Metal enrichment of the intra-cluster medium by thermally and cosmic-ray driven galactic winds

An analytical prescription for galactic outflows

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Abstract

Aims. We investigate the efficiency and time-dependence of thermally and cosmic ray driven galactic winds for the metal enrichment of the intra-cluster medium (ICM) using a new analytical approximation for the mass outflow. The spatial distribution of the metals are studied using radial metallicity profiles and 2D metallicity maps of the model clusters as they would be observed by X-ray telescopes like XMM-Newton.

Methods. Analytical approximations for the mass loss by galactic winds driven by thermal and cosmic ray pressure are derived from the Bernoulli equation and implemented in combined N-body/hydrodynamic cosmological simulations with a semi-analytical galaxy formation model. Observable quantities like the mean metallicity, metallicity profiles, and 2D metal maps of the model clusters are derived from the simulations.

Results. We find that galactic winds alone cannot account for the observed metallicity of the ICM. At redshift $z = 0$ the model clusters have metallicities originating from galactic winds which are almost a factor of 10 lower than the observed values. For massive, relaxed clusters we find, as in previous studies, a central drop in the metallicity due to a suppression of the galactic winds by the pressure of the ambient ICM. Combining ram-pressure stripping and galactic winds we find radial metallicity profiles of the model clusters which agree qualitatively with observed profiles. Only in the inner parts of massive clusters the observed profiles are steeper than in the simulations. The slope of the redshift evolution of the mean metallicity in the simulations agrees reasonably well with recent observations.

Key words. galaxies: clusters: general – intergalactic medium – ISM: jets and outflows – methods: numerical

1. Introduction

A well observable consequence of the interaction processes between galaxies and the hot, thin intra-cluster medium (ICM) is the high metal abundance ($\approx 0.3$ in solar units) in the intra-cluster gas. These heavy elements cannot be primordial but must have been mostly processed in stars within galaxies, and transported to the ICM by some interaction processes. Galactic winds were one of the first origins proposed for metal enriched gas found by X-ray observations (De Young 1978). Recently, it has been shown (Everett et al. 2008) that the best model to explain the soft X-ray emission of the Milky Way halo from ROSAT observations is a cosmic ray driven galactic wind. Further mechanisms that can act as enrichment process are ram-pressure stripping (Gunn & Gott 1972), tidal interactions (Gnedin 1998; Kapferer et al. 2005), active galactic nuclei (AGNs) (e.g. Moll et al. 2007), and intra-cluster supernovae (Domainko et al. 2004).

With the first generation of X-ray satellites it was just possible to measure radial metallicity profiles (see e.g. De Grandi et al. 2004; Boehringer et al. 2005; Baldi et al. 2007; Sato et al. 2009). Using the current satellites XMM and CHANDRA also the 2D spatial distribution of the metals became measurable, i.e. metallicity maps (e.g. Schmidt et al. 2002; Furusho et al. 2003; Sanders et al. 2004; Fukazawa et al. 2004; Hayakawa et al. 2004). These maps show clearly a non-uniform and non-spherical distribution of the metals, which agrees with the results of simulations (e.g. Schindler et al. 2005). Recent observations also shed some light on the redshift evolution of the metallicity. Balestra et al. (2007) showed that there is a mild evolution of the Fe content in the ICM with redshift. From observations of 36 clusters they conclude that the average Fe content of the ICM in local clusters is a factor of $\approx 2$ larger than at $z = 1$, even though with a large scatter. Maughan et al. (2007) confirmed this result with a sample of 115 clusters of galaxies in a redshift interval $0.1 < z < 1.3$ observed with Chandra.

Numerical simulations are widely used to investigate the efficiency and time dependence of the various processes. Several groups have simulated one or more of the possible enrichment mechanisms of an isolated galaxy, e.g. ram-pressure stripping (Abadi et al. 1999; Quilis et al. 2000; Tonazzo & Schindler 2001; Schulz & Struck 2001; Vollmer et al. 2001) or galactic winds (e.g. Tenorio-Tagle & Munoz-Tunon 1998; Strickland & Stevens 2000).

On galaxy cluster scales metal enrichment processes are implemented into cosmological simulations to explain the overall
enrichment of the ICM. De Lucia et al. (2004) and Nagashima et al. (2005) use combined semi-analytic techniques and N-body simulations to calculate the overall ICM metallicity. They find that mainly massive galaxies contribute to the enrichment and that there is a mild metal evolution since \( z \approx 1 \) and a stronger evolution for \( z > 1 \). Tornatore et al. (2004, 2007) and Valdarnini (2003) use smoothed particle hydrodynamics (SPH) with detailed yields from type Ia and II supernovae. Cora (2006) also used combined N-body/SPH simulations together with a semi-analytic model. Aguirre et al. (2001) investigated the efficiency of galactic winds at \( z \approx 3 \). They did, however, not calculate the distribution of the metals that arise from the winds. They conclude that there are degeneracies in the results and that other enrichment processes might lead to the same result.

In Kapferer et al. (2007a) we have simulated, for the first time, two enrichment processes (galactic winds and ram-pressure stripping) acting simultaneously. Compared to our previous work (Schindler et al. 2005; Kapferer et al. 2006; Domainko et al. 2006; Moll et al. 2007) this investigation was extended to high redshifts. With this approach a reasonable agreement with observed metallicity profiles was achieved. The wind model adopted in Kapferer et al. (2007a) was, however, a phenomenological one, in which the mass loss scales linearly with the star formation rate of the galaxy. This model does not allow for a deeper insight into the physical processes involved in the outflow and neglects environmental effects such as the possible suppression of galactic winds by high ICM pressure (Schindler et al. 2005). We extend here the work presented in Kapferer et al. (2007a) by introducing a new analytical model for the mass loss due to galactic winds. A major advantage of this implementation of outflows by galactic winds presented in this work compared to the outflow model in Schindler et al. (2005) is the analytical nature of the calculation. Whereas in Schindler et al. (2005) the mass outflow was calculated with an external numerical scheme (Breitschwerdt et al. 1991) individually for each galaxy at each timestep, the scheme presented in this work can be easily implemented on top of semi-analytical models due to its analytical nature.

The paper is organized as follows: in Sect. 2 we present the new analytical model used for this work. In Sect. 3 we present the numerical setup and the implementation of the analytical model. The results are presented and compared to observations in Sect. 4. We end with a summary of the main conclusions in Sect. 5.

### 2. Analytical wind model

An analytical model for galactic winds driven by thermal, cosmic ray, and magnetohydrodynamic (MHD) wave pressure has been presented by Breitschwerdt et al. (1991). To account for the plane-parallel geometry of the outflow near the disc and the spherical geometry at large distances from the disc, Breitschwerdt et al. (1991) use a flux tube geometry, where the area cross section \( A(z) \) varies as

\[
A(z) = A_0 \left[ 1 + \left( \frac{z}{Z_0} \right)^2 \right].
\]

Here \( z \) denotes the height above the plane of the galaxy, \( A_0 \) the area at a reference level typically 1kpc above the plane of the galaxy, and \( Z_0 \) is the height above the galactic plane, at which flux tube divergence becomes significant, taken to be equal to the galactic radius here. In this geometry the conservation of mass and energy of the outflow can be written as

\[
\rho u A = \text{const.}
\]

and

\[
\rho u A \left[ \frac{1}{2} u^2 + \frac{\gamma_g}{\gamma_g - 1} \rho_g + \Phi \right] + \frac{\gamma_c}{\gamma_c - 1} \rho c A (u + v_\lambda) + p_w A (3u + 2v_\lambda) = \text{const.},
\]

where \( \rho \) is the gas mass density and \( u \) the bulk velocity of the gas. \( \gamma_g \) and \( \gamma_c \) denote the adiabatic indices of the thermal plasma and the cosmic rays, respectively. We assume a non-relativistic monatomic gas, i.e. \( \gamma_g = 5/3 \), while for the cosmic rays we chose the ultra-relativistic case, i.e. \( \gamma_c = 4/3 \). \( p_g \), \( p_c \), and \( p_w \) refer to the pressure of the gas, the cosmic rays, and the MHD waves, respectively. The cosmic ray pressure is obtained by taking the appropriate moment of the particle distribution function. Pressure gradients can be calculated in a hydrodynamic approximation using dynamical equations presented in Breitschwerdt et al. (1991). Finally, \( v_\lambda \) refers to the Alfvén velocity.

Using Eq. (3), the Bernoulli equation, we derive an analytical approximation for the mass loss due to thermally driven winds.

With the continuity equation Eq. (2) and the assumptions \( p_c \ll p_g \) and \( p_w \ll p_g \), Eq. (3) simplifies to

\[
\frac{1}{2} u_0^2 + \frac{\gamma_g}{\gamma_g - 1} \rho_0 + \Phi_0 = \frac{1}{2} u_\infty^2 + \frac{\gamma_g}{\gamma_g - 1} \rho_\infty + \Phi_\infty,
\]

where the subscripts 0 refer to the quantities at the reference level, taken to be at \( z = 1 \) kpc. While the subscripts \( \infty \) corresponds to the values of the unbound outflow at large distances, i.e. \( z \to \infty \). For large \( z \) the gravitational potential and the gas pressure tends towards zero. With these approximations we can further simplify Eq. (4) to

\[
\frac{1}{2} u_0^2 + \frac{\gamma_g}{\gamma_g - 1} \rho_0 + \Phi_0 = \frac{1}{2} u_\infty^2.
\]

Here we have also used \( \gamma_g = 5/3 \). Equation (5) holds if \( c_\infty \ll u_\infty \), which is always fulfilled for high Mach number winds. It is now possible to solve for the initial outflow velocity \( u_0 \):

\[
u_0 = \sqrt{\frac{2}{\gamma_g} + \frac{v_{esc}^2}{\gamma} - \frac{5}{\gamma} \frac{c_\infty^2}{v_{esc}^2}},
\]

where we inserted the relation

\[
c^2 = \frac{\gamma P}{\rho}
\]

for the sound speed \( c \) and the definition of the escape velocity \( v_{esc} = \sqrt{2\Phi_0} \). The local mass loss rate per unit area associated with an outflow with an initial velocity \( u_0 \) given by Eq. (6) is then

\[
m = \rho_0 u_0.
\]

The total mass loss of a galaxy due to galactic winds can be found by integrating Eq. (2) over the galactic disc or the area over which mass loss occurs, i.e.

\[
M = 2 \times 2\pi \times \int_0^{R_{\text{gal}}} \rho_0(r) u_0(r) dr,
\]

where \( R_{\text{gal}} \) is the star formation radius of the galaxy.
In the same way Breitschwerdt et al. (1991) derived an analytical approximation for the mass loss due to cosmic ray driven winds, i.e. the case where \( p_g \ll p_c \) and \( p_w \ll p_c \), which reads
\[
m = \frac{2 F_{\odot}}{v_{\text{esc}} A_{\text{gal}}},
\]
where \( F_{\odot} \) denotes the spatially averaged energy flux density of the cosmic rays and \( A_{\text{gal}} \) is the surface area of the galactic disc. This model is ideally suited for high resolution \( N \)-body/hydrodynamic simulations, in which the galaxies and the inter-stellar medium (ISM) are spatially resolved. Most quantities in Eq. (6) would be known directly from the simulations and the initial outflow velocity \( v_0 \) could be directly measured in such simulations. Our setup, however, does not allow such a procedure, as we do not have the internal velocity field of the ISM near the reference level. Therefore, in the following, we have to rely on several assumptions about the thermodynamic properties of the ejected gas, i.e. its temperature and density. These uncertainties have to be kept in mind when interpreting the presented results.

3. Simulations

We implement the prescription of galactic wind mass loss given by Eq. (2) into the setup described in Kapferer et al. (2007a) which was improved with respect to the setup used in Schindler et al. (2005), Kapferer et al. (2006) and Domainko et al. (2006) by the use of comoving coordinates in the hydrodynamic code. In this setup we use different code modules to calculate the main components of a galaxy cluster in the framework of a standard \( \Lambda \)CDM cosmology, i.e. using \( \Omega_m = 0.3, \Omega_\Lambda = 0.7, h = 0.7, s_{\odot} = 0.93, \) and \( \Omega_b = 0.02 h^2 \). In the following subsections we will detail these code modules and their interplay.

3.1. Dark Matter and galaxy formation models

The non-baryonic dark matter (DM) component is calculated using GADGET2 (Springel 2005) with constrained random field initial conditions (Hoffman & Ribak 1991; implemented by van de Weygaert & Bertschinger 1996). From the DM distribution we calculate at each time step the underlying gravitational potential for the hydrodynamic code by solving the Poisson equation. Additionally we can calculate the dynamically fully described orbits and the merger tree of galaxy haloes from the DM distribution.

The properties of the galaxies are calculated by an improved version (van Kampen et al. 2005) of the galaxy formation code of van Kampen et al. (1999) which is a semi-analytic model in the sense that the merging history of galaxy haloes is taken directly from the cosmological \( N \)-body simulation. Halo mergers are identified in the \( N \)-body simulations as events in which a new halo is formed that is both virialised and contains at least two progenitors. Gas that cools within virialised haloes is assumed to settle in a disc with an exponential profile. To set the disk-scale length we use the model of Mo et al. (1998), with the distinction that we measure the angular momentum of the dark halo from the \( N \)-body simulation data instead of assuming an analytical model for it. Gas-rich galaxies undergo a burst of star formation during a halo merger event. Galaxy-galaxy mergers are treated in a different way: all galaxies within a dark matter halo or subhalo suffer from dynamical friction, and will merge with the central galaxy eventually, triggering a starburst as well. This starburst uses up most of the cold gas left in the satellite, however not all is turned into stars due to supernovae feedback, which heats the surrounding gas. Stars which are formed during halo merger events and galaxy-galaxy mergers contribute to the stellar mass of the bulge. In between merger events star formation is quiescent in discs with a threshold according to the Kennicutt criterion (Kennicutt 1998). Stellar evolution is modelled using the stellar population synthesis models of Bruzual & Charlot (2003). A fraction of the metals formed in stars is ejected by supernovae and stellar winds into the surrounding inter-stellar medium (ISM). The metals that end up in the hot gas component also affect the metallicity dependent cooling rates (Sutherland & Dopita 1993). Yields are taken from the metallicity evolution model of Matteucci & Francois (1989), in a manner as described in van Kampen et al. (1999), which includes SN types I and II. The evolution of the metallicity is followed for the stellar populations as well as for the cold and hot gas reservoirs, and exchanges are tracked as well. Material returned to the cold ISM by stellar winds and supernovae has been chemically enriched by the nuclear processes inside the stars.

3.2. Hydrodynamics

For the treatment of the ICM we use comoving Eulerian hydrodynamic parts with shock capturing scheme (PPM, Collela & Woodward 1984), with a fixed mesh refinement (Ruffert 1992) on four levels and radiative cooling (Sutherland & Dopita 1993). For the initial conditions of the hydrodynamic simulation we distribute the gas as the dark matter in a Gaussian random field at \( z = 40 \). The largest of the four nested grids covers a comoving volume of (20 Mpc)\(^3\). Each finer grid covers \( \frac{1}{4} \) of the volume of the next larger grid. Using a resolution of 128\(^3\) grid cells on each grid we obtain a finest spacing of \( \sim 19.5 \) kpc comoving for each cell on the innermost grid. The \( N \)-body and hydrodynamic code are calculated starting at \( z = 40 \), while the semi-analytic galaxy formation model covers the redshift interval from \( z = 20 \) to \( z = 0 \).

3.3. The model galaxy clusters

With this numerical setup we model a sample of merging systems, from which we draw a non-cooling flow cluster which is a lower mass cluster with several strong sub-cluster mergers. We will name this model cluster hereafter “model cluster A”. The second model cluster we use for this analysis is a more massive merging system with about twice the mass of model cluster A and several minor merger events. This model cluster will be referred to as “model cluster B”. These model clusters were also used in Kapferer et al. (2007a), with respect to the initial conditions of the dark matter and the baryonic matter. Main improvements were done regarding the semi-analytical galaxy formation model. One improvement is the change of the IMF, where we now use the IMF proposed by Chabrier (2003). This produces better fits to the luminosity function without large changes to the star formation history. Other improvements include adopting a 40% shorter galaxy merger rate timescale, and a different ratio for the distinction between minor and major mergers, which is now 0.3. In the previous model the metallicity of the cold gas in the disc galaxies was higher, therefore the stripping leads to higher metallicities in the ICM. To constrain the model parameters for the semi-analytical model which is applied, we made sure to reproduce the Tully-Fisher relation and the global star formation history. The luminosity functions in the B-band (star forming galaxies) and the K-band (passively evolving galaxies)
are in good agreement around $L_*$ in both bands, but overpredict abundances at the bright end. This problem is usually fixed by implementing an AGN feedback recipe, which the model used for this work does not include. For completeness we summarise here the main properties of the two model clusters as described in Kapferer et al. (2007a).

- Model Cluster A: the cluster starts to form at $z \sim 1.5$ and has two major merger events at $z = 0.8$ and $z = 0.5$. The total mass at $z = 0$ is $1.5 \times 10^{14} M_\odot$ in a sphere with 1 Mpc radius.
- Model Cluster B: the formation redshift for this cluster is $z \sim 1.7$. Four minor merger events appear at $z = 1.4, z = 1.1, z = 0.5$ and $z = 0.3$. The cluster has a final mass of $3.4 \times 10^{14} M_\odot$ within a sphere of 1 Mpc radius.

3.4. Implementation of the analytical wind model into the numerical setup

The semi-analytic galaxy formation model limits the applicability of Eq. (6), because it does not give spatially resolved information about the star formation. Instead it gives a global value for the disc. Density and temperature distributions are also unknown. Therefore, to make use of Eq. (6) in our numerical setup, we have to rely on several assumptions. To calculate the gravitational potential and its escape velocity, we assume for the dark matter halo a Hernquist (1990) potential:

$$\Phi_{\text{DM}}(r) = -\frac{GM_{\text{DM}}}{r+a}, \quad (11)$$

where $a$ is a scale length and $M_{\text{DM}}$ the total mass of the dark matter halo. The density profile associated with this potential via the Poisson equation reads

$$\rho_{\text{DM}}(r) = \frac{M_{\text{DM}}}{2\pi} \frac{a}{r(r+a)^3}. \quad (12)$$

For the potential of the disc we use a Toomre (1963) model (first derived by Kuzmin 1956), which is given by

$$\Phi_{\text{disc}}(r,z) = -\frac{GM_{\text{disc}}}{(r^2 + (b + |z|)^2)^{1/2}}. \quad (13)$$

where $r$ and $z$ denote the cylindrical coordinates and $b$ is a non-zero scale length. The potential at a certain radius can then be directly calculated from Eqs. (11) and (13), using the total mass of the disc and of the dark matter halo. The scale length $a$ in Eq. (11) follows from the disc scale length of an exponential disc $r_d$ as $a = r_d/(1 + \sqrt{2})$ (Hernquist 1990).

The terminal velocity of the outflow $u_{\text{esc}}$ is also known, so we assume $u_{\text{esc}} = v_{\text{esc}}$. Breitschwerdt et al. (1991) have shown that the terminal velocity of the wind $u_{\text{esc}}$ and the escape velocity of the system $v_{\text{esc}}$ differ typically by not more than a factor of two. We have tested the consequences of this uncertainty by using $u_{\text{esc}} = v_{\text{esc}}/2$ and $u_{\text{esc}} = 2v_{\text{esc}}$, respectively. We found that quantitatively the resulting absolute metallicity values change up to a factor of three. The resulting metal distribution (radial profiles and 2D metal maps) and the redshift evolution of the metallicity, however, are only marginally affected. Given all the uncertainties in the simulation setup, e.g. within the semi-analytical galaxy formation model, this uncertainty appears acceptable.

To derive the sound speed we would require a pressure and density distribution through the gaseous disc, which is not available from the semi-analytical model. Therefore, we follow the argumentation line of Breitschwerdt et al. (1991), who estimated that for a Milky-Way type galaxy with a supernova rate of once every 30 years the time averaged halo filling factor is of order unity. Therefore the pressure support for a flux tube should be, on average, maintained. We couple the supernova rate to the star formation rate (SFR) via the assumption of a Salpeter initial mass function (IMF) with a slope of $-1.35$ in the range of $0.1 M_\odot$ and $40 M_\odot$. A model galaxy is hence having a galactic wind driven purely by thermal pressure if the SFR exceeds a certain threshold, for which we adopt here a value of $4 M_\odot/yr$. Below this SFR the galaxy can still have a cosmic ray driven wind, for which we calculate the mass loss using Eq. (10). As in Breitschwerdt et al. (1991) we then assume that the flux tubes are homogeneously distributed over the galactic disc. This obvious oversimplification is necessary, as we have no information on the location of the supernovae from the semi-analytical model. We set the temperature and the density at the reference level to $1 \times 10^7$ K and $1 \times 10^{-26}$ g/cm$^3$, respectively. These are typical values for gas fed into a galactic wind (e.g. Breitschwerdt et al. 1991). For an outflow to occur we furthermore demand that the pressure of the outflow exceeds the pressure of the surrounding ICM.

4. Results

In the following we investigate the efficiency and the time dependency of galactic winds as enrichment process. In order to compare our results to observed quantities we will present mean metallicities, metallicity profiles, and 2D metal maps of our model clusters. In addition we compare the efficiency of the proposed wind model with ram-pressure stripping as source of metals in the ICM. Metals originating from galaxies, either from galactic winds or ram-pressure stripping, are advected and mixed with the hydrodynamic solution of the ICM for each timestep in the simulation.

4.1. Metallicity profiles

The most basic measure to quantify the metal distribution in the ICM is its mean metallicity, obtained from emission weighted metallicity maps. We assume that the X-ray measurements extend to a radius of 1 Mpc and that only galactic winds are acting. Within this volume, the mean metallicity in solar units (Grebesh & Sauerl 1998) is 0.02 and 0.04 at $z = 0$ for model cluster A and B, respectively. For both model clusters this value is significantly lower than observed metallicities in real clusters. More information on the metal distribution is given by radial metallicity profiles, especially by their slope. The normalisation of the profile depends strongly on the uncertain ISM metallicity, present in semi-analytic simulations. In Fig. 1 we present the metallicity profile of model cluster A and B at redshift $z = 0$. Note that for these profiles only metals originating from galactic winds are taken into account. The metal profiles are obtained from X-ray weighted metal maps (see Kapferer et al. 2007b). For model cluster A the metallicity is almost constant up to a radius of $\sim 300$ kpc. Beyond $\sim 500$ kpc the profile decreases constantly. Model cluster B is more massive than model cluster A and, as a result of a prominent infall region, the metallicity at a radius of 1 Mpc is with $0.03$ solar units higher than in cluster A. A striking feature of the profile is the decreasing metallicity towards the centre of the cluster. This behaviour is different from model cluster A. Galactic winds are suppressed by the high central pressure of the ambient medium, a phenomenon which was already discussed by Schindler et al. (2005) for quiet (i.e. mainly cosmic-ray driven) galactic winds.
Fig. 1. Radial metallicity profile of model cluster A and B at redshift $z = 0$. For the shown metallicity profiles only metals originating from galactic winds are taken into account.

Fig. 2. Metallicity profiles for observed nearby ($z < 0.2$) clusters (symbols) from Pratt et al. (2007) compared to emission weighted simulated profiles from model cluster A at redshift $z = 0$ with galactic winds (red, solid line) and with combined wind and ram-pressure stripping (red, dashed line) as enrichment processes.

Finally, we compare the simulated metallicity profiles to observed profiles from Pratt et al. (2007) in Fig. 2. Using only galactic winds as enrichment process (red, solid line), the radial metallicity profile of model cluster A lies at all radii significantly below the observed profiles. The slope agrees reasonably well with the observed values. This result indicates, that additional processes are acting in clusters, presumably ram-pressure stripping and/or AGNs. We calculate the combined effect of galactic winds and ram-pressure stripping and present the result in Fig. 2 (red, dashed line). Ram-pressure stripping was modelled using a Gunn & Gott (1972) criterion, as described in Kapferer et al. (2007a). The profile agrees then reasonably well at most radii. In the very centre (the inner 50 kpc), where our resolution is not sufficient, a central AGN might still be responsible for the observed steepening there. In the very outer parts of the cluster the simulated metallicity profile lies below the observed values.

We carried out the same analysis for model cluster B. However, as this model cluster is mostly relaxed at redshift $z = 0$, it is not reasonable to compare it to the set of merging clusters from Pratt et al. (2007). Therefore we use the mean of cool-core clusters presented in De Grandi et al. (2004) for comparison. The result is shown in Fig. 3. Again, with wind as the only enrichment process, neither the slope nor the absolute values agree with the observations, especially in the inner parts of the cluster. Combining winds and ram-pressure stripping leads to reasonable agreement in the slope of the profiles for radii $r \geq 120$ kpc. At smaller radii, however, the mean observed profile is steeper than our simulated cluster profile. This might be a selection effect, as we show only a snapshot of one specific model cluster. It may also indicate, however, that we miss an enrichment process acting in the centre of massive, relaxed clusters (e.g. enrichment by a central AGN).

In the case of the massive galaxy cluster the difference between the phenomenological model for galactic outflow in Kapferer et al. (2007a) and the present work is more striking. In the phenomenological wind model the contribution to the enrichment of the ICM is up to a factor of ten more efficient compared to the wind model presented in this work. The analytical wind model introduced in this work gives much less metallicities compared to the outflow model which scales the outflow linearly with the galaxies’ star formation rate. The strong mismatch between the reproduction of the observed metallicity profiles in the case of the massive system B leads to the conclusion that additional sources for metal enrichment in massive galaxy clusters play an important role. In addition the amount of metals originating from ram-pressure stripping is much lower compared to Kapferer et al. (2007a). The explanation lies in the improved semi-analytical model, see Sect. 3.3. The investigation of the metal enrichment through AGNs will be part of an upcoming work.

We note once more, that the absolute values of the profile depend strongly on the adopted parameters of the semi-analytic galaxy formation model and the parameters of the wind model.
The slope of the simulated profile, on the contrary, is robust against reasonable changes of the parameters.

Similar studies have been performed by other groups. Tornatore et al. (2007), for example, used an N-body/SPH code. They found generally good agreement of the metallicity profiles with observations. The same is true for Cora (2006), whereas they apply a semianalytical model in their work. Their adopted wind model might, however, overestimate the mass loss caused by galactic winds (see Sect. 4.3).

In Fig. 4 we present the redshift evolution of the mean metallicity of the two model clusters and compare them with the observed evolution of a sample of clusters from Balestra et al. (2007). Both enrichment processes (ram-pressure stripping and galactic winds) are taken into account. For both clusters the evolution agrees with the observational trend but the absolute values are lower than expected from observations. This is especially true at lower redshift ($z < 0.5$), where the enrichment processes do not seem to be efficient enough. In the observational sample of Balestra et al. (2007) the extraction radius varied roughly from 200–1000 kpc, depending on the signal-to-noise ratio. We assumed a constant extraction radius of 600 kpc, which we also use for comparison of the metallicity profiles with observations. A variation of this radius does not change the general trend significantly. Note that 1 Mpc corresponds roughly to the virial radius of the two galaxy clusters at $z = 0$.

### 4.2. X-ray weighted maps

With modern X-ray space telescopes it is feasible to study also the 2D metal distribution. It was found that the metals are not homogeneously distributed within the ICM (e.g. Sanders et al. 2004; Durret et al. 2005; O’Sullivan et al. 2005; Sauvageot et al. 2005; Werner et al. Werner; Sanders & Fabian 2006; Hayakawa et al. 2006; Finoguenov et al. 2006; Bagchi et al. 2006). In Fig. 5 we present such an X-ray weighted metal map for model cluster A at redshift $z = 0$. The X-ray surface brightness map is overlayed as contours and shows the overall ICM distribution. A filament along which galaxies fall into the cluster is visible at the bottom left. As the ICM density in the filament is relatively low ($\sim 7 \times 10^{-29}$ g/cm$^3$ compared to $\sim 7 \times 10^{-27}$ g/cm$^3$ in the centre), it can be more easily enriched there (i.e. a higher metal mass fraction is achieved). In the centre of the cluster the metallicity is slightly lower.

In Fig. 6 we present the X-ray weighted metal map for model cluster B at redshift $z = 0$. The X-ray surface brightness map is again overlayed as contours and shows the overall ICM distribution. The suppression of the galactic winds in the centre of the cluster, as discussed in Sect. 4.1, is clearly visible. In the left and upper-right parts of the cluster the outflows of galaxies, falling into the cluster along a filament, cause a complex metallicity pattern with several maxima.
5. Summary and conclusions

We have investigated the efficiency and time-dependence of thermally and cosmic-ray driven galactic winds for the metal enrichment of the intra-cluster medium (ICM) by a combination of a new analytical model and cosmological hydrodynamic simulations. The analytical approximations for the mass loss by galactic winds driven by thermal and cosmic-ray pressure were derived from the Bernoulli equation. We extend in this work the previous model presented in Kapferer et al. (2007a) by introducing a new analytical model for the mass loss due to galactic winds. This new model does allow a deeper insight into the physical processes involved in the outflow and addresses environmental effects such as the possible suppression of galactic winds by high ICM pressure (Schindler et al. 2005). It is still simple enough to be readily implemented in metal enrichment and semi-analytic galaxy formation models. We simulated the enrichment processes for a galaxy cluster with major merger events (cluster A) and a less merging system (cluster B). Investigating observable quantities, we found that:

- Galactic winds alone cannot account for the observed mean metallicity of the ICM. At redshift \( z = 0 \) the model clusters have mean metalicities, which are almost a factor of 10 lower than observed values. Within a radius of 1 Mpc model cluster A has a mean metallicity of 0.02 and model cluster B a metallicity of 0.04 in solar units.

- A central drop in the metallicity of the relatively relaxed model cluster B is due to a suppression of steady state galactic winds by the pressure of the ambient ICM. In the merging model cluster A, no decrease of the metallicity towards the centre is observable.

- 2D metallicity maps reveal important additional information on the metal distribution, e.g. infalling groups from filaments and inhomogeneities.

- Combining ram-pressure stripping and galactic winds we find radial metallicity profiles of the model clusters which agree in their slopes with observations. In the inner parts of massive clusters the observed profile is steeper than in the simulations.

- The slope of the redshift evolution of the mean metallicity in the simulations agrees reasonably well with recent observations of Balestra et al. (2007).

5.1. What additional processes do enrich the ICM

Ram-pressure stripping and galactic winds, as modelled in this work, are not able to account for the observed metallicities in the ICM. Therefore additional processes need to be taken into account. An important source of enriched matter in the central part of galaxy clusters would be an AGN in a massive central cluster galaxy. The injection of buoyant bubbles in the ICM transports enriched matter from the central cluster galaxy to the surrounding ICM (Roediger et al. 2007). Simionescu et al. (2009) find that 15% of the total amount of Fe in the inner region of the galaxy cluster Hydra A belongs to gas, which is uplifted by buoyant bubbles from the central AGN. This effect would be stronger in relaxed, more massive systems, as the stratification of the ICM is not strongly disturbed by mergers and therefore the bubbles can survive longer.

Ram-pressure stripping, as it is able to trigger star formation in the gaseous wake of stripped galaxies, can enrich the ICM in situ (Kronberger et al. 2008; Kapferer et al. 2008; Kapferer et al. 2009). In the case of strong ram pressures stripping nearly all new stars are formed in the wake of the stripped galaxies. Their influence on the overall metal enrichment is yet unknown, but first simulations of ram-pressure stripping including recipes for star formation point towards the picture that off disc star formation due to ram-pressure stripping is very efficient as an enrichment process of the ICM. Also Intra-cluster stellar populations can enrich the ICM very efficiently as shown in Sivanandam et al. (2009).

Galaxy-galaxy interaction is able to enrich the surroundings by redistributing the ISM kinematically in large volumes around the interacting galaxies (Kapferer et al. 2005). In the model of galactic winds, described in this work, the effect of mergers on the star formation are taken into account, which lead to stronger outflows in the galactic winds. Nevertheless the redistribution of the ISM is not modelled within the presented simulations. The heating of the kinematically redistributed ISM, so that it can contribute to the observed X-ray flux, is not well understood. Hence conclusions on the contribution to the overall enrichment of the ICM due to galaxy interactions have to be investigated in detail.

In a recent paper Fabjan et al. (2008) studied the redshift evolution of the metal content of the ICM with N-body/SPH simulations combined with a detailed model of chemical evolution. They found good agreement with observations for a Salpeter initial mass function. They have shown that gasdynamical processes which redistribute metals, like the sinking of low entropy enriched gas to the central cluster regions, is an additional process that helps explain the increase of the observed emission-weighted metallicity of the ICM at low \( z \). These results also confirm those found by Cora et al. (2008) which were obtained by using a combination of N-body/SPH simulations with an analytic model of galaxy formation.

Concluding, the effects of AGN, ram-pressure stripping induced off-disc star formation and direct enrichment by galaxy-galaxy interactions will be investigated in upcoming works, with the aim to obtain a more complete picture of the relative strength of the enrichment processes in galaxy clusters and the influence on the evolution of the galaxies.

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