

# Constraints on the progenitor systems of type Ia supernovae

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## ABSTRACT

Bolometric light curves provide a valuable insight into the nature of type Ia supernovae. We present an analysis of sixteen well-observed type Ia supernovae. Constraints are placed on several global parameters concerning the progenitor system, explosion mechanism, and subsequent radiation transport. By fitting a radioactive decay energy deposition function to the quasi-exponential phase (50 to 100 days after maximum light), it is found that the ejected mass varies by at least a factor of two. This result suggests that a sub Chandrasekhar mass white dwarf could be the progenitor system of some type Ia supernovae. We find that the range in the amount of synthesized <sup>56</sup>Ni indicates a significant variation in the burning mechanism. In order to explain a factor of ten range in the observed bolometric luminosity, more detailed modeling of the explosion mechanism is required.

**Key words.** stars: supernovae: general

## 1. Introduction

Type Ia supernovae (hereafter SNe Ia) have become an exceptional tool in modern cosmology. Due to their high luminosity, they are used to place constraints on cosmological parameters, and so far provide the only *direct* evidence for the existence of dark energy (Riess et al. 1998; Perlmutter et al. 1999; Leibundgut 2001). Despite the insight SNe Ia have given us into the universe, several key issues related to the nature of their progenitor system(s) and the physics of the explosion mechanism(s) have remained unsolved (for reviews see Hillebrandt & Niemeyer 2000; Livio 2000).

Today it is commonly believed that SNe Ia emerge from the thermonuclear incineration of a carbon oxygen (C–O) white dwarf exploding near or at the Chandrasekhar mass (Nomoto et al. 1984; Woosley & Weaver 1986; Hillebrandt & Niemeyer 2000). The energy released from burning to nuclear statistical equilibrium (NSE) completely destroys the white dwarf. The optical/IR light curves are powered by the Comptonization of  $\gamma$  rays produced from the radioactive decay chain  $^{56}\text{Ni} \rightarrow ^{56}\text{Co} \rightarrow ^{56}\text{Fe}$  (Pankey 1962; Colgate & McKee 1969). Within this paradigm the C–O white dwarf accretes matter from an evolved massive star either via Roche lobe overflow or through stellar winds. With the detection of  $H\alpha$  in the

well-observed SN 2002ic (Hamuy et al. 2003; Nomoto et al. 2004; Kotak et al. 2004), the single degenerate model has become favored over the double degenerate model.

It is clear that SNe Ia do not represent a homogeneous group of stellar explosions rather, they display a range in luminosity of a factor of ten or more (Suntzeff 1996; Contardo et al. 2000; Suntzeff 2003; Stritzinger 2005). In fact not one self-consistent explosion model has been presented yet to successfully account for this observed range in luminosity. This lack of understanding of the progenitor systems is unsettling, and it must be addressed if we are to have confidence in the cosmological results provided by SNe Ia.

Fortunately during the past decade, a number of observing campaigns (see Leibundgut 2000, for a list) have obtained excellent data sets for a large number of SNe Ia. With these data sets we are currently in a position to conduct a systematic investigation of their photometric and spectroscopic properties. Our goal here was to place further constraints on both the progenitor systems and explosion mechanisms with these observations. In particular, we constructed UltraViolet Optical near-InfraRed (UVOIR) bolometric light curves from the broad-band photometry of a number of SNe Ia. With the UVOIR light curve we determine several global parameters, e.g. total ejected mass, <sup>56</sup>Ni mass, and the  $\gamma$ -ray escape fraction. Investigating the range of such parameters can provide insights into the nature of SNe Ia and help differentiate between the various paths of

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stellar evolution that the progenitors follow, as well as the manner in which thermonuclear combustion occurs.

The structure of this paper is as follows. Section 2 discusses the observational data used and the UVOIR light curves. Section 3 describes our analysis of the UVOIR light curves, while Sect. 4 contains the results of this analysis, and we conclude in Sect. 5.

## 2. Observational data and UVOIR light curves

The  $(U)BVRI$ -band observations for sixteen SN Ia have been procured from a variety of sources. Table 1 lists all the events considered in this study, along with references to the sources of the data and a number of important parameters used and determined in this work. All events listed in Table 1 have excellent optical photometry that extends from pre-maximum out to  $\sim 100$  days past maximum light. See Stritzinger (2005) for more details concerning the method and sample.

To determine the amount of  $^{56}\text{Ni}$  produced in the explosion from the observed UVOIR flux, two parameters are required. They include an estimate for the total extinction and the distance to the host galaxy. Values listed for Galactic reddening are those given by the COBE dust maps of Schlegel et al. (1998). Host galaxy reddenings were selected from Phillips et al. (1999) for those SNe Ia that coincide with our sample. For more recent events we adopted host galaxy extinctions from the literature, with a preference for those calculated by the Phillips method. The chosen distances depended mainly on what was available in the literature. For SNe Ia without a direct distance measurement, in this case a Cepheid distance measurement or a surface brightness fluctuation (SBF) distance, we used a Heliocentric velocity obtained from NED and converted it to the CMB reference frame<sup>1</sup>. For each CMB distance we assumed an uncertainty of  $300 \text{ km s}^{-1}$ .

With the advent of the *Hubble Space Telescope* (HST) there has been a substantial effort from two groups, namely the HST Key Project (HKP) and the Saha, Tammann, and Sandage (STS) group, to obtain accurate Cepheid distance measurements to galaxies that have hosted SNe Ia. Typically these two independent groups determine different distances for any one galaxy, even though they use the same data and similar data reduction software. These differences are a reflection of assumptions made in their analysis. The main factor that contributes to these discrepancies is the exact  $P - L$  relation used, while several other subtle nuances exacerbate the problem. These include: (1) the criteria adopted to select the Cepheids for determining the distance, (2) if and how metallicity corrections are applied, and (3) anomalies related to the camera(s) on HST (see Parodi et al. 2000; Gibson et al. 2000; Riess et al. 2005).

In short, the HKP obtains a *short* distance scale that leads to a value of  $H_0 \sim 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$ , while the STS group determines a *long* distance scale that gives  $H_0 \sim 60 \text{ km s}^{-1} \text{ Mpc}^{-1}$ . Riess et al. (2005) review this issue, in order to reconcile the distances obtained by the two groups to galaxies that have hosted a SN Ia.

Four of the SNe Ia used in our study have a direct Cepheid distance to their host galaxy, and one has a Cepheid distance to its galaxy cluster. Whether the distance scale is long or short will depend on which data we use (i.e. from which of these two groups). This in turn will lead to either an under- or over-estimation of the distance. This uncertainty in the distance will affect the  $^{56}\text{Ni}$  mass we determine, hence the ejected mass.

To illustrate the effect of this on our results, we consider the galaxy NGC 3982. This galaxy has three independent Cepheid distance measurements, one from each of the two teams just mentioned and one from Riess et al. (2005), who use a new calibration of the  $P - L$  relationship and an elegant metallicity correction.

The STS group has published a distance modulus of  $\mu = 31.72 \pm 0.14$  (Saha et al. 2001b), which is based on the Cepheid  $P - L$  relation published by Madore & Freedman (1991). Using a  $P - L$  relation based on  $\sim 650$  Cepheids located in the Large Magellanic Cloud that were observed by the Optical Gravitational Lensing Experiment (OGLE) (Udalski et al. 1999), the HKP team concluded that  $\mu = 31.56 \pm 0.08$  (Stetson et al. 2001). More recently Riess et al. (2005) used the Advanced Camera for Surveys on the HST to obtain a Cepheid distance. They use the  $P - L$  relation presented by Tammann & Reindl (2002) and Thim et al. (2003). This relation is based on only those Cepheids in the OGLE data set that have periods longer than 10 days. With this new  $P - L$  relation, and after applying a metallicity correction, Riess et al. found  $\mu = 31.66 \pm 0.09$ .

With the HKP distance modulus we obtain a  $^{56}\text{Ni}$  mass that is 9% less compared to the STS distance modulus and 4% less with the Riess et al. distance modulus. In turn, the ejected mass derived with the HKP distance modulus is 22% greater compared to the STS distance modulus and 13% greater compared to the Riess et al. distance modulus.

We used a SBF distance for three SNe Ia in this sample. The zero-point for this method is based on an empirical relation derived from Cepheids, which can lead to a systematic under- or over-estimation of the distance, depending on whose Cepheids are used for the calibration. The three SBF distances we used are calibrated with the HKP Cepheid distances of Ferrarese et al. (2000). As pointed out by Tonry et al. (2001), the zero-point for the SBF distance scale is still being improved. With the application of the Cepheids determined with the complete set of OGLE data, the SBF distances used here would be  $\sim 0.1$  mag fainter. With this correction our derived  $^{56}\text{Ni}$  masses would increase by  $\sim 8\%$ , and the ejected masses would decrease by  $\sim 16\%$ .

Finally, in Table 1 we list two parameters calculated in this study: (1) an estimate of the amount of  $^{56}\text{Ni}$  produced from burning to NSE (see Sect. 3.1) and (2) an estimate of the time when the ejecta makes the transition from being optically thick to optically thin (see Sect. 3.2).

To construct the UVOIR light curves we used the method already employed by Vacca & Leibundgut (1996, 1997), Contardo et al. (2000), and Stritzinger & Leibundgut (2005). We refer the reader to these articles for more detailed descriptions of this empirical fitting method, which we briefly summarize here.

<sup>1</sup> Throughout this work we adopt  $H_0 = 72 \text{ km s}^{-1} \text{ Mpc}^{-1}$ .

Table 1. Well-observed SNe Ia.

SN	Filters	Ref.	$E(B - V)_{\text{gal}}^a$	$E(B - V)_{\text{host}}$	$\mu$	vel ( $\text{km s}^{-1}$ )	Ref. <sup>b</sup>	$M_{\text{Ni}}$ ( $M_{\odot}$ )	$t_0$ (days)	$M_{\text{ej}}$ ( $M_{\odot}$ )	$M_{\text{IME}}$ ( $M_{\odot}$ )
SN 1989B	UBVRI	1	0.032	0.340(0.04)	30.22(0.12)	797	21	0.64(0.18)	32.23(0.12)	1.06(0.32)	0.42
SN 1991T	UBVRI	2	0.022	0.140(0.05)	30.74(0.12)	1012	22	0.93(0.30)	34.44(0.23)	1.21(0.36)	0.28
SN 1991bg	BVRI	3, 4, 5	0.040	0.030(0.05)	31.32(0.11)	1322	23	0.11(0.03)	21.62(0.11)	0.48(0.14)	0.37
SN 1992A	UBVRI	6	0.017	0.000(0.02)	31.35(0.07)	1341	24	0.40(0.03)	26.58(0.10)	0.72(0.22)	0.32
SN 1994D	UBVRI	7, 8, 9	0.022	0.000(0.02)	31.08(0.20)	1184	25	0.64(0.13)	25.31(0.11)	0.65(0.20)	0.01
SN 1994ae	BVRI	10	0.031	0.120(0.03)	32.29(0.06)	2067	13	0.84(0.13)	32.33(0.13)	1.07(0.32)	0.23
SN 1995D	BVRI	10, 11	0.058	0.040(0.02)	32.50(0.26)	2272	CMB	0.66(0.23)	35.15(0.12)	1.26(0.38)	0.60
SN 1995E	BVRI	10	0.027	0.740(0.03)	33.42(0.18)	3478	CMB	0.88(0.26)	31.49(0.11)	1.01(0.30)	0.13
SN 1996X	UBVRI	10, 12	0.069	0.010(0.02)	32.40(0.20)	2174	12	0.73(0.21)	28.70(0.10)	0.84(0.25)	0.11
SN 1998aq	UBVRI	13	0.014	0.002(0.05)	31.66(0.09)	1547	13	0.68(0.18)	28.88(0.17)	0.85(0.25)	0.17
SN 1998de	BVRI	14	0.060	0.000(0.05)	34.05(0.14)	4653	CMB	0.09(0.03)	27.80(0.10)	0.68(0.20)	0.59
SN 1999ac	UBVRI	15	0.046	0.120(0.05)	33.06(0.21)	2949	CMB	0.67(0.29)	33.24(0.11)	1.13(0.34)	0.46
SN 1999dq	UBVRI	16	0.024	0.139(0.05)	33.74(0.16)	4029	CMB	0.80(0.29)	34.91(0.14)	1.24(0.37)	0.44
SN 2000cx	UBVRI	16, 17, 18	0.082	0.000(0.05)	31.90(0.20)	1727	23	0.38(0.16)	25.40(0.09)	0.66(0.20)	0.28
SN 2001el	UBVRI	19	0.014	0.206(0.05)	30.83(0.54)	1053	CMB	0.40(0.38)	31.94(0.12)	1.04(0.31)	0.64
SN 2003du	UBVRI	20	0.010	0.000(0.05)	32.23(0.30)	2011	CMB	0.38(0.21)	32.16(0.13)	1.05(0.32)	0.67

<sup>a</sup> Taken from Schlegel et al. (1998) dust maps.

<sup>b</sup> For events without a direct distance estimate we selected Heliocentric velocities listed in NED and transformed these to the CMB reference frame. To account for peculiar velocities throughout this work we assume an error of  $300 \text{ km s}^{-1}$  for all CMB distances.

References (1) Wells et al. (1994); (2) Lira et al. (1998); (3) Filippenko et al. (1992); (4) Leibundgut et al. (1993); (5) Turatto et al. (1996); (6) Suntzeff (1996); (7) Meikle et al. (1996); (8) Patat et al. (1996); (9) Richmond et al. (1995); (10) Riess et al. (1999); (11) Sadakane (1996); (12) Salvo et al. (2001); (13) Riess et al. (2005); (14) Modjaz et al. (2001); (15) Phillips et al. (2006); (16) Jha (2002); (17) Li et al. (2001); (18) Candia et al. (2003); (19) Krisciunas et al. (2003); (20) Stanishev et al. (2005); (21) Saha et al. (1999); (22) Saha et al. (2001a); (23) Tonry et al. (2001); (24) Madore et al. (1999); (25) Ajhar et al. (2001).

Each filtered light curve is fitted with a ten-parameter function. This function consists of a Gaussian for the peak phase, a linear decline for the late-time decay (i.e.  $^{56}\text{Co} \rightarrow ^{56}\text{Fe}$ ), an exponentially rising function to fit the initial rise to maximum, and a second Gaussian for the inflection or secondary maximum that is observed in the *VRI*-band light curves.

A correction was added for those SNe Ia without a *U*-band light curve as described by Contardo et al. (2000). They used a correction based on SN 1994D (Patat et al. 1996; Richmond et al. 1995; Meikle et al. 1996); however, this event had an unusual blue color at maximum, so corrections based on SN 1994D tend to overestimate the fraction of flux associated with the *U*-band photometry (Stritzinger 2005). Instead we employed a correction derived from SN 1992A (Suntzeff 1996). Although there are many well observed events, SN 1992A is one of the only *normal* SN Ia that does not suffer extinction due to host galaxy reddening.

Owing to a lack of data we did not include the fraction of flux associated with wavelengths above 10 000 Å. However, at maximum light the *JHK*-bands contribute no more than  $\sim 5\%$  (Suntzeff 1996) to the total bolometric flux. Around 60 days after maximum light, when the bolometric light curve follows a nearly linear decline, the infrared contribution rises to no more than  $\sim 10\%$  of the total bolometric flux (Contardo 2001).

To produce the UVOIR light curve, each fitted light curve is converted to flux ( $\text{erg s}^{-1}$ ). Next a reddening correction is applied, and then each filtered light curve is summed to obtain the total flux. Note that we do not normalize the flux to any decline-rate relation (e.g.  $\Delta m_{15}$  (Phillips et al. 1999), MLCs (Riess et al. 1996), or stretch (Perlmutter et al. 1997; Nobili et al. 2005)).

### 3. Determining global parameters of SNe Ia

In this section we describe the manner in which UVOIR light curves are used to determine the parameters of interest here.

#### 3.1. The $^{56}\text{Ni}$ mass

At maximum light the peak luminosity of a SN Ia is related, to first order, to the amount of  $^{56}\text{Ni}$  produced during the explosion. The amount of  $^{56}\text{Ni}$  synthesized from burning to NSE is itself thought to be largely dependent on the explosion mechanism. With the  $^{56}\text{Ni}$  mass we are directly probing the most sensitive part of the explosion and can use observations to place constraints on the explosion mechanism.

Suntzeff (1996) showed that at maximum light  $\sim 80\%$  or more of the total flux from a SN Ia is emitted in the optical. Therefore with UVOIR light curves constructed from *UBVRI* broad-band photometry, one easily obtains a measure of the total flux and, through application of Arnett's Rule, the  $^{56}\text{Ni}$  mass. Arnett's Rule states that at maximum light, the luminosity of a SN Ia is equal to the instantaneous energy deposition rate from the radioactive decays within the expanding ejecta (Arnett 1982; Arnett et al. 1985). To determine the  $^{56}\text{Ni}$  mass

we use the simple relation that gives for 1  $M_{\odot}$  of  $^{56}\text{Ni}$  a total luminosity at maximum light of

$$L_{\text{max}} = (2.0 \pm 0.3) \times 10^{43} \left( \frac{M_{\text{Ni}}}{M_{\odot}} \right) \text{erg s}^{-1}. \quad (1)$$

The error in Eq. (1) corresponds to a 3-day uncertainty in the adopted bolometric rise time of 19 days (see Sect. 4.1 of Stritzinger & Leibundgut 2005, for more details). As approximately 10% of the total flux at maximum light is emitted outside of the optical, each  $^{56}\text{Ni}$  mass derived from Eq. (1) has been increased by a factor of 1.1. The dominant errors in the deduced  $^{56}\text{Ni}$  mass are associated with the adopted distance to the host galaxy and the total extinction (Contardo et al. 2000).

#### 3.2. Total ejected mass

To place constraints on the ejected mass we perform a least-squares fit of a radioactive beta-decay energy (RDE) deposition function to the post maximum phase UVOIR light curve. Prior works that discuss this method include the pioneering investigations of Colgate et al. (1980a,b), followed by the more sophisticated treatment presented by Jeffery (1999); see also Cappellaro et al. (1997), Milne et al. (1999), and Milne et al. (2001) for similar methods and techniques. However, so far no attempt has been made to apply such a method to UVOIR light curves derived from real observations.

An expression for the energy deposition of  $N_{\text{Ni0}}$  atoms of  $^{56}\text{Ni}$  in the optically thin limit (i.e. when  $\tau \ll 1$ ) is represented by

$$\begin{aligned} E_{\text{dep}} &= E_{\text{Ni}} + E_{\text{Co } e^+} + [1 - \exp(-\tau)]E_{\text{Co } \gamma} \\ &= \lambda_{\text{Ni}} N_{\text{Ni0}} \exp(-\lambda_{\text{Ni}} t) Q_{\text{Ni } \gamma} \\ &\quad + \lambda_{\text{Co}} N_{\text{Ni0}} \frac{\lambda_{\text{Ni}}}{\lambda_{\text{Ni}} - \lambda_{\text{Co}}} [\exp(-\lambda_{\text{Co}} t) - \exp(-\lambda_{\text{Ni}} t)] \\ &\quad \times \{Q_{\text{Co } e^+} + Q_{\text{Co } \gamma} [1 - \exp(-\tau)]\}. \end{aligned} \quad (2)$$

Here,  $\lambda_{\text{Ni}}$  and  $\lambda_{\text{Co}}$  are the respective e-folding decay times of 8.8 and 111.3 days for  $^{56}\text{Ni}$  and  $^{56}\text{Co}$ ;  $Q_{\text{Ni } \gamma}$  (1.75 MeV) is the energy released per  $^{56}\text{Ni} \rightarrow ^{56}\text{Co}$  decay;  $Q_{\text{Co } e^+}$  (0.12 MeV) and  $Q_{\text{Co } \gamma}$  (3.61 MeV) are the positron and  $\gamma$ -ray energies released per  $^{56}\text{Co} \rightarrow ^{56}\text{Fe}$  decay; for a detailed discussion of the radioactive properties of this decay chain see, e.g. Nadyozhin (1994). Note that throughout this work we assume that all neutrinos produced from the  $^{56}\text{Ni} \rightarrow ^{56}\text{Co} \rightarrow ^{56}\text{Fe}$  decay chain escape the ejecta entirely and do not contribute to the observed UVOIR flux.

As Eq. (2) is only applicable in the optically thin limit, when the thermalized photons can freely escape, it is safe to assume that at these epochs the majority of  $^{56}\text{Ni}$  has decayed to  $^{56}\text{Co}$ , and therefore the remaining amounts of  $^{56}\text{Ni}$  provide a negligible contribution to the energy deposition. At these epochs the UVOIR light curve appears to be nearly first order exponential, however it is more accurately described as “quasi-exponential” (see Jeffery 1999, for a detailed discussion). With

the presence of only one radioactive species, the mean optical depth  $\tau$  has a simple  $t^{-2}$  dependence:

$$\tau = \frac{t_0^2}{t^2}. \quad (3)$$

If we replace  $\tau$  in Eq. (2) with Eq. (3) and then perform a least-squares fit of Eq. (2) to the UVOIR light curve (between 50 and 100 days past maximum light when Eq. (2) is valid), we can determine the “fiducial time”  $t_0$ . It is at this time that the ejecta becomes optically thin.

Following the discussion of Jeffery (1999), one finds that  $t_0$  can be expressed as

$$t_0 = \left( \frac{M_{\text{ej}} \kappa q}{8\pi} \right)^{\frac{1}{2}} \frac{1}{v_e}. \quad (4)$$

The variable  $M_{\text{ej}}$  is the total ejected mass,  $\kappa$  the  $\gamma$ -ray mean opacity,  $v_e$  the e-folding velocity of an exponential model’s density profile, and  $q$  a general form factor that describes the distribution of  $^{56}\text{Ni}$  in the ejecta.

During the optically thin phase for an all-metal ejecta ( $\mu_e = 2$ ),  $\kappa$  is expected to be in the range 0.025 to 0.033  $\text{cm}^2 \text{g}^{-1}$  (see Swartz et al. 1995; Jeffery 1999, and references therein for a detailed discussion). We adopted the value of 0.025  $\text{cm}^2 \text{g}^{-1}$  as our fiducial  $\gamma$ -ray mean opacity. Jeffery (1999) lists the model e-folding velocity of several successful 1D explosion models consisting of 1.4  $M_{\odot}$  Chandrasekhar-size white dwarfs. These e-folding velocities are  $\sim 2700 \text{ km s}^{-1}$  for W7 (Nomoto et al. 1984), 2750  $\text{ km s}^{-1}$  for DD4 (Woosley & Weaver 1994a), and 3000  $\text{ km s}^{-1}$  for M 36 (Höflich 1995). In addition Jeffery et al. (1992) find that the DD2 model of Woosley (1991) has a e-folding velocity of  $\sim 3160 \text{ km s}^{-1}$ .

More recently Röpke & Hillebrandt (2004) published two full-star 3D explosion models of a 1.4  $M_{\odot}$  white dwarf, with different ignition conditions: a centrally ignited configuration (c3\_4 $\pi$ ) and a foamy multi-bubble flame structure (f1). Using Eq. (A10) of Jeffery (1999) and parameters given in Table 1 of Röpke & Hillebrandt (2004), we calculated the e-folding velocities for these two models. The e-folding velocities correspond to  $\sim 1611 \text{ km s}^{-1}$  for the c3\_4 $\pi$  simulation and  $\sim 1842 \text{ km s}^{-1}$  for the f1 simulation. These values are substantially smaller than the previously cited 1D models and reflect the difference between the density profiles generated by 1D and 3D simulations. Note that all these models are based on the explosion of a 1.4  $M_{\odot}$  Chandrasekhar-size white dwarf. In the calculations presented below we arbitrarily adopted 3000  $\text{ km s}^{-1}$  as our “average” fiducial e-folding velocity.

The parameter  $q$  is equal to one for high concentrations of  $^{56}\text{Ni}$  at the center of the ejecta, small for low concentrations within the center, and one-third for the case when the  $^{56}\text{Ni}$  is evenly distributed throughout the ejecta (see Jeffery 1999, for a detailed discussion). There is mounting evidence that an appreciable amount of  $^{56}\text{Ni}$  is moderately mixed within the ejecta. However, it is likely that the amount of mixing may vary significantly from supernova to supernova.

An analysis of the early-time spectra of SN 1991T (Ruiz-Lapuente et al. 1992; Mazzali et al. 1995) indicates the

existence of an outer shell of  $^{56}\text{Ni}$ . In contrast, Georgii et al. (2002) presented observations of SN 1998bu obtained with COMPTel. They concluded that their non-detection of  $\gamma$  rays from the  $^{56}\text{Co} \rightarrow ^{56}\text{Fe}$  decay chain indicates that there is no appreciable mixing of radioactive nuclides within the ejecta in the context of current models. More recently Stehle et al. (2005) present “abundance tomography” of SN 2002bo. With their unique technique they determine that the vast majority of  $^{56}\text{Ni}$  was distributed between 3000 to 11 000  $\text{ km s}^{-1}$  for this particular event. Jeffery (1999) showed that for W7, the parameter  $q$  was equal to approximately one-third. As W7 has been able to fit observed spectra for normal to bright SNe Ia (Harkness 1991; Mazzali et al. 1995; Mazzali 2001) quite successfully, we adopted a  $q$  value of one-third in the calculations presented below.

With values of  $t_0$  derived from the least squares fit of Eq. (2) to the UVOIR light curve during the quasi exponential phase, along with the adopted fiducial values for all the parameters in Eq. (4), we can proceed to place constraints on the ejected mass for each SN Ia in our sample.

### 3.3. The $\gamma$ -ray escape fraction

By comparing the UVOIR light curve to the energy input from the radioactive decays – for both cases of complete trapping of  $\gamma$  rays and complete escape of  $\gamma$  rays – we can obtain a quantitative description of the  $\gamma$ -ray escape fraction. An expression for the UVOIR light curve based on this prescription can be written as

$$LC(t)_{\text{obs}} = (1 - \gamma(t))LC(t)_{\tau \gg 1} + \gamma(t)LC(t)_{\tau \ll 1}. \quad (5)$$

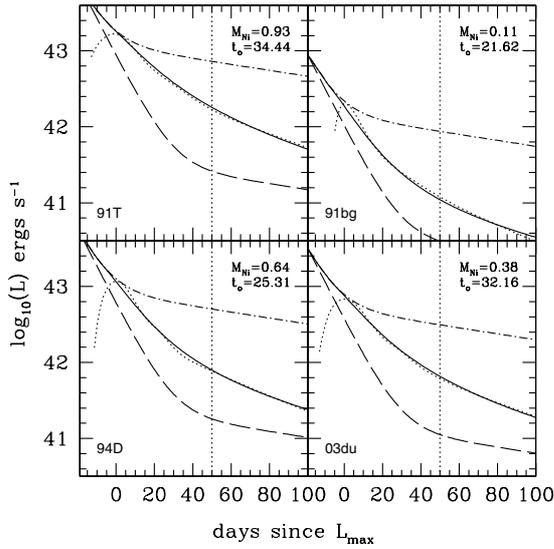
In this expression  $LC(t)_{\text{obs}}$  is the UVOIR light curve,  $LC(t)_{\tau \gg 1}$  represents the energy input from the radioactive decays assuming complete trapping of  $\gamma$  rays,  $LC(t)_{\tau \ll 1}$  represents the case of a complete escape of  $\gamma$  rays, and  $\gamma(t)$  is the  $\gamma$ -ray escape fraction. Solving Eq. (5) for  $\gamma(t)$  we obtain the  $\gamma$ -ray escape fraction

$$\gamma(t) = \frac{LC(t)_{\tau \gg 1} - LC(t)_{\text{obs}}}{LC(t)_{\tau \gg 1} - LC(t)_{\tau \ll 1}}. \quad (6)$$

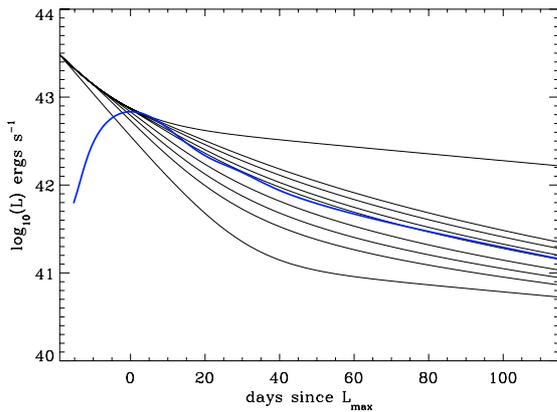
## 4. Results

In Fig. 1 we present the least squares fits of Eq. (2) to several UVOIR light curves. The four events shown in Fig. 1 are representative of the complete population of SN Ia, ranging from the bright SN 1991T to the subluminous SN 1991bg. Also plotted are the energy deposition curves corresponding to the  $^{56}\text{Ni} \rightarrow ^{56}\text{Co} \rightarrow ^{56}\text{Fe}$  decay chain for the cases of complete  $\gamma$ -ray trapping (dash-dotted line) and complete  $\gamma$ -ray escape (dashed line). Table 1 lists the  $^{56}\text{Ni}$  mass calculated for each event through Eq. (1), as well as the determined values of  $t_0$ . For this sample of SNe Ia, the  $^{56}\text{Ni}$  mass varies by a factor of  $\sim 10$ , while  $t_0$  varies by a factor of 1.6.

In order to give the reader a more intuitive feeling of how the RDE deposition curve depends on the value of  $t_0$ , we present Fig. 2. This figure contains the UVOIR light curve of



**Fig. 1.** Fit of Eq. (2) (solid line) to the UVOIR bolometric light curve (dotted curve) between 50 and 100 days past maximum light. The dashed-dotted line is the energy deposition of  $\gamma$  rays and positrons from the  $^{56}\text{Ni}$  to  $^{56}\text{Co}$  to  $^{56}\text{Fe}$  decay, assuming complete trapping (i.e.  $\tau \gg 1$ ). The dashed line is the case for the complete escape of  $\gamma$  rays (i.e.  $\tau \ll 1$ ). The vertical dotted line indicates the epoch (+50 days) when the fit begins.

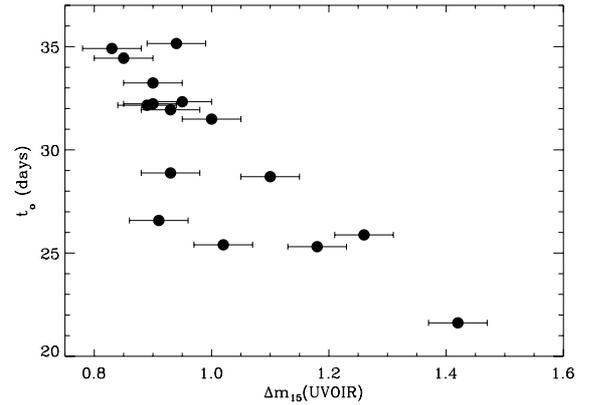


**Fig. 2.** Plot of Eq. (2) for a fixed  $^{56}\text{Ni}$  mass of  $0.38 M_{\odot}$  while varying  $t_0$  (solid lines). Here  $t_0$  ranges (from top to bottom) from  $\infty$ , 45, 40, 35, 32.16, 25, 20, 15, to 0 days. The light curve corresponds to SN 2003du.

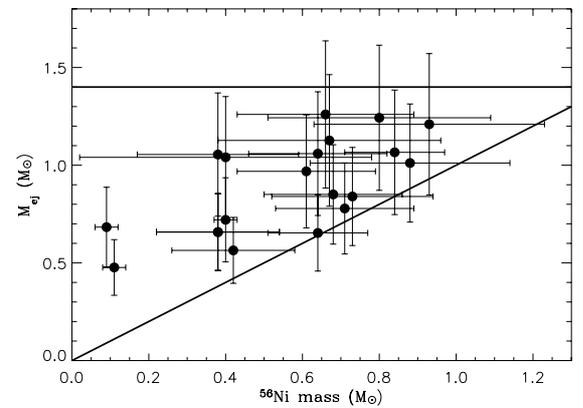
SN 2003du, along with the energy deposition curves for different values of  $t_0$  that vary from  $\infty$ , 45, 40, 35, 32.16, 25, 20, 15, to 0 days. As expected for a fixed  $^{56}\text{Ni}$  mass, when  $t_0$  is increased, the energy RDE deposition function evolves more slowly with respect to time. Physically this effect is associated with an increase in the diffusion time of the photons trapped within the ejecta.

In Fig. 3 we plot  $t_0$  versus  $\Delta m_{15}(\text{UVOIR})^2$ . Values for  $\Delta m_{15}(\text{UVOIR})$  were determined from the UVOIR light curves. From this figure it is clear that a correlation exists between these two parameters that is in accord with our expectations, as it is well established that more luminous SNe Ia have smaller

<sup>2</sup> By plotting  $\Delta m_{15}(\text{UVOIR})$  rather than the  $^{56}\text{Ni}$  mass, we bypass the effect upon the luminosity (hence  $^{56}\text{Ni}$  mass) associated with the uncertainty in the adopted distance to each event.



**Fig. 3.** Fiducial time,  $t_0$  plotted vs.  $\Delta m_{15}(\text{UVOIR})$ . Note the error bars associated with the values of  $t_0$  are smaller than the size of the points.



**Fig. 4.** Ejected mass plotted vs.  $^{56}\text{Ni}$  mass for 16 SNe Ia. Units are in solar mass. See text for comments concerning the error bars. The solid horizontal line indicates the Chandrasekhar mass. The slanted line has a slope of 1.

decline rates. Thus the epoch in which their ejecta transform to the nebular phase occurs at a later time; see Pinto & Eastman (2001), and references within for a detailed discussion of the physics that describes the luminosity-width relation.

Armed with our values of  $t_0$ , we can now proceed to place constraints on the total ejected mass. Figure 4 is a plot of our calculated ejected mass versus the  $^{56}\text{Ni}$  mass. To calculate the ejected mass we used  $q = 1/3$ ,  $v_e = 3000 \text{ km s}^{-1}$  and  $\kappa = 0.025 \text{ cm}^2 \text{ g}^{-1}$ . The error bars that accompany each  $^{56}\text{Ni}$  mass account for uncertainties in host galaxy reddening and the adopted distance (see Table 1). For events with a CMB distance we assumed a  $300 \text{ km s}^{-1}$  uncertainty for (random) peculiar velocities.

The ejected mass error bars include: (1) the uncertainty listed in Table 1 for each value of  $t_0$ ; (2) a  $300 \text{ km s}^{-1}$ , i.e. 10%, uncertainty in  $v_e$ ; (3) a 10% uncertainty in  $\kappa$ ; and (4) a 30% uncertainty in the adopted value of  $q$ . These “1- $\sigma$ ” error bars are not statistical but rather a sensible estimation of the possible range of each parameter.

Figure 4 displays several striking features that are worthy of comment. First, this figure suggests that a range exists in the ejected mass of about a factor of two. Three events (SN 1992A, SN 1994D, and SN 2000cx) with moderate amounts of  $M_{ej}$  (i.e.

0.4–0.6  $M_{\odot}$ ) are of particular interest. These events are located nearly 3- $\sigma$  below the most massive events, which lie near the canonical value of 1.4  $M_{\odot}$ . In order to increase the ejected mass of these three events to a Chandrasekhar mass, it is necessary to reduce either  $q$  (which is highly unlikely) or our fiducial value of  $\kappa$  by a factor of two, else increase either the value of  $t_0$  by a factor of  $\sim 1.3$  or  $v_e$  by a factor of  $\sim 1.4$  or more. Implementing any of these changes results in ejected masses for all the other “normal” SNe Ia to be comparable to that of a neutron star mass. In other words, if we change any one of the parameters in Eq. (4) while keeping all others constant, a relative difference will always exist in the ejected mass of  $\sim 2$  between these three events shown in Fig. 4, as compared to the more massive SNe Ia. Of course this is the case if the changes are applied uniformly to the whole sample. In reality some events may have different values for the parameters listed in Eq. (4) when compared to each other.

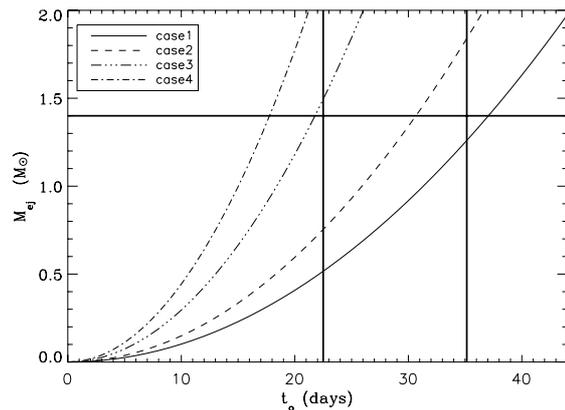
The problem can, of course, be inverted to derive mean values of  $q$ ,  $\kappa$ , and  $v_e$  for a fixed ejected mass. With an ejected mass of 1.4  $M_{\odot}$  we find mean values  $\langle v_e \rangle = 3762 \text{ km s}^{-1}$ ,  $\langle q \rangle = 0.224$ , and  $\langle \kappa \rangle = 0.0080 \text{ cm}^2 \text{ g}^{-1}$ . If the two subluminous events (i.e. SN 1991bg and SN 1998de) are excluded, these parameters change to  $\langle v_e \rangle = 3625 \text{ km s}^{-1}$ ,  $\langle q \rangle = 0.236$ , and  $\langle \kappa \rangle = 0.0084 \text{ cm}^2 \text{ g}^{-1}$ .

This e-folding velocity may be slightly on the high side compared to what is predicted from successful 1D explosion models. However, it is not radically different from our adopted e-folding velocity. An explosion model with the majority of the  $^{56}\text{Ni}$  mixed in the outer layers, as implied by  $q = 0.224$ , is most unlikely for the vast majority of robust explosion models. But this could be the case for a Chandrasekhar mass progenitor that produces a subluminous SN Ia. As mentioned before, in the optically thin limit  $\kappa$  ranges from 0.025 to 0.033  $\text{cm}^2 \text{ g}^{-1}$ . A factor of two (or even three) less for  $\kappa = 0.025 \text{ cm}^2 \text{ g}^{-1}$  is unlikely. At most one could conceive of  $\kappa$  varying by  $\sim 50\%$ .

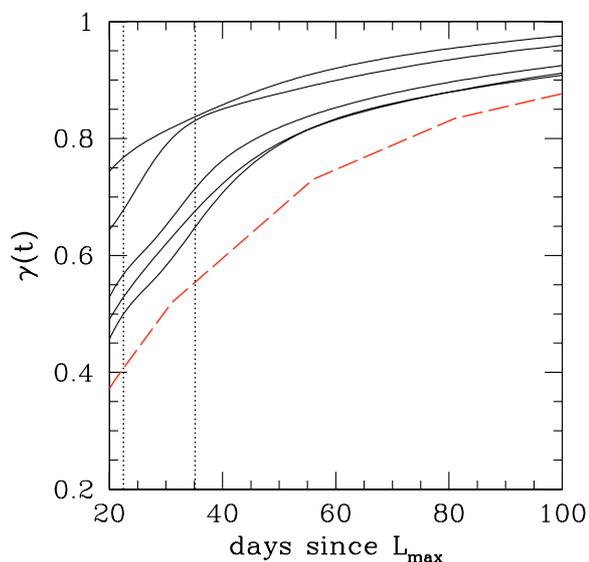
To calculate the amount of intermediate mass elements (IMEs) produced during nuclear burning, we simply subtract the ejected mass from the amount of  $^{56}\text{Ni}$  produced. Note this value also includes any stable Fe group elements and the remaining amount of unburned carbon and oxygen. These values are listed in Table 1. Excluding SN 1994D we find that the IMEs range from  $\sim 0.11$  to  $\sim 0.67 M_{\odot}$ .

In Fig. 5 we plot the ejected mass versus  $t_0$ , while holding the other parameters of Eq. (4) constant. Case 1 corresponds to all the fiducial values used to determine the ejected masses in Fig. 4. Case 2 shows the effect of keeping  $q$  and  $\kappa$  fixed at the fiducial values while using  $v_e = 3625 \text{ km s}^{-1}$ . For case 3 we used  $v_e = 3625 \text{ km s}^{-1}$ ,  $\kappa = 0.0084 \text{ cm}^2 \text{ g}^{-1}$  and  $q = 0.5$ . Finally case 4 corresponds to  $v_e = 3625 \text{ km s}^{-1}$ ,  $q = 1/3$ , and  $\kappa = 0.0084 \text{ cm}^2 \text{ g}^{-1}$ . This figure illustrates the strong dependencies of the ejected masses. Masses much above the Chandrasekhar mass are achieved for only extreme cases. Case 1 and 2 both provide ejected masses at or near the Chandrasekhar mass for events with large values of  $t_0$  and substantially less for those events with values of  $t_0 \approx 22$ –26 days.

Another interesting feature displayed in Fig. 4 is that there appears to be little or no correlation between the ejected mass and the amount of  $^{56}\text{Ni}$ . This is not entirely unexpected



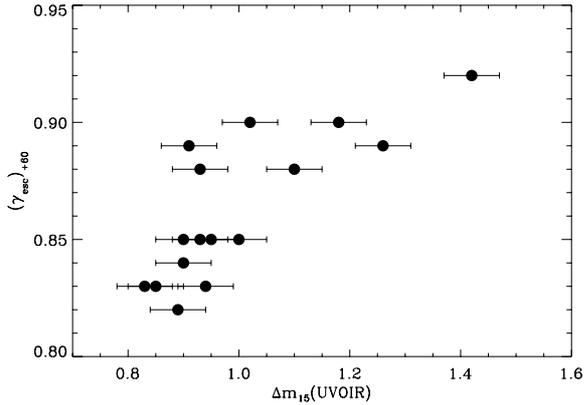
**Fig. 5.** Ejected mass plotted vs.  $t_0$  for fixed values of the parameters in Eq. (4). See Sect. 4 for a complete description of each curve. Solid vertical lines indicate the minimum and maximum values for  $t_0$  in our sample, and the solid horizontal line indicates the Chandrasekhar mass.



**Fig. 6.** The  $\gamma$ -ray escape fraction as a function of time since maximum light for five SN Ia in our sample. These include (from top to bottom) SN 1991bg, SN 1994D, SN 2003du, SN 1991T, and SN 1999dq. The red dashed line corresponds to W7. The vertical dot lines are the minimum and maximum values of  $t_0$ . For W7 we have assumed a rise time to bolometric maximum of 19 days.

because, even with the presumption that all SNe Ia originate from a Chandrasekhar-size white dwarf, a range of ten or more still exists in the amount of  $^{56}\text{Ni}$  produced. Nevertheless this is additional evidence suggesting that there is a significant variation in the burning of SNe Ia.

We now turn our attention to the issue of the  $\gamma$ -ray escape fraction. In Fig. 6 we present the  $\gamma$ -ray escape fraction as a function of time (determined from Eq. (6)) for five of the SNe Ia in our sample. As the ejecta of the supernova expands, there is an increase in the  $\gamma$ -ray escape fraction. This can be attributed to the decrease in the column density, which is accompanied with the expansion of the ejecta. Most of the curves in this figure are accompanied by a “bump” between 20 and 40 days past maximum light. Also included in Fig. 6 is the



**Fig. 7.** The  $\gamma$ -ray escape fraction at sixty days past maximum light vs.  $\Delta m_{15}(\text{UVOIR})$ .

$\gamma$ -ray escape fraction calculated from W7. The agreement between W7 and our calculated  $\gamma$ -ray escape fraction curves is encouraging, considering that we are not adjusting any parameters<sup>3</sup>. For the first three weeks after maximum light the  $\gamma$ -ray escape fraction from the UVOIR light curves is unreliable, as it is based on the assumption of  $\tau \ll 1$ , which clearly is not the case for  $t < t_0$ .

From Fig. 6 it is clear that the  $\gamma$ -ray escape fraction evolves faster in time for less luminous events. This is confirmed by Fig. 7 where we plot the  $\gamma$ -ray escape fraction at sixty days past bolometric maximum light versus  $\Delta m_{15}(\text{UVOIR})$ . At this epoch  $\sim 10\%$  more  $\gamma$  rays escape in the least luminous SNe Ia than in the brightest events. However, between 20 and 40 days past maximum light the differences are even more pronounced. This is expected, as at these epochs the UVOIR light curve has not yet reached its linear decline. In addition, the morphology of the secondary maximum can vary radically from SN to SN (Suntzeff 2003; Stritzinger 2005). This may then have a significant effect on the evolution of the  $\gamma$ -ray escape fraction during these phases.

## 5. Discussion

With the stipulation that the UVOIR light curve reasonably traces the true bolometric flux, from within the period soon after explosion to one hundred days past maximum light, we have been able to derive constraints on several important global parameters that relate directly to the progenitor systems of SNe Ia. The appeal of our approach is that, with relative ease and simple assumptions, we used existing data to gain a deeper understanding of the origins of SNe Ia, as well as to provide sorely needed constraints on current models.

As previously mentioned, it is commonly believed that SNe Ia are the result of the thermonuclear disruption of a C–O white dwarf. The premise that thermonuclear combustion occurs at the Chandrasekhar limit was invoked to address the issue of homogeneity. However, today it is well established that SNe Ia are not true standard candles as once thought in

the past (e.g. Leibundgut 2004)<sup>4</sup>. Therefore we now must carefully scrutinize the data at hand in order to find plausible explanations that can account for the radical differences observed between different SNe Ia.

We first showed that the  $^{56}\text{Ni}$  mass (hence luminosity) ranges from  $\sim 0.1$  to  $\sim 1.0 M_{\odot}$ . This confirms results previously attained by several similar and independent methods (Bowers et al. 1997; Cappellaro et al. 1997; Contardo et al. 2000; Strolger et al. 2002; Suntzeff 2003). But this result is quite disheartening from earlier assertions that SNe Ia are standard candles. If all SNe Ia do indeed originate from a Chandrasekhar mass, an immediate question then is: what physical mechanism(s) can explain this range in luminosity?

There has been considerable effort on the part of modelers to address this question. Yet they have had little success identifying what parameter(s) can be tuned in order to account for a factor of ten in  $^{56}\text{Ni}$  mass. Obvious candidates that may affect the production of  $^{56}\text{Ni}$  are the initial parameters prior to explosion, e.g. metallicity, central density, and ignition mechanism(s). Recently, Röpke & Hillebrandt (2004) have shown that the C–O ratio has essentially no effect on the amount of  $^{56}\text{Ni}$  produced from burning to NSE. If prior to explosion there is a significant amount of alpha elements within the white dwarf, one may reasonably expect the production of more stable isotopes, thus reducing the amount of  $^{56}\text{Ni}$  synthesized (Brachwitz et al. 2000). Moreover it has been shown that changes in the central density of the white dwarf do influence the robustness of the explosion. Nevertheless, it is unrealistic that any one of these parameters, or even a combination of the three, can account for a factor of ten range in the  $^{56}\text{Ni}$  mass. In reality these parameters affect the production of  $^{56}\text{Ni}$  by no more than  $\sim 20\%$ .

The explosion mechanism itself is more likely to influence the amount of  $^{56}\text{Ni}$  synthesized (see Stritzinger & Leibundgut 2005). Currently the explosion mechanism and the subsequent evolution of the burning front are openly debated, as varying from a subsonic deflagration to a supersonic delayed detonation. Today the best Chandrasekhar mass models predict  $^{56}\text{Ni}$  masses that range between  $\sim 0.40$  to  $0.60 M_{\odot}$ . Due to computational limitations, the state-of-the-art 3D deflagration models (Reinecke et al. 2002a,b) do not produce copious amounts of  $^{56}\text{Ni}$  (Travaglio et al. 2004) and have appreciable amounts of unburned carbon and oxygen left over in the inner ashes (Kozma et al. 2005). The delayed detonation models (Khokhlov 1991; Woosley 1990; Woosley & Weaver 1994a; Höflich & Khokhlov 1996), on the other hand, can account for some of the more luminous events; but this class of models requires an additional free parameter to force the transition of the flame propagation from a deflagration to a detonation, and is not physically understood (however, see Gamezo et al. 2004 and Golombek & Niemeyer 2005). The fact that a single class of Chandrasekhar mass models does not exist that can account for the complete population of SNe Ia is not satisfying and should be seriously addressed by theorists, if we are to

<sup>3</sup> Note that we assumed a rise time to bolometric maximum of 19 days.

<sup>4</sup> Recently Krisciunas et al. (2004) have presented evidence that SNe Ia appear to be nearly “standard candles” in the near-infrared.

insist that a Chandrasekhar-size white dwarf accounts for the progenitor system of *all* SNe Ia.

Under the main assumption that at longer than fifty days past maximum light the energy deposition in the ejecta of a SN Ia is solely due to the  $^{56}\text{Co} \rightarrow ^{56}\text{Fe}$  decay chain, and thus the optical depth has a  $t^{-2}$  dependence, we can estimate (from the UVOIR light curve) the epoch when the photosphere transforms from being optically thick to optically thin. With this knowledge we can then use the parameterized SN Ia model of Jeffery (1999) to place constraints on the ejected mass.

The results presented in Fig. 4 provide us with evidence that not *all* SNe Ia originate from a Chandrasekhar-size white dwarf or that other very severe differences exist in the explosions like the distribution of  $^{56}\text{Ni}$  or kinetic energies (expansion velocities). This would then immediately imply that some sort of sub-Chandrasekhar mass model is responsible for at least some SNe Ia. If true, this would be a radical change in thinking from the currently favored paradigm for the progenitor systems of SNe Ia. However, the suggestion that a sub-Chandrasekhar mass model may be a viable candidate for the progenitors of some SNe Ia is certainly not a new concept. Similar to Chandrasekhar mass models, previous attempts to simulate these systems have been plagued with their own problems. We refer the reader to Hillebrandt & Niemeyer (2000) and Livio (2000) for detailed reviews concerning this class of progenitor system; we briefly summarize them here.

Previous attempts to model sub-Chandrasekhar explosions (Woosley & Weaver 1994b; Livne & Arnett 1995; Höflich & Khokhlov 1996) have met with some success in reproducing the observed light curves. However, these models typically predict a high-velocity layer of  $^{56}\text{Ni}$  and helium above the IMEs, which is not observed in any spectra. It must be noted that relatively little effort has been made to conduct detailed 3D simulations of *sub*-Chandrasekhar mass models (but, see Garcia-Senz et al. 1999; Benz 1997). With more detailed modeling, this progenitor channel may provide an attractive alternative to the Chandrasekhar mass model. We also note that one appealing advantage offered by this model is the ability to obtain the progenitor statistics predicted by population synthesis calculations (see Livio 2000, and references within).

Previously, Cappellaro et al. (1997) employed a technique that used observations of SNe Ia to determine both the  $^{56}\text{Ni}$  mass and the ejected mass. In their method they modeled the *V*-band light curves of a small sample of SNe Ia using a simple Monte Carlo code. We find that our overall results are analogous to what they determined for both the range in the  $^{56}\text{Ni}$  mass and the ejected mass. In contrast to their work we employed a different manner to determine these parameters and used UVOIR light curves rather than *V*-band light curves. By using the UVOIR light curve instead of the *V*-band light curve, we circumvented the crude assumption that the latter is a close surrogate to the former during post maximum times. Indeed, a comparison between our UVOIR light curves and the *V*-band light curves indicates that by fifty days past maximum light, the bolometric correction ( $m_{\text{bol}} - m_{\text{v}}$ ) is  $\sim 0.2$  mag or more. At later times this difference is amplified, as the near infrared passbands provide an increasing contribution to the bolometric flux (Sollerman et al. 2004).

Although we find that our conclusions are in line with those presented in Cappellaro et al., there are subtle differences between the four events that coincide in both studies. The numbers we provide below for our results were obtained using Eq. (4) and the fiducial values quoted previously. Also, note that there are slight differences (no larger than  $\mu = 0.20$ ) in the distances used between our work and Cappellaro et al.

For SN 1991bg, Cappellaro et al. found a  $^{56}\text{Ni}$  mass  $M_{\text{Ni}} = 0.1 M_{\odot}$  and an ejected mass  $M_{\text{ej}} = 0.7 M_{\odot}$ . This is comparable to our findings of  $M_{\text{Ni}} = 0.11 M_{\odot}$  and  $M_{\text{ej}} = 0.48 \pm 0.14 M_{\odot}$ . Furthermore, our  $M_{\text{Ni}}/M_{\text{ej}}$  ratio of 0.23 is larger compared to their 0.14. For SN 1992A, we found  $M_{\text{Ni}} = 0.40 M_{\odot}$  and  $M_{\text{ej}} = 0.72 \pm 0.27 M_{\odot}$ , as compared to their  $M_{\text{Ni}} = 0.4 M_{\odot}$  and  $M_{\text{ej}} = 1.0 M_{\odot}$ . This then gives us an  $M_{\text{Ni}}/M_{\text{ej}}$  ratio of 0.56 compared to their 0.40.

We find that our results with respect to the next two SNe Ia differ more than the first two stated events. For SN 1994D we calculated  $M_{\text{Ni}} = 0.64 M_{\odot}$  and  $M_{\text{ej}} = 0.65 \pm 0.25 M_{\odot}$ , compared to their values of  $M_{\text{Ni}} = 0.8 M_{\odot}$  and  $M_{\text{ej}} = 1.4 M_{\odot}$ . Thus we obtain a larger difference in our  $M_{\text{Ni}}/M_{\text{ej}}$  ratio of 0.98 compared to their 0.57. However, the  $^{56}\text{Ni}$  mass of SN 1994D maybe viewed as uncertain. To determine it we used a new SBF distance (Ajhar et al. 2001) rather than the SBF distance (Tonry et al. 1997) used by Contardo et al. (2000) who determined a  $^{56}\text{Ni}$  mass of  $0.40 M_{\odot}$ . Using the distance modulus adopted by Cappellaro et al. we obtained a  $^{56}\text{Ni}$  mass of  $0.67 M_{\odot}$ . Recently Feldmeier et al. (2005) have calculated a planetary nebulae distance to the host galaxy of SN 1994D. In their study they determine the distance modulus  $\mu = 30.66$ . This is comparable to the Tonry et al. (1997) distances modulus  $\mu = 30.68$ . Using the planetary nebulae distance the  $^{56}\text{Ni}$  mass would be reduced to  $\sim 0.40 M_{\odot}$ . Nonetheless the  $^{56}\text{Ni}$  mass determined by us and Contardo et al. is less than the  $0.8 M_{\odot}$  calculated by Cappellaro et al. with their method. The discrepancies between these values of the  $^{56}\text{Ni}$  mass underscores the effect of the uncertainty in the distances.

Finally, for SN 1991T Cappellaro et al. assumed  $M_{\text{ej}} = M_{\text{Ni}}$  where  $M_{\text{Ni}} = 1.1 M_{\odot}$ . We, on the other hand, found  $M_{\text{Ni}} = 0.93 M_{\odot}$  and  $M_{\text{ej}} = 1.21 \pm 0.36 M_{\odot}$ . In summary we find the results presented by Cappellaro et al. to be in fair agreement with our calculations, although some discrepancies do exist.

We have presented an investigation of the bolometric behavior of sixteen SNe Ia. In particular we provided important constraints on the progenitor system(s) of these stellar explosions. Our results suggest that some progenitor system(s) of SN Ia may emanate from the thermonuclear explosion of a sub Chandrasekhar-size white dwarf. This result may be difficult to reconcile with the current paradigm of the progenitor system of SNe Ia, i.e. a Chandrasekhar-size white dwarf. Moreover, our results suggest that the amount of  $^{56}\text{Ni}$  produced during the explosion is most likely dependent not on the mass of the progenitor, but more on the manner in which nuclear burning is initiated and the subsequent dynamics of the flame propagation through the white dwarf. The range in synthesized  $^{56}\text{Ni}$  possibly indicates that there are two different explosion mechanisms. Further modeling of the explosion mechanism is required in order to investigate how different initial conditions can affect the observed range in luminosity.

In Fig. 4 we see – in contrast to current thinking – that the mean ejected mass of many explosions is on the low side. A valid concern is that the parameters used to determine the ejected masses may not exactly represent those of a real SN Ia explosion. One parameter that could be in error and that does have a significant effect on our estimates of the ejected masses, is the adopted value of the e-folding velocity (see Fig. 5). If we assume slightly higher values of  $v_e$ , the mean ejected mass for our sample would be in better agreement with  $1.4 M_{\odot}$ . How this parameter differs in 3D simulations compared to 1D simulations is not yet clear.

In addition, the simple assumption that any one of the parameters in Eq. (4) is unique for all events is probably incorrect. This may have a significant effect on the determined ejected mass for each event. However, this does not necessary imply that we would obtain larger ejected masses. It would be helpful if the theorists in the future provided values of  $v_e$  and  $q$  from their simulations.

An acceptable argument concerning the results presented in this work is the validity of the model used to determine the ejected mass. There may be several assumptions built into the parameterized model of Jeffery (1999), which may be too naïve, and therefore the model may not adequately account for various complicated physical processes that occur within the progenitor of a SN Ia. However, no other method currently exists using observed photometry to place constraints on such a parameter.

We would like to compare the UVOIR light curves to detailed NLTE-modeled light curves. Unfortunately there has been little success with such an endeavor, owing to the complications of performing such time-dependent calculations, as well as the limits of atomic line data; however, see Kozma et al. (2005). The next step will be to fit UVOIR light curves to a grid of model light curves produced from 3D radiative transfer calculations, and then place further constraints on the progenitor systems of SNe Ia.

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