

# Generation of a secondary shock wave during the oblique collision between a current sheet and a fast magnetosonic shock wave

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## ABSTRACT

**Aims.** We investigate what happens when a fast magnetosonic shock wave associated with a coronal mass ejection (CME) collides obliquely with a coronal streamer with a stable current sheet.

**Methods.** A two-dimensional relativistic and fully electromagnetic Particle-In-Cell (PIC) code is used.

**Results.** It is shown that the fast magnetosonic shock with initial Alfvén Mach  $M_A = 5.6$  compresses the current sheet, resulting in strong deformation of the current sheet. In the later stage a secondary fast magnetosonic shock wave can be generated almost perpendicular to the current sheet, and it propagates away to the opposite side of the original shock. This newly generated shock wave may emit a type II radio burst. The simulation results may be applied to a split of electromagnetic wave emissions when a shock wave associated with CMEs collides obliquely with a coronal streamer. For weak initial Alfvén Mach  $M_A = 2.8$ , a secondary shock wave does not appear, while the current sheet can be deformed and become unstable for tearing-like modes associated with magnetic reconnection.

**Key words.** plasmas – shock waves – radiation mechanisms: non-thermal – methods: numerical – Sun: radio radiation

## 1. Introduction

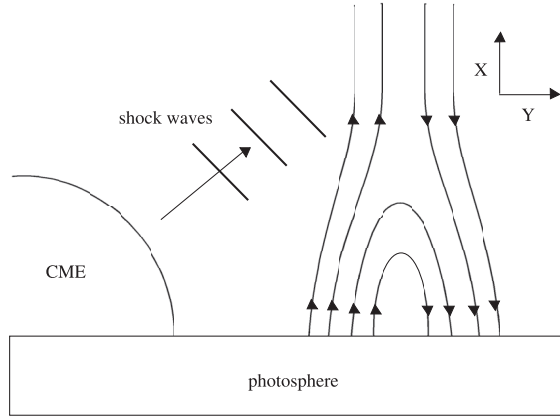
The shock waves generated by coronal mass ejections (CMEs) are observed in the interplanetary (IP) medium since they accelerate electrons, which can emit type II radio waves. Recent observations of IP type II bursts imply that changes in the shock and CMEs dynamics can be caused by interaction with some structures in the IP medium, such as collision with another CME or shock-shock collision (Gopalswamy et al. 2001). Recently Sakai et al. (2005) showed that the electron Bernstein waves or Z-modes generated near the shock front can be converted into extraordinary electromagnetic waves (type II radio bursts) through direct linear mode conversion. Sakai et al. (2006) also simulated the shock-shock collision observed by Gopalswamy et al. (2001) and found that the type II radio bursts can be enhanced after the shock-shock collision.

Sheeley et al. (2000) show examples of the fast CMEs associated with the deflection of coronal streamers, and van der Holst et al. (2002) observe that when the fast CME collides with a helmet streamer, a split occurs in the type II emission. They modeled this CME-streamer interaction by using a 2D MHD simulation. Mancuso & Abbo (2004) investigate the observed bifurcation of the radio emission lanes by modeling the interaction of a piston-driven spherical shock with a vertical current sheet located above the active region.

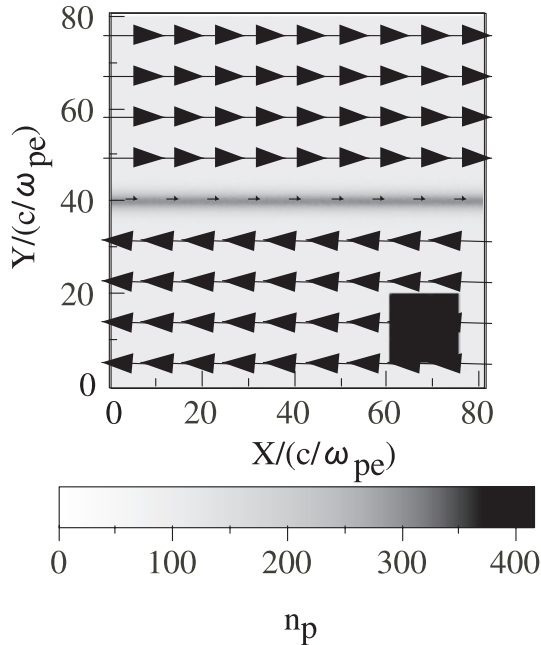
Previous theoretical and simulation models of the interaction between a current sheet and a fast magnetosonic shock wave are based on MHD models. To understand the physical processes of the emissions of type II radio bursts during the shock-streamer collision, we must take plasma kinetic processes into account by using particle-in-cell (PIC) simulation. Recently, Haruki et al. (2006) investigated how the emission of electromagnetic waves can be enhanced when a fast magnetosonic shock wave

associated with CMEs collides perpendicular to a coronal streamer with a stable current sheet, by using a two-dimensional relativistic and fully electromagnetic PIC code. It was shown that the ions in front of the shock can be accelerated by the shock-surfing acceleration mechanism (Sagdeev & Shapiro 1973; Lee et al. 1996; Lipatov & Zank 1999; Hoshino & Shimada 2002; Lee et al. 2005; Dieckmann et al. 2006). This shock compresses the current sheet, resulting in the local electron temperature anisotropy. Electron Bernstein waves are generated by the local electron temperature anisotropy and are converted into electromagnetic waves (X-mode) through the linear mode conversion due to density inhomogeneity (Murtaza & Shukla 1984; Yin et al. 1999). The nonlinear excitation process of the electron Bernstein waves in a pinching current sheet was investigated by Haruki & Sakai (2001). There, the electromagnetic waves are observed in both forward and backward regions of the shock. These simulation results were applied to the enhancement of electromagnetic wave emission when a shock wave associated with a CME collides with a coronal streamer.

In the present paper we extend the above work by Haruki et al. (2006) to investigate what happens when a fast magnetosonic shock wave associated with a CME collides obliquely with a coronal streamer with a stable current sheet. It is shown that the fast magnetosonic shock for strong initial Alfvén Mach  $M_A = 5.6$  compresses the current sheet, resulting in strong deformation of the current sheet. In the later stage a secondary fast magnetosonic shock wave can be generated almost perpendicular to the current sheet, and it propagates to the opposite side of the original shock. This newly generated shock may emit the type II radio burst, as shown by Sakai et al. (2005). For weak initial Alfvén Mach  $M_A = 2.8$  a secondary shock wave does not appear, while the current sheet can be deformed and become



**Fig. 1.** Schematic picture of the coronal mass ejection (CME) associated with a shock wave that collides obliquely with Harris type current sheet and the coordinate system used in the simulation.



**Fig. 2.** The initial magnetic field structure of a Harris type current sheet and proton density. The square high-density region moves with Alfvén Mach speed  $M_A = v_s/v_A = 5.6$ , resulting in formation of a shock wave.

unstable for tearing-like modes associated with magnetic reconnection.

This paper is organized as follows. In Sect. 2 we present our simulation model and in Sect. 3 we show our simulation results. In the final section we summarize our results.

## 2. Simulation model

Figure 1 shows a schematic picture of our simulation model. It is assumed that a CME originating in the lower corona produces a shock and that this shock undergoes an oblique collision with a coronal streamer that contains a current sheet as shown. The initial magnetic field and plasma number density for a Harris type current sheet are the same as in Haruki et al. (2006). Figure 2 shows the initial magnetic field and the proton density distribution. As shown in Fig. 2 we impose a dense plasma cloud (square region) far from the center of the current sheet to excite a fast magnetosonic shock wave by imposing the plasma velocity with

Alfvén Mach speed  $M_A = v_s/v_A = 5.6$  on the cloud. The initial velocity of the cloud is  $v_x = v_y = 4v_A$ .

The code used here is a 2D relativistic and fully electromagnetic PIC code, modified from the 3D TRISTAN code (Buneman 1993). The system size in 2D is  $L_x = L_y = 800\Delta$ , where  $\Delta (=1)$  is the simulation grid size. It is assumed that the physical quantities are constant in  $z$ , i.e.,  $\partial/\partial z = 0$ . The average number density of background electrons and ions is 100 per cell. The given particles fill the whole domain. Charge neutrality is initially kept because of having the same position for the electron and proton. Periodic boundary conditions in the  $x$ -direction and free boundary conditions in the  $y$ -direction are imposed on particles and fields.

First, we impose the following Harris type current sheet (Harris 1962; Pritchett 2001) that is characterized by the magnetic field, current, and plasma particle number density, namely,

$$B_x(y) = B_0 \tanh\left(\frac{y-y_c}{L}\right),$$

$$J_z(y) = -\frac{B_0}{\mu_0 L} \cosh^{-2}\left(\frac{y-y_c}{L}\right),$$

$$n(y) = n_c \cosh^{-2}\left(\frac{y-y_c}{L}\right),$$

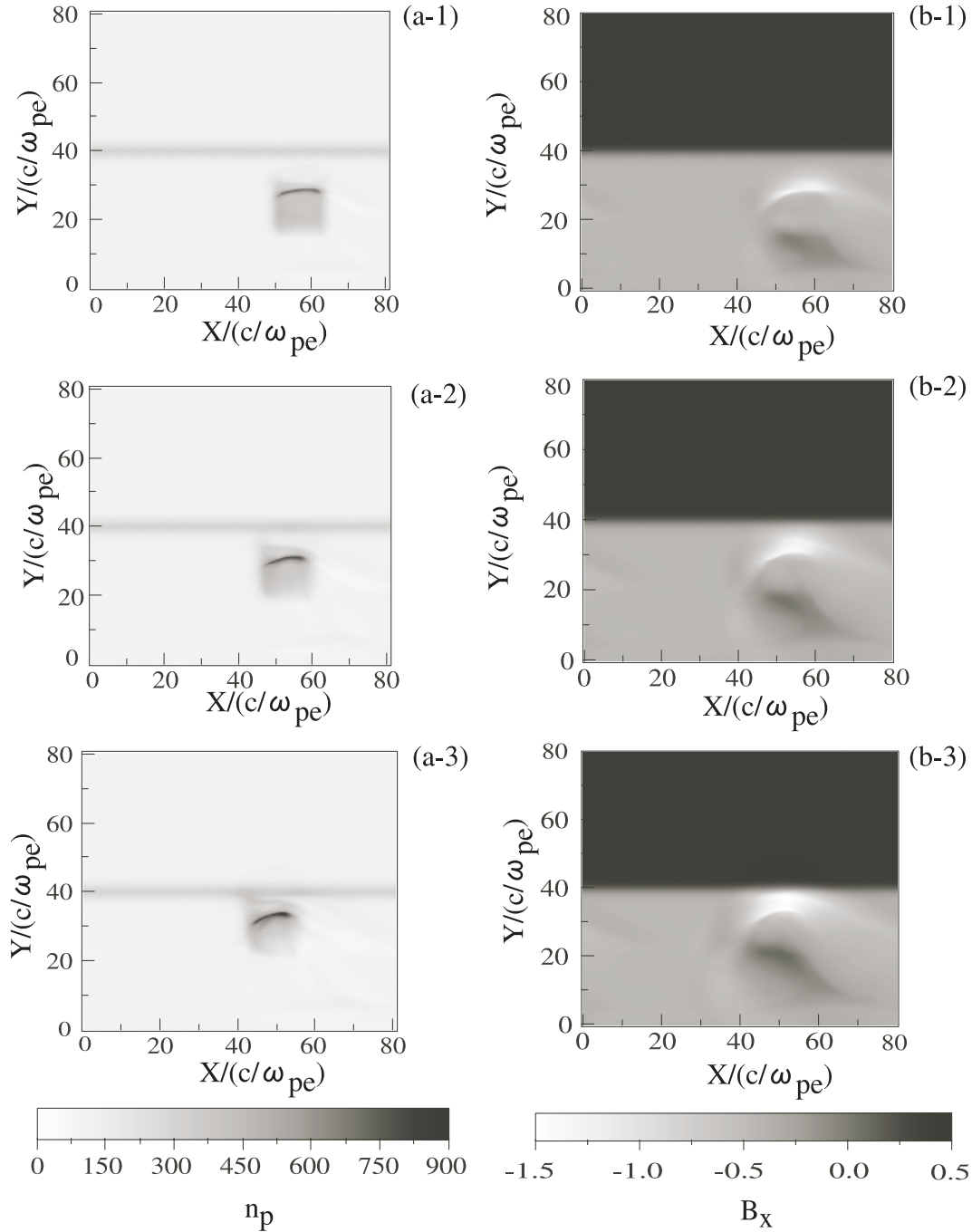
where  $y_c = 400\Delta$  and half thickness  $L = 20\Delta$ . We assume a low beta plasma  $\beta = 0.5$  and electron thermal velocity  $v_{te}/c = 0.1$  ( $c$  is light speed) in the background plasma, and then  $n_c/n_0 = 3$  and  $\omega_{ce}/\omega_{pe} = 0.2$  are obtained theoretically, where  $\omega_{pe}$  and  $\omega_{ce}$  are electron plasma and cyclotron frequencies, respectively. Moreover, the Alfvén velocity far from the center of the current sheet is automatically solved with about  $v_A = 0.02c$ . Next, to excite a shock wave far from the center of the current sheet, we impose a dense plasma cloud whose number density is 400 per cell from  $x = 600\Delta$  to  $750\Delta$  and  $y = 50\Delta$  to  $200\Delta$ . The cloud velocity is set up with  $v_s = 5.6v_A = 0.11c$ .

The other parameters used for this simulation are as follows. The simulation time step is  $\omega_{pe}\Delta t = 0.05$ , where  $\omega_{pe}$  is used as a normalization of time. The Debye length is  $\lambda_D = v_{te}/\omega_{pe} = 1\Delta$ . The electron skin depth is  $c/\omega_{pe} = 10\Delta$ , which is also used as a normalization of space. The mass ratio of electron and proton is  $m_i/m_e = 100$ , whose value is artificial due to computer memory. The temperatures of the electrons and protons are the same,  $T_i/T_e = 1$ . The Larmor radii of electrons and protons are  $5\Delta$  and  $50\Delta$ , respectively.

We performed another simulation case without the dense plasma cloud. We confirmed that the current sheet is very stable until  $\omega_{pe}t = 500$ . For this case, we did not observe any wave generation.

## 3. Simulation results

The square high-density region with Alfvén Mach speed  $M_A = v_s/v_A = 5.6$  in Fig. 2 approaches the current sheet at an angle of  $45^\circ$ , resulting in the formation of shock wave. To see the shock formation stage, we show the time development of proton number density  $n_p$  and magnetic field  $B_x$  in the  $x-y$  plane at  $\omega_{pe}t = 150$ (a-1, b-1),  $200$ (a-2, b-2), and  $250$ (a-3, b-3) in Fig. 3. We find that the shock front speed at near  $\omega_{pe}t = 200$  is about  $M_A = 3.4$ . The proton density near the shock front at  $\omega_{pe}t = 250$  is increased about 6.5 times of background density due to the density inhomogeneity. The shock enhancement due to density inhomogeneity near the current sheet was studied by



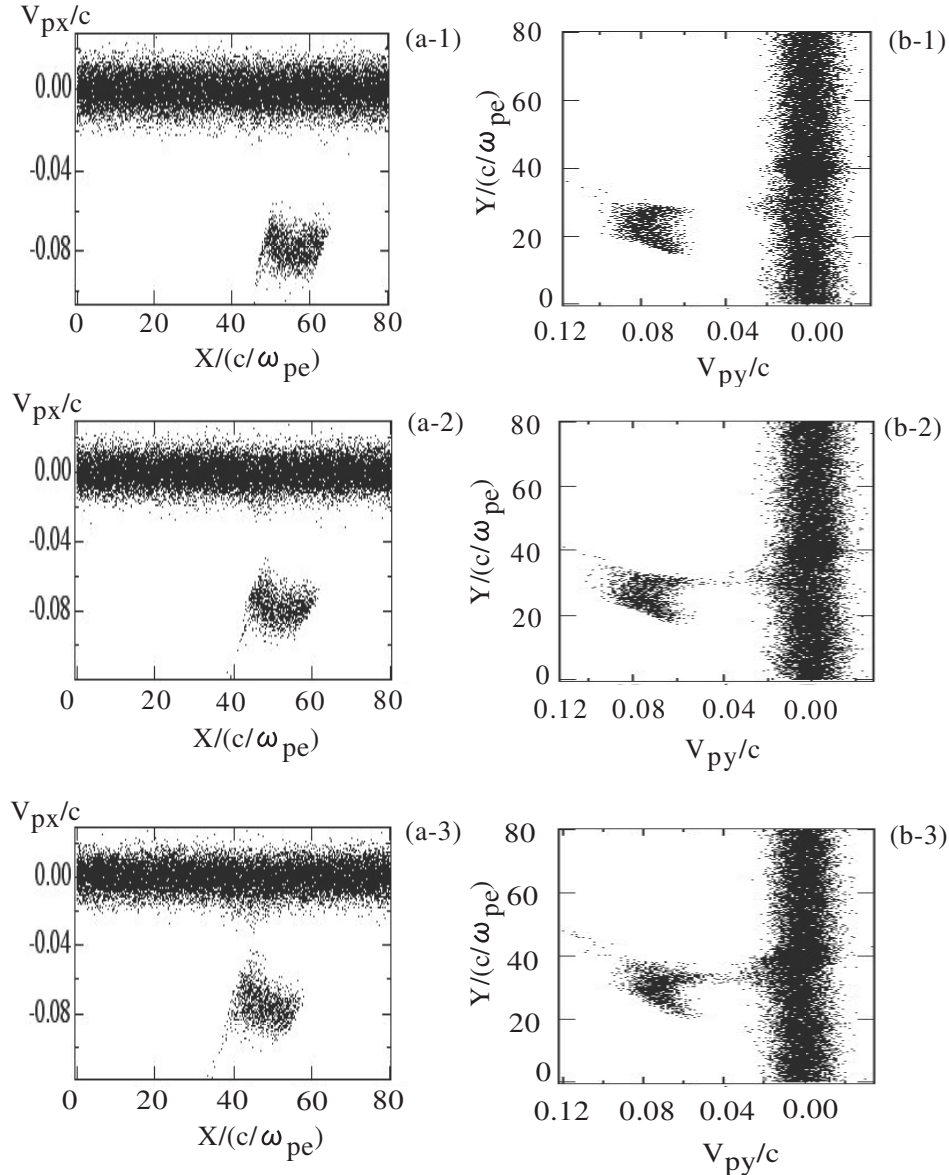
**Fig. 3.** Time development of proton number density  $n_p$  and magnetic field  $B_x$  in the  $x - y$  plane at  $\omega_{pe}t = 150$ (a-1, b-1), 200(a-2, b-2), and 250(a-3, b-3).

Sakai (1973). In Fig. 4 we show the time development of proton phase space,  $V_{px} - X$  and  $V_{py} - Y$  at  $\omega_{pe}t = 150$ (a-1, b-1), 200(a-2, b-2), and 250(a-3, b-3). The average bulk velocity of the cloud is about  $0.08c$  in both  $x$ - and  $y$ -directions which gives us about  $M_A = 5.6$  close to the initial cloud velocity. It is seen from the shock front that a small fraction of protons are accelerated ahead of the shock front.

The generated fast magnetosonic shock wave collides with the current sheet and moves along the current sheet with strong deformation. In Fig. 5 we show the time development of the proton number density in the  $x - y$  plane at a  $\omega_{pe}t = 500$ , b 750, c 850, and d 1000. As seen in the region of  $60 < Y/(c/\omega_{pe}) < 80$ , a fast magnetosonic wave with a bow-like structure propagates to

the upper direction. While near the upper part of the current sheet where strong density deformation is seen, the strong proton density detachment can be observed in Fig. 5b. This enhanced density cloud propagates to the positive  $y$  direction almost perpendicular to the current sheet, as seen in Figs. 5b–d. This plasma cloud detached from the current sheet can develop to a secondary fast magnetosonic shock wave. The shock front speed is about  $0.06c$ , which gives us about  $M_A = 3$  by using  $V_A = 0.02c$ .

In Fig. 6 we present the spatial structure associated with the secondary generated shock wave at  $\omega_{pe}t = 850$ . Figures 6a, c, and d show proton density distribution, magnetic field  $B_x$ , and electric field  $E_y$  near the the shock front, respectively. Figure 6b shows the proton phase space plot ( $V_{pz} - y$ ) at  $\omega_{pe}t = 850$ .



**Fig. 4.** Time development of proton phase space,  $V_{px} - X$ (a-1–a-3) and  $V_{py} - Y$ (b-1–b-3) at  $\omega_{pe}t = 150$ (a-1, b-1), 200(a-2, b-2), and 250(a-3, b-3).

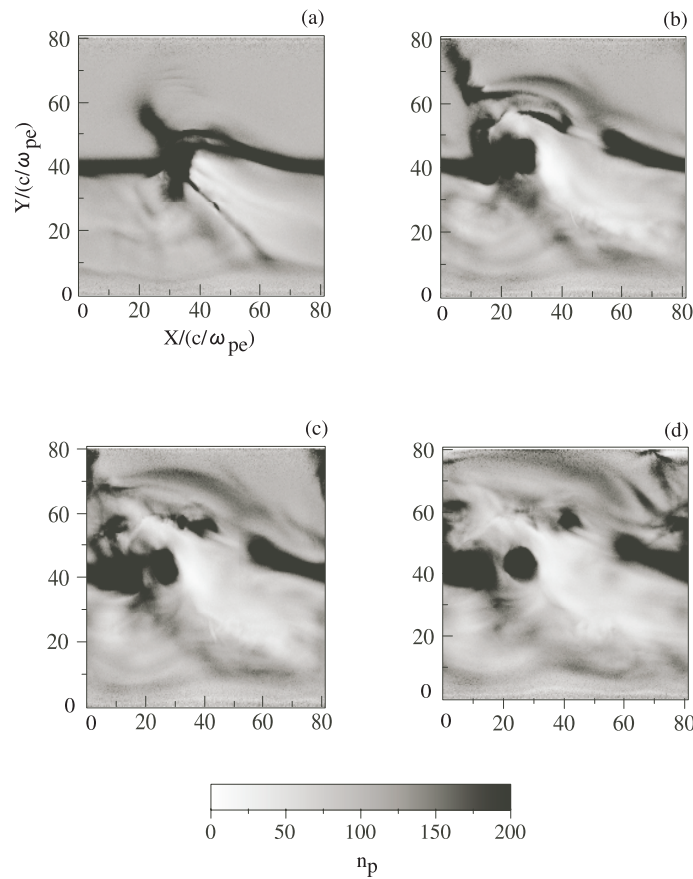
Some protons near  $Y = 70$  can be accelerated to the positive  $z$ -direction. These protons are accelerated by the shock surfing acceleration mechanism (Sagdeev & Shapiro 1973) near the secondary generated shock wave. We can estimate the maximum proton velocity obtained near the shock front as  $V_{\max}/c = E_y/B_x$ . We obtain  $V_{\max} = 0.18c$  by using the field data of  $E_y = 0.14$  and  $B_x = 0.76$  at  $X = 36.6$  and  $Y = 72.9$ . This value is almost consistent with the simulation result seen in Fig. 6b. Therefore we may expect that the secondary generated fast magnetosonic shock wave can emit the type II radio bursts shown in Sakai et al. (2005). To see the wave emission in this simulation, we need larger simulation box.

Finally we present simulation results with a different Mach number that is smaller than the above case. We show the case where the initial driving flow velocity is  $M_A = 2.8$ . Figure 7 shows the time development of proton number density at a)  $\omega_{pe}t = 500$ , b)  $\omega_{pe}t = 1000$ , and c)  $\omega_{pe}t = 1500$ . As seen in Fig. 7b, the plasma cloud associated with the shock moves along

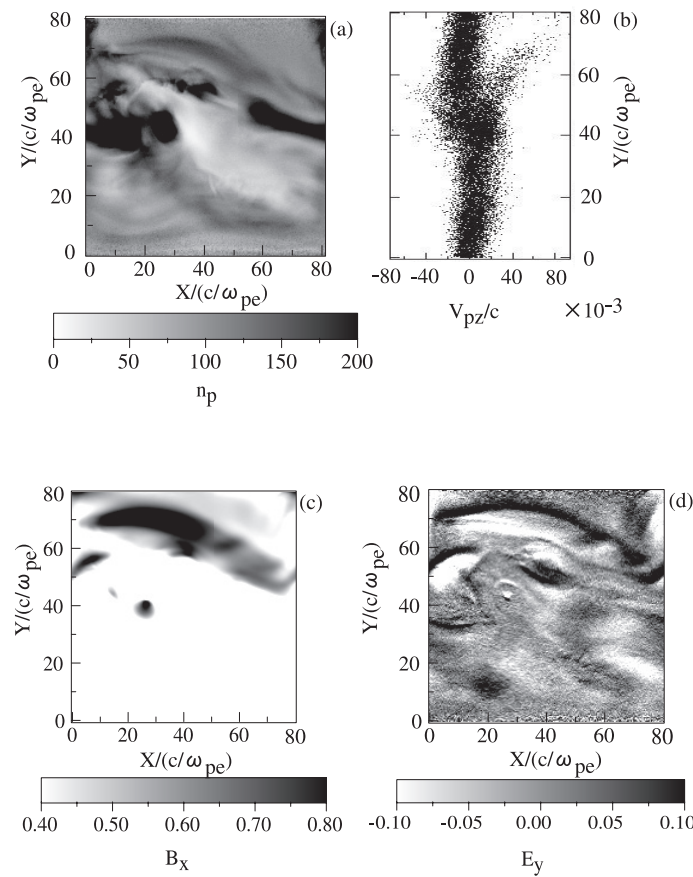
the current sheet, resulting in the bending of the current sheet. In this case there appears no secondary shock wave as observed in the previous case. During the later stage (see Fig. 7c), the current sheet breaks into two current filaments. Figure 8 shows the spatial distribution of current  $J_z$  at  $\omega_{pe}t = 1500$ , corresponding to Fig. 7c. In Fig. 9 we show the time development of vector plots of magnetic fields corresponding to Fig. 7. From Fig. 9c we see the formation of magnetic islands corresponding to the current filaments seen in Fig. 7c. From all this, we conclude that for a weak Mach number like  $M_A = 2.8$  the current sheet can be deformed and become unstable for tearing-like modes associated with magnetic reconnection.

#### 4. Conclusions

By using a 2D relativistic and fully electromagnetic PIC code, we investigated the oblique collision between a fast magnetosonic shock and a Harris type current sheet. It was shown that

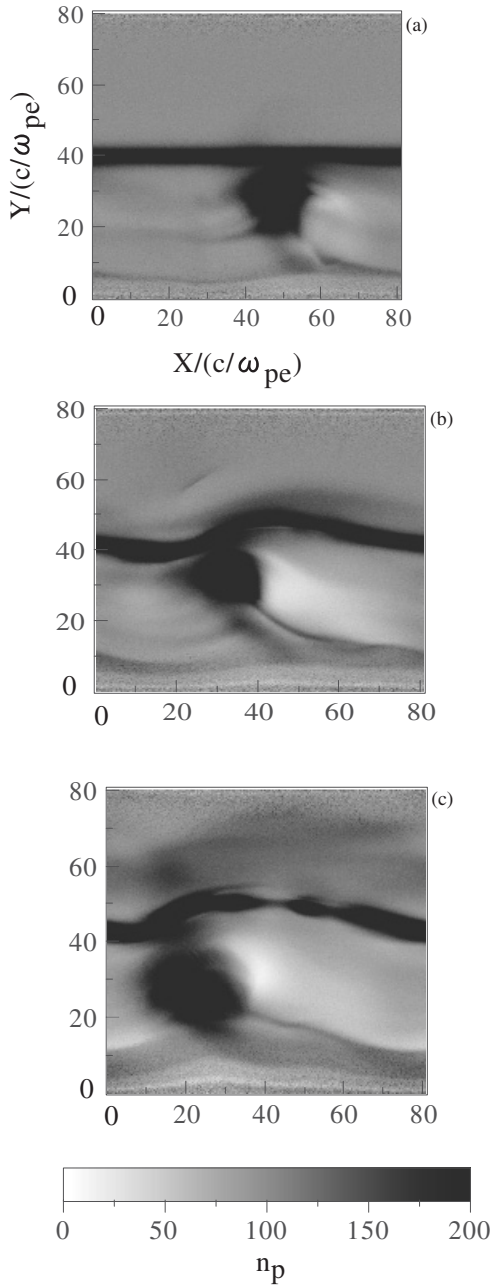


**Fig. 5.** Time development of proton density distribution at **a**)  $\omega_{pe}t = 500$ , **b**)  $\omega_{pe}t = 750$ , **c**)  $\omega_{pe}t = 850$ , and **d**)  $\omega_{pe}t = 1000$ .

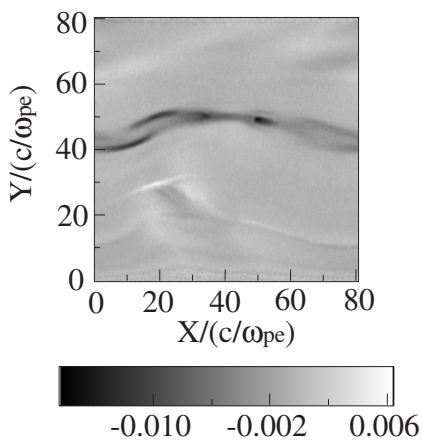


**Fig. 6.** **a**) Proton density distribution at  $\omega_{pe}t = 850$  for  $M_A = 5.6$ . **b**) Proton phase space plot ( $V_{pz} - Y$ ) at  $\omega_{pe}t = 850$ . **c**) Magnetic field  $B_x$  and **d**) electric field  $E_y$  at  $\omega_{pe}t = 850$ .

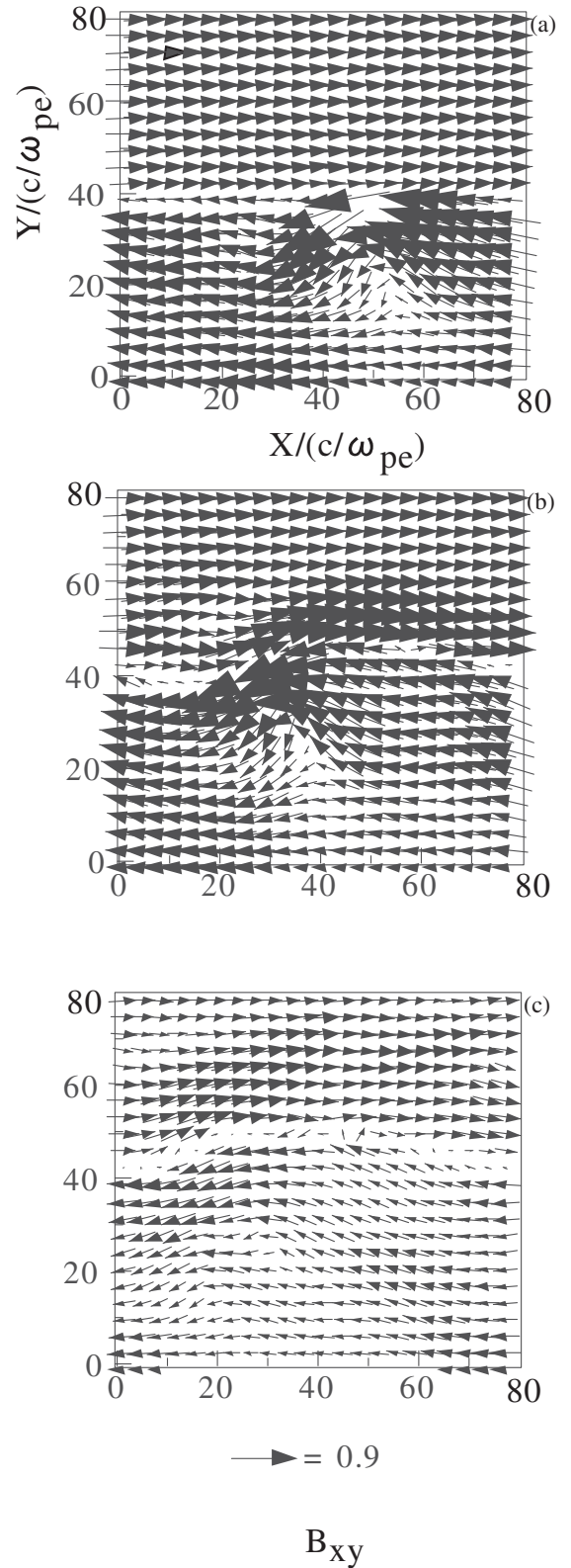




**Fig. 7.** Time development of proton density distribution for  $M_A = 2.8$  at **a)**  $\omega_{pe}t = 500$ , **b)**  $\omega_{pe}t = 1000$  and **c)**  $\omega_{pe}t = 1500$ .



**Fig. 8.** Current  $J_z$  for  $M_A = 2.8$  at  $\omega_{pe}t = 1500$ .



**Fig. 9.** Time development of vector plots of magnetic fields for  $M_A = 2.8$  at **a)**  $\omega_{pe}t = 500$ , **b)**  $\omega_{pe}t = 1000$  and **c)**  $\omega_{pe}t = 1500$ .

the fast magnetosonic shock with Mach number  $M_A = 5.6$  compresses the current sheet, resulting in strong deformation of it. In the later stage a secondary fast magnetosonic shock wave can be generated almost perpendicular to the current sheet and it propagates away to the opposite side of the original shock. This newly

generated shock wave may emit the type II radio burst. The simulation results may be applied to a split of electromagnetic wave emissions when a shock wave associated with CMEs collides obliquely with a coronal streamer.

While for a weak shock with  $M_A = 2.8$ , the secondary shock wave does not appear. But the current sheet can be deformed and become unstable for tearing-like modes associated with magnetic reconnection.

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## References

- Buneman, O. 1993, in *Computer Space Plasma Physics, Simulation Techniques and Software*, ed. H. Matsumoto, & Y. Omura (Tokyo: Terra Scientific), 67
- Dieckmann, M. E., Eliasson, B., Shukla, P. K., Sircombe, N. J., & Dendy, R. O. 2006, *Plasma Phys. Contr. Fusion*, 48, B303
- Gapalswamy, N. S., Yashiro, S., Kaiser, M. L., Howard, R. A., & Bougeret, J.-L. 2001, *ApJ*, 548, L91
- Harris, E. G. 1962, *Nuovo Cimento*, 23, 115
- Haruki, T., & Sakai, J. I. 2001, *ApJ*, 552, L175
- Haruki, T., Sakai, J. I., & Saito, S. 2006, *A&A*, 455, 1099
- Hoshino, M., & Shimada, N. 2002, *ApJ*, 572, 880
- Lee, M. A., Shapiro, V. D., & Sagdeev, R. Z. 1996, *JGR*, 101, 4777
- Lee, R. E., Chapman, S. C., & Dendy, R. O. 2005, *Phys. Plasmas*, 12, 012901
- Lipatov, A. S., & Zank, G. P. 1999, *PRL*, 82, 3609
- Mancuso, S., & Abbo, L. 2004, *A&A*, 415, L17
- Murtaza, G., & Shukla, P. K. 1984, *J. Plasma Phys.*, 31, 423
- Pritchett, P. L. 2001, *JGR*, 106, 3783
- Sagdeev, R. Z., & Shapiro, V. D. 1973, *JETP Lett.*, 17, 279
- Sakai, J. I. 1973, *Ap&SS*, 23, 285
- Sakai, J. I., Mori, T., & Saito, S. 2005, *A&A*, 442, 687
- Sakai, J. I., Mori, T., Saito, S., Tanaka, Y., & Aurass, H. 2006, *A&A*, 454, 983
- Sheeley, N. R., Hakala, W. N., & Wang, Y. M. 2000, *J. Geophys. Res.*, 105, 5081
- van der Holst, B., van Drel-Gesztelvi, L., & Poedts, S. 2002, in *Solar variability: from core to outer frontiers*, ESA SP-506, 1, 71
- Yin, L., & Ashour-Abdalla, M. 1999, *Phys. Plasmas*, 6, 449