LETTER TO THE EDITOR

The column density towards LMC X-1

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ABSTRACT

We measure the neutral absorption towards the black hole X-ray binary system LMC X-1 from six archival soft X-ray spectra obtained with the gratings and/or CCD detectors on *Chandra*, *XMM-Newton*, and *Swift*. Four spectral models for the soft continuum are investigated. While the powerlaw model may overestimate N_{H} considerably, the others give consistent results. Taking the lower metallicity of the Large Magellanic Cloud into account, we find equivalent hydrogen column densities of $N_{\text{H}} = (1.0\text{--}1.3) \times 10^{22} \text{ cm}^{-2}$, with a systematic dependence on the orbital phase. This variation in the neutral absorption can nearly explain the orbital modulation of the soft X-ray flux recently detected with the All Sky Monitor (ASM) on the *Ross X-ray Timing Explorer (RXTE)*.

Key words. X-rays: individuals: LMC X-1 – X-rays: binaries – X-rays: ISM – galaxies: abundances

1. Introduction

The extragalactic X-ray sources in the Large Magellanic Cloud (LMC), our ≈ 48 kpc distant neighboring galaxy, were discovered in the late 1960s (Mark et al. 1969; Price et al. 1971). Because the density of stars is high, their optical identifications were uncertain for a long time. The X-ray binary system (XRB) LMC X-1 is located ≈ 0.5 south-southeast of the 30 Doradus star-formation region, in the NGC 2078 (LMC N159F) nebula. Pakull (1980), Hutchings et al. (1983, 1987), and Cowley et al. (1995) were able to identify the counterpart of LMC X-1 with an $m_V = 14^m 5$ O7/8 giant (Hutchings et al. 1983; Negueruela & Coe 2002). This has allowed the placement of strong dynamical constraints on the compact object's mass. Orosz et al. (2009) have recently used optical spectra of this star – labeled as “star #32” by Cowley et al. (1978) and also often called Pakull's star – to confirm the black hole (BH) candidacy of LMC X-1. They derive an orbital period of 3.909 d, which is consistent with the modulation of the soft X-ray flux of LMC X-1 (Levine & Corbet 2006). Deriving an extinction of $A_V = 2.28 \pm 0.06$ – much more than previously assumed – from the $V - K$ color excess, Orosz et al. (2009) infer a BH mass of $10.9 \pm 1.6 M_{\odot}$.

The persistent XRB LMC X-1 is the only dynamically confirmed BH candidate that so far has only been found in the high/soft (thermal dominant) X-ray spectral state; that is, its X-ray spectrum can be described by a multi-temperature disk blackbody component plus a weak soft ($\Gamma \gg 2$) power-law component (Ebisawa et al. 1989; Schlegel et al. 1994; Wilms et al. 2001; Nowak et al. 2001; Haardt et al. 2001; Cui et al. 2002; Yao et al. 2005). In comparison, LMC X-3 usually shows a similarly soft X-ray spectrum, but also (partial) transitions to the low/hard state (Wilms et al. 2001; Smith et al. 2007), while Cyg X-1 regularly transits between the low/hard and a soft-intermediate state and never reaches the thermal dominant state (Wilms et al. 2006). LMC X-1 is therefore an ideal target for measuring the BH spin parameter a_* from the soft X-ray continuum produced by the relativistic accretion disk. Gierliński et al. (2001)

constrained a_* to be less than 0.998 from a 24 ks 0.7–10 keV ASCA-SIS spectrum. Gou et al. (2009) have recently reported $a_* = 0.90^{+0.04}_{-0.09}$ from 18 selected RXTE-PCA spectra with exposures between 5–11 ks and covering 2.5–20 keV. These authors fix the column density for the photoelectric absorption to $N_{\text{H}} = 4.6 \times 10^{21} \text{ cm}^{-2}$ as reported by Cui et al. (2002) based on low statistics.

An appropriate description of the absorption is, however, indispensable for modeling the soft X-ray continuum and likewise for modeling the visual extinction, hence the derivation of the system parameters from the dereddened optical spectrum of the companion star. In this Letter, we therefore aim to accurately describe the column density towards LMC X-1. We describe the data in Sect. 2 and present the methods and our analysis in Sect. 3. We summarize and discuss our results in Sect. 4.

2. Observations and data reduction

We study the spectra from all six recent observations with instruments providing soft X-ray spectra (Table 1).

The *Chandra* observation C1 was performed using the HETGS (Canizares et al. 2005) and with the detector CCDs operated in timed exposure mode. The $\pm$ first order HEG and MEG spectra, as well as the corresponding response matrices, were taken from the *Chandra* Transmission Grating Catalog archive TGCat¹.

All instruments of *XMM-Newton* (Jansen et al. 2001) were active during the first (shorter) *XMM* observation X1. The EPIC-pn camera (Strüder et al. 2001) was operated in timing mode. Its data are therefore not affected by photon pile-up (Wilms et al. 2003). The same is true for data from the Reflection Grating Spectrometers (RGS; den Herder et al. 2001) due to their dispersion of the photons, but not for data from the MOS cameras (Turner et al. 2001), which were operated in full frame imaging mode. For this reason, we only use the EPIC-pn spectrum and

¹ See <http://tgcatal.mit.edu>

Table 1. Log of recent soft X-ray observations of LMC X-1 with good S/N. (Instruments not considered here are in parenthesis.)

Obs.	Start date	Start date (MJD)	Exposure (ks)	$\phi_{\text{orb}}^{(\text{T3})\dagger}$	$\phi_{\text{orb}}^{(\text{F9})\ddagger}$	Satellite	ObsID	Instruments
C1	2000-01-16	51559.2	19	0.45–0.51	0.50–0.56	<i>Chandra</i>	93	HETGS
X1	2000-10-21	51838.7	5–7	0.94–0.96	0.98–0.01	<i>XMM</i>	0112900101	PN, RGS 1+2, (MOS 1+2)
X2	2002-09-26	52543.2	35	0.17–0.28	0.21–0.32	<i>XMM</i>	0023940401	RGS 1+2, (MOS 1+2)
S1	2007-10-31	54404.7	2.4	0.37–0.42	0.37–0.43	<i>Swift</i>	00037079001	(BAT), XRT/PC, (UVOT)
S2	2007-12-06	54440.4	9.8	0.49–0.61	0.50–0.62	<i>Swift</i>	00037079002	(BAT), XRT/WT, (UVOT)
S3	2007-12-10	54444.1	4.4	0.43–0.50	0.43–0.50	<i>Swift</i>	00037079003	(BAT), XRT/WT, (UVOT)

Notes. ^(†) Orbital phase calculated from the ephemeris of Orosz et al. (2009, Table 3): $T_0 = \text{MJD } 53\,390.8436$, $P = 3.90917$ d; ^(‡) orbital phase calculated from the ephemeris of Orosz et al. (2009, Fig. 9): $T_0 = \text{MJD } 53\,390.75174$, $P = 3.9094$ d.

Fig. 1. Flux-corrected spectra of LMC X-1 from the six observations, shifted in flux according to the labels with respect to C1 for visual clarity. The gray data have been ignored because of calibration issues. The models shown here for illustrative purposes are also broadened by the instrumental response.

the first and second order spectra of RGS 1 and 2. For the second (longer) *XMM* observation X2, however, no pn-data are available. The data were reduced with the Science Analysis Software, XMMSAS, v. 7.1, following standard procedures, i.e., applying the SAS tasks `epchain`, `emchain`, `rgsproc`, `evselect`, `rmfgen`, and `arfgen` to produce spectra and response matrices.

Swift's X-ray telescope (XRT; Burrows et al. 2005) was operated in photon counting (PC) mode during the first *Swift* observation S1, which resulted in pile-up. For S2 and S3, the windowed timing (WT) mode was used. After reprocessing the data to apply the newest calibration, spectra were extracted using standard FTOOLS, handled via `xselect`. For the PC mode observation S1, we extract an annulus to exclude the region affected by pile-up, only yielding a low-quality spectrum. Ancillary response files were created with `xrtmkarf`, and suitable response files for each observation were obtained from the CALDB. The WT mode spectra are not calibrated as well as the PC mode one around the Si edge (Fig. 1), so we exclude their 1.5–2 keV data.

All spectral analysis was performed with the Interactive Spectral Interpretation System (ISIS; Houck & Denicola 2000; Noble et al. 2006; Noble & Nowak 2008)².

² See <http://space.mit.edu/cxc/isis/>

Table 2. Comparison of elemental abundances (by number) in the Galactic ISM and in the LMC as $\epsilon(X) = 12 + \log_{10}(X/H)$.

X	$\epsilon_{\text{gal}}(X)^{(1)}$	$\epsilon_{\text{LMC}}(X)$	$10^{\Delta\epsilon(X)}$
He	10.99	10.93 ⁽⁵⁾	0.87
C	8.38	8.03 ⁽²⁾	0.45
N	7.88	7.01 ⁽²⁾	0.13
O	8.69	8.38 ⁽²⁾	0.49
Ne	7.94	7.6 ⁽⁴⁾	0.46
Mg	7.40	7.12 ⁽²⁾	0.53
Si	7.27	7.21 ⁽²⁾	0.87
S	7.09	6.7 ⁽⁴⁾	0.41
Ar	6.41	6.2 ⁽⁴⁾	0.62
Fe	7.43	7.2 ⁽³⁾	0.59

References. (1) Wilms et al. (2000) or using `xspec_abund("wilm")`; in ISIS; (2) Przybilla (priv. comm.): average of 7 B-stars in the LMC (see also Korn et al. 2002, 2005); (3) Przybilla (priv. comm.): 1 star in the LMC (see also Przybilla et al. 2008); (4) Garnett (1999): H II regions in the LMC; (5) Dufour (1984).

Notes. The last column is the LMC abundance relative to the Galactic abundance, which is a parameter of the `tbvarabs` absorption model (Wilms et al. 2000, 2009, in prep.). For all other elements (which hardly contribute to the absorption in the soft X-ray band), the average value $10^{\Delta\epsilon(X)} = 0.5$ is assumed.

3. Analysis

An overview of previous N_H measurements for LMC X-1 is given by Orosz et al. (2009, Table 2). We caution, however, that only <12% of the hydrogen column density towards the LMC, $N_H = 4 \times 10^{21} \text{ cm}^{-2}$ (measured in the LAB 21 cm survey; Kalberla et al. 2005; Bajaja et al. 2005), is of Galactic origin³, while the largest part is detected at $v_{\text{LSR}} = 200\text{--}300 \text{ km s}^{-1}$ and thus is probably local to the LMC (Richter et al. 1987). As the absorption in the 0.5–10 keV band is mostly caused by metals (Wilms et al. 2000) and the LMC has a much lower metallicity than our Galaxy, we compile both abundance sets in Table 2. The LMC abundances are henceforth used throughout our analysis.

As for all previous observations (see Sect. 1), the X-ray spectra of LMC X-1 investigated here are very soft (see Fig. 1), but a hard (albeit very steep) component in addition to a thermal one is nonetheless needed to describe the data, except for S2 and S3. The powerlaw model, however, becomes unphysically strong at low energies (e.g., Shrader & Titarchuk 1998; Done et al. 2002). A steep photon index $\Gamma \gg 2$ (e.g., $\Gamma = 3.7 \pm 0.1$ as measured for X1, which has the best high-energy coverage

³ See http://www.astro.uni-bonn.de/~webaiub/english/tools_labsearch.php?alpha=05+39+38.7&beta=-69+44+36

Table 3. Column density in units of 10^{22} cm^{-2} for the six observations and the sine fit, obtained with different continuum models.

Observation or fit $\phi_{\text{orb}}^{(\text{T3})}$	X2 0.17–0.28	S1 0.37–0.42	S3 0.43–0.50	C1 0.45–0.51	S2 0.49–0.61	X1 0.94–0.96	Sine fit full orbit
diskbb + powerlaw*	$(2.00^{+0.17}_{-0.19})^*$	$(1.2^{+0.5}_{-0.2})^*$	$0.96^{+0.03}_{-0.02}$	$(1.25^{+0.04}_{-0.01})^*$	1.031 ± 0.017	$(1.81^{+0.06}_{-0.05})^*$	$(1.43 \pm 0.43)^*$
eqpair	1.279 ± 0.005	$1.17^{+0.15}_{-0.10}$	1.02 ± 0.02	$1.065^{+0.000}_{-0.019}$	1.088 ± 0.017	$1.191^{+0.006}_{-0.007}$	1.15 ± 0.15
simpl(kerrbb)	1.278 ± 0.005	$1.17^{+0.11}_{-0.10}$	$1.01^{+0.03}_{-0.02}$	$1.085^{+0.018}_{-0.016}$	1.088 ± 0.017	$1.187^{+0.014}_{-0.012}$	1.15 ± 0.14
simpl(diskbb)	$1.288 \pm 0.016^\dagger$	$1.14^{+0.15}_{-0.11}$	0.97 ± 0.02	$1.009^{+0.018}_{-0.017}$	1.038 ± 0.017	$1.133^{+0.005}_{-0.004}$	1.10 ± 0.18

Notes. Quoted errors are statistical uncertainties at the 90% confidence level for the observations, but semi-amplitudes for the sine fits.

(*) The diskbb + powerlaw model overestimates N_{H} more, the more the powerlaw contributes at low energies, see text.

(†) As the lack of data above 2 keV did not allow us to constrain the power law with the simpl model, we only used diskbb.

Fig. 2. Correlation of the column density N_{H} and the photon index Γ , derived with the powerlaw model (left) and the simpl model (right) for observation X1. The contours show the 68%, 90%, and 99% confidence regions for two parameters of interest (i.e., $\Delta\chi^2 = 2.30, 4.61, \text{ and } 9.21$).

due to the EPIC-pn spectrum) is compensated for in spectral fits by an incorrectly strong absorption (e.g., Yao et al. 2005; Suchy et al. 2008; Gou et al. 2009). In contrast, the empirical convolution model simpl (Steiner et al. 2009) has an intrinsic low-energy cut-off when convolving an input spectrum modeled by, e.g., diskbb or kerrbb⁴. Figure 2 shows that the (well known) correlation between N_{H} and Γ vanishes when simpl is used instead of powerlaw. Although an even steeper photon index was found using simpl, the value of N_{H} is lower and is more narrowly constrained.

Because the derived absorption might depend on the shape of the continuum, we investigated different models, namely empirical ones – such as diskbb + powerlaw, simpl(diskbb), and simpl(kerrbb) (Li et al. 2005) – and the physical Comptonization model eqpair (Coppi 2000)⁵. These models typically describe our data equally well. In all fits, the disk has a temperature between 0.65 and 1.1 keV. The other parameters, too, are similar to previously obtained values. Table 3 and Fig. 3 show our results for the column density (assuming the LMC abundances given in Table 2) as a function of orbital phase ϕ_{orb} for each of the six observations and all four of the aforementioned continuum models. In all cases where a steep power law substantially contributes to the model, the diskbb + powerlaw model gives a much higher N_{H} than the other models, because of the systematic error of the powerlaw model. We therefore ignore these values. The other models, however, are quite consistent with one another: their agreement on N_{H} is within $< 8 \times 10^{20} \text{ cm}^{-2}$, which is therefore an upper limit of the systematic error due to the choice of the continuum. Using the LMC abundances (Table 2), we find column densities in the range of $(1.0\text{--}1.3) \times 10^{22} \text{ cm}^{-2}$.

We detect a modulation of N_{H} with orbital phase. The observations X1 and X2 close to $\phi_{\text{orb}} \approx 0$, when the BH is behind the donor star, require a systematically higher N_{H} than S3, C1,

Fig. 3. N_{H} as a function of orbital phase $\phi_{\text{orb}}^{(\text{T3})}$ (see Table 1) using various continuum models. Note the different scale for the diskbb + powerlaw model, which may predict an unreliably large N_{H} (see text). The gray lines fit the results with sine curves.

and S2 close to $\phi_{\text{orb}} \approx 0.5$. To quantify this modulation by its mean and amplitude (Table 3), we fit sine curves to the six measurements for each continuum model (see Fig. 3), although we are aware that they do not describe the data very well and also predict the strongest absorption at $\phi_{\text{orb}} = 0.15\text{--}0.17$, which is not expected.

Finally, we find marginal evidence of ionized absorption in the high-resolution spectra (Fig. 4), but a detailed study of these features is beyond the scope of this paper.

4. Summary and discussion

The elements with the largest contribution to the photoabsorption in the soft X-ray band are significantly less abundant in the

⁴ As a convolution model that relies upon a spectral model outside of the energy range spanned by the noticed data, simpl must be evaluated on a suitably extended grid.

⁵ For X1, the N_{H} derived with diskbb + compTT (Titarchuk 1994) is also consistent with the one from, e.g., simpl(diskbb).

Fig. 4. The Ne-edge in observation X2. The first order RGS spectra (black) reveal absorption lines of Ne IX at 13.45 Å and probably also Ne II at 13.62 Å, but the quality of the spectrum does not allow for a detailed study of the ionized absorber.

LMC than in the Galaxy (Table 2). Because of the lower metallicity, simply using radio-measured N_{H} values in an absorption model without adopting the LMC abundances will not allow for a correct description of the physical situation. Specifically for LMC X-1, the *equivalent* hydrogen column density inferred from this X-ray absorption study – taking the proper LMC abundances into account – is actually much higher than the H-column resolved by the LAB survey (at a half-power beam-width of 0.6; Kalberla et al. 2005), which is likely caused by additional material in the environment of LMC X-1 and in the system itself. This result was not obtained in earlier X-ray absorption measurements, as erroneously applying Galactic abundances resulted in lower N_{H} values.

In addition, we presented the first evidence that the column density varies in the range $(1.0\text{--}1.3) \times 10^{22} \text{ cm}^{-2}$. A modulation with orbital phase is strongly suggested and would be consistent with absorption in the stellar wind of the donor giant. Orosz et al. (2009) assume that the orbital modulation of the X-ray flux is mostly caused by Thomson scattering in the stellar wind since they find similar amplitudes⁶ in all three *RXTE*-ASM energy bands, namely $A_{\text{A}(1.5\text{--}3 \text{ keV})} = 7.2 \pm 1.0\%$, $A_{\text{B}(3\text{--}5 \text{ keV})} = 7.7 \pm 1.1\%$, and $A_{\text{C}(5\text{--}12 \text{ keV})} = 3.8 \pm 2.9\%$. From a modulation in N_{H} with a full amplitude of $3 \times 10^{21} \text{ cm}^{-2}$, $A_{\text{A}} = 7.7\text{--}6.9\%$, $A_{\text{B}} = 1.6\text{--}2.7\%$, and $A_{\text{C}} = 0.4\text{--}1.7\%$ are expected, depending on the assumptions about the ASM response; i.e., the variation seen with the ASM is almost consistent with the suggested neutral absorption. The phase of the current sine fit, however, is not. More soft X-ray observations covering more phases are clearly needed, because the structure of the stellar wind might be more complex than a sine curve. With the three 50 ks *Chandra* observations that we have gained for AO 11, we will be able to better constrain the modulation.

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⁶ The fractional full amplitude is here $A = (\text{max} - \text{min}) / \text{mean}$.