The activity of main belt comets

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ABSTRACT

Context. Main belt comets represent a recently discovered class of objects. They are quite intriguing because, while having a Tisserand invariant value higher than 3, are showing cometary activity.

Aims. We study the activity of the main belt comets making the assumption that they are icy-bodies and that the activity has been triggered by an impact. We try to determine the characteristics of this activity. We also try to determine if the nowadays impact rate in the main asteroid belt is compatible with the hypothesis of an activity triggered by a recent impact.

Methods. Due to the fact that the main belt comets can be considered as a kind of comets, we apply a thermal evolution model developed for icy bodies in order to simulate their activity. We also apply a model to derive the impact rate, with respect to the size of the impactor, in the main belt.

Results. We demonstrate that a stable activity can result from a recent impact, able to expose ice-rich layers, and that the impact rate in the main belt is compatible with this explanation.

Key words. minor planets, asteroids: general – comets: general – comets: individual: P/2005 U1 (Read)

1. Main belt comets: a new class of objects

The main belt comets (MBCs) are a recently discovered class of objects, composed until now by only four objects (Table 1). These objects are puzzling because they are orbiting in the main belt on stable orbits, with Tisserand invariant with respect to Jupiter higher than 3, but at the same time they are showing a more or less stable cometary activity. Four known objects imply many more presently inactive or faintly active and as a consequence undetectable. It is probable that as a result of the surveys being conducted (Gilbert & Wigert 2009) more objects will be added to this new class in a near future.

The first of the MBCs that has been discovered is 133P/Elst-Pizarro. At the moment of the discovery, in 1992 (Elst et al. 1996), it has been designated as 7968 Elst-Pizarro. When in July 1996 the body was found showing a dust tail, the activity was initially attributed to an impact (Boehnhardt et al. 1998; Toth 2000), but when later on the object was found periodically active at the successive perihelions (2002 and then 2007) it became clear that a different explanation had to be found (Hsieh et al. 2004). P/2005 U1 (Read) and 176P/LINEAR followed in a short time (Read et al. 2005; Green 2006), both active and orbiting on similar orbits (Table 1). More recently, P/2008 R1 (Garradd) has been discovered (Garradd et al. 2008).

The Tisserand invariant values rule out the possibility that these bodies are newcomers in this part of the solar system. The orbits of two of them, 133P/Elst-Pizarro and 176P/LINEAR, can be linked with the 2 Gyr-old Themis dynamical family (Zappalà et al. 1990) and the smaller and younger (10 Myr) Beagle family (Nesvorny et al. 2008). The orbit of P/2005 U1 (Read) is falling just outside the Themis family, and P/2008 R1 (Garradd) appears to be a dynamically unstable object, probably formed in a different part of the main belt (Jewitt et al. 2009).

As for the causes of dust ejection, it became soon evident that it is due to sublimation. Not only this activity is recurrent, as in the case of 133P/Elst-Pizarro, but it is also lasting for weeks and months. Moreover, dust velocities, estimated from the sunward extent of the coma, are greatly in excess of what would be expected from electrostatic levitation or rotational ejection (Hsieh & Jewitt 2006).

If these bodies formed in-situ, the question of how can they still contain ice arises. In the protoplanetary disk, opacity due to grains inhibited radiative cooling and raised the mid-plane kinetic temperature (Jewitt et al. 2007). Growth and migration of solids in the disk would have caused the opacity to change, so moving the snow line, that for a fraction of a million years may have been within the main belt. In this way, asteroids orbiting in the main belt could have incorporated water ice upon formation. It is well know that many asteroids lack the hydration feature in their spectra. This has been interpreted as a sign that their ice never reached the liquid phase and so could still be found frozen in the interior (Jones et al. 1990; Carvano et al. 2003). These bodies would be possible candidates for the new class of MBCs.

The recent detection of water ice on the surface of 24 Themis (Campins et al. 2010; Rivkin & Emery 2010) came as no surprise, and give a strong support to the sublimation-driven explanation for the MBCs activity. At the end of 2009, two independent teams observing 24 Themis in the infrared range detected the presence of water ice widespread on the surface of the body. It has been interpreted as frost, replenished by some subsurface source. This detection, and those of main belt comets, are contributing to definitively shatter the old, traditional view of the...
main belt as the realm of rocky bodies as opposed to the icy, active bodies that can be found farther.

The implications deriving from the existence of a third source (besides the Oort cloud and the Edgeworth-Kuiper belt) of "cometary bodies" are remarkable. The water contained in the terrestrial oceans is thought to come from impacting icy bodies, but the few D/H ratios measured until now in comets have double values with respect to the average ratio obtained from terrestrial water. A third potential source for Earth water, different from long-period and short-period comets, could solve the problem, if the D/H ratio in MBCs will prove to be more similar to the terrestrial one.

2. The activity of main belt comets

Dust ejection due to sublimation implies the existence of both ice and dust particles. This leads us to imagine that MBCs are comet-like bodies, that means intimate mixtures of ice and dust, and not rubble-pile rocky objects with some ice filling the interstices. If this assumption is coupled with the further assumption that the activity is driven by sublimation, then we can simulate and study the activity of MBCs through the thermal modeling codes used for comets, KBOs and icy bodies in general.

Prialnik & Rosenberg (2009) applied their comet nuclei thermal evolution model to 177P/Elst-Pizarro. In their paper the authors demonstrate that deep-buried ice could have survived since the main belt formation time, and that this ice is most probably under 130 K, to have survived till now, even under an insulating mantle. The model is one-dimensional. The spherical nucleus is porous and composed of ices (water and up to two different species, typically CO and CO2) and a refractory component. Water ice can be initially amorphous, and in this case a fraction of gases such as CO can be trapped in the amorphous matrix and released during the transition to crystalline phase. In this work, anyway, we will deal only with water ice in its crystalline status. Together with Prialnik & Rosenberg (2009), we deem extremely improbable, for ices sublimating at temperatures well under 130 K, to have survived till now, even under an insulating mantle.

Energy and mass conservation is expressed by the following system of coupled differential equations, solved for the whole nucleus:

\[
\rho c \frac{\partial T}{\partial t} = \nabla [K \cdot \nabla T] + Q_i \\
\frac{1}{RT} \frac{\partial P_i}{\partial t} = \nabla [G_i \cdot \nabla P_i] + Q'_i 
\]

(1)

where \(\rho, c, K\) are the bulk density, specific heat and thermal conductivity, \(Q_i\) is the energy exchanged by the solid matrix in the sublimation and recondensation of the water ice, \(R\) is the gas constant, \(P_i\) the gas partial pressure, \(G_i\) its diffusion coefficient, and \(Q'_i\) is the gas source term due to sublimation-recondensation processes.

Gas diffusion coefficients are computed on the basis of the mean free path of the molecules in the pore system; the model accounts for three different diffusion regimes: Knudsen, viscous and a transition one.

The temperature on the surface is obtained by a balance between the solar input and the energy re-emitted in the infrared, conducted in the interior and used to sublime ices present on the surface. The following expression is used:

\[
\frac{S(1 - A_s) \cos \theta}{R^2_h} = \epsilon_\sigma T^4_s + K(T_s) \frac{dT}{dr} \mid_{r=R_h} + f_{H_2O} H(T_s) H_2O \delta(T_s) H_2O 
\]

(2)

where \(S\) is the solar constant, \(R_h\) the heliocentric distance of the comet, \(A_s\) the Bond bolometric albedo of the surface, \(\epsilon\) the infrared emissivity of surface, \(\sigma\) the Stefan-Boltzmann constant, \(K\) the thermal conductivity, and \(\delta\) the cometary latitude.

In the last term of right member of Eq. (2), \(f_{H_2O}\) represents the surface fraction covered by water ice, \(H\) is the latent heat of sublimation and \(\delta\) is the sublimation rate.

The surface boundary condition used to solve diffusion equation when ice is present on the surface is:

\[
P = P^{sat}(T).
\]

(3)

### Table 1. Main belt comets (as of May 2011).

<table>
<thead>
<tr>
<th>Name</th>
<th>(a) (AU)</th>
<th>(e)</th>
<th>(i) (°)</th>
<th>(P) (year)</th>
<th>(T)</th>
</tr>
</thead>
<tbody>
<tr>
<td>133P/Elst-Pizarro</td>
<td>3.156</td>
<td>0.165</td>
<td>1.39</td>
<td>5.62</td>
<td>3.184</td>
</tr>
<tr>
<td>P/2005 U1 (READ)</td>
<td>3.196</td>
<td>0.192</td>
<td>0.24</td>
<td>5.63</td>
<td>3.166</td>
</tr>
<tr>
<td>176P/LINEAR</td>
<td>3.165</td>
<td>0.253</td>
<td>1.27</td>
<td>5.71</td>
<td>3.15</td>
</tr>
<tr>
<td>P/2008 R1 (Garradd)</td>
<td>2.726</td>
<td>0.342</td>
<td>15.9</td>
<td>4.43</td>
<td>3.216</td>
</tr>
</tbody>
</table>

**Notes.** (a) Semimajor axis, (b) Eccentricity, (c) Inclination, (d) Orbital period, (e) Tisserand parameter.
When no ice is present, surface boundary condition is obtained assuming free sublimation at comet nucleus surface:

\[ P = 0. \]  

(4)

When the temperature rises, ices start to sublimate, beginning from the more volatile ones; even if the nucleus is initially homogeneous a differentiated, layered structure is always obtained, in which the boundary between different layers is a sublimation front. Surface erosion due to ice sublimation and particles ejection is taken into account.

The dust component is represented as size distributions of spherical grains characterized by a density, a specific heat and a thermal conductivity; in the code we can consider up to two distributions, with a maximum of ten size classes each. Dust distributions characteristics and their physical properties were chosen to simulate as much as possible Giotto findings. These experiments onboard of the mission demonstrated that in P/Halley’s refractory component it is possible to evidence two chemical phases: an organic one with low atomic weight, called CHON, and a Mg-rich silicate one (Jessberger & Kissel 1991; McDonnell et al. 1991; Mumma 1997). Measured particles were in the range of 10^{-16}–10^{-11} g. One third of it did not contain organic components, and the remainder was a mixture of the two phases; CHON component was probably coating silicate cores. Average densities were found to be 2500 kg m^{-3} for silicate grains and 1000 kg m^{-3} for CHON-dominated particles.

For these reasons, the dust component is simulated by two distributions: the first distribution is composed of silicatic particles, and the second one by mixed silicatic/CHON particles. The characteristics attributed to the two distributions are collected in Table 2, and are explained hereafter.

Table 2. Properties of the dust distributions.

<table>
<thead>
<tr>
<th>Property</th>
<th>Silicatic</th>
<th>CHON/organic</th>
</tr>
</thead>
<tbody>
<tr>
<td>Size classes</td>
<td>6</td>
<td>6</td>
</tr>
<tr>
<td>Size ranges (m)</td>
<td>10^{-6}–10^{-1}</td>
<td>10^{-8}–10^{-1}</td>
</tr>
<tr>
<td>Density (kg m^{-3})</td>
<td>2.5 \times 10^{3}</td>
<td>1.0 \times 10^{3}</td>
</tr>
<tr>
<td>Conductivity (grain) (K kg^{-1} m^{-3})</td>
<td>3</td>
<td>0.25</td>
</tr>
<tr>
<td>Conductivity (mantle) (K kg^{-1} m^{-3})</td>
<td>0.01</td>
<td>0.2</td>
</tr>
</tbody>
</table>

These two phases have different physical properties (density, thermal conductivity, and so on); as a consequence, the characteristics (thermal conductivity, tensile strength and cohesion) of a crust mainly composed of silicatic particles would be different from those of a crust with an abundant component of refractory organic material.

For the grains of the first distribution a thermal conductivity value of 3 W K^{-1} m^{-1}, typical of silicates, has been adopted, while for the CHON-dominated grains a value of 0.25 W K^{-1} m^{-1}, typical of organic substances thought to be analogues of cometary organic material (Kömle et al. 1996), has been preferred. Average density is 2500 kg m^{-3} in the first distribution, and 1000 kg m^{-3} in the second one, accordingly with Giotto findings.

The size distributions of dust particles in the nucleus could be different from those measured in the coma: observed particles are the smaller ones, and larger particles can be seen only by radar (Harmon et al. 1999). The observed exponential distributions could be the results of fragmentation processes in the inner coma. A way to define an initial size distribution in the nucleus could be to suppose that the grains are the result of the coagulation processes acting in the protosolar nebula: following this idea, we attributed to both kind of grains a gaussian distribution taken from a paper by Coradini et al. (1977) on the accretion of grains in the solar nebula.

It remains to define a value for the conductivity of a silicate-dominated crust and for the conductivity of a crust with a high abundance of organic refractory material. It was found, during KOSI experiments (Grün et al. 1993), that thermal conductivity of dust layers composed of silicatic grains is very low (~10^{-2}–10^{-3} W K^{-1} m^{-1}); even a thin layer of dust causes a large temperature gradient. Following this result, we attributed a value of 0.01 W K^{-1} m^{-3} to the thermal conductivity of a crust composed only of silicatic particles. In the case of the “organic” distribution, lacking for direct measurements, we deduced the physical properties from the results of the laboratory experiments conducted at the Space Research Institute of Graz (Kömle et al. 1996). The thermal evolution of an analogue of cometary material composed of a mixture of minerals, ices and hydrocarbons has been studied, obtaining a sort of cohesive crust composed of minerals glued together by organic materials. This kind of crust has a thermal conductivity higher than that of silicatic crust, and also has a higher cohesive strength: an admixture with organic material raises crust conductivity of one order of magnitude or more with respect to a crust composed of silicatic grains. So, our “organic” crust is characterized by a higher thermal conductivity than the “silicatic” one: we attributed to a crust mainly composed of organic particles a value of 0.2 W K^{-1} m^{-1}.

At the beginning of computations the dust particles are embedded in the porous ice. When the ice sublimates the embedded particles become free, in a number proportional to the amount of sublimated ice, and can undergo the drag exerted by the gas flux. Average pore size is increasing due to the ice sublimation: a “pore widening factor” proportional to the amount of sublimated ice is locally applied to the pore average size. In this way we are taking into account that a sublimating ice produces holes and cavities, and as a consequence free particles can move towards the surface (particles can move and be blown off only if their size is less than the local average pore size!). Free particles that are found close to the surface can move toward the surface and be blown off or accumulate to form a dust mantle. Free particles are moving under the opposite effects of gravity and gas flux; only grains smaller than the pore average size can move toward the surface in the pore system. When the ice is condensing, a proportional amount of free particles become embedded and the pores becomes smaller (porosity decreases).

To determine how many particles can be blown off to contribute to dust flux, and how many can instead be accumulated on the surface, the different forces acting on the single grain are compared, obtaining for each distribution a critical radius, depending on grain density. The critical radius represents the radius of the largest particle that can leave the surface of the comet:

\[ a^* = \frac{3}{4} \rho_{	ext{dust}} \left( \frac{G M_a}{R_R^3} \right)^{1/2} \sin \theta \left[ \frac{H_2O}{V_{H_2O}} \right] \]  

(5)

where \( G \) is the gravitational constant, \( M_a \) the mass of the comet, \( R_R \) its radius, \( \omega \) its angular rotation velocity, \( \rho_{	ext{dust}} \) the dust grain density, \( \Phi_{H_2O} \) is the gas flux, and \( V_{H_2O} \) the velocity of the gas flux. In the Eq. (5) the numerator represents the lifting force exerted by the outflowing gases, and the denominator represents the gravitational attraction corrected by the centrifugal force. At each time step the number of free dust particles for each size class and the value of the critical radius are computed. All the free particles with radius \( a < a^* \) are considered ejected (blown off) and contribute to the dust flux, while those with \( a \geq a^* \)
accumulate on the surface. This refractory surface layer (dust mantle) is not necessarily stable, and can be later on blown off if the gas flux is strong enough. It could also increase in thickness if more and more particles are not able to leave the surface, substantially reducing and then quenching the gas flux. Dust mantle compaction due to a volume reduction when ice is sublimated is taken into account. If the dust mantle is not too thick the gas flux from the interior is able to entrain a dust flux, so it is possible to have a dust flux even when there is no ice left on the surface.

In this way, even an originally homogeneous body becomes quickly highly inhomogeneous: composition, density and porosity are changing with depth.

### 2.2. Thermal modeling of P/Read

A thermal model depends not only on the assumptions of the model itself, but also on the values attributed to the initial parameters. These parameters describe the orbit, the initial state of the body and the properties of the matter of which it is composed. They are defined or derived, when possible, from observation and laboratory experiments. A given set of these parameters define a “Case”. By changing a small number of these parameters, and keeping fixed all the rest, we can build different Cases that are the subject of the simulation.

To apply the above described model to a real case we need to define the characteristics of the body that we want to simulate, assuming an initial structure and composition. As for the real case, we chose to simulate the behaviour of P/2005 U1 (Read). The results of this simulation can be applied also to the other MBCs known until now, because orbits and sizes are reasonably similar.

As written before, we start from the assumption that the model body has a cometary nature, that is it is composed of ice and dust grains. A further assumption is being made that the surface of the body is covered by a devolatilized mantle, and that a recently happened impact has opened a crater in this mantles. As a consequence, the heat from the Sun is now able to reach ice-rich layers, so triggering a cometary-like activity (sublimating gas entraining dust particles). At the beginning of the simulation, the immediate effects of the impact (release of heat) have already ceased.

As for the composition and physical properties, it is difficult to make safe assumptions. We have no reason to think, anyway, that these bodies are absolutely similar to the classical comets (Jupiter-family, Halley-family and Long Period comets), because their origin and evolution history is different. They formed closer to the Sun than the comets now stocked in the Kuiper Belt or Oort cloud. During the solar system formation period materials from different distances from the Sun were mixing up and the snow line could have been closer to the Sun than nowadays: this can explain the presence of dust-ice bodies orbiting what is now the main belt. Collision evolution also played a major role in the past of these bodies, probable survivors of the catastrophic event that gave origin to Themis family. Hardly the ice now remaining in MBCs was formed in the amorphous state, because this requires extremely low temperatures (much lower than 50 K). For similar reasons, it is extremely improbable that this ice could still be mixed with other ices more volatile than water that, even if they existed, should have been disappeared long time ago. We will make the assumption that the model body contains only H2O crystalline ice.

Some of the values given to the initial parameters of the model are listed in the Table 3. The properties attributed to the dust distribution are listed in the first column of the Table 2.

<table>
<thead>
<tr>
<th>Property</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>3.165</td>
</tr>
<tr>
<td>e</td>
<td>0.253</td>
</tr>
<tr>
<td>Dust/ice</td>
<td>3</td>
</tr>
<tr>
<td>Initial temperature (K)</td>
<td>130</td>
</tr>
<tr>
<td>Surface albedo</td>
<td>0.04</td>
</tr>
<tr>
<td>Surface emissivity</td>
<td>0.96</td>
</tr>
<tr>
<td>Spin period (h)</td>
<td>10</td>
</tr>
<tr>
<td>Initial pore radius (m)</td>
<td>10^{-4}</td>
</tr>
<tr>
<td>Initial porosity</td>
<td>0.4</td>
</tr>
<tr>
<td>Initial radius (km)</td>
<td>0.3</td>
</tr>
</tbody>
</table>

The values given to orbital parameters (semimajor axis and eccentricity) and to the radius of the model body are derived from observation, and refers to P/2005 U1 (Read). The values given to surface albedo, emissivity, and pore radius can be considered typical of comets, and are largely used in comet modeling (Huebner et al. 2006). The spin period is not known, so we are using a value (10 h) typical of many small bodies. The value for dust/ice ratio we are using in this simulation is 3, higher than the one usually assumed for comets (1), as a way to take into account the origin of the comet in a zone of the solar system less rich in volatiles. The porosity is 0.4. The initial temperature, 130 K, has been defined taking into account the orbit of the body.

The dust component is described as a distribution of 6 size classes with similar density and thermal conductivity (see Table 2).

The model was run in the fixed-latitude approximation. The reasons for this choice are that the rotation period is not known, and the variations of gas and dust production with respect to the daily hour are irrelevant for the present analysis. In this way, gas and dust production rates depend only on the latitude and on the position along the orbit.

### 2.3. Results: exposed ice

Case 1 has been ran assuming that the impact has directly exposed to the sun heating an icy zone located at given cometo-centric latitude. The model is ran for 4 different latitudes of the impact crater: equator (sub-solar point), 30°, 60° and 85°. The dust component is represented by one distribution, the silicatic one (first column of Table 2). With these parameters, bulk thermal conductivity along the whole evolution has an average value of 0.07 K kg^{-1} m^{-3}; average density values for the matter composing the model body are of the order of 586 kg m^{-3}.

The results can be seen in Figs. 1–4, showing, respectively, gas and dust fluxes, stratigraphy and internal temperature profile. After a time of almost 900 years, the ice material exposed by the impact at the subsolar point is completely consumed, and gas flux, that has been continuously reducing (Fig. 1, upper panels), is completely quenched. At all the latitudes, most of the dusty material is left behind: not all the dust grains freed from the ice are going to contribute to the dust flux. At higher latitudes the situation is different, as can be seen in the bottom left panel of Fig. 1, showing the gas flux with respect to heliocentric distance for impacts at the equator, 30° and at 60°. In the bottom right panel of the same figure the water gas flux with respect to heliocentric distance is shown for an impact at a latitude of 85°. In this case, the flux is extremely reduced. Bottom panels show the gas flux ten years after the impact exposing the ice-rich layers.

The dust flux with respect to time for an impact on the planet at a period of 60 years, starting 10 years after the impact, is
Fig. 1. Case 1 – Water flux along the orbit for a P/Read-like body on which an impact has exposed ice-rich layers. Upper left panel: impact at the equator, water flux with respect to time, for the first 140 years after the impact; upper right panel: impact at the equator, water flux with respect to time for a period of one hundred years immediately before the disintegration of the available icy material; bottom left panel: impact at the equator (upper curve) and at 30° (lower curve), water flux with respect to heliocentric distance. The fluxes are shown 10 years after the impact; bottom right panel: impact at 85°, water flux with respect to heliocentric distance. The flux is shown 10 years after the impact.

Fig. 2. Case 1 – Impact at the equator, dust flux with respect to time for a period of 60 years following the impact.

Fig. 3. Case 1 – Stratigraphy showing the erosion of the surface with respect to time. Upper panel: impact at the equator (lower black curve) and at 30° (red curve); lower panel: impact at 60° (lower black curve) and 85° (orange curve). At the beginning of computations, the surface has always a radius of 300 m. Depending on the latitude of the impact, the radius shrinks with respect to time.

Fig. 4. Case 1 – Internal temperature profile for a P/Read-like body at the aphelion, 900 years after the impact; impact at the equator (panel a) and at 85° (panel b)).

The erosion level of the surface of the crater varies with the latitude of the impact and is proportional to the intensity of dust and gas emissions, as can be seen in Fig. 3, showing the stratigraphy (surface radius, in meters, with respect to time in years) for a period of 50 years after the impact: it is almost null close to the poles (lower panel), where the solar input is minimum, while at the sub-solar point the available ice is consumed in less than one thousand years (almost two meters of surface lost per orbit, upper panel).

The temperature profiles shown in Fig. 4 are photographing the situation at the aphelion, after almost 9 hundreds years of revolutions around the Sun. At the equator only 30 m of active material remain (panel a), while at 85° of latitude (panel b) not even 1 cm of surface has been lost. Surface and interior temperatures give an explanation for this difference: at temperatures equal or less than 145 K, as is the case at latitudes close to the pole, water ice can be considered stable against sublimation. At equator, in the 30 m of icy material remaining after 900 years of activity, interior temperatures are much higher, always well above the sublimation limit. The first 5 m under the surface are under the influence of the orbital heat wave. In the deeper layers the temperature slowly decreases until it reaches 155 K, 25 K higher than the temperature at the time of the impact (130 K).

2.4. Results: mantle-covered ice

In order to trigger some activity, it is not necessary that the impact exposes directly icy-rich layers to the action of the Sun. The result of a shallow impact in a devolatilized mantle could
be excavate a crater, without directly exposing ice-rich layers, but leaving only a thinner dust layer covering regions that had remained safely buried for millions of years. In this case it could be possible not only activate the body (as a consequence of the impact itself) but also generate a stable or periodic activity, although fainter than in the situation described in the preceding section. It is well known that ice sublimation can be possible from under a mantled surface (see, for example, Capria et al. 2001), providing that ice-rich layers are reasonably close to the surface and the mantle itself is somewhat porous. This phenomenon has been observed, for example, on the comet 9P/Tempel 1, target of Deep Impact. The few small patches of icy surface visible in the returned images are not enough to account for the activity of the comet, if sublimation from the mantled zones is not considered (Belton and Melosh 2009).

To simulate this kind of activity, 4 Cases have been run with different assumption than in the preceding section: the bottom of the crater is still covered by a dust layer that has survived the impact. In this case, the duration and intensity of the activity depend strongly on the mantle thickness and physical properties. It would be impossible to run Cases exploring all the different combination of input parameters having a direct influence on the results. Two different thicknesses (0.1 and 0.5 m) and two extremely different compositions (silicatic and organic/CHON) have been considered for the surviving dust layer, obtaining 4 Cases (see Table 4). The thickness of the mantle before the impact should have been much larger: in order to keep sealed volatile materials on an extremely long timescale, tens of meters of insulating materials are necessary (see also Schorghofer 2008). The surviving dust layer thicknesses to be tested have been chosen somewhat arbitrarily, on the basis of our preceding experience on comet nucleus modeling. The results of these Cases can be easily extrapolated to different thicknesses of the surviving dust layer.

The aim of testing two different dust compositions is instead to show how the characteristics of the activity would depend on the physical properties of the involved materials: we are aware that pure silicatic or pure organic dust are somewhat unrealistic. The different compositions correspond in the code to two dust distributions with the characteristics listed in Table 2. The remaining input parameters are the same as the ones listed in Table 3. The impact point is always assumed at the equator (subsolar point).

Figures 5–7 show the result of these 4 Cases. In Fig. 5 the gas flux is shown for a body with a 0.1 m thick surviving mantle layer, assuming a silicatic composition (upper panels, Case 2) and an organic composition (bottom panels, Case 4). The left panels show the evolution of the water flux in the years following the impact, while the right panels show the flux after almost 500 years after the impact. A similar Fig. 6 show the result of Cases 3 and 5, where the thickness of the surviving mantle is 0.5 m.

A quite obvious result is that the water ice is sublimating with a rate much lower than in Case 1, depending on the thickness of the surviving dust layer: between Cases 2, 4 (0.1 m thick layer) and Cases 3, 5 (0.5 m thick layer) there are orders of magnitude of difference. Less obvious are the long-term evolution, and the dependence of the activity on the properties of the material forming the dust layer. When the computations begin, the interior temperature of the body is homogeneous and equal to...
the given initial temperature, 130 K in this case. With the passing of the years, the interior temperature slowly increases, and this corresponds to an increase in the sublimation rate. The process goes on till the interior temperature stabilizes, along with the sublimation rate (right panels in Figs. 5 and 6). Surface temperatures, mainly determined by solar input, are spanning the range from 148 K to 191 K in all the four Cases.

Due to the action of two competing processes, the thickness of the surviving dust layer changes, even by few millimeters, in the time after the impact. After 5000 years, in Cases 2 and 4 the thickness of the mantle has increased, at the bottom, by 15 cm and almost 12 cm respectively. This increase is the result of the slow devolatilization of the ice-rich layers adjacent to the bottom of the mantle. During the same time, a faint dust flux has eroded the surface by 2 and 3 mm in the two Cases. As for the Cases in which the initial thickness of the mantle was higher, after 5000 years of evolution less than 5 cm of devolatilized material has been added at the bottom of the crust, while the surface erosion is less than 2 mm in Case 5 and nothing in Case 3.

The different values attributed to the thermal conductivity and density of the refractory component of the model body (see Table 2) explain the differences in the activity between the Cases 2, 3 and 4, 5. Due to the higher thermal conductivity of silicatic grains, in Cases 2 and 4 higher internal temperatures are attained with respect to Cases 4 and 5. Figure 7 shows the temperature profiles of Cases 3 and 5, at the beginning (left panels) and towards the end of computation (right panels). The strong temperature gradient between the surface and the sublimation front (where water ice, mixed with dust, still survives), is visible, along with the difference in surface temperature between the aphelion, at 3.96 AU, and a point on the orbit, 3.16, closer to perihelion (2.36 AU).

At a certain point, the increase in the internal temperature ceases because an equilibrium temperature has been reached. This process has a different duration depending on the physical properties of the materials forming the body. It can be noticed that when the computation stops, 5000 years after the impact, the model bodies are still active, and it is reasonable to assume that they will continue to be active for a very long time. As for the thickness of the surviving dust layer, there are two competitive processes at work: dust emission from the surface (and the closest layers), and progressive devolatilization of layers close to the bottom of the mantle. The second process is the winner, and so the thickness of the mantle is slowly growing. As a consequence, the gas flux is slowly reducing. In order to study how much time would the body remain active, much longer, and heavy, computations would be required. This will be the subject of a future work.

2.5. Comparison with observation

The results of the theoretical models should now be compared with observations. Only in this way would it be possible to judge which ones, between the different Cases presented in the above sections, are closer to reality. Unfortunately, what we have from observation about P/Read is not enough to make possible such a comparison. From the paper by Hsieh et al. (2009a), who observed this object for almost three months in 2005 and one night in 2007, P/Read has been always found active in 2005, while in 2007 it was too faint to permit an estimation of the activity level. It must be noted that P/Read in July 2005 passed at its perihelion, and the aphelion passage was in May 2008, a few months after the observation of 2007. In 2005, coma and tail were clearly visible. Monte Carlo numerical simulation of dust emission indicates that coma and tail were optically dominated by dust grains greater than 10 micron. Mass-loss rate has been estimated to be of the order of 0.2 kg s⁻¹. Dust emission probably began at least few months before the discovery of the activity (October 2005).

This estimation of dust emission rate cannot be directly compared with the results of the 5 Cases shown before, because we have no idea if the activity is confined at the bottom of a crater or if it is instead widespread on large areas of the surface. In order to give some numbers, let us make the assumption that only the bottom of a recently excavated crater at the subsolar point is the source of the observed activity (the walls would not contain volatile material). The surface area of P/Read is approximately 1.1 × 10⁶ m². If we assume a dust production rate, at the equator, of 8.8 × 10⁻⁶ kg s⁻¹ m⁻² (Fig. 2), in order to obtain the observed dust emission rate we need an active area of approximately 2.3 × 10⁶ m². The evaluation, in turn, gives a very rough estimation of the depth of the crater, if we assume a bowl-like shape. The implied crater diameter, for a planar surface, is ~170 m. Assuming a depth-to-diameter ratio of 0.2 (Melosh 1989), the corresponding crater depth is ~34 m. This number cannot be interpreted as a precise measure of the thickness of the original mantle of P/Read (could have been thinner at the impact point), but is only useful to give an idea of the orders of magnitude involved. This rough computation is performed for a crater close to the subsolar point: in case of an impact at a higher latitude, all the numbers should be scaled correspondingly.

The crater size estimate given above is a lower limit. It would apply only for inert mantle thickness much lower that the estimated crater depth. However, we expect that MBCs have mantles thickness of the order of tens of meters because thinner mantles would have not been able to prevent the complete sublimation of volatiles for MBC-sized objects. For instance, in the case that a thickness of half of excavated depth consist of inert mantle, the same active area is obtained for a crater diameter about √2 times larger.

Looking to the plots in Figs. 1, 2, 5 and 6, the hypothesis of an impact leaving a mantled bottom appears much less compatible with observation, unless we consider a surviving dust layer much thinner that in the Cases 2, 3, 4 and 5: the activity level is so faint that it would be hardly detected from ground.

3. How frequent are the impacts?

In order to address if cratering events are a viable process to explain the observed activity and number of MBCs, it is important to estimate not only the size of the crater required to sustain the observed activity, but also the frequency of its formation.

The estimate of the projectile size needed to form a crater of 170 m has been performed considering two scaling laws,

<table>
<thead>
<tr>
<th>Case</th>
<th>Dust distribution</th>
<th>Thickness of the dust layer at impact location (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>silicatic</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>silicatic</td>
<td>0.1</td>
</tr>
<tr>
<td></td>
<td>silicatic</td>
<td>0.5</td>
</tr>
<tr>
<td></td>
<td>organic</td>
<td>0.1</td>
</tr>
<tr>
<td></td>
<td>organic</td>
<td>0.5</td>
</tr>
</tbody>
</table>

Table 4. Input parameters characterizing the surviving dust layer at the point of the impact in the 5 Cases.

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namely for porous material and cohesive soils (Holsapple & Housen 2007). The material strength has been set to $2 \times 10^4$ and $10^3$ dyne/cm$^2$. We assumed a target and projectile density of 1000 kg/m$^3$ and 2600 kg/m$^3$ respectively. Moreover, the computed P/Read intrinsic average impact probability within the main belt is about $3.48 \times 10^{-6}$ km$^2$ yr$^{-1}$ and the average impact velocity is about 3.7 km s$^{-1}$. These values are computed according to the Bottke et al. (2005) main belt population, and following the procedure described in the work of Marchi et al. (2010). The derived projectile sizes are ~8, 18.5 m for porous and cohesive material, respectively.

The computed time for having a collision with a projectile $\geq 8$ m on a body with the size of P/Read (0.6 km) is $5.1 \times 10^7$ yr. The estimated total number of objects larger than 0.6 km is $2.9 \times 10^9$, therefore such a collision is expected to occur on average every ~17 yr everywhere in the main belt. This time become $\sim 147$ yr for projectiles $\geq 18.5$ m.

Of course these numbers have to be taken as a rough indication, given the uncertainties in the main belt size distribution at such small size and in the target material parameters. Note that the timescales above also depend on the target size. For a body having the size of Elst-Pizarro (5 km), it is estimated that the same impacts occur every ~10 and ~100 yr, respectively for projectiles of 8 and 18.5 m.

4. Discussion

When running a simulation, it would be impossible to test all the possible combination of input parameters. What is usually done is, once found a meaningful combination, to keep fixed values for most of the parameters and vary only one or two at a time, in order to test the influence of the changes on the results. The variable parameters are the ones considered to be most influential on the properties or phenomena that are the object of the simulation. In this paper, an initial composition for P/2005 U1 (Read) has been assumed, and we have varied, to build the 5 Cases that have been studied, the parameters defining the thickness and composition of the dust mantle. As for the possible effects of changing the value attributed to the remaining initial parameters, it is here discussed on the basis of our experience.

A lower value of dust/ice, (for example, a value of 1, usually attributed to classical comets) would give as a result a lower dust flux, and consequently a slower erosion of the surface. Changing the thermal conductivity, porosity, density, pore radius would have the effect of slowing or quickening the evolution of the model body. The thickness of the surviving mantle in the Cases 2, 3, 4 and 5 has been chosen in a quite arbitrary way. It is clear, anyway, that a larger thickness would tend to completely quench any possible activity. The mantle thickness necessary to completely block the underneath sublimation strongly depends on the average porosity, thermal conductivity and the other physical properties of the dust layer.

The issue of the initial temperature attributed to the model body deserves some more discussion. Surface temperature is mainly determined by the solar input, and is spanning, along the orbit followed by the model body, the range 147–190 K (subsol lar point, fast rotator approximation). Obviously, nobody knows what really is the average internal temperature (below diurnal and seasonal skin depth) of such a body, but the assumption has been made that it should be around 130 K, a value at which water ice can survive. When the insulating mantle is disrupted, the internal temperature is steadily rising till an equilibrium value is reached. A different value of the initial temperature would result in a slowing or quickening of this process.

In this paper the possible effect of a single impact has been simulated. During the long time spent orbiting around the Sun, many small impactors hit the surface of bodies in the main belt. Even if these impacts are not able to disrupt the insulating mantle, it is probable that they are producing some changes on the surface. The effect of the impact itself, and of the released heat, could be that, for example, of locally compacting a porous surface mantle and locally changing its properties.

The results obtained for P/2005 U1 (Read) can be easily applied to the other MBCs known until now, because they are all revolving on similar orbits, with the only possible exception of P/2008 R1 (Garradd), that is coming closer to the Sun at perihelion. For this object, solar input is slightly higher and the results obtained for P/2005 U1 (Read) should be consequently scaled.

From the results of these simulation (in particular of Cases 2 to 4), it is also possible to understand how icy material buried deep enough under an insulating mantle could have survived for such a long span of time. A thorough analysis of this process will be the subject of a future paper. As for the origin of these ice-rich layers still surviving in bodies orbiting well inside the snow line border, it must probably be sought in the chaotic processes that were shaping the solar system at the beginning of its history, bringing bodies away from their formation places.

5. Summary and conclusions

Assuming that the newly discovered main belt comets are icy bodies on which a stable cometary activity has been induced by a recent impact that excavated a crater in a dust mantle, two different scenarios have been simulated. In the first one, it has been assumed that ice-rich layers, remained buried under an insulating dust layer for a very long period of time, are now directly exposed to Sun heating. In the second one, it has been assumed that the bottom of the newly excavated crater is still covered by a layer of dust much thinner than before the impact, so that the solar input is now able to reach ice-rich layers. The characteristics attributed to the model body are those of P/2005 U1 (Read).

It has been demonstrated that, given the existence of buried ice, the activity observed in the MBCs can be explained as cometary activity, that means dust emission sustained by ice sublimation.

In the first scenario, a stable cometary activity can be obtained, compatible with observations. Making a rough estimate, a crater at the subsolar point with a diameter of 170 m would be compatible with the observed dust production rate. The activity would be stable, but the water ice is quickly consumed, depending on the cometary latitude of the impact point. At the subsolar point, the surface erosion could reach two meters per orbit. When, as assumed in the second scenario, a dust layer still remains, covering the bottom of the crater, a stable activity is still possible, providing that the heat of the Sun is able to reach ice-rich layers underneath. The activity is much fainter and long lasting than in the preceding case, depending on the latitude of the impact and the physical properties of the dust mantle. This kind of activity is probably not compatible with the activity observed on P/2005 U1 (Read).

The computed time for having a collision with a projectile $\geq 8$ m on a body with the size of P/Read (0.6 km) is $5.1 \times 10^7$ yr. The estimated total number of objects larger than 0.6 km is $2.9 \times 10^9$, therefore such a collision is expected to occur on average every ~17 yr everywhere in the main belt. This time become $\sim 147$ yr for projectiles $\geq 18.5$ m. For a body having the size of Elst-Pizarro (5 km), it is estimated that the same impacts occur every ~10 and ~100 yr, respectively for projectiles of 8 and 18.5 m.
There are no clues as how many other MBCs could exists in the main belt. Surely the great majority of bodies still keeping some ice in their interior are presently inactive, or their activity is so faint that it cannot be detected, at least from Earth-based observation.

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