

Semi-classical Stark broadening calculations of HeI lines in a non-ideal plasma

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ABSTRACT

New semi-classical collision functions are used to compute the inelastic contribution to the impact electronic total width, by considering three interaction potentials (Coulomb Debye, Cut-off, and Ion Sphere). Numerical results are calculated for the neutral helium 6678 Å ($2^1P^o-3^1D$) and 5876 Å ($2^3P^o-3^3D$) visible lines. The lines corresponding to these transitions are isolated, and the plasma is weakly non-ideal for all temperatures and electronic densities of interest. For electronic collisions, semi-classical perturbation theory is sufficient and the impact approximation is well satisfied. The ion effects can be treated within the quasistatic approximation, and the quasistatic ionic contribution is dominated by the polarization (or quadratic) r_p^{-4} -interaction. To consider both the electron and the ion effects, the microfield distributions and the complete reduced Stark profile of isolated line are calculated using different methods. The computed total widths corresponding to the three interaction potentials are compared to the available experimental widths and then approximated by appropriate formulae. The data we obtained provide an opportunity to test various approximations included in the semi-classical perturbation formalism. They are also of interest for stellar spectroscopic diagnosis in dense atmospheres (white dwarfs for instance).

Key words. atomic data – line: profiles – atomic processes

1. Introduction

Stark broadening of spectral lines by interactions of radiating atoms or ions with perturbing electrons is of great importance for a number of astrophysics applications. It is found to be a reliable tool for characterizing strongly coupled plasmas that have become experimentally more accessible in recent years. This requires, in practice, a detailed knowledge of the various governing atomic processes, especially for dense plasmas where the screening effects are not negligible (Song & Jung 2003). To describe the interactions between the perturbing electrons and the emitting atoms in these non-ideal plasmas, we may use either the Cut-off V^C (Ben Nessib et al. 1997) or the Ion Sphere models V^{IS} (Salzmann & Szichman. 1987; Gutierrez 1994; Jung & Yoon 2000a), where appropriate corrective terms for the Coulomb potential are introduced.

In a previous paper (Ben Chaouacha et al. 2004), we modified the standard formalism of Stark impact broadening of spectral lines by using the cut-off V^C and the ion sphere V^{IS} interaction potential instead of the Coulomb-Debye V^{CD} one, which should be more appropriate at high densities. Thus we have derived new semi-classical collision functions for both the transition probability and the cross section in the case of electron-atom collisions. These new functions take into account the plasma screening effects by introducing a reliable cut-off in the interaction potential when the electron-atom distance exceeds a certain radius. They will be used here in order to compute the inelastic contribution to the impact electronic total width: the upper

cut-off at R_D (Debye length) for the Coulomb Debye model has been replaced by R_c (mean distance between particles) for the Cut-off and the Ion Sphere models; see below.

The purpose of this paper is to validate our theoretical approach. Our numerical results will be compared to experimental widths. Helium is selected as an example because of its importance in stellar spectra, and because it is a simple atomic system so that the wave functions are calculated with fair accuracy (Griem 1964, 1974; Konjević et al. 2002).

In a recent paper, Omar et al. (2006) investigated Stark widths of isolated neutral helium lines at electron densities less than $5 \times 10^{17} \text{ cm}^{-3}$ using thermodynamic Green functions.

A detailed analysis of the broadening of helium spectral lines of dense plasmas can be used to test our understanding of correlation effects in these plasmas. The cases of the 6678 Å ($2^1P^o-3^1D$) and 5876 Å ($2^3P^o-3^3D$) HeI visible lines are chosen by considering the same conditions of densities N_e and temperatures T as the experiments of Gauthier et al. (1981) and Bücher et al. (1995), and an upper cut-off at R_D for the Coulomb Debye model and at R_c for the Cut-off and the Ion Sphere models.

The impact inelastic electronic widths $W_{e,inel}^{CD}$, $W_{e,inel}^C$ and $W_{e,inel}^{IS}$ are obtained with the three different potentials, but the contribution of the elastic electronic collisions $W_{e,el}^{CD}$ will be calculated only with the Coulomb Debye model. Since the very long-range collisions are not important for the elastic contribution, it is expected to be relatively weak for this line. In addition, it will be possible to consider that the results for the elastic

contribution should not be very different in the case of the Cut-off and the Ion Sphere potentials.

For the studied lines, the contribution of the collisions with the ions of the plasma is important and cannot be ignored. It is quasistatic at the considered densities, that are rather high ($4 \times 10^{17} \text{ cm}^{-3} < N_e < 9 \times 10^{17} \text{ cm}^{-3}$, for the 6678 Å line). The adiabatic assumption is always valid for the ion broadening of isolated lines. The quasistatic ionic contribution is dominated by the polarization (or quadratic) r_p^{-4} -interaction.

To consider both the ionic and the electronic effects, the total width will be obtained from the Full Width at Half Maximum (FWHM) deduced from the complete reduced Stark profile $j_{A,r}(x)$ of isolated lines. The profile depends on the Debye shielding parameter r and the quasistatic quadratic ion broadening parameter A which must be related to the impact electronic total width; the associated microfield distribution W_r will be calculated with: (a) Baranger & Mozer's method (1959, 1960); (b) Hooper's method (Hooper 1966, 1968a,b); and (c) the Analytic Fitting Formulas (AFF) method (Potekhin et al. 2002).

The computed total widths $W_{\text{tot}}^{\text{CD}}$, $W_{\text{tot}}^{\text{C}}$ and $W_{\text{tot}}^{\text{IS}}$ will be compared to the experimental widths W^{exp} (Gauthier et al. 1981; Bücher et al. 1995).

The results obtained in the present paper provide an opportunity to test various approximations included in the semi-classical perturbation formalism.

This paper is divided into five sections. In Sect. 2, we give some theoretical background with the basic assumptions and equations regarding: i) the non-ideality factor γ and the plasma classification; ii) the isolated line approximation; iii) the validity criteria of the impact approximation; iv) the Stark broadening impact theory of isolated lines; v) the main interaction potentials describing the non-ideal plasmas; vi) the collision functions associated with the inelastic cross-section and the transition probability; and vii) the numerical methods used to derive the electrical microfield distributions. The validity criteria of our investigated theoretical approach, as well as the applicability range of the main governing parameters, are discussed in this section. Section 3 deals with the description of the numerical method used to calculate the different contributions to the width. Section 4 discusses the effects of the parameters that govern the different contributions to the width calculated for the considered lines.

Then, we compare the three total widths $W_{\text{tot}}^{\text{CD}}$, $W_{\text{tot}}^{\text{C}}$ and $W_{\text{tot}}^{\text{IS}}$ with the experimental widths W^{exp} relative to the same transitions (Gauthier et al. 1981; Bücher et al. 1995), and approximate them with appropriate formulae. Section 5 summarizes the main results and gives some related open problems.

2. Theoretical background

We present here a brief summary of the theory because Stark broadening impact theory has been extensively developed since the fundamental work by Baranger (1958a,b,c).

2.1. Non-ideality factor γ

Plasmas may be classified into different types, depending on their temperature T and their electronic density N_e (Günther et al. 1985; Ben Nessib et al. 1997). A plasma is ideal if the interactions between particles of the medium can be neglected. Non-ideality may be due to charge-charge, charge-neutral and neutral-neutral interactions. At extremely high densities, atomic valence electrons are shared by other atoms; such a dense plasma

is similar to liquid metals, though its free electrons are not necessarily degenerate. This type of plasma is called non-ideal, strongly coupled, non-Debye, or simply dense plasma.

Non-ideal plasmas cover the range of densities between gases and solids. These may be obtained by gas plasma compression or by extension and heating of solids and liquids. In these conditions, the mean interaction potential energy E_p between charged particles is not small compared with their kinetic energy E_k .

Contrary to low pressure plasmas, where the kinetic energy E_k of a particle is always high in comparison to the mean interaction potential energy E_p between two neighboring charged particles, in dense plasmas it is of the same order of magnitude or even lower than E_p . Thus, the so-called non-ideality parameter γ that characterizes this behavior:

$$\gamma = \frac{E_p}{E_k}, \quad (1)$$

is expected to be greater than unity ($\gamma \geq 1$).

At high neutral density, non-ideality due to neutrals is also possible, but if we restrict ourselves only to charged-particle interaction, the potential energy E_p may be expressed as (Vitel et al. 1990):

$$E_p = \frac{Z^2 e^2}{4\pi\epsilon_0 r_0}, \quad (2)$$

where the radius r_0 is related to the ion charge Z and the electron concentration N_e by:

$$r_0 = \left(\frac{3Z}{4\pi N_e} \right)^{\frac{1}{3}}. \quad (3)$$

The velocity average \bar{v} involved in the electron kinetic energy ($E_k = \frac{1}{2} m_e \bar{v}^2$), is expressed as (Freudenstein 1978):

$$\bar{v} = (3k_B T / m_e)^{1/2}, \quad (4)$$

which is expected to be convenient, because the most important contribution to the widths comes from high velocities due to the properties of the collision functions $a(z)$. The non-ideality factor γ is expressed as follows:

$$\gamma = 2.693 \cdot 10^{-3} \frac{(N_e)^{1/3}}{T}. \quad (5)$$

The electronic density N_e is expressed in cm^{-3} and the plasma temperature T in Kelvin. For a constant plasma density N_e , the plasma temperature T decreases when the non-ideality factor γ increases. Hence, the main physical characteristics are expected to be significantly different from one plasma type to another, which needs systematically different theoretical and experimental approaches to study their spectral responses.

Depending on the value of γ , the considered plasma may be qualified either as ideal, weakly coupled, coupled, or strongly coupled. Unfortunately, a γ -range relative to each of these plasma types is not yet precisely defined in the literature, which may be ascribed mainly to the lack of sufficient experimental data, especially for both the coupled and strongly coupled plasmas. In modern plasma experiments, γ may approach unity, whereas in stellar matter it can be much larger. In these cases, correlations between plasmas particles should not be neglected.

Table 1 gives the values of the non-ideal factor γ for the studied lines, calculated by considering the conditions of densities N_e and temperatures T of the experiments of Gauthier et al. (1981)

Table 1. Validity criteria for the isolated line approximation and the impact approximation, calculated for the considered HeI transitions. γ : non-ideality factor – N_e/N_i : ratio of the electronic density to the maximum electron density for which the line may be considered as isolated – C_{impact}^e : impact approximation validity criterion for the electronic collisions – C_{impact}^i : impact approximation validity criterion for the ionic collisions – $C_{\text{impact}}^{s,e}$: impact approximation validity criterion for the strong electronic collisions – $C_{\text{impact}}^{s,i}$: impact approximation validity criterion for the strong ionic collisions.

Transition	T (10^4 K)	N_e (10^{17} cm $^{-3}$)	γ	N_e/N_i	C_{impact}^e (10^{-3})	C_{impact}^i	$C_{\text{impact}}^{s,e}$ (10^{-3})	$C_{\text{impact}}^{s,i}$
$(2^1\text{P}^\circ - 3^1\text{D})$ 6678 Å	1.35	2.0	0.116	0.19	38.3	3.72	4.7	2.0
	1.78	3.3	0.104	0.29	45.0	5.42	5.5	3.0
	1.86	4.9	0.114	0.35	59.5	7.65	7.9	4.4
	1.93	6.2	0.119	0.44	68.6	9.14	9.4	5.5
	2.01	6.9	0.118	0.46	72.3	9.92	10.1	6.0
	2.13	8.4	0.119	0.56	79.8	11.34	11.4	7.1
	2.09	8.9	0.124	0.58	84.8	11.76	12.4	7.7
	2.28	10.0	0.118	0.64	86.4	12.82	12.6	8.3
	2.32	10.7	0.119	0.68	89.8	13.41	13.2	8.8
	2.40	11.8	0.119	0.72	94.0	14.27	14.0	9.5
	2.44	13.2	0.121	0.79	100.6	15.13	15.4	10.5
$(2^3\text{P}^\circ - 3^3\text{D})$ 5876 Å	2.59	13.7	0.116	0.81	99.0	15.79	14.9	10.7
	2.55	14.9	0.121	0.91	106.4	16.27	16.5	11.6
	4.46	4.9	0.157	0.07	19.4	0.80	3.0	0.4
	5.20	10.2	0.200	0.15	34.7	1.55	5.5	0.8
	5.21	12.0	0.211	0.18	40.3	1.82	6.4	0.9
	5.60	18.4	0.244	0.26	56.5	2.70	9.2	1.4
	6.35	24.9	0.270	0.35	67.9	3.44	11.1	1.8

and Bücher et al. (1995). As $\gamma \approx 0.12$ for the 6678 Å line and $\gamma < 0.3$ for the 5876 Å line, the considered plasmas are weakly non-ideal for these densities.

Another physical parameter allowing a quantitative comparison of the different plasma types is the number of particles in the Debye sphere, N_D , which is defined by:

$$N_D = \frac{4}{3}\pi R_D^3 (N_e + N_i), \quad (6)$$

where $N_i = N_e$ designates the ion density and R_D the Debye radius, which is expressed by:

$$R_D = \left(\frac{k_B T}{4\pi N_e e^2} \right)^{\frac{1}{2}}. \quad (7)$$

Weakly non-ideal means that there is approximately one charged particle in the Debye sphere ($N_D = 1$). Strongly non-ideal means that there are about one tenth or fewer particles in the Debye sphere. This condition implies that the Debye theory is no longer valid.

2.2. Isolated line approximation

It is not necessary to discuss uncertainties arising from all the approximations involved in the broadening calculations, since the criteria for their application are given in detail elsewhere (Sahal-Bréchet 1969a,b). However, we recall the conditions of validity for the isolated line approximation (Sahal-Bréchet 1969a,b; Dimitrijević & Sahal-Bréchet 1984a,b).

A line is isolated if non-degenerate energy levels broadened by collisions do not overlap. Denoting by $2w_i$ and $2w_f$ the corresponding level widths, we can express the specified conditions by:

$$2w_i \leq \omega_{i'f}, \quad 2w_f \leq \omega_{ff'}, \quad (8)$$

where $\omega_{j'j}$ ($j = i, f$) is the energy distance to the nearest perturbing level [$\omega_{j'j} = \min(\omega_{i'f}, \omega_{ff'})$]. If $w \leq \omega_{j'j}$, where w is the half-width of the line, the line can be considered as isolated. Thus, if we want to make certain that the line is isolated, we must verify that (Dimitrijević & Sahal-Bréchet 1984a,b):

$$2w(\text{Å}) \leq C/10^{16}, \quad (9)$$

where

$$C = 10^8 \lambda^2 (\text{Å}) [(E_j - E_{j'}) (\text{cm}^{-1})]. \quad (10)$$

If half-widths are available for a certain electron density N_e (e.g., 10^{16} cm $^{-3}$, as reported in Dimitrijević & Sahal-Bréchet 1984a,b, 1990), an electron density N_i (cm $^{-3}$) is defined as:

$$N_i = \frac{C}{2w(\text{Å})} \times \frac{N_e}{10^{16}}. \quad (11)$$

So, for an electron density lower than N_i , the line can be treated as isolated in the core, even if weak forbidden components due to the failure of this approximation still appear in the wings (Dimitrijević & Sahal-Bréchet 1984b). If $\frac{N_e}{N_i} > 1$ we have to treat the problem of overlapping lines.

For the 6678 Å line, the energy distance between the upper level (3^1D) and its nearest perturbing level (3^1P°) is $\Delta E_{j'j} = 100$ cm $^{-1}$, so $C = 4.5 \times 10^{17}$, while for the 5876 Å line, $\Delta E_{j'j} = 537$ cm $^{-1}$ and $C = 1.8 \times 10^{18}$. Table 1 shows that the ratio $\frac{N_e}{N_i}$ is less than unity, especially when the temperature decreases. Thus the lines corresponding to these transitions are well isolated in these conditions.

2.3. Validity criteria of the Impact approximation

As already discussed by Baranger (1958c, 1962) and Sahal-Bréchet (1969a,b), the impact (or binary) approximation

is valid when the average effect of collisions is weak, or equivalently when strong collisions are separated in time. Following Baranger (1958a,b,c), the condition of validity of the impact approximation has been rederived by Ben Nessib et al. (1996):

$$C_{\text{impact}} = N \times \pi \frac{4}{3} \rho_{\text{typ}}^3 \sim N \pi \rho_{\text{typ}}^3 \ll 1, \quad (12)$$

where $\rho_{\text{typ}} = \tau_{\text{typ}} \bar{v}$ is a typical impact parameter for strong collisions and N is the density of the perturbers.

A typical value of the impact parameter ρ_{typ} can be obtained by

$$2w = N \bar{v} \pi \rho_{\text{typ}}^2. \quad (13)$$

The mean duration of a typical collision, the so-called collision time τ_{typ} , must be very much smaller than the mean interval

$$\Delta T = \frac{1}{2w} \text{ between two collisions:}$$

$$\tau_{\text{typ}} = \frac{\rho_{\text{typ}}}{\bar{v}} \ll \frac{1}{N \bar{v} \pi \rho_{\text{typ}}^2}, \quad (14)$$

that gives:

$$N \pi \rho_{\text{typ}}^3 \ll 1. \quad (15)$$

This means that the collision volume $\pi \frac{4}{3} \rho_{\text{typ}}^3$ must be very small compared to the inverse of the density of the perturbers N . In other words, there is only one particle at the same time in the collision volume. This condition is well verified by electronic collisions for a large range of densities. However, at high densities ($N_e \geq 10^{18} \text{ cm}^{-3}$), one must check if the validity criterion of the electron-impact approximation ($\rho w / \bar{v} \ll 1$) is fulfilled or not. This is a general problem of dense plasmas, since the criterion cannot remain fulfilled with increasing densities for a constant temperature (Griem et al. 1962; Griem 1974).

If the plasma is strongly non-ideal (high density and low temperature), ρ_{typ} is of the order of the thermal de Broglie length $\lambda = \frac{\hbar}{m_e \bar{v}}$. Thus, for strongly non-ideal plasmas, the validity criterion for the impact approximation can be written as follows (Ben Nessib et al. 1997)

$$T N_e^{-2/3} > \left(\frac{4\pi}{3} \right)^{2/3} \frac{\pi \hbar^2}{8 m_e k_B}. \quad (16)$$

So, if the temperature is expressed in Kelvin and the density in cm^{-3} , this condition becomes $T N_e^{-2/3} > 9.02 \times 10^{-12}$.

This allows Ben Nessib et al. (1997) to construct a diagram representing the different plasma conditions, which shows that there is a region where the impact approximation is valid for a strongly non-ideal plasma.

Table 1 shows the impact validity criteria for the two studied lines, by considering the same conditions of densities N_e and temperatures T as the experiments of Gauthier et al. (1981) and Bücher et al. (1995) and the Coulomb Debye model with an upper cut-off at R_D .

For the 5876 Å line, the impact approximation is always fulfilled for collisions with electrons: the corresponding value of C_{impact}^e is small compared to unity. For the 6678 Å line, C_{impact}^e is of the order of 0.1 which corresponds to the limit of the impact approximation. As reported in Gauthier et al. (1981), the impact approximation for the treatment of the electrons breaks down at densities greater than 10^{18} cm^{-3} .

Since the strong electronic collisions are well separated in time (for the 6678 Å line, $C_{\text{impact}}^{s,e}$ are of the order of 5×10^{-3} to 10^{-2}), the impact approximation remains valid. Weak collisions can be treated by the perturbation theory, and thus their contributions are additive, allowing us to treat them with the impact theory (Baranger 1958a,b,c, 1962), even if C_{impact}^e is not very small compared to unity.

Concerning collisions of neutral atoms with ions, the impact approximation is most often valid in the physical conditions of hot stellar atmospheres where the density is weak (10^{10} to 10^{14} cm^{-3}) and where the ion perturbers are light, such as protons and He^+ ions. For example, at $N_e = 10^{13} \text{ cm}^{-3}$, one obtains $C_{\text{impact}}^i = 1,66 \times 10^{-4}$. In laboratory experiments, the density is higher (10^{16} – 10^{18} cm^{-3}) and the perturbers are heavier (Ar^+ for instance). At medium densities (10^{16} cm^{-3}), ion dynamics effects are generally not negligible and have to be considered (Ben Nessib et al. 1996). At high densities (10^{17} cm^{-3} and more), the impact approximation breaks down and the quasistatic approximation must be applied. In the studied experiment, the density is high (10^{18} cm^{-3} and more) and the quasistatic approximation is reliable. We will show in Sect. 3 that the quadratic interaction is predominant and the quadrupolar one is negligible.

2.4. Stark broadening impact theory of isolated lines

The semi-classical description has been extensively used for Stark broadening calculations and for collisional transition probabilities entering the statistical equilibrium equations for non-Local Thermodynamical Equilibrium (N-LTE) studies. The calculation procedure is well described elsewhere (Sahal-Bréchet 1969a,b). We recall the basic formulae leading to the evaluation of electron impact-broadening parameters of isolated spectral lines, within the framework of semi-classical perturbational formalism.

Within the impact approximation, the profile is Lorentzian for isolated lines. Overlapping lines are outside the scope of the present study. The following set of equations was used for the computation of the impact total electron width W_e (in angular frequency units).

For the line corresponding to the transition between the initial level i and the final level f , the half-width w and the shift d are given by Baranger's formula (Baranger 1958c)

$$w + id = N_e \int_0^\infty v f(v) dv \int_0^\infty 2\pi \rho d\rho \times \left\{ 1 - \langle i | S | i \rangle \langle f | S^{-1} | f \rangle \right\}_{AV}, \quad (17)$$

where $w + id$ is a complex number ($i^2 = -1$). N_e denotes the electron density, S , the scattering matrix obtained for the atom-perturber interaction corresponding to the impact parameter ρ of the incoming electron and the relative velocity v , $f(v)$, the relative atom-perturber Maxwell distribution of velocities, and, $\{\dots\}_{AV}$, the angular average over the magnetic quantum numbers which will not be detailed here.

Equation (17) is the general result to be used in all cases where electron broadening is treated by the impact approximation. In the derivation by Sahal-Bréchet (1969a,b), the line-width can be expressed in terms of elastic and inelastic contributions. For the transition between the levels $i(n_i l_i L_i S_i J_i)$ and $f(n_f l_f L_f S_f J_f)$, the full width at half intensity $W_e = 2w_e$

can be put in the form (Sahal-Bréchet 1969a,b; Dimitrijević & Sahal-Bréchet 1984a,b, 1985)

$$W_e = 2w_e = N_e \int_0^\infty v f(v) dv \sigma_t(v), \quad (18)$$

where the total cross-section $\sigma_t(v)$ is defined by

$$\sigma_t(v) = \sum_{j \neq i} \sigma_{ij}(v) + \sum_{j' \neq f} \sigma_{fj'}(v) + \sigma_{el}, \quad (19)$$

where j and j' respectively denote the levels that perturb i and f .

The inelastic cross-sections $\sigma_{ij}(v)$ (resp. $\sigma_{fj'}(v)$) are given by an integration over the impact parameter ρ of the transition probabilities $P_{ij}(v, \rho)$ (resp. $P_{fj'}(v, \rho)$) as

$$\begin{aligned} \sum_{j \neq i} \sigma_{ij}(v) &= \pi R_1^2 \sum_{j \neq i} P_{ij}(v, R_1) \\ &+ \int_{R_1}^{R_D} 2\pi \rho d\rho \sum_{j \neq i} P_{ij}(v, \rho). \end{aligned} \quad (20)$$

The expression for P_{ij} (resp. $P_{fj'}$) is given within the first order time dependent perturbation theory by an average over the initial Zeeman states M_i and a sum over the final states M_j (Seaton 1962)

$$\begin{aligned} P_{ij}(\rho, v) &= \frac{1}{2J_i + 1} \sum_{M_i, M_j} \frac{1}{\hbar^2} \\ &\times \left| \int_{-\infty}^{+\infty} \langle n_i l_i J_i M_i | V(t) | n_j l_j J_j M_j \rangle \exp\left(\frac{i(E_j - E_i)t}{\hbar}\right) dt \right|^2, \end{aligned} \quad (21)$$

where $V(t)$ denotes the interaction potential between the atom and the charged perturber moving along a classical path at time t , and E_i (resp. E_j), the energy of the i (resp. j) level.

The elastic cross-section σ_{el} is given by

$$\sigma_{el} = 2\pi R_2^2 + \int_{R_2}^{R_D} 8\pi \rho d\rho \sin^2 \delta, \quad (22)$$

with

$$\delta = (\Phi_p^2 + \Phi_q^2)^{1/2}, \quad (23)$$

where the phase-shifts Φ_p and Φ_q are respectively due to the polarization potential ($\sim r^{-4}$) and the quadrupolar potential ($\sim r^{-3}$) parts (Sahal-Bréchet 1969a,b). We refer to the original papers by Sahal-Bréchet (1969a,b) for the choice of the cut-offs R_1 and R_2 .

The transition probabilities, the cross-sections and the impact parameter are symmetrized, in order to ensure the unitarity and the symmetry of the collision S-matrix. We refer to Seaton (1962), Feautrier (1968) and Sahal-Bréchet (1969a,b) for details of the symmetrization procedures.

2.5. Interaction potentials in plasmas

In the standard formalism of Stark impact broadening of spectral lines and of cross sections, the electrostatic Coulomb potential is used to describe the interaction between the perturbing electrons and the emitting atom. It is well known, however, that the extreme conditions of some plasma environments can drastically alter transition rates from their values for the corresponding isolated systems. Long-range Coulomb interactions are screened by plasmas, leading to shorter-range interactions (Stewart & Pyatt 1966). The effect of the plasma was modelled in these collision studies by static screened interactions, the justification of

which requires some rather specific conditions (Weisheit 1984; Scheibner et al. 1987). First, the reciprocal of the electron-ion collision duration, $1/\tau_{ei} = \nu_{ei}$, must be less than the plasma (electron) frequency, $\nu_e = \left(\frac{4\pi e^2 N_e}{m_e}\right)$. If this condition is not fulfilled, plasma screening of the target may not be accurately represented by a static potential arising from the average electronic charge density in the ion's vicinity. Second, substantial screening of the electronic interaction is achieved only when the threshold energy of the excitation, ΔE , is less than $h\nu_e$; otherwise the bound electron's motion is too fast to permit screening by most of the free electrons. Furthermore, in the absence of plasma screening, it is known that as the ratio of $k_B T / \Delta E$ increases, the relative importance of ion-impact excitation increases with respect to electron-impact excitation.

In the case of a weakly coupled plasma, the amount of the Coulomb forces in the interaction energy may be defined by the Debye-Hückel theory which corresponds to a classical treatment of the charged particle interactions (Debye & Hückel 1923). In standard Stark broadening calculations, the following approximation is most often used:

$$\begin{cases} V^{CD}(t) = \frac{Z_p e^2 (Z + N)}{r_p} \\ -Z_p e^2 \sum_{i=1}^N \frac{1}{r_{ip}}; r_p \leq R_D, \\ V^{CD}(t) = 0; r_p > R_D \end{cases} \quad (24)$$

where r_p denotes the distance between the perturber electron and the emitter center, r_{ip} is the distance between the perturber and a bound atomic electron, $Z_p e$ is the charge of the perturber ($Z_p = -1$ for an electron), $Z e$ is charge of the radiating atom ($Z = 0$ for a neutral atom), and N is the number of its electrons. The two-particle Coulomb field is shielded by the ensemble of surrounding electrons: the electronic correlations (screening effects) are taken into account by introducing a cutoff in the interaction when the electron-atom distance exceeds the Debye radius R_D .

This Coulomb-Debye potential V^{CD} is often a good approximation for high temperature and low density plasmas, but it is no longer valid at the limit of low temperatures and high densities, where the mean electrostatic interaction energy is much greater in magnitude than the mean kinetic energy of the ions. For these non-ideal plasma conditions, the Coulomb Cut-off potential V^C is more suited to describe the interaction between the perturber and the emitter, since it adds a corrective term as follows (Scheibner et al. 1987):

$$\begin{cases} V^C(t) = \frac{Z_p e^2 (Z + N)}{r_p} \\ -Z_p e^2 \sum_{i=1}^N \frac{1}{r_{ip}} \left(1 - \frac{r_p}{R_c}\right); r_p \leq R_c, \\ V^C(t) = 0; r_p > R_c \end{cases} \quad (25)$$

where R_c designates a cut-off parameter assumed to be equal to the Ion Sphere radius $R_c = (3Z/4\pi N_e)^{1/3}$ (Scheibner et al. 1987).

A reasonable model describing the strongly correlated plasmas that is widely used in the literature is one in which each ion of charge Z is surrounded by a sphere of radius R_c containing Z uniformly distributed free electrons. In this Ion Sphere picture,

two corrective terms are added to the Coulomb model (Salzmann & Szichman, 1987):

$$\begin{cases} V^{\text{IS}}(t) = \frac{Z_p e^2 (Z + N)}{r_p} \\ -Z_p e^2 \sum_{i=1}^N \frac{1}{r_{ip}} \left(1 - \frac{3}{2} \frac{r_p}{R_c} + \frac{1}{2} \frac{r_p^3}{R_c^3} \right); r_p \leq R_c \\ V^{\text{IS}}(t) = 0; r_p > R_c. \end{cases} \quad (26)$$

Several comments about the Ion Sphere potential V^{IS} can be made. First, for the calculated cross sections to be significant, the binary collision picture must be valid, that is, strong collisions must be separated in time. Second, the Ion Sphere model may represent only the strong screening limit. Moreover, at short distances, electronic overlapping must be considered. Account of these quantum effects has new consequences which may be explained quasi-classically as short-range inter-particle repulsion forces. An effective repulsion is due to electron degeneracy, although that last effect appears at very high densities ($\gamma > 1$). However, under these conditions it becomes very difficult to derive exact expressions for the associated potentials.

2.6. Collision functions

In the standard formalism of Stark impact broadening of spectral lines and of cross sections, the Coulomb-Debye potential Eq. (24) is used. In addition, the integration over the time Eq. (22) is performed from $-\infty$ to $+\infty$ and not from $-t_D$ to $+t_D$, t_D being the time when the atom-perturber distance is equal to the Debye length R_D . Consequently, an upper cut-off at R_D is introduced at the impact parameter integration stage.

Under this condition, the integration over the time gives the collision function for the transition probability, $A^{\text{CD}}(z)$ (Griem et al. 1962; Sahal-Br  chot 1969a,b):

$$A^{\text{CD}}(z) = z^2 \left[K_0^2(z) + K_1^2(z) \right]. \quad (27)$$

$K_0(z)$, $K_1(z)$ designate the modified Bessel functions of the zero and first order, and $z = \frac{\rho \omega_{ij}}{v}$, where v designates the electron perturber velocity, ρ , the impact parameter, and $\omega_{ij} = \frac{E_i - E_j}{\hbar}$, where E_i , E_j correspond to the energies of the states i and j .

The integration of $A^{\text{CD}}(z)/z$ over the impact parameter z gives the collision function for the total inelastic cross-section, $a^{\text{CD}}(z)$ (Griem et al. 1962; Sahal-Br  chot 1969a):

$$a^{\text{CD}}(z) = z [K_0(z)K_1(z)]. \quad (28)$$

The corresponding functions for the Cut-off model (Ben Nessib et al. 1997) are denoted by $A^{\text{C}}(z)$ and $a^{\text{C}}(z)$. Their expressions are given in Ben Chaouacha et al. (2004).

The corresponding functions for the Ion Sphere model (Ben Chaouacha et al. 2004, 2005) are denoted by $A^{\text{IS}}(z)$ and $a^{\text{IS}}(z)$. Their expressions are given in Ben Chaouacha et al. (2004, 2005).

As in the standard formalism of the Coulomb-Debye potential, the integration over the time Eq. (23) is performed from $-\infty$ to $+\infty$ and not from $-t_c$ to $+t_c$, t_c being the time when the atom-perturber distance is equal to the R_c . Then an upper cut-off at R_c will be introduced at the impact parameter integration stage.

For collisions with electrons, the parameter $z_c = \frac{R_c \omega_{ij}}{v}$ is expressed as (Sahal-Br  chot 1969a,b):

$$z_c = \frac{1}{2} \sqrt{\frac{m_p}{m_e}} \frac{\Delta E_{ij}}{I_H} \sqrt{\frac{I_H}{E}} R_c, \quad (29)$$

where m_p is the proton mass, m_e is the electron mass, I_H is the ionization energy of hydrogen, $\Delta E_{ij} = 100 \text{ cm}^{-1}$ for the 6678   HeI line (3^1P° is the nearest perturber level of 3^1D). For $T = 40\,000 \text{ K}$ and $N_e = 10^{16} \text{ cm}^{-3}$, $E = \frac{3}{2} k_B T = 42250 \text{ cm}^{-1}$ and $R_c = 549 a_0$. Thus a typical value for z_c is 0.40.

2.7. Electrical microfield distributions

Because of the Stark effect, stochastic electric microfields have an effect on optical and thermodynamic properties of a plasma. Line shape calculations in turn require as input the electric microfield distribution at the emitting atom or ion.

Various approximate theories have been proposed to evaluate the electric microfield distribution W_r . In this section, we summarize the basic relations derived in the literature that are used for the calculations presented in this paper.

For a wide class of spectral lines, the observed frequencies (measured from line center) are sufficiently large that the ions in the plasma are effectively stationary over the corresponding radiation time. The emitting atoms or ions in plasmas are under the influence of electric fields produced by relatively rapidly moving electrons and slowly moving ions. This effect is associated with the idea that the electric microfield acting on the test particles is the sum of all the electric fields created by the perturbing ions, on the scale of distances at which the quasi-neutrality condition is not fulfilled. The radiator is immersed in a statistically fluctuating field produced by the configuration of the plasma during the time of emission; this is assumed short compared to times in which the configuration changes significantly. The Hamiltonian $H(F)$ describing the usual static Stark effect depends on the electric field strength F produced by the perturbing ions. Hence the evaluation of the quasistatic broadening is reduced to determining both the Stark levels of $H(F)$ and the proper statistical distribution function $W(F)$ of the perturbing electric fields.

2.7.1. Baranger & Mozer's distribution

The first calculations were made neglecting all interactions between charged particles (Holtmark 1919; Margenau & Lewis 1959). Only the Coulomb electric fields of point ions were considered and assumed to be random and static. Then the distribution function is dependent only on the ion density and may be written as (Griem et al. 1962; Griem 1974):

$$W(F) = \frac{1}{F_0} W_H \left(\frac{F}{F_0} \right) = \frac{1}{F_0} W_H(\beta), \quad (30)$$

where the normal field strength F_0 is expressed by

$$F_0 = \frac{2.61 e}{4\pi \epsilon_0} N_c^{2/3} \approx \frac{(4\pi N_e/3)^{2/3} e}{4\pi \epsilon_0}, \quad (31)$$

for singly charged ions (we assume here that $N_e = N_i$, where N_i is the ion density). When cgs units are used, $4\pi \epsilon_0 = 1$.

The Holtmark distribution function $W_H(\beta)$ for the normalized ion field strength $\beta = \frac{F}{F_0}$ is (Holtmark 1919)

$$W_H(\beta) = \frac{2}{\pi} \beta \int_0^\infty \eta \exp(-\eta^{3/2}) \sin(\beta \eta) d\eta. \quad (32)$$

In the calculation of $W_H(\beta)$, it has been implicitly assumed that the perturbing ions were statistically independent and that the electron screening is negligible. This assumption is justified for

very hot or rarefied plasmas for which the Coulomb coupling parameter γ is close to zero. However, at high charged particles densities where Stark broadening is important, interactions between perturbers are not negligible, and the probability of a given configuration of ions depends on the electrostatic interaction energy between the ions. With relation to this problem, various theories of the electric microfield distribution have been formulated that are based mainly on a cluster expansion in powers of density (Baranger & Mozer 1959; Mozer & Baranger 1960). The primary aim of these efforts has been to include particle-particle correlations to various orders and thus to improve the original work done by Holtzmark (1919).

The corrected distribution function in which ion-ion correlations and Debye shielding by electrons are taken into account is expressed as (Griem 1974)

$$W(F) = \frac{1}{F_0} W_r \left(\frac{F}{F_0} \right) = \frac{1}{F_0} W_r(\beta). \quad (33)$$

Then the ion field strength distribution function $W_r(\beta)$ at neutral points and at singly charged ions is expressed by Griem (1974)

$$W_r(\beta) = \frac{2}{\pi} \beta \int_0^\infty \eta A_r(\eta) \sin(\beta\eta) d\eta. \quad (34)$$

$W_r(\beta)$ depends on the ratio r of the mean distance between the ions R_c and the Debye length R_D , i.e.:

$$r = R_c/R_D = 6^{1/3} \pi^{1/6} (k_B T)^{-1/2} e N_e^{1/6}, \quad (35)$$

The $A_r(\eta)$ function designates the Fourier transform of $W(F)$ (Griem 1974; Mozer & Baranger 1960):

$$A_r(\eta) = \frac{4}{\pi} \int \frac{\exp(i\eta F) W(F)}{F^2} dF. \quad (36)$$

This function was calculated using an Ursell cluster integral expansion (Mozer & Baranger 1960) and takes the following form

$$A_r(\eta) = \exp \left[-\eta^{3/2} \chi'(r\eta^{1/2}) - \psi'(r\eta^{1/2}) \right], \quad (37)$$

which is reduced in the Holtzmark limit with $r = 0$ to

$$A_0(\eta) = \exp(-\eta^{3/2}). \quad (38)$$

The two functions χ' and ψ' depend only on the variable $r\eta^{1/2}$. They represent, respectively, the contributions of one-body and two-body clusters to the series expansion (Mozer & Baranger 1960).

2.7.2. Hooper's distribution

In order to extend the theory to higher densities and lower temperatures, Hooper (1966, 1968a,b) developed a new method based on a collective-coordinate technique that allows for the inclusion of all correlations to a high degree of accuracy. The plasma is assumed as a system of N singly charged particles moving in a uniform neutralizing background. Each of these N particles interacts with each other through an effective potential which includes the effect of the ion-electron interactions. The plasma is assumed to be in thermal equilibrium and macroscopically neutral. The effect of the uniform neutralizing background may be included by writing the potential energy of the system in terms of its Fourier expansion, which makes a distinction between the Coulomb-Debye model and the correlated

models (Hooper 1966, 1968a,b). Then, the expression for the microfield distribution $W_r(\beta)$ is written as

$$W_r(\beta) = \frac{1}{2\pi} \beta \int_0^\infty T(t) \sin(\beta t) t dt. \quad (39)$$

To proceed further, this integral is treated by an Ursell cluster expansion technique similar to that employed by Mayer & Mayer (1940) and Baranger & Mozer (Baranger & Mozer 1959; Mozer & Baranger 1960). Although the general technique is similar, the characteristic functions $T(t)$, in terms of which the expansion is made, are very different from those used by Mayer & Mayer (1940) and Baranger & Mozer (Baranger & Mozer 1959; Mozer & Baranger 1960). The final result is given in the following.

For the correlated plasmas, the asymptotic $W_r(\beta)$ curve can, with a high degree of accuracy, be calculated using only the first approximation to the theory. $T(t)$ may be put into a more convenient form (Hooper 1966, 1968a,b):

$$T(t) = \exp [-\tilde{\gamma} L^2 + I_1(t)], \quad (40)$$

where the functions $\tilde{\gamma}$, L and I_1 depend on the potential model, the shielding parameter r and an arbitrary, real, positive parameter $\tilde{\alpha}$ which will be independently determined (Hooper 1966, 1968a,b).

Due to the difficulties of optimizing the adjustable parameter $\tilde{\alpha}$ (Hooper 1966, 1968a,b), a direct evaluation of the microfield distributions $W_r(\beta)$ using this method involves significant effort, particularly when a large number of integrals at different values of β are needed. As a result, extensive numerical tables for $W_r(\beta)$ are available (Vidal et al. 1971), which are accurate to 8 significant figures for the range $0 \leq \beta \leq 30$. Beyond this range, the known asymptotic approximation for $W_r(\beta)$ can be used, while a convenient interpolation on both r and β within the tables allows us to derive $W_r(\beta)$ in the conditions of densities N_e and temperatures T of the experiments of Gauthier et al. (1981) and Bücher et al. (1995).

Hooper's approach is not applicable for the treatment of extremely dense plasmas (solar cores), i.e. in the limit of extremely strong coupling parameter ($\gamma \gg 10$): it has been primarily concerned with less dense plasmas, such as those produced in the laboratory.

2.7.3. APEX distribution and analytic fitting formula

The first theory able to provide reliable numerical results for the microfield distributions $W_r(\beta)$ in both weakly and strongly coupled plasmas proved to be the adjustable-parameter exponential approximation (APEX, Iglesias et al. 1983; Iglesias & Lebowitz 1984; Iglesias 2000). This method can be derived from a renormalized cluster expansion that maximizes the independent-particle contribution relative to the Baranger-Mozer series (Iglesias et al. 2000). It is based on a formalism that expresses the Fourier transform of $W_r(\beta)$ in terms of a special term-distribution function containing a free parameter which is then fixed to give the exact second moment of $W_r(\beta)$ (Iglesias et al. 1983; Iglesias & Lebowitz 1984; Iglesias 2000). The numerical results obtained from this scheme agree well with computed simulations for strongly coupled one-component plasmas.

However, the calculation of the different integrals involved in this method needs a considerable effort, especially in the case of correlated plasma. Thus, assuming that our system is isotropic, the microfield distribution $W_r(\beta)$ may be obtained by

elementary differentiation of the cumulative probability distribution (CPD) $Q(\beta)$ which satisfies the relation

$$Q(\beta) = \int_0^\beta W(\beta') d\beta', \quad (41)$$

where $Q(\beta).d\beta$ denotes the probability of finding a normalized electric field β , at a singly charged or neutral point, due to a collection of N -charged particles moving in a uniform neutral background and contained in a volume V . The CPD function calculated by the APEX method for a neutral point in a correlated plasma can be approximated by the formula (Potekhin et al. 2002)

$$Q(\beta) = \frac{a_0\beta^3 - 2\beta^{9/2} + \beta^6}{a_1 + a_2\beta + a_3\beta^2 + a_4\beta^3 - \beta^{9/2} + \beta^6}, \quad (42)$$

where the fitting parameters a_i can be approximated as functions of the coupling parameter γ and the screening parameter s defined as (Potekhin et al. 2002)

$$s = R_c k_s, \quad (43)$$

The analytic fitting formula of Eq. (42) has been checked for the range of the plasma parameters, i.e., at $0 \leq \Gamma \leq 100$ and $0 \leq s \leq 3$ (Potekhin et al. 2002). At $\Gamma = 0$, the differentiation of the CPD function reproduces the Holtmark data at any β with a maximum fractional error of 0.24% (Potekhin et al. 2002). Therefore, it is suitable for our application.

In the linear first-order perturbation approximation, the effective electron-screening wave number k_s is related to the Fermi-Dirac integral $F_n(\chi)$ of order $-1/2$ (Potekhin et al. 2002)

$$k_s = C_1 F_{-1/2}(\chi), \quad (44)$$

$$F_n(\chi) = \int_0^\infty \frac{t^n dt}{e^{t-\chi} - 1}, \quad n > -1, \quad (45)$$

$$C_1 = \frac{e}{\pi \hbar^3} (2m_e)^{3/2} (k_B T)^{1/2}. \quad (46)$$

The electronic chemical potential $\chi = \mu/k_B T$ is determined from the inverse function $X_n(f)$ of the complete Fermi-Dirac integral of order $1/2$ (Potekhin et al. 2002)

$$\chi = X_{1/2}(C_2), \quad (47)$$

$$C_2 = \frac{\pi^2 \hbar^3}{\sqrt{2}} (m_e k_B T)^{-3/2} N_e. \quad (48)$$

The solutions of Eq. (45) and Eq. (47) may be determined by using accurate Padé approximations for the complete Fermi-Dirac integral $F_n(\chi)$ and its corresponding inverse function $X_n(f)$ (Antia 1993)

$$F_n(\chi) \approx \begin{cases} e^\chi R_{m_1 k_1}^1(e^\chi) & \chi < 2 \\ \chi^{n+1} R_{m_2 k_2}^2(\chi^{-2}) & \chi \geq 2, \end{cases} \quad (49)$$

$$X_n(f) \approx \begin{cases} \text{Ln}[f R_{m_1 k_1}^1(f)] & \chi < 4 \\ f^{1/(n+1)} R_{m_2 k_2}^2(f^{-1/(n+1)}) & \chi \geq 4, \end{cases} \quad (50)$$

$$R_{m_1 k_1}^1(\chi) = \sum_{i=1}^{m_1} \widehat{a}_i \chi^i / \sum_{i=1}^{k_1} \widehat{b}_i \chi^i, \quad (51)$$

$$R_{m_2 k_2}^2(\chi) = \sum_{i=1}^{m_2} \widehat{c}_i \chi^i / \sum_{i=1}^{k_2} \widehat{d}_i \chi^i, \quad (52)$$

where the values of $m_1, k_1, m_2, k_2, \widehat{a}_i, \widehat{b}_i, \widehat{c}_i$ and \widehat{d}_i are given in Antia (1993). These rational function minima approximations are used to efficiently compute the values of the integrals $F_n(\chi)$ and $X_n(f)$ with maximum relative errors $\approx 10^{-12}$ and $\approx 10^{-8}$, respectively.

3. Calculation of the spectral width

Numerical results are only given in the present paper for the HeI 6678 Å ($2^1\text{P}^\circ - 3^1\text{D}$) and 5876 Å ($2^3\text{P}^\circ - 3^3\text{D}$) lines, but the method can be readily extended to a wide class of spectral lines of other atoms.

To evaluate the total width W_{tot} we must consider both electron and ion perturbing effects. The influence of electrons and ions can be treated separately due to the difference in mass and mobility. If the electron density is not very high, electron collisions are treated by the impact theory which takes into account deviations from adiabaticity. The corresponding profiles are, therefore, of dispersion (Lorentz-Weisskopf) type. For the ion effects, the adiabatic and in most cases the quasistatic approximation must be used, due to the high density of the experiment.

Several numerical modifications have been made in the original Sahal-Bréchet computer code in order to introduce the new collision functions and compute the different contributions to the width in the case of a non-ideal plasma.

The input parameters of the code are the atomic data relative to the considered transition, the density N_e of the plasma and its temperature T . In the present paper, energy levels and oscillator strength for the considered lines have been taken from TOPbase (Cunto et al. 1993; Zeippen 1995; The Opacity Project Team 1995). As TOPbase does not provide mean radii and mean square radii, we have calculated them within the hydrogenic approximation by using the effective quantum numbers n_i^* obtained from the values of the energy levels.

3.1. Impact electronic contribution

The impact electronic total width W_e contains three contributions, i.e.: the elastic part and the two inelastic parts relative to the initial i and final f states. The inelastic contributions have been calculated taking into account the new collision functions (Ben Chaouacha et al. 2004, 2005).

Three main steps are executed to compute the impact electronic total width W_e . First, the collision functions relative to the transition probability $A(z)$ and the cross section $a(z)$ are calculated for the three interaction potentials. Then, the $A(z)$ function is used to calculate the sum $\sum_{j \neq i} P_{ij}(\rho, \nu)$. In the same way, the $a(z)$ function is used to calculate the sum $\sum_{j \neq i} \sigma_{ij}(\nu)$.

The perturbation theory used for the derivation of the S -matrix leads to a divergence in the integration over the impact parameter: a lower cut-off is thus required. For high densities or for very small energy differences, an upper cut-off is also used, in order to take into account the shielding. The symmetrization procedures and the choice of the lower cut-off to enforce the unitarity of the S -matrix have been widely discussed in Feautrier (1968) and Sahal-Bréchet (1969a,b).

By applying the same procedure to both the initial $i(n_i l_i L_i S_i J_i)$ and the final $f(n_f l_f L_f S_f J_f)$ states, the total cross section $\sigma_i(\nu)$ will be calculated using Eq. (19).

The integral in Eq. (18) is calculated numerically using the trapezoid method with an exponential step (Feautrier 1968; Sahal-Br echot 1969a,b).

3.2. Quasistatic ionic contribution

The quasistatic ionic contribution W_{quas} can be estimated using the approach developed by Griem et al. (1962) and Griem (1974), due to its simple applicability to different kinds of perturbing ions.

For most of the isolated lines, it is convenient to use the impact electron width as the unit of frequency detuning from the line shifted by electron impacts, i.e., to introduce as a reduced variable the frequency shift x (Griem et al. 1962; Griem 1974)

$$x = \frac{\omega - \omega_0 - d}{W_e}, \quad (53)$$

where ω_0 and ω are the angular frequencies of the unperturbed and the perturbed lines, W_e is the impact electronic total width in angular frequency, and d is the impact electronic shift also in angular frequency unit. The reduced profile of allowed components is expressed as (Griem et al. 1962; Griem 1974)

$$j_{A,r}(x) = \frac{1}{\pi} \int_0^\infty \frac{W_r(\beta) d\beta}{1 + (x - A^{4/3}\beta^2)^2}. \quad (54)$$

The quasistatic quadratic ion broadening parameter A , denoted by α in Griem et al. (1962) and Griem (1964), is a measure of the relative importance of ion broadening. It represents the quasistatic ionic correction without the Debye cut-off, while r is the quasistatic ionic correction due to the Debye cut-off; its expression can be written as (see e.g. Ben Nessib et al. 1996)

$$A = \left(\frac{eF_0^2}{\hbar W_e} |\alpha_i - \alpha_f| \right)^{3/4}, \quad (55)$$

where the atomic polarizability α_i of the level i (resp. f) is given by

$$\alpha_i = 4a_0^3 \sum_{j \neq i} f_{ij} \left(\frac{I_H}{\Delta E_{ij}} \right)^2, \quad (56)$$

where a_0 is the Bohr radius and I_H the ionization energy of hydrogen. It can be seen from this definition that its magnitude is determined by the magnitude of the oscillator strengths f_{ij} and the energy difference ΔE_{ij} between the levels j and i . Since W_e is proportional to N_e , the parameter A is only proportional to $N_e^{1/4}$.

Contrary to the A -value of Griem who used a simplified Coulomb approximation for the atomic structure (Griem et al. 1962; Griem 1974), the quasistatic ion broadening parameter A is computed with the TOPbase sophisticated atomic structure as in Ben Nessib et al. (1996).

The quasistatic approximation will be valid provided the frequencies characterizing the ion field, namely v_{ion}/R_c , which is of the order of the inverse of the duration of an interaction [v_{ion} being a typical ion velocity, R_c is the mean ion-ion separation], are considerably smaller than W_e , which essentially determines the width of the profile (Griem 1962). If the parameter

$$\sigma = W_e R_c / v_{\text{ion}} = W_e (4\pi N_e / 3)^{-1/3} / v_{\text{ion}} \quad (57)$$

becomes of order 1 or smaller, the time dependence of the ion field can no longer be neglected (Griem 1974).

Equation (54) is only applicable if the quasistatic approximation holds for ion broadening, which is justified for $\sigma > 1$. In addition, it cannot be expected to be accurate for $r \approx 1$ or larger, because the Debye theory is no longer valid and the cluster integral expansion should be carried further. This restriction on r is not serious because, for densities corresponding to larger values of this parameter, spectral lines are usually too broad to be observable. However, the opposite extreme, $r \gg 1$, rarely occurs in plasma spectroscopy, and a discussion of calculations for such situations may therefore be omitted (Griem 1962).

3.3. Total width

Δx being the Full Width at Half Maximum (FWHM) in reduced units, obtained from the computed and tabulated $j_{A,r}(x)$, the total width W_{tot} of the line in frequency units is

$$W_{\text{tot}} = W_e \Delta x. \quad (58)$$

Moreover, an approximate formula for the total width W_{tot}^G of the complete profile can be obtained (Griem 1962, 1974)

$$W_{\text{tot}}^G \approx [1 + 1.75A(1 - 0.75r)]W_e. \quad (59)$$

The formula of Eq. (59) is adapted only for an ideal plasma studied with the Coulomb Debye model. It is reasonably accurate in view of the uncertainties introduced by the various other approximations, as long as $A \leq 0.5$ and $r \leq 0.8$ (Griem 1974). For higher values of A , Eq. (58) must be used.

4. Results and discussion

To validate our theoretical approach, the different contributions to the width are calculated for the HeI 6678 Å ($2^1P^\circ - 3^1D$) and 5876 Å ($2^3P^\circ - 3^3D$) lines, by considering the same conditions of densities N_e and temperatures T as those of the experiments of Gauthier et al. (1981) and B ucher et al. (1995).

The impact approximation criterion is well satisfied for electronic collisions. In a first step, the impact electronic total width was calculated in the case of the Coulomb-Debye potential, i.e. W_e^{CD} , with an upper cutoff at R_D . By calculating the relative contribution of the strong collisions to the impact total width, the validity conditions of the perturbation theory can also be checked.

Table 2 shows that the electronic strong collision contribution $W_{s,e}^{\text{CD}}$ does not exceed 30% of the impact electronic total width W_e^{CD} . Consequently, the perturbation theory approximation is well satisfied for collisions with electrons for these lines. About 90% to 95% of the inelastic electronic part is related to the upper level (Table 2).

Figure 1 compares the impact electronic total width W_e^{CD} , the elastic contribution $W_{e,\text{el}}^{\text{CD}}$ and the inelastic contribution $W_{e,\text{inel}}^{\text{CD}}$. It can be noted that for the two lines the inelastic collisions give the largest contribution. The two contributions $W_{e,\text{inel}}^{\text{CD}}$ and $W_{e,\text{el}}^{\text{CD}}$ present almost the same behavior and increase with the electronic density N_e . The elastic term $W_{e,\text{el}}^{\text{CD}}$ is relatively low and does not exceed 15% of the impact electronic total width W_e^{CD} . The inelastic contributions due to weak collisions are dominant (70%), because the excited states of the HeI are very close together (Sahal-Br echot 1969a,b).

In a second step, we have calculated the inelastic electronic contribution in the case of the Cut-off and Ion Sphere potentials, with an upper cut-off at R_c . Figure 2 compares the evolution of the inelastic electronic contributions $W_{e,\text{inel}}^{\text{CD}}$, $W_{e,\text{inel}}^{\text{C}}$ and $W_{e,\text{inel}}^{\text{IS}}$ for the considered lines. The two inelastic widths $W_{e,\text{inel}}^{\text{CD}}$ and $W_{e,\text{inel}}^{\text{C}}$

Table 2. Different contributions to the width calculated for the considered HeI transitions. W^{exp} : experimental width – W_e^{CD} : impact electronic total width – $W_{s,e}^{\text{CD}}$: width due to the strong electronic collisions – $W_{e,\text{el}}^{\text{CD}}$: impact elastic electronic contribution – $W_{e,\text{inel}}^{\text{CD,L}}$: impact inelastic electronic contribution of the lower level – $W_{e,\text{inel}}^{\text{CD,U}}$: impact inelastic electronic contribution of the upper level.

Transition	T	N_e	W^{exp}	W_e^{CD}	$W_{s,e}^{\text{CD}}$	$W_{e,\text{el}}^{\text{CD}}$	$\frac{W_{e,\text{inel}}^{\text{CD,L}}}{W_{e,\text{inel}}^{\text{CD,U}}}$
	(10^4 K)	(10^{17} cm $^{-3}$)	(Å)	(Å)	(Å)	(Å)	(%)
($2^1\text{P}^\circ-3^1\text{D}$)	1.35	2.0	8.6	11.4	2.8	1.0	5.6
6678 Å	1.78	3.3	12.9	17.2	4.2	1.7	6.5
	1.86	4.9	15.5	24.2	6.3	2.5	7.1
	1.93	6.2	19.9	29.4	7.8	3.1	7.5
	2.01	6.9	20.7	32.2	8.6	3.4	7.7
	2.13	8.4	25.0	37.7	10.3	4.2	8.1
	2.09	8.9	25.9	39.7	11.0	4.4	8.2
	2.28	10.0	28.5	43.6	12.1	4.9	8.6
	2.32	10.7	30.2	46.2	12.9	5.3	8.8
	2.40	11.8	31.9	50.0	14.1	5.8	9.0
	2.44	13.2	35.4	54.7	15.6	6.5	9.3
	2.59	13.7	36.3	56.6	16.0	6.8	9.5
	2.55	14.9	40.6	60.5	17.5	7.3	9.7
($2^3\text{P}^\circ-3^3\text{D}$)	4.46	4.90	17.5	13.8	4.0	1.9	9.0
5876 Å	5.20	10.2	36.7	28.0	8.1	3.9	10.2
	5.21	12.0	43.2	32.6	9.6	4.6	10.4
	5.60	18.4	66.0	48.9	14.6	7.1	11.2
	5.35	24.9	89.2	65.1	19.5	9.4	12.2

increase with the plasma density N_e , and their shape is almost the same. For the 6678 Å line, the Ion Sphere contribution $W_{e,\text{inel}}^{\text{IS}}$ decreases when N_e exceeds 10^{16} cm $^{-3}$. The three contributions converge at weak plasma densities ($N_e \approx 10^{15}$ cm $^{-3}$) since the effects of the corrective terms become negligible, i.e., the plasma may be considered effectively as ideal.

In the case of a non-ideal plasma ($N_e > 10^{15}$ cm $^{-3}$), the two correlated inelastic contributions $W_{e,\text{inel}}^{\text{C}}$ and $W_{e,\text{inel}}^{\text{IS}}$ are smaller than the Coulomb-Debye one, following the general tendency of the corresponding collision functions $A(z)$ and $a(z)$ (Ben Chaouacha et al. 2004, 2005). The contribution relative to the Ion Sphere model $W_{e,\text{inel}}^{\text{IS}}$ is the lowest; in parallel, the difference between the two correlated terms $W_{e,\text{inel}}^{\text{C}}$ and $W_{e,\text{inel}}^{\text{IS}}$ tends to increase as the electronic density N_e increases. However, if the density N_e exceeds the value ($N_e \geq 10^{18}$ cm $^{-3}$), this tendency is expected to no longer be systematic: the semi-classical approach and the Ion Sphere model are expected to be not well adapted to describe a plasma in such extreme conditions.

We have calculated the elastic contribution only with the Coulomb-Debye model ($W_{e,\text{el}}^{\text{CD}}$). The validity of this assumption is justified by the fact that the elastic cross sections are mainly due to strong collisions: Table 3 shows that the ratio of the impact elastic electronic contribution to the electronic density $\frac{W_{e,\text{el}}^{\text{CD}}}{N_e}$ is quite constant, since the difference does not exceed 1% for the two lines. Therefore, the upper cut-off at R_D has a negligible effect for the elastic contribution, even at high electronic densities. In addition, still concerning elastic collisions, the contribution of the quadratic r_p^{-4} -potential which is short-range is dominant compared to the quadrupolar one. Hence, the very long-range collisions are not important, and the results for the elastic contribution should not be very different in the case of

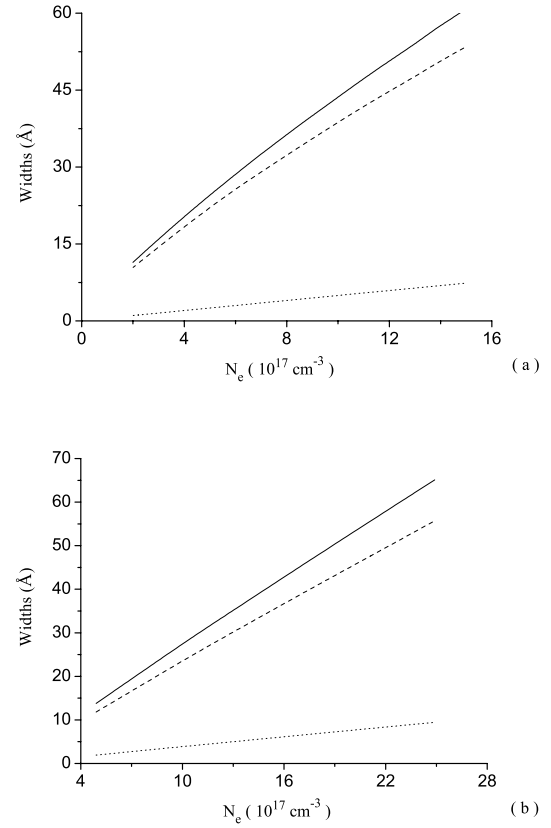


Fig. 1. Different contributions to the impact electronic total width W_e^{CD} calculated for the considered HeI transitions. Straight line: impact electronic total width W_e^{CD} ; Dashed line: inelastic electronic contribution $W_{e,\text{inel}}^{\text{CD}}$; Dotted line: elastic electronic contribution $W_{e,\text{el}}^{\text{CD}}$. [a]: 6678 Å ($2^1\text{P}^\circ-3^1\text{D}$), b): 5876 Å ($2^3\text{P}^\circ-3^3\text{D}$).

the Coulomb-Debye, Cut-off and Ion Sphere models. However, this might be improved in a further paper.

Table 4 lists the values of the Debye shielding parameter r and the three quasistatic quadratic ion broadening parameters A^{CD} , A^{C} and A^{IS} for the studied lines. They are obtained from Eq. (55) by using the associated impact electronic total widths W_e^{CD} , W_e^{C} and W_e^{IS} . For the 6678 Å line, $r \approx 0.6$ and that A^{CD} is slightly higher than the upper limit of validity (0.5). Hence, for the Coulomb Debye model, the total width W_{tot} has been estimated using the approximated formula of Eq. (59). For both the Cut-off and the Ion Sphere models, the formulae given by Eq. (58) and Eq. (54) have been used, since A^{C} and A^{IS} are much greater than unity. For the 5876 Å line, $r \approx 0.4$ and only A^{IS} is slightly higher than the upper limit of validity (0.5).

By considering the values of r , A^{CD} , A^{C} and A^{IS} tabulated in Table 4, the complete reduced Stark profiles $j_{A,r}(x)$ of isolated lines have been evaluated numerically. In a first step, we checked our code by verifying that our numerical procedure reproduces the same data tabulated in Griem (1974). Then, the $j_{A,r}(x)$ profiles were analyzed to determine their Full Width at Half Maximum (FWHM) Δx .

The three total widths $W_{\text{tot}}^{\text{CD}}$, $W_{\text{tot}}^{\text{C}}$ and $W_{\text{tot}}^{\text{IS}}$ of the considered lines obtained from the expression of Eq. (58), by considering micro-field distributions $W_r(\beta)$ derived with the different numerical methods presented above are compared in Figs. 3 and 4 to the experimental widths W^{exp} of Gauthier et al. (1981) and

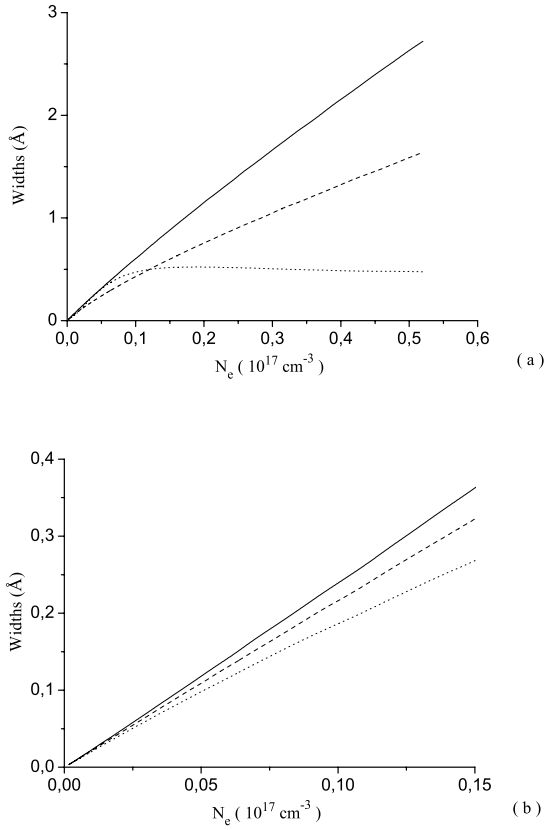


Fig. 2. Impact inelastic electronic widths $W_{e,inel}^{CD}$, $W_{e,inel}^C$, and $W_{e,inel}^{IS}$ calculated for the considered HeI transitions, by considering a small non-ideality factor ($\gamma = 0.03$). Straight line: $W_{e,inel}^{CD}$; Dashed line: $W_{e,inel}^C$; Dotted line: $W_{e,inel}^{IS}$. [a): 6678 Å ($2^1P^\circ-3^1D$), b): 5876 Å ($2^3P^\circ-3^3D$)].

Table 3. Ratio of the impact elastic electronic contribution to the electronic density $\frac{W_{e,el}^{CD}}{N_e}$ (10^{-18} Å cm³) calculated for the considered HeI transitions.

Transition	N_e (10^{17} cm ⁻³)	0.1	1.0	10.0	16.0
	T (10^4 K)				
$(2^1P^\circ-3^1D)$ 6678 Å	1.0	5.57	5.56	5.42	5.35
	1.5	5.15	5.14	5.09	5.06
	2.0	5.00	5.00	4.97	4.96
	2.5	4.95	4.94	4.93	4.92
$(2^3P^\circ-3^3D)$ 5876 Å	1.0	6.25	6.25	6.22	6.19
	1.5	5.41	5.41	5.40	5.39
	2.0	4.88	4.88	4.87	4.86
	2.5	4.57	4.57	4.56	4.56

Bücher et al. (1995). Unfortunately, these experiments correspond to relatively weak values of the non-ideality factor ($\gamma < 0.3$). It is generally difficult to provide experimental data at the high electronic densities N_e required by the Ion Sphere model.

Figure 3 shows that for the 6678 Å line the different total widths W_{tot}^{CD} , W_{tot}^C and W_{tot}^{IS} increase with the plasma density N_e and are more important with a micro-field distribution $W_r(\beta)$ derived by the AFF method (Potekhin et al. 2002). The Coulomb Debye model overestimates the experimental data for a micro-field distribution $W_r(\beta)$ derived either by Baranger & Mozer's method (Baranger & Mozer 1959; Mozer & Baranger 1960) or by Hooper's method (Hooper 1966, 1968a,b), W_{tot}^{CD}

exceeds 310% of W^{exp} , and this difference is close to 350% for the APEX method. This confirms the importance of taking into account the correlations in a non-ideal plasma. The Cut-off model also disagrees with the experimental data: W_{tot}^C is greater than the experimental width W^{exp} and a difference close to 300% is typically obtained at high electron densities N_e for the APEX method. Therefore, this correlated model cannot reproduce all the physical considerations. The Ion Sphere model presents a difference with the experiment, but this difference tends to be the closest one for the electron density range (4×10^{17} cm⁻³ $< N_e < 9 \times 10^{17}$ cm⁻³) and with a microfield distribution $W_r(\beta)$ derived by Hooper's method. However, W_{tot}^{IS} does not exceed 63% of W^{exp} at low electron densities N_e , while a difference close to 54% is obtained at high electron densities N_e .

For the 5876 Å line, the correlated total widths W_{tot}^C and W_{tot}^{IS} are lower than W^{exp} (Fig. 4). A difference close to 4% is obtained with the Coulomb Debye model and with a microfield distribution $W_r(\beta)$ derived by Hooper's method. Hence, this discussion shows that our theoretical approach would require new refinements in order to be in perfect agreement with the experiment.

Table 5 shows that the Coulomb-Debye total width W_{tot}^{CD} calculated from the associated Full Width at Half Maximum (FWHM) Δx^{CD} using Eq. (58) is in good agreement with the approximated total width W_{tot}^G obtained from Eq. (59), by considering the quasistatic quadratic ion broadening parameters A^{CD} and the Debye shielding parameter r tabulated in Table 4: their difference does not exceed 3%. However, the total width $W_{tot}^{G,*}$ obtained from the expression of Eq. (59) without taking into account the quasistatic ionic correction due to the Debye cut-off ($r = 0$) is greater than W_{tot}^G (up to 136%, for the 6678 Å line) (Table 5). Thus, r cannot be neglected if the electronic density N_e is relatively high.

To generalize such result to the two correlated models, approximate formulae for the total width $W_{tot,app}$ similar to the expression of Eq. (59) are derived, by introducing two constants a and b so that

$$W_{tot,app} \approx W_e(ar + bA + 1). \quad (60)$$

The parameters a and b can be readily obtained by a Least Square method using the following equations

$$Y = aX + b, \quad (61)$$

$$X = r, \quad (62)$$

$$Y = \frac{\left(\frac{W_{tot}}{W_e} - 1\right)}{A}, \quad (63)$$

where W_{tot} is previously obtained using Eq. (58). The resulting formulae, in turn, are

$$W_{tot,app}^{CD} \approx W_e^{CD}(a^{CD}r + b^{CD}A^{CD} + 1), \quad (64)$$

$$W_{tot,app}^C \approx W_e^C(a^C r + b^C A^C + 1), \quad (65)$$

$$W_{tot,app}^{IS} \approx W_e^{IS}(a^{IS}r + b^{IS}A^{IS} + 1), \quad (66)$$

where the values of the associated parameters (a^{CD} , b^{CD}), (a^C , b^C) and (a^{IS} , b^{IS}) are tabulated in Table 6. As shown in Table 5, the three total widths $W_{tot,app}^{CD}$, $W_{tot,app}^C$ and $W_{tot,app}^{IS}$ are comparable to those calculated using Eq. (58).

Table 4. Quasistatic quadratic ion broadening parameters A^{CD} , A^{C} and A^{IS} calculated for the considered HeI transitions. $r = \frac{R_c}{R_D}$: Debye shielding parameter – W_e^{CD} , W_e^{C} and W_e^{IS} : impact electronic total widths.

Transition	T (10^4 K)	N_e (10^{17} cm^{-3})	r	W_e^{CD} (\AA)	W_e^{C} (\AA)	W_e^{IS} (\AA)	A^{CD}	A^{C}	A^{IS}
$(2^1\text{P}^\circ - 3^1\text{D})$ 6678 \AA	1.35	2.0	0.591	11.4	5.1	1.46	0.46	0.84	2.15
	1.78	3.3	0.559	17.2	7.8	2.37	0.56	1.01	2.45
	1.86	4.9	0.586	24.2	10.6	3.47	0.64	1.20	2.77
	1.93	6.2	0.597	29.4	12.7	4.34	0.70	1.32	2.94
	2.01	6.9	0.596	32.2	13.9	4.84	0.73	1.37	3.03
	2.13	8.4	0.598	37.7	16.3	5.77	0.79	1.47	3.21
	2.09	8.9	0.610	39.7	17.1	6.09	0.81	1.52	3.29
	2.28	10.0	0.595	43.6	19.0	6.84	0.84	1.57	3.38
	2.32	10.7	0.597	46.2	20.2	7.28	0.87	1.61	3.46
	2.40	11.8	0.597	50.0	21.9	7.97	0.90	1.67	3.57
	2.44	13.2	0.603	54.7	24.0	8.86	0.94	1.74	3.67
	2.59	13.7	0.589	56.6	25.1	9.25	0.95	1.75	3.70
2.55	14.9	0.601	60.5	26.7	9.98	0.98	1.82	3.80	
$(2^3\text{P}^\circ - 3^3\text{D})$ 5876 \AA	4.46	4.9	0.378	13.8	9.2	5.42	0.19	0.26	0.39
	5.20	10.2	0.396	28.0	17.3	7.10	0.24	0.34	0.66
	5.21	12.0	0.406	32.6	19.7	7.71	0.25	0.36	0.73
	5.60	18.4	0.420	48.9	28.2	10.3	0.28	0.42	0.89
	6.35	24.9	0.415	65.1	36.8	13.5	0.30	0.47	0.99

5. Summary of the results and conclusion

Ben Chaouacha et al. (2004, 2005) derived new semi-classical collision functions for both the transition probability and cross section by using the classical path approximation in the standard formalism of Stark impact broadening of spectral lines. These functions have been used in the present paper to compute the inelastic contribution $W_{e,\text{inel}}$ to the electronic total width W_e in the case of a non-ideal plasma, by considering three different interaction potentials (Coulomb-Debye, Cut-off, and Ion Sphere). An upper cut-off at R_D for the Coulomb-Debye model (ideal case) and at R_c for the Cut-off and the Ion Sphere models has been used. To validate our theoretical approach, the numerical results have been calculated for the HeI 6678 \AA ($2^1\text{P}^\circ - 3^1\text{D}$) and 5876 \AA ($2^3\text{P}^\circ - 3^3\text{D}$) transitions, by considering the same conditions of densities N_e and temperatures T as those of the experiments of Gauthier et al. (1981) and Bücher et al. (1995).

The lines corresponding to these transitions are well isolated and the plasma is weakly non-ideal for all temperatures and electronic densities of interest. For electronic collisions, the semi-classical perturbation theory is sufficient and the impact approximation is well satisfied.

The contribution of elastic electronic collisions $W_{e,\text{el}}$ calculated by considering the Coulomb Debye model is weak for these lines. Since the very long-range collisions are not important for this contribution, we consider that the corresponding results should not be very different in the case of the Cut-off and the Ion Sphere potentials.

The inelastic contribution $W_{e,\text{inel}}$ depends both on the choice of the non-ideality γ -value and the interaction potential model. The three impact inelastic electronic widths $W_{e,\text{inel}}^{\text{CD}}$, $W_{e,\text{inel}}^{\text{C}}$ and $W_{e,\text{inel}}^{\text{IS}}$ become of the same order of magnitude at weak plasma densities ($N_e \approx 10^{15} \text{ cm}^{-3}$). The two correlated widths are lower than the ideal one, which is in agreement with the general behavior of the associated collision functions.

The ion effects on such a line are as important as the electron ones. The impact approximation fails for ionic collisions, due to the relatively high densities prevailing in these experimental conditions. The interactions with the ions may be treated within

the quasistatic approximation. In that case, atom-ion interaction is quadratic. Therefore, the quasistatic ionic contribution W_{quas} is dominated by the polarization (or quadratic) r_p^{-4} -interaction.

To consider both the electron and the ion effects, the total width W_{tot} is obtained from the Full Width at Half Maximum (FWHM) Δx deduced from the complete reduced Stark profile $J_{A,r}(x)$ of isolated lines. The Debye shielding parameter r and the quasistatic quadratic ion broadening parameter A are relevant to numerically evaluate such profiles. For comparison, the calculations of the associated microfield distributions $W_r(\beta)$ are performed using three different numerical methods.

The computed total widths $W_{\text{tot}}^{\text{CD}}$, $W_{\text{tot}}^{\text{C}}$ and $W_{\text{tot}}^{\text{IS}}$ relative to the considered lines are compared to the corresponding experimental widths W^{exp} (Gauthier et al. 1981; Bücher et al. 1995). For the 5876 \AA line, the Coulomb Debye width $W_{\text{tot}}^{\text{CD}}$ is comparable to W^{exp} . For the 6678 \AA line, the Ion Sphere model gives the best results with a microfield distribution $W_r(\beta)$ derived by Hooper's method (1966, 1968a,b): such a numerical method is sufficient for use in our case. A difference close to 50% is expected at both low and high electron densities N_e . Such a discrepancy may be due to different reasons, which are discussed in the following.

It is impossible to have a perfect agreement between the calculated widths and the experimental data only by improving the calculation of the collision functions: our model only improves the inelastic electronic contribution $W_{e,\text{inel}}$ to the impact electronic total width W_e ; it takes into account the quasistatic ionic contribution.

Since a real plasma is intrinsically dynamic and complex, it may be studied by considering the collective effects rather than the binary ones: such effects cannot be described by a simple corrective term in the interaction potential expression.

The calculation of the excitation cross section needs the introduction of a minimum cut-off radius which may eliminate certain significant terms in the numerical integration procedure.

A semi-classical treatment for electron collisions neglects the emitter-perturber exchange, which is mainly due to the strong collisions. Hence, when strong collisions are abundant, quantum effects must be considered.

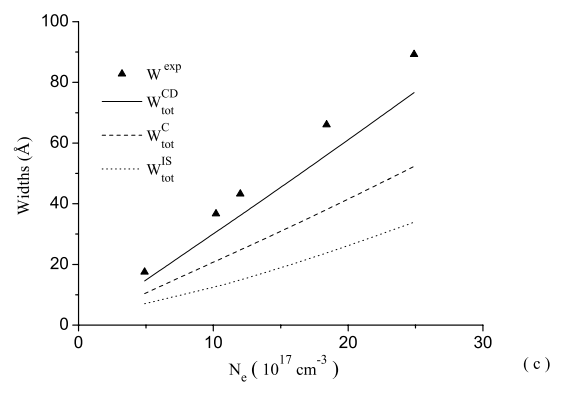
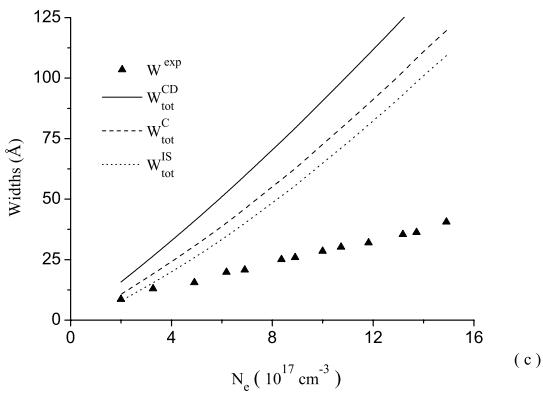
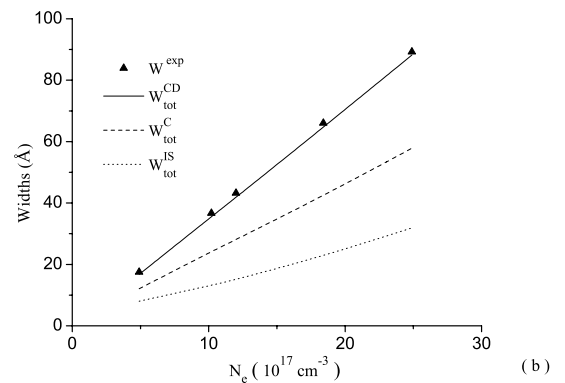
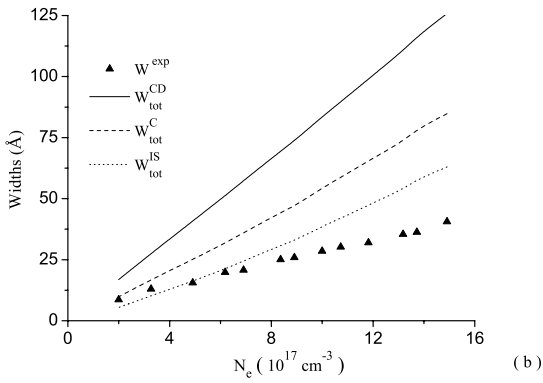
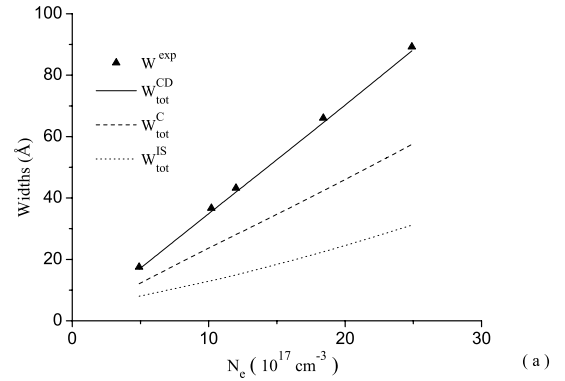
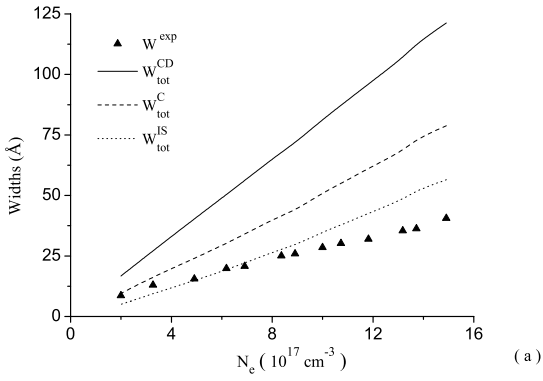


Fig. 3. Total widths $W_{\text{tot}}^{\text{CD}}$, $W_{\text{tot}}^{\text{C}}$ and $W_{\text{tot}}^{\text{IS}}$ obtained from the expression of Eq. (58) for the HeI 6678 Å ($2^1\text{P}^\circ - 3^1\text{D}$) transition, where the associated micro-field distribution $W_r(\beta)$ is determined with: **a)** the Baranger & Mozer's method (Baranger & Mozer 1959; Mozer & Baranger 1960), **b)** the Hooper's method (Hooper 1966, 1968a,b), and **c)** the AFF method (Potekhin et al. 2002). W^{exp} is the experimental width relative to the same transition (Gauthier et al. 1981).

Fig. 4. Same as Fig. 3 for the HeI 5876 Å ($2^3\text{P}^\circ - 3^3\text{D}$) line studied in the same conditions of densities N_e and temperatures T of the experiment of Bücher et al. (1995).

The different results may be improved by considering a hyperbolic trajectory. Such a trajectory would be more reliable for describing screening effects on the perturber motion colliding with a neutral atom, especially for very low collision energies in the neighborhood of the threshold (Jung 1994). However, for large impact parameters, the straight line trajectory can be used even when the emitter is an ion (Jung 2000). As we are interested only in neutral atom emitters for large impact parameters at relatively low energies (temperatures of the order of a few thousand

or few ten thousands degrees), we have neglected the plasma screening effects on the semi-classical straight line trajectory. The dynamic plasma screening effects on the atomic excitation process are found to be significant only for relatively high energy projectiles (Jung & Yoon 2000b). The excitation cross section including screening effects is shown to decrease as the non-ideality factor γ increases (Song & Jung 2003; Jung 2000).

This study has qualitatively shown the importance of the electronic correlations for a non-ideal plasma. However, many refinements should be more deeply studied and introduced gradually with care, before trying to generalize our theoretical approach to other plasmas studies.

Table 5. Total width ratios calculated for the considered HeI transitions, where the micro-field distribution $W_r(\beta)$ is determined with: (a) the Baranger & Mozer's method (Baranger & Mozer 1959; Mozer & Baranger 1960); (b) the Hooper's method (Hooper 1966, 1968a,b); and (c) the AFF method (Potekhin et al. 2002). $W_{\text{tot}}^{\text{G}}$: total width obtained from the expression of Eq. (59) – $W_{\text{tot}}^{\text{G},*}$: total width obtained by considering $r = 0 - W_{\text{tot}}^{\text{CD}}$, $W_{\text{tot}}^{\text{C}}$ and $W_{\text{tot}}^{\text{IS}}$: total widths obtained from the expression of Eq. (58) – $W_{\text{tot,app}}^{\text{CD}}$, $W_{\text{tot,app}}^{\text{C}}$ and $W_{\text{tot,app}}^{\text{IS}}$: total widths approximated by the expressions of Eqs. (64)–(66).

$\frac{W_{\text{tot}}^{\text{G}}}{W_{\text{tot}}^{\text{CD}}}$	$\frac{W_{\text{tot}}^{\text{G},*}}{W_{\text{tot}}^{\text{CD}}}$	$\frac{W_{\text{tot,app}}^{\text{CD}}}{W_{\text{tot}}^{\text{CD}}}$	$\frac{W_{\text{tot,app}}^{\text{CD}}}{W_{\text{tot}}^{\text{CD}}}$	$\frac{W_{\text{tot,app}}^{\text{CD}}}{W_{\text{tot}}^{\text{CD}}}$	$\frac{W_{\text{tot,app}}^{\text{C}}}{W_{\text{tot}}^{\text{C}}}$	$\frac{W_{\text{tot,app}}^{\text{C}}}{W_{\text{tot}}^{\text{C}}}$	$\frac{W_{\text{tot,app}}^{\text{C}}}{W_{\text{tot}}^{\text{C}}}$	$\frac{W_{\text{tot,app}}^{\text{IS}}}{W_{\text{tot}}^{\text{IS}}}$	$\frac{W_{\text{tot,app}}^{\text{IS}}}{W_{\text{tot}}^{\text{IS}}}$	$\frac{W_{\text{tot,app}}^{\text{IS}}}{W_{\text{tot}}^{\text{IS}}}$
(%)	(%)	(%) ^(a)	(%) ^(b)	(%) ^(c)	(%) ^(a)	(%) ^(b)	(%) ^(c)	(%) ^(a)	(%) ^(b)	(%) ^(c)
(2 ¹ P ^o –3 ¹ D)										
6678 Å										
98.80	123.16	100.43	101.41	112.33	101.45	103.21	116.35	104.85	105.78	113.39
98.89	124.65	100.17	99.87	98.93	99.92	99.74	98.75	99.59	99.58	99.03
97.92	127.62	99.83	100.44	102.87	100.58	100.82	103.04	101.18	101.30	102.49
97.80	129.81	100.03	100.57	103.62	100.71	101.11	103.94	101.59	101.79	103.32
97.72	130.47	99.99	100.34	102.16	100.51	100.73	102.24	101.09	101.15	102.12
97.58	131.86	100.00	100.20	100.58	100.21	100.33	100.52	100.37	100.40	100.61
97.66	133.38	100.39	100.52	103.80	100.76	101.08	104.17	101.39	101.69	103.21
97.42	132.73	99.86	99.64	97.36	99.67	99.30	97.07	99.12	98.96	97.86
97.30	133.25	99.82	99.61	97.13	99.60	99.15	96.88	98.96	98.76	97.60
97.34	134.01	99.90	99.44	95.83	99.32	98.78	95.63	98.45	98.19	96.55
97.26	135.27	100.04	99.44	96.55	99.37	98.97	96.46	98.63	98.48	97.22
96.95	133.89	99.38	98.59	91.18	98.36	97.35	90.77	96.75	96.23	92.96
97.09	135.83	99.89	99.06	94.44	98.87	98.31	94.33	97.79	97.58	95.58
(2 ³ P ^o –3 ³ D)										
5876 Å										
101.36	109.14	100.07	100.01	100.06	99.92	99.95	100.12	100.17	100.20	101.45
101.21	110.78	99.92	99.89	99.74	100.07	100.02	99.59	99.66	99.53	97.15
101.13	111.32	99.92	100.24	100.70	100.30	100.29	101.05	100.13	100.31	100.69
101.30	112.96	100.17	100.08	100.90	100.07	100.24	101.52	100.76	100.85	103.60
101.20	113.47	99.92	99.75	98.46	99.61	99.44	97.53	99.19	99.00	96.80

Table 6. Parameters (a^{CD} , b^{CD}), (a^{C} , b^{C}) and (a^{IS} , b^{IS}) of the expressions of Eqs. (64)–(66), calculated for the considered HeI transitions, where the micro-field distribution $W_r(\beta)$ is determined with: (a) the Baranger & Mozer's method (1959; 1960), (b) the Hooper's method (Hooper 1966; 1968a,b), and (c) the AFF method (2002). For the sake of comparison, we give also in (d) the values of a^{CD} and b^{CD} defined in the expression of Eq. (59) of Griem (1962, 1974).

Transition	Models	a^{CD}	b^{CD}	a^{C}	b^{C}	a^{IS}	b^{IS}
(2 ¹ P ^o –3 ¹ D) 6678 Å	(a)	–0.8275	1.5153	–1.0433	1.6831	–0.5560	1.5275
	(b)	–0.0885	1.1303	0.3223	0.9744	0.4179	1.1065
	(c)	7.7626	–3.4044	8.5954	–3.3916	6.8722	–1.6409
	(d)	–1.3125	1.75	–	–	–	–
(2 ³ P ^o –3 ³ D) 5876 Å	(a)	–0.6395	1.4135	–0.1114	1.2334	1.6013	0.6352
	(b)	0.2977	1.0317	0.5720	0.9681	2.7525	0.2069
	(c)	5.8749	–1.9181	8.8274	–2.8408	16.6070	–5.4567

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