Solar off-limb line widths: Alfvén waves, ion-cyclotron waves, and preferential heating

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ABSTRACT

Context. Alfvén waves and ion-cyclotron absorption of high-frequency waves are frequently brought into models devoted to coronal heating and fast solar-wind acceleration. Signatures of ion-cyclotron resonance have already been observed in situ in the solar wind (HELIOS spacecrafts) and, recently, in the upper corona (UVCS/SOHO remote-sensing results).

Aims. We propose a method to constrain both the Alfvén wave amplitude and the preferential heating induced by ion-cyclotron resonance, above a partially developed polar coronal hole observed with the SUMER/SOHO spectrometer.

Methods. The instrumental stray light contribution is first subtracted from the spectra. By supposing that the non-thermal velocity is related to the Alfvén wave amplitude, it is constrained through a density diagnostic and the gradient of the width of the Mg $\lambda 625$ Å line. The temperatures of several coronal ions, as functions of the distance above the limb, are then determined by subtracting the non-thermal component to the observed line widths.

Results. The effect of stray light explains the apparent decrease with height in the width of several spectral lines, this decrease usually starting about 0.1–0.2 $R_\odot$ above the limb. This result rules out any direct evidence of damping of the Alfvén waves, often suggested by other authors. We also find that the ions with the smallest charge-to-mass ratios are the hottest ones at a fixed altitude and that they are subject to a stronger heating, as compared to the others, between 57\arcsec and 102\arcsec above the limb. This constitutes a serious clue to ion-cyclotron preferential heating.

Key words. Sun: corona – Sun: UV radiation – line: profiles

1. Introduction

Ion-cyclotron resonance is often suggested as one of the possible processes that accelerate the fast solar wind and heat the corona. Different modelling approaches are used, like hybrid simulations (e.g. Lieuwer et al. 1999; Ofman 2004), kinetic models (Isenberg et al. 2001; Isenberg 2001; Marsch & Tu 2001; Vocks & Marsch 2002), or fluid models. In this last category Cramer et al. (1999a) for example, include several ion species and show that it is necessary to regenerate the cyclotron waves through the wind to provide enough energy to the wind. This may be done, for example, by including an Alfvén wave turbulent cascade, as in Tu & Marsch (1997) (two fluids) or Hu et al. (2000) (four fluids), while Markovskii (2001) and Markovskii & Hollweg (2002) study the direct generation of cyclotron waves via plasma instabilities.

In the models that use turbulent cascade, the Alfvén wave power is distributed into a power law spectrum, with ion-cyclotron waves being its high frequency limit. On the one hand, these waves are gradually absorbed by the particles as the different local ion gyrofrequencies decrease with altitude and match the wave frequency, taking into account the Doppler effect due to the particle velocity (for the theoretical aspects of the cyclotron absorption, see e.g. Hollweg & Isenberg 2002). On the other hand, they replenish through the energy cascade process from low to high frequencies. The large decrease in the magnetic field intensity because of the rapid expansion of the flux tubes can favour the resonance occurring at a relatively low altitude above the solar surface, as in the so-called “funnels” (e.g. Hackenberg et al. 2000; Li 2002). In this respect, the superradial expansion of the flux tubes in coronal holes (Kopp & Holzer 1976), which are thought to be the source of the fast solar wind, is also important.

In some models, Alfvén waves are directly dissipated to provide energy to the wind. According to Parker (1991), though, this dissipation is not significant below 5 $R_\odot$, so that it is more likely that Alfvén waves stay undamped in the low corona.

Several signatures of wave-particle interaction, which can be attributed to the ion-cyclotron resonance, have already been observed in the solar wind. The in situ observations of the Helios spacecrafts, for example, showed differential speed of minor heavy ions, anisotropies of temperatures ($T_\parallel/T_\perp$), and preferential heating of some ion species (Schwenn & Marsch 1991). In the upper corona, the UVCS spectro-coronometer on board SOHO made it possible to observe the same kinds of signatures from 2.5 to more than 5 $R_\odot$ from disc centre, through spectroscopic studies coupled to some modelling (Li et al. 1998; Kohl et al. 1998; Cramer et al. 1999b; Esser et al. 1999). In the lower corona, in contrast, there is lack of conclusive studies, and yet it is particularly important to verify whether any process that accelerates the fast solar wind starts acting in the lower corona. Observing this region is also important for constraining the energy actually dissipated by the cyclotron resonance and for differentiating the different theories that have been proposed.

In this article, we concentrate on the possibility of revealing the preferential heating of the ion species having the lowest charge-to-mass ratios ($q/m$). Retrieving the temperature of...
different ion species can be made via the analysis of the widths of emission lines. It is worthwhile noting that the temperature diagnostics based on line ratios are sensitive to the electron temperature and cannot help in measuring the ion one.

Our paper is organised as follows. In Sect. 2, we present the usual interpretation of the coronal line widths and of their variations above the limb, as well as solutions proposed in the literature for distinguishing the thermal and the non-thermal components. In Sect. 3, we present the observations and the associated data processing, with emphasis on the correction for the stray light contribution in the spectra. In Sect. 4, we explain the method we used to separate thermal and non-thermal Doppler effects in the measured line widths. The results are presented in Sect. 5, while Sect. 6 gives the conclusions.

2. Retrieving the information contained in coronal line widths

2.1. Interpretation of the VUV line widths of coronal ions

The plasma observed above the limb is thinest for most of the transition region and coronal lines in the VUV range observed by instruments like SUMER (Dere & Mason 1993; Chae et al. 1998; Lee et al. 2000). The two main contributions to the line width then come from thermal and non-thermal Doppler effects. The non-thermal velocity, also known as “unresolved” velocity, ξ was originally introduced to interpret the width of the transition region and coronal lines observed on the disc. In fact, there is an excess broadening as compared to the thermal component due to the formation temperature \( T_f \) of these lines. This additional contribution was first attributed to velocity fluctuations induced by acoustic waves (Boland et al. 1973), before MHD waves or fluid turbulence were considered (e.g. Boland et al. 1975; Hassler et al. 1990; Doyle et al. 1999; Harrison et al. 2002). The term “unresolved velocity” in fact refers to motions on scales smaller than the resolution scale. One should also take into account the motions integrated on the depth of the line of sight (LOS), and on scales smaller than the temporal resolution of the instrument. If both thermal and non-thermal contributions are Gaussian (Tu et al. 1998), the half-width \( \sigma \) at 1/\( \sqrt{e} \) follows the formula given by Dere & Mason (1993):

\[
\sigma^2 = \frac{\lambda^2}{2c} \left( \frac{2kT}{m} + \xi^2 \right)
\]

where \( \lambda \) is the wavelength, \( c \) the speed of light, \( k \) the Boltzmann constant. The non-thermal velocity \( \xi \) is proportional to the mean velocity fluctuations integrated on the observed solid angle and the exposure time, \( (\delta v^2)^{1/2} \). The coefficient of proportionality, relatively close to 1, depends on the degrees of freedom of the fluid motion (e.g. Tu et al. 1998).

Variations in the non-thermal velocity have been investigated by several authors: (i) centre-to-limb variations by Mariska et al. (1978), Chae et al. (1998), Lee et al. (2000), Doyle et al. (2000), see also Erdelyi et al. (1998) for the interpretation in terms of MHD modes; (ii) variation depending on the nature of the observed region (coronal holes, “quiet Sun”, active region); and (iii) radial variation out of the limb, which is of interest for this article and which we will present in the next section. Depending on all these different conditions, the value of \( \xi \) varies roughly from 10 to 30 km s\(^{-1}\).

From on-disc observations, we retain the results of Chae et al. (1998), which assumed that the temperature of each ion species that they observed was the corresponding formation temperature \( T_f \). They consequently deduced the non-thermal velocity from the line widths, and plotted it as a function of \( T_f \). The same kind of analysis was also performed by, e.g., Boland et al. (1975) and Dere & Mason (1993). The curve of Chae et al. (1998) increases from \( \approx 5 \) km s\(^{-1}\) at 10\(^6\) K up to \( \approx 30 \) km s\(^{-1}\) around \( 3 \times 10^5 \) K (O VI), then decreases to \( \approx 17 \) km s\(^{-1}\) at 10\(^7\) K (Fe XII). One can roughly interpret this curve in terms of LOS integration: different \( T_f \) of ions observed at the same pointing on the disc can be associated to different altitudes above the solar surface. The curve then traces the value of the non-thermal velocity through the different temperature layers of the solar atmosphere (Mariska et al. 1978).

2.2. Past observations of line widths above the solar limb

Most authors who have observed above the limb, in coronal holes, report that the line widths first increase with the altitude before presenting a plateau or, sometimes, starting to decrease at 1.1 \( R_\odot \) from disc centre: e.g. Hassler et al. (1990), with the Mg X 609 and 625 Å lines up to 1.2 \( R_\odot \), or Banerjee et al. (1998), with SUMER/SOHO observing the Si VIII 1445 Å line. These authors interpreted this behaviour as caused by Alfvén waves, with the increase due to flux conservation and decrease due to damping. Using CDS/SOHO, O’Shea et al. (2003) observed the width of the Mg X 625 Å line starting to decrease around 1.06 \( R_\odot \), the exact position varying with the data sets, but always for the same value of the line widths. But O’Shea et al. (2004), when observing the Si XII 520 Å line in addition to the two Mg X 609 and 625 Å lines, found a discrepancy between both species and concluded that the behaviour of the Mg X lines results from photoexcitation growing as the altitude increases. Still above a coronal hole, using SUMER, Lee et al. (2000) found a link between the altitude where the line widths change their behaviour and the intensity scale height. Nevertheless, they used a lot of particularly cold lines, which they could not observe more than 20″ above the limb. They also found a curve \( \xi = f(T_f) \) as did Chae et al. (1998).

Above a quiet Sun region at the equator, Harrison et al. (2002) observed a decrease in the line width of the Mg X 625 Å line, with CDS, starting at about 1.04 \( R_\odot \), the width being narrower than above coronal holes. They linked this behaviour to the damping of Alfvén waves in close field loops. Wilhelm et al. (2004), using SUMER still at the equator but at a different date, did not find the same behaviour. The results of both instruments were reconciled after joint observations (Wilhelm et al. 2005) that revealed no decrease, but a slight plateau. Besides, Peter & Vocks (2003) observed a local maximum of the widths of transition region lines (O V and S VI), less than 10\(^{-1} \) (\( \approx 0.01 \) \( R_\odot \)) above the limb, which they attribute to the dissipation of ion-cyclotron waves, the decrease at higher altitudes being due to collisional cooling when the ion-cyclotron dissipation vanishes.

Singh et al. (2003a,b) analysed ground-based observations of Fe X, Fe XIII, and Fe XIV lines (visible and infrared), up to 140″ in streamers. On average, the Fe X 6374 Å line width increases with altitude, those of the Fe XIII 10747 and 10798 Å lines increase slightly less, whereas that of the Fe XIV 5303 Å line decreases slightly. Concluding that the line-width behaviour depends on the formation temperature, they reject the interpretation in terms of variation of Alfvén wave amplitude and prefer to explain it by an LOS effect in a thermally stratified corona. Still from the ground, Contesse et al. (2004) observe no clear decrease in the width of the Fe XIV 5303 Å line, but instead a
plateau up to 1.5 $R_\odot$ at the equator (east and west) and up to 1.2 $R_\odot$ above both poles, the observed line widths being larger above the poles than above the equatorial regions.

Using UVCS/SOHO, it is possible to observe several solar radii above the solar limb, essentially the H i part of the corona, i.e. above 2 $R_\odot$ from disc centre, than in the lower one (Li et al. 1998; Kohl et al. 1998; Cranmer et al. 1999b; Esser et al. 1999; Frazin et al. 1999; Doyle et al. 1999; Morgan & Habbal 2004).

2.3. Distinguishing thermal and non-thermal Doppler effects

The line width contains information about the result of potential heatings (the temperature $T_i$ of the different ions species) and about the possible source of heating, that is to say, the Alfvén wave amplitude via direct dissipation or via ion-cyclotron resonance after a turbulent cascade. All difficulties come from these two pieces of information merged in only one observable. Most methods used in the literature consist in making an assumption about one of the above quantities, depending on the purpose of the authors, i.e. constraining the Alfvén wave amplitude or revealing any preferential heating.

One can find mostly two kinds of hypotheses on the ion temperature: the isothermal or the formation temperature hypotheses. One example of isothermal hypothesis can be found in Feldman et al. (2000) or Doschek et al. (2001). They determine the electron temperature through the emission measure and assume that all species are in thermal equilibrium. Then, they find different values of $\xi$ for the different ion species and discuss about possible errors to explain why they do not obtain a unique value for $\xi$. In fact, Moran (2003) shows for a coronal hole that it is not possible for all ion species to have the same temperature and the same non-thermal velocity at the same time.

Numerous authors prefer to assume that the temperature $T_i$ of each ion is the formation temperature of the line (e.g. Hassler et al. 1990; Contesse et al. 2004). But this supposes ionization equilibrium, while several authors think that the plasma above coronal holes is weakly collisional (Tu et al. 1998; Banerjee et al. 1998). When a preferential heating process, like ion-cyclotron resonance, is at work on time scales smaller than the collisional cooling (cf. Table 1), the assumption $T_i = T_e$ no longer makes sense.

Doyle et al. (1999), for a coronal hole, use a more elaborated hypothesis for the temperature. They suppose that the electron temperature $T_e$ is equal to the formation temperature of the observed Si VIII line and deduce the proton temperature $T_p$ from hydrostatic equilibrium, constrained by a density diagnostic. Then, they suppose that $T_{\text{Si VIII}} = T_p$ (and $T_p > T_e$) before they deduce $\xi$ from the Si VIII line width.

The first hypothesis about the non-thermal velocity $\xi$ that can be made is that all ion species have the same $\xi$. This is reasonable if this velocity comes from fluid motions, i.e. regardless of the species; this may be false if some species have high differential speeds (Hollweg & Isenberg 2002), which should not be the case in the lower corona. The problem is then to determine the value of $\xi$. Seely et al. (1997) adjust $\xi$ so that the temperature of the Fe ion species, i.e. the heaviest element they observe, is similar to that of ion species of neighbouring $T_i$, as they suppose that all ion species that have a common $T_i$ are in thermal equilibrium. They then deduce the temperature of all the other ion species, which appear to be larger than their own formation temperature; the lower the formation temperature, the larger the difference. These authors conclude that this situation may come from out-of-equilibrium processes (heating or cooling phase) or from preferential heating. They also conclude that the underestimation of the ion temperatures led Hassler et al. (1990) to overestimate $\xi$ at altitudes of 100–200 arcsec.

When looking for the signature of preferential heating in coronal holes, Tu et al. (1998) cautiously give an upper and a lower limit to $\xi$. The lower one being 0, they set the upper one by setting to zero the thermal width of the lines from the heaviest ion having the smallest Doppler width (Fe XII) in their data set. Then, they constrain the temperature of all ion species, and note a stronger heating of ions having the smallest $q/m$ between about 1.04 and 1.18 $R_\odot$.

One possibility for better constraining $\xi$ is to suppose that the non-thermal velocity is solely due to undamped Alfvén waves. To conserve the wave energy in an expanding flux tube, while the mass density $\rho$ decreases, the wave amplitude must increase so that (e.g. Moran 2001)

$$\xi \propto \rho^{-1/4}. \quad (2)$$

The line-width variation with the altitude has been analysed with respect to this effect in Hassler et al. (1990) for Mg X and Banerjee et al. (1998) and Pekkimli et al. (2002) for Si VIII.

Conclusions that can be drawn from the study of VUV solar line widths appear to strongly depend on the method used to separate the thermal from the non-thermal contribution. Two points emerge from past studies: (i) the probable existence of a non-thermal velocity whose radial behaviour above the limb mimics that of undamped Alfvén wave amplitude. The question of whether these waves begin to damp at a certain point above the solar surface does not seem to have been solved. (ii) Another process may be at work that affects different lines in different ways. A $q/m$ dependence is suspected that could be associated to ion-cyclotron resonance.

The purpose of this article is to verify and constrain both of these two points without using hypotheses that a priori preclude one of them. We will focus on observations of a polar coronal hole, below 1.2 $R_\odot$. To avoid bias resulting from the line formation (e.g. photoexcitation) and from unknown line blendings, it seems useful to observe as many lines as possible. A wide range of masses and $q/m$ of the ion species also favour the distinction between the relative contribution of thermal and non-thermal velocity in the observed line widths.

<table>
<thead>
<tr>
<th>Species</th>
<th>$q/m^2$</th>
<th>$\tau_e (s)^p$</th>
<th>$\tau_p (s)^p$</th>
</tr>
</thead>
<tbody>
<tr>
<td>e−</td>
<td>1758</td>
<td>$4 \times 10^{-7}$</td>
<td>120</td>
</tr>
<tr>
<td>p+</td>
<td>1</td>
<td>$6 \times 10^{-3}$</td>
<td>3</td>
</tr>
<tr>
<td>Mg X</td>
<td>0.37</td>
<td>$2 \times 10^{-3}$</td>
<td>1</td>
</tr>
<tr>
<td>Fe X</td>
<td>0.16</td>
<td>$4 \times 10^{-3}$</td>
<td>2</td>
</tr>
</tbody>
</table>

*Charge-to-mass ratio, normalized to the proton one. Mg X and Fe X are the ion species having the highest and lowest values of $q/m$, respectively, in the spectrum observed by SUMER.

b $\tau_e = 2 \pi \frac{m_e}{q} B$, with $q$ the charge and $m$ the mass of the particle, and $B$ the magnetic field.

c Heat exchange time with protons $\tau_{\text{ex}}^m$ and $\tau_{\text{ex}}^e$ (e.g. Wesson 2004, p. 68).

All these times are calculated with the following conditions: $B = 1$ Gauss, electron density $n_e = 10^{14}$ m$^{-3}$, and proton and electron temperatures both equal to $10^6$ K ($\beta = 0.35$).
Table 2. Description of data sets.

<table>
<thead>
<tr>
<th>Data set</th>
<th>Date</th>
<th>Position</th>
<th>$R_s$ (arcsec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>30 May 2002</td>
<td>$X = 0, Y = 1150$</td>
<td>956.5</td>
</tr>
<tr>
<td>2</td>
<td>28 May 2002</td>
<td>$X = 0, Y = -1150$</td>
<td>956.5</td>
</tr>
<tr>
<td>3</td>
<td>19 Nov. 2003</td>
<td>$X = 0, Y = 1145$</td>
<td>980.0</td>
</tr>
<tr>
<td>4</td>
<td>12 June 2004</td>
<td>$X = 0, Y = -1140$</td>
<td>960.0</td>
</tr>
</tbody>
</table>

a Observations are all made with the $1^\prime\prime \times 300^\prime\prime$ slit, and detector A. In data sets 2–4, only the Mg $625$ Å line was analysed in the present paper, for comparison purpose.

b Position of the centre of the slit, in arcseconds from disc centre.

c Solar radii as seen from SOHO.

3. Observations and data processing

The VUV Spectrometer SUMER on board the SOHO spacecraft is described in Wilhelm et al. (1995), Wilhelm et al. (1997), and Lemaire et al. (1997). Table 2 briefly presents all data sets used in this article. The main one, called set 1, consists of ten spectral ranges, observed using detector A on 30 May 2002 during MEDOC Campaign #9. The lines of interest are listed in Table 3. The complete observation was about 13 h long. The centre of the slit was pointed at $X = 0^\prime\prime, Y = 1150^\prime\prime$ (i.e. at the North Pole). The $1^\prime\prime \times 300^\prime\prime$ slit was used, oriented in the north-south direction, covering a wide range of altitudes at the same time (from about 50$^\prime\prime$ to 350$^\prime\prime$ above the solar limb, with an apparent solar radius of 956$^\prime\prime$). The width of $1^\prime\prime$ reaches a compromise between the photon statistics and the instrumental width.

The EIT/SOHO images on that day (Fig. 1) show that the coronal hole appearing on the solar disc at the North Pole is not developed well. Inspection of EIT movies of the preceding and following solar rotations reveals that the coronal hole is far from being symmetric, and highly elongated along one particular direction towards the equator. Nonetheless, it appears that some part of the coronal hole is lying right under the position we are pointing at in the plane of the sky, and LASCO images show no streamer on the north-south axis. However, we cannot dismiss the possibility of a contamination of the LOS by any plasma belonging to non-hole (i.e. “Quiet Sun”, QS) part of the corona. To gain more confidence, we compared the behaviour of the width of the Mg X $625$ Å line (observed at 1249.88 Å in second order) in three other data sets. Data set 2 corresponds to the south pole observed two days before data set 1 (same altitude range); the EIT survey shows that there is no coronal hole at the south pole at this period. Data sets 3 and 4 correspond to other polar coronal holes (CH). Figure 2 shows that the behaviour of the line width in set 1 compares well to those in sets 3 and 4, because it keeps increasing at low altitudes and then decreases at the highest altitudes. In contrast, data set 2 displays a different behaviour, with a large plateau starting from 60$^\prime\prime$, and it will be analysed more thoroughly in a future paper. According to Wilhelm et al. (2004), the Mg X $609$ and $625$ Å line widths are larger in coronal holes than in the Quiet corona (by more than 30% at 100$^\prime\prime$). Data sets 1 to 4 do not show such large differences. The maximum one is between sets 1 and 2, and the Mg X line width in set 1 is only larger than that of set 2 by $\approx 4\%$ at 100$^\prime\prime$. In fact, from 60$^\prime\prime$ to 100$^\prime\prime$, our values are higher than those of Wilhelm et al. (2004) in the Quiet corona by about 15% and lower than those in coronal holes by about 15%. Nevertheless, they are closer to what was observed by Doschek et al. (2001) in coronal holes, although a contamination by non-hole material cannot be dismissed, especially because the magnetic topology is far from being as simple as during solar minima. The density, discussed in Sect. 4.1, is similar to what has been previously measured in coronal holes. A density diagnostic has been made using additional data acquired on 30 May 2002. The lines of Si viii at 1440 and 1445 Å were observed by SUMER, covering the same field of view as
data set 1, with a 4′′ × 300″ slit. This wider slit thus provides better photon statistics for the line ratio, at the expense of an optimal instrumental width. The total exposure time was about 2 h and 50 min.

Raw data were corrected using the standard SUMER procedures provided by Solar Software (flatfield and geometric distortion of the detector). Note that the observation of faint lines with long exposure times is only possible because the detector noise is low, ≈ 3 × 10^3 counts s^-1 px^-1 (Wilhelm et al. 1997), which makes ≈ 0.1 counts px^-1 for a 1-h exposure time. The final spectra were obtained through the addition of consecutive 300 s exposures, after visual inspection of each exposure. The complete detector image was recovered (1024 × 360 pixels, wavelength × spatial dimension Y). The instrument is stigmatic in the spatial dimension Y, with a theoretical spatial resolution around 1 ″. For better statistics, several spatial pixels were added before analysing the spectral profiles. These intervals appeared to be narrow enough to avoid any significant artificial broadening of the lines owing to the residual distortion of the detector. A rough estimate of the altitude corresponding to each spectrum was provided through the pointing coordinates of the instrument.

3.1. Correction from the instrumental stray light

As SUMER is not a coronagraph (no occultor is included), the solar disc produces stray light during off-limb observations, essentially via the point-spread function properties induced by defects in the reflective surfaces, of spatial sizes of the same order of magnitude as the observed wavelength. Note that, whatever the pointing is, the complete image of the Sun is permanently formed by the main parabola.

This instrumental stray light is negligible for on-disc observations, but the contamination increases as the altitude of observation above the limb increases, until it is responsible for the quasi-complete photon rate detected above 1.6 R⊙ (Feldman et al. 1999). This problem is even more critical in coronal holes than above the “quiet” corona, as the emissivity is lower. Consequently, each off-limb spectrum is the sum of the real spectrum emitted by the corona and of the stray-light spectrum. At each point of the image of the Sun produced by the mirror, the intensity of the stray light results from contributions convolved over the entire source (disc plus corona seen above the limb). But the main contribution comes from the disc, where the different regions (active regions, coronal holes, and “Quiet Sun”) emit different spectra. This results in a stray-light spectrum that varies with the position and date of observations.

Every line that can be observed on the disc contributes to the stray-light spectrum observed above the limb, so that coronal lines (Mg X 625 Å, Fe XII 1242 Å, etc.) are not only blended with their own stray light, but they can also be blended with colder lines of neighbouring wavelengths. This last effect is usually underestimated.

To correct for the instrumental stray light, we used a method already described in Dolla et al. (2003), Dolla et al. (2004), and Dolla (2006), which enabled us to predict the stray-light spectrum contaminating the coronal spectrum observed at any altitude. This predicted spectrum is then subtracted from the off-limb spectrum (see also Banerjee et al. 2000; Singh et al. 2003a,b). For the observed spectral ranges, a reference spectrum was taken well above the limb, so that the spectrum can be considered as purely due to stray light. All reference spectra were acquired with a long exposure (several hours), usually pointing at (X = 0″, Y = 1700″). The same slit was used as for the off-limb spectra. The stray-light spectrum is then predicted at any lower altitude by determining the factor that makes the total counts in a reference cold line coincide in both the observed off-limb spectrum and the predicted stray-light spectrum. If no line offers sufficient statistics, one can use the continuum, such as for the Fe X/Fe XI spectral range, near 1465 Å. Some examples of stray light prediction are shown in Fig. 3 (see also Dolla et al. 2003, 2004; Dolla 2006).

We showed in Dolla et al. (2003) that reference spectra taken directly on the disc pointing at a “quiet Sun” region, and averaged over all the spatial pixels observed by the slit, do not allow a precise prediction of the stray-light spectrum, because these spectra do not take every kind of region on the disc into account. With high-altitude spectra, on the contrary, the convolution on the entire disc has already been performed. This also avoids modeling it like in Gabriel et al. (2003). Of course, the extrapolation of the high-altitude spectrum as a stray-light reference at any altitude is not totally correct, as the different contributions from the different areas of the disc are modified. This affects the ratios between the predicted lines, but the relative error on this ratio becomes more negligible as the altitude increases (cf. Feldman et al. 1999; Doschek & Feldman 2000), precisely as the absolute correction increases.

During the observations, a high-altitude reference spectrum for the stray light was not taken for every spectral range observed at lower altitudes in the corona. In particular, judging from previous SUMER data and from spectral lines atlases, we thought that this was not necessary for the Si VIII 1440 and 1445 Å lines. Nevertheless, Fig. 4 shows a bump in the blue wing, growing as the altitude increases. The same bump can be found in different data sets, so that statistical error is excluded. A possible stray light contamination, also noticed by Banerjee et al. (1998), may explain it. We suspect that another bump is present on the red wing. In fact, these bumps do not appear when using the 4″ slit, probably because the wider instrumental profile smoothes the emission profiles.

According to Ekberg & Feldman (2003), the Si XI 604.15 Å line is blended with an Fe VII line. The blending line is a cold one (class "b", following the designation of Feldman et al. 1997), so that any direct blending is probably negligible above the limb. A stray light contamination is likely, but has been underestimated at the time of the data acquisition, and no high-altitude spectrum is available for the stray light determination.

3.2. Gaussian width

The half-width at 1/√e is provided through a least-square Gaussian fit including a second-order polynomial. The spectrum corrected for the stray light is in counts px^-1, so as to use statistical errors as weights. The width in pixels is turned into angstroms by using the known dispersion of the spectrometer. The equivalent size of a pixel ranges from 42 to 45 mÅ in first order, depending on the observed wavelength. No precise calibration of the line wavelength is necessary, and we used the values given by Feldman et al. (1997). The fitting procedure provides a 1-sigma error on the width, which we set to 0.1 pixel as a minimum. When the counts at line maximum were below 150 or so, the fitting procedure became unstable, so that we only show results of lines presenting more than 150 counts at their maximum.

The spectrum observed on the detector corresponds to the convolution of the spectrum arriving at the aperture of the spectrometer with the instrumental profile. This profile mainly comes
The non-thermal velocity is not well-constrained prevents direct conclusion about the preferential heating, by plotting either the temperature at a given altitude or the difference in temperature between two altitudes, as a function of \( q/m \). In effect, owing to the small number of available lines, the ion species that are more likely to take advantage of cyclotron heating, i.e. having low \( q/m \) ratios, are also those with low \( 1/m \) ratios, that is to say, those whose width is more sensitive to the value of \( \xi \) (cf. Eq. (1)).

Instead of making an assumption on the value of \( \xi \), we preferred to make an assumption on its nature. If we suppose that Alfvén waves are responsible for the non-thermal velocity, then its radial variation can be constrained using Eq. (2) and a density diagnostic. We also consider that the Mg x species, having the highest \( q/m \) ratio in our data set, is less likely to be heated through the cyclotron resonance, and we suppose that its line width will only increase because of an increase in the non-thermal velocity. This hypothesis will then be verified a posteriori on a given interval.

4. Method of separating the two contributions in the coronal line widths

As shown in Dolla et al. (2004), the non-thermal velocity is not well-constrained prevents direct conclusion about the preferential heating, by plotting either the temperature at a given altitude or the difference in temperature between two altitudes, as a function of \( q/m \). In effect, owing to the small number of available lines, the ion species that are more likely to take advantage of cyclotron heating, i.e. having low \( q/m \) ratios, are also those with low \( 1/m \) ratios, that is to say, those whose width is more sensitive to the value of \( \xi \) (cf. Eq. (1)).

Instead of making an assumption on the value of \( \xi \), we preferred to make an assumption on its nature. If we suppose that Alfvén waves are responsible for the non-thermal velocity, then its radial variation can be constrained using Eq. (2) and a density diagnostic. We also consider that the Mg x species, having the highest \( q/m \) ratio in our data set, is less likely to be heated through the cyclotron resonance, and we suppose that its line width will only increase because of an increase in the non-thermal velocity. This hypothesis will then be verified a posteriori on a given interval.

4.1. Density diagnostic

The Si viii spectra are produced by a running sum over 40 pixels in the spatial direction of the detector. The total counts in the spectral ranges corresponding to both Si viii lines (1440 and 1445 Å) are integrated. The continuum contribution is then subtracted. The mass density \( \rho \) can be obtained through the electron density \( n_e \), which is derived in Fig. 5 from the theoretical curve linking the line ratio (1445/1440) to the electron density (Doschek et al. 1997, their Fig. 1).

Above 270″, the measured line ratio becomes lower than 1, so that no solution is given by the diagnostic. The Si viii line ratio becomes far less sensitive at electron densities below \( 10^7 \) cm\(^{-3} \) and the 1445 Å line suffer from the stray light mentioned above. For all these reasons, we have less confidence in the results above 180″.

These density values are similar to those of Doschek et al. (1997) measured in a polar coronal hole and at the same altitude range. They nevertheless decrease more rapidly with the altitude.

4.2. Determination of \( \xi \) at the lowest altitude

Equation (1) can be rewritten as the quadratic sum of thermal and non-thermal velocity:

\[
v^2 = \frac{2kT}{m} + \xi^2.
\]

By using the assumption that the Mg X 625 Å line-width variation is solely due to a variation in \( \xi \) between positions \( r_0 \) and \( r \) (i.e. \( \Delta T(r) = T(r) - T(r_0) \), with \( r_0 \) the lowest position in data set 1 i.e. at the bottom of the slit), we can write

\[
\Delta v^2(r) = v^2(r) - v^2(r_0) = \xi^2(r) - \xi^2(r_0).
\]

A new procedure con_width_funct_4 differs only for detector B.

Fig. 3. Examples of stray-light spectrum predictions for a spectral range covering \( \approx 40 \) Å around the Si viii line at 944 Å (data set 2). Each observed off-limb spectrum (in grey) is the sum of an instrumental stray-light spectrum (predicted in black) and of the real coronal spectrum. As the altitude increases (here, from 60 to 134 and 253 arcsec above the limb), several cold lines become more prominent in the off-limb spectrum (like H i and S vi lines, here). Meanwhile, some coronal lines become more and more contaminated by the blending with neighbouring cold lines (like Si viii blended with S vii); blending can also be caused by the same coronal line when this one is prominent in on-disc spectra (e.g., for Mg x around 1250 Å in second order). In these figures, spectra are in counts per wavelength pixels (with integration over wider spatial ranges for increasing altitude).
Fig. 4. Si VIII line profiles (1445 Å) at 58′′ and 178′′ above a coronal hole (data set 1). No correction of the stray light has been applied, because no high-altitude reference spectrum was taken for that. The “bumps” marked by the arrows, getting larger with the altitude and present on other data sets, suggest that this line is slightly contaminated by one cold line or more, appearing as instrumental stray light.

Fig. 5. Electron density $n_e$ with increasing altitude above the North polar coronal hole (data set 1). The dotted lines denote the error bars.

The flux conservation of the Alfvén waves yields

$$\frac{\xi(r)}{\xi(r_0)} = \left(\frac{\rho(r)}{\rho(r_0)}\right)^{1/4}. \quad (5)$$

From Eqs. (4) and (5), we get

$$\xi(r_0) = \left[\frac{\Delta v^2(r)}{\rho(r_0)}\right]^{1/2} \cdot \left(1 - \frac{1}{2}\right). \quad (6)$$

Thus, $\xi(r_0)$ can be determined for any $r$ where the hypothesis $\Delta T(r) = 0$ is true and where $\rho(r)$ and $v(r)$ can be measured.

Figure 6 shows that the value of $\xi(r_0)$ is relatively constant for $r$ in the range [70; 150] arcsec, which tends to prove that the $\Delta T = 0$ hypothesis is valid on that interval. As the error on $\xi(r_0)$ increases when the values of $v^2(r)$ and $\rho(r)$ are close to that at $r_0$, the lowest altitudes are associated with particularly large error bars. To get a higher precision, we made a weighted average of $\xi(r_0)$ over the [90; 150] interval, reduced not to unnecessarily broaden the error bars. We got $\xi(r_0) = 15 \pm 2$ km s$^{-1}$.

4.3. Determination of $\xi$ and $T$ at every altitude

Once we have $\xi(r_0)$, $\xi(r)$ comes from Eq. (5) (Fig. 7), every where we know $\rho(r)$. The Mg x 625 Å line width and the $\Delta T = 0$ hypothesis were only used to determine the constant $\xi(r_0)$. The determination of $\xi(r)$ now only requires the density diagnostic. Nevertheless, Eq. (5) is only valid if we assume that Alfvén waves undergo no damping between $r_0$ and $r$ and, of course, if Alfvén waves are entirely responsible for the appearance of the non-thermal velocity.

Above 150′′, the slope of the density curve changes. This may be due to the presence of a different structure on the plane of the sky, e.g. a difference between plume and interplume. If so, one would expect that the flux conservation is no longer valid...
above 150°, as the necessary continuity of the flux tubes is compromised. We nevertheless derived $\xi$ up to 270°, keeping in mind that the results are less reliable above 150°.

Temperature for each ion species can now be determined from the observed linewidths (shown in Fig. 8) by using Eq. (1). The altitude range is nonetheless restricted to positions where the non-thermal velocity is determined, i.e. below about 270°. To produce each spectrum, we performed a running sum over 40 spatial pixels. The results are shown in Fig. 9 and discussed below.

5. Results and discussion

5.1. No evidence of Alfvén wave damping

Before analysing more deeply the coronal line widths in terms of temperature and non-thermal velocity, we will discuss the radial variation of the width as a whole. This is an important issue because, in past studies, the fact that the widths of coronal lines were decreasing above some given altitude was sometimes interpreted as the signature of the damping of Alfvén waves. In fact, it appears that this decrease is essentially an effect of the instrumental stray light.

Figure 8 shows some examples of the width of different lines, with increasing altitude above the limb. The Mg X 625 Å and Si VIII 1445 Å lines, in particular, have been widely analysed in the literature. When no stray light correction is made, the Mg X 625 Å line presents the same behaviour as observed by previous authors: first, the line width increases, then reaches a maximum around 200'' ($\approx 1.2 R_\odot$ from disc centre), and starts to decrease. We find the same kind of behaviour for the Fe X 1242 Å line. There are not enough statistics for the Si VIII 1445 Å line to extend the curve above 140''. When we correct spectra from the stray light contribution in the case of the Mg X line, it is no longer possible to see any decrease, but maybe a flattening trend. For the Fe X and Fe XII lines, the stray light becomes so strong that there are not enough statistics to follow them as high as in the case with no correction; nevertheless, it appears an increasing trend for both lines.

That the stray light contamination is responsible for reducing the coronal line widths observed above the limb is well known, but appears to be underestimated in most studies with SUMER, as we find that the effect is already noticeable well below 200°. One should question in particular any study that does not directly predict the stray-light spectra.

The explanation of this effect is rather simple: lines are always narrower in stray-light spectra than in off-limb spectra; therefore, when the stray light contamination grows as the altitude increases, the observed line width is reduced. It is worth-while recalling that a stray-light spectrum is similar to any typical spectrum that could be observed on the disc in the same wavelength range. Therefore two cases are possible: either the stray-light blending is caused by the same coronal or transition region line, when it is particularly prominent on the disc (e.g. for Mg X 625 Å or Fe XII 1242 Å and 1349 Å), or it is due to another line of neighbouring wavelength (e.g. Fe X lines that are blended with O I near 1028 Å or with C I near 1463.5 Å). In this case, the blending line is usually a colder and narrower one, dominant on the disc, while the hotter one is dominant above the limb.

When no stray light correction is made, the observation of either a plateau or a decrease after the initial increase with the altitude, and the altitude where this is observed, is then simply determined by the way the ratio of stray light to coronal emission evolves with the altitude. In general, lines having a lower formation temperature than the others present a radiance that decreases more rapidly with the altitude, and are consequently subject to more contamination. Thus, in Fig. 8, the uncorrected Fe X line width starts to decrease at a lower altitude ($\approx 150°$) than that of Mg X ($\approx 190°$), which also starts to decrease at a lower altitude than that of Fe XII ($\approx 230°$; cf. Fig. 10 for the formation temperatures of these ions). But from one data set to another, the same line can also present different behaviours. One can notice in Fig. 2 (upper panel) that the Mg X 625 Å line width presents a plateau from 60° to 180°, while it reaches a maximum at three different altitudes in data sets 1, 3, and 4. For these sets, the difference in altitude of the maximum present some correlation with the observed radiance (bottom panel). Note that if the observed radiance consists of the addition of the intrinsic and of the stray light radiance, the last one is negligible at low altitude, so that the curves give a good idea of the intrinsic radiance there. Thus, the curve starts to decrease before all the others in set 3 ($\approx 150°$) and reaches a plateau in set 4 (still around 150°) before
the maximum seen in set 1 (≈230″). This fact can be explained by an almost identical stray light contribution in all data sets, dominating more rapidly in data sets where the intrinsic emission is smaller.

There is, however, one reservation concerning the interpretation of the decrease in the line width in terms of stray light contamination: even after correction, there is still a decrease, or an almost constant value, for some lines in data set 1: both O vi, the Si xi 580.91 Å, and the S x 1196.20 Å lines (Fig. 8, right panel). For these lines, there is no increase phase, as this decreasing trend begins at 57″. Once the non-thermal velocity is removed, the derived temperatures decrease with increasing altitude (Fig. 9, third panel). We have no explanation for this behaviour, as these lines are not intense enough on-disc to be subject to photoexcitation, except for O vi. It is possible that these lines are affected by some blends.

The ion temperatures in Fig. 9 are of the same order of magnitude as what is found in previous studies (e.g. Tu et al. 1998; Patsourakos et al. 2002); they all exceed $2 \times 10^6$ K at 57″. They exhibit a wide range of values, which makes the isothermal hypothesis unlikely. The temperature of the three iron lines, for example, are arranged in the opposite order to their corresponding ionization temperature (Fig. 10). Then the LOS effect associated to the stratification in temperature of the corona also appears unlikely. The temperature increases with the altitude for most of the lines, except in the bottom frame of Fig. 9 corresponding to the exceptions mentioned above. This implies some heating mechanism. The relative discrepancy between both temperatures yielded by the Fe xii lines at 1242 and 1349 Å, below 130″, may be explained by the blending of the 1242 Å line with an Si x line (cf. Table 1 in Feldman et al. 1997), as well as by the error bars. The temperature of Fe x is very high, but it is confirmed at low altitude by a second Fe x line, at 1463 Å (see Fig. 12).

To reveal a preferential heating, we plot in Fig. 11 the difference in temperature as a function of the $q/m$ ratio between 57″ and 102″, for as many lines as possible in data set 1. The line widths and temperatures measured at these altitudes are presented in Table 3. It is important to note that, for lines seen in second order, the widths are twice as large as what would be measured in first order. This is taken into account when using Eq. (1) and the derived ones. We average over 30 pixels at 57″ and 60 pixels at 102″, to exploit some very faint lines. There were not enough statistics at 102″ to analyse the Fe x line at 1463 Å, so that we only keep the one at 1028 Å. In the left panel, the non-thermal velocity has been taken into account, using results in Fig. 7: 15 and 17 km s$^{-1}$ at 57″ and 102″, respectively. The right panel corresponds to the case where no variation in non-thermal velocity is considered between 57″ and 102″, which is discussed in Sect. 5.3. The large error bars are due to the errors propagated from both the observed and the stray-light spectra to the line width (Gaussian-fit procedure) and the error on the determination of the non-thermal velocity. The weighted power law and linear fits show a trend for the ion species having the lowest $q/m$ ratios to experience more heating than the others, which is compatible with ion-cyclotron preferential heating. Both kinds of fit curves are not very different from each other. We do not intend to fit the data with any particular theoretical model. However, the power law tends to 0 for high $q/m$, while
the non-thermal velocity has been removed from the line widths). The interest of making a linear fit is discussed in Sect. 5.2. The slopes of the linear fits are \( -1.9 \pm 3.1 \) and \( -2.4 \pm 2.1 \), respectively, in the left and the right panels (in \( 10^6 \) K per unit of normalized \( q/m \)).

To interpret these curves, some points must be emphasised. First, the protons can be considered as a cooling source for all minor ion species that could be subject to any preferential heating. They compose the largest part of the coronal plasma so that collisions of one given minor ion are much more frequent with protons than with other species. As the \( q/m \) ratio of the protons, equal to 1 with our normalization, is higher than those of all the minor ions, they are also least likely to experience ion-cyclotron heating. Consequently, their temperature must be lower than or equal to that of the ions having the highest \( q/m \) ratios.

A second kind of analysis consists in plotting the ion temperatures as functions of \( q/m \), at a given altitude (Fig. 12). It shows that the ion species having the lowest \( q/m \) have a higher temperature than the others. The trend is emphasised more at 102″ than at 57″, which is consistent with the previous analysis. The particularly high temperature of Fe X tends to compress the graph, but the trend does not rely on this ion alone. To show that, we use a weighted linear fit including the Fe X data or not. Even if a straight line is obviously not the proper function to fit the data, it makes the comparison simpler, while no theoretical function is available. At 57″, the slope is equal to \( -2.2 \pm 1.2 \) with Fe X and \( -0.9 \pm 1.3 \) without it, still in \( 10^6 \) K per unit of normalized \( q/m \). At 102″, it gives \( -4.7 \pm 1.7 \) with Fe X and \( -2.7 \pm 1.8 \) without it.

To interpret these curves, some points must be emphasised. First, the protons can be considered as a cooling source for all minor ion species that could be subject to any preferential heating. They compose the largest part of the coronal plasma so that collisions of one given minor ion are much more frequent with protons than with other species. As the \( q/m \) ratio of the protons, equal to 1 with our normalization, is higher than those of all the minor ions, they are also least likely to experience ion-cyclotron heating. Consequently, their temperature must be lower than or equal to that of the ions having the highest \( q/m \) ratios, and the temperature of all other species is the result of a competition between preferential heating and cooling with the protons. By measuring differences in temperature, one only has access to the net heating. Second, most of the ion-cyclotron numerical simulations show that the species having the lowest \( q/m \) absorb most of the wave power available, to the detriment of the others that cannot resonate efficiently yet (e.g. Cranmer 2000; Vocks & Marsch 2002). This could explain the high temperature of Fe X as compared to the other species.

That low \( q/m \) ions are already hotter than the others at 57″ suggests that ion-cyclotron resonance has already taken place at lower altitudes. Such a preferential heating is still at work between 57″ and 102″ (cf. Fig. 11). If the net heating experienced

![Fig. 11. Difference in temperature between 57″ and 102″, once the non-thermal contribution is removed (left panel). The right panel corresponds to the case where we suppose that there is no variation in non-thermal velocity, only a temperature one. This case is equivalent to the case \( \xi = 0 \), i.e. when no non-thermal velocity is considered at all. The fitting functions are discussed in Sect. 5.2. The slopes of the linear fits are \( -1.9 \pm 3.1 \) and \( -2.4 \pm 2.1 \), respectively, in the left and the right panels (in \( 10^6 \) K per unit of normalized \( q/m \)).](image)

![Fig. 12. Temperatures as functions of the charge-to-mass ratio \( q/m \), 57″ (left panel) and 102″ (right panel) above a polar coronal hole (data set 1; the non-thermal velocity has been removed from the line widths). The interest of making a linear fit is discussed in Sect. 5.2.](image)
Table 3. Line widths measured in data set 1 (coronal hole) at two positions above the solar limb, and the associated ion temperatures.

<table>
<thead>
<tr>
<th>Line</th>
<th>$q/m$</th>
<th>$57''$ ($n_t = 4.8 \times 10^7$ cm$^{-3}$, $\xi = 15$ km s$^{-1}$)</th>
<th>$102''$ ($n_t = 2.7 \times 10^7$ cm$^{-3}$, $\xi = 17$ km s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Width</td>
<td>$T_e$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(Å)</td>
<td>(10^6 K)</td>
</tr>
<tr>
<td>Fe X 1028.02</td>
<td>0.16</td>
<td>0.1111 ± 0.004</td>
<td>0.1102 ± 0.004</td>
</tr>
<tr>
<td>Fe X 1463.50</td>
<td>0.16</td>
<td>0.1434 ± 0.004</td>
<td>0.1435 ± 0.013</td>
</tr>
<tr>
<td>Fe XI 1467.08</td>
<td>0.18</td>
<td>0.1310 ± 0.004</td>
<td>0.1272 ± 0.007</td>
</tr>
<tr>
<td>Ar VII 700.26</td>
<td>0.18</td>
<td>0.1153 ± 0.004</td>
<td>0.1351 ± 0.002</td>
</tr>
<tr>
<td>Ar VIII 713.82</td>
<td>0.18</td>
<td>0.1291 ± 0.004</td>
<td>...</td>
</tr>
<tr>
<td>Fe XII 1242.00</td>
<td>0.20</td>
<td>0.1035 ± 0.004</td>
<td>0.1039 ± 0.004</td>
</tr>
<tr>
<td>Fe XII 1349.36</td>
<td>0.20</td>
<td>0.1071 ± 0.004</td>
<td>0.1078 ± 0.004</td>
</tr>
<tr>
<td>Ca X 574.00*</td>
<td>0.22</td>
<td>0.1111 ± 0.004</td>
<td>0.1118 ± 0.002</td>
</tr>
<tr>
<td>Si VIII 1445.75</td>
<td>0.25</td>
<td>0.1605 ± 0.004</td>
<td>...</td>
</tr>
<tr>
<td>S X 1196.20</td>
<td>0.28</td>
<td>0.1250 ± 0.004</td>
<td>...</td>
</tr>
<tr>
<td>N V 1238.81</td>
<td>0.29</td>
<td>0.1532 ± 0.004</td>
<td>0.1709 ± 0.004</td>
</tr>
<tr>
<td>O VI 1031.93</td>
<td>0.31</td>
<td>0.1426 ± 0.004</td>
<td>...</td>
</tr>
<tr>
<td>Mg IX 706.05</td>
<td>0.33</td>
<td>0.1669 ± 0.004</td>
<td>0.1669 ± 0.002</td>
</tr>
<tr>
<td>Na X 681.72</td>
<td>0.35</td>
<td>0.1561 ± 0.004</td>
<td>0.1587 ± 0.002</td>
</tr>
<tr>
<td>Si X 580.91</td>
<td>0.36</td>
<td>0.1269 ± 0.004</td>
<td>0.1271 ± 0.002</td>
</tr>
<tr>
<td>Si X VI 604.15*</td>
<td>0.36</td>
<td>0.1229 ± 0.005</td>
<td>...</td>
</tr>
<tr>
<td>Mg X 624.94</td>
<td>0.37</td>
<td>0.1477 ± 0.004</td>
<td>0.1485 ± 0.002</td>
</tr>
</tbody>
</table>

* Wavelengths in angstroms are taken from Feldman et al. (1997). Lines marked with an asterisk are observed in second order.

5.3. Derived non-thermal velocity and its effect on the signature

The signatures of preferential heating are sensitive to the derived non-thermal velocity. In particular, any variation in width is distributed among variations in temperature and in non-thermal velocity:

$$\delta \sigma = \frac{\lambda^2}{2 \pi c^2} \left( \frac{k}{m} \delta T + \xi \delta \xi \right).$$

Even if there is little variation in $\xi$ between 57'' and 102'', the actual value of $\xi$ has a strong effect on the interpretation of the line-width variation. The value of $\xi(r)$ was derived under flux conservation condition, with no damping occurring for the Alfvén waves. We have already said that it was not possible to verify this assumption, because the Mg X 625 Å line width keeps increasing, so a possible decrease in $\xi$ may be hidden by an increase in temperature. If $\delta \xi(r)$ starts to decrease, in reality, above some position $r$ or even becomes negative, i.e. the damping is greater than the amplitude increase due to the flux conservation, then the line-width growth only has to be attributed to a growth of temperature. But this situation may only amplify the preferential heating trend, both in absolute temperatures and in differences in temperature, as shown in the right panel of Fig. 11. Note that the case $\delta \xi = 0$ is equivalent to the case $\xi(r_0) = 0$ km s$^{-1}$ (cf. Eq. (7)). In contrast, if $\xi(r)$ is larger than what we find, considering for example that Alfvén waves are not responsible for the apparent non-thermal velocity, hence that $\xi$ is not constrained by the flux conservation, then the preferential heating trends are weakened.

The non-thermal velocities that we got at low altitude in the coronal hole are within the lower limit of previously published results. However, most of those results were obtained by using the formation temperature hypothesis, which underestimates the ion temperatures.

A value of 25 or 30 km s$^{-1}$ for the Alfvénic fluctuations is typically used as a boundary condition at the coronal base in numerical simulations of heating and acceleration of the fast solar wind (see references in Sect. 1). However, this value is only encountered above 200'' in our results. There is then a lack of energy at the coronal base to reproduce the speed and temperature of the fast solar wind by using these models.
6. Conclusions

Alfvén waves and ion-cyclotron resonance, i.e. absorption of the high frequencies, are commonly used in theoretical models to provide the corona with heating and/or the fast solar wind with acceleration. Signatures of ion-cyclotron heating have been reported in the upper corona (>2.5 R\textsubscript{S}) and in the solar wind. It appears important, then, to investigate ion-cyclotron resonance closer to the Sun, where the coronal line widths offer the opportunity to study both the temperature of different ion species and the amplitude of possible Alfvén waves. This is of course a challenging task as these quantities are merged into one observable, the line width. Most of the time, methods were used that excluded a priori the possibility of analysing both contributions simultaneously. Our analysis, on the contrary, achieves a synthesis of different approaches that can be found separately in the literature, to both test and constrain the presence of Alfvén waves and the preferential heating. We constrained the former by the gradient of the Mg\textsc{x} 625 Å line width, while the latter appears from the gradient of ion temperatures and from the distinct ion temperatures measured at a given altitude.

Our analysis rests on the following hypotheses: i) the coronal lines broadening is solely due to the thermal and non-thermal Doppler effects through Gaussian contributions. ii) The non-thermal velocity \( \xi \) comes from the integration of fluid motions of the coronal plasma on both the observed solid angle and the exposure time, and is identical for all ion species at a given altitude. iii) These motions are due to the presence of Alfvén waves; if there is no damping, their amplitude increases with the altitude to conserve the energy flux in a density-stratified corona. iv) The increase in width of the Mg\textsc{x} 625 Å line (the highest \( q/m \)) at low altitude, results only from undamped Alfvén waves, i.e. \( \Delta T = 0 \), so that a boundary constraint can be set for \( \xi \) using a density diagnostic (Si VIII line ratio) and the energy flux conservation. v) The Alfvén waves stay undamped on the entire observed spatial range, so that \( \xi(r) \) can be derived.

Several results must be emphasised. The decrease in the coronal line widths, occurring around 1.2 R\textsubscript{S}, for Mg\textsc{x} for example, is essentially an effect of the instrumental stray light contamination that disappear when we remove the predicted stray-light spectrum. We cannot rule out, though, the existence of a plateau at higher altitudes than we observed. This result is in accordance with some theoretical ones that find it difficult to damp the Alfvén waves in the lower corona (Parker 1991).

The derived non-thermal velocity is about 15 km s\textsuperscript{-1} at 60°, while a value of 25 km s\textsuperscript{-1} is only reached at 200° above the limb. This means a widely lower wave energy than that commonly used in numerical simulations of heating and acceleration of the fast solar wind. Consequently, one has to find another form of energy, or of dissipation process, to replace or at least complement the processes usually presented in models based on Alfvénic fluctuations.

Two kinds of signatures of preferential heating are found: ion species having the lowest \( q/m \) ratios are the hottest ones at a given altitude and experience more heating as the altitude increases from 57° to 102°. If some damping of the Alfvén waves occurred, i.e. if hypothesis v) was wrong, then these trends would be stronger. Yet, this is neither a proof by itself of cyclotron resonance occurring in the corona, nor does it imply that this is a dominant energy source for acceleration of the fast solar wind or the heating of the corona: the energetics have to be analysed in more depth. Minor ions can only help to trace the cyclotron resonance that may also concern the protons. The ion temperatures and probably the proton one are higher than the electron temperature usually measured in coronal holes, which imply some preferential heating that must have taken place below the lowest altitude where we observed, i.e. 57°.

Some facts may possibly weaken our analysis. First, the width of some lines starts to decrease at the lowest altitude we observed. This contradicts our interpretation in terms of a common increase in the wave amplitude, but this can be due to another contribution in the line width, influencing these lines more.

Second, the lines associated with the lowest \( q/m \) ratios (Fe\textsc{x} and Fe\textsc{x}t, particularly) are highly contaminated with stray light, so that it is difficult to follow their behaviour at higher altitudes. We are also aware of the large error bars in our derived quantities. Therefore, our results have to be confirmed by additional observations and further analyses.

This work also emphasises some needs for future instrumentation, especially in terms of spectrometers. The study of line widths emitted in the low corona requires a small instrumental width as compared to the intrinsic width. It is important to develop a better rejection of the light coming from the solar disc, for off-limb observations. Furthermore, a solar probe could achieve important in situ observations to complement the remote-sensing observations, and even calibrate their interpretation.

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