApJS*, 89, 123  
 Martín-Hernández, N. L., Bik, A., Puga, E., Nürnberger, D. E. A., & Bronfman, L. 2008, *A&A*, 489, 229  
 Matzner, C. D., & McKee, C. F. 2000, *ApJ*, 545, 364  
 Mookerjee, B., Kramer, C., Nielbock, M., & Nyman, L.-Å. 2004, *A&A*, 426, 119  
 Motte, F., André, P., & Neri, R. 1998, *A&A*, 336, 150  
 Motte, F., André, P., Ward-Thompson, D., & Bontemps, S. 2001, *A&A*, 372, L41  
 Motte, F., Schilke, P., & Lis, D. C. 2003, *ApJ*, 582, 277  
 Motte, F., Bontemps, S., Schilke, P., et al. 2007, *A&A*, 476, 1243  
 Muñoz, D. J., Mardones, D., Garay, G., et al. 2007, *ApJ*, 668, 906  
 Mühle, S., Seaquist, E. R., & Henkel, C. 2007, *ApJ*, 671, 1579  
 Mundy, L. G., Evans, II, N. J., Snell, R. L., & Goldsmith, P. F. 1987, *ApJ*, 318, 392  
 Nutter, D., & Ward-Thompson, D. 2007, *MNRAS*, 374, 1413  
 Ossenkopf, V., & Henning, T. 1994, *A&A*, 291, 943  
 Padoan, P., & Nordlund, A. 2002, *ApJ*, 576, 870  
 Panagia, N. 1973, *AJ*, 78, 929  
 Peters, T., Klessen, R. S., Mac Low, M., & Banerjee, R. 2010, *ApJ*, 725, 134  
 Qiu, K., Zhang, Q., Megeath, S. T., et al. 2008, *ApJ*, 685, 1005  
 Rathborne, J. M., Jackson, J. M., Zhang, Q., & Simon, R. 2008, *ApJ*, 689, 1141  
 Ridge, N. A., & Moore, T. J. T. 2001, *A&A*, 378, 495  
 Reid, M. A., & Wilson, C. D. 2005, *ApJ*, 625, 891  
 Reid, M. A., & Wilson, C. D. 2006, *ApJ*, 644, 990  
 Rodmann, J., Henning, T., Chandler, C. J., Mundy, L. G., & Wilner, D. J. 2006, *A&A*, 446, 211  
 Rodón, J. A. 2009, Ph.D. Thesis, Max-Planck-Institut für Astronomie, Heidelberg, Germany  
 Rodón, J. A., Beuther, H., Megeath, S. T., & van der Tak, F. F. S. 2008, *A&A*, 490, 213  
 Rodón, J. A., Zavagno, A., Baluteau, J., et al. 2010, *A&A*, 518, L80



- Salpeter, E. E. 1955, *ApJ*, 121, 161
- Scalo, J., Vazquez-Semadeni, E., Chappell, D., & Passot, T. 1998, *ApJ*, 504, 835
- Schilke, P., Phillips, T. G., & Mehringer, D. M. 1999, in *The Physics and Chemistry of the Interstellar Medium*, eds. V. Ossenkopf, J. Stutzki, & G. Winnewisser, 330
- Shirley, Y. L., Evans, N. J., Young, K. E., Knez, C., & Jaffe, D. T. 2003, *ApJS*, 149, 375
- Smith, R. J., Clark, P. C., & Bonnell, I. A. 2009, *MNRAS*, 396, 830
- Sridharan, T. K., Beuther, H., Schilke, P., Menten, K. M., & Wyrowski, F. 2002, *ApJ*, 566, 931
- Stahler, S. W., & Palla, F. 2005, *The Formation of Stars*, eds. S. W. Stahler, & F. Palla (Wiley-VCH), 865
- Stutzki, J., & Guesten, R. 1990, *ApJ*, 356, 513
- Swift, J. J., & Williams, J. P. 2008, *ApJ*, 679, 552
- Testi, L., & Sargent, A. I. 1998, *ApJ*, 508, L91
- Tieftrunk, A. R., Gaume, R. A., & Wilson, T. L. 1998, *A&A*, 340, 232
- Tohill, N. F. H., White, G. J., Matthews, H. E., et al. 2002, *ApJ*, 580, 285
- van der Tak, F. F. S., van Dishoeck, E. F., & Caselli, P. 2000, *A&A*, 361, 327
- Watanabe, T., & Mitchell, G. F. 2008, *AJ*, 136, 1947
- Williams, J. P., Mann, R. K., Beaumont, C. N., et al. 2009, *ApJ*, 699, 1300
- Wilner, D. J., Wright, M. C. H., & Plambeck, R. L. 1994, *ApJ*, 422, 642
- Wootten, A., Evans, II, N. J., Snell, R., & vanden Bout, P. 1978, *ApJ*, 225, L143
- Xu, Y., Reid, M. J., Menten, K. M., et al. 2009, *ApJ*, 693, 413
- Zhang, Q., Ho, P. T. P., & Ohashi, N. 1998, *ApJ*, 494, 636