

Submillimeter and X-ray observations of an X class flare

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ABSTRACT

The GOES X1.5 class flare that occurred on August 30, 2002 at 1327:30 UT is one of the few events detected so far at submillimeter wavelengths. We present a detailed analysis of this flare combining radio observations from 1.5 to 212 GHz (an upper limit of the flux is also provided at 405 GHz) and X-ray. Although the observations of radio emission up to 212 GHz indicates that relativistic electrons with energies of a few MeV were accelerated, no significant hard X-ray emission was detected by RHESSI above ~250 keV. Images at 12–20 and 50–100 keV reveal a very compact, but resolved, source of about $\sim 10'' \times 10''$. EUV TRACE images show a multi-kernel structure suggesting a complex (multipolar) magnetic topology. During the peak time the radio spectrum shows an extended flatness from ~7 to 35 GHz. Modeling the optically thin part of the radio spectrum as gyrosynchrotron emission we obtained the electron spectrum (spectral index δ , instantaneous number of emitting electrons). It is shown that in order to keep the expected X-ray emission from the same emitting electrons below the RHESSI background at 250 keV, a magnetic field above 500 G is necessary. On the other hand, the electron spectrum deduced from radio observations ≥ 50 GHz is harder than that deduced from ~70–250 keV X-ray data, meaning that there must exist a breaking energy around a few hundred keV. During the decay of the impulsive phase, a hardening of the X-ray spectrum is observed which is interpreted as a hardening of the electron distribution spectrum produced by the diffusion due to Coulomb collisions of the trapped electrons in a medium with an electron density of $n_e \sim 3\text{--}5 \times 10^{10} \text{ cm}^{-3}$.

Key words. Sun: activity – Sun: flares – Sun: radio radiation – Sun: X-rays, gamma rays – Sun: particle emission

1. Introduction

During solar flares, a fraction of the released energy is used to accelerate electrons with energies well above 1 MeV. The interaction of these particles with the magnetic field of the flaring region produces gyrosynchrotron / synchrotron radiation observed at cm or smaller wavelengths (see e.g. Bastian et al. 1998; Pick & Vilmer 2008, for reviews) and a bremsstrahlung continuum caused by Coulomb collisions observed with X- and γ -ray detectors. It was shown (e.g. Kundu et al. 1994) that the electron spectrum $N(E)$ determined by means of ≥ 30 GHz radio observations is harder than that deduced from Hard X-ray (HXR) below a few hundred keV. However for a few events, the electron spectra were found consistent with spectra inferred from γ -ray continuum above ~1 MeV (Trotter et al. 1998, 2000). Since radio emission above 30 GHz is produced mainly by electrons of a few MeV (see e.g. White & Kundu 1992; Ramaty et al. 1994), these results have an impact on acceleration mechanism models, which are still, an open question in solar flare theory, and reinforces the need for good diagnostics of the >1 MeV particles.

Continuum X- and γ -ray detectors may observe photons from a few keV up to tens of MeV, but have as a limitation the low sensitivity and / or high background in the high energy range. In the past three solar cycles only a few tens of flares have been observed above 1 MeV. On the other hand, radioastronomy at millimeter and submillimeter wavelengths is more

efficient than the γ -ray detectors. Routine solar flare observations at 212 and 405 GHz started in March 2001 with the Solar Submillimeter Telescope (SST, Kaufmann et al. 2001), installed in the Argentinean Andes. A few flares were also observed at 210, 230, and 345 GHz with a receiver array installed at the focus of the Köln Observatory for Submillimeter and Millimeter Astronomy (KOSMA) telescope (Lüthi et al. 2004b,a). The first observations using such instruments showed that the spectrum above 100 GHz is a continuation of the cm-wavelength optically thin spectrum (e.g. Trotter et al. 2002; Lüthi et al. 2004b) and extended the diagnostic tools of radio observations to higher energy (a few tens of MeV) electrons. However, an unexpected upturn of the spectrum above 100 GHz was reported for other $\geq M$ class events (e.g. Kaufmann et al. 2004; Lüthi et al. 2004a; Cristiani et al. 2008). The physical processes responsible for the production of the spectrum upturn are still unknown and are a subject of debate (Kaufmann & Raulin 2006; Silva et al. 2007; Trotter et al. 2008).

In this paper, we present a combined analysis of the impulsive phase of the August 30, 2002, X class flare using RHESSI X-ray observations and spatially unresolved radio data covering the range between 1.5 to 212 GHz (and an upper limit for 405 GHz) obtained by different instruments. The event has been analyzed by different authors. Karlický et al. (2004) related radio observations between 0.8 and 2.0 GHz and X-ray spectra and images from RHESSI. They found high-frequency drifting

structures between 1327:38 and 1327:50 UT with a global drift of -25 MHz s^{-1} . The 10–20 keV X-ray sources show a north-east displacement with a projected velocity of about 10 km s^{-1} , while the 29–44 keV emission is delayed by about 0.5 to 0.7 s after the radio drifting structure. Microwave observations of a short pulse during the onset of this event was analyzed by Giménez de Castro et al. (2006) who found a strikingly narrow spectrum that was explained as gyrosynchrotron emission of accelerated electrons with a maximum energy (high energy cutoff) of about 250 keV. Another event with similar properties was qualitatively discussed by Lüthi et al. (2004b). In this work we extend the analysis of Giménez de Castro et al. (2006) to the entire event. Moreover, we perform a quantitative analysis of the data which allows us to estimate the characteristics of the emitting electrons (energy spectrum, total number) and of the flaring region (density, magnetic field strength) that are necessary to account for the apparent discrepancy between X-ray and radio observations.

2. Instrumentation

The hard X-ray (HXR) and radio data used in the present analysis of the August 30, 2002 event were obtained with the NASA Reuven Ramaty High Energy Solar Spectroscopic Imager (RHESSI), the Solar Submillimeter Telescope (SST, installed in the Argentinean Andes), the nulling interferometer and patrol telescopes of the University of Bern (Switzerland), the Radio Solar Telescope Network (RSTN), and the Solar Radio-polarimeter of the Radio Observatory of Itapetinga (ROI, Brazil).

RHESSI provides imaging and spectral HXR/ γ -ray observations, with high spatial (~ 2 arcsec) and spectral (~ 1 keV) resolution in the ~ 3 keV–17 MeV energy range (Lin & et al. 2002).

The SST (Kaufmann et al. 2000) operates simultaneously at 212 and 405 GHz and with a time resolution of 1 ms for the present event. The focal system consists of four receivers at 212 GHz and two at 405 GHz. At 212 GHz this produces a cluster of beams that, in principle, allows us to determine the centroid of the emitting region whenever an event is detected (see Giménez de Castro et al. 1999, and references therein for details). During the August 30, 2002 flare, SST was tracking NOAA region 10095, with one of the two 405 GHz beams pointing at the active region. At 212 GHz, the event was observed with only one beam so that it was not possible to estimate the centroid position of the emitting region. The antenna temperatures have been corrected for atmospheric attenuation (zenith optical depth $\tau_{212} = 0.3$ nepers and $\tau_{405} = 1.35$ nepers) and converted to flux density assuming that: (i) the source is much smaller than the beam size and; (ii) there is no important main-lobe gain correction due to a possible offset pointing. Since the HPBW of the beams are respectively $\sim 4'$ and $2'$ at 212 and 405 GHz, hypothesis (i) is justified here, because this event is very compact in the HXR domain (see Sect. 3.2). On the other hand, the projected position of the beam that observed the burst in the sky is separated by less than $30''$ from the HXR emitting region observed by RHESSI. As this is comparable to the absolute position uncertainty of the SST antenna, hypothesis; (ii) is also justified. It should be emphasized that a misalignment of $30''$ produces a main-lobe gain correction of less than 5% at 212 GHz ($HPBW \sim 4'$).

The two-element nulling interferometer of the University of Bern provides total flux measurements at 89.4 GHz with a sensitivity of ~ 35 s.f.u. ($1 \text{ s.f.u.} = 10^{-22} \text{ W m}^{-2} \text{ Hz}^{-1}$) and a time resolution of 31 ms (Lüthi et al. 2004b). Total flux densities at 11.8, 19.6, 35, and 50 GHz were recorded by the patrol telescopes at

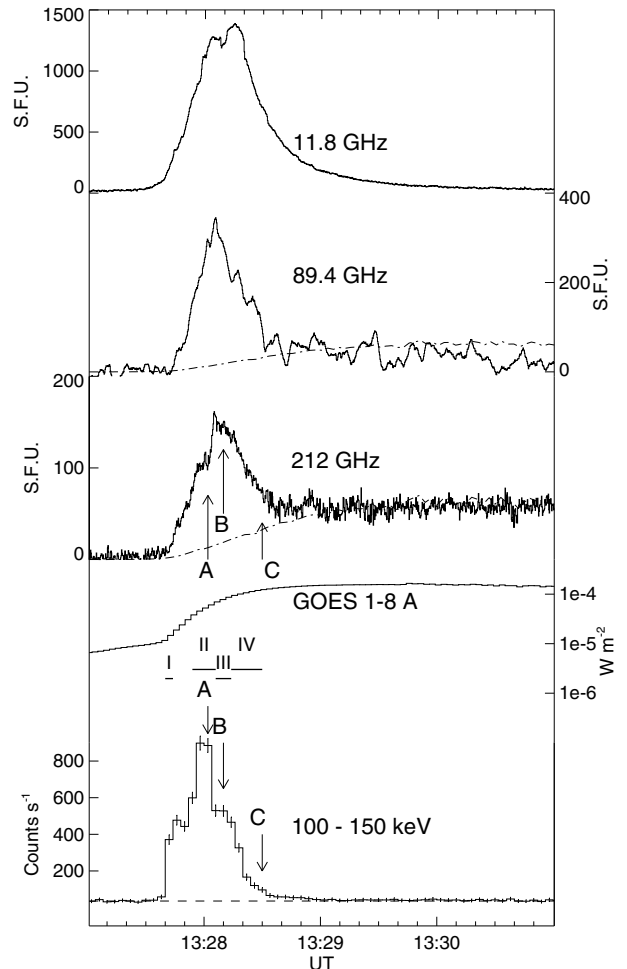


Fig. 1. Time evolution of the August 30, 2002 flare, at different radio frequencies and in selected SXR and HXR energy channels. At 89.4 and 212 GHz the dashed curve represents the computed contribution of an isothermal source. A, B, and C indicate, respectively, characteristic time bins around the maximum of the HXR emission, the maximum of the 212 GHz radiation, and the decay phase of the burst. Horizontal bars denote the time intervals I through IV (see text).

Bumishus (Switzerland) with a time resolution of 100 ms. Total flux density measurements made at 1.415, 2.695, 4.995, 8.8, and 15.4 GHz by the RSTN with a time resolution of 1 s, and at 7 GHz by the Solar Radio-polarimeter of the Radio Observatory of Itapetinga with 20 ms time resolution have also been used.

3. Observations and data analysis

The August 30, 2002 HXR and radio event starting at $\sim 1327:30$ UT is associated with a GOES X1.5 SXR burst and, with a surprisingly small, $H\alpha$ sub-flare which occurred in NOAA Active Region 10095 (N15 E74). This event was observed by RHESSI up to ~ 250 keV around its maximum and in a large part of the radio spectrum ranging from submillimeter to decameter and longer wavelengths. Figure 1 displays the time profile of the event in the 100–150 keV HXR band, in the SXR 1–8 Å channel; it also shows the total flux densities at 11.8, 89.4, and 212 GHz. The flare comprises an impulsive phase that starts at $\sim 1327:40$ UT in the 100–150 keV band and which lasts for about 60 s.

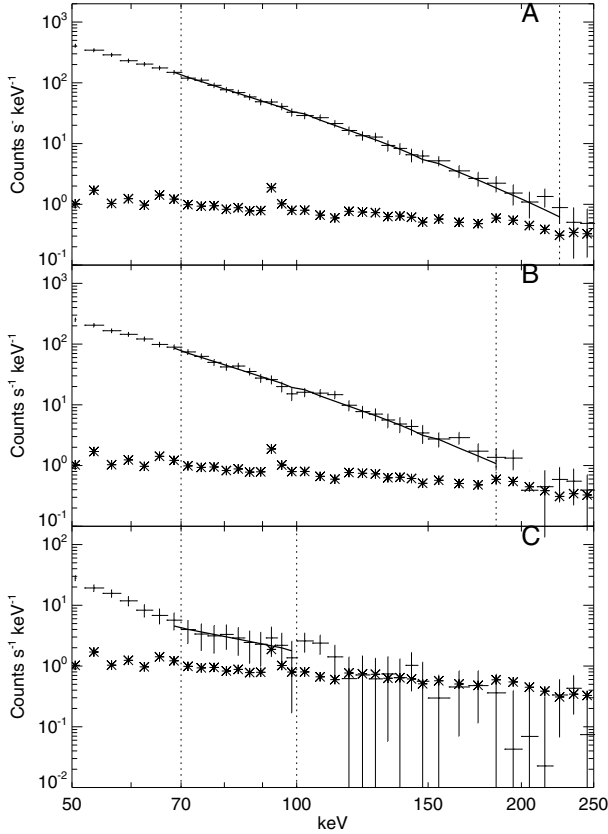


Fig. 2. Background subtracted count rate spectra measured by RHESSI (error bars) during time bins A, B, and C marked in Fig. 1. The asterisks show the background spectrum. The continuous lines show the best fit models (see text). The vertical dashed lines indicate the fitted energy range.

3.1. Flux and spectra

3.1.1. Hard X-rays

Spectral analysis of RHESSI data was performed between 1327:28 and 1328:36 UT. Count rate spectra were accumulated between 1327:38 and 1327:44 UT (before the thick shutter came in) and in all 4 second intervals between 1327:52 and 1328:32 UT using front detectors 1, 3–6, 8 and 9. We applied pile up and decimation corrections. Each spectra consists of 77 energy bands between 3 and 250 keV. For each interval, spectral fitting was carried out for energies ranging from 40 keV to the highest energy where count rates in excess of 2σ above background are measured. It is found that the count rate spectra could be reasonably represented by considering either a single power law or a double power-law. In the latter case, the break energy lies around 70 keV. Since we are interested in the non-thermal X-ray emission, we have restricted the analysis to the energies above 70 keV using a single power-law of spectral index γ for the trial photon spectra. Figure 2 displays examples of the fitted spectra for the time bins labeled A, B, and C in Fig. 1. The time evolution of γ is shown in Fig. 3.

3.1.2. Radio

At frequencies above 20 GHz there is a time extended emission that lasts for tens of minutes after the impulsive phase (see Fig. 1 at 89.4 and 212 GHz). This gradual component is most likely of thermal origin because it seems to follow the SXR emission

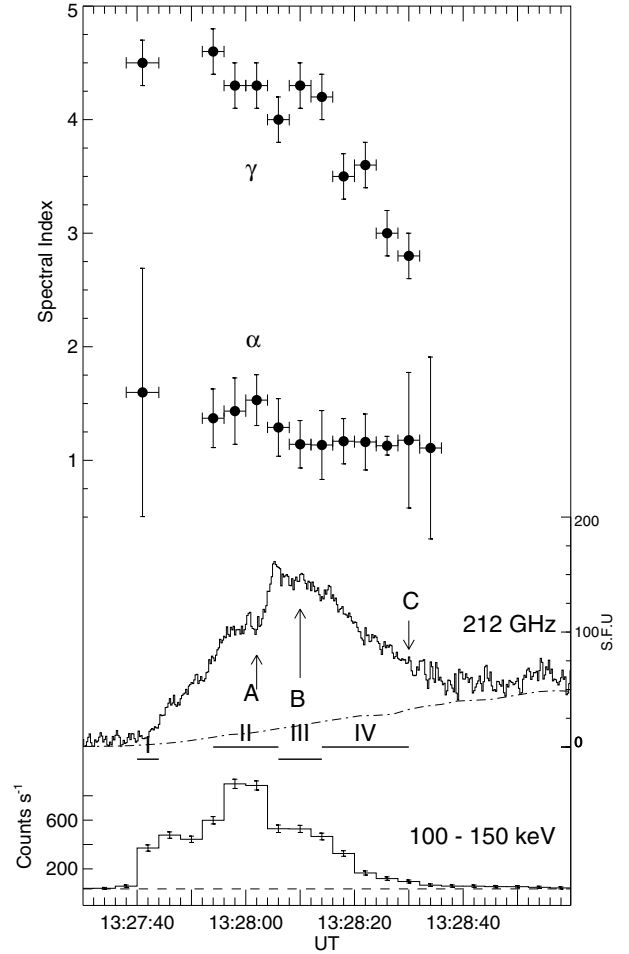


Fig. 3. From top to bottom: time evolution of the HXR spectral index γ and of the radio spectral index α (dots), of the radio flux density at 212 GHz (the dot-dashed curve represents the computed contribution of an isothermal source), and of the 100–150 keV emission. Horizontal bars show the time intervals I through IV (see text).

from GOES and has no HXR counterpart. The comparison of the >20 GHz time evolution with that of the 1–8 Å SXR indicates that this thermal component may have started at the beginning of the impulsive phase and therefore should be subtracted from the total flux densities in order to estimate the non thermal emission of the radio burst. For this we consider that the thermal emission arises from the hot thermal source that produces the SXR emission observed by GOES. We computed the free-free flux density of an isothermal source with temperature and emission measure (EM) derived from GOES 8 observations. A source size of $60''$ provides a reasonable agreement with the observations as illustrated in Fig. 1 (dot-dash lines at 89.4 and 212 GHz curves). Figure 4 shows the non-thermal radio spectrum for the three time bins marked A, B and C in Fig. 1 that correspond, respectively, to the maximum of the 100–150 keV emission, to the maximum of the 212 GHz, and to the decay of the impulsive phase. The main characteristics of the radio spectra can be summarized as follows:

from 1 to 7 GHz: the spectrum increases with frequency and can be represented by a power law with spectral index ~ 1 ;
 from 7 to 35 GHz: there is a plateau observed during the impulsive phase (Fig. 4A, B). During the decay of the impulsive phase the spectrum gradually evolves exhibiting a rather well defined turnover frequency around 5 GHz (Fig. 4C);

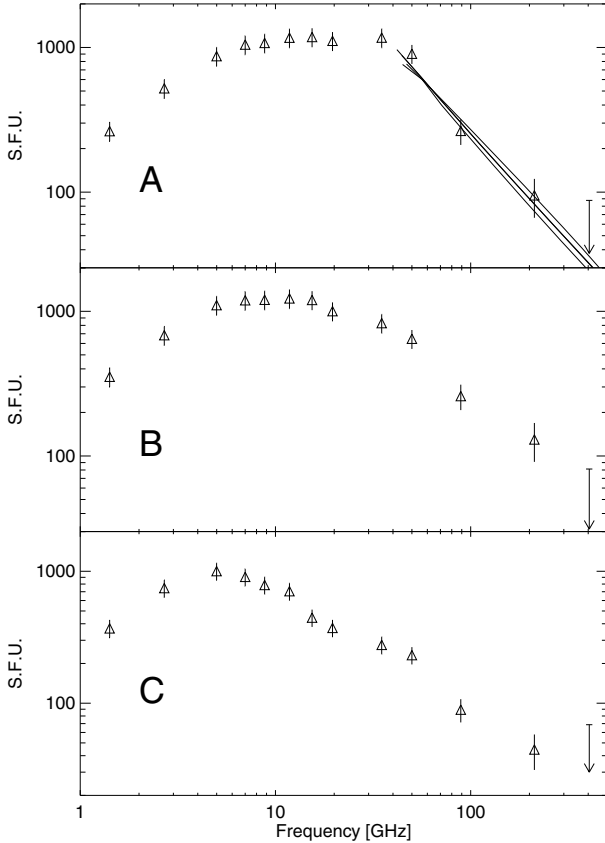


Fig. 4. The radio spectrum at instants labeled A, B, and C. (see Fig. 1) Solid curves represent the homogeneous gyrosynchrotron solution fits discussed in Sect. 4.3.

above 50 GHz: the flux density is roughly proportional to $\nu^{-\alpha}$. Figure 3 shows the time evolution of α .

3.2. HXR images

Figure 5 displays RHESSI contours in the 12–20 keV and 50–100 keV bands overlaid on a 195 Å TRACE image taken at 1327:31 UT for the four intervals marked by horizontal bars in Fig. 1. Intervals I and II cover the first two 100–150 keV peaks, interval III spreads over the maximum of the 212 GHz, while interval IV extends over the HXR decay phase. RHESSI images were obtained by applying the PIXON algorithm (Metcalf et al. 1996) and by using front detector segments 1 to 6. Detector 2 was not used for the 12–20 keV images. The TRACE image was taken close to the onset of the radio and HXR impulsive peaks. The figure shows that the impulsive phase of the flare was triggered within a complex pattern of bright EUV features in a compact region ($10'' \times 10''$). Unfortunately, subsequent 195 Å TRACE images are saturated until 1350 UT. During intervals I and II, the 50–100 keV emission (solid contours) arises from two compact regions ($\sim 3\text{--}7''$) overlaying bright EUV structures. During the rest of the event (intervals III to IV), only the southeast source is observed at 50–100 keV. During the whole event the lower energy HXR (12–20 keV, dashed contours) arise predominantly from a single source close to the southeast of the 50–100 keV emitting region. However, the interpretation of the HXR images at 50 keV for interval III and IV is inconclusive as up to half of the counts are due to pile up of thermal photons. To correct pile up in images is very difficult as the corrections

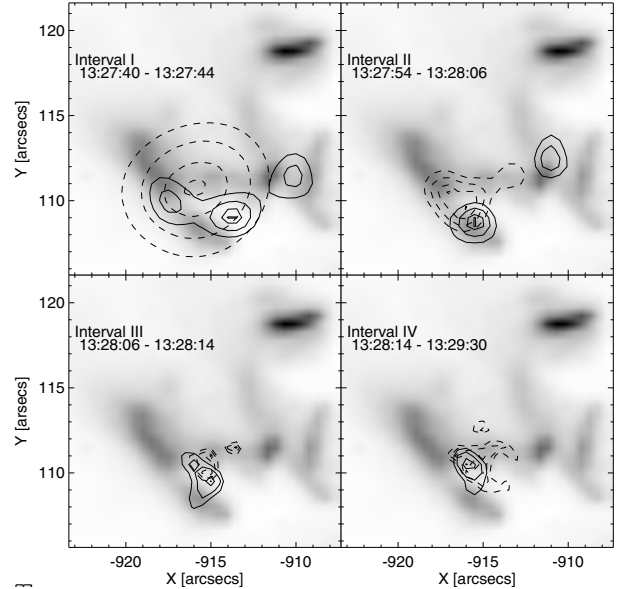


Fig. 5. RHESSI emitting regions of 50–100 keV (solid contours) and of 12–20 keV (dashed contours) for different time intervals superimposed on a negative 195 Å image taken by TRACE at 1327:31 UT. Contour levels are: 50, 70, 90, and 99% of the image maximum.

should be done in the modulated light curves. Currently, the RHESSI software does not provide pile up correction in images.

4. Discussion

EUV observations close to the onset of the impulsive phase of the August 30, 2002 event reveal that this flare arose from a compact region with a multi kernel structure that suggests a complex (multipolar) magnetic field topology. The HXR emitting sources are observed in association with different EUV bright structures, suggesting that they are located at the footpoints of different magnetic loops (see Fig. 5). The compactness of this flare is further supported by the fact that such an X class event produced only an H α sub-flare. In the following, we discuss some peculiarities of this HXR and radio event:

- the unusually flat radio spectrum between 7 and 35 GHz during most of the impulsive phase (intervals I to III on Fig. 1);
- the lack of significant γ ray emission detected by RHESSI in the MeV domain, although ≥ 90 GHz radio data indicate that relativistic electrons were produced during the flare;
- the strong hardening of the >70 keV HXR spectrum during the decay of the impulsive phase.

Figure 3 (top) presents the time evolution of the HXR spectral index γ obtained assuming that the photon distribution is a single power law from 70 keV to the highest energy where count rates are above the background (see Sect. 3.1.1). During intervals I to III, the spectral index does not vary significantly, remaining around $\gamma = 4.3 \pm 0.3$, however during interval IV there is a spectral hardening. We consider that intervals I, II, and III correspond to three successive different particle injections:

- during intervals I and II, the 100–150 keV emission is consistent with thick-target emission because it arises predominantly from footpoint sources. Furthermore there is no long-term coronal trapping because the HXR peaks occur simultaneously at all energies within the RHESSI time resolution (4 s). Thus, the time evolution of the HXR emission

mimics that of the electron injection into the thick-target region;

- taking into account the above arguments, interval III corresponds to a third injection which is reflected by the shoulder in the 100–150 keV time profile range and corresponds to the maximum of the 212 GHz emission;
- the hardening of the HXR spectrum during interval IV may be indicative of some trapping.

4.1. The flat radio spectrum

It is well documented that cm-mm emission comes from gyrosynchrotron radiation of energetic relativistic electrons propagating in the magnetic structures (e.g. [Pick & Vilmer 2008](#), and references therein). The radio spectra of the present event are indeed reminiscent of this emission process. In a uniform magnetic field, the emission would lead to a spectral index larger than 2.5 in the optically thick region and a rather well defined turnover frequency. However, the spectral index for the frequency range 1–7 GHz (optically thick emission) remains around or below 1 during the whole event. And until the decay of the impulsive phase (interval IV) the radio spectrum is flat between 7 and 35 GHz (see Fig. 4). Both these characteristics are indications that radio emitting electrons propagate in a highly inhomogeneous magnetic field (e.g. [Dulk 1985](#); [Klein et al. 1986](#); [Lee et al. 1994](#)). This inhomogeneous magnetic field interpretation is consistent with the complex magnetic structure revealed by TRACE and RHESSI images. During the decay of the impulsive phase, a well defined turnover frequency gradually becomes better defined. At the same time, the X-ray emission arises from a single source, so that the observed radio spectrum is closer to that expected from a homogeneous source.

[Ramaty & Petrosian \(1972\)](#) explained flat microwave spectra as observed by [Hachenberg & Wallis \(1961\)](#) by including the free-free absorption of a cold medium uniformly mixed in the homogeneous gyrosynchrotron source region. Indeed: (i) at low frequencies, where both gyrosynchrotron and free-free opacities are >1 , the radio flux increases with frequency; (ii) at frequencies for which the gyrosynchrotron opacity is <1 while the free-free opacity remains >1 , a plateau is observed because while the gyrosynchrotron emission starts to decrease the free-free emission is still increasing; (iii) at higher frequencies both emissions are optically thin and the radio spectrum decreases with frequency. The observation of simultaneous brightenings and line broadening of hot ($\sim 10^7$ K) and cold ($\sim 10^4$ K) plasmas during a solar limb flare ([Kliem et al. 2002](#)) provides some support to the Ramaty & Petrosian hypothesis. In addition to magnetic field inhomogeneities, free-free absorption may also contribute to provide the observed flat radio spectrum. In that case, as the flare evolves, the free-free opacity should decrease in order to allow lower frequency radiation to become optically thin. Since free-free opacity is proportional to $n_p^2 T_p^{-3/2}$ (n_p , T_p medium density and temperature, respectively, and assuming $n_e = n_p$), this would imply either a decrease of the density, or an increase of the temperature, or an increase of both. In the latter case the temperature should increase faster than the density.

Above 50 GHz (optically thin emission), the radiation, which is mostly emitted by highly relativistic electrons, is not affected by the medium, and the spectral radio index α is only related to the index of the instantaneous electron distribution δ . For the present event α remains between 1.1 and 1.3 (Fig. 3). Considering the ultra-relativistic case as a gross approximation, this leads to $\delta = 2\alpha + 1 = 3.2\text{--}3.6$ ([Dulk 1985](#)).

4.2. HXR spectral hardening during the decay of the impulsive phase

During interval IV the HXR spectral index γ decreases from 4.1 to 2.8 (Fig. 3). This provides some indication that a significant amount of HXR was produced by trapped electrons, the diffusion rate being governed by Coulomb collisions, the trapping time $t^{\text{trap}} \simeq t^{\text{def}}$, with t^{def} the characteristic deflection time, which is given by [Trubnikov \(1965\)](#) and [Melrose & Brown \(1976\)](#)

$$t^{\text{def}} \simeq \frac{E}{2} \left(\frac{dE}{dt} \right)_{\text{coll}}^{-1}, \quad (1)$$

where $(dE/dt)_{\text{coll}}$, the electron energy loss rate due to Coulomb collisions, is approximated by ([Bai & Ramaty 1979](#))

$$\left(\frac{dE}{dt} \right)_{\text{coll}} = \begin{cases} -4.9 \cdot 10^{-9} E^{-0.5} n_e & E \leq 160 \text{ keV} \\ -3.8 \cdot 10^{-10} n_e & E > 160 \text{ keV} \end{cases} \quad (2)$$

with E the electron energy in keV and n_e the medium electron density in cm^{-3} .

We consider that the injection of electrons in the HXR emitting region stopped at 1328:14 UT because it is the last time bin where γ remains almost constant (see Fig. 3). Under these conditions the time evolution of the distribution of the trapped electrons is approximately given by ([Aschwanden 1998](#))

$$N(E, t) \propto E^{-\delta} \exp\left(-\frac{t}{t^{\text{def}}}\right), \quad (3)$$

with δ the electron index at the end of the injection. The photon flux at energy ϵ as a function of time t may be written as (see e.g. [Brown 1971](#))

$$F(\epsilon, t) = n_e \int_{\epsilon}^{\infty} \sigma(\epsilon, E) v(E) N(E, t) dE, \quad (4)$$

where $v(E)$ is the electron velocity corresponding to energy E , $\sigma(\epsilon, E)$ is the bremsstrahlung differential cross-section per unit photon energy ϵ for an electron of energy E . For $\sigma(E)$ we adopted the Bethe-Heitler electron – proton bremsstrahlung cross-section. It should be noted that the photon flux produced by precipitated electrons has a time evolution as $F(\epsilon, t)$ ([Melrose & Brown 1976](#)). Therefore, for a given δ , the time evolution of the photon flux depends only on n_e . By using Eq. (4) we computed the expected photon flux $F(\epsilon, t)$ and compared its time evolution at different energies ϵ with that observed by RHESSI during the decaying of the impulsive phase. Comparing the expected and observed time profiles at 70, 100, and 150 keV, we obtained reasonable agreement for $n_e \sim 3\text{--}5 \times 10^{10} \text{ cm}^{-3}$ when δ ranges between 3.5 and 5, which correspond respectively to thin and thick target limits for $\gamma \sim 4$. [Krucker et al. \(2008\)](#) find similar electron densities for coronal γ -ray emission during flares.

Spectral hardening has been reported during the impulsive phase of long duration GOES X class flares and associated with non thermal footpoint bremsstrahlung ([Qiu et al. 2004](#); [Saldanha et al. 2008](#)). [Grigis & Benz \(2008\)](#) analyzed the spectral hardening during the gradual phase of great flares and concluded that the cause is the continuing acceleration with longer trapping in the accelerator before escape. [Kiplinger \(1995\)](#) has shown that the hardening is associated with SEP events.

4.3. Relationship between HXR and radio emission

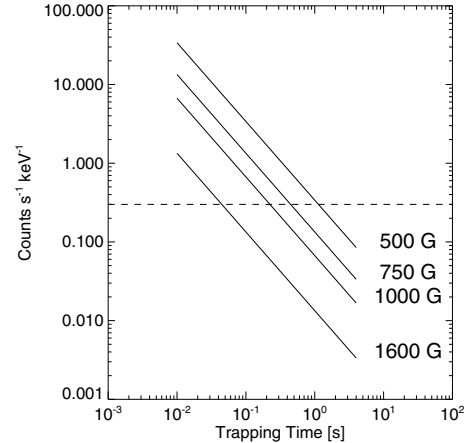
The absence of HXR emission >250 keV while we observe radio emission above 50 GHz can be used to constrain the high

Table 1. Derived characteristic of radio radiating electrons for different magnetic field strengths and view angle equal to 84° .

B (Gauss)	$N(> 25 \text{ keV}) \times 10^{33}$	$K \times 10^{29}$ ($e^- \text{ MeV}^{-1}$)
500	38.1	76.0
750	15.0	30.0
1000	7.5	15.0
1600	1.5	3.0

energy electron distribution, the magnetic field, and the trapping time in the radio emitting region. For that, we consider that non thermal electrons are injected in coronal loops. The radio emission is produced in the coronal portion of these loops where they become partially trapped while precipitating electrons produce the HXR radiation by thick target interaction at the loop footpoints. Since no spatially resolved radio data are available for this event and the optically thin part of the radio spectrum does not depend on the structure details of the medium, we used a homogeneous model to derive the mean parameters of the radio source and emitting electrons. For that, we computed the radio optically thin emission by using the numerical code for a gyrosynchrotron source with a homogeneous ambient density and magnetic field and an isotropic electron distribution developed by Ramaty (1969) and corrected by Ramaty et al. (1994)¹. The instantaneous electron distribution in the radio source was taken as $N(E) = KE^{-\delta}$, where K is the number of electrons per MeV at 1 MeV and the energy E is in MeV. The angle between the observer and the magnetic field (view-angle) was set to 84° (the maximum allowed value in Ramaty's solution) in order to obtain the lower limit of the total number of electrons necessary to produce a given radio spectrum for a given magnetic field strength. For a view-angle of 45° , as is usually assumed, the computed number of electrons is roughly twice that obtained for 84° . Table 1 displays the values of the instantaneous total number of electrons above 25 keV $N(> 25 \text{ keV})$ and K obtained for different values of the magnetic field at the maximum of the 100–150 keV HXR (time bin A). $N(> 25 \text{ keV})$ was computed for $\delta = 3.4$ which provides the best fit to the radio data. This is in agreement with the value of δ inferred from the slope of the optically thin part of the radio spectrum α (see Sect. 4.1).

The mean electron flux $\dot{N}(E)$ entering the thick target HXR source is $\dot{N}(E) \simeq N(E)/t^{\text{trap}}$, where t^{trap} is the time spent by the electrons in the radio source. The thick target photon emission from these precipitating electrons was calculated by using a numerical code that takes into account both electron-proton and electron-electron collisions. The photon spectrum is then convolved with the RHESSI response matrix to get the corresponding count rate spectrum. Figure 1 shows that within the RHESSI time resolution (4 s), the 89.4 GHz, 212 GHz and 100–150 keV count rates show simultaneous peaks during intervals I to III. The electron trapping time t^{trap} can thus be considered independent of energy as a first approximation. This suggest that during intervals I to III the precipitation rate is more likely governed by wave-particle interactions (turbulent trapping) than by Coulomb collisions (e.g. Vilmer 1987). The computations were then carried out for $10^{-2} \leq t^{\text{trap}} \leq 4 \text{ s}$, the lower and upper limits correspond respectively to free streaming of the electrons in a compact loop ($\sim 10''$), and to the RHESSI time resolution. Figure 6 displays the RHESSI expected count rates in the 250–265 keV band as a function of t^{trap} for different values of the

**Fig. 6.** Expected RHESSI count rates at 250 keV as a function of the emitting electron trapping time for different magnetic field strengths and view angle equal to 84° . Each solid line represents a different solution determined by a different magnetic field. The dashed horizontal line represents the measured background count rate at 250 keV.

magnetic field. The dashed horizontal line corresponds to the RHESSI count rate in this channel, the highest energy where this event was detected. We conclude that the mean magnetic field strength should be greater than about 500 G to keep the thick target photon flux expected from radio emitting electrons with trapping times smaller than 1 s below the detection limit of RHESSI.

It has been shown that the thick target spectral index γ is bounded between $\delta - 1.5 \leq \gamma \leq \delta - 1$, the lower limit corresponding to turbulent trapping of electrons with energies above a few 100 keV, whereas the higher limit is set by free propagating electrons with energies below a few 100 keV (see e.g. Trotter et al. 1998, and references therein.). Therefore if $\delta = 3.4$, the HXR emission of these electrons should have an index between $1.9 \leq \gamma \leq 2.4$ which is significantly smaller than the observed values, ~ 4.3 , during intervals I to III (see Fig. 3). This is in accordance with previous works that show that radio high frequency emission is generated by electrons with energies above $\sim 500 \text{ keV}$ with an electron index harder than the $< 500 \text{ keV}$ electrons (White & Kundu 1992; Kundu et al. 1994; Trotter et al. 1998; Silva et al. 2000).

5. Summary

In this paper we have analyzed X-ray observations from RHESSI and radio data obtained at submillimeter wavelengths by the Solar Submillimeter Telescope (SST) of the X1.5 event that occurred in Active Region 10095 on August 30, 2002, at 1327:30 UT, complemented with radio observations from 1.5 to 89.4 GHz from other instruments. EUV images from TRACE provided information about the source emitting region.

The radio spectrum above 100 GHz is the continuation of the optically thin microwave spectrum, therefore does not belong to the so called THz bursts (Kaufmann et al. 2004), although it is an X Class flare. We summarize below our main findings:

- The magnetic structure of the flare is complex and highly inhomogeneous. This is revealed by the 50–100 keV and EUV images. Such an inhomogeneous source may produce the flatness in the radio spectrum observed between 7 and 35 GHz, although we do not discard the free-free absorption.

¹ See <http://lhea-www.gsfc.nasa.gov/users/ramaty>

- The electron spectrum $N(E)$ above 1 MeV is harder than that at energies below a few hundred keV.
- Modeling simultaneously the expected RHESSI count rate and the expected gyrosynchrotron emission, we obtain 500 G as a lower limit for the mean magnetic field of the flaring region.
- The time evolution of the spectral index deduced from X-ray observations at the end of interval III suggests that trapped electrons are diffused by Coulomb collisions. This leads to a mean ambient electron density of $3\text{--}5 \times 10^{10} \text{ cm}^{-3}$, typical of the low corona / upper chromosphere and is compatible with previous results (Krucker et al. 2008) and with the small size of the EUV pattern observed by TRACE, which also suggests that the flaring region does not extend high in the corona.

Finally it should be emphasized that radio observation in the sub-THz domain provide a unique tool to constrain acceleration model because they constitute a more sensitive diagnostic of ultra-relativistic electrons than present HXR/ γ -ray measurements.

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