Finding pulsars with LOFAR

J. van Leeuwen and B. W. Stappers

1 Stichting ASTRON, PO Box 2, 7990 AA Dwingeloo, The Netherlands
e-mail: j.leeuwen@astron.nl
2 Jodrell Bank Centre for Astrophysics, School of Physics and Astronomy, University of Manchester, Manchester M13 9PL, UK

Received 14 August 2009 / Accepted 23 October 2009

ABSTRACT

We investigate the number and type of pulsars that will be discovered with the low-frequency radio telescope LOFAR. We consider different search strategies for the Galaxy, for globular clusters and for other galaxies. We show that a 25-day all-sky Galactic survey can find approximately 900 new pulsars, probing the local pulsar population to a deep luminosity limit. For targets of smaller angular size such as globular clusters and galaxies many LOFAR stations can be combined coherently, to make use of the full sensitivity. Searches of nearby northern-sky globular clusters can find new low luminosity millisecond pulsars. Giant pulses from Crab-like extragalactic pulsars can be detected out to over a Mpc.

Key words. pulsars: general – telescopes – instrumentation: interferometers

1. Introduction

Since the discovery of the first four pulsars with the Cambridge radio telescope (Hewish et al. 1968), an ongoing evolution of telescope systems has doubled the number of known radio pulsars roughly every 4 years: an evolution from a large flat receiver with a fixed beam on the sky (the original Cambridge radio telescope) to focusing dishes (Arecibo – Hulse & Taylor 1975), often steerable (Green Bank Telescope), on both hemispheres (the Parkes telescope – Manchester et al. 2001), with large bandwidths and multiple simultaneously usable receivers for wider fields of view (Parkes, Arecibo). The types of pulsars discovered have changed accordingly, from slow, bright, single and nearby pulsars (the original four) to fast (young and millisecond pulsars), far-away (globular clusters) or dim pulsars, some of which are in binaries.

The next step in radio telescope evolution will be the use of large numbers of low-cost receivers that are combined interferometrically. These telescopes, the Allen Telescope Array (Bower 2007), LOFAR (Röttgering 2003), MeerKAT (Jonas 2007), ASKAP (Johnston et al. 2008) and the SKA (Kramer et al. 2004), create new possibilities for pulsar research.

In this paper, we investigate the prospects of finding radio pulsars with LOFAR, the LOw Frequency ARray. We outline and compare strategies for targeting normal and millisecond pulsars (MSPs), both in the disk and globular clusters of our Galaxy, and in other galaxies.

2. LOFAR – the low frequency array

With the stations operational and the first pulsars detected LOFAR is on track to start operation in 2010. We have evaluated and simulated the LOFAR reference configuration for pulsar searches, and will describe that configuration in some detail below.

Using two different types of dipoles, LOFAR can observe in a low and a high band that range from 30–80 MHz and 110–240 MHz respectively. The sensitivity using the high-band antenna (HBA) is several times that of the low-band antenna (LBA) although their survey speeds are similar due to the larger LBA field of view. The low band is expected to be an exciting new window for exploring radio pulsar behavior (cf. Stappers et al. 2007, for an overview of the possibilities for emission physics and interstellar medium studies), but the impact on a pulsar survey of some of the smearing effects further discussed is so strong in the LBA band, that we will only discuss the HBA half of LOFAR in this paper.

The basic collecting elements are the individual dual-polarization dipoles; each 4 × 4 set of these dipoles is combined in an analog beamformer and forms an antenna “tile”. Til e sizes are grouped together in stations; stations farther from the array center are larger than inner stations. In the core, HBA stations are grouped in pairs. The innermost 12 stations are 24 tiles each and are packed tightly in a “superstation”. Spread over the 2-km core there are 24 more HBA stations of 24 tiles each (making for 36 core stations in total). These core stations are 32 m in diameter, but are tapered to an about 30 m effective diameter to reduce sidelobes. Next there are 18 Dutch “remote” stations that are outside the core and consist of 48 tiles each, while the ~8 international stations that are spread over Europe use 96 HBA tiles.

At each station the tiles are combined to form up to 8 independently steerable “station beams”. With the cumulative data rate out of the station being the limiting factor, the product of the number of beams times their bandwidth cannot exceed 32 MHz (potentially 48 MHz), e.g.: a station beam set up can range from having a single full-bandwidth station beam to 8 independent beams of 4 MHz each. Station beams are subdivided in 195 kHz channels, and sent to the central processor (CEP) supercomputer for correlation, addition and/or different types of beam forming. As illustrated in Fig. 1 CEP can further combine station beams to form ~128 16-bit full-polarisation tied-array beams for the superstation, the core and/or the entire array. That number of formed beams is limited by the maximum CEP output rate, currently 50 Gigabits/s.
toward zenith is 28 m$^2$ per antenna tile, halving at a zenith angle.

Wilhelmsson (2007, private comm.) and we will also describe it
for 4 different observing frequencies. From Wilhelmsson (2007, private comm.).

The high-band antennas operate in a 110–240 MHz frequency range and are spaced to optimize sensitivity for the low end. They are maximally sensitive toward the zenith. The fall-off of effective area $A_{\text{eff}}$ with zenith angle and observing frequency has been well characterized as shown in Fig. 2 (after Wilhelmsson 2007, private comm.) and we will also describe it qualitatively here: at its maximum at 120 MHz, the effective area toward zenith is 28 m$^2$ per antenna tile, halving at a zenith angle of ~50°. Toward higher frequencies both quantities decrease until at 240 MHz the maximum effective area is 8 m$^2$ per antenna tile, dropping to half that at ~30° away from zenith. For the $N_{\text{station}} = 36$ stations of the compact core at 120 MHz, with their $N_{\text{tiles}} = 24$ tiles each, this effective area translates into a theoretical maximum core gain $G_{\text{max,core}}$ of

$$G_{\text{max,core}} = \frac{28 \, m^2}{N_{\text{station}} \times N_{\text{tile}}} \times 2 \times 10^{-26} \, \text{W s} \times \frac{\text{Jy}}{m^2} = 8.8 \, \text{K/Jy} \quad (1)$$

where $k$ is Boltzmann’s constant in W s m$^2$. Finally, the noise temperature $T_{\text{antenna}}$ of the HBA is expected to be 140 K at 120 MHz and around 180 K in the upper half of the band (Gunst 2007, private comm.).

3. Pulsar searches

3.1. All-sky surveys

Although a pulsar survey generally addresses several science questions in parallel, it can be optimized for a specific goal: by using short integration times potential acceleration smearing is kept to a minimum to optimize for finding millisecond pulsars; when aiming to maximise the total number of new pulsars found, a survey should generally focus on the Galactic plane; while for a representative understanding of the local population an all-sky survey that is equally sensitive in all directions is optimal. Here we will focus on such an all-sky survey.

Below we first investigate different beam forming scenarios. These we compare assuming use of a single station beam, at full bandwidth, at the lowest observing frequency of 120 MHz. We investigate frequency and bandwidth dependencies in more detail in Sect. 3.1.2.

3.1.1. Beam forming

To first order an all-sky pulsar survey is optimized to reach best sensitivity per given overall time. For that one should minimise system noise while maximising collecting area, bandwidth, and integration time per pointing.

For a given survey time and sky area, maximising the time per pointing is equivalent to maximising the instantaneous field of view. This can be done by forming multiple simultaneous beams; while for sparse telescopes like LOFAR, where receivers are spread out over a large area, one can also add stations incoherently instead of coherently. This increases the field of view at the cost of increasing uncorrelated noise over correlated signal (cf. Backer 1999). In the incoherent case the beam on the sky will be larger, but in the coherent case the system is more sensitive.

From the above we can construct the following survey figure of merit $FoM$ for a given observing frequency (see Cordes 2002; Smits et al. 2009, for related definitions):

$$FoM = 10^{-3} \left( \frac{A}{T_{\text{sys}}} \right) \left( \frac{N_{\text{beams}} \times \Omega \times B}{1/N_{\text{stations}}} \right)^{1/2} \quad (2)$$

where the factor $10^{-3}$ scales the reference $FoM$ to be 1.0; $A/T_{\text{sys}}$ is the ratio of effective area and system noise equivalent temperature, averaged over the field of view, a ratio indicating telescope gain. $N_{\text{beams}}$ is the number of simultaneous beams formed and $\Omega$ denotes the field of view as derived from the beam size. Here and below we estimate all beam sizes by their full width at half maximum ($FWHM$) as $1.22 \frac{\text{deg}}{\lambda}$ with $\lambda$ the observing wavelength, and $D$ the diameter of the element over which the beam is formed (e.g.: a station, the core, or the full array). Then

$$\Omega = \pi \left( \frac{D}{2 \lambda} \right)^2 \, \text{deg}^2.$$ $B$ is the observing bandwidth; the right-hand denominator is 1 for coherent addition, or $N_{\text{stations}}$ when that number of stations is added incoherently. This $FoM$ is inversely proportional to the minimum detectable flux $S_{\text{min}}$. When comparing between setups, the ratio of survey speeds – the time needed to reach a given sensitivity over the whole sky – is $FoM^2$.

In Table 1 we list the $FoM$ for three survey set ups discussed below.
Table 1. Figure of merit FoM per Eq. (2) for the three different survey set ups as described in the text: Full Incoherent, Core Coherent and Superstation Coherent.

<table>
<thead>
<tr>
<th>Type</th>
<th>$A/T_{sys}$ (m$^2$/K)</th>
<th>$N_{beams}$</th>
<th>$\Omega$ (deg$^2$)</th>
<th>$B$ (MHz)</th>
<th>$N_{stations}$</th>
<th>FoM</th>
</tr>
</thead>
<tbody>
<tr>
<td>Full Incoherent</td>
<td>260</td>
<td>1</td>
<td>27</td>
<td>32</td>
<td>54</td>
<td>1.0</td>
</tr>
<tr>
<td>Core Coherent</td>
<td>170</td>
<td>128</td>
<td>0.006</td>
<td>32</td>
<td>1</td>
<td>0.8</td>
</tr>
<tr>
<td>Superstation Coherent</td>
<td>40</td>
<td>128</td>
<td>0.23</td>
<td>32</td>
<td>1</td>
<td>1.2</td>
</tr>
</tbody>
</table>

All parameters derived using the lowest observing frequency, 120 MHz. In the first column, $A/T_{sys}$, we use 54, 36 and 12 stations respectively, of 24 tiles at 28 m$^2$, and 140 K, while for the Superstation Coherent case we also multiply by 0.70 to correct for the lower sensitivity at the station beam edge.

To outline the various trade-offs involved with these survey setups, we first compare scenarios for coherent versus incoherent addition for the LOFAR core only, and not the total array – given the sparseness of the distribution of remote stations, coherent addition of the entire array would result in an extremely limited field of view.

In the Core Coherent scenario all 36 stations in the 2 km diameter $D_{core}$ compact core are combined coherently. In this case $\Omega = 0.0060$ deg$^2$ and the gain is as per Eq. (1). For comparison, each of the individual roughly $D_{station} = 30$-m core stations forms a beam on the sky of 27 deg$^2$. If added incoherently, the resulting beam is as large as for an individual core station (cf. Fig. 1) but at a factor $\sqrt{N_{stations}} = 6$ decreased sensitivity compared to the coherent case. The factor $(D_{station}/D_{core})^2 = (3000/2000)$$^2 = 4.4 \times 10^3$ increase in beam area allows for longer integrations by the same factor. For synthesis telescopes that form a single coherent “tied-array” beam, like the Westerbork Synthesis Radio Telescope or the Very Large Array, such a factor would well describe the trade-off between beam size decreases as frequency increases with frequency as $\nu^{-1}$.5 on average (Malofeev et al. 2000). Other circumstances are more favorable at higher frequencies: the background sky noise decreases steeply as $\nu^{-2}$ which limits integration time per pointing in a fixed-time all-sky survey; the effective collecting area falls off with frequency; and the intrinsic pulsar brightness decreases with frequency as $\nu^{-1.5}$ on average (Lawson et al. 2000). Other circumstances are more favorable at higher frequencies: the background sky noise decreases steeply as $\nu^{-2}$ and the pulse smearing from dispersion and scattering, which makes the pulsar periodicity harder to detect, is less. Much of the effect of dispersion can be removed by searching over many ($\sim 10^3$) incoherently dedispersed trials
The minimum detectable flux \( S_{\text{min}} \) depends on the signal-to-noise ratio at which one accepts a signal as real (SNR), the system temperature \( T_{\text{sys}} = T_{\text{rec}} + T_{\text{sky}} \) as it varies over the sky, the number of polarisations \( N_{\text{pol}} \), the bandwidth \( B \), the integration time \( t \), the pulsar period \( P \) and pulse width \( W \) and the zenith-angle dependent gain \( G(z) \). Compared to the theoretical gain the real-life gain is always less; although in Eq. (1) we already use the simulated effective area and take aperture efficiency into account there, we apply a conservative factor 0.66 to estimate the real-life gain for our simulations below. Regarding the impact of RFI on the amount of usable bandwidth, testing has shown the radio-interference environment to be relatively clear, and RFI is significantly reduced by the 12-bit digitisation and the many-element interferometer design, especially when elements are combined coherently. As the total bandwidth can furthermore be quickly split up and spaced to avoid channels contaminated by RFI, we expect that the entire specified 32 MHz band (potentially 48 MHz) will be usable, but below we shall conservatively use 80% of 32 MHz. The potential 1.5-fold increase in usable bandwidth from 32 to 48 MHz would increase sensitivity by \( \sqrt{48/32} \). As \( S_{\text{min}} \) depends on zenith distance and sky noise, it varies per pointing, but after Dewey et al. (1985) we can estimate a typical value for a 1-min pointing towards the zenith using a coherently formed core beam, for a pulsar with a 10% duty cycle:

\[
S_{\text{min}} = SNR \left( \frac{T_{\text{sys}}}{0.66 G_{\text{max}} (N_{\text{pol}} 0.8 B t)^{0.5}} \right)^{2/3} \left( \frac{W - W}{P} \right)^{0.5} = 10 \left( \frac{0.66 \times 8.8 \times 10^{3} K}{2 \times 0.8 \times 32 \text{ MHz} \times 60 \text{ s}^{2}} \right)^{0.5} (1/2) \]

\[
= 10.3 \text{ mJy.} \tag{3}
\]

For comparison the \( S_{\text{min}} \) for incoherently added pointings for our reference survey described below (1-h integrations, 54 stations added) comes to 5.8 mJy.

### 3.1.4. Simulations

To determine the number and type of pulsars LOFAR can find, we have used the above characteristics to model the detection of a large number of simulated normal pulsars. For this, we have used a population synthesis code that simulates the birth, evolution, death and possible detection of radio pulsars (for details see Bhattacharya et al. 1992; Hartman et al. 1997; van Leeuwen & Verbunt 2004). We do not simulate millisecond pulsars, as a realistic treatment of the survey selection effects associated with their binary history would be essential but is beyond the scope of this work. For our simulated pulsars we draw birth velocities from the Lyne & Lorimer (1994) distribution with its 450 ± 90 km s\(^{-1}\) mean velocity. Initial positions are simulated as in Hartman et al. (1997): heights above the Galactic plane are randomly selected from an exponential distribution with a scale height of 60 pc; for the initial distribution in galactocentric radius we use their Eq. (4), modified to scale per unit area:

\[
p(R) \, dR = \frac{R}{R_{\infty}} \exp \left( -\frac{R}{R_{\infty}} \right) \, dR \tag{4}
\]

where scale length \( R_{\infty} \) is 5 kpc. This modified distribution does not peak as strongly toward the Galactic centre as the original does; for the local population there is no significant change but surveys that sample the inner Galaxy are better reproduced. We next calculate the 3D orbits through the Galaxy. We evolve magnetic fields and periods, determine whether the pulsar is still above the death-line. We estimate the luminosity at 400 MHz (per Hartman et al. 1997; who follow Narayan & Ostriker 1990). With a spectral index drawn from a Gaussian distribution of width 0.76 around −1.5 (Malofeev et al. 2000, takes luminosity

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**Fig. 3.** Number of pulsars detected in simulated surveys at different frequencies and sensitivity estimates, plotted as a ratio over the productivity of our reference 25-day all-sky survey of 1-hr pointings at 140 MHz. Towards lower frequencies the yield goes up, mostly caused by the increasing effective area as the wavelength approaches the telescope’s optimum at twice the antenna spacing of 1.25 m; equally important is the increasing beam size which allows for longer integrations for the same total survey time.

DMs (Lorimer & Kramer 2005). No such removal process exists for scatter broadening, where the pulsar emission takes different paths through the interstellar medium with different travel times, resulting in an observed pulse profile that is significantly smeared out. Scattering smearing time increases sharply with decreasing observing frequency (as \( r^{-4.5} \), Ramachandran et al. 1997; or alternatively \( r^{-3.9} \), Bhat et al. 2004) and with increasing distance to the pulsar (Taylor & Cordes 1993).

Although the sky background and scatter broadening increase towards lower frequency, we find in our simulations further described below that the total survey productivity, if defined as the total number of pulsars detected (Fig. 3), is mainly determined by the effective collecting area and the beam size. These peak towards the lower edge of the band, leading us to conclude that the survey is most efficient at lowest frequencies. When using a single full-bandwidth 32 MHz station beam this means a central frequency of 140 MHz, from here on our reference frequency. As can be seen from Eq. (2), bandwidth can be freely traded for beams with no impact on the FoM. Splitting up the available bandwidth over multiple independently pointing stations beams (keeping beams-bandwidth product equal to 32 MHz as outlined in Sect. 2) and moving each beam to a lower, more sensitive observing frequency may therefore further increase the overall survey output. This does increase integration time per pointing, which may be only beneficial in the Core Coherent scenario where short default integration times could limit sensitivity to intermittent pulsars.

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**3.1.3. Sensitivity**

The number of simulated normal pulsars, as well as their angular and velocity distributions, are given in Table 1 (Appendix). The minimum detectable flux \( S_{\text{min}} \) depends on the signal-to-noise ratio at which one accepts a signal as real (SNR), the system temperature \( T_{\text{sys}} = T_{\text{rec}} + T_{\text{sky}} \) as it varies over the sky, the number of polarisations \( N_{\text{pol}} \), the bandwidth \( B \), the integration time \( t \), the pulsar period \( P \) and pulse width \( W \) and the zenith-angle dependent gain \( G(z) \). Compared to the theoretical gain the real-life gain is always less; although in Eq. (1) we already use the simulated effective area and take aperture efficiency into account there, we apply a conservative factor 0.66 to estimate the real-life gain for our simulations below. Regarding the impact of RFI on the amount of usable bandwidth, testing has shown the radio-interference environment to be relatively clear, and RFI is significantly reduced by the 12-bit digitisation and the many-element interferometer design, especially when elements are combined coherently. As the total bandwidth can furthermore be quickly split up and spaced to avoid channels contaminated by RFI, we expect that the entire specified 32 MHz band (potentially 48 MHz) will be usable, but below we shall conservatively use 80% of 32 MHz. The potential 1.5-fold increase in usable bandwidth from 32 to 48 MHz would increase sensitivity by \( \sqrt{48/32} \). As \( S_{\text{min}} \) depends on zenith distance and sky noise, it varies per pointing, but after Dewey et al. (1985) we can estimate a typical value for a 1-min pointing towards the zenith using a coherently formed core beam, for a pulsar with a 10% duty cycle:

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turn-overs into account) we scale this luminosity to the observing frequency.

Using the simulated position we look up the sky background temperature (Haslam et al. 1982) and combined with the distance we also estimate the dispersion measure and the scatter broadening from Taylor & Cordes (1993). Given that both sky background and scatter broadening time increase toward lower observing frequencies we next scale these using power laws with spectral index $-2.6$ and $-4.4$ respectively (Lawson et al. 1987; Taylor & Cordes 1993).

For each of the 8 pulsar surveys in Table 2 we model the sensitivity function versus period, dispersion and scattering smearing, and sky position. We also model the decrease of pulse width and hence detectability with period. By comparing the simulated and real pulsar samples for the first four of the above surveys Hartman et al. (1997) determined the most probable underlying initial model parameters.

We use this best model to determine the yield of a future survey with LOFAR. As tests, we also model the second 81.5-MHz Cambridge survey (Shrauner et al. 1998) to check the validity of our extrapolations to lower frequencies and the Parkes Multibeam pulsar survey (Manchester et al. 2001; Lorimer et al. 2006, hereafter PMB) because of its superior statistics. These tests we describe in some more detail in the two paragraphs below.

For each simulated pulsar, we model if it would be detected by the Cambridge survey given its sky position, dispersion and scatter smearing, and luminosity. We estimate the minimum detectable flux from the $S_{\text{min}}$ versus DM and period plot in Shrauner et al. (1998, their Fig. 3). That figure does not take scattering into account, although for these simulations one realistically should. For each simulated pulsar we therefore determine the “effective” (higher) DM-value that would produce the same smearing as the actual dispersion and scattering do combined. We next determine the sensitivity for the period and that “effective” DM. The sensitivity thus estimated is valid for the pulsar. Finally we multiply the sensitivity by the declination-dependent power response (Fig 1a., Shrauner et al. 1998) for the sky position and check if the simulated pulsar is bright enough to be detected. With $27\pm5$ simulated pulsars found, our model reproduces the actual tally of 20 pulsars quite well, validating the luminosity, sky-noise and scattering extrapolations to lower frequencies that we also use for the LOFAR predictions.

As a further check on our model, the PMB simulations find $800\pm40$ pulsars, which compares reasonably well to the actual number of 987 non-recycled pulsars detected (Manchester et al. 2005, ATNF catalog per Jan. 1, 2009).

For LOFAR, we have evaluated surveys for different telescope parameters, total survey time and minimum sensitivity. Our reference survey is a Full Incoherent survey using 54 stations, 64-min pointings, a gain per Eq. (3) of 0.66 times the theoretical gain, with 80% of 32 MHz bandwidth at a central frequency of 140 MHz. With a single beam such a survey can scan the visible sky in 25 days. In an all-sky survey with this reference set up 1100 ± 100 pulsars could be detected (the full curve in Fig. 4), $900\pm100$ of which are new. Our sensitivity estimate B uses a less conservative sensitivity of 0.8 times the theoretical gain. In the same overall time it finds about 100–200 more pulsars that are new; i.e. not detected by older surveys we simulate. We do not take into account findings from ongoing surveys such as the GBT350 search project (Hessels et al. 2008; Archibald et al. 2009). Here, and below, the errors quoted for simulation runs indicate variations in output caused by using different initial random seeds. Between simulation runs, the number of new detections is a stable fraction of the total number of detected pulsars, indicating that in the simulations there is a well-defined part of the pulsar population that only LOFAR is sensitive to. In contrast, there are also known pulsars that LOFAR will not be able to detect in this reference survey, mainly due to scattering effects.

We have evaluated pointings of 1, 2, 4–256 min duration (see Fig. 4). Here the duration effects the minimum detectable flux; using the figures of merit in Table 1 this incoherent survey can be scaled to the other survey types.

If pulsar luminosity is the limiting factor in the detections, a larger time per pointing $t$ decreases the minimum detectable flux $S_{\text{min}}$ as $t^{-2}$, increasing the distance $d$ out to which pulsars can be detected as $t^{2}$. At the scale of the Galaxy pulsars are located in a disk; if one could observe pulsars throughout the Galaxy, the number of detectable pulsars is $N \sim d^{2} \sim t^{2}$. Locally, pulsars are

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**Table 2.** Name, year, number of detected pulsars ($N_{\text{real}}$), number of simulated detected pulsars ($N_{\text{sim}}$) and frequency observed at ($\nu$) for the eight surveys simulated.  

<table>
<thead>
<tr>
<th>Survey</th>
<th>Year</th>
<th>$N_{\text{real}}$</th>
<th>$N_{\text{sim}}$</th>
<th>$\nu$ (MHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jodrell</td>
<td>1972</td>
<td>51</td>
<td>$20 \pm 2$</td>
<td>408</td>
</tr>
<tr>
<td>UMass-Arecibo</td>
<td>1974</td>
<td>50</td>
<td>$39 \pm 4$</td>
<td>430</td>
</tr>
<tr>
<td>MolongloII</td>
<td>1978</td>
<td>224</td>
<td>$227 \pm 7$</td>
<td>408</td>
</tr>
<tr>
<td>UMass-NRAO</td>
<td>1978</td>
<td>50</td>
<td>$54 \pm 6$</td>
<td>400</td>
</tr>
<tr>
<td>Parkes</td>
<td>1991–1994</td>
<td>298</td>
<td>$335 \pm 10$</td>
<td>400</td>
</tr>
<tr>
<td>Cambridge 80MHz</td>
<td>1993–1994</td>
<td>20</td>
<td>$27 \pm 5$</td>
<td>82</td>
</tr>
<tr>
<td>Parkes Multibeam</td>
<td>1997–2000</td>
<td>987</td>
<td>$801 \pm 41$</td>
<td>1374</td>
</tr>
<tr>
<td>LOFAR</td>
<td>2010–2012</td>
<td>–</td>
<td>$1100 \pm 100$</td>
<td>140</td>
</tr>
</tbody>
</table>

The error on $N_{\text{sim}}$ is the standard variation in the outcomes when simulating the model described in the text with different random number seeds. The $N_{\text{real}}$ data is taken from Davies et al. (1977); Hulse & Taylor (1975); Manchester et al. (1978); Damashek et al. (1978); Manchester et al. (1996); Shrauner et al. (1998) and Manchester et al. (2005) respectively. The LOFAR numbers are for the incoherent 25-day reference design described in the text.
distributed roughly isotropically; then $N \sim d^3 \sim \tau^2$ (cf. Cordes 2002). We find that for LOFAR surveys, $N$ is even less dependent on $\tau$ than $N \sim \tau^2$ because scatter broadening is the limiting factor, not luminosity (cf. Fig. 4, where the $\tau^2$ line is scaled to be equal to the reference sensitivity estimate at the 6.25-day point).

Compared to the Parkes Multibeam survey, the pulsars found with LOFAR are different in several ways. The PMB is more strongly focused on the Galactic centre. The range of the population detected by LOFAR is limited by scatter broadening. Because of its higher sensitivity, LOFAR detects more low-luminosity nearby pulsars (Fig. 5a). A lower limit to pulsar luminosity of 1 mJy kpc$^2$ at 400 MHz has been suggested (Lyne et al. 1998, cf. similar lower limit at 1400 MHz in Lorimer et al. 2006); with a spectral index of $-1.5$, this compares to a luminosity at 120 MHz of 6 mJy kpc$^2$. If this lower limit exists the reference survey can detect all pulsars that are beamed toward us up to 1 kpc. If it does not exist, then this survey will certainly illuminate how many low-luminosity pulsars were formed nearby (cf. PSR J0240+62 in Hensels et al. 2008): a number of importance if one wants to understand the neutron-star birthrate.

Furthermore, LOFAR finds more pulsars out of the Galactic disk (Fig. 5b) as its high sensitivity is unimpeded by scattering in that direction. As pulsars are born in the plane ($z = 0$), this observed $z$-distribution could disclose their much debated birth velocity (cf. Hartman 1997; Arzoumanian et al. 2002).

For the detection of millisecond pulsars (MSPs) scatter broadening will be the limiting factor. Although there is much variation in scattering measure for different lines of sight, on average the scatter broadening at 120 MHz is on the order of 1 ms for sources with DMs higher than 30 pc/cm$^3$ (using the rough empirical $t_{sc} = 2 \times 10^9$ DM$^{1.5}$ relation between DM and scattering time by Shitov 1994) or distances of about 1 kpc (using distance-scattering relation from Taylor & Cordes 1993). As many of the currently known Galactic-disk MSPs are within this range of 1 kpc in which scatter broadening does not hinder detection (Manchester et al. 2005), LOFAR could probe the local population to a much lower flux limit.

3.2. Galactic globular cluster surveys

In a fixed-time all-sky survey, one can gain field of view at a cost of instantaneous sensitivity by adding the signal of the stations incoherently instead of coherently. When the incoherent $FOM$ is higher (as in Table 1) this trade-off increases the number of detectable pulsars because it allows for more time per pointing. In contrast, specific, smaller regions on the sky with higher densities of radio pulsars can potentially be better targeted with smaller field of view, but significantly higher sensitivity.

Globular clusters fit the description well; they are compact and form regions on the sky with high stellar densities. These high densities also cause globular clusters to contain more binaries and binary products than are found in the disk. This makes globular clusters very good candidates for MSP searches (cf. Lyne et al. 1987). To estimate which clusters are most promising for a LOFAR search, we evaluated several of their properties: location on the sky, dispersion measure (DM), distance ($d$), and the number of radio pulsars potentially present.

As discussed above for sources in the Galactic plane, scatter broadening is a concern for detecting far-away fast millisecond pulsars. Most globular cluster pulsars have periods of around 2–5 ms (Freire 2008, see Fig. 6). Using the above mentioned DM versus scattering time relations, at 120 MHz such MSPs are detectable up to a DM of about 30–40 pc/cm$^3$. Observing at 200 MHz extends this limit to 60–80 pc/cm$^3$. For the longer period pulsars also present in these clusters, these limits are less of a problem, so we will further investigate globular clusters with DMs up to 100 pc/cm$^3$ below. From low-frequency studies with the Westerbork telescope Stappers et al. (2008) also conclude that the DM versus scattering time relation is uncertain to the extent that some DM = 100 pc/cm$^3$ MSPs may be detectable. We rate the candidate clusters by the expected number of detectable pulsars: assuming $\frac{d \log N}{d \log L} = -1$ (Anderson 1992), this number scales as $d^{-2}$, as the declination-dependent telescope gain $G(z)$ (cf. Fig. 2), and as the collision number $\Gamma \equiv \rho_c^2 r_c^2$, where $\rho_c$ and $r_c$ are the central density and the core radius, respectively.
Table 3. Name, declination (Dec), distance (d), dispersion measure (DM) observed or modeled after Taylor & Cordes (1993), core radius (r_c), collision number (I) and number of detected pulsars (N) for the ten highest-ranking candidates for a LOFAR globular cluster survey.

<table>
<thead>
<tr>
<th>Name</th>
<th>Dec</th>
<th>d (kpc)</th>
<th>DM (pc cm(^{-3}))</th>
<th>r_c (arcmin)</th>
<th>I</th>
<th>N</th>
</tr>
</thead>
<tbody>
<tr>
<td>M15</td>
<td>+12</td>
<td>10.3</td>
<td>67.3</td>
<td>0.07</td>
<td>665</td>
<td>8</td>
</tr>
<tr>
<td>M92</td>
<td>+43</td>
<td>8.2</td>
<td>29</td>
<td>0.23</td>
<td>106</td>
<td>5</td>
</tr>
<tr>
<td>M5</td>
<td>+02</td>
<td>7.5</td>
<td>30.0</td>
<td>0.42</td>
<td>79</td>
<td>5</td>
</tr>
<tr>
<td>M10</td>
<td>-04</td>
<td>4.4</td>
<td>43</td>
<td>0.86</td>
<td>28</td>
<td>4</td>
</tr>
<tr>
<td>M13</td>
<td>+36</td>
<td>7.7</td>
<td>30.4</td>
<td>0.78</td>
<td>39</td>
<td>5</td>
</tr>
<tr>
<td>M3</td>
<td>+28</td>
<td>10.4</td>
<td>26.3</td>
<td>0.55</td>
<td>66</td>
<td>4</td>
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<td>M2</td>
<td>-01</td>
<td>11.5</td>
<td>29</td>
<td>0.34</td>
<td>120</td>
<td>5</td>
</tr>
<tr>
<td>M14</td>
<td>-03</td>
<td>9.3</td>
<td>76</td>
<td>0.83</td>
<td>54</td>
<td>5</td>
</tr>
<tr>
<td>Pal 2</td>
<td>+31</td>
<td>27.6</td>
<td>97</td>
<td>0.24</td>
<td>209</td>
<td>5</td>
</tr>
<tr>
<td>M12</td>
<td>-02</td>
<td>4.9</td>
<td>39</td>
<td>0.72</td>
<td>10</td>
<td>5</td>
</tr>
</tbody>
</table>

Data from Harris (1996) and Freire (2008).

Fig. 6. Periods of the 115 MSPs in globular clusters with periods less than 10 ms. There are another 23 pulsars with longer periods (Freire 2008).

The next over-dense regions on the sky are galaxies. Their distance is a problem, but compared to globular clusters, galaxies have several advantages for a LOFAR pulsar survey. They are distributed equally over both hemispheres, while most globular clusters are invisible from the central telescope site in The Netherlands; and if visible face-on and located in the part of the sky that is pointed away from our Galactic disk, the scatter broadening is relatively low.

In the relatively nearby galaxy M 31, a periodicity search based on a 10 hour pointing with the compact core at 140 MHz could detect all pulsars more luminous than \(-200\) Jy kpc\(^{-2}\) (see Eq. (3)), which is comparable to the top end of the luminosity distribution in our own galaxy. Any M 31 pulsars that emit giant pulses (Argyle & Gower 1972) could be discovered more easily through these giant pulses than through their periodicity if the flux ratio between giant and normal pulses exceeds 10\(^5\) (McLaughlin & Cordes 2003). Two young pulsars, the Crab pulsar B0531+21 and LMC pulsar B0540-69 (Staelin & Reifenstein 1968; Johnston & Romani 2003), are known to emit such giant pulses and the former was indeed discovered through them. Compared to the regular periodic emission, giant pulses show a steeper spectral index (\(-3.0\) to \(-4.5\), Voûte 2001; McLaughlin & Cordes 2003) making giant-pulse searches especially attractive for a low-frequency telescope like LOFAR. Using the McLaughlin & Cordes (2003) maximum distance estimator for giant-pulse detection in 1-h pointings

\[
d = 0.85 \text{ Mpc} \left( \frac{5 \text{ Jy}}{S_{\text{sys}}} \right)^{1/2} \left( \frac{S_{\text{GP}}}{10^3 \text{ Jy}} \right)^{1/4} \left( \frac{B}{10 \text{ MHz}} \right)^{1/4}
\]

with \(S_{\text{sys}} = G_{\text{core}}/T_{\text{sys}} = (0.8 \times 8.8 \text{ K} \text{ Jy})/(1.0 \times 10^3 \text{ K}) = 140 \text{ Jy},\) bandwidth \(B = 32 \text{ MHz} \) and scaling the giant pulse flux with spectral index \(-3.0\), the Crab pulsar would be detectable out to \(~1.5\) Mpc.

Detection of a handful of pulsars in each of several nearby galaxies would enable comparison of the top end of their luminosity functions, and potentially show a relation with galaxy
Table 4. Name, distance \((d)\), size on the sky \((s)\), inclination angle \((i)\), Galactic latitude \((gb)\) and logarithm of the mass \((\log M)\) for the ten highest-ranking candidates for a LOFAR extragalactic pulsar survey.

<table>
<thead>
<tr>
<th>Name</th>
<th>(d)</th>
<th>(s)</th>
<th>(i)</th>
<th>(gb)</th>
<th>(\log M)</th>
</tr>
</thead>
<tbody>
<tr>
<td>M 31</td>
<td>0.7</td>
<td>193</td>
<td>78</td>
<td>−22</td>
<td>11.4</td>
</tr>
<tr>
<td>M 81</td>
<td>1.4</td>
<td>22</td>
<td>60</td>
<td>41</td>
<td>10.7</td>
</tr>
<tr>
<td>M 33</td>
<td>0.7</td>
<td>56</td>
<td>56</td>
<td>−31</td>
<td>10.1</td>
</tr>
<tr>
<td>M 94</td>
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<td>76</td>
<td>10.8</td>
</tr>
<tr>
<td>NGC 2403</td>
<td>4.2</td>
<td>23</td>
<td>62</td>
<td>29</td>
<td>10.7</td>
</tr>
<tr>
<td>NGC 4236</td>
<td>2.2</td>
<td>19</td>
<td>73</td>
<td>47</td>
<td>9.8</td>
</tr>
<tr>
<td>NGC 4244</td>
<td>3.1</td>
<td>15</td>
<td>90</td>
<td>77</td>
<td>10.0</td>
</tr>
<tr>
<td>NGC 4395</td>
<td>3.6</td>
<td>13</td>
<td>38</td>
<td>82</td>
<td>10.1</td>
</tr>
<tr>
<td>NGC 3077</td>
<td>2.1</td>
<td>5</td>
<td>43</td>
<td>42</td>
<td>9.1</td>
</tr>
<tr>
<td>UGC 7321</td>
<td>3.8</td>
<td>5</td>
<td>90</td>
<td>81</td>
<td>9.7</td>
</tr>
</tbody>
</table>

Data taken from Tully (1988).

4. Discussion

4.1. Steep spectrum sources

Generally pulsars are increasingly bright toward lower frequencies, but this steep spectrum of pulsars typically flattens out or turns over at a frequency between 100 and 250 MHz (Malofeev et al. 1994). There is, however, a small fraction of pulsars for which no such spectral break is observed down to frequencies as low as 50 MHz. Sources with a spectral index steeper than the spectral index of the sky background of −2.6 (e.g. PSR B0943+10, spectral index −4.0; Ramachandran & Deshpande 1994) will be more easily detectable by a telescope like LOFAR, producing quantitative input for radio emission models.

4.2. Follow up

With high sensitivity most important and field of view not a consideration, follow up timing (the determination of pulsar and potential binary parameters, cf. Lorimer & Kramer 2005) will use the entire core, and potentially more of the LOFAR array if it can be reliably phased up, for beam forming. Given the small 3′ field of view, such follow up needs very accurate candidate source positions. Determining the source position that accurately also directly facilitates timing follow-up by eliminating position as a variable.

In some of the above surveys sources are only localised to within the 30′ superstation or 5′ station beams (cf. Sect. 3.1.1). Detections can be more accurately located later by following up with many, smaller tied-array beams. As the DM is now known the total computational burden of searching through these many tied-array beams is not as problematic as for an entirely coherent survey. For example, we find that about 50% of incoherent-survey pointings will have sources brighter than the reference \(S_{\text{min}}\). Each of these station-beams pointings could subsequently be filled out with 128 coherent superstation beams in about 1/3rd of the original total survey time (50% \(\sqrt{\text{FoM}_{\text{superstation}}}\) = 0.36, cf. Eq. (2) and Table 1) to reach the same \(S_{\text{min}}\). This would provide the necessary first conformation observation but also an improved position. In a next step 128 compact-core beams can then similarly tile out the superstation beam in which the source is located to provide full localisation, and the first timing data.

Once sources are properly localised, long-term follow up timing uses tied-array beams. From our simulations we find that in the incoherent reference survey about 80% of sources have nearest neighbors at less than one \(FWMH\) station beam away and hence these pairs of sources can be timed simultaneously. 18% and 12% of simulated pulsars are in groups of 3 and 4 per station field-of-view respectively. In total the follow up needs to re-observe about 50% of the survey pointings to time each newly found pulsar once. Sub-arraying or trading bandwidth for independently steerable station beams could potentially increase overall follow-up timing efficiency. The timing observation should hold at least several hundred pulses for a steady profile to form, which at an average 1 s-pulsar translates to about 10 min integrations. Given the \(\sqrt{N_{\text{stations}}} = 7.3\)-fold increase in gain between incoherent surveying and tied-array follow-up, a timing run can thus produce high SNR detections for all candidates.

![Fig. 8. Seven coherently formed beams from the 2-km LOFAR core projected on candidate galaxy M 81 at their FWHM.](image)
4.3. Fast radio transients

Given the software-telescope nature of LOFAR, piggybacking and simultaneous observing are relatively straightforward to implement. As the “telescope time” concept at LOFAR includes the availability of central signal processing at CEP, observation modes that are not computationally or IO intensive, such as the incoherent station addition mode, are especially suited for parallel observing. This incoherent mode can therefore run contemporaneously with many of the imaging projects (Röttgering et al. 2006; Fender et al. 2007) to continuously scan a large part of the sky for intermittent pulsars such as PSR B1931+24 (Kramer et al. 2006) and millisecond radio transients (Lorimer et al. 2007; Hessels et al. 2009).

4.4. Survey strategies