A polar+equatorial wind model for broad absorption line quasars

I. Fitting the C IV BAL profiles

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ABSTRACT

Context. Despite all the studies, the geometry of the wind at the origin of the blueshifted broad absorption lines (BAL) observed in nearly 20% of quasars still remains a matter of debate.

Aims. We want to see if a two-component polar+equatorial wind geometry can reproduce the typical BAL profiles observed in these objects.

Methods. We built a Monte Carlo radiative transfer code (called MCRT) to simulate the line profiles formed in a polar+equatorial wind in which the photons, emitted from a spherically symmetric core are resonantly scattered. Our goal is to reproduce typical C IV line profiles observed in BAL quasars and to identify the parameters governing the line profiles.

Results. The two-component wind model appears to be efficient in reproducing the BAL profiles from the P Cygni-type profiles to the more complex ones. Some profiles can also be reproduced with a pole-on view. Our simulations provide evidence of a high-velocity rotation of the wind around the polar axis in BAL quasars with non P Cygni-type line profiles.

Key words. quasars: absorption lines – radiative transfer – methods: numerical

1. Introduction

Depending on the selection technique and the definition used, about 20% to 30% of the quasars detected in recent surveys show the presence of the broad absorption line (BAL) troughs associated with the emission lines in their rest frame UV spectrum (e.g. Knigge et al. 2008; Ganguly et al. 2008). These BALs, reminiscent of the P Cygni-type profiles seen in the spectra of massive stars, are mainly observed in high ionization lines like C IV and Si IV and are sometimes detected in lower ionization species like Mg II. They reveal strong outflows from quasars (Scargle 1972), which can reach velocities up to 0.2 c (Foltz et al. 1983).

Despite the large number of observations, the physical and geometrical properties of the wind at the origin of the BALs remain largely unknown (e.g. Brotherton 2007). Moreover, the distance at which those objects are found (z ≥ 1.5, so that C IV is shifted in the optical domain) hampers direct observation of the regions at the origin of the BALs even with the best telescopes presently available. Thus, all the information we can get about the inner regions of BAL quasars comes mainly from indirect observations.

The first attempts to model the BAL profiles considered the resonant scattering of photons emitted by a continuum source in a spherically symmetric stellar-like wind (e.g. Scargle et al. 1972; Surdej & Hutsemékers 1987). However, the growing number of observed spectra displaying a huge variety of line profiles (Korista et al. 1993) revealed the need for other wind models.

Facing the diversity of line profiles, Turnshek (1984a) proposed that BAL quasars could be broadly divided into two samples: those quasars that exhibit smooth P Cygni-type profiles, and other ones that display an absorption trough that is detached in velocity from the associated weaker and wider emission peak. These observations indicate that the properties of the wind are more complex than the simple spherically symmetric outflow inferred for stellar winds (Lee & Blandford 1997). However, as emphasized by Turnshek (1984b), it is very likely that distinct types of BAL QSOs do not exist but are instead different manifestations of the same phenomenon.

The similarities of the emission line, optical continuum, and infrared properties of BAL and non-BAL QSOs (e.g. Weymann et al. 1991; Gallagher et al. 1999; Reichard et al. 2003; Gallagher et al. 2007), as well as the spectropolarimetric observations (e.g. Schmidt & Hines 1999; Ogle et al. 1999; Lamy & Hutsemékers 2004), favor a unification by orientation scheme for the BAL QSOs over the evolutionary scheme (Hazard et al. 1984; Becker et al. 2000). In the unification by orientation scheme, only a fraction (roughly corresponding to the observed fraction of BAL QSOs) of the continuum source is covered by optically thick material producing the broad absorption lines, which suggests a disk-like equatorial geometry for the BAL region (e.g. Turnshek 1984a; Hamann et al. 1993; Murray et al. 1995; Elvis et al. 2000; Yamamoto 2002). Such a geometry is supported by theoretical studies and commonly accepted, since the QSOs are thought to be powered by accretion of matter onto a supermassive black hole in the form of a disk, from which the wind could be launched. However, the recent discovery of radio loud BAL QSOs (e.g. Becker et al. 2000) and subsequent...
radio variability studies reveal polar outflows in at least some of them (Brotherton et al. 2006; Zhou et al. 2006; Ghosh & Punsly 2007). Models combining polar and equatorial components have also been suggested (e.g. Lamy & Hutsemékers 2004) and evaluated from a theoretical point of view (Pereyra et al. 2004; Proga et al. 2000; Proga 2003; Proga & Kallman 2004).

In this context and given the similarities between typical BAL profiles (e.g. Korista et al. 1993) and the line profiles produced by a two component polar+equatorial wind like the one presented by Bjorkman et al. (1994), our goal in this first paper is to determine whether such a simple two-component wind can qualitatively reproduce the various types of line profiles observed among the BAL QSOs. We also try to identify the key ingredients needed to reproduce BAL profiles. In a second paper, we will investigate the effect of microrelensing on these profiles, aiming at a realistic interpretation of the spectral differences observed in gravitationally lensed BAL QSOs like H1413+117 (cf. Hutsemékers et al. 2010).

In Sect. 2, we present MCRT, the Monte Carlo radiative transfer code we implemented in order to simulate resonance line profiles in a two-component axisymmetric wind. The use of the Monte Carlo simulation technique allows the radiative transfer equation to be solved exactly (i.e. without making use of the Sobolev approximation), as well as ensuring the self consistent treatment of the radiative coupling between distant regions in a wind subject to more complex velocity fields than monotonic radial laws (e.g. Knigge et al. 1995).

Monte Carlo RT code have been extensively described (e.g. Knigge et al. 1995; Wood et al. 2001; Dijkstra et al. 2006), so that we only recall here the fundamental principles of this technique and the particularities of the code we developed.

As stated in the introduction, our main goal is to identify of the key ingredients (geometry and overall kinematics) of the wind governing the typical profile of the BAL QSO UV resonance lines. Thus we do not consider negligible effects, such as the relativistic ones that remain small even for outflows with high \( v_{\text{max}} \leq 0.2 \) c terminal speed (Hutsemékers & Surdej 1990) or the fact that the line is a resonance doublet, because the velocity separation of the doublet components is small with respect to \( v_{\text{max}} \) (e.g. Hewitt et al. 1974; Grinin 1984).

### 2. The MCRT code

MCRT is a Fortran77 fully 3D Monte Carlo (MC) radiative transfer (RT) code that we built to compute the resonance line profiles produced in axisymmetric winds. The use of the Monte Carlo simulation technique allows the radiative transfer equation to be solved exactly (i.e. without making use of the Sobolev approximation), as well as ensuring the self consistent treatment of the radiative coupling between distant regions in a wind subject to more complex velocity fields than monotonic radial laws (e.g. Knigge et al. 1995).

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### 2.1. Radiative transfer with Monte Carlo techniques

When using the MC technique, the solution of the RT equation is found by following a huge number of photons on their way through the wind. Each step in the photon’s life (position and direction of emission, position of interaction, etc.) is determined by the mean of random numbers distributed according to the normalized probability density function (NPDF) of the corresponding simulated physical process. Thus if one wishes that the frequency \( v_i \) of all of the emitted photons follows a given law \( L(v) \) over the frequency interval \([v_{\text{min}}, v_{\text{max}}]\), then \( v_i \) will be randomly chosen by solving the transformation equation (Press et al. 1992):

\[
\xi = \int_{v_{\text{min}}}^{v_i} L(v) \, dv, \tag{1}
\]

where \( \xi \) is a random number drawn from a uniform distribution in the interval \([0, 1]\). In MCRT this number is generated using the “ran2” subroutine of Press et al. (1992). In the following, each new occurrence of \( \xi \) refers to the call of such a new random number. In general, there is seldom an analytical solution to Eq. (1) so we implemented the “table lookup method” (see Avery & House 1968), which allows us arbitrary NPDF’s.

In MCRT the initial position of emission of the photons is chosen isotropically on the surface of the continuum emission region, which is modeled by a sphere of radius \( R_{\text{a}} \) and of infinite optical depth (\( \tau_\infty = \infty \)) located at the center of the wind. The direction of travel through the wind is then determined by randomly sampling a half sphere taking into account that the photons are forced to leave the continuum source upward.

#### 2.2. Continuum photons and resonance scattering

The wind is filled with 2-level atoms whose rest-frame normalized absorption profile \( \phi_{\text{abs}} \) is described by a Gaussian (Natta & Beckwith 1986; Knigge et al. 1995) such that

\[
\phi_{\text{abs}}(v - v_0) = \left\{ \begin{array}{ll}
\phi_{\text{abs}}(v - v_0, \sigma_{\text{turb}}) & \text{if } |v - v_0| \leq |\Delta v_{\text{abs}}| \\
0 & \text{everywhere else,}
\end{array} \right. \tag{2}
\]

where \( v_0 \) is the rest-frame frequency of the considered transition, and

\[
\phi_{\text{abs}}(v - v_0, \sigma_{\text{turb}}) = \frac{1}{H} \left\{ \frac{1}{2 \sqrt{\pi} \sigma_{\text{turb}}} \exp \left( \frac{-(v - v_0)^2}{\sigma_{\text{turb}}^2} \right) + K \right\}, \tag{3}
\]

in which \( K \) ensures a continuous transition between the absorption profile and the zero intensity. Here, \( H \) is a constant allowing for the normalization of the line profile over the interval \( v_0 \pm |\Delta v_{\text{abs}}|/2 \), where \( \Delta v_{\text{abs}} \) is the full width at zero intensity (FWZI) of the absorption profile. We choose the value of \( \Delta v_{\text{abs}} \) to ensure the continuity of the absorption profile at the border of the interval \( v_0 \pm |\Delta v_{\text{abs}}|/2 \). The parameter \( \sigma_{\text{turb}} = \Delta v_{\text{FWZI}}/(2 \sqrt{\ln 2}) \) is such that \( \Delta v_{\text{FWZI}} = 2 v_0 (\sigma_{\text{turb}}/c) \) is the FWHM of the absorption profile. The velocity \( v_{\text{urb}} \) includes the thermal and the macroscopic turbulence components in the wind that broaden the absorption profile. We assume \( v_{\text{urb}} \) to be constant throughout the wind.

Owing to the velocity field \( \mathbf{v}(r, \theta, \phi) \) present in the wind, the initial frequency \( v_i \) of a photon flying in the direction \( \mathbf{n} \) is seen Doppler-shifted by an atom of the wind in such a way that its “local” frequency \( v_l \) in the atom rest-frame is given by

\[
v_l = v_i \left( 1 - \frac{\mathbf{n} \cdot \mathbf{v}}{c} \right). \tag{4}
\]

Thus a photon will enter in resonance with the surrounding atoms only if its local frequency fulfills the condition defining the so-called “resonance zone”:

\[
v_0 - \frac{\Delta v_{\text{abs}}}{2} < v_l < v_0 + \frac{\Delta v_{\text{abs}}}{2}. \tag{5}
\]

When the photon enters such a region, the opacity of the medium becomes nonzero as does the probability of being absorbed.
If \( n \) resonance zones are found along the direction of propagation of the photon in the wind, the total optical depth \( \tau_{\text{tot}} \) seen by the photon until it escapes the wind is simply computed as

\[
\tau_{\text{tot}}(v_i) = \sum_{j=1}^{n} \int_{s_j}^{s_{j+1}} \kappa_{\nu} \phi_{\text{abs}}(v_i - v_0, \sigma_{\text{turb}}) \, ds,
\]

where \( \kappa_{\nu} \) is the total absorption coefficient of the considered resonance transition, and \( s_j \) and \( s_{j+1} \) are respectively the coordinates of the beginning and of the end of the \( j \)th resonance zone found along the line of flight of the photon.

Given the probabilistic interpretation of the RT, a photon experiencing a total optical depth of \( \tau_{\text{tot}}(v_i) \) has a probability \( p = e^{-\tau_{\text{tot}}(v_i)} \) of escaping the medium without being absorbed. This interpretation is used in the MC code to identify the occurrence and the position of the scattering sites along the path of the photon through the wind. Indeed by using the transformation equation (Eq. (1)) we can determine the random optical depth \( \tau_{\text{MC}} \) at which the photon interacts:

\[
\tau_{\text{MC}} = -\ln(1 - \xi).
\]

Because we stored the run of \( \tau_{\text{tot}} = \tau_{\text{MC}}(s) \) along the photon path, it is easy to invert this relation and find the point \( s \) where \( \tau_{\text{MC}} = \tau_{\text{tot}} \). At this location the photon is radiatively absorbed and then instantaneously re-emitted at a frequency and in a direction chosen by assuming a complete redistribution in frequency and direction (CRFD, Lucy 1971; Mihalas et al. 1976). This photon may then either be re-absorbed somewhere else in the wind or leave it and be detected by one of the detector (spectrographs, imagers) located around the wind.

To decrease the simulation time in the case of non-spherically symmetric winds we make an intense use of the advanced concepts of “first forced interaction” (e.g. Cashwell & Everett 1959; Witt 1977) and “peeling off” (e.g. Yusef-Zadeh et al. 1984; Wood & Reynolds 1999) where we follow a photon packet rather than a single photon.

We checked the validity of our MCRT code by comparing the line profiles we obtained to line profiles computed with two traditional methods for spherical winds that allow an exact integration of the transfer equation. These benchmarks are the well-known SEI method of Lamers et al. (1987) and the comoving frame method of Hamann et al. (1981). We noted good agreement between the general shape of the computed profiles, regardless of the considered turbulence (\( \Delta F/F \leq 5\% \) on the normalized emission peak flux, as well as a good match between the absorption profiles). We also tested MCRT in the case of axi-symmetric winds by comparing the profiles obtained with MCRT to those produced by the SEI method adapted by Bjorkman et al. (1994). Once again we observed good agreement between the line profiles produced by both methods (see Borguet 2009, for details).

### 2.3. Pure emission

While the shape of the C IV line in BAL QSOs can be mostly governed by resonance scattering (Scargle et al. 1972), the presence of C III] emission constitutes evidence that part of the emission is due to collisional excitation (Turnshek 1984a, 1988; Hamann et al. 1993). To account for this second source of photons, we allow the production directly in the wind of a fraction of photons \( f_e = I_{\text{pure emission}}/I_{\text{continuum}} \). The choice of the location of the emission (\( r_e, \theta_e, \phi_e \)) of these photons is made using a random sampling of the corresponding NPDF:

\[
\xi = p(r_e, \theta_e, \phi_e) = \int_{r_0}^{r_0} \int_{\theta_0}^{\theta_0} \int_{\phi_0}^{\phi_0} \eta(r, \theta, \phi) \gamma^2 \sin \theta \, dr \, d\theta \, d\phi,
\]

where the \( \eta(r, \theta, \phi) \) is a function that describes the emissivity throughout the wind. Once again, our goal here is not to provide a detailed self-consistent model of the wind so we choose as a first guess an emissivity function of the form

\[
\eta(r, \theta, \phi) = n(r, \theta, \phi) \left( \frac{R_a}{r} \right)^{\gamma},
\]

where \( n(r, \theta, \phi) \) is the density of the ion through the wind and where the second term allows taking the temperature distribution and the ionization fraction into account. In the following we simply take \( \gamma = 1 \) in order to reduce the number of free parameters.

Each photon emitted then makes its way through the wind where it can be scattered and then finally escapes the wind in order to be detected by a distant observer.

### 2.4. The wind model

#### 2.4.1. Introduction

As stated in the introduction, it is difficult to give a simple explanation to the observed BAL profiles when using a spherically symmetric expanding wind. The obvious next type of geometry that can then be considered is the axi-symmetric one. The simplest of these models would still consist in a wind originating from the central core. Such a generic model, with polar and equatorial components like the one presented in details by Bjorkman et al. (1994) produces line profiles remarkably similar to those observed in some BAL QSOs. Although simple, this model is versatile enough to produce a variety of line profiles, as observed in BAL QSOs. It constitutes a first good approximation to the more complex wind from disk models proposed for AGN outflows in which the BALR and the BELR are generally cospatial (Sect. 1).

In our model, we adopt stellar wind laws to describe the kinematics of the winds observed in quasars. Indeed, quasar winds are also supposed to be driven by radiation (Arav & Li 1996; Murray et al. 1995) as suggested by the line-locking in the spectra of some BAL QSOs (e.g. Weymann et al. 1991; Korista et al. 1993; Arav 1996, 1997). However, there are important differences between stars and quasars (e.g. Arav 1994). One of them is the so-called overionization problem caused by the strong UV/X-ray central source in quasars (e.g. Proga et al. 2000). Several scenarios have been suggested to solve this problem: Murray et al. (1995), Murray & Chiang (1997), Risaliti & Elvis (2000), Punsly (1999) and Ghosh & Punsly (2007). In our study we assume the existence of shielding material between the radiation source and the outflow that prevents the total ionization of the outflow (see Krolik 1999).

Another difference between stellar objects and quasars comes from a significant fraction of the radiation in quasars supposedly being emitted from an accretion disk rather than from a spherically symmetric photosphere (e.g. Proga et al. 2000). Outflows with axial geometries have been studied by several authors, who show that the flow can be launched vertically from the disk and then pushed away by the radiation from the central source (Murray et al. 1995; Proga et al. 2000) with the elevation of the wind over the disk is still small when the flow...
starts to expand radially. Since the launching conditions are unclear (Risaliti & Elvis 2009) and since we assume the BALR and the BELR to be cospatial, we simplify the geometry by assuming that the wind is purely radial, which is correct at some distance from the disk. We considered a wind launched from a sphere with a radius equal to the inner radius of a typical BELR (10⁻² pc). The outer radius of the BELR/BALR was chosen to be 1 pc, the radius at which the wind reaches the terminal velocity. If needed, the anisotropy of the radiation field from the continuum source can be readily introduced into our model.

2.4.2. Velocity field and density law

Keeping in mind the aforementioned simplifications we then decided to implement the model described by Bjorkman et al. (1994). We recall its basic characteristics here. The velocity field \( \mathbf{v}(r, \theta, \phi) \) considered here can be written in spherical coordinates:

\[
\mathbf{v}(r, \theta, \phi) = v_r(r, \theta) \mathbf{e}_r + v_\theta(r, \theta) \mathbf{e}_\theta + v_\phi(r, \theta) \mathbf{e}_\phi,
\]

where for simplicity we assume, as in Bjorkman et al. (1994), that the streamlines lie on surfaces of constant polar angle so that \( v_\phi = 0 \). The radial component of the velocity field has the typical \( \beta \)-law shape:

\[
v_r(r, \theta) = v_{\text{min}} + (v_{\text{max}}(\theta) - v_{\text{min}}) \left( 1 - \frac{R_{\text{in}}}{r} \right)^\beta,
\]

where \( v_{\text{min}} \) is the wind speed at the surface of the source of the continuum. The variable terminal speed \( v_{\text{max}}(\theta) \) allows for the introduction of a slow expanding equatorial wind in a faster polar wind:

\[
v_{\text{max}}(\theta) = v_{\text{max}}^0(\theta) + (v_{\text{eq}}^0 - v_{\text{max}}^0) f(\theta),
\]

where \( v_{\text{eq}}^0 \) and \( v_{\text{max}}^0 \) are respectively the terminal velocity of the equatorial and the polar components. The function that allows the smooth transition between the two components of the wind takes the form

\[
f(\theta) = 0.5 \left[ 1 + \frac{2}{\pi} \arctan \left( \frac{\sin \Delta \theta - \cos \theta}{\Delta \theta} \right) \right],
\]

where \( \Delta \theta \) is the equatorial wind half opening angle and where the parameter \( \Delta \theta \) controls the transition between the equatorial and the polar components of the wind. We chose, as in to Bjorkman et al. (1994), a low value for \( \Delta \theta = 0.001 \) in order to keep this region much thinner than the equatorial wind opening angle.

The velocity component of the velocity field is simply given by assuming conservation of the angular momentum in the wind:

\[
v_\phi = \frac{V_{\text{rot}} R_{\text{in}}}{r} \sin \theta,
\]

where \( V_{\text{rot}} \) is the rotational speed at the surface of the source of the continuum.

The law governing the distribution of the ion density is derived from the equation of continuity of matter in a central wind and is parameterized using

\[
n(r, \theta, \phi) = n_0(\theta) \left( \frac{r}{R_{\text{in}}} \right)^{-\alpha} \left( \frac{v_r(r, \theta)}{v_{\text{min}}} \right)^{-1},
\]

with the parameter \( \alpha \) implicitly including the radial variation of the ionization (i.e. \( \alpha = 2 \) meaning a constant ionization throughout the wind) and \( n_0(\theta) \) allowing the transition between the polar and the equatorial components:

\[
n_0(\theta) = n_0^p + (n_0^e - n_0^p) f(\theta),
\]

Table 1. Wind parameter for the benchmark model.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( v_{\text{in}} )</td>
<td>10000 km s⁻¹</td>
<td>( \alpha )</td>
<td>2.00</td>
</tr>
<tr>
<td>( v_{\text{min}} )</td>
<td>100 km s⁻¹</td>
<td>( \beta )</td>
<td>1.00</td>
</tr>
<tr>
<td>( v_{\text{max}} )</td>
<td>2500 km s⁻¹</td>
<td>( \Delta \theta )</td>
<td>15°</td>
</tr>
<tr>
<td>( V_{\text{rot}} )</td>
<td>0 km s⁻¹</td>
<td>( \Delta \theta )</td>
<td>0.001</td>
</tr>
<tr>
<td>( v_{\text{turb}} )</td>
<td>500 km s⁻¹</td>
<td>( \gamma )</td>
<td>90°</td>
</tr>
<tr>
<td>( \tau_{\text{tot}} )</td>
<td>4.00</td>
<td>( f_c )</td>
<td>0.0</td>
</tr>
<tr>
<td>( k_{\text{pm}} )</td>
<td>10.0</td>
<td>( \gamma )</td>
<td>1.0</td>
</tr>
</tbody>
</table>

where \( n_0^e, n_0^p \) are, respectively, the density of the considered ion at the base of the wind in the equatorial or in the polar component. The value of \( n_0^p \) is computed by specifying the value \( \tau_{\text{tot}} \), the total optical depth of the wind along the pole axis (i.e. \( \theta = 0° \)) integrated over frequency:

\[
\tau_{\text{tot}} = \int_{-\Delta \nu}^{\Delta \nu} \tau(\nu) d\nu,
\]

with \( 2 \Delta \nu \) the measured width of the observed line profile. The value of \( n_0^e \) is fixed by the free parameter \( k_{\text{pm}} \), which defines the ratio of the ion density between the two components at the base of the wind:

\[
n_0^e = k_{\text{pm}} n_0^p.
\]

3. Parameter study

Here we concentrate on the main parameters affecting the line profiles for a two-component wind where we suppose no pure emission (i.e. \( f_c = 0 \)). We do not discuss the effects of the parameters governing the velocity and density laws or the effects of the turbulent component in the wind since they are similar to those observed in the well-understood spherically expanding wind case (Castor & Lamers 1979; Beckwith & Natta 1987; Hamman 1981; Lamers et al. 1987).

The most important parameters we have to specify for computing a line profile are the frequency integrated polar optical depth \( \tau_{\text{tot}} \), the ratio between the equatorial and the polar ionization density \( k_{\text{pm}} \), the velocity ratio between the polar and the equatorial terminal speed \( v_{\text{max}}^0/v_{\text{max}}^e \), the disk half-opening angle \( \Delta \theta \), the viewing angle \( \alpha \), and the ratio \( V_{\text{rot}}/v_{\text{max}}^0 \) between the rotational speed of the source of continuum and the polar terminal velocity. The parameters used for the reference line profile are summarized in Table 1. Such a parameter study was previously carried out by Bjorkman et al. (1994) using an SEI-type method. Because their calculations agree with ours using an exact method, we only recall here the general effects produced by each parameter and refer the reader to the Bjorkman et al. paper for further details. We do, however, emphasize the effect of the wind rotation given the important changes in the line profile produced by the variation of this parameter, more particularly when the equatorial disk is viewed near edge-on (Mazzali 1990; Petrenz & Puls 1996; Busche & Hillier 2005).

The profiles illustrated in the panel A of Fig. 2 are representative of the profiles that can be produced in a two-component wind when the equatorial component is seen near edge-on. The shape of these profiles is constituted by typical P Cygni-type profile extending to the higher velocities coming from the polar component, but where a sharp absorption trough is produced at lower velocities by the slowly expanding equatorial wind. In this panel we illustrate the evolution of the line profiles as
Fig. 1. Illustration in the $x-z$ plane of the two-component wind used in our MC simulations, the velocity field is pictured by arrows in the lower part of the picture. The equatorial wind is shown edge-on (in dark grey) so that the wind model is rotationally symmetric along the $z$ axis. The viewing angle of the observer is $i = 90^\circ$, and the absorption profile is produced by both component, the polar one contributing only at low velocities (i.e. for $x < r_{\text{lim}}$) given the disk opening angle and the viewing angle. Inspired from Fig. 8 of Bjorkman et al. (1994).

a function of the total polar optical depth integrated over frequencies $\tau_{\text{tot,p}}$. Similar to the spherically symmetric expanding wind case (e.g. the atlas constructed by Castor & Lamers 1979), when $\tau_{\text{tot,p}}$ is increased, we observe an increase in the emission peak and in the equivalent width of both the emission and absorption parts of the line profile. No variations are observed in the equatorial absorption since that part of the profile is already saturated for the lower value of $\tau_{\text{tot,p}}$.

The change in the ratio between the terminal speed $v_{\text{eq}}^{\text{max}}$ and $v_{\text{lim}}^{\text{po}}$ of the two components essentially modifies the position of the edge of the low-velocity absorption component (see panel C of Fig. 2). We also observe that, when $v_{\text{eq}}^{\text{max}}$ is increased, the absorption due to the presence of the disk no longer remains black near the line center. Indeed, to produce a black absorption, the disk has to cover the whole source of continuum. But for an equatorial wind with a half-opening angle $\Delta \theta$, this only happens beyond the radial coordinate $r > r_{\text{lim}} = R_{\text{in}} \cotan \Delta \theta$ (see Fig. 1), which corresponds to the velocity $v_{\text{eq}}^{\text{lim}} \sim v_{\gamma}(r_{\text{lim}}, 90^\circ)$, the value of which is sensitive to $v_{\text{max}}(\theta)$ (cf. Eq. (11)).

In panel D of Fig. 2, we illustrate the evolution of the line shape as a function of the half-opening angle of the equatorial wind $\Delta \theta$. We observe the development of a broad high-velocity absorption when $\Delta \theta$ is decreased. This observation is once more explained by considering the radial coordinate $r_{\text{lim}}$ at which the disk completely covers the source of the continuum. As the high-velocity absorption (due to the polar component) occurs to the equatorial wind, the high absorption velocity range is limited within the interval $[0, v_{\text{lim}}^{\text{po}}]$, where $v_{\text{lim}}^{\text{po}} \sim v_{\gamma}(r_{\text{lim}}, 0^\circ)$. In contrast, when $\Delta \theta$ is increased, we observe the apparition of a secondary blueshifted emission peak beyond $v_{\text{lim}}^{\text{po}}$ given that, for a sufficiently wide disk, there is no remaining polar absorption of the continuum.

The viewing angle $i$ to the wind plays a critical role in the line profile (see panel E of Fig. 2). Indeed the equatorial absorption component is only seen when the disk is viewed near edge-on (i.e. $i \approx 90^\circ$). Because $i$ is decreased from an edge-on to a pole-on ($i = 0^\circ$) view of the disk, the low-velocity absorption produced by the disk decreases, since only the high-velocity end of this component covers the continuum.

Finally, panel F of Fig. 2 illustrates the modifications of the line profile when varying the rotational speed of the wind. The major effect of the rotation is observed on the emission peak, which decreases and is significantly redshifted when the $V_{\text{rot}}/v_{\text{max}}$ ratio is increased. Indeed, when there is no rotation, the emission peak is relatively sharp because that part of the profile is produced in the inner, optically thicker regions of the wind, whose velocity range is narrow. When rotation is considered, the resonance zones become twisted in such a way that the inner regions are distributed over a wider range of projected velocity. This induces the smoothening of the emission peak since the rotation allows the absorption to occur in the redder part of the continuum at frequencies centered on the rest-frame frequency of the line transition $\nu_0$ (e.g. $X = 0.0$) (see Fig. 3 and also Hall et al. 2002, for a detailed explanation). The bluer part of the absorption profile is not significantly affected by the rotation because this part of the profile is produced in front of the continuum source, i.e. where the projected rotational velocity is nearly zero.

### 4. Fitting BAL profiles with the polar+equatorial wind model

In this section we try to reproduce a representative sample of C IV line profiles observed in BAL QSOs and extracted from the paper of Korista et al. (1993), which provides homogeneous and high-quality spectroscopic data for a large sample of BAL QSOs. Our goal is to check that such profiles can be modeled using a simple two-component wind geometry for the BALR. Ten spectra were carefully selected out of the 72 BAL QSOs presented in the Korista et al. paper on the basis of two criteria.

- We retained as far as possible objects free of doublet effects (i.e. $v_{\text{po}}^{\gamma} \gg$ C IV doublet separation), non-blended and with smooth emission/absorption C IV line profiles (i.e. those less affected by multiple absorption troughs).
- We selected objects for which the continuum can be securely defined on both sides of the C IV line profile, allowing for a correct normalization of the spectra.

The observed and the fitted spectra of each selected object are illustrated, normalized to the continuum level, in Figs. 4 and 5. We note good qualitative agreement between the observed line profile and the model. The parameters used in the fit of each C IV line profile are collected in Table 2. While some parameters ($\theta^{\text{eq}}$, $\tau_{\text{tot,p}}$, $i$, $\tau_{\text{rot}}$, $\alpha$, $f_\gamma$ ... ) were allowed to vary, we tried to keep fixed the radial velocity gradient in the wind (the $\beta$ parameter), the emission parameter $\gamma$ and the disk opening angle $\Delta \theta$. The latter was chosen equal to the value generally adopted for the opening angles of disk winds in AGN models (Murray et al. 1995; Proga & Kallman 2004). However, even those parameters were varied in a few cases to slightly modify the part of the profile in emission. In particular, we found that the opening angle $\Delta \theta$...
Fig. 2. Illustration of the effects of the wind’s main parameter on the line profile (see text for details). Each spectrum is represented as a function of the normalized wavelength \( X = (\lambda - \lambda_0) / (\lambda_{\text{max}} - \lambda_0) \) and is the result of the simulation of \( 2 \times 10^6 \) photon paths through the wind (\( S/N > 100 \) on the continuum level).

The empirical fitting procedure we adopted here makes the distinction between three types of line profiles, each possessing its own set of spectral signatures. The first kind of line profile is the P Cygni-type (Q1333+2840 and Q1413+1143). In this subsample, the absorption profile extends to velocities up to \(-10000 \text{ km s}^{-1}\), these characteristics suggest that there is an equatorial denser disk-like region seen nearly edge-on and producing the narrow absorption component observed. The necessity of considering such a more slowly expanding disk in a polar wind is illustrated particularly well when observing the C IV line profile of Q1413+117. In this object, the absorption profile extends to velocities up to \(-10000 \text{ km s}^{-1}\).

The sample contains various types of BAL spectra, from the P Cygni-type to the more complex profiles discussed in the paper of Korista et al. (1993). This subdivision of BAL QSO spectra was introduced by Turnshek (1984b) and based on the visual properties of the BAL profiles, where the P Cygni-type profiles with a smooth absorption and a high emission peak relative to the continuum level are distinguished from the complex/detached absorption ones with a lower emission peak. However we tried to model all these line profiles using the same wind geometry since, as suggested by Turnshek (1984b), it is likely that distinct types of BAL profiles are the consequence of a unique mass-loss phenomenon.

of the disk has to be decreased for fitting the high-velocity absorption component (see Sect. 3) observed in the P Cygni-type line profiles (Q1333+2840 and Q1413+1143).
speed generally needs to be quite higher than the polar terminal velocity (reaching up to 50% of \( v_{\text{max}} \)) and is approximately equal to the equatorial wind terminal velocity. For the P Cygni-type profiles (Q1333+2840, Q1413+1143 or even Q0041-4023), it is also necessary to consider a rotation of the wind around the polar axis, although it must be smaller to properly account for the higher emission peak and the sharp transition between the emission and the absorption parts of the profiles.

In each case, the best fit was chosen by eye, once the model was qualitatively similar to the profile of the observed line. The simulation time needed to produce a single line profile in these optically thick winds prevents us from using a \( \chi^2 \) type technique while searching for the best model. However, this is not a main drawback since our main goal is to show that a simple wind model is able to approximately reproduce a variety of resonance line profiles observed in BAL QSOs. Moreover, given the degeneracy between some of the model parameters (\( k_{\text{em}} \) with \( i \), \( v_{\text{eq}} \) with \( i \), \( \beta \) with \( \alpha \), etc.), as well as the difficulty in some cases of correctly evaluating \( v_{\text{po}} \) or other model parameters, more than one best fit is generally possible.

The absence of the two-component wind signatures defined above in the C\( IV \) line profile of some objects led us to define a third subsample of line profiles. These line profiles can be fitted by a two-component wind (see upper panel of Fig. 5). However, some profiles (the prototype being Q0019+0107) do not show evidence of a polar absorption component at high velocities, suggesting that the polar outflow may not be present in these objects. Several tests performed on such line profiles with MCRT showed that Q0019+0107-type line profiles can be produced in a single, rapidly rotating equatorial wind seen nearly edge-on (see lower left panel of Fig. 5). In the same vein, in the bottom right panel of Fig. 5, we illustrate how the C\( IV \) line profile of Q0041-4023 can be reproduced by a two-component wind seen nearly pole-on. This arises when a single deep absorption trough is associated with a quasi-symmetric emission profile. Once again, given the uncertainties on the wind parameters because of the lack of clear signatures in the line shape, several wind models can be fitted to the observed line profiles (here we chose as typical values for model M2 \( v_{\text{eq}} = v_{\text{rot}} = 0.5 v_{\text{max}} \)).

From Figs. 4 and 5, we note that our simple model is able to reproduce the diversity of the BAL profiles observed in a real sample of objects quite well. Interestingly enough, in order to be able to fit the C\( IV \) profiles with MCRT, we must shift the whole simulated line profile with respect to the emission peak, usually used for redshift determination. This shift is needed to center the underlying emission component of the profile on the zero velocity. Indeed, when dealing with resonant scattering, an absorption trough extending over the velocity range \([-v_{\text{max}}, 0]\) produces an emission feature extending from \(-v_{\text{max}} \) to \(v_{\text{max}}\). The redshift of the quasar determined from the center of the underlying C\( IV \) emission line is given in the second column of Table 2.

From the fitting procedure, one of the major parameters that control the line profile in this type of wind remains the viewing angle \( i \), which plays a crucial role in the shape of the absorption part of the line by controlling the relative contribution of the equatorial and polar components (when both are required). Thus when a line profile exhibits a sharp, deep absorption trough superimposed on a shallower high-velocity absorption component, the quasar is probably viewed along a line of sight, such as the dense equatorial wind seen nearly edge-on (e.g. Q1413+1177). However, it should be kept in mind that an edge-on disk does not necessarily produce a completely black absorption trough, even for the highest optical depths (cf. Table 2), since photons scattered to the observer may not be completely reabsorbed by...
Fig. 4. Illustration of the best fit for eight out of the ten C IV line profile selected from the BAL quasar sample of Korista et al. (1993). The observed spectrum is represented by a full line and the two-component model profile by a dashed line. Each spectrum is normalized to the continuum level and represented as a function of the velocity.

the disk then filling in the absorption trough. This agrees with what is usually observed among the Korista et al. (1993) spectra and has already been pointed out by Lee & Blandford (1997) or Arav et al. (2007, and references therein).
Fig. 5. Illustration of the non-uniqueness of the fit for two particular objects of our sample. The upper panels (labelled M1) of this figure show that the C IV line profile of these two objects can be fitted in the framework of the two-component wind model. In the lower panels (labeled M2), we show that the lack of typical two-component wind signatures in the line profile allows alternative fits with different parameters (see text). As in Fig. 4 the observed spectrum is represented by a full line and the two-component model profile by a dashed. Each spectrum is normalized to the continuum level and represented on a velocity scale.

Table 2. Parameter of the two-component wind model for the best fit of the C IV BALs in the selected quasar sample.

<table>
<thead>
<tr>
<th>BAL QSO Name</th>
<th>z</th>
<th>τ tot</th>
<th>k pm</th>
<th>v max (km s⁻¹)</th>
<th>v eq max (km s⁻¹)</th>
<th>V rot (km s⁻¹)</th>
<th>α</th>
<th>β</th>
<th>Δθ (°)</th>
<th>i (°)</th>
<th>f e</th>
</tr>
</thead>
<tbody>
<tr>
<td>Q1333+2840</td>
<td>1.897</td>
<td>3.00</td>
<td>10.0</td>
<td>13 000</td>
<td>4000</td>
<td>1000</td>
<td>3.0</td>
<td>0.8</td>
<td>10</td>
<td>80</td>
<td>0.21</td>
</tr>
<tr>
<td>Q1413+1143</td>
<td>2.522</td>
<td>10.0</td>
<td>15.0</td>
<td>11 000</td>
<td>3500</td>
<td>2000</td>
<td>3.0</td>
<td>0.8</td>
<td>10</td>
<td>80</td>
<td>0.16</td>
</tr>
<tr>
<td>Q0041-4023</td>
<td>2.075</td>
<td>1.00</td>
<td>15.0</td>
<td>16 000</td>
<td>9000</td>
<td>8000</td>
<td>3.0</td>
<td>1.0</td>
<td>15</td>
<td>90</td>
<td>0.10</td>
</tr>
<tr>
<td>Q0019+0107 M1</td>
<td>2.075</td>
<td>0.00</td>
<td>15.0</td>
<td>10 000</td>
<td>5000</td>
<td>3000</td>
<td>2.0</td>
<td>0.5</td>
<td>15</td>
<td>0</td>
<td>0.07</td>
</tr>
<tr>
<td>Q0019+0107 M2</td>
<td>2.075</td>
<td>5.00</td>
<td>5.00</td>
<td>6000</td>
<td>3000</td>
<td>2000</td>
<td>2.0</td>
<td>0.5</td>
<td>15</td>
<td>0</td>
<td>0.07</td>
</tr>
</tbody>
</table>

Notes. (a) k pm represents the total equatorial (i = 90°) optical depth integrated over frequencies since τ tot = 0.

Finally in all modeled profiles, we need to allow for the creation of photons inside the wind (a fraction f e  > 0 relative to the continuum intensity). This intrinsic emission produces stronger emission peaks than in the case of a purely resonant scattering wind.

5. Discussion

We showed that a simple two-component equatorial+polar wind model is able to reproduce a variety of BAL profiles, ranging from detached absorption troughs to P Cygni-type profiles. The solutions of the fits are not unique and several models with different geometries and/or physical properties can equally reproduce the observed spectra. In accordance with previous studies (e.g. Hamann et al. 1993), this demonstrates that a unique physical characterization of the outflow cannot be derived from line profile fitting.

While detailed information on the geometry of the outflows cannot be derived, we nevertheless reached some interesting conclusions. First, in some objects, it is necessary to include both the equatorial and the polar absorption regions. This is indeed the case for objects like Q1413+117, Q1333+2840, but...
also Q1235+1453 or Q0842+3431, where the polar component allows reproduction of the shallow absorption trough observed at higher velocities and where the lower velocity equatorial component is needed to reabsorb the emission from the polar wind. In other objects (the prototype in our sample being Q0019+0107), the polar component is not necessary and the profiles can be fitted with only a rapidly rotating equatorial wind seen nearly edge-on. In this particular case, there is a strong degeneracy between the model parameters, as also suggested by similar profiles having been computed in the framework of other wind models (e.g. Proga 2003; Proga & Kallman 2004).

Interestingly, in many of the fitted spectra, the viewing angle to the wind axis is found to be high, suggesting that BAL quasars are essentially observed when the optically thick equatorial wind blocks the direct view to the continuum source. This agrees with the high inclination generally inferred to account for the spectropolarimetric properties of BAL QSOs (Schmidt & Hines 1999; Ogle et al. 1999). In this case, the polar wind could play the role of the extended scattering region at the origin of the polarization. We also showed that, when the profile is constituted of a single deep absorption trough and a quasi-symmetric emission peak (e.g. Q0041-4023), the line can be produced in a two-component wind seen at low inclination (see the bottom right panel of Fig. 5). This result underlines that some BAL troughs can be observed as the result of a polar outflow in a two-component wind with a large covering factor. As mentioned in the introduction, a growing number of radio observations of BAL QSOs provide evidence for such two-component wind models, while recent hydrodynamical simulations show that a stable two-component wind can result from the flow around a polar component.

In our study we decided to use a simple radially expanding wind model with an equatorial and a polar component. This type of wind can account for most characteristics of the resonance line profiles observed in the spectra of BAL QSOs. However, we were not able to fit the C IV line shape of the P Cygni-type quasar prototype PHL5200. This indicates that the model used does not include all the ingredients needed. Indeed, the model cannot reproduce the very sharp transition observed between the absorption and the emission components in the C IV profile of PHL5200 (Turnshek et al. 1988). Such a sharp transition at zero velocity could in turn be produced in a wind launched from the disk itself. In that type of model, which exhibits large-scale properties similar to those of the model considered in the present study, the wind is launched from the disk and then radially accelerated by the radiation pressure (Murray et al. 1995; Proga & Kallman 2004). When observed nearly edge-on, it can produce strong absorption at the center of the line as observed in PHL5200. Proga (2003) shows the capabilities of these winds to produce a sharp transition between the absorption and emission in the case of cataclysmic variable stars. Implementing that type of wind is beyond the scope of this paper and has been left for future work.

Furthermore, in a majority of objects we found it necessary to use high values of the ratio of the rotational speed to the polar terminal speed of the wind \( \frac{v_{rot}}{v_{\text{rot}}^{\text{max}}} \) to adequately reproduce the asymmetry of the emission line profiles. Such a high value of the rotation accounts for the redshift and the faintness of the emission peak. These characteristics result from the continuum emitted on the red side of the line profile possibly being absorbed by the optically thick material located between the source of continuum and the distant observer when rotation is present (see Fig. 3). The rotational velocity at the base of the wind can reach several thousand \( \text{km s}^{-1} \), which is consistent with the rotational velocities inferred for gas orbiting in the vicinity of a supermassive black hole (e.g. Murray et al. 1995; Young et al. 2007). Interestingly, we found that the rotational velocity must remain low in quasars with P Cygni-like line profiles. Indeed, to keep the emission intense, the redward absorption due to the rotation must be small (cf. Fig. 3). As a consequence, the shallow blue absorption wing only comes from the polar wind. This may indicate a possible dynamical difference between the BAL QSOs with detached profiles and those ones with P Cygni type profiles.

The rotation of the wind naturally provides a simple and straightforward interpretation of the correlation between the properties of the broad emission lines (BELs) and those of the broad absorption lines as reported by Turnshek (1984a). Indeed, as shown in that paper, BAL QSOs having complex absorption generally have a weaker C IV emission peak relative to the continuum than does BAL QSOs with smooth P Cygni absorption. This can be explained by the stronger/wider absorption on the red side of the line profile resulting from the rotation of optically thick material in front of the continuum source. Combining the emission profile and the redshifted absorption of the continuum results in profiles resembling the so-called detached troughs observed in several BAL QSO spectra (Korista et al. 1993; Arav & Begelman 1994; Hall et al. 2002; Proga & Kallman 2004).

Recently, spectropolarimetry of the BAL QSO PG1700+518 have revealed significant variations in the polarization position angle over the Hz BEL, which is interpreted as the typical signature of a rotating wind (Young et al. 2007; Wang et al. 2007).

When fitting the C IV line profiles, we found it necessary to adopt a systemic redshift for the wind lower than the redshift given by the peak of the C IV emission line. This “wind redshift” corresponds to the centroid of the full emission component that underlies the observed absorption + emission profile and defines the rest frame of the outflow model. It is interesting to compare this redshift to the redshift determined from the narrow forbidden lines usually thought to provide the true systemic redshift of the quasar and its host galaxy (e.g. McIntosh et al. 1999; Vanden Berk et al. 2001). Unfortunately, only a few measurements are available because the [O III] lines are shifted in the near-infrared and are fainter in BAL QSOs than in non-BAL QSOs (Yuan & Wills 2003). For the BAL QSOs of our sample, only three accurate determinations are available, as given in Table 3. For these quasars, we find a net blueshift of the simulated C IV line profiles by several thousand \( \text{km s}^{-1} \) with respect

### Table 3. Blueshift of the C IV line relative to the systemic redshift \( \Delta v_{\text{sys}} \) for the three quasars from our sample with secured [O III] line measurement.

<table>
<thead>
<tr>
<th>BAL QSO Name</th>
<th>( \Delta v_{\text{sys}} )</th>
<th>Ref.</th>
<th>( \Delta v_{\text{sys}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Q0019+0107</td>
<td>2.131</td>
<td>Dietrich et al. (2009)</td>
<td>5500 km s(^{-1})</td>
</tr>
<tr>
<td>Q0226-1024</td>
<td>2.268</td>
<td>McIntosh et al. (1999)</td>
<td>9200 km s(^{-1})</td>
</tr>
<tr>
<td>Q1413+1143</td>
<td>2.553</td>
<td>Hutsemékers et al. (2010)</td>
<td>2500 km s(^{-1})</td>
</tr>
</tbody>
</table>
Interestingly enough, the velocity distribution outflow in the host galaxy rather than in the BAL wind. These velocities suggest that they originate in a large-scale outflow in the host galaxy rather than in the BAL wind. Interestingly enough, the velocity distribution in the wind rest frame (Fig. 4), i.e. at -8000 and -2000 km s\(^{-1}\) in the systemic quasi-star host frame. These velocities suggest that they originate in a large-scale outflow in the host galaxy rather than in the BAL wind. Interestingly enough, the velocity difference between these narrow absorption lines is close to the velocity separation between the Lyα and NV resonance doublets (-5000 km s\(^{-1}\)), suggesting a possible line locking effect (Korista et al. 1993; Arav & Begelman 1994).

6. Conclusions
In this study, we used a combination of a Monte Carlo radiative transfer code and a simple two-component polar-equatorial wind model in which photons are emitted from a central spherically symmetric source and resonantly scattered in the wind to reproduce typical CIV resonance line profiles selected from a homogeneous sample of BAL QSO spectra.

Although the lack of uniqueness of the line profile fitting does not allow us to strongly constrain the geometry of the wind, we can summarize our main findings as follows.

1. The diversity of BAL profiles produced by the adopted polar-equatorial model ranges from the typical P Cygni-type profiles to the detached absorption ones, reproducing those observed in a homogeneous sample of BAL QSOs.

2. While in some cases the line profiles can be reproduced by a single equatorial wind, we find it necessary to use a two-component polar-equatorial wind in a majority of objects.

3. The viewing angle to the wind is generally large (disk seen near edge-on); however in some cases, the line profiles can also be reproduced when assuming a pole-on view, in accordance with the results of recent radio surveys of BAL QSOs. In this context, it would be interesting to obtain good quality spectra of bona-fide polar BAL quasars and try to fit their line profiles by assuming the pole-on view.

4. The equatorial wind is rotating, and the rotational velocity at the base of the wind can reach a significant fraction of the polar terminal speed.

A possible way to break the degeneracy between the various parameter combinations of the two-component model that can reproduce the observed BAL profiles is to use gravitational microlensing. Indeed, a microlensing model moving across the quasar inner regions can differentially magnify the different line-forming regions, inducing line profile variations from which the geometry of the outflow can in principle be retrieved (e.g. Hutsemékers 1993; Hutsemékers et al. 1994; Lewis & Belle 1998; Chelouche 2003, 2005). Our code MCRT has been explicitly built to integrate these microlensing effects. The effect of microlensing on BAL profiles, their use for deriving the physical properties of the outflow, and application to a known lensed system will be presented in a separate paper.

References
Arav, N. 1997, ASP Conf. Ser., 128, 208
Girn, V. P. 1984, Afz, 20, 190
Lucy, L. B. 1971, AJ, 163, 95
Press, W. H., Teukolsky, S. A., Vetterling, W. T., & Flannery, B. P. 1992, 
(New York: Cambridge Univ. Press)
Richards, G. T. 2008, AGN in the Caribbean, Workshop, St. John. UVSI
509, 132
Turnshek, D. A. 1988, QSO Absorption Lines: Probing the Universe (Cambridge 
University Press)
651
Monte Carlo Radiation Transfer
Young, S., Axon, D. J., Robinson, A., Hough, J. H., & Smith, J. E. 2007, Nature, 
450, 74
Yusef-Zadeh, C. N., & Burns, P. J. 1999, Random Number Generator 
Recommendation, Colorado State Univ.