What can be learned about dark energy evolution?

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ABSTRACT

We examine constraints obtained from SNIa surveys on a two parameter model of dark energy in which the equation of state \( w(z) = P(z)/\rho(z) \) undergoes a transition over a period significantly shorter than the Hubble time. We find that a transition occurring at a redshift as low as \( z \approx 0.17 \) could still remain undistinguishable from a standard cosmological constant. The addition of a prior on the matter density \( \Omega_m = 0.3 \) only modestly improves the constraints. Even deep space experiments would still fail to identify a rapid transition at a redshift above 0.5. These results illustrate that a Hubble diagram of distant SNIa alone will not fail to identify a rapid transition at a redshift below 0.8.

Key words. cosmology: cosmic microwave background – cosmology: cosmological parameters – cosmology: observations

1. Introduction

The nature of dark energy is one of the most puzzling mysteries of modern cosmology. It is now widely accepted that our universe is experiencing a phase of accelerated expansion (Peebles & Ratra 2003). The evidence was first found using a type Ia supernovae luminosity vs. redshift diagram (Riess et al. 1998; Perlmutter et al. 1999), but a number of other observations now support this conclusion. In particular, estimations of the matter density of the universe generally lead to a low value, while the CMB anisotropies point toward a spatially flat Universe (Lineweaver et al. 1997; de Bernardis et al. 2000). WMAP data also require the presence of dark energy (Spergel et al. 2007) unless one considers an unexpectedly low value of the Hubble parameter \( H_0 \lesssim 50 \) km s\(^{-1}\) Mpc\(^{-1}\) (Blanchard et al. 2003; Hunt & Sarkar 2007). The possible correlation of the CMB fluctuation map with surveys of extragalactic objects (Fosalba et al. 2003; Corasaniti et al. 2005; Pogosian 2005) also provides direct evidence, although with a limited significance level (\(<3\sigma\)), for the existence of an unclustered dark energy component in the universe, the detected correlation being explainable through the integrated Sachs-Wolfe effect, i.e., a time variation of the gravitational potential, which is achieved only if the (baryonic + cold) matter density parameter \( \Omega_m \) significantly differs from 1. Finally, the shape of the correlation function on scales up to 100 h\(^{-1}\) Mpc which has been recently measured accurately (Eisenstein et al. 2005) in combination with the CMB data advocates for the presence of dark energy (Blanchard et al. 2006) in the framework of general relativity. However, the nature of this dark energy has been the subject of numerous speculations. The simplest model, which was originally proposed (in another context) by Einstein (1917), is a pure cosmological constant \( \Lambda \), a term on the left hand side of Einstein’s equations. However, a cosmological constant can also be regarded as the contribution of the vacuum to the right hand side of the equation with a specific equation of state, i.e., a component with negative pressure \( P_\Lambda \) related to the energy density \( \rho_\Lambda \) by the relation \( P_\Lambda = -\rho_\Lambda \). Indeed, quantum field theory predicts that the lowest energy state of any mode contributes to a vacuum energy density that behaves exactly as a cosmological constant (see, e.g. Binétruy 2000). A number of problems arise with this possibility, in particular the so-called hierarchy problem: the expected contribution is usually enormous, naive calculation gives \( \rho_\Lambda \approx 10^{105} \) GeV\(^4\), around 122 orders of magnitude larger than the present critical density of the universe. However, there exist mechanisms, such as supersymmetry, which allow one to reduce considerably the vacuum energy density, but since supersymmetry is broken at a scale larger than 100 GeV one is still plagued with an enormous vacuum energy density of the order of \( 10^8 \) GeV\(^4\). The usual explanation is then to say that there exists a yet unknown mechanism which ensures that the contribution of the vacuum energy density is zero. One is therefore left to explain the nature of dark
energy, which differs from a cosmological constant, avoiding the extreme fine tuning required to obtain the observed dark energy density (Binétruy 2000). Most models that have been proposed so far (quintessence models) therefore rely on the idea that some scalar field (Caldwell et al. 1998) behave today like a cosmological constant, exactly as an other scalar field did during inflation. The most remarkable feature of quintessence models is that both the scalar field pressure $P_\Omega$ and energy density $\rho_\Omega$ evolve according to dynamical equations. Consequently, the so-called equation of state parameter $w_\Omega \equiv P_\Omega/\rho_\Omega$, varies with time between 1 and $-1$, as the field evolves along the potential. In some extreme (and possibly ill-defined) models, this parameter can even take any arbitrary value, for example if one allows the density $\rho_\Omega$ to take negative values or a change in the sign of the kinetic term (Caldwell 2002). Other models involving scalar tensor theories also allow for such transient behaviour (Elizalde et al. 2004).

The detection of such a variation would therefore be of great importance for our understanding of dark energy.

The aim of the present paper is to study models with a rapid transition of the equation of state and to illustrate that in this case, the Hubble diagram of SNIa provides surprisingly weak constraints compared to the case of a smooth transition. In Sect. 2, we recall a few basic aspects of simple quintessence models, and the motivation for a convenient parametrization of the equation of state parameter $w_\Omega(z)$ allowing rapid transition. In Sect. 3, we describe the analysis we perform, and state our main results. In Sect. 4 we discuss the crucial issue of the impact of the epoch of observation on the parameter estimation. We draw the main conclusions of our work in Sect. 5.

2. Dark energy parametrization

Historical quintessence models rely on the idea of a tracking solution (Ratra & Peebles 1988; Wetterich 1988), which involves a scalar field evolving in an inverse power potential, $V(\phi) \propto Q^{-\alpha}$, the proportionality constant being tuned so as to obtain the desired value of the dark energy density parameter $\Omega_\Lambda \sim 0.7$ today. The main feature of these models is that the pressure to energy density ratio, $w_\phi$, remains constant both in the radiation era and in the matter era (with different values during each epoch), and that it tends toward $-1$ once the quintessence energy density dominates. The value of the parameter $w_\Omega$ depends on the power law index of its potential. From existing data, it seems that only values close to $w_\Omega \sim -1$ today, or even possibly lower, are acceptable (Caldwell 2002; Melchiorri et al. 2003). Note however that in the latter case, values of $w_\Omega$ below $-1$ cannot be obtained naturally through a standard scalar field. Single power law potentials suffer from the fact that, once quintessence dominates, the $w_\phi$ parameter approaches the asymptotic value $-1$ very slowly so that today, if the quintessence density parameter $\Omega_\Lambda$ is close to 0.7, then $w_\phi$ is still far from the value $-1$, contrary to what most analyses suggest. In order to avoid this problem, one has to add extra features in the potential, such as a rapid change in the slope of the potential or a local minimum, such as in the SUGRA model proposed by Brax & Martin (1999). Many other possibilities have been proposed since then (see for example references in Brax et al. 2000; Peebles & Ratra 2003).

On the other hand, without precise ideas about the correct quintessence model, it has become natural to adopt a more phenomenological approach in which one parametrizes the functional form of $w_\Omega(z)$ which exhibits the main features described above.

The simplest model of quintessence (in the sense that it introduces only one new parameter as compared to a $\Lambda$CDM model) is to assume a constant $w_\Omega$. However there is little motivation for constant $w_\Omega$ beyond the economical argument and it is increasingly recognized that evolving $w_\Omega$ should be investigated with a minimal number of priors. In the absence of well motivated theoretical considerations one is left with the empirical option to examine constraints on the analytical form for $w_\Omega(z)$. Most investigations have been based on expressions with one or two parameters. However, such expressions often vary with time in a relatively slow way and that rapidly varying expressions have to be examined as well. In other words, if one considers the typical time scale:

$$\tau_\Omega \sim \frac{w}{w-1},$$

constant $w$ corresponds to $\tau_\Omega \gg \tau_H$ where $\tau_H = 1/H$ is the Hubble time, a smoothly varying expression such as the inverse power law potential corresponds to $\tau_\Omega \sim \tau_H$ and a more rapidly varying $w$ correspond to $\tau_\Omega \ll \tau_H$, such as in the SUGRA model. Our aim is primarily to investigate constraints on models for which $\tau_\Omega \ll \tau_H$. This lead us to use the following model which allows arbitrary rapid transitions and in which the dark energy $w_\Omega$ parameter evolves as a function of the scale factor $a$ according to

$$w_\Omega(a) = \frac{1}{2}(w_1 + w_\infty) - \frac{1}{2}(w_1 - w_\infty) \tanh \left( \Gamma \log \left( \frac{a}{a_i} \right) \right),$$

The $w$ parameter goes from $w_1$ at early times to $w_\infty$ at late times, the transition occurring at $a_i$. The transition occurs at redshift $z_t = 1/a_i - 1$ (a negative value of which corresponds to a transition in the future) and lasts of the order of $\Gamma^{-1}$ Hubble times; $\Gamma$ is therefore a parameter describing the speed of the transition: high values ($\gg 1$) correspond to fast transitions, in the limit $\Gamma = \infty$ the transition is instantaneous. This expression was proposed by Linder & Huterer (2005). The quintessence conservation equation $D_\mu T_{\mu\nu}^\nu = 0$ can be integrated exactly giving to

$$\rho_\Omega(a) = \rho_\Omega^i \left( \frac{a}{a_i} \right)^{-3(1+w_\infty)} \left[ \left( \frac{a}{a_i} \right)^{\Gamma} \left( 1 + \frac{a}{a_i} \right)^{\Gamma} \right]^{\frac{\Delta w}{3}},$$

where we have set

$$w_{av} \equiv \frac{1}{2}(w_1 + w_\infty), \quad \Delta w \equiv (w_1 - w_\infty),$$

and where $\rho_\Omega^i$ corresponds to the values of the quintessence energy density at the present epoch. Therefore, the model can be implemented without much modification in existing cosmological codes such as CAMB (Lewis et al. 2000). Dark Energy perturbations are implemented accordingly to Riazuelo & Uzan (2002); Brax et al. (2000), i.e. the initial spectrum of the dark energy perturbation follows an attractor mechanism, exactly as the unperturbed part of the DE fluid does, and the DE initial spectrum is lost. One modification concerns the sound speed $c_s$ since in the SUGRA model, $c_s^2 = 1/3$.

With an increase of these parameters, the implementation of our model is such that the integral of the DE energy density $\Omega_\Lambda$ and $\Omega_\phi$ remains constant at late times.

$$\Omega_\Lambda(z) \sim \Omega_\Lambda^{i} \sim 0.7 \quad \text{and the duration of the transition is larger}$$
than the Hubble time (it depends on how steep the potential is, that is, on $\alpha$). For the SUGRA potential the first two above constraints on $w_l$ and $w_{00}$ remain, whereas the latter are modified: the epoch of transition for $w_Q$ no longer necessarily corresponds to the scalar field domination (but corresponds to the epoch where the field reaches a local minimum in its potential), and the transition duration is usually much shorter. Various other models have different predictions concerning these parameters, but the above parametrization is sufficiently general to encompass a large number of already proposed models.

One of these parameters, $w_l$, is not expected to be as relevant as the parameter $a_t$: because at early times $\Omega_Q(z)$ is negligible compared to $\Omega_m$, the quintessence field does not play a crucial role, at least with respect to supernovae and CMB data. One should impose a value of $w_l$ slightly lower than 0, in order to ensure that at early times $\Omega_Q \ll \Omega_m$. The reason is that with $w_l = 0$ and a low $z$ transition $\Omega_Q$ would be close to its present value at the recombination epoch (or even nucleosynthesis, see references in Peebles & Ratra 2003). At low redshift, this would lead to a dramatic suppression of the cosmological perturbation growth rate (Douspis et al. 2003). In addition, we found that this introduces additional changes in the $C_l$ curve at high $l$ (i.e., other than changes due to the modification of the angular distance). For these reasons we fix $w_l = -0.2$. Putting a constraint on $w_{00}$ is less desirable since it implicitly selects a limited class of models, which do not seem excluded by the data. We have chosen the value $w_{00} = -1$, which seems in agreement with the present data, and we focus on the two remaining parameters, $\Gamma$ and $a_t$ which describe the transition experienced by $w_Q(z)$ between its early and late behaviour.

3. Analysis

We focus here on constraints that can be set in the transition parameters $z_t$ and $\Gamma$, and we set $w_l = -0.2$ and $w_{00} = -1$ as explained above. Note that a pure cosmological constant behaviour is obtained by considering large $z_t$ with a sufficiently small transition duration (so that it does not last long after $z_t$).

3.1. Supernovae Hubble diagram

The luminosity distance is one of the main sources of constraint on the nature of dark energy (Astier 2001). We therefore first examine what kind of constraints the Supernovae Hubble diagram allows. The number of well observed SNIa has rapidly increased in recent years and a significant number of supernovae above redshift one have been detected. In the following we use the compilation from Davis et al. (2007) of recent SNIa (Wood-Vasey et al. 2007; Riess et al. 2007; Astier et al. 2006).

We have examined constraints on our three parameters, $a_t = 1/(1 + z_t)$, $\Gamma$ and $\Omega_Q$. We use the publicly available Monte Carlo Markov Chains code, cosmomc (Lewis & Bridle 2002), using the modified version of CAMB described above. 2D contours shown in Figs. 1 and 4 encompass 68% and 95% confidence levels (CL). In each figure, the third parameter is marginalised over.

The upper graph of Fig. 1 presents the allowed regions in the plane: $a_t = 1/(1 + z_t)$ versus the inverse duration of the transition $\Gamma$. The lower graph gives the constraints in the $a_t - \Omega_Q$ plane. Constraints on possible transitions appear very weak: only sharp transitions at very low redshift ($z_t < 0.1$ at the two sigma level) are firmly excluded. Surprisingly, the data suggest a transition at low redshift, a tendency that has been noticed elsewhere

Fig. 1. Contour constraints on the transition at epoch $a_t = 1/(1+z_t)$, and the rate of the transition $\Gamma$. The results are independent of $\Gamma$ when it is sufficiently large. Bottom figure shows the results in the $(\Omega_Q, a_t)$ plane.
the effect of changing $w_i$; changing $w_i$ from 0 to $-0.6$ produces changes that are small and easy to understand as the model becomes degenerate with the $\Lambda$CDM model.

For this reason, in the following, we concentrate our analysis on $a_t$.

We have redone the above analysis on $a_t$ for a simulated survey with the precision and statistics expected from space experiments. We generated 2000 supernovae distributed in 16 bins in redshift between 0.2 and 1.7 according to Table 1 of Kim et al. (2004) completed by 300 nearby supernovae. The number of supernovae per bin fluctuates according to a Poisson law. For a given bin, the magnitude of the supernovae is taken from a Gaussian distribution of the mean value given by the standard concordance $\Lambda$CDM model, and the sigma fixed to 0.2 mag. The resulting magnitude of each bin is obtained by a fit of the distribution of magnitudes and the associated error is added in quadrature with a systematic error of 0.02 mag and an offset error of 0.01 mag for the intercalibration between the two sets of data. The constraints inferred from this simulated sample again reveal that the transition epoch $a_t$ is moderately constrained: transitions at redshift as low as 0.5 (2$\sigma$ CL) are still acceptable when a rapid transition ($\Gamma > 2$) is assumed.

The situation is therefore paradoxical: although space survey precision improves the constraints by pushing the acceptable redshift from 0.25 to 0.5 (for rapid transitions), this last result is modest as a significant fraction of the high precision data provided by the experiment extends up to redshift ~2. The reason for this apparent paradox is clarified in Sect. 4.

### 3.2. Constraints from the CMB

Given that SNIa Hubble diagram hardly suggests the presence of a transition in the dark energy content of the universe, it is interesting to examine whether such a possibility could be acceptable using additional constraints. CMB is known to provide such constraints on the quintessence scenario, e.g. (Spergel et al. 2003; Douspis et al. 2003; Ödman et al. 2004). We therefore examine CMB constraints on the type of models introduced above, although we leave to a future work a full investigation of the constraints that can be set on this type of model. We use the WMAP 3 data-set, as well as CBI, VSA and Boomerang data at small scales, and a version of the CAMB cosmological code (Lewis et al. 2000) that we have modified. Modifications of the code are straightforward since its public version includes models with constant $w_0$, and we have implemented the energy density $\rho_Q(z)$ and the pressure $P_Q(z)$ as a function of redshift. Our ansatz for the equation of state parameter $w_0(z)$ allows us to integrate the conservation equation to obtain an analytical form for $\rho_Q(z)$.1

The angular power spectrum of CMB fluctuations in the presence of dark energy is modified mainly through the

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1 One has also to make the distinction between the equation of state parameter $w_0 = P_Q/\rho_Q$ and the “sound speed” squared $c^2_s = P_Q/\rho_Q$, which are identical when $w$ is constant.
modifications of the angular distance (Blanchard 1984) (see Fig. 3 and Elgaroy & Multamäki 2007). Although a strong dependence appears, this is partially lost through parameter degeneracies which strongly weaken the final constraints. In addition, ISW will contribute to lower levels as the transition is assumed at lower redshift, and this effect contributes to modify the angular power spectrum of the CMB fluctuations. We have investigated the CMB constraints on models with rapid transitions described by Eq. (2). $\Gamma$ was set to 10. We have checked that varying $\Gamma$ above 5 produces no appreciable differences. The other parameters that were left free are the baryon budget $\Omega_B$, the optical depth $\tau$, the Hubble constant $H_0$, the dark energy density at the present day $\Omega_Q$, the index of the primordial spectrum $n$, the amplitude of fluctuations $\sigma_8$ and the transition epoch $\alpha_t = 1/(1 + z_t)$. From the contours obtained in Fig. 4, one can see that the constraints that can be set on the transition redshift $z_t$ from the CMB are rather stringent, $z_t > 0.54$ (1$\sigma$ on one parameter) when $\Omega_Q$ represents less than 50% of the total density. These constraints being slightly dependent on $H_0$ we have also examined whether a combination of CMB and supernova data allows to improve the transition epoch constraints, but although the SNIa data restricted the dark energy density much more around $\Omega_Q \sim 0.7$, the final constraints do not represent a significant improvement: the final constraint shown in Fig. 4 is $z_t > 0.66$ (2$\sigma$ on one parameter). Some different dark energy models could in principle lead to different conclusions in the case where the sound speed varies in a way that significantly affects the integrated Sachs-Wolfe effect on large angular scales, even though no such model was found in our analysis. Clearly, better constraints could be obtained from additional data of cosmological relevance, but this is beyond the scope of the present paper.

4. Observing the Universe at $z = 0$ and at $z = 0.3$

In order to distinguish quintessence models from a pure cosmological constant, it is crucial to be able to track the dark energy evolution as early as possible. The main impact of dark energy comes from its influence on the expansion rate of the universe. An important question is therefore until what epoch the dark energy density plays a role in observable quantities, and as a corollary, until what epoch one can hope to reconstruct either its energy density or its equation of state parameter. As we have seen in Sect. 3, the SNIa Hubble diagram poorly constrains a possible transition epoch in the equation of state of the dark energy component. As we have stated, this appears somewhat paradoxical as data extending up to redshift 2 fail to reveal a transition occurring at redshifts as low as 0.25, at which the dark energy component is still dominant. Indeed, in a model with $\Omega_Q = 0.7$, $\Omega_m = 0.3$ today, with $w_0$ constant and equal to $-1$, the matter to dark energy transition, defined when $\Omega_Q(z) = \Omega_m(z) = 0.5$, occurs at redshift $z_t = (\Omega_0/\Omega_m)^{1/3} - 1 \sim 0.33$. Let us now consider two alternatives. First, we can consider a pure cosmological constant model, with $w_0 = -1$ also at early times. Second, we can consider a model where $w_0 \sim 0$ for $z > z_t$. In the first case, one has a usual LCDM model, whereas in the second case, one has a model close to a flat Einstein-de Sitter model at epoch $z > z_t$. An observer at $z = z_t$ should easily be able to distinguish between the two models, just as we are able to distinguish between a flat CDM model today, and a flat Einstein-de Sitter model today. Now, are we able to distinguish today between these two models, which differ only in $z > z_t$? Surprisingly, the answer is no if one considers supernovae data only, as is convincingly illustrated by Fig. 2. The explanation of this apparent paradox is as follows. Present data favour dark energy because high redshift supernovae are dimmer than expected in a flat Einstein-de Sitter universe. This is usually expressed as a difference of magnitude between the two models one considers for some standard candle at some redshift, the exact value of which depend on the quality of the data. The magnitude is essentially the logarithm of the luminosity distance as a function of the redshift. Let us define $d_L(z)$ and $d_L^{\text{ISW}}(z)$ the luminosity distance as a function of the redshift in a flat LCDM model with $\Omega_\Lambda = \Omega_m = 0.5$ today, and in a flat Einstein-de Sitter model. Let us assume these two models can be distinguished. Let us now consider $d_L(z)$ and $d_L^{\text{ISW}}(z)$ the luminosity distance vs. redshift relation in a flat LCDM model with $\Omega_\Lambda = \Omega_m = 0.3$ today, and in a flat energy model with $\Omega_Q = 0.7$, $\Omega_m = 0.3$ today, with $w_0$ experiencing a sudden transition from 0 to $-1$ at $z = z_t$. An observer at $z = z_t$ would therefore measure either $d_L(z')$ or $d_L^{\text{ISW}}(z')$. The epoch corresponding
to a redshift of $z'$ measured by an observer at $z_t$ corresponds to a redshift $z$ given by

$$z = (1 + z_t)(1 + z') - 1 = z_t + z' + z_t z', \quad (5)$$

measured by an observer today. Let us define $d_t$ as the luminosity distance of the observer at $z = z_t$ as seen from today. The exact value of $d_t$ does not matter here, but it can be computed as

$$d_t = \frac{1}{1 + z_t}.$$  \quad (6)

Luminosity distances do not add but are proportional to comoving distances. The luminosity distance at redshifts above $z_t$ is therefore given by

$$d^h_L(z) = \frac{1 + z}{1 + z_t} d_t + \frac{1 + z}{1 + z_t} d^h_L(z'),$$  \quad (7)

$$d^0_L(z) = \frac{1 + z}{1 + z_t} d_t + \frac{1 + z}{1 + z_t} d^0_L(z'),$$  \quad (8)

in the two models. Now, in term of difference of magnitude between the two models, this is translated into

$$\Delta m(z) \propto \log \frac{d_t + \frac{1 + z}{1 + z_t} d^h_L(z')}{d_t + \frac{1 + z}{1 + z_t} d^0_L(z')},$$  \quad (9)

whereas for the observer at $z_t$, this simply gives

$$\Delta m(z') \propto \log \frac{d^h_L(z')}{d^0_L(z')}.$$  \quad (10)

Two differences arise here. First, the redshift range which today’s observer must use in order to distinguish between the two models is larger than that of the observer at $z_t$. If the latter must collect data between $z' = 0$ and $z' = z$, say, then the former must observe supernovae between $z(0) = z_t$ and $z(z_t) = z_t + z_t + z_t > z_t + z$. Second, the magnitude difference between the two models is strongly attenuated for the observer today because of the presence of the extra term $d_t$ both in the numerator and the denominator of Eq. (9). This behavior is somewhat surprising at first but can be understood from the expression of the comoving coordinate $r$:

$$r(z) = \int_0^z \frac{dz}{H(z)},$$  \quad (11)

where $H(z)$ follow the Friedmann-Lemaître equation:

$$H^2(z) = 8\pi G\rho_m + \rho_Q$$  \quad (12)

(for $k = 0$). Let us assume that a rapid transition occurs at $z = z_t$ between $w = -1$ and $w = 0$; it is straightforward to compute the relation between the Hubble constant $H(z)$ in such a model to the Hubble constant $H(z_t)$ in the standard model:

$$\frac{H^2(z)}{H^2(z_t)} = \frac{1 + \frac{1}{3+4k_0(z_t)}}{1 + \frac{1}{3+4k_0(z+1)}},$$  \quad (13)

It is clear from this expression that the values of the Hubble constant in the two models do not differ by much when the transition redshift is not close to zero. As the integrand in the calculation of $r$ is higher at low redshift, the limited difference in $H$ translates to a small difference in $r$. For instance a transition at $a_t \sim 0.7$ results in a 5% decrease in $r$ at redshift 1 corresponding to $\Delta m \sim 0.1$ as can be seen in Fig. 2.

The net result is that while both models are easy to distinguish at $z = 0.3$, this is no longer the case at $z = 0$ as seen in Fig. 5.

**5. Conclusion**

We have investigated a class of models that undergo a rapid transition in the equation of state of their dark energy component. In order to establish the constraints that can be obtained on the characteristics of the transition we have focused our study on a class of models in which dark energy transits rapidly between $w \sim 0$ and $w \sim -1$. We found that the duration of the transition cannot be constrained when it is shorter than the Hubble time. More surprisingly we found that SNIa Hubble diagram does not constrain this type of scenario very much, as even with the data expected from space experiments a transition can still be allowed at epochs when the dark energy density represents 40% of the density of the Universe. This suggests that the SNIa diagram is poorly sensitive to dynamics of dark energy at redshifts above 0.5. On the contrary, we found that existing CMB data, in combination with SNIa data, provide tight constraints on this type of scenario, allowing rapid transitions to happen only at redshifts beyond 0.66, when dark energy represents less than 10% of the total density of the Universe. This illustrates the importance of combinations of various data in order to accurately constrain the evolution of dark energy.

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