

The correlated optical and radio variability of BL Lacertae

WEBT data analysis 1994–2005*

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ABSTRACT

Context. Since 1997, BL Lacertae has undergone a phase of high optical activity, with the occurrence of several prominent outbursts. Starting from 1999, the Whole Earth Blazar Telescope (WEBT) consortium has organized various multifrequency campaigns on this blazar, collecting tens of thousands of data points. One of the main issues in the study of this huge dataset has been the search for correlations between the optical and radio flux variations, and for possible periodicities in the light curves. The analysis of the data assembled during the first four campaigns (comprising also archival data to cover the period 1968–2003) revealed a fair optical-radio correlation in 1994–2003, with a delay of the hard radio events of ~100 days. Moreover, various statistical methods suggested the existence of a radio periodicity of ~8 years.

Aims. In 2004 the WEBT started a new campaign to extend the dataset to the most recent observing seasons, in order to possibly confirm and better understand the previous results.

Methods. In this campaign we have collected and assembled about 11 000 new optical observations from twenty telescopes, plus near-IR and radio data at various frequencies. Here, we perform a correlation analysis on the long-term *R*-band and radio light curves.

Results. In general, we confirm the ~100-day delay of the hard radio events with respect to the optical ones, even if longer (~200–300 days) time lags are also found in particular periods. The radio quasi-periodicity is confirmed too, but the “period” seems to progressively lengthen from 7.4 to 9.3 years in the last three cycles. The optical and radio behaviour in the last forty years suggests a scenario where geometric effects play a major role. In particular, the alternation of enhanced and suppressed optical activity (accompanied by hard and soft radio events, respectively) can be explained in terms of an emitting plasma flowing along a rotating helical path in a curved jet.

Key words. galaxies: active – galaxies: BL Lacertae objects: general – galaxies: BL Lacertae objects: individual: BL Lacertae – galaxies: jets – galaxies: quasars: general

1. Introduction

BL Lacertae ($z = 0.0688 \pm 0.0002$; Miller & Hawley 1977) is the prototype of a class of active galactic nuclei (AGNs), the BL Lac objects, which are well known for their pronounced variability at all wavelengths, from the radio to the γ -ray band (see e.g. Villata et al. 2002, for an extended description of this object). It has been one of the favourite targets of the Whole Earth Blazar Telescope (WEBT)¹, which has organized several multifrequency campaigns on this source. Two short campaigns took place in 1999, in conjunction with observations of the X-ray satellites ASCA and BeppoSAX (Ravasio et al. 2002). The campaign carried out in May 2000 – January 2001 was particularly successful, with periods of exceptionally dense sampling that allowed Villata et al. (2002) to follow the intranight flux variations in detail. The optical spectrum was found to be weakly

sensitive to the long-term brightness trend, but to strictly follow the short-term flux variations, becoming bluer when brighter. The authors suggested that the essentially achromatic modulation of the flux base level on long time scales is due to a variation of the relativistic Doppler beaming factor, and that this variation is likely due to a change of the viewing angle. In contrast, the strongly chromatic fast variability may be the result of intrinsic energetic processes. The data of this WEBT campaign on BL Lac were compared to the X-ray data taken in the same period by BeppoSAX and RXTE by Böttcher et al. (2003), who found some hint of correlation.

A subsequent campaign was carried out in 2001–2003. On that occasion, historical optical and radio light curves were reconstructed back to 1968, and both colour and time series analyses were performed. Colour analysis on a longer time period confirmed the conclusions by Villata et al. (2002), and allowed Villata et al. (2004b) to quantify the degree of chromatism of both the short-term and long-term variability components. The optical spectral behaviour was further analysed by Papadakis et al. (2007), who interpreted the bluer-when-brighter mild

* The radio-to-optical data presented in this paper are stored in the WEBT archive; for questions regarding their availability, please contact the WEBT President Massimo Villata.

¹ <http://www.oato.inaf.it/blazars/webt/>

chromatism of the long-term variations in terms of Doppler factor variations due to changes in the viewing angle of a curved and inhomogeneous jet.

The time series analysis performed by Villata et al. (2004a) showed that the main radio outbursts repeat every ~ 8 years (see also Ciaramella et al. 2004), with a possible progressive stretching of the period. Moreover, when considering the best-sampled time interval 1994–2003, the optical light curve was found to correlate with the radio hardness ratios, with a radio time delay of about 100 days. Thus, Villata et al. (2004a) proposed a scenario where the variability mechanism propagates downstream in the jet, crossing less and less opaque regions. In the inner regions it produces connected optical and hard radio events, while in outer zones it gives rise to softer events that are apparently uncorrelated with the former ones. The WEBT light curves were then used by Bach et al. (2006) for a comparison with the time evolution of the VLBI core and jet structure on parsec and sub-parsec scales. The authors showed that sometimes prominent jet features can become as bright as, or even brighter than, the core, which complicates the cross-correlation analysis between the radio light curves and those at other frequencies. However, they found that the radio hardness ratios derived from the WEBT light curves can trace the variability of the VLBI core. Their analysis then confirmed the optical-radio time lags of Villata et al. (2004a). Jet bending was invoked to explain both the modest optical variability in the period 1981–1996 with suppressed radio-optical correlation, and the low-emission region in the jet around 1 mas from the core.

In this paper we present optical (*R* band) and radio data taken during the WEBT campaign covering the 2002–2005 period². Their addition to the historical light curves allows us to further investigate both the radio quasi-periodicity and the correlation between optical flux and radio hardness ratio found by Villata et al. (2004a).

A new campaign on BL Lacertae was organized by the WEBT in the 2007–2008 observing season, including three pointings by the XMM-Newton satellite as well as spectroscopic observations with the Telescopio Nazionale Galileo (TNG). The results of this further WEBT effort on BL Lac will be presented elsewhere (Raiteri et al., in preparation).

2. Observations and results

During the 2002–2005 WEBT campaign, we assembled about 11 000 observations in the optical *UBVRI* bands from 16 observatories (20 telescopes); in order of longitude they are: Yunnan, Mt. Maidanak, Abastumani, Crimean, Tuorla, MonteBoo, Armenzano, Perugia, Torino, Sabadell, Bordeaux, Roque de los Muchachos (KVA, Liverpool, NOT, and TNG), Boltwood, Capilla Peak, Lowell (Hall and Perkins), and Kitt Peak (SARA). *JHK* data were collected from 3 observatories: Campo Imperatore, TIRGO, and Roque de los Muchachos (NOT). Radio observations were carried out between 1 and 43 GHz at: SAO RAS (RATAN-600)³, Metsähovi⁴, Noto, Medicina⁵, MDSCC (PARTNeR), and UMRAO. Optical and near-IR data were processed as explained in Villata et al. (2002). Radio data were

collected as already calibrated flux densities and complemented by data from the VLA/VLBA Polarization Calibration Database⁶.

The top panel of Fig. 1 shows the optical *R*-band flux-density light curve starting from 1994 (12 418 data points). It was built with data collected by the WEBT in five campaigns (blue dots), including the 2002–2005 one, as well as with literature data⁷ (red dots). The flux densities have been corrected for the Galactic extinction and the host galaxy contribution has been subtracted according to Villata et al. (2002, see also Villata et al. 2004b). Radio light curves at 22, 14.5, and 5 GHz are shown in the following three panels, together with cubic spline interpolations through the 30-day binned data. These splines are reported in the last two panels, to compare the 22 and 14.5 GHz variations to the 5 GHz ones. Following Villata et al. (2004a), we define the hardness ratio H_{22} as the ratio between the 22 and 5 GHz flux densities. Analogously, H_{14} is the ratio between the 14.5 and 5 GHz flux densities. The events where these hardness ratios are greater than 1 are highlighted in yellow and called “hard” events. “Soft” events are characterized by higher flux densities at lower frequencies.

After a period of moderate activity (1981–1996; see Fig. 1 in Villata et al. 2004a), from 1997 the source has shown several prominent outbursts in the optical band. In contrast, the radio activity in the last 25 years does not present a corresponding change of behaviour. In particular, the major radio outburst of 1995–1996 occurred during a “quiescent” optical phase, and it was stronger at longer wavelengths. In the following years the reverse was observed, with outbursts appearing enhanced at the higher radio frequencies. This behaviour led Villata et al. (2004a) to distinguish the soft radio events, with no optical counterpart, from the hard events, which are correlated with the optical outbursts. Indeed, a cross-correlation analysis with the discrete correlation function (DCF, see Edelson & Krolik 1988; Hufnagel & Bregman 1992; Peterson et al. 1998) method yielded a fair correlation (DCF ~ 0.5) between the optical fluxes and H_{22} , with a time delay of about 100 days.

One of the main purposes of the new WEBT campaign in 2002–2005 was to check if this result would have been confirmed by the data of the new period. In the top panel of Fig. 1 the solid line represents the average between H_{22} and H_{14} , H_{mean} , shifted in time by -100 days and properly scaled. It allows us to recognize that most optical outbursts have their counterpart in the H_{mean} curve, but with a less clear correspondence in the period ~ 2002 – 2004.5 . When cross-correlating the optical light curve with H_{mean} , we obtain a result (green dots in Fig. 2) very similar to that of Villata et al. (2004a), with the DCF peak at ~ 100 days slightly enhanced (~ 0.55), and a secondary peak at about 200 days now more pronounced. Hence, it seems that the hard radio events can lag behind the optical ones with two different time delays. To see whether a change of behaviour occurred at some stage, we divided the optical light curve in two periods. The first period runs from 1994 to 2005, with the exclusion of the time interval where we noticed a lack of correspondence between optical and radio events, i.e. JD = 2 452 150–2 453 200 (~ 2001.7 – 2004.5), which represents the second period. The blue filled circles in Fig. 2 show the DCF between the optical data in the first period and H_{mean} . The peak at ~ 100 days appears strongly enhanced (≥ 0.7), while the second one is essentially

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³ See e.g. Korolkov & Parijskij (1979); Kovalev et al. (1999).

⁴ See e.g. Teräsranta et al. (2005) and references therein.

⁵ See e.g. Bach et al. (2007).

⁶ <http://www.vla.nrao.edu/astro/calib/polar/>

⁷ Besides the papers already cited in Villata et al. (2004b), literature data were taken from Hagen-Thorn et al. (2004), Zhang et al. (2004), and Gu et al. (2006).

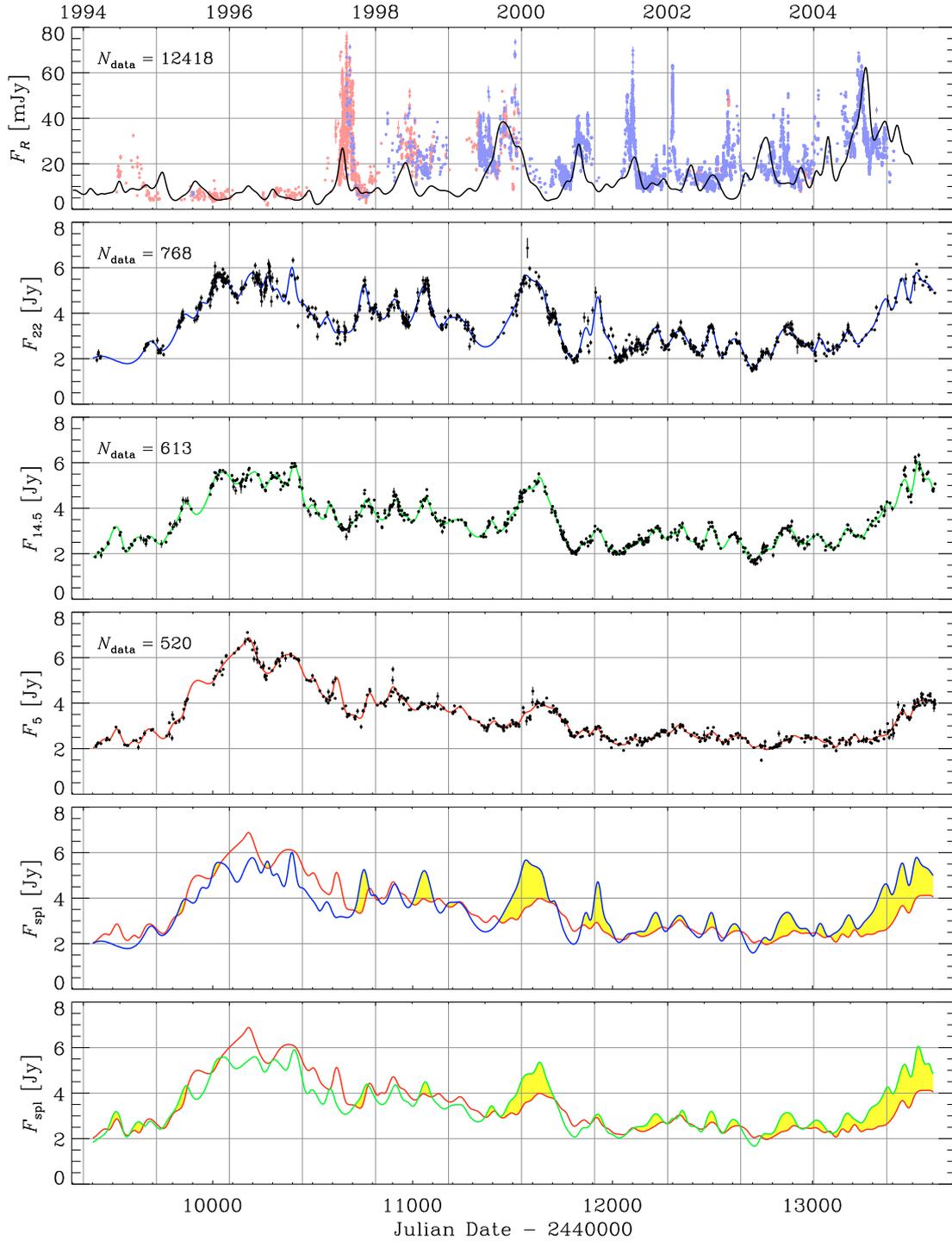


Fig. 1. *R*-band flux-density light curve (top, mJy) and radio light curves (Jy) at 22, 14.5, and 5 GHz with their cubic spline interpolations under-plotted; grey horizontal and vertical lines have been drawn to guide the eye through the flux variations; the fifth and sixth panels show the 22 GHz (blue line) and the 14.5 GHz (green line) splines compared to the 5 GHz (red) one; the regions where the higher-frequency spline exceeds the lower-frequency one have been highlighted in yellow. In the top panel the solid line represents the average between H_{22} and H_{14} , H_{mean} , raised to 3.5, multiplied by 10, and shifted in time by -100 days, for an easier comparison with the optical light curve.

unchanged. On the other hand, the red empty circles show the radio delays in the second period: the main peaks are now at about 200 and 300 days. Thus, the hard radio outbursts seem to lag behind the optical ones by about 100 days in 1997–2001 with a possible lengthening to ~ 200 days, while later the delay appears to increase in the range 200–300 days, until it comes back to the original value in 2004–2005.

Another issue to be investigated is the quasi-periodicity (~ 8 years) of the main radio outbursts, particularly evident in the longer-wavelength light curves (see Villata et al. 2004a). This result is based on the presence of three events peaking around 1980, 1988, and 1996. Moreover, Villata et al. (2004a) also noticed a possible stretching of the period: the separation between the first two outbursts is noticeably less than 8 years, and the following time interval is slightly longer than 8 years. The

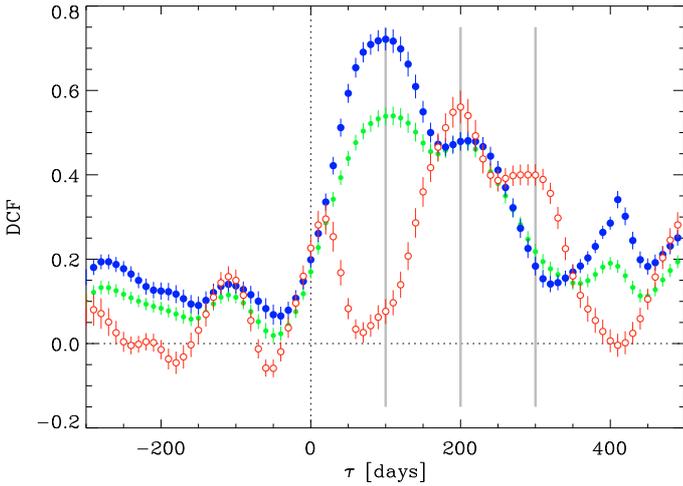


Fig. 2. Discrete correlation functions between the optical flux densities and the radio hardness ratio H_{mean} (see text) for different optical time intervals: total 1994–2005 light curve (green dots), total period excluding the interval JD = 2452150–2453200 (blue filled circles), and this interval alone (red empty circles). The grey vertical bars indicate the typical time delays of 100, 200, and 300 days.

occurrence of the radio outburst observed in 2005 seems to confirm an increasing time separation between the events, the last time interval being of at least 9 years (see Fig. 1).

To quantify the effect, we auto-correlated the 8 GHz light curve (the best sampled one) by means of the DCF, taking the main radio outbursts two by two. In Fig. 3 we show the results for the time intervals JD = 2443000–2449000 (~1976.6–1993.0; blue filled circles), JD = 2446000–2452000 (~1984.8–2001.2; green empty circles), and JD = 2449000–2453700 (~1993.0–2005.9; red filled circles). By considering the centroid of the peak distribution (see e.g. Raiteri et al. 2003), the first two outbursts are found to be separated by 2701 days (~7.4 years), the second pair by 2949 days (~8.1 years), and the last events present a time lag of 3400 days (~9.3 years).

3. Discussion

In this paper we have analysed new (unpublished) as well as old multifrequency data collected by the WEBT consortium during various campaigns on BL Lacertae to address two main issues: i) the correlation and time delay between the optical and radio flux variations; and ii) the possible quasi-periodicity of the main radio outbursts.

We have found that the hard radio events lag behind the optical outbursts with time scales varying from about 100 to 300 days. In particular, the longest delays occurred in the period 2002–2004.5. A possible explanation for this variable radio delay can be found in an inhomogeneous jet scenario, where the mechanism producing the flux enhancement propagates downstream, triggering optical and then radio outbursts as it crosses the corresponding emitting regions. If the jet changes its orientation with respect to the line of sight, relativistic effects produce a variation in the observed time scales. In particular, if the jet portion emitting the optical-to-radio radiation has a smaller (larger) viewing angle, this yields a shorter (longer) delay of the radio events with respect to the optical ones. However, the optical light curve in the period 2002–2004.5 does not show any peculiar behaviour that may suggest a significant change of the bulk orientation of the optical emitting region. Hence, the change

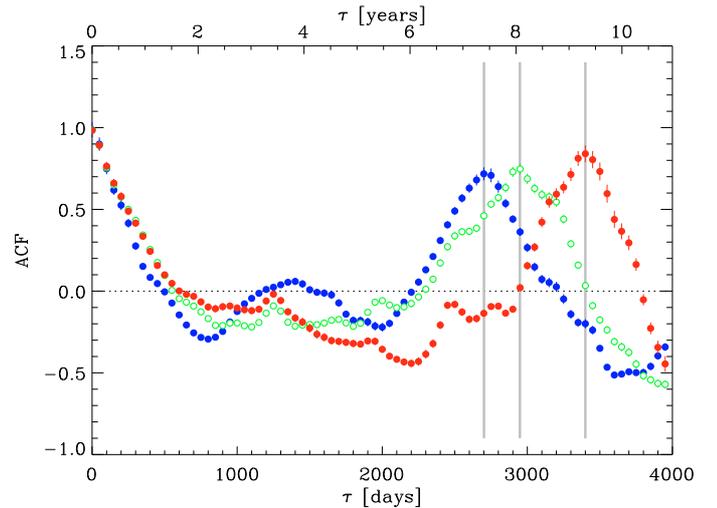


Fig. 3. Auto-correlation functions on subsequent pairs of radio outbursts at 8 GHz. Blue filled circles refer to the period JD = 2443000–2449000, green empty circles to JD = 2446000–2452000, and red filled circles to JD = 2449000–2453700.

in orientation must have occurred outward in the jet, toward the radio region, i.e. the jet changed its curvature. Indeed, by looking at the radio light curves in Fig. 1, we can see that the minimum radio level is achieved just around 2003, and the following hard radio outburst of the same year is the most delayed one with respect to its optical counterpart of late 2002.

Auto-correlation analysis performed on the historical 8 GHz light curve revealed a progressive lengthening of the time lag between subsequent major radio outbursts: 7.4, 8.1, and 9.3 years. If we assume that the intrinsic period is constant, the observed stretching might be due to increased light travel time. Even considering that the distance between the emitting region and the AGN core does not vary, a change in the orientation of the former departing from the AGN line of sight would augment the distance to us and hence the light travel time. High-resolution VLBA maps of BL Lacertae at 43 GHz presented by Marscher et al. (2008) show that the resolved jet structure may have typical length scales of the order of a light year. These distances may imply much longer de-projected lengths, so that our hypothesis of a ~1-year increase of the light travel time appears to be reasonable.

As a general view of the BL Lac multiwavelength emission behaviour in the last about forty years, we can distinguish three different phases. In 1968–1980 the source appears to be active in both the optical and radio bands, and this phase culminates and ends with the exceptional 1980–1981 radio outburst, which presented a particularly hard spectrum in its first major peak (see Fig. 1 in Villata et al. 2004a). In the second phase, 1981–1996, the reverse is observed: low optical levels and variability accompanied by a reduced and softer radio activity, which however culminates in the large, soft radio outburst of 1995–1997. The third phase seems more similar to the first one, with strongly enhanced optical activity and hard radio events. This behaviour may be explained by an orientation change of the emitting jet, where the optical and hard-radio emitting regions are better aligned with the line of sight during the first and third phases, the soft-radio part of the jet having a larger viewing angle. The opposite for the second phase.

In addition to this scenario, we also observe the radio “periodicity”, where the major periodic events maintain the hard or soft nature of the phase they belong to. In other words,

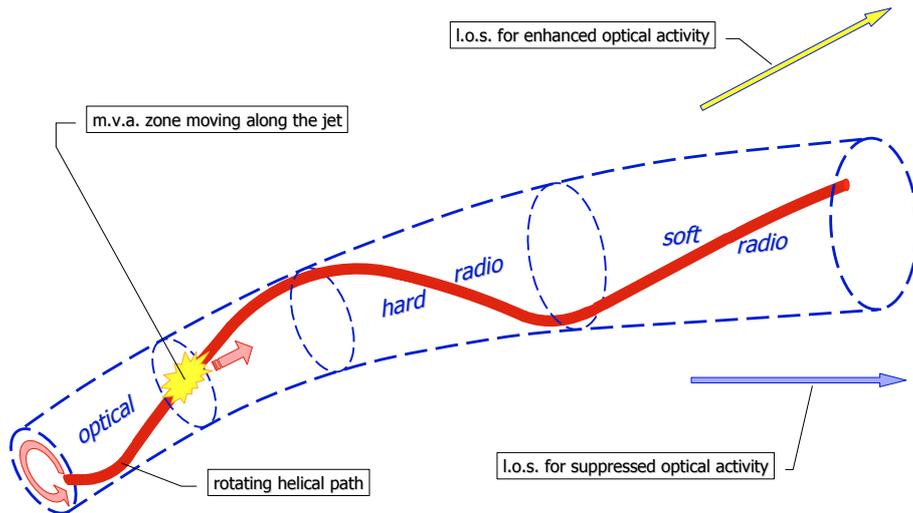


Fig. 4. Sketch of a curved jet model with a rotating helical path.

whatever the periodicity mechanism is, the 1980–1981 outburst occurred when the radio region was very well aligned, especially in the harder part. During the second, 1987–1988 outburst, the radio (especially hard) region was probably more poorly aligned, while the very soft 1995–1997 event occurred when the lower-frequency emitting regions had a smaller viewing angle. The last, hard radio outburst is located well inside the hard last phase. The radio periodicity we observe is much better seen at longer radio wavelengths, which are less affected by the “noise” of the optical and hard-radio activity, so that the relative amplitude of the four major outbursts is probably essentially due to the corresponding emitting region orientation.

Inside this long-term behaviour, probably of geometric origin, one can wonder what the nature of the single events is, i.e. whether the optical and correlated radio events shown in Fig. 1 are due to intrinsic or geometric variations. Villata et al. (2004b) argued that the poor chromatism of the optical outbursts compared to the strong chromatism of the fast flares suggests a geometric origin of the former. In this view, the mechanism producing the flux enhancement that travels downstream would be the Doppler boosting arising from a rotating helical path (see e.g. Villata & Raiteri 1999; Ostorero et al. 2004). The portion of the helical path having the smallest viewing angle successively crosses and lights up the different emitting regions. Alternatively, the existence of physical disturbances going through the jet may also explain the observed correlated events, but in this case the above-mentioned different chromatism does not have a simple explanation.

Figure 4 helps clarify the “geometrical” model, sketching the part of the jet emitting optical-to-radio frequencies. The emitting plasma flows along a rotating helical path. The yellow spot marks the portion of the helical path having the minimum viewing angle when the line of sight is represented by the yellow arrow. As the helix rotates, this zone shifts along the jet, thus originating optical and then radio outbursts when crossing the corresponding emitting regions. The orientation of the curved jet with respect to the yellow line of sight yields a Doppler enhancement of the optical activity. In contrast, when the jet moves and the line of sight is represented by the blue arrow, the alignment of the optical emitting region changes and consequently the optical activity is suppressed. At the same time the soft-radio emitting region now has a smaller viewing angle and hence the soft-radio activity increases. This bulk jet motion would thus explain the

alternate epochs of optical (and hard-radio) and soft-radio activity noticed in the historical light curves.

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