

Investigation of long-duration arcade flares^{*}

II. Energy release

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ABSTRACT

Aims. We analyse three well-observed long-duration arcade flares (LDAFs) to find their general properties. Results concerning energy release in LDAFs (energy balance and diagnostic diagrams) are shown.

Methods. *Yohkoh* observations and Kitt Peak Vacuum Telescope magnetograms are used to determine physical parameters of flare loop-top kernels (temperature, density, altitude). Using these parameters the energy release is studied in detail.

Results. We found that: (1) the energy release in LDAFs occurs during their whole decay phase; (2) the kernel heating (E_H) is of the order of $0.01\text{--}1\text{ erg cm}^{-3}\text{ s}^{-1}$; (3) the kernels usually cannot be distinguished in SXT images when E_H is drops below a particular value. This value depends on the altitude of the kernels.

Key words. Sun: corona – Sun: flares – Sun: X-rays, gamma rays

1. Introduction

Long-duration arcade flares (LDAFs) are very interesting phenomena. This type of solar flare is characterized, like all long-duration events (LDE), by a slow decrease of brightness in soft X-rays (SXR) lasting for many hours. The second characteristic feature of these flares is their morphology. A typical LDAF consists of several loops which form an arcade with bright emission kernels placed at the tops of the loops (loop-top kernels). Analysis of SXR images indicates that the kernels may be connected by a magnetic tube (so-called arcade channel; see Jakimiec et al. 1997; Tomczak 1994 and Kołomański 2007 (Paper I)).

LDAFs have more a complicated structure than compact flares. Nevertheless, their investigation can help us in better understanding the physics of flaring structures. Detailed analysis of satellite observations carried out by many authors has led to several important results (e.g. Sheeley et al. 1975; Kahler et al. 1977; Feldman et al. 1995; Harra-Murnion et al. 1998; Shibasaki 2002). One of the most important conclusions is that continuous energy release and plasma heating must exist during the LDAF decay phase to ensure the long duration of their loop-top kernels in spite of radiative and conductive losses (Vorpahl et al. 1977). Czaykowska et al. (1999) found that during the decay phase of LDAFs chromospheric evaporation occurs, indicating that the reconnection and heating processes must take place during that phase. In Isobe et al. (2002) LDAF of 12 May 1997 was analysed. The authors estimated the energy release rate for the decay phase of the flare as a whole, but excellent *Yohkoh* observations allow the investigation of heating of individual kernels. Depending on the flare model the energy release takes place inside the kernels (Jakimiec 2002a,b) or above the kernels (e.g. Kopp & Pneuman 1976; Shibata 1999; Hirose et al. 2001). In the

Table 1. Analysed LDAFs – data from *GOES/SEM* database.

Date	Beginning [UT]	Duration [h]	X-ray class
7 May 1993	20:20	7	M1.6
14 May 1993	21:54	10	M4.5
27 Apr. 1998	08:55	19	X1.0

second model the primary energy release site is difficult to observe. Thus, the detailed investigation of kernel heating allows us to study the magnetic energy release during the decay phase and helps us to understand the reconnection process. Recently in Bąk-Stęślicka & Jakimiec (2005) several LDEs with slow rise phase (so-called slow LDEs) were investigated. The authors estimated kernel heating rates for the rise phase.

We present the analysis of three LDAFs well observed by *Yohkoh*. In a previous paper (Paper I) we investigated the morphological properties and physical parameters of these flares. In this paper we concentrate on the energy release during the decay phase. Methods that we used allow us to investigate the heating rates of loop-top kernels. These methods are described in Sect. 2. Results of the investigation are shown in Sect. 3. Conclusions are given in Sect. 4.

2. Analysis

Basic information about the selected LDAFs are given in Table 1. To analyse the flares we applied observations made by *Yohkoh* SXT and HXT telescopes and the Kitt Peak Vacuum Telescope (KPVT). Values of parameters necessary for the energy release estimation (temperature T , density N , altitude h) were presented in Paper I. The estimation can be made in two ways. In the first method temperature–density ($T - N$) diagnostic diagrams are used. The second one concerns the energy

^{*} Appendices are only available in electronic form at <http://www.aanda.org>

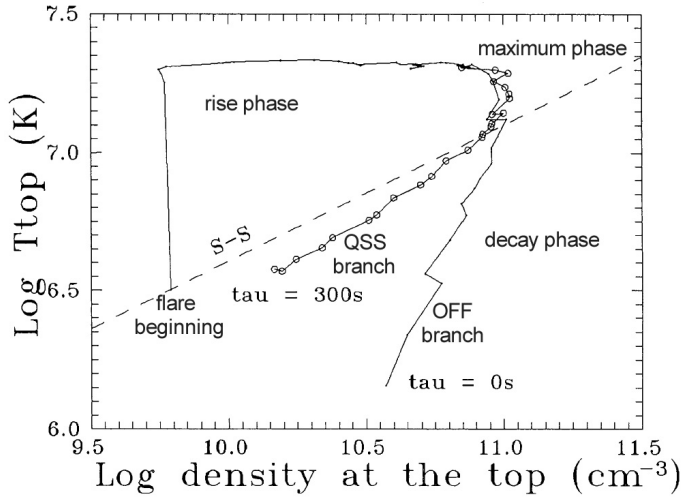


Fig. 1. Computed $T - N$ diagram illustrating the dependence of the decay phase on energy release decay-time. The S-S line is defined by the relation between T and N for steady-state loops with a given length. The thermodynamic decay time τ_{th} is equal to 165 s. Figure taken from Jakimiec et al. 1992).

balance calculation. Both methods were used to analyse the selected LDAFs. Below we describe them.

2.1. Temperature-density diagnostic diagrams

The method of investigation of flare evolution in temperature-density diagrams was worked out by Jakimiec et al. (1986, 1987, 1992) and Sylwester et al. (1993). It was shown that temporal evolution of flares does not depend much on their morphology. Thus, the diagrams allow us to qualitatively study temporal changes of the energy release in flares.

The flare evolution in $T - N$ diagrams is described in detail in Jakimiec et al. (1992). We present here only the description of the decay phase. Figure 1 shows an example of a $T - N$ diagram computed for two different energy release decay-times. Evolution of a flare during the decay phase depends on how fast the heating rate (E_H) decreases.

- If E_H decreases very fast, with an e-folding decay time shorter than the thermodynamic decay time $\tau_{th} \propto L/\sqrt{T_0}$ (L – semilength of a loop, T_0 – initial temperature at the top of a flaring loop) then the flare evolves along the OFF branch (E_H switched-off evolution). The evolution is characterized by a fast decrease of T caused by the loop cooling due to thermal conduction losses and radiative losses (the second ones are larger) not balanced by the heating rate, which is too low. This evolution is represented in Fig. 1 by a branch for E_H e-folding decay time $\tau = 0$ s.
- If E_H decreases slowly, with τ longer than τ_{th} , the flaring loop will go through a sequence of steady-state configurations. In a $T - N$ diagram such a flare evolves along the QSS branch (quasi-steady-state evolution) which is parallel to the S-S line (steady state). This line is defined by the relation between T and N for steady-state loops with a given L . During the QSS evolution T drops slower than for the OFF evolution because the thermal conduction and radiative losses (the first ones are larger) are balanced by the heating rate which is high enough. The QSS evolution is shown in Fig. 1 by a branch for the E_H e-folding decay time $\tau = 300$ s.

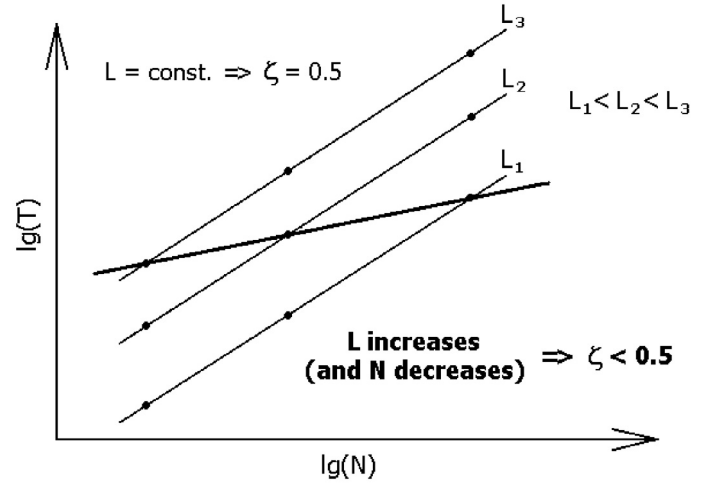


Fig. 2. Schematic $N - T$ diagram showing effect of a changing flaring loop length on the QSS evolution. Flares with a larger and constant L (L_1, L_2, L_3) lie higher on the $T - N$ diagram than those with a shorter L . In most cases L increases with time and simultaneously N decreases. In such case a flare evolves along the branch with an inclination smaller than 0.5. In the figure an example for which $\frac{d \lg L}{d \lg N} = \text{const.}$ is shown. Such a flare has a straight QSS branch.

The described examples of evolution are limiting cases. Intermediate cases can operate for $\tau \approx \tau_{th}$ with branches running between the OFF and QSS paths.

The inclination ζ of the decay-phase branch is defined as:

$$\zeta = \frac{d \lg T}{d \lg N}. \quad (1)$$

Numerical calculations for a flaring loop with a constant L shows that ζ has the value 2.0 and 0.5 for the OFF and QSS evolution, respectively (Jakimiec et al. 1992). However, observations show that the height of flaring loops increases during the flare evolution. Thus, we must estimate the effect of this increase of the L on inclination ζ . Here we perform this estimation only for the QSS branch because analysed LDAFs had decay evolutions with ζ significantly smaller than 1.0. The QSS branch is parallel to the S-S line thus we must find the relation between ζ for this line and L . Using the RTV scaling law for steady-state loops (Rosner et al. 1978): $T \propto (Lp)^{1/3}$ (where p is the pressure in a loop) and the equation of state $p \propto NT$, we obtain after simple transformations:

$$\lg T = 0.5 \lg N + 0.5 \lg L + \lg c \quad (2)$$

where c is a const. According to Eq. (2) flares with different but constant L evolve during the decay phase along parallel straight lines. Flares with larger L lie on the $T - N$ diagram higher than those with shorter L (see Fig. 2). From Eq. (2) we calculate the inclination ζ :

$$\zeta = \frac{d \lg T}{d \lg N} = 0.5 + 0.5 \frac{d \lg L}{d \lg N}. \quad (3)$$

If $L = \text{const.}$ during the flare decay phase then $\zeta = 0.5$. However, in most cases L increases with time and simultaneously N decreases. This means that the second term of the right side of Eq. (3) is negative and in consequence $\zeta_{QSS} < 0.5$. Estimations of the term $0.5 \frac{d \lg L}{d \lg N}$ for the analysed flares are shown in Sect. 3.

The second factor affecting the QSS branch inclination has an instrumental background. It was shown in Paper I that LDAFs

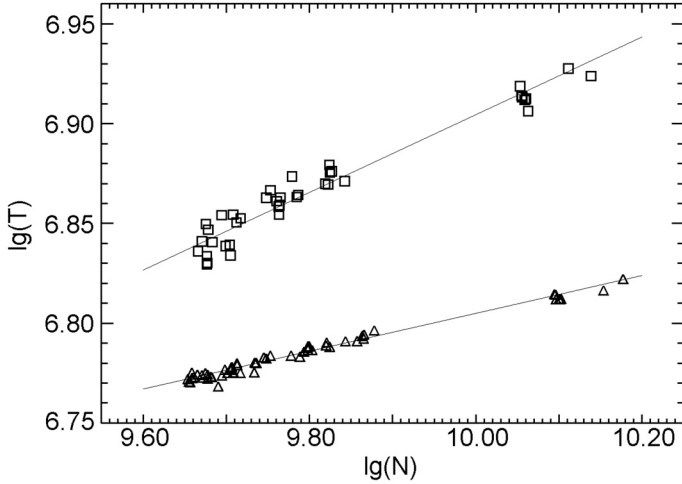


Fig. 3. The temperature-density diagnostic diagram for the decay phase of the 27 April 1998 flare. The N and T values were obtained from the Be119/A112 (squares) and A112/A1.1 (triangles) diagnostics.

kernels are multithermal during the decay phase. Because the SXT temperature diagnostics is more sensitive to cooler plasma (see Jakimiec et al. 1998), the temperature changes ΔT are underestimated and hence the emission measure changes $\Delta \epsilon$ as well as the electron density changes ΔN are overestimated. Together this leads to a significant underestimation of the inclination ζ . This effect is confirmed when one compares the temperature obtained from the A112/A1.1 diagnostics with the temperature obtained from the Be119/A112 diagnostics. The first diagnostics gives systematically lower temperatures and smaller inclination ζ than Be119/A112 diagnostics (see Fig. 3), which is in agreement with the fact that the A1.1 intensities are more sensitive to cooler plasma than Be119 intensities (see Fig. 9 in Tsuneta et al. 1991).

Due to the above-mentioned factors we can expect that the observed inclination ζ for the QSS evolution in the T - N diagram might be significantly smaller than the theoretical value of 0.5.

2.2. Energy balance calculations

The energy balance of a loop-top kernel during the decay phase can be written as follows:

$$\left(\frac{d\mathcal{E}}{dt}\right)_{\text{obs}} = \left(\frac{d\mathcal{E}}{dt}\right)_{\text{ad}} - E_C - E_R + E_H \quad (4)$$

where $\mathcal{E} = 3NkT$ is thermal energy density, $\left(\frac{d\mathcal{E}}{dt}\right)_{\text{obs}}$ is the decrease of \mathcal{E} per second estimated from T and N values, $\left(\frac{d\mathcal{E}}{dt}\right)_{\text{ad}}$ is the decrease due to the adiabatic expansion of plasma in a kernel, E_C is the energy losses due to thermal conduction, E_R – the radiative losses and E_H is the heating rate or thermal energy release (E_C , E_R and E_H are in $\text{erg cm}^{-3} \text{ s}^{-1}$). We calculated $\left(\frac{d\mathcal{E}}{dt}\right)_{\text{ad}} = 5kT \left(\frac{dN}{dt}\right)$, $E_C = 3.9 \times 10^{-7} T^{3.5} / (Lr)$ where r is a kernel radius and L is calculated as $L = (\pi/2)h$ (Jakimiec et al. 1997), $E_R = N^2 \Phi(T)$, where $\Phi(T)$ is the radiative loss function taken from Rosner et al. (1978). In our calculations, energy of nonthermal electrons was not included. It was shown by Czaykowska et al. (2001) that during the decay phase this component can be omitted because it is much smaller than E_C .

The Eq. (4) allows us to calculate upper and lower limits for the heating rate. The upper limit $(E_H)_{\text{max}}$ is calculated directly from Eq. (4). However sometimes loops connecting a kernel with

the chromosphere are faint. The low intensity of these loops suggests that the energy flow might be reduced e.g. due to their filamentary structure (see Jakimiec et al. 1998). Therefore the lower limit of heating rate $(E_H)_{\text{min}}$ is obtained under the assumption $E_C = 0$. The relative error of E_H is about 30–40 per cent.

For all analysed kernels we use values of parameters (T and N) obtained from fluxes measured in the A1.1 and A112 filters (the ratio A112/A1.1 will be called the A112 diagnostics). It was shown in Paper I that the A112 diagnostics gives lower temperatures for analysed kernels than the Be119 diagnostics (from the ratio of fluxes measured in the filters Be119 and A112). This means that the mean temperature of kernels taken from the A112 diagnostics is significantly underestimated. This fact affects the energy balance calculation. The Be119 diagnostics also underestimates the temperature, but not so much (the Be119 diagnostics is not very sensitive to 20 MK plasma (see Jakimiec et al. 1998)). Because of this it would be better to use the Be119 diagnostics. Unfortunately, the Be119 images are usually available only for the rise and maximum phases of flares evolution. Thus, we decided to calculate the energy balance with T and N taken from the A112 diagnostics. This approach allows us to study the almost entire decay phase of LDAFs, but we must estimate how this diagnostics affects the values $(E_H)_{\text{min}}$ and $(E_H)_{\text{max}}$:

- $(E_H)_{\text{min}}$. The lower limit of the heating rate is mainly defined by radiative losses, $E_R = N^2 \Phi(T)$. It was shown in Paper I that N weakly depends on the diagnostics. Also the value of the radiative loss function $\Phi(T)$ has a small change in a temperature range of LDAFs kernels. Thus, $(E_H)_{\text{min}}$ is rather insensitive to T underestimation by the A112 diagnostics.
- $(E_H)_{\text{max}}$. The upper limit of the heating rate is mainly defined by thermal conduction losses because $E_C \leq E_R$ (see Tables A.4–A.6). The losses strongly depend on T , thus underestimation of this parameter leads to significant underestimation of E_C and, in consequence, $(E_H)_{\text{max}}$.

As we can see, the energy balance with the A112 diagnostics places the upper limit of the heating rate too low. However, more important it is that it does not affect the lower limit, which allows us to determine whether analysed kernels were heated during the decay phase.

3. Results and discussion

3.1. Selected flares

In this subsection we give a short description of the selected flares morphology. A more comprehensive presentation was given in Paper I.

The LDAF of 7 May 1993 occurred in the NOAA AR 7500 at the N14E41. The flare began at 20:30 UT and reached its maximum (M1.6) 50 min later. The decay phase of the flare lasted about 6 h. Four loop-top kernels (A, B, C and D) were observed during the decay phase of the flare (see Fig. 4a).

The 14 May 1993 flare occurred at the N19W48, in the same active region as the 7 May 1993 flare. It began at 21:55 UT and had two maxima. The first one (M1.4) was at 22:05 UT, then the SXR flux decreased until 22:26 UT. The second, higher maximum (M4.4) was reached at 22:58 UT. After that the flare flux decreased for about 8 h. *Yohkoh*/SXT images show that both maxima occurred in the same flare. The flare has four loop-top kernels (A, B, C and D; see Fig. 4b). The kernels B and C were not well separated and this is why they were analysed as one structure (the kernel B+C).

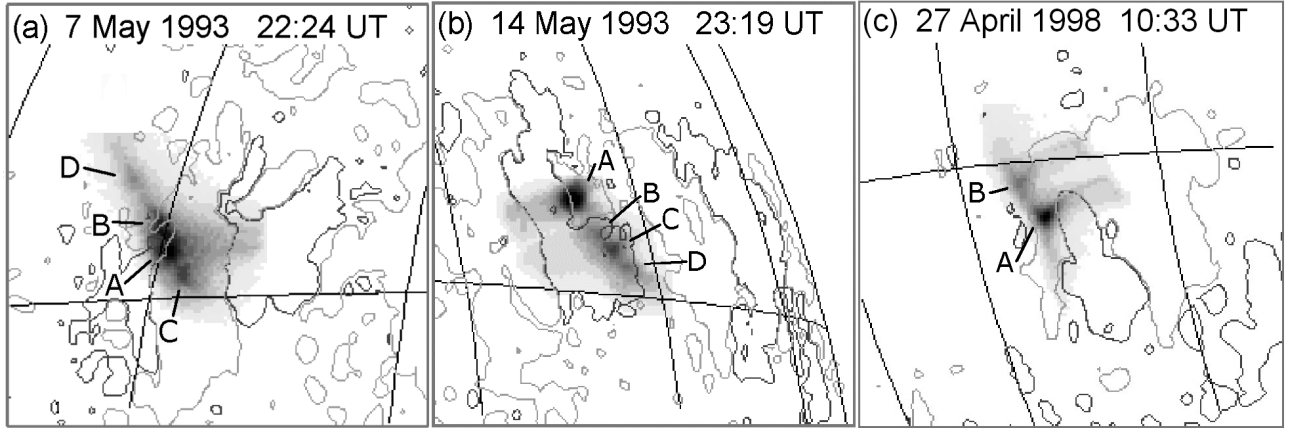


Fig. 4. *Yohkoh*/SXT images in the Al12 filter for the analysed LDAFs. In each image the heliographical grid and the magnetic field configuration taken from the Kitt Peak magnetogram are overlaid (light-grey line: +5 Gs, dark-grey line: -5 Gs).

The X1.0 flare of 27 April 1998 occurred in the NOAA AR 8210 at the S16E50. The flare began at 8:36 UT and was preceded by a slow increase of the soft X-ray. After the flare maximum, which was at 9:20 UT, the SXR flux very slowly decreased for about 20 h. In the SXT images we can see two kernels (A and B) during the early decay phase (see Fig. 4c). Later, after 15 UT, the kernels disappeared and we see in the images a bright structure which connected the tops of arcade loops. The structure is called “the whole arcade channel” in Fig. 7.

3.2. $T - N$ diagram and energy balance

The $T - N$ diagrams for all kernels are shown in Figs. 5–7. Gaps in the decay-phase branches are caused by satellite nights. The inclination ζ_{obs} of these branches are presented in Tables A.1–A.3. The tables give also values of the term $0.5 \frac{d \lg L}{d \lg N}$ and values of ζ for the QSS branch corrected on a flaring loop length increase (ζ_{QSS}). The results of energy balance calculations for kernels are given in Tables A.4–A.6.

3.3. Discussion

3.3.1. Evolution on $T - N$ diagram

Kernels belonging to one flare might be in the different stages of evolution at a given time. For example, while the kernel A of the 7 May flare was on the decay branch, the kernel D was at its ϵ maximum. Moreover, in some cases there are significant differences in E_{H} between kernels of a given flare (see Tables A.4–A.6). These two results may suggest that reconnection is not uniform along the flaring arcade. This conclusion is supported by the morphology (see Paper I). In the case of the 14 May 1993 LDAF, kernels appeared and disappeared sequentially. It looks as if the reconnection developed progressively along the arcade.

In many cases the inclination of the decay-phase branch was not constant and might change significantly over a short time. In some cases this behavior can be explained as a result of the change in the upward motion velocity of a kernel (see kernel B+C before and after 3:00 UT, Table A.2). However in most cases this explanation is not sufficient and we can expect that “bends” in the decay branch are due to some changes in the reconnection rate.

The value of ζ is smaller than 0.3 for all analysed kernels. Cases with $\zeta \approx 0$ are not rare. Such a situation may appear in the early and late decay phase as well. Comparison between the

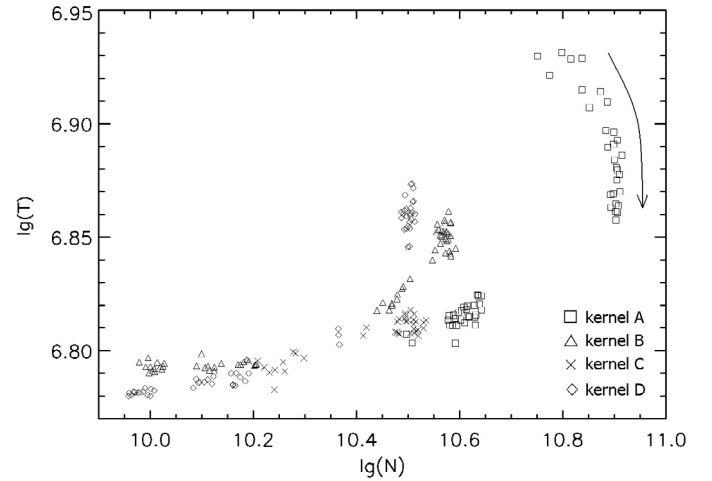


Fig. 5. $T - N$ diagnostic diagram for the decay phase of the 7 May 1993 flare kernels. The evolution runs as the arrow indicates and then from the right to the left.

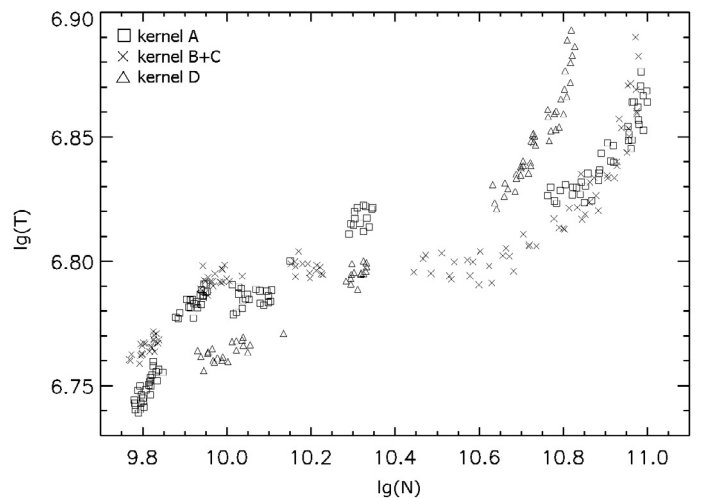


Fig. 6. The same as Fig. 5 but for kernels of the 14 May 1993 flare.

observed inclinations ζ_{obs} and the QSS inclination corrected on the loop length increase (ζ_{QSS}) shows that the first ones are always smaller. This indicates that the kernels were heated during the whole decay phase, which suggests continuous energy

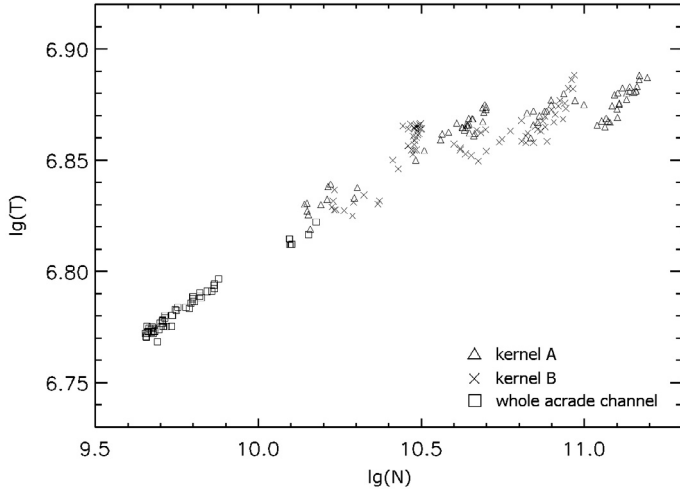


Fig. 7. The same as Fig. 5 but for kernels of the 27 April 1998 flare.

release with e-folding decay time τ longer than thermodynamic decay time τ_{th} . This is confirmed by calculations. Estimated τ for the kernels are in the range of 3000–7000 s and are several times larger than τ_{th} . In some cases differences between ζ_{obs} and ζ_{QSS} are too large to be explained by the instrumental effect described in Sect. 2.1, especially when $\zeta_{obs} \approx 0$. In the paper of Jakimiec et al. (2005) this behavior (so-called below-the-QSS evolution) is explained as being the result of specific evolution of E_H .

3.3.2. Heating rates of the kernels

The calculated energy balance for LDAFs kernels indicates that kernels were heated during their whole decay phase. Values of E_H are small (smaller than $1 \text{ erg cm}^{-3} \text{ s}^{-1}$) but even the lower limit of the heating rate $(E_H)_{min}$ is not zero. This proves that there is energy release during this phase in LDAFs. These results are similar to those obtained by Isobe et al. (2002) and Bąk-Stęślicka & Jakimiec (2005). Calculated heating rates decreased very slowly with time. This confirms conclusions derived from the $T - N$ diagrams.

A very interesting result of our investigation is that the kernels cannot be distinguished in SXT images when E_H drops below a particular value. This value seems to depend on the altitude (or loop semilength; see Fig. 8). This suggests that at a given altitude above the photosphere, loop-top kernels cannot exist and flaring loops become more uniformly bright when the heating/energy release rate drops below a particular value. The higher the altitude of a kernel the lower the rate of heating necessary to support the kernel existence. This relation can be easily explained. From Tables A.4–A.6 we see that

$$\left| \left(\frac{d\mathcal{E}}{dt} \right)_{obs} - \left(\frac{d\mathcal{E}}{dt} \right)_{ad} \right| \approx 0 \quad (5)$$

and hence

$$E_H \approx E_C + E_R = 3.9 \times 10^{-7} \frac{T^{3.5}}{Lr} + N^2 \Phi(T). \quad (6)$$

In Preś & Kołomański (submitted) it is shown for loop-top kernels at the same evolution stage that temperature does not depend on altitude, density decreases slightly with h and kernel radius r increases with h . Of course, the higher the altitude, the longer the loop semilength is. The value of the radiative loss function $\Phi(T)$ shows small changes in the temperature range of LDAFs kernels. From these relations we see that losses E_C and E_R decrease

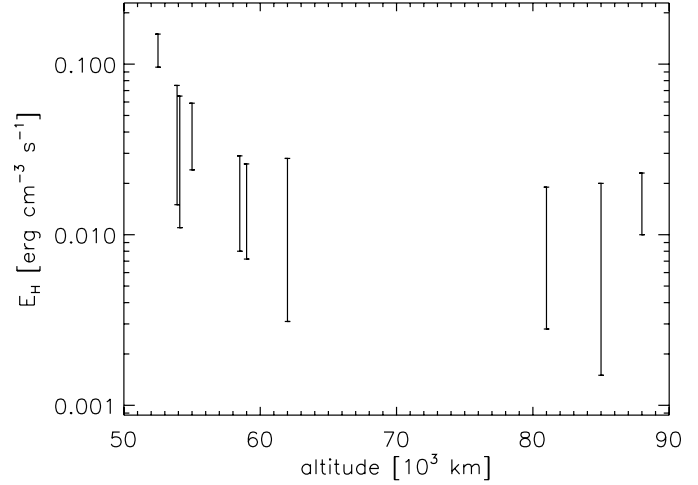


Fig. 8. Relation between the altitude and heating rate E_H at the moment when analysed kernels could not be distinguished in SXT images. Error bars are defined by $(E_H)_{min}$ and $(E_H)_{max}$.

with altitude. Hence, at higher altitude the lower heating rate is needed to balance the losses and to support the kernel existence.

4. Conclusions

Since *Skylab* observations it has been known that continuous energy release must take place during the decay phase of long-duration flares. In this paper we qualitatively and quantitatively described the evolution of this process. We applied two methods to the *Yohkoh*/SXT observations of LDAFs. The conclusions of our investigation are as follows:

1. The energy release in LDAFs occurs during their whole decay phase.
2. The kernel heating (E_H) is of the order of 0.01 – $1 \text{ erg cm}^{-3} \text{ s}^{-1}$.
3. The kernels usually cannot be distinguished in SXT images when E_H is drops below a particular value. This value depends on the altitude of the kernels.

The new solar observatory *Hinode* will provide X-ray images with better angular resolution than *Yohkoh*. The observations will allow us to continue the study of the energy release in the LDAF decay phase. Moreover, *Hinode* will provide high resolution magnetograms of the photospheric magnetic fields (the longitudinal and transverse component). In Isobe et al. (2002) the method to derive the reconnection rate from X-ray images and magnetograms was presented. The new, high quality *Hinode* X-ray images and magnetograms will allow us to use the method to study the magnetic reconnection process in the LDAF decay phase with high angular resolution.

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Online Material

Appendix A: Tables**Table A.1.** Evolution during the decay phase for the 7 May 1993 flare.

Time period [UT]	ζ_{obs}	$0.5 \frac{d\lg L}{d\lg N}$	ζ_{QSS}
kernel A			
22:24–22:40	0.16	−0.07	0.43
kernel B			
22:40–23:19	0.25	−0.07	0.43
00:03–00:57	0.01	−0.00	0.50
kernel C			
22:24–22:40	0.03	−0.21	0.29
22:40–23:19	0.11	−0.07	0.43
kernel D			
00:03–00:57	0.04	−0.00	0.50

Table A.2. Evolution during the decay phase for the 14 May 1993 flare.

Time period [UT]	ζ_{obs}	$0.5 \frac{d\lg L}{d\lg N}$	ζ_{QSS}
kernel A			
23:41–01:40	0.02	−0.09	0.41
01:40–02:48	0.15	−0.13	0.37
02:48–04:06	0.00	−0.15	0.35
04:06–06:18	0.30	−0.00	0.50
kernel B+C			
23:10–23:30	0.14	−0.13	0.37
23:30–03:00	0.03	−0.16	0.34
03:00–04:51	0.18	−0.03	0.47
kernel D			
23:43–03:16	0.10	−0.10	0.40

Table A.3. Evolution during the decay phase for the 27 April 1993 flare.

Time period [UT]	ζ_{obs}	$0.5 \frac{d\lg L}{d\lg N}$	ζ_{QSS}
kernel A			
09:38–09:55	0.17	−0.17	0.33
10:00–11:20	0.03	−0.23	0.27
11:30–14:42	0.08	−0.17	0.33
kernel B			
09:38–09:55	0.15	−0.15	0.35
10:00–11:20	0.00	−0.28	0.22
11:30–14:42	0.15	−0.32	0.18

Table A.4. Energy balance for the kernels of the 7 May 1993 flare.

Time period [UT]	$(d\mathcal{E}/dt)_{\text{obs}}$	$(d\mathcal{E}/dt)_{\text{ad}}$	E_C	E_R	$(E_H)_{\text{max}}$	$(E_H)_{\text{min}}$
[erg cm ⁻³ s ⁻¹]						
kernel A						
21:41–22:24	–0.046	–0.065	0.072	0.20	0.29	0.22
22:24–22:40	–0.037	–0.056	0.052	0.076	0.15	0.096
kernel B						
22:40–23:01	–0.0088	–0.0120	0.057	0.058	0.12	0.062
23:01–23:19	–0.014	–0.020	0.048	0.046	0.099	0.052
23:19–00:03	–0.013	–0.0190	0.032	0.027	0.066	0.034
00:03–00:20	–0.0072	–0.0120	0.023	0.012	0.040	0.017
00:20–00:43	–0.0048	–0.0081	0.022	0.0080	0.033	0.011
00:43–00:57	–0.0034	–0.0058	0.021	0.0056	0.029	0.0080
kernel C						
22:24–22:40	–0.023	–0.037	0.039	0.049	0.10	0.063
22:40–23:01	–0.013	–0.021	0.034	0.029	0.071	0.036
23:01–23:19	–0.0095	–0.016	0.035	0.018	0.059	0.024
kernel D						
23:09–00:03	–0.0075	–0.011	0.036	0.021	0.060	0.024
00:03–00:20	–0.0063	–0.0099	0.025	0.011	0.040	0.015
00:20–00:43	–0.0055	–0.0089	0.020	0.0077	0.031	0.011
00:43–00:57	–0.0035	–0.0055	0.018	0.0052	0.026	0.0072

Table A.5. Energy balance for the kernels of the 14 May 1993 flare.

Time period [UT]	$(d\mathcal{E}/dt)_{\text{obs}}$	$(d\mathcal{E}/dt)_{\text{ad}}$	E_C	E_R	$(E_H)_{\text{max}}$	$(E_H)_{\text{min}}$
[erg cm ⁻³ s ⁻¹]						
kernel A						
23:05–23:54	–0.059	–0.089	0.13	0.40	0.56	0.43
23:54–01:22	–0.019	–0.031	0.075	0.10	0.19	0.11
01:22–02:26	–0.0063	–0.0094	0.053	0.018	0.074	0.022
02:26–03:16	–0.0035	–0.0055	0.037	0.0084	0.047	0.010
03:16–04:06	–0.0012	–0.0019	0.030	0.0052	0.036	0.0059
04:06–04:51	–0.0015	–0.0022	0.027	0.0039	0.031	0.0046
04:51–05:45	–0.00065	–0.00063	0.026	0.0031	0.029	0.0030
05:45–06:18	–0.0014	–0.0020	0.025	0.0025	0.028	0.0031
kernel B+C						
23:05–23:33	–0.10	–0.13	0.092	0.28	0.40	0.31
23:33–01:22	–0.012	–0.021	0.039	0.071	0.11	0.079
01:22–02:26	–0.0041	–0.0068	0.024	0.011	0.038	0.014
02:26–03:16	–0.0020	–0.0031	0.020	0.0053	0.026	0.0065
03:16–04:06	–0.0018	–0.0025	0.018	0.0034	0.022	0.0041
04:06–04:51	–0.0010	–0.0015	0.016	0.0024	0.019	0.0028
kernel D						
23:05–23:54	–0.024	–0.021	0.097	0.11	0.21	0.11
23:54–01:22	–0.012	–0.018	0.031	0.060	0.098	0.066
01:22–02:26	–0.0059	–0.0086	0.016	0.018	0.037	0.021
02:26–03:16	–0.0042	–0.0068	0.014	0.0074	0.023	0.010

Table A.6. Energy balance for the kernels of the 27 April 1998 flare.

Time period [UT]	$(d\mathcal{E}/dt)_{\text{obs}}$	$(d\mathcal{E}/dt)_{\text{ad}}$	E_C	E_R	$(E_H)_{\text{max}}$	$(E_H)_{\text{min}}$
	[erg cm ⁻³ s ⁻¹]					
	kernel A					
09:38–09:50	−0.18	−0.25	0.32	0.97	1.37	1.04
10:00–10:13	−0.083	−0.13	0.27	0.39	0.72	0.44
10:22–10:33	−0.027	−0.033	0.25	0.25	0.50	0.25
11:17–11:28	−0.027	−0.034	0.18	0.11	0.30	0.12
11:42–11:55	−0.019	−0.028	0.14	0.073	0.23	0.082
12:12–12:58	−0.012	−0.018	0.088	0.034	0.13	0.040
13:32–13:49	−0.0040	−0.0051	0.058	0.013	0.073	0.014
14:33–14:42	−0.0012	−0.0019	0.054	0.010	0.065	0.011
	kernel B					
09:38–09:50	−0.12	−0.17	0.28	0.34	0.66	0.38
10:00–10:13	−0.036	−0.060	0.18	0.15	0.36	0.17
10:22–10:33	−0.034	−0.052	0.17	0.094	0.28	0.11
11:17–11:28	−0.0029	−0.0056	0.14	0.048	0.19	0.050
11:42–11:55	−0.0063	−0.010	0.13	0.040	0.18	0.044
12:12–12:58	−0.0035	−0.0041	0.096	0.031	0.13	0.032
13:32–13:49	−0.0056	−0.0074	0.071	0.021	0.095	0.023
14:33–14:42	−0.0032	−0.0027	0.060	0.015	0.075	0.014