Quasi-Hilda comet 147P/Kushida-Muramatsu
Another long temporary satellite capture by Jupiter

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ABSTRACT

Context. The quasi-Hilda comets (QHCs), being in unstable 3:2 Jovian mean motion resonance, are considered a major cause of temporary satellite capture (TSC) by Jupiter. Although the QHCs may be escaped Hilda asteroids, their origin and nature have not yet been studied in sufficient detail. Of particular interest are long TSC/orbiters. Orbiters – in which at least one full revolution about the planet is completed – are rare astronomical events, because only four have been known to occur in the last several decades.

Every case has been associated with a QHC: 82P/Gehrels 3, 111P/Helin-Roman-Crockett, P/1996 R2 (Lagerkvist), and the possibly QHC-derived D/1993 F2 (Shoemaker-Levy 9, SL9).

Aims. We focus on long TSC/orbiter events involving QHCs and Jupiter. Thus we survey the known QHCs, searching for other long TSC/orbiters over the past century.

Methods. First, we confirmed the long TSC/orbiter events of 82P, 111P, and 1996 R2 in order to test our method against previous work, applying a general N-body Newtonian code. We then used the same procedure to survey the remaining known QHCs and search for long TSC/orbiter events.

Results. We newly identified another long TSC/orbiter: 147P/Kushida-Muramatsu from 1949 May 14 to 1961 July 15. Our result is verified by integrations of 243 cloned orbits that take account of the present orbital uncertainty of this comet. The event involves an $L_3 \rightarrow L_1$ transition as with 82P and 1996 R2. This may represent a distinct subtype of TSCs from QHC-derived ($L_3 \rightarrow L_1$) longer captures exemplified by 111P and (probably) SL9, though this classification is still only based on a small database of TSCs.

Conclusions. This is the third long TSC and the fifth orbiter to be found, thus long TSC/orbiter events involving Jupiter have occurred once per decade. Two full revolutions about Jupiter were completed and the capture duration was 12.17 ± 0.25 years. Both these numbers rank 147P as third among long TSC/orbiter events, behind SL9 and 111P. This study also confirms the importance of the QHC region as a dynamical route into and out of Jovian TSC, via the Hill’s sphere.

Key words. minor planets, asteroids – comets: general – celestial mechanics – solar system: formation – Kuiper Belt

1. Introduction

Among all the asteroids that have been recorded up to the present in the asteroid database, e.g., the “JPL Small-Body Database” (http://ssd.jpl.nasa.gov/), a large number (more than 1000 including unnumbered objects) are known to populate the region of the 3:2 mean motion resonance (MMR) with Jupiter, in the outer main belt. These are the “Hilda asteroids” (Schubart 1968, 1982, 1991; Ip 1976; Yoshikawa 1989; Franklin et al. 1993; Nesvorny & Ferraz-Mello 1997). Their semimajor axes, $a$, concentrate in the range $3.7 \text{ AU} \leq a \leq 4.2 \text{ AU}$, at eccentricities $e \leq 0.3$, and inclinations $i \leq 20^\circ$ (Zellner et al. 1985). This results in a range of the Tisserand parameter with respect to Jupiter, $T_j$, of $\sim 2.90 - 3.05$, where $T_j = a_j/a + 2 \sqrt{a_j/a_j(1 - e_j^2)} \cos \lambda_j$, with $a_j$ being the semimajor axis of Jupiter and $I$ the mutual inclination between the orbits. The critical arguments for the Hildas, $\phi = 3\lambda_j - 2\lambda - \sigma$, librate about $0^\circ$, being stable in the long-term ($\lambda$ is mean longitude, $\sigma$ is longitude of perihelion, and $J$ indicates Jupiter). As regards physical properties, the low-albedo D- and P-types are more abundant in Hildas’ surface colours than the small fraction of C-types (Dahlgren & Lagerkvist 1995; Dahlgren et al. 1997; Gil-Hutton & Brunini 2008; Licandro et al. 2008). The surface colour of D- and P-type asteroids, such as Hildas and Trojans in the outer main belt, corresponds well with that of cometary nuclei (Fitzsimmons et al. 1994; Jewitt 2002), which means that they are covered with a similar mineralogical surface, suggestive of a common origin.

More than 50 Jovian irregular satellites are known at present (Jewitt & Haghighipour 2007). Cuk & Burns (2004) pointed out that the progenitor of the main prograde cluster, the Himalia family, was plausibly derived from the Hildas long ago, if it was captured by a gas-drag assisted mechanism. Thus tracing the origin and nature of irregular satellites is very significant for studying the accretion processes in the early solar system. Satellite capture mechanics in the circular restricted three-body
Among the QHCs, 39P/Oterma was the first known to be temporarily captured by Jupiter, in 1936–1938 (Marsden 1962). However, this comet flew through the region near Jupiter over a rather short time, during which the comet did not complete a full revolution orbiting about the planet. In contrast, unlike 39P’s “fly-through” capture, there is a different kind of TSC, in which at least one full revolution about the planet is completed; we deal with these in the present paper. Following Kary & Dones (1996) we call such objects “orbiters”. These are otherwise defined by the jovicentric Kepler energy, \(E\), being negative, \(E_3 < 0\), with the additional condition that the bound small body must be within the jovicentric sphere of gravitational influence: Kary & Dones (1996) set its boundary at 3 Hill’s sphere radii (\(=1.065\) AU) of Jupiter. However, Howell et al. (2001) defined the TSC duration as the residence time in the Hill’s region. The former generally lasts longer than the latter, and here we regard the former as the TSC duration. The dynamics involved in TSC is quite different from that of quasi-satellites in 1:1 libration with Jupiter far outside the Hill’s region (Wiepert et al. 2000; Kinoshita & Nakai 2007).

Apart from SL9, only three orbiters have been known to occur. Every case has been associated with a QHC: 82P/Shoemaker-Levy 9, 110P/Helin-Roman-Crockett; and, though it is not in Toth’s (2006) QHC list, P/1996 R2 (Lagerkvist). These TSCs were found by Rickman (1979), Tanceredi et al. (1990), and Hahn & Lagerkvist (1999), respectively, and are discussed further in Sect. 2. The occurrence of these few events during the last several decades is consistent with the rarity of long TSC/orbiter events suggested by Kary & Dones (1996). Although 74P encountered Jupiter at distances of 0.24 AU and 0.47 AU in 1955 October and 1963 September respectively, it was not bound to Jupiter (Rickman 1979; Carusi et al. 1985b); this comet is, however, expected to experience a TSC by Jupiter in this century (Carusi et al. 1985b; see also Sect. 4). There further exist some JFCs that encountered Jupiter more closely than several QHCs involved in TSC, e.g., 39P/Oterma, 74P/Smirnova-Chernykh, and 82P/Gehrels 3. Di Sisto et al. (2005) integrated the motions of 500 fictitious Hildas for \( \sim 10^5 \) years, and found that most of them escaped from the Hilda zone into the JFC population, i.e., left the 3:2 MMR and evolved quickly on to unstable orbits; such a chaotic diffusion from the Hilda zone has also been demonstrated by Nesvorný & Ferraz-Mello (1997). In addition, large-scale collisional processes, such as the late heavy bombardment, might also release small bodies from the Hilda zone into JFCs, e.g., see Gil-Hutton & Brunini (2000). Hence, some QHCs may indeed be such escaped Hildas themselves. Recently, Toth (2006) updated the QHC list, finding a total of 17 members (see Sect. 3). This includes bodies such as the renowned Comet D/1993 F2 (Shoemaker-Levy 9, SL9) that have undergone TSC by Jupiter and then disappeared after colliding with the planet. Surface spectroscopic (or colorimetric) measurements for QHCs have only been carried out for 82P (De Sanctis et al. 2000), the results of which also indicate a taxonomic D-type.

The work of Kary & Dones (1996) supports this possibility: they traced the motions of numerous fictitious JFCs for \( \sim 10^5 \) years and found that half the SL9-like very long captures >50 years were due to QHCs. They estimated that the frequency of such a very long TSC (\(=\) “long capture” as designated by them) is extremely rare, only 0.02% of all the TSC events in their simulations. Interestingly, impacts on Jupiter are more frequent than the very long TSCs by a factor of \(8 \sim 9\). They also evaluated that long TSCs (\(=\)”orbiters bound >10 yr” as designated by them) and orbiters are still rare events, at the respective levels of 0.8% (> very long TSCs) and 2% (> long TSCs) relative to all events, with about 98% being the short TSC type which contains the fly-through events. Carusi & Valsecchi (1979) had earlier confirmed the rarity of orbiter events, simulating motions of fictitious small bodies as well.

In the jovicentric Keplerian system, a TSC (especially a long TSC/orbiter) occurs whenever a small body passes near one of the collinear libration points \(L_1\) or \(L_2\) in the CR3BP of the Sun-Jupiter system. Considering such a transition using newly developed dynamical systems techniques based on a Hamiltonian formulation in the CR3BP, Koon et al. (2001) and Howell et al. (2001) demonstrated that a TSC by Jupiter occurs when the small body passes through a region inside the invariant manifold structure related to periodic halo orbits around \(L_1\) or \(L_2\) in the Hill’s region. The TSC (or its duration) is usually defined by the jovicentric Kepler energy, \(E_3\), being negative, \(E_3 < 0\), with the additional condition that the bound small body must be within the jovicentric sphere of gravitational influence: Kary & Dones (1996) set its boundary at 3 Hill’s sphere radii (\(=1.065\) AU) of Jupiter. However, Howell et al. (2001) defined the TSC duration as the residence time in the Hill’s region. The former generally lasts longer than the latter, and here we regard the former as the TSC duration. The dynamics involved in TSC is quite different from that of quasi-satellites in 1:1 libration with Jupiter far outside the Hill’s region (Wiepert et al. 2000; Kinoshita & Nakai 2007).

Apart from SL9, only three orbiters have been known to occur. Every case has been associated with a QHC: 82P; 110P/Helin-Roman-Crockett; and, though it is not in Toth’s (2006) QHC list, P/1996 R2 (Lagerkvist). These TSCs were found by Rickman (1979), Tanceredi et al. (1990), and Hahn & Lagerkvist (1999), respectively, and are discussed further in Sect. 2. The occurrence of these few events during the last several decades is consistent with the rarity of long TSC/orbiter events suggested by Kary & Dones (1996). Although 74P encountered Jupiter at distances of 0.24 AU and 0.47 AU in 1955 October and 1963 September respectively, it was not bound to Jupiter (Rickman 1979; Carusi et al. 1985b); this comet is, however, expected to experience a TSC by Jupiter in this century (Carusi et al. 1985b; see also Sect. 4). There further exist some JFCs that encountered Jupiter more closely than several QHCs involved in TSC, e.g., 16P/Brooks 2; D/1770 L1 (Lexell); 81P/Wild 2; but they were not captured by the planet owing to their high-velocity encounters (Carusi et al. 1985a; Emel’yanenko 2003).
Therefore studying the origin and nature of QHCs is of great importance from various astronomical points of view mentioned above, especially as regards their origin and being possibly related to the Hildas and the Jovian irregular satellites. Such studies may provide unique knowledge and clues about their origin and being possibly related to the Hildas and the Jovian irregular satellites. Additionally, they may provide unique knowledge and clues about the orbital stability for the retrograde satellites. The Jovian oblateness terms and the perturbations by the Galilean satellites were also ignored since their effects are negligible in our investigations (see Kary & Dones 1996); these effects should be included in analyses of very long TSCs of SL9-like objects having highly inclined Jupiter-grazing orbits.

As initial parameters, up to date osculating orbital elements were taken from the JPL Small-Body Database, mentioned above in Sect. 1, for 82P and 1996 R2 and from Nakano (2005) for 111P, as listed in Table 1. 82P and 111P are numbered, multiple-apparition comets, covered by very long observational arcs, hence their orbital solutions are highly precise. Meanwhile, although 1996 R2 is unnumbered and still a one-apparition comet, consequently with a shorter arc, the number of astrometric positions is the most, 135, and the RMS residual is the least, 0′′76, among the three comets, hence we judged that the TSC of 1996 R2 is worth simulating here. The nongravitational parameters for these QHCs’ motions were not detectable from their astrometry hence were not included in our integrations – in any case their motions are chaotic during TSC. The Jovian oblateness terms and the perturbations by the Galilean satellites were also ignored since their effects are negligible in our investigations (see Kary & Dones 1996); these effects should be included in analyses of very long TSCs of SL9-like objects having highly inclined Jupiter-grazing orbits.

Table 1. Initial parameters of QHCs 82P/Gehrels 3, 111P/Helin-Roman-Crockett, and P/1996 R2 Lagerkvist (equinox J2000).

<table>
<thead>
<tr>
<th>Object</th>
<th>82P</th>
<th>111P</th>
<th>1996 R2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Osculation epoch (TT)</td>
<td>2002 Mar. 27.0</td>
<td>2004 Dec. 21.0</td>
<td>1996 Oct. 08.0</td>
</tr>
<tr>
<td>Mean anomaly $M$</td>
<td>24°27332</td>
<td>359°25243</td>
<td>346°17074</td>
</tr>
<tr>
<td>Semimajor axis $a$ (AU)</td>
<td>4.138678</td>
<td>4.0400597</td>
<td>3.782078</td>
</tr>
<tr>
<td>Eccentricity $e$</td>
<td>0.1238743</td>
<td>0.1402634</td>
<td>0.3099920</td>
</tr>
<tr>
<td>Argument of perihelion $\omega$</td>
<td>227°65115</td>
<td>10°56557</td>
<td>334°04513</td>
</tr>
<tr>
<td>Longitude of ascending node $\Omega$</td>
<td>239°62851</td>
<td>91°93769</td>
<td>40°24804</td>
</tr>
<tr>
<td>Inclination $i$</td>
<td>1°12654</td>
<td>4°23300</td>
<td>2°60532</td>
</tr>
<tr>
<td>Number of astrometric positions</td>
<td>103</td>
<td>126</td>
<td>135</td>
</tr>
<tr>
<td>RMS residual</td>
<td>0′′79</td>
<td>0′′86</td>
<td>0′′76</td>
</tr>
<tr>
<td>Source reference</td>
<td>JPL 12</td>
<td>Nakano (2005)</td>
<td>JPL 18</td>
</tr>
</tbody>
</table>

2. Computation method and its application to the known TSCs

The heliocentric trajectories for the long TSCs/orbiters, except for SL9, have been numerically simulated by Carusi & Valsecchi (1979) and Carusi et al. (1985a,b) for 82P, by Tancredi et al. (1990), Belbruno & Marsden (1997) and Howell et al. (2001) for 111P, and by Hahn & Lagerkvist (1999) for 1996 R2. First of all, we attempted to reproduce their TSC events in order to compare our simulations with these previous studies, integrating back to the time of each TSC. We applied a general N-body Newtonian code, then equations of motion for the ith body are:

\[
\begin{align*}
\frac{\text{d}^2 r_i}{\text{d}t^2} = -G \frac{(M_0 + m_i) r_i}{r_i^3} - \sum_{j=1, j \neq i}^{N} G m_j \left( \frac{r_i - r_j}{r_{ij}^3} + \frac{r_j}{r_j^3} \right),
\end{align*}
\]

where $G$ is the gravitational constant, $M_0$ and $m_i$ are respectively the mass of the sun and the ith body ($i = 1, 2, \ldots, N$), $r_i$ is the heliocentric position vector of the ith body, $r_{ij}$ is the heliocentric distance of the ith body, and $r_{ij}$ is the distance between the ith and jth bodies. Here, we regarded comets as massless bodies.

The integrator that we applied here is the “SOLEX”, Ver. 9.1 package, developed by Vitagliano (1997) based on the Bulirsch-Stoer method. Coordinates and velocities of the planets, regarded as point masses, were based on the JPL Planetary and Lunar Ephemeris DE409. We confirmed that the results of our numerical integrations did not significantly change when we used other integration methods that we have often applied in our studies, e.g., the Adams method. Our integrator can accurately process very close encounters by means of a routine that makes automatic time step adjustments, and truncation and round-off errors are almost negligible for our investigation here. Therefore the SOLEX integrator is sufficiently reliable to deal with the problem of close encounters with Jupiter.

Among these TSCs, the trajectories of 82P and 1996 R2 are similar in profile to each other. Both these QHCs came tangentially from outside Jupiter’s orbit with a low-inclination retrograde motion, i.e., their pre-capture heliocentric orbits imply that they came from the Centaur region, their perihelia being beyond the Jovian orbit. During the TSC, first they passed close to $L_2$ with low relative velocities (between Jupiter and comets in the heliocentric frame) of respectively ~0.7 km s$^{-1}$ and ~0.6 km s$^{-1}$, then revolved about Jupiter, completing one full revolution, and finally escaped from the Jovian system into the QHC region, passing near $L_1$. In the $L_2 \rightarrow L_1$ transition, an object that enters the Jovian system close to $L_2$ seems to have enough orbital energy to rapidly escape through the region near $L_1$ (Tanikawa 1983). The long lasting captures for 82P and 1996 R2 may be somewhat related to the orbital stability for the retrograde satellites (Huang & Innanen 1983; Nesvorný et al. 2003). However, the TSC duration is below 10 years in both cases; so to be more exact these orbiters should perhaps not be categorized as long TSCs.
secondly, the Li asymptotic trajectory winding onto a periodic halo orbit of Jupiter, in the jovicentric rotating frame where the sun is always in the direction of the −x-axis. The arrows indicate the direction of time (opposite to the direction of the integrations, which went backwards in time).

On the other hand, the motion of 111P was more complicated than those of 82P and 1996 R2. 111P completed three full revolutions about Jupiter during its long TSC of 18.45 years, both of which numbers rank second next to SL9 among known TSCs. Its pre-capture and post-escape heliocentric orbits were both QHC type (Belbruno & Marsden 1997), entering through the region near \( L_1 \) at a relative velocity of \( \sim 1.0 \) km s\(^{-1}\) and escaping near \( L_1 \) again. Its capture/escape trajectory is almost symmetric about the x-axis (cf. Murison 1989) inside the Hill’s region in the CR3BP. Howell et al. (2001) demonstrated that the 111P capture/escape trajectory is almost identical to some asymptotic trajectory winding onto a periodic halo orbit of \( L_1 \), such trajectories forming segments of the invariant manifolds.

We therefore reconfirmed the long TSC/orbiter events involving 82P, 111P and 1996 R2. Our orbiter trajectories look exactly as in Belbruno & Marsden (1997) and Howell et al. (2001) for 111P, and as in all the above papers for 82P, but the results by Tancredi et al. (1990) for 111P and Hahn & Lagerkvist (1999) for 1996 R2 show somewhat different behaviours. Both these can be ascribed to slight differences in initial parameters — their initial orbits were based on observational arcs of respectively 2–4 months and 111 days whereas ours were based on longer time spans of 4643 and 153 days. Besides, Hahn & Lagerkvist (1999) plotted the trajectory not of the nominal orbit but of a clone, i.e., a possible TSC trajectory within the uncertainty of the initial parameters. In fact, we could not reach the TSC of 1996 R2 by using their nominal orbit. This demonstrates that in studying TSC events, initial parameters must be determined precisely, based on long-arc improved orbital solutions where possible, since jovian-orbital events during TSC have a chaotic nature.

The capture situations of these QHCs are summarized in Table 2. During these TSCs, 82P, 111P and 1996 R2 experienced 2, 6 and 3 perijove passages, respectively. In particular, 82P passed its closest perijove of 3.01 \( R_J \) in 1970 August, just outside the Roche limit for comets \( \sim 2.7 R_J \) (assuming a cometary bulk density \( \rho \sim 1 \) g cm\(^{-3}\)). Table 2 also shows the minimum values of the jovian Kepler energy \( E_J = -1/2a' \) (in AU\(^{-1}\)) where \( a' \) is the semimajor axis for the jovian orbit. The low values attained, −2.80, −3.20, and −3.28 for the three comets, are often a feature of long TSCs/orbiters, as against −1.79 which we have computed for 39P during its fly-through in the 1930s.

### Table 2. Long TSC/orbiter data of QHCs 82P, 111P, and 1996 R2.

<table>
<thead>
<tr>
<th>Object</th>
<th>TSC duration</th>
<th>No. rev(^a)</th>
<th>min. ( E_J ) (^b)</th>
<th>Heliocentric orbit &amp; ( L_1 ) to ( L_1 ) transition(^c)</th>
<th>Perijove time(^d)</th>
<th>dist.(^e) ((\text{AU}))</th>
<th>( V_J ) ((\text{km s}^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>82P</td>
<td>1966 Dec. 11–1974 Jul. 11</td>
<td>1</td>
<td>−2.80</td>
<td>2.3 → 3.2 ( L_2 \rightarrow L_1 )</td>
<td>1970 Aug. 15.6</td>
<td>0.0014 ((3.01 R_J))</td>
<td>34.25</td>
</tr>
<tr>
<td></td>
<td>7.58 yr</td>
<td></td>
<td></td>
<td>1973 Mar. 24.9</td>
<td>0.041 ((85.16 R_J))</td>
<td>9.18</td>
<td></td>
</tr>
<tr>
<td>111P</td>
<td>1967 Jan. 25–1985 Jul. 08</td>
<td>3</td>
<td>−3.20</td>
<td>3.2 → 3.2 ( L_1 \rightarrow L_1 )</td>
<td>1969 Oct. 14.4</td>
<td>0.057 ((119.4 R_J))</td>
<td>5.00</td>
</tr>
<tr>
<td></td>
<td>18.45 yr</td>
<td></td>
<td></td>
<td>1972 Sep. 03.2</td>
<td>0.175 ((336.4 R_J))</td>
<td>2.33</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>1976 Apr. 11.2</td>
<td>0.012 ((24.31 R_J))</td>
<td>11.85</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>1979 Jul. 18.6</td>
<td>0.211 ((442.4 R_J))</td>
<td>2.11</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>1980 Nov. 17.0</td>
<td>0.201 ((421.1 R_J))</td>
<td>2.20</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>1983 Aug. 10.1</td>
<td>0.063 ((131.7 R_J))</td>
<td>4.74</td>
<td></td>
</tr>
<tr>
<td></td>
<td>9.77 yr</td>
<td></td>
<td></td>
<td>1990 Jun. 28.8</td>
<td>0.169 ((352.7 R_J))</td>
<td>2.78</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>1992 Sep. 18.5</td>
<td>0.325 ((680.0 R_J))</td>
<td>1.82</td>
<td></td>
</tr>
</tbody>
</table>

\(^a\) Number of completed full revolutions about Jupiter.
\(^c\) Transition associated with the TSC: firstly, the Jovian MMR (heliocentric orbit) the comet is closest to immediately before/after the TSC; and secondly, the \( L_1 \) point near which the comet passes at the start/end of the TSC phase.
\(^d\) Time of perijove passage in TT.
\(^e\) Perijove distance in AU and also in \( R_J \).
\(^f\) Jovian velocity in km s\(^{-1}\) at perijove.
Table 3. Quasi-Hilda comets.

<table>
<thead>
<tr>
<th>Numbered QHCs:</th>
<th>Unnumbered QHCs:</th>
</tr>
</thead>
<tbody>
<tr>
<td>36P/Whipple</td>
<td>D/1977 C1 (Skiff-Kosai) P/2001 YX_{127} (LINEAR)</td>
</tr>
<tr>
<td>82P/Gehrels 3^a</td>
<td>D/1993 F2 (Shoemaker-Levy 9)^a P/2003 CP_{7} (LINEAR-NEAT)</td>
</tr>
<tr>
<td>135P/Shoemaker-Levy 8</td>
<td>P/1996 R2 (Lagerkvist)^a</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>Not included in Toth’s (2006) QHC list; # involved in previously known TSC.</td>
<td></td>
</tr>
</tbody>
</table>

Table 4. Initial parameters of QHC 147P/Kushida-Muramatsu (equinox J2000) and their ±1σ error estimates (Nakano 2002).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>Osculation epoch (TT)</td>
<td>2001 May 11.0</td>
<td>±0.00081</td>
</tr>
<tr>
<td>Perihelion time T (TT)</td>
<td>2001 Apr. 29.48509 (M = 1.52643)</td>
<td>±0.0000019</td>
</tr>
<tr>
<td>Perihelion distance q (AU)</td>
<td>2.7524408</td>
<td>±0.00000019</td>
</tr>
<tr>
<td>Semimajor axis a (AU)</td>
<td>3.8094146</td>
<td>±0.0000010</td>
</tr>
<tr>
<td>Eccentricity e</td>
<td>0.2774636</td>
<td>±0.0000005</td>
</tr>
<tr>
<td>Argument of perihelion ω</td>
<td>347.55482</td>
<td>±0.00047</td>
</tr>
<tr>
<td>Longitude of ascending node Ω</td>
<td>93°69336</td>
<td>±0.00044</td>
</tr>
<tr>
<td>Inclination i</td>
<td>2°36694</td>
<td>±0.00004</td>
</tr>
<tr>
<td>Number of astrometric positions</td>
<td>197</td>
<td></td>
</tr>
<tr>
<td>Astrometric arc</td>
<td>1993 Dec. 08–2002 Mar. 20</td>
<td>3024 days (8.28 yr)</td>
</tr>
<tr>
<td>RMS residual</td>
<td>0'85</td>
<td></td>
</tr>
</tbody>
</table>

Shortly after TSC, these three QHCs were discovered and observed as “quasi-Hilda comets” for the first time. The time difference, $\Delta T_{\text{TSC-obs}}$, between the end time of the TSC, given in Table 2, and the first astrometric time, given in Table 1, is notable. Every $\Delta T_{\text{TSC-obs}}$ is short enough (1.3 years for 82P, 3.49 years for 111P, and 3.16 years for 1996 R2) to indicate that the simulated TSC should be a real event.

3. 147P/Kushida-Muramatsu: another long TSC/orbiter

Next we surveyed the remaining objects in Toth’s (2006) QHC list (Table 3) to determine whether other long TSCs/orbiters around Jupiter exist. We applied our code to integrate each orbit back 100 years from its initial epoch, since the Lyapunov time of JFCs is rather short, generally 100 ± 50 yr (Tancredi 1995). Moreover, going back more than 100 yr may not be meaningful because of likely weak nongravitational accelerations, in addition to the accumulation of orbital errors. We recognized that short TSC events have sometimes occurred, for which results will be published as an additional paper elsewhere. Eventually, we successfully found another long TSC, involving 147P/Kushida-Muramatsu.

The observational history of 147P is described by Green (1993, 2000) and Kronk (2008). The comet was photographically discovered by Kushida and Muramatsu (Yatsugatake South Base Observatory, Japan) on 1993 December 8.65, using a 0.25-m f/3.4 reflector. It was then at magnitude ~16.5 and slightly diffuse, about 1–2’ in diameter with a central condensation. The comet was recovered on 2000 October 3.72, when Oriebe (Saji Observatory, Japan) obtained CCD images with the 1.03-m reflector. Thus 147P has been detected at two perihelion returns, allowing it to be numbered, although it has not been astrometrically observed since 2002 March.

In our integration of 147P, the initial parameters were taken from Nakano (2002), as listed in Table 4. Its orbital solution was accurately improved based on 197 carefully selected positions covering an arc of 3024 days and also provided associated error estimates (Table 4). We believe that this solution is the best determined for this comet, probably based on a longer arc and more astrometric positions than any other. The nongravitational accelerations in 147P’s motion were not detected from the astrometry. Integrating back this orbit, we found that the comet was captured by Jupiter in the mid-20th century. The 3D-view of 147P’s trajectory during TSC in the joviancentric rotating frame covering 1 AU square. The vertical lines, spaced at 10-day intervals, each connect a position of the comet on the trajectory with its projection onto the $x$–$y$ plane.

However, $\Delta T_{\text{TSC-obs}}$ of 147P is extremely large, more than 30 years, which greatly exceeds the values of 3.5 years for 82P, 111P and 1996 R2 (and also SL9 with negative $\Delta T_{\text{TSC-obs}}$). Thus we must further examine whether or not 147P really underwent a long TSC/orbiter phase in the mid-20th century. To answer this, we traced other possible orbital motions of 147P back to and during its TSC, generating multiple “clones” at initial epoch, and integrating them. As well as the nominal 147P osculating orbit, other clones had slightly different orbital elements, within the ±1σ error, given in Table 4. We generated
permutations yielded a total of 243 (\(\pm\) of their trajectories corresponds to \(\pm\)TSC

tion. Hence we conclude that the real 147P indeed experienced a long

\[\pm\]

revolutions about Jupiter during the

\[\pm\]

generated from 147P. They underwent long TSCs, completing two full

\[\pm\]

at Jupiter's orbit, i.e., with a low-

\[\pm\]

long TSC in the mid-20th century. The motions of all the clones in and around the TSC interval, where

\[\pm\]

sometimes expected with chaotic trajectories. We conclude that

\[\pm\]

to be the most strongly

\[\pm\]

capture heliocentric Centaur orbit of 147P had

\[\pm\]

inclination retrograde motion in the jovicentric frame. The pre-

\[\pm\]

coming tangentially from outside Jupiter's orbit, i.e., with a low-

\[\pm\]

capture orbital phase display a scatter that is as evident as the

\[\pm\]

We found that all 243 clones underwent TSCs. In Fig. 3,

\[\pm\]

we can see that their trajectories become scattered in their pre-

\[\pm\]

phase, while converging toward the post-escape

\[\pm\]

since the orbital motions were integrated back in time. However, the dispersion of their TSC trajectories, corresponding to \(\pm\)1\(\sigma\) error in the orbit determination, is not as scattered as is

\[\pm\]

set of clones. Conversely, we found \(a\) to be the most strongly

\[\pm\]

effective parameter in causing divergence among the clones' orbital

behaviours.

Figure 4 shows the variations in \(r_J\), \(E_J\), \(E_o\), and \(T_J\) of 243 clones of 147P in and

\[\pm\]

and around their interval of TSC, where \(r_J\) = jovicentric distance (in AU); \(E_J\) and \(E_o\) = jovicentric and heliocentric Kepler energy, respectively; \(T_J\) = Tisserand parameter. The abscissa for all the plots covers 2 431.596.5 (1945 May 21.0 TT) to 2 438.095.5 (1963 March 07.0 TT), the time for

\[\pm\]

which the nominal 147P was within 2 AU of Jupiter.

The comet entered the Jovian sys-

\[\pm\]

\[\pm\]

Tisserand parameter. The abscissa for all the plots covers 2 431.596.5 (1945 May 21.0 TT) to 2 438.095.5 (1963 March 07.0 TT), the time for

\[\pm\]

which the nominal 147P was within 2 AU of Jupiter.
was slightly higher than 3.0 in the pre-capture orbital phase, as is often associated with low-velocity encounters at Jupiter (Kresák 1979), and it suddenly dropped twice around the closest perijove passages. We summarize the capture situation data of 147P in Table 5 (again, error estimates come from the range shown by all the clones).

Also indicated in the $E_0$ diagram in Fig. 4 is the commensurability of 147P with Jupiter changing from 3.4 Centaur-type in the pre-capture orbital phase to 8.5 (rather than 3.2) QHC in the post-escape phase. This, however, corresponds to the osculating orbit immediately post-escape, and integrations for motions of all the clones over a longer timescale suggest instead that 147P might librates in the 3.2 Jovian MMR for ~350 yr following the TSC (and is doing so at the present time), though with a somewhat faster libration period and higher libration amplitude (~135° for the nominal orbit) than the more stable, typical Hilda asteroid orbits (e.g., Schubart 1982, 1991; Franklin et al. 1993; Nesvorný & Ferraz-Mello 1997). Moreover, test integrations of the other objects suggest that of the QHCs known to have been involved in a TSC, only 147P has undergone an interval where the critical TSCs of the 3.2 MMR librates.

Further backward integrations of 147P inform us of the possibility of another TSC somewhere between the late-19th to early-20th century. However, as all the clones were extremely scattered by that time, we do not consider that TSC here.

4. Concluding remarks

On the basis of our investigations above, we have presented a newly identified TSC of a comet by Jupiter. This is in the rare, orbiter class of TSCs and involves 147P from a newly identified TSC of a comet by Jupiter. This is in contrast, the close encounter of 147P with Jupiter around 1952 August 26 (Table 5) was at a perijove distance of 14 J, comfortably outside the Roche limit. The radius, $R_e$ of 147P’s nucleus was estimated at 0.21 km by Lamy et al. (2004), the smallest among all their measured comet nuclei.

The jovian tidal stress, $\sigma_T$, acting on small bodies (QHCs here), is given by:

$$\sigma_T \approx \frac{Gm_JR_e^2}{r_J^3},$$

where $m_J$ is the mass of Jupiter. Compared to the $\sigma_T$ acting on SL9 at perijove $<1.5$ $R_J$ in 1992 (Scotti & Melosh 1993; Asphaug & Benz 1994, 1996), the $\sigma_T$ for 147P was extremely small, amounting to <0.005% if we take the original, pre-encounter $R_e$ of SL9 as ~1 km (Scotti & Melosh 1993; Asphaug & Benz 1994) and $\rho$ of both the comets as being equal. Hence, although our treatment here is approximate, there seems no reason to believe that 147P was affected by jovian tides. On the
other hand, 82P, which passed its perijove at 3.01 $R_J$ in 1970, just outside the cometary Roche limit, may have suffered some effect due to the Jovian tides, even though it was not broken up. Taking $R_*$ for 82P as 0.73 km (Lamy et al. 2004), and equal $\rho$ as above, implies that the $\sigma_T$ acting on 82P could be up to 7% of that for SL9. If 82P is a friable and furthermore a loose rubble-pile object, the heating energy from continual Jovian tides might sufficiently affect the comet’s nucleus structure so as to allow $H_2O$ ice, if present, to sublimate even though 82P is beyond the usual heliocentric distance for $H_2O$ sublimation. If our hypothetical scenario is true, such tidal heating effects could trigger cometary activity on 82P and produce an outburst. In this event, the coma size and consequent brightness would peak several days (or more) after the maximum tidal effects.

Another intriguing point is whether or not other tidal effects, e.g., tidal distortion and tidal torques leading to rotation state changes (Scheeres et al. 2004), are detectable in the light-curve observations of the captured QHCs. In the physical database of cometary nuclei by Lamy et al. (2004), we can notice a rather high axis ratio ($a/b > 1.6$) and long rotation period $\sim 50$ h in the dataset of 82P, though an interpretation in terms of such tidal effects is still speculative.

4.4. Comets or asteroids?

At any rate, we have considered here only a small subset of the TSC events, focusing on the long TSCs/orbiters, for which there still exist only limited available data. Therefore we know little about such unique and extraordinary astronomical events, which are still full of ambiguities. In addition, we do not know whether QHCs are comets or asteroids. Indeed, several QHCs have sometimes been discovered or recovered as asteroids because of their cometary activity being weak: e.g., 36P, 9P, and 433 Eros. For example, 39P (cometary activity being weak: e.g., 36P, 9P, and 433 Eros), D/1977 C1 (==1977 DV1), P/1999 XN120, P/2001 YX127, and P/2003 CP7. Further observations and research for the QHCs will be necessary to unlock their origin and nature.

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