

LETTER TO THE EDITOR

Constraints on mass loss and self-enrichment scenarios for the globular clusters of the Fornax dSph[★]

S. S. Larsen¹, J. Strader^{2,3}, and J. P. Brodie⁴

¹ Department of Astrophysics / IMAPP, Radboud University Nijmegen, PO Box 9010, 6500 GL Nijmegen, The Netherlands
e-mail: S.larsen@astro.ru.nl

² Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, MA 02138, USA

³ Department of Physics and Astronomy, Michigan State University, East Lansing, Michigan 48824, USA

⁴ UCO/Lick Observatory, University of California, Santa Cruz, CA 95064, USA

Received 26 June 2012 / Accepted 19 July 2012

ABSTRACT

Recently, high-dispersion spectroscopy has demonstrated conclusively that four of the five globular clusters (GCs) in the Fornax dwarf spheroidal galaxy are very metal-poor with $[\text{Fe}/\text{H}] < -2$. The remaining cluster, Fornax 4, has $[\text{Fe}/\text{H}] = -1.4$. This is in stark contrast to the field star metallicity distribution which shows a broad peak around $[\text{Fe}/\text{H}] \approx -1$ with only a few percent of the stars having $[\text{Fe}/\text{H}] < -2$. If we only consider stars and clusters with $[\text{Fe}/\text{H}] < -2$ we thus find an extremely high GC specific frequency, $S_N \approx 400$, implying by far the highest ratio of GCs to field stars known anywhere. We estimate that about 1/5–1/4 of all stars in the Fornax dSph with $[\text{Fe}/\text{H}] < -2$ belong to the four most metal-poor GCs. These GCs could, therefore, at most have been a factor of 4–5 more massive initially. Yet, the Fornax GCs appear to share the same anomalous chemical abundance patterns known from Milky Way GCs, commonly attributed to the presence of multiple stellar generations within the clusters. The extreme ratio of metal-poor GC- versus field stars in the Fornax dSph is difficult to reconcile with scenarios for self-enrichment and early evolution of GCs in which a large fraction (90%–95%) of the first-generation stars have been lost. It also suggests that the GCs may not have formed as part of a larger population of now disrupted clusters with an initial power-law mass distribution. The Fornax dSph may be a rosetta stone for constraining theories of the formation, self-enrichment and early dynamical evolution of star clusters.

Key words. galaxies: individual: Fornax dSph – galaxies: star clusters: general – galaxies: stellar content

1. Introduction

The Fornax dwarf spheroidal galaxy (dSph) is well-known for its high globular cluster (GC) specific frequency, i.e., the number of GCs normalized to a host galaxy $M_V = -15$ (Harris & van den Bergh 1981). Assuming $M_V = -13.2$ (Mateo 1998), the five GCs (Hodge 1961) correspond to a specific frequency of $S_N = 26$. Specific frequencies rivalling that of Fornax have only been found in other similarly faint dwarf galaxies (Peng et al. 2008; Georgiev et al. 2010). Spiral galaxies typically have $S_N \approx 1$, while normal elliptical galaxies have $S_N \approx 3$ –5, slightly higher in clusters than in the field (Harris 1991). Even the most cluster-rich cD galaxies generally have $S_N \lesssim 15$ (Harris 1991; Brodie & Strader 2006). These differences constitute the classical “specific frequency problem”.

A second specific frequency problem becomes apparent when considering the numbers of GCs associated with different stellar populations *within* galaxies. Early-type galaxies are generally redder (more metal-rich) than the average of their GC systems (Forte et al. 1981; Larsen et al. 2001; Forbes & Forte 2001), and direct comparisons of metallicity distributions for stars and globular clusters have confirmed that the specific frequency tends to increase with decreasing metallicity within galaxies (Harris & Harris 2002; Harris et al. 2007). This is also evident in our own Galaxy: of the roughly 150 GCs known in the Milky Way, about 2/3 are associated with the halo (Zinn 1985),

even though the halo only contains 1%–2% of the stellar mass (Suntzeff et al. 1991; Dehnen & Binney 1998).

It has, in fact, been suggested that a significant fraction of the Milky Way halo stars originate from disrupted GCs. If the Galactic GC population formed with a power-law mass function similar to that observed in young cluster systems at the present epoch (Larsen 2009), then the stars lost from dissolving clusters over a Hubble time might be sufficient to account for essentially the entire stellar halo (e.g. Kruijssen & Portegies Zwart 2009).

The above estimate only involves standard dynamical evolution of the clusters. However, a similar conclusion can be reached via a different line of reasoning, starting from the increasing body of evidence that GCs host dual or multiple stellar generations (Gratton et al. 2012). In the following we will refer to the “first” and “second” generation of stars, keeping in mind that the actual star formation histories may be more complex. The second generation is characterized, among other things, by anomalous abundances of several light elements that imply *p*-capture nucleosynthesis at high temperatures. The currently favored sites are massive AGB stars (D’Ercole et al. 2008), fast-rotating massive main sequence stars (Decressin et al. 2007), or massive interacting binaries (de Mink et al. 2009). A fundamental challenge faced by most scenarios for the origin of multiple stellar generations in GCs is the “mass budget” problem: at the present epoch, the second generation of stars has a mass similar to, or even greater than the first generation. However, for a standard IMF the ejecta produced by the first-generation stars fall short by large factors compared to the mass required to form

[★] Based on observations made with ESO Telescopes at the La Silla Paranal Observatory under programme ID 078.B-0631(A).

Table 1. Metallicities and absolute magnitudes for the Fornax GCs.

| | [Fe/H] | M_V |
|----------|------------------|----------|
| Fornax 1 | -2.5 ± 0.1^1 | -5.2^3 |
| Fornax 2 | -2.1 ± 0.1^1 | -7.3^3 |
| Fornax 3 | -2.3 ± 0.1^2 | -8.2^3 |
| Fornax 4 | -1.4 ± 0.1^2 | -7.2^3 |
| Fornax 5 | -2.1 ± 0.1^2 | -7.4^3 |

References. (1) Letarte et al. (2006); (2) Larsen et al. (2012); (3) Webbink (1985).

the observed second generation, even if a 100% star formation efficiency is assumed. This has led to the suggestion that a large fraction of the first generation, up to 90–95%, was lost soon after the formation of the second generation (D’Ercole et al. 2008; Schaerer & Charbonnel 2011; Bekki 2011). Accounting for subsequent dynamical evolution, one again finds that a significant fraction of the Milky Way stellar halo might come from GCs, even without considering that a significantly larger population of lower-mass clusters may have been present initially (Gratton et al. 2012).

In this Letter we discuss the globular cluster system of the Fornax dSph in the context of the second specific frequency problem and self-enrichment scenarios. While these two issues may seem unrelated, the Fornax dSph turns out to be such an extreme case of the second S_N problem that it puts tight constraints on the amount of mass that could have been lost from its GCs.

2. Chemical composition of the Fornax GCs

We have recently carried out a detailed analysis of the chemical composition of the three clusters Fornax 3, 4 and 5 from integrated-light high-dispersion spectroscopy with UVES on the ESO Very Large Telescope (VLT). Our analysis techniques are described in a companion paper (Larsen et al. 2012), along with a more detailed discussion of the abundance measurements and references to previous determinations of the metallicities. We measured iron abundances of $[\text{Fe}/\text{H}] = -2.3 \pm 0.1$ (Fornax 3), -1.4 ± 0.1 (Fornax 4) and -2.1 ± 0.1 (Fornax 5). The clusters Fornax 1, 2 and 3 were observed by Letarte et al. (2006), who measured abundances for three individual red giant branch (RGB) stars in each cluster; they obtained $[\text{Fe}/\text{H}] = -2.5 \pm 0.1$ (Fornax 1), -2.1 ± 0.1 (Fornax 2) and -2.4 ± 0.1 (Fornax 3). We note that there is excellent agreement between the two independent measurements of the Fe abundances are summarized in Table 1. It is clear that Fornax 4 is significantly more metal-rich than the other clusters, all of which have $[\text{Fe}/\text{H}] < -2$. We also list the GC M_V magnitudes, based on the magnitudes in Webbink (1985) and using the same apparent distance modulus of $m - M = 20.80$ as for the Fornax dSph itself for consistency (Mateo 1998; Pietrzyński et al. 2009).

Data on abundance variations within the clusters are still relatively limited. Letarte et al. (2006) noted that two of their nine stars show enhanced Na and depleted O abundances, as well as low Mg abundances. These patterns are similar to those observed in putative second-generation stars in Milky Way globular clusters. In our integrated-light measurements we observed Mg to be depleted relative to other α -elements (Ca, Ti) in Fornax 3, 4 and 5, again suggesting that some stars in these clusters display anomalous abundances. It thus appears that the Fornax GCs are similar to the Milky Way GCs in this respect.

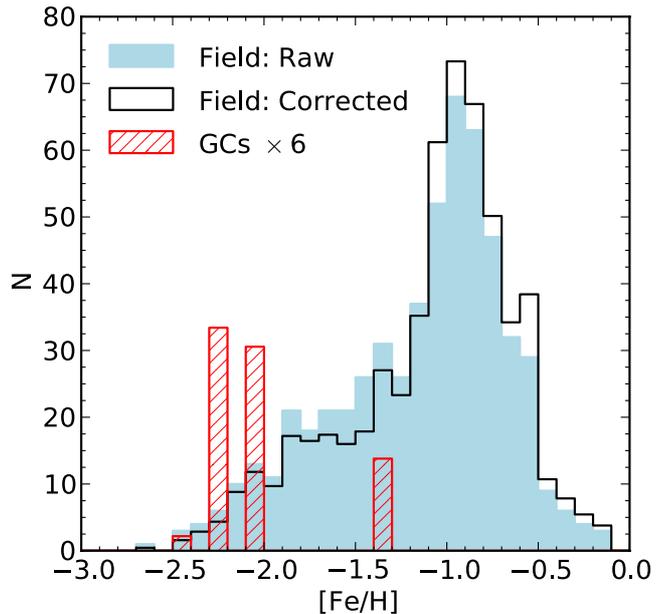


Fig. 1. Metallicity distributions for field stars and globular clusters in the Fornax dSph. The filled histogram shows the raw distribution of field star metallicities from Battaglia et al. (2006), while the outlined histogram is corrected for radial variations in the coverage (see main text). The hashed histogram represents the GCs with weights scaled by their luminosities and exaggerated by a factor of 6 (note that Fornax 2 and Fornax 5 fall in the same bin).

3. The globular cluster specific frequency revisited

Battaglia et al. (2006) measured metallicities for 562 field red giants in the Fornax dSph covering the full radial range out to ~ 1.2 , using spectroscopy of the Ca II near-infrared triplet obtained with the FLAMES spectrograph on the ESO VLT. About 7% of the stars in their sample have metallicities $[\text{Fe}/\text{H}] < -2$. However, the raw sample may not accurately represent the true metallicity distribution of the Fornax stars as the metallicity distribution does show a radial variation (with more metal-rich stars in the center), and no correction has been made for the varying degree of completeness as a function of galactocentric distance. We have attempted to make a rough correction for this effect, proceeding as follows:

We divided the profile of the Fornax dSph into 10 radial bins. For each bin, we computed the total number of stars $N_T(R)$ from the Sersic model fit of Battaglia et al. (2006) and counted the number of stars with FLAMES metallicity measurements, $N_F(R)$. We then assigned a weight, $W(R) = N_T(R)/N_F(R)$, to each star in the corresponding bin. Finally, a corrected metallicity distribution was derived by counting each star according to its weight. The raw and corrected metallicity distributions are shown in Fig. 1. Perhaps somewhat surprisingly, this procedure leads to a somewhat *less* pronounced low-metallicity tail, with about 5% of the stars having $[\text{Fe}/\text{H}] < -2$. This is because a much smaller fraction of the stars within a given FLAMES field are actually sampled in the central regions of the galaxy, so that the weights $W(R)$ increase towards the center where there are fewer very metal-poor stars. For comparison we also include the GCs in Fig. 1. Each cluster was “counted” as $6 \times N_{\text{stars}} \times 10^{-0.4(M_{V,\text{GC}} + 13.2)}$ stars, where $N_{\text{stars}} = 562$ is the total number of stars with FLAMES data, $M_{V,\text{GC}}$ are the M_V magnitudes of the individual clusters and $M_V = -13.2$ is the magnitude of the Fornax dSph. The difference between the metallicity distributions of the field stars and the GCs is rather striking.

If we simply scale the luminosity of the Fornax dSph by 5%, we obtain a total absolute magnitude of $M_V = -10.0$ for the low-metallicity tail. Relative to this tail, the four metal-poor GCs then correspond to a specific frequency of $S_N = 400$. With an absolute magnitude of $M_V = -8.9$ these GCs account for over 1/4 of the integrated luminosity of all the stars with $[\text{Fe}/\text{H}] < -2$ in Fornax! Note that this calculation assumes that numbers of RGB stars and integrated luminosities are equivalent, which is only approximately true as the number of RGB stars per unit luminosity depends somewhat on age and metallicity.

Alternatively, we can scale by stellar mass. From resolved color–magnitude diagrams, Coleman & de Jong (2008) estimated that a total of $6.1 \times 10^7 M_\odot$ of stars have formed in Fornax (for a Salpeter IMF extending down to $0.15 M_\odot$). A somewhat smaller mass of $4.3 \times 10^7 M_\odot$ within 0.8 was found by de Boer et al. (2012). Although the star formation history is complex and extends up to a few 100 Myr ago, the vast majority of the stars formed more than 2–3 Gyr ago, and would therefore contribute to the RGB star population on which the Battaglia et al. metallicities are based. Converting the observed numbers of RGB stars per metallicity bin to stellar mass per bin is, however, slightly non-trivial, as this conversion depends on both age and metallicity. Of interest here is the number of RGB stars that are sufficiently bright to be included in the Battaglia et al. (2006) sample. The faintest stars in their sample are slightly fainter than $V = 20$, corresponding to a limit of $M_V \approx -0.5$. From stellar model tracks (Dotter et al. 2007), we find that the amount of time an RGB star spends at $M_V < -0.5$ is very nearly independent of age, but decreases with increasing metallicity from about 25 Myr at $[\text{Fe}/\text{H}] = -2$ to about 20 Myr at $[\text{Fe}/\text{H}] = -1$. If there are no age differences, low-metallicity stars would then be somewhat *over-represented* in Fig. 1 relative to the actual amount of mass present at low metallicities. To find the relation between number of RGB stars per unit stellar mass formed and *age*, the RGB lifetime must be multiplied by the specific evolutionary flux, essentially the product of the IMF (evaluated at the turn-off mass) and the rate at which the turn-off mass decreases (Renzini & Buzzoni 1986). The net result is that the number of RGB stars per unit mass decreases by roughly a factor of two over the time interval 3–12 Gyr at fixed metallicity (Fig. 2). This would then cause *older* stars to be *under-represented* in Fig. 1, counteracting the trend with metallicity if there is an age-metallicity relation (Battaglia et al. 2006; Coleman & de Jong 2008). If the bulk of the metal-rich stellar population is as young as 3–4 Gyr and the metal-poor population is very old (>10 Gyr), then Fig. 2 suggests that we will underestimate the mass of the metal-poor population by up to ~60%. The actual star formation history has probably been somewhat more continuous over the range ~3–10 Gyr (Battaglia et al. 2006; Coleman & de Jong 2008; de Boer et al. 2012), in which case Fig. 1 would more closely represent the true metallicity distribution by mass. From similar considerations, we find that the number of RGB stars per unit integrated luminosity varies much less with age, while the metallicity dependence is similar to that in Fig. 2. We may then have *over-estimated* the fraction of light coming from metal-poor stars by ~10–20%.

Scaling the Coleman & de Jong (2008) mass estimate by 5%, we then find that $3.1 \times 10^6 M_\odot$ formed in stars with $[\text{Fe}/\text{H}] < -2$. About 35% of the stellar mass will have been lost due to stellar evolution over a Hubble time (e.g. Lamers et al. 2005), leaving $\sim 2 \times 10^6 M_\odot$ in metal-poor stars today. The combined masses of the four metal-poor GCs are $\sim 1.0 \times 10^6 M_\odot$ assuming an average $M/L_V = 3.5$ (Dubath et al. 1992; Larsen et al. 2012). From this we find that these clusters have a combined mass of

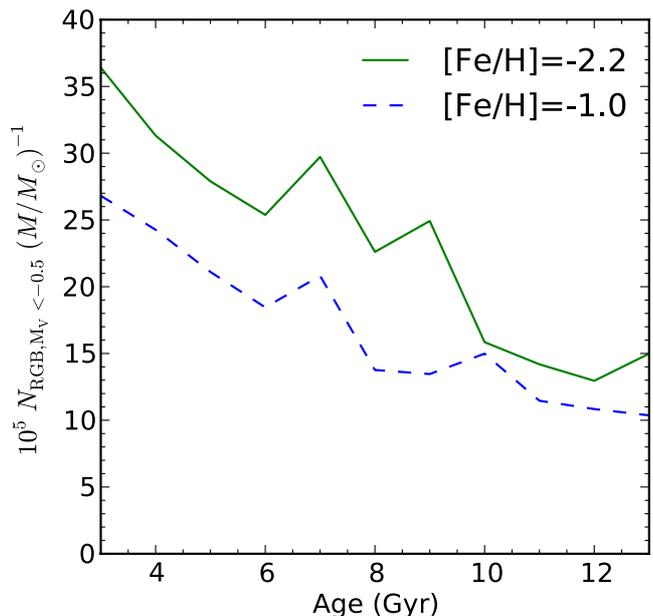


Fig. 2. Number of RGB stars (with $M_V < -0.5$) per $10^5 M_\odot$ formed versus age, based on Dotter et al. (2007) isochrones and assuming a Salpeter (1955) IMF normalized over the range 0.15–100 M_\odot .

about 1/2 of the mass in metal-poor field stars, and that about 1 in 3 stars with $[\text{Fe}/\text{H}] < -2$ belongs to one of the four metal-poor GCs. If we correct for age effects, as discussed above, this ratio might decrease to 1:4 or 1:5. These estimates are very similar to that based on the luminosities.

These are evidently rather rough estimates. The total mass of Fornax is uncertain, and the assumption that the metal-poor stars are smoothly distributed may not be valid if they formed in a few discrete events associated with the GCs (Peñarrubia et al. 2009b). Note that the FLAMES data preferentially sample fields close to, or including the GCs. Also, the dynamically based M/L_V ratio used for the GCs is higher than the $M/L_V \approx 2$ predicted by SSP models for a standard IMF (e.g. Strader et al. 2011). Further, the Ca II triplet-based metallicity measurements may not be on exactly the same scale as our high-dispersion spectroscopy of the GCs, although this mainly affects the shape of the metallicity distribution for $[\text{Fe}/\text{H}] < -2$ (Starkenburg et al. 2010). Nevertheless, it is clear that a *staggeringly large fraction of the most metal-poor stars in Fornax belong to the four metal-poor GCs*. For comparison, the Milky Way GC system has a combined mass of $\sim 2.8 \times 10^7 M_\odot$ (Kruijssen & Portegies Zwart 2009), or about 2% of the mass of the stellar halo if a total mass of $\sim 10^9 M_\odot$ is assumed for the latter (e.g. Suntzeff et al. 1991) and we take into account that only $\sim 2/3$ of the Galactic GC system is associated with the halo.

4. GC formation and self-enrichment

The fact that, after a Hubble time of dynamical evolution, a large fraction of the metal-poor stars in the Fornax dSph still belong to the GCs, has important implications for our understanding of the formation and dynamical evolution of GCs.

First, there is little room for dissolution of any additional clusters formed together with the four extant metal-poor objects. Each of these four surviving metal-poor GCs has likely lost several times $10^5 M_\odot$ due to evaporation over a Hubble time (e.g. Jordán et al. 2007), so that these combined losses may well

amount to over a million M_{\odot} . The implication is then that perhaps half of the most metal-poor stars now present in Fornax may originally have formed in these four GCs. This might suggest that the Fornax GCs did not form as part of a larger population of star clusters with a power-law mass distribution extending down to low masses. This is reminiscent of the star cluster populations in some present-day star forming dwarf galaxies which host a single, or a few, outstandingly massive clusters, one of the most extreme examples being NGC 1705 (O’Connell et al. 1994; Ho & Filippenko 1996).

Second, these numbers represent a challenge for self-enrichment scenarios in which GCs were initially much more massive than they are now (D’Ercole et al. 2008; Schaerer & Charbonnel 2011; Bekki 2011). It seems to be ruled out that the Fornax GCs could possibly have been more than a factor of a few more massive initially than they are now. This limit may be even more stringent for Fornax 3, the most massive of the clusters, whose very low metallicity places it even further out in the tail of the field star metallicity distribution. Nevertheless, detailed abundance measurements suggest that the Fornax GCs share the same abundance anomalies seen in Galactic GCs. It has been suggested that the second generation may have formed partly from gas that was subsequently accreted (Conroy & Spergel 2011; Pflamm-Altenburg & Kroupa 2009). However, even this possibility does not easily explain the high ratio of GC to field stars in the Fornax dSph. It would require that each cluster was able to accrete a significant amount of gas with the same composition as the first-generation stars, while little gas of this composition was available for the formation of additional field stars.

An important assumption in the above discussion is that the field star population observed in Fornax today has not been significantly stripped by the Galactic tidal field. While this has likely affected some dSphs, the stellar component in Fornax itself does not appear to have been affected by tidal stripping (Peñarrubia et al. 2009a). Conversely, it is possible that the GCs did not originate within the Fornax dSph, but formed in halos that were stripped of stars and dark matter before being accreted onto Fornax. This has also been suggested as a possible solution to the “timing problem”, i.e., the fact that the clusters have not yet been dragged into the center of the galaxy as expected due to dynamical friction (Cole et al. 2012). This scenario is difficult to rule out, but it is unclear why four or five globular clusters would have formed close enough to the Fornax dSph to be captured by it, given that no significant population of inter-galactic GCs has been found elsewhere in the Local Group.

5. Conclusions

We have used the most recent measurements of metallicities for globular clusters and field stars in the Fornax dwarf spheroidal galaxy to estimate the specific frequency of metal-poor GCs. Four of the GCs have $[\text{Fe}/\text{H}] < -2.0$; associating these GCs with field stars in the same metallicity range we estimate $S_N \approx 400$, by a wide margin the highest known anywhere. We find that about one quarter of all stars in the Fornax dSph with $[\text{Fe}/\text{H}] < -2$ belong to these four most metal-poor clusters. Accounting for standard dynamical evolution, an even larger fraction of the metal-poor stars must initially have been born in the clusters. This puts tight constraints on any further amount of stars that could have been lost from metal-poor star clusters due to early “infant weight loss” or “infant mortality”. The extant clusters could at most have been a factor of ~ 4 – 5 more massive initially than they are now, and this requires a rather extreme scenario in which no

field stars or other clusters of similar metallicity were formed initially.

It would be of significant interest to carry out detailed chemical tagging of the most metal-poor stars in Fornax to determine how many of them can be traced back to the GCs. With sufficient accuracy, it should be possible to detect peaks in the field star metallicity distribution corresponding to stars lost from the GCs. One might also expect to see a significant fraction of metal-poor field stars with peculiar, GC-like abundance patterns. Fornax and other dSph galaxies may be unique laboratories in which the presence or absence of anomalous abundances of light elements in the field stars might shed light on the origin of multiple stellar populations in globular clusters.

Acknowledgements. We thank Charlie Conroy, Mark Gieles, Tom Richtler and the referee for valuable comments and discussion. S.S.L. acknowledges support by an NWO/VIDI grant and J.P.B. acknowledges NSF grant AST-1109878.

References

- Battaglia, G., Tolstoy, E., Helmi, A., et al. 2006, A&A, 459, 423
 Bekki, K. 2011, MNRAS, 412, 2241
 Brodie, J. P., & Strader, J. 2006, ARA&A, 44, 193
 Cole, D. R., Dehnen, W., Read, J. I., & Wilkinson, M. I. 2012, MNRAS, submitted [arXiv:1205.6327]
 Coleman, M. G., & de Jong, J. T. A. 2008, ApJ, 685, 933
 Conroy, C., & Spergel, D. N. 2011, ApJ, 726, 36
 de Boer, T. J. L., Tolstoy, E., Hill, V., et al. 2012, e-print [arXiv:1206.6968]
 de Mink, S. E., Pols, O. R., Langer, N., & Izzard, R. G. 2009, A&A, 507, L1
 Decressin, T., Meynet, G., Charbonnel, C., Prantzos, N., & Ekström, S. 2007, A&A, 464, 1029
 Dehnen, W., & Binney, J. 1998, MNRAS, 294, 429
 D’Ercole, A., Vesperini, E., D’Antona, F., McMillan, S. L. W., & Recchi, S. 2008, MNRAS, 391, 825
 Dotter, A., Chaboyer, B., Jevremović, D., et al. 2007, AJ, 134, 376
 Dubath, P., Meylan, G., & Mayor, M. 1992, ApJ, 400, 510
 Forbes, D. A., & Forte, J. C. 2001, MNRAS, 322, 257
 Forte, J. C., Strom, S. E., & Strom, K. M. 1981, ApJ, 245, L9
 Georgiev, I. Y., Puzia, T. H., Goudfrooij, P., & Hilker, M. 2010, MNRAS, 406, 1967
 Gratton, R. G., Carretta, E., & Bragaglia, A. 2012, A&ARv, 20, 1
 Harris, W. E. 1991, ARA&A, 29, 543
 Harris, W. E., & Harris, G. L. H. 2002, AJ, 123, 3108
 Harris, W. E., & van den Bergh, S. 1981, AJ, 86, 1627
 Harris, W. E., Harris, G. L. H., Layden, A. C., & Wehner, E. M. H. 2007, ApJ, 666, 903
 Ho, L. C., & Filippenko, A. V. 1996, ApJ, 472, 600
 Hodge, P. W. 1961, AJ, 66, 83
 Jordán, A., McLaughlin, D. E., Côté, P., et al. 2007, ApJS, 171, 101
 Kruijssen, J. M. D., & Portegies Zwart, S. F. 2009, ApJ, 698, L158
 Lamers, H. J. G. L. M., Gieles, M., Bastian, N., et al. 2005, A&A, 441, 117
 Larsen, S. S. 2009, A&A, 494, 539
 Larsen, S. S., Brodie, J. P., Huchra, J. P., Forbes, D. A., & Grillmair, C. J. 2001, AJ, 121, 2974
 Larsen, S. S., Brodie, J. P., & Strader, J. 2012, A&A, submitted
 Letarte, B., Hill, V., Jablonka, P., et al. 2006, A&A, 453, 547
 Mateo, M. 1998, ARA&A, 36, 435
 O’Connell, R. W., Gallagher, J. S., & Hunter, D. A. 1994, ApJ, 433, 65
 Peñarrubia, J., Navarro, J. F., McConnachie, A. W., & Martin, N. F. 2009a, ApJ, 698, 222
 Peñarrubia, J., Walker, M. G., & Gilmore, G. 2009b, MNRAS, 399, 1275
 Peng, E. W., Jordán, A., Côté, P., et al. 2008, ApJ, 681, 197
 Pflamm-Altenburg, J., & Kroupa, P. 2009, MNRAS, 397, 488
 Pietrzyński, G., Górski, M., Gieren, W., et al. 2009, AJ, 138, 459
 Renzini, A., & Buzzoni, A. 1986, in Spectral evolution of galaxies: Proceedings of the Fourth Workshop, Erice, eds. C. Chiosi, & A. Renzini (Dordrecht: Reidel Publishing Co.), 195
 Salpeter, E. E. 1955, ApJ, 121, 161
 Schaerer, D., & Charbonnel, C. 2011, MNRAS, 413, 2297
 Starkenburg, E., Hill, V., Tolstoy, E., et al. 2010, A&A, 513, A34
 Strader, J., Caldwell, N., & Seth, A. C. 2011, AJ, 142, 8
 Suntzeff, N. B., Kinman, T. D., & Kraft, R. P. 1991, ApJ, 367, 528
 Webbink, R. F. 1985, in Dynamics of star clusters, eds. J. Goodman, & P. Hut (Dordrecht: Reidel Publishing Co.), IAU Symp., 113, 541
 Zinn, R. 1985, ApJ, 293, 424