Galaxy distribution and evolution around a sample of 2dF groups

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Received 28 May 2009 / Accepted 1 July 2009

ABSTRACT

Context. We study galaxy evolution and spatial patterns in the surroundings of a sample of 2dF groups.

Aims. Our aim is to find evidence of galaxy evolution and clustering out to 10 times the virial radius of the groups and so redefine their properties according to the spatial patterns in the fields and relate them to galaxy evolution.

Methods. Group members and interlopers were redefined after the identification of gaps in the redshift distribution. We then used exploratory spatial statistics based on the the second moment of the Ripley function to probe the anisotropy in the galaxy distribution around the groups.

Results. We found an important anticorrelation between anisotropy around groups and the fraction of early-type galaxies in these fields. Our results illustrate how the dynamical state of galaxy groups can be ascertained by the systematic study of their neighborhoods. This is an important achievement, since the correct estimate of the extent to which galaxies are affected by the group environment and follow large-scale filamentary structure is relevant to understanding the process of galaxy clustering and evolution in the Universe.

Key words. galaxies: evolution – galaxies: interactions – galaxies: clusters: general

1. Introduction

Small groups of galaxies contain about half of all galaxies in the Universe (e.g., Huchra & Geller 1982; Geller & Huchra 1983; Nolthenius & White 1987; Ramella et al. 1989). They represent the link between galaxies and large-scale structures, and have at least two important features: galaxies inside groups interact more with each other than they do in the field; and groups have small crossing times, generally \(0.1 H_0^{-1}\), indicating that they are dynamical units, that are possibly in virial equilibrium. However, the dynamical state of a galaxy group is not easy to determine. Group environments are unstable, the systems still may be separating from the cosmic expansion, collapsing, accreting new members, or merging with other groups to produce larger objects. Generally, the estimated properties of these systems are based on the assumption that groups of galaxies defined by friends-of-friends algorithm (and other clustering methods) are gravitationally bound objects. This is not completely true, since projection effects can dominate the statistics of these systems (e.g., Diaferio et al. 1993). In a \(Λ\)CDM cosmology, Niemi et al. (2007) showed that about 20% of nearby groups are not bound, but merely visual objects. There is no methodology for determining the dynamical status of galaxy groups. An interesting attempt at describing group evolution is the fundamental track diagram, a plane that follows the evolution of isolated galaxy systems in an expanding Universe (see Mamon 1993). The plane is defined by the dimensionless crossing time and the dimensionless mass bias. This diagram, however, suffers from degeneracies between the expansion and early collapse phases, and also between the full collapse and rebound phases. Although most groups lie close to the fundamental track, there is a large scatter and the result is inconclusive (Mamon 2007). Giuricin et al. (1988) applied a correction factor to the virial mass and assumed a specific model for the system evolution, but the model only accounted for internal gravitational forces and neglected tidal interactions with the neighborhoods. Galaxy groups, however, interact significantly with their surroundings. For instance, the shapes and galaxy flows around these systems are related to large-scale structures and are relevant to the internal dynamics of the groups (e.g., Plionis et al. 2004; Ceccarelli et al. 2005; Paz et al. 2006). Generally, one assumes that bound groups reach a quasi-equilibrium state in which galaxies have isotropic orbits and are not deflected from their radial trajectories until the group has collapsed to a small fraction of its maximum radius. In this case, the collapse is violent and the group first reaches equilibrium at \(~200\times\) times the mean cosmic density. At the opposite extreme in which a nascent group is strongly influenced by surrounding objects, the collapse is gentle and the group attains equilibrium at lower density contrasts. Hence, measuring environmental influence over galaxy systems can be a way of accessing their formation history and present dynamical state. In the present work, this important point is investigated where we study the surroundings of galaxy groups previously selected from 2dF by...
Tago et al. (2006). Using some tools of spatial statistical analysis, we examine the possible correlation between the anisotropy around groups and galaxy evolution. This relationship may shed some light on the dynamical state of galaxy groups.

This paper is organized as follows: In Sect. 2 we present the methodology and data used in this work; in Sect. 3, we present our results and explore the relation between anisotropy and galaxy evolution; and in Sect. 4, we discuss our results.

2. Methodology and data

2.1. Probing anisotropy around groups

For the projected distribution, anisotropy can be probed by the reduced second-order moment measure $K$ of a point pattern (e.g., Stoyan et al. 1994). In this work, we estimate $K$ using the library spatstat (see Baddeley 2008) within the R statistical package. The command Kmeasure (spatstat) executes the following steps:

1. A point pattern is assumed.
2. A list of all pairs of distinct points in the pattern is produced.
3. The vectors that join the first point to the second point in each pair are computed.
4. These vectors are considered to be a new pattern of “points”.
5. A Gaussian kernel smoother is applied to them.

The algorithm approximates the point pattern and its window with binary pixel images, introduces a Gaussian smoothing kernel, and uses the Fast Fourier Transform to form a density estimate of $\hat{\kappa}$, the density estimate of $K$. The calculation takes into account the edge correction known as the “translation correction” (see Ripley 1977). The density estimate of $\kappa$ is returned in the form of a real-valued pixel image. The $\hat{K}$ estimator is defined as the expected number of points lying within a distance $r_{\text{max}}$ of a typical point, and with a displacement vector of orientation in the range $[\alpha, \beta]$. This can be computed by summing the entries over the relevant region, i.e., the sector of the disc of radius $r$ centered on the origin with angular range $[\alpha, \beta]$. Hence, we can compute a measure of anisotropy (A) as integrals of the form

$$A \equiv \int_{0}^{r_{\text{max}}} \int_{\alpha}^{\beta} dv(r, \theta).$$  \hspace{1cm} (1)

Note that the second-order moment function $K$ is used to test the hypothesis that a given planar point pattern is a realization of a Poisson process. Thus, the objective is to search for significant peaks in the integral given in Eq. (1) for angular steps $\Delta\theta = \beta - \alpha$. The uncertainty in the anisotropy measurement is computed directly from the variance in the pixel values in the corresponding circular sector. Of course, the choice of $\Delta\theta$ is arbitrary. In this work, we assume that $\Delta\theta = 10^\circ$, based on the following analysis.

Consider a controlled sample corresponding to a point pattern given by a Poisson distribution (100 points) plus a central group defined as a Hernquist spheroid (Hernquist 1990). An additional group is located initially at $\sim 4h^{-1}\text{ Mpc}$ around an angle of $45^\circ$, and then around an angle of $135^\circ$. In Fig. 1, we present both the mock field and the anisotropy signal as a function of the angle for the two positions of the second group. It is clear from this figure that the second group produces significant anisotropy signal. To justify our choice of $\Delta\theta$, we present in Fig. 1 (lower panel) a reanalysis in the case of the second group at $45^\circ$ for $\Delta\theta = 5^\circ$, $10^\circ$, and $20^\circ$. For $\Delta\theta = 5^\circ$, we still detect the peak, but there are now secondary peaks and a more noisy behavior for $A$. For $\Delta\theta = 20^\circ$, the peak is still there, but now less significant. This result suggests that in the limit of a too small value $\Delta\theta$, we have a noisy anisotropy curve (possibly with false peaks), while in the limit of very large $\Delta\theta$, the signal can be completely lost.

In this work, we set $\Delta\theta = 10^\circ$ as a confidence scanning angle to probe anisotropy in galaxy fields of our sample.

2.2. The 2dF sample

We apply the anisotropy estimator to a sample consisting of 32 galaxy groups previously identified by Tago et al. (2006) applying the friends-of-friends algorithm to data from the 2dFGRS (Colless et al. 2001). This subset corresponds to those groups located in areas of at least 80% redshift coverage out to 10 times the virial radius roughly estimated from the projected harmonic mean. Group members and interlopers were redefined after the identification of gaps in the redshift distribution according to the technique described by Lopes et al. (2009). Before selecting
group members and rejecting interlopers we first refine the spectroscopic redshift of each group and identify its velocity limits. For this purpose, we employ the gap technique described in Katgert et al. (1996) and Olsen et al. (2005) to identify gaps in the redshift distribution. A variable gap, called density gap (Adami et al. 1998), is considered. To determine the group redshift, only galaxies within 0.50 $h^{-1}$ Mpc are considered. Details about this procedure are found in Lopes et al. (2009).

With the new redshift and velocity limits, we apply an algorithm for interloper rejection to define the final list of group members. We use the “shifting gapper” technique (Fadda et al. 1996), which consists of the application of the gap technique to radial bins from the group center. We consider a bin size of 0.42 $h^{-1}$ Mpc (0.60 Mpc for $h = 0.7$) or larger to ensure that at least 15 galaxies are selected. Galaxies not associated with the main body of the group are discarded. This procedure is repeated until the number of group members is stable and no further galaxies are eliminated as intruders. An example of the application of the shifting gapper procedure is seen in Fig. 2 (upper panel). The main difference from the study of Lopes et al. (2009) is that here we consider all galaxies within 10 times the virial radius (as listed in Tago et al. 2006). In Lopes et al. (2009), the interloper removal procedure was applied to galaxies within a maximum radius of 2.5 $h^{-1}$ Mpc. Next, we estimate the velocity dispersions ($\sigma$) and physical radius ($R_{200}$) of each group. Finally, a virial analysis is performed for mass estimation ($M_{200}$). Further details regarding the interloper removal and estimation of global properties ($\sigma$, physical radius and mass) are found in Lopes et al. (2009).

The physical properties of these groups are presented in Table 1. The columns correspond to

1. Group identification number;
2. RA (J2000.0) in degrees (mean of member galaxies);
3. DEC (J2000.0) in degrees (mean of member galaxies);
4. $z$, the new redshift, determined within 0.5 $h^{-1}$ Mpc;
5. $\sigma$, the velocity dispersion in km s$^{-1}$ (computed with the group members);
6. $R_{200}$ in Mpc;
7. $M_{200}$ ($10^{13} M_\odot$);
8. number of member galaxies (after exclusion of interlopers);
9. number of member galaxies within $R_{200}$;
10. global anisotropy (see definition in Sect. 2.3);
11. fraction of $\eta_1$ galaxies (Sect. 2.3);
12. fraction of galaxies within $R_{200}$.

### 2.3. Description of one group + surroundings field

The methodology presented in Sect. 3.1 is now applied to describe in detail the anisotropy features of Group 91 plus its neighborhood. This field is presented in Fig. 2 (lower panel), where equatorial coordinates were transformed to Cartesian ones using redshift information for a flat universe with $\Omega_M = 0.3$. We can see that the galaxy distribution is clearly anisotropic. In Fig. 3, we present the same field, but now we identify differences in the general behavior according to the galaxy spectral type defined by Madgwick et al. (2002). The $\eta$ parameter is a measure of spectral type, which corresponds approximately to the following division:

<table>
<thead>
<tr>
<th>$\eta$</th>
<th>Spectral Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>$&lt; -1.4$</td>
<td>E-S0 galaxies</td>
</tr>
<tr>
<td>$-1.4 \leq \eta &lt; 1.1$</td>
<td>Sa galaxies</td>
</tr>
<tr>
<td>$1.1 \leq \eta &lt; 3.5$</td>
<td>Sb galaxies</td>
</tr>
<tr>
<td>$\geq 3.5$</td>
<td>Scd galaxies</td>
</tr>
</tbody>
</table>

(see Madgwick et al. (2002) for more details about the spectral type classification and data division by $\eta$).

In this work, we ascertain whether the anisotropy pattern is related to the galaxy types in the group + surroundings field. The anisotropy profile of Group 91 is presented in Fig. 4 (upper panel), where we see the overall behavior in the small box and the behavior per type in colors (main box). Typically, our fields are so dominated by $\eta_1$ galaxies (~60% in average) that the number of Objects in the remaining bins are too small for comparisons between each other. Here, we just compare $\eta_1$ with the other types, according to $\eta_1 \times \eta_2$, $\eta_1 \times (\eta_3 + \eta_1)$, and $\eta_1 \times (\eta_2 + \eta_3 + \eta_4)$. To verify whether the respective profiles differ significantly from each other, we applied a bootstrap hypothesis test, assuming as the null hypothesis that the mean of the difference in the anisotropy signal between two populations is zero ($H_0 : \mu = 0$), while the alternative hypothesis is $\mu \neq 0$. A small $p$-value makes the null hypothesis appear implausible. Obtaining $p$ can be done using the bootstrap resampling approach. In this work, based on 1000 bootstrap sample replications, we obtain
for Group 91: $\eta_1 \times \eta_2$: $p = 0.008$; $\eta_1 \times \eta_{24}$: $p = 0.014$; and $\eta_1 \times \eta_{24}$: $p = 0.015$. Taking the usual cutoff of $p = 0.05$ (5% significance level), we reject the null hypothesis in all cases and conclude that $\eta_1$-type galaxies in this case have a distinctive spatial distribution. Additionally, determining the group + surroundings shape by diagonalizing the moments of the inertia tensor as a function of the radius, we find that there is an elongation jump close to $R_{200}$ (see Fig. 4, lower panel). This suggests that the group is embedded in a highly anisotropic structure.

We applied this methodology to the remaining groups of our sample and found that only 15% of the groups (91,139,189,193, and 250) have a distinctive $\eta_1$ population. However, the number of fields with significant elongation is quite high. To help us understand that, we define a new quantity, the global anisotropy (GA) as

$$GA = \frac{\text{Max}(A) - \text{Median}(A)}{\sigma(A)}.$$  \hfill (2)

Basically, this is a measure of the relative importance of the anisotropy peak with respect to the entire profile. The values of GA are listed in Table 1. Here, we require that a significant elongation corresponds to $GA \geq 2$, i.e., $\text{Max}(A) \geq 2\sigma(A) + \text{Median}(A)$. Following this criterium, we have found that 94% of the fields have a high degree of elongation. Being more restrictive and setting $GA \geq 3$, 37% of the systems still have this alignment prominence. In our control sample of 1000 Hernquist spheroids + Poisson background, we found just 12% of alignments by chance. Hence, we conclude that our sample consists of a significant number of group + surroundings predominantly elongated.

![Fig. 3. Galaxy distribution around Group 91 per $\eta$-type division with central $1\ h^{-1}$ Mpc squares in dashed lines.](image-url)
defined by one of the other quantities ($M_B$, $B-R$, and distance to the center of the groups, $d_c$). In the second case, the two data sets are redefined for increasing (or decreasing) values of the quantity, so we can find the corresponding divisory line (i.e., the first value in which the null hypothesis is rejected).

We first probe the distribution of galaxies as a function of the distances to the center of the groups. To illustrate our results more clearly, galaxies were sorted in $\eta$ and divided into seven subgroups with the same number of objects. In Fig. 5 (upper panel), we see that low $\eta$ (early-type) galaxies are more concentrated than high $\eta$ objects. We verified a corresponding horizontal line at $d_c/R_{200}$ = 1.5, where data can be divided into two statistically distinct groups, after a $t$-test ($p = 1.78 \times 10^{-5}$). This expected result is just a manifestation of the morphology-density (radius) relation (e.g., Dressler 1980). We also find that our sample is dominated by dwarf galaxies ($M_B \geq -20$ for \(-90\% of the sample) and that low $\eta$ galaxies are more luminous than the remainder (see Fig. 5, middle panel), where a horizontal line at $M_B = -18.55$ divides data into two subgroups that are statistically distinct ($p = 1.02 \times 10^{-5}$). Finally, the distribution of $(B-R)$ color indicates two distinct groups at $B-\sigma = 1.1$ ($p = 8.07 \times 10^{-5}$), where low $\eta$ galaxies are redder than the rest (see Fig. 5, lower panel). Thus, our sample is dominated by dwarfs, and low $\eta$ objects are more central, luminous, and redder than the other galaxies.

### 3. Anisotropy and galaxy evolution

The intrinsic elongated shape of groups can be a very important factor when determining their dynamical state (e.g., Tovmassian & Plionis, 2009). In this section, we investigate a possible correlation between anisotropy and galaxy evolution for all galaxies in our sample.

#### 3.1. Characterizing galaxies around groups

We use the spectral parameter $\eta$ to characterize galaxy evolution around groups. We applied the Welch’s $t$-test (Welch 1947), also known as the $F$-test (Press et al. 1986), which is an adaptation of the Student’s $t$-test, to the comparison of two samples (in this case $\eta < -1.4$ and $\eta \geq -1.4$) with unequal variance. This statistic tests the null hypothesis that the mean of each of the two samples are equal, assuming a normally distributed parent population. The test was applied in two ways: i) testing the two samples by keeping the divisory line $\eta = -1.4$ and ii) testing data iteratively in samples...
Distances of galaxies to the center of the groups (normalized by $R_{200}$) as a function of $\eta$ (upper panel). Absolute magnitudes as a function of $\eta$ (middle panel). $B-R$ color as a function of $\eta$ (lower panel). Dashed lines divide data into two groups statistically distinct.

A fitted plane given by $M_{200} = 0.001\sigma + 3.985R_{200} - 2.792$ ($p = 1.2 \times 10^{-15}$, for a $F$-statistic). Dividing groups according to their galactic content, i.e., the fraction of $\eta_1$ galaxies, we can see a clear difference in the group distribution on this plane. Open circles denote groups with $f_{\eta_1} > 0.55$, which are distributed more to the left and bottom of the plane, while filled circles represent groups with $f_{\eta_1} \leq 0.55$, predominantly located to the right and top of the plane (0.55 is the median value for $f_{\eta_1}$). The existence of a plane in the $(\sigma, R_{200}, M_{200})$ space indicates that groups are sufficiently evolved for their properties to be well correlated in this dynamical frame. We note, however, that $f_{\eta_1}$ is related to entire fields, and not only to groups. Hence, different loci on this plane for low and high $f_{\eta_1}$ fields indicate a relation between the groups and their surroundings. Recall that $f_{\eta_1}$ is also anticorrelated with GA, another field (not group) measurement. Hence, a tantalizing view of this result is that we have groups in different dynamical states approximately along the diagonal from the top-right to the bottom-left corners of the fitted plane. This is not exactly an evolutionary track, but an indicator of how anisotropy, galactic content, and dynamics are intimately connected during the formation of galaxy systems.

### 4. Discussion

The spatial distribution of galaxies traces the shape of the dark matter potential in which they are embedded. Simulations show that dark matter halos are not spherical, as one would expect from dark matter dissipationless nature, but they are strongly flattened triaxial ellipsoids (e.g., Dubinski & Carlberg 1991). Groups are probably the most suitable objects to use in studying the shapes of dark matter halos, since they connect the general field of galaxies and large-scale structure. Indeed, any correlation between morphological properties of the groups and galaxy evolution can provide an indication of how matter assembles to form larger and larger galaxy systems, and how the environment affects galaxy evolution during this process.

In this work, we have introduced a new method to probe extended regions around galaxy groups. Based on the second moment of the Ripley function, the method allows us to define an operational anisotropy profile that indicates preferential
directions around the systems. We also define a GA from the anisotropy profile, a quantity that can be compared to other properties of the groups. Galaxies in our 2dF group sample are distributed out to $\sim 10R_V$ around the center of the groups, so we have fairly extended samples of group + surrounding galaxies. We find that GA is correlated with the spectral parameter $\eta$ (Madgwick et al. 2002), an indicator of the star formation rate of galaxies. Observations indicate that the lower star formation rate of group galaxies is visible out to 2$R_{200}$ (Balogh et al. 1998), while $\Lambda$CDM numerical simulations show that particles that penetrate deep into dark matter halos travel out to $\approx 2.6R_{200}$ (Gill et al. 2005). In this work, we have found that galaxies represent two statistically distinct groups with a transition at $\eta = -1.4$ and $d_L = 1.5R_{200}$, a scale somewhat smaller (by 25%) than the observed radius for decreased star formation, but consistent with this value. At the same time, our sample by dwarf galaxies ($M_B > -20$ for $\sim 90\%$ of all objects) with statistical transition line at $M_B = -18.55$, such that the central galaxies are the most luminous as well. These are also redder than the more external ones, with a transition line at $B-R = 1.1$. All of this suggests that our sample consists mainly of dwarf ellipticals (dE). Interestingly, dE are potentially the only galaxy type whose formation is sensitive to global, rather than local, environment (Conselice 2005). In this context it is important to note that we found about 94\% groups have significant elongation throughout the group and the surrounding fields (GA $\geq 2$), and a (negative) linear relation between GA and the fraction of $\eta_1$ galaxies. In the case when these objects are predominantly dEs, we conclude that these galaxies are tracing the anisotropic large-scale accretion of matter onto groups. We also know that the high dwarf-to-giant ratio observed in rich clusters suggests that cluster dE do not form in groups that later merge to build clusters (Conselice 2005). Bright galaxies that follow the Kormendy relation (Kormendy 1977) are indeed unlikely to have been formed by mergers of dwarf early-type systems (Efstathiou et al. 2004). Likewise, our results indicate that a

Fig. 7. Additional trends in our sample with respect the fraction of $\eta_1$ galaxies and to the fraction of galaxies within $R_{200}$. 95\% confidence levels contours are presented as dashed lines.

Fig. 8. 3D plot in [$\sigma$ (km s$^{-1}$), $R_{200}$ (Mpc), $M_{200}$ ($10^{14} M_\odot$)] space. Open circles denote groups with $f_{\eta_1} > 0.55$, while filled circles represent groups with $f_{\eta_1} \leq 0.55$. 
high number of dEs exist in both the groups and the flow of matter along the filamentary structure feeding these systems.

Acknowledgements. We thank the referee for useful suggestions. We also thank A. Baddeley and B. Carvalho for the statistical tips. A. L. B. R. thanks the support of CNPq, Grants 201322/2007-2 and 471254/2008-8. P. A. A. Lopes was supported by the Fundação de Amparo à Pesquisa do Estado de São Paulo (FAPESP, processes 06/04955-1 and 07/04655-0).

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