About putative Neptune-like extrasolar planetary candidates

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ABSTRACT

Context. We re-analyze the precision radial velocity (RV) data of HD 208487 by the Anglo-Australian Planet Search Team, HD 190360, HD 188015, HD 114729 by the California and Carnegie Planet Search Team, and HD 147513 by the Geneva Planet Search Team. All these stars are supposed to host Jovian companions in long-period orbits.

Aims. We test a hypothesis that the residuals of the 1-planet model of the RV or an irregular scatter of the measurements around the synthetic RV curve may be explained by the existence of additional planets in short-period orbits.

Methods. We performed a global search for the best fits in the orbital parameters space with genetic algorithms and simplex method. This makes it possible to verify and extend the results with an application of commonly used FFT-based periodogram analysis for identifying the leading periods.

Results. Our analysis confirms the presence of a periodic component in the RV of HD 190360 that may correspond to a hot-Neptune planet. We found four new cases in which the 2-planet model yields significantly better fits to the RV data than the best 1-planet solutions. If the periodic variability of the residuals of single-planet fits indeed has a planetary origin, then hot-Neptune planets may exist in these extrasolar systems. We estimate their orbital periods as in the range of 7–20 d and minimal masses of about 20 masses of the Earth.

Key words. planetary systems – stars: individual: HD 208487 – stars: individual: HD 190360 – stars: individual: HD 188015 – stars: individual: HD 114729 – stars: individual: HD 147513

1. Introduction

The precision radial velocity (RV) surveys for extrasolar planets approach the limit of detection of Neptune-like companions. In the past year, a 14-Earth mass planet was announced by Santos et al. (2004), and a low-mass companion was found in the $\rho^1$ Cancri system (McArthur et al. 2004). Almost at the same time, a Neptune-like planet was also discovered by Butler et al. (2004). Very recently, Rivera et al. (2005) announced the discovery of ~7 Earth-mass planet in ~2 d orbit around the famous Gliese 876 planetary system. Also Vogt et al. (2005) announced a new multi-planet system around HD 190360 involving a Neptune-mass planet in $\approx$17.1 d orbit with a Jupiter-like companion with ~3000 d orbital period. These discoveries change the view of multi-planet systems. The low-mass planets found so far are very likely rocky bodies rather than massive gaseous hot-Jupiters. The architecture of their environment, involving also giant planets in relatively distant orbits, begin to resemble our own Solar System.

There are already speculations as to which of the extrasolar systems involving Jupiter-like planets can contain smaller companions. At present, such objects cannot be clearly detected because of the small amplitude of the contributed RV signal and observations that are not frequent enough. Nevertheless, the existence of such planets seems to be natural. The dynamical relaxation of planetary systems (Adams & Laughlin 2003) can lead to final configurations with orbits filling up the dynamically available space of stable orbits (Laskar 2000). In particular, many extrasolar systems containing distant Jupiter-like planets may contain smaller, still undetectable companions, which can easily survive in a close neighborhood of the parent star. Baraffe et al. (2005) show that the three recently detected hot-Neptune planets (around GJ 436, $\rho^1$ Cnc, $\mu$ Arae) may originate from more massive gas giants that have undergone significant evaporation. This work suggests that hot-Neptunes and hot-Jupiters may share the same origin and evolution history and that they can be as frequent as hot-Jupiters are. The numerical simulations by Brunini & Cionco (2005) show that the formation of compact systems of Neptune-like planets close to solar type stars could be a common by-product of planetary accretion. In turn, these theoretical works are supported by several new detections of hot-Neptune and hot-Saturn candidates (e.g., Bonfils et al. 2005; Udry et al. 2005; Curto et al. 2005; Fischer et al. 2005)$^1$.

The detection of Neptune-mass exoplanets is a breakthrough in the field, but the inevitable problem still lies in the limitations of the Doppler technique. The radial velocity signal of small, Neptune-like planets revolving close to the host

$^1$ For frequent updates of the references, please see the Extrasolar Planets Encyclopedia by Jean Schneider, http://www.obspm.fr/planets.
star has the semi-amplitude of a few meters per second, i.e., at a similar range as the measurement errors and chromospheric variability of the RV. This can be a source of erroneous interpretation of the observations. For instance, in a recent work, Wisdom (2005) claims that the orbital period of 2.38 d of companion d detected by McArthur et al. (2004) in the ρ1 Cancri system is an alias of two periods originating from the orbital motion of planets b and c, but instead, he found a evidence of another planet in a ~261 d orbit. Actually, a proper interpretation of the observations is still very difficult. Often, they can be equally well modeled by qualitatively different configurations, and even the number of planets cannot be resolved without doubt. An example will be given in this paper, too.

In this work, for a reference and a test of our approach, we re-analyze the published RV data of two stars. We check the results of Gregory (2005a) who claims that a second planet accompanies a confirmed Jovian companion b of HD 208487 (Timney et al. 2005). In the second case, HD 190360, the discovery team (Vogt et al. 2005) claims the existence of a hot-Neptune and a Jovian planet in long-period orbit. Next, using the same method, we study other three extrasolar systems: HD 188015 (Marcy et al. 2005b), HD 114729 (Butler et al. 2003), and HD 147513 (Mayor et al. 2004), in which Jupiter-like companions have been discovered in long-period orbits. However, the residuals of the 1-Keplerian fits are either relatively large or we see “suspicious” scatter of the residuals. We use the available measurements to test a hypothesis that additional short-period planets exist in these systems and their signals may be already hidden in the existing data, but are very likely at the detection limit. Our reasoning follows the theoretical predictions that Neptune-like planets can form easily and survive close to the parent star.

The main difficulty is a small number of measurements, typically of about 30–40 data points spread over several years. It makes it very difficult to determine orbits of such planetary candidates without any doubt. In particular, this concerns the identification of the orbital periods with the application of traditional Fourier-based analysis. Instead, we prefer a global search for the best-fit 2-planet configurations using the genetic algorithms and scanning $(\chi^2_\nu)^{1/2}$ in the multidimensional space of orbital parameters. This could be an alternative to the already classic Lomb-Scargle periodogram (e.g., Butler et al. 2004) or sophisticated Bayesian-based analysis, which has recently been proposed by Gregory (2005a,b). That author claims evidence of additional planets using the same RV measurements as are modeled by 1-planet configurations by the discovery teams, around HD 73526 and HD 208487.

2. The fitting algorithm, numerical setup and tests

In all cases studied in this paper, we assume that the second, putative planet is closer to the star than the already known companion b in a relatively long-period orbit. To model the RV signal, we use the standard formulae (e.g., Smart 1949). For every planet, the contribution to the reflex motion of the star at time $t$ is the following:

$$V(t) = K[\cos(\omega + \nu(t)) + e \cos \omega] + V_0,$$

where $K$ is the semi-amplitude, $\omega$ the argument of pericenter, $\nu(t)$ the true anomaly involving implicit dependence on the orbital period $P$ and the time of periastron passage $T_p$, $e$ the eccentricity, and $V_0$ is the velocity offset. Some argue that it is best to interpret the derived fit parameters $(K, P, e, \omega, T_p)$ in terms of Keplerian elements and minimal masses related to Jacobi coordinates (Lee & Peale 2003; Goździewski et al. 2003).

To search for the best-fit solutions, we apply a kind of hybrid optimization. A single program run starts the genetic algorithms (GAs) optimization. In particular, we use the PIKAIA code by Charbonneau (1995). The GAs has many advantages over more popular gradient-type algorithms, such as the Levenberg-Marquardt scheme (Press et al. 1992). The power of GAs lies in their global nature, the requirement of knowing only the $(\chi^2_\nu)^{1/2}$ function, and the ease of constrained optimization. In particular, GAs permit defining parameter bounds or adding a penalty term to $(\chi^2_\nu)^{1/2}$ (Goździewski et al. 2003, 2005).

In our code, the initial population of randomly chosen 2048 members represents potential solutions to the RV model. The code produces 128 new off-spring generations. The best fit found by PIKAIA is refined by the simplex algorithm of Melder and Nead (Press et al. 1992). In that method, we set the fractional tolerance for $(\chi^2_\nu)^{1/2}$ variability to $10^{-15}$. Such a procedure runs thousands of times for each analyzed data set. Thanks to the non-gradient character of both algorithms we may bound the space of examined parameters, according to specific requirements. Usually, due to a small number of measurements, the best-fit $e_\nu$ is barely constrained, and tends to be large, in particular in the range of very short periods. Nevertheless, we assumed that the tidal circularization limits the eccentricity of the short-period orbit, and we arbitrarily set its upper bound to 0.3. The orbital periods of putative planets are searched in the range of [2,136] d.

The internal errors of the RV data are rescaled according to $\sigma^2 = \sigma^2_m + \sigma^2_\nu$, where $\sigma$ is the joint uncertainty, $\sigma_m$ and $\sigma_\nu$ is the internal error and adopted variance of stellar jitter, respectively. Typically, we choose $\sigma_\nu$ following estimates for Sun-like dwarfs (Wright 2005), or we set its value as quoted by the discovery teams. The particular estimates are given in Table 1.

The best fits found in the entire hybrid search are illustrated by projections onto planes of particular parameters of the RV model, Eq. (1). Usually, we choose the $(P, K)$- and $(P, e)$-planes. Marking the elements within the formal 1$\sigma$, 2$\sigma$, 3$\sigma$ confidence intervals of the best-fit solution (always marked in the maps by two crossing lines), we have a convenient way of visualizing the shape of the local minima of $(\chi^2_\nu)^{1/2}$ and obtaining reasonable estimates of the fit errors (Bevington & Robinson 2003).

Still, even we find very good best-fit configurations, a problem persists: is the obtained fit not an artifact caused by a specific time-distribution of measurements or by the stellar jitter? In order to answer this question, we apply the test of scrambled velocities (Butler et al. 2004). We remove the synthetic RV contribution of the first confirmed planet from the RV data, according to its best-fit parameters. Next, the residuals are
randomly scrambled, keeping the exact moments of observations, and we search for the best-fit elements of the second (usually, inner) planet. For an uncorrelated residual signal, we should get close to the Gaussian distribution of \( \chi_p^2 \). For each synthetic data set, the minimization is performed with the hybrid method. Let us note that in this case, we are dealing with 1-planet model (and 6 parameters only), so the large population of the GA step and precise simplex code assure that the best-fit solution can be reliably found in one single run of the hybrid code. The runs of the code are repeated at least 20,000 times for every analyzed data set. If the best fit corresponding to the real (not scrambled) data lies on the edge of this distribution, such an experiment assures us that the real data produce much smaller \( \chi_p^2 \) than the most frequent outcomes obtained for the scrambled data. Such a test provides a reliable indication that the residuals are not randomly distributed. A likelihood \( p_{\text{H}} \) that the residuals are only white noise can be measured by the ratio of the best fits with \( \chi_p^2 \) less or equal to the one corresponding to the real data against all possible solutions.

Unfortunately, even with a positive outcome of the test of scrambled residuals, we still are not done. Even if we find a strong indication that the residuals are not randomly distributed, and find a periodic component in the residual signal, then we still cannot be sure that it has a planetary origin, and it does not eliminate jitter as a source of the RV signal. This is the main reason why our work cannot be considered in terms of a discovery paper; additional measurements and analysis are required to confirm (or withdraw) the hypothesis about the planetary nature of the RV variability. Our basic goal is to test the approach on a few non-trivial and representative examples. We try to find characteristics of the RV data sets to confirm the periodogram-based approach (e.g., Butler et al. 2004) and, possibly, these may be helpful to extend its results. Our analysis may be useful to speedup the detections of new planets and in planning the strategy of future observations.

### 2.1. Test case I: HD 208487

The first test case of HD 208487 (Tinney et al. 2005) illustrates the nuances of modeling the RV data. The observational window of this star spans about 2500 d, but the number of data points is only 31. The discovery team found a planetary companion with minimal mass of 0.7 \( m_1 \) and orbital period of about 130 d. An rms of this 1-planet solution is \( \sim 7 \) m/s, while the joint uncertainty is about 6 m/s, assuming a jitter estimate of 3 m/s, a reasonable value for the quiet, 6 Gyr old star with log \( R'_{\text{HK}} \approx -4.90 \) (Tinney et al. 2005). The data have been reanalyzed by Gregory (2005a), who applies his Bayes-periodogram method and finds much better 2-planet solution, explaining the residual signal of the 1-planet solution by the presence of a distant, second companion in a 998 d orbit. This solution has significantly better rms of 4.2 m/s and \( \chi_p^2 \approx 0.83 \) than the best single planet solution, \( \chi_p^2 \approx 1.27 \).

This analysis of the HD 208487 data is a good reference for our simpler approach. First we did the hybrid search for the best 2-planet configurations, assuming that 130 d < \( P_e < 1200 \) d. The results of this search are illustrated in Fig. 1. Curiously, the best-fit has \( \chi_p^2 \approx 0.62 \) and an rms \( \approx 3.1 \) m/s, so it is apparently better than the fit quoted by Gregory (2005a). The best-fit parameters \( (K, P, e, \omega, T_p - T_0) \) are: (17.532 m/s, 129.224 d, 0.195, 188.232, 1421.112 d) and (13.117 m/s, 997.953 d, 0.433, 190.470, 2358.258 d) for the inner and outer planet, respectively, \( (T_0 = \text{JD} 2450000) \).

Table 1. Primary parameters of the model in Eq. (1) and the inferred elements of the best-fits found in this paper. \( T_0 \) is JD 2450000. See the text and figures for error estimates.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>HD 158015</th>
<th>HD 114729</th>
<th>HD 147513</th>
<th>HD 190360</th>
<th>HD 208487</th>
</tr>
</thead>
<tbody>
<tr>
<td>( M_p ) [( M_\odot )]</td>
<td>1.08</td>
<td>0.93</td>
<td>1.11</td>
<td>0.95</td>
<td>0.96</td>
</tr>
<tr>
<td>( m \sin i ) [( M_\odot )]</td>
<td>0.074</td>
<td>1.76</td>
<td>0.064</td>
<td>0.84</td>
<td>0.110</td>
</tr>
<tr>
<td>( a ) [AU]</td>
<td>0.08</td>
<td>1.22</td>
<td>0.11</td>
<td>2.12</td>
<td>0.08</td>
</tr>
<tr>
<td>( P ) [d]</td>
<td>8.389</td>
<td>476.23</td>
<td>13.849</td>
<td>1171.19</td>
<td>7.894</td>
</tr>
<tr>
<td>( K ) [m/s]</td>
<td>7.21</td>
<td>44.75</td>
<td>5.87</td>
<td>17.71</td>
<td>10.95</td>
</tr>
<tr>
<td>( e )</td>
<td>0.23</td>
<td>0.24</td>
<td>0.25</td>
<td>0.30</td>
<td>0.30</td>
</tr>
<tr>
<td>( \omega ) [deg]</td>
<td>103.9</td>
<td>242.4</td>
<td>301.1</td>
<td>66.3</td>
<td>9.1</td>
</tr>
<tr>
<td>( T_p [\text{JD-2450000}] )</td>
<td>859.67</td>
<td>2270.10</td>
<td>2496.77</td>
<td>1558.98</td>
<td>1047.23</td>
</tr>
<tr>
<td>( \chi_p^2 / 2 )</td>
<td>1.021</td>
<td>0.775</td>
<td>0.505</td>
<td>0.680</td>
<td>0.581</td>
</tr>
<tr>
<td>( \sigma_p ) [m/s]</td>
<td>4.0</td>
<td>4.0</td>
<td>9.0</td>
<td>3.1</td>
<td>3.0</td>
</tr>
<tr>
<td>( \sigma_p^2 + \sigma_r^2 ) [m/s]</td>
<td>4.1</td>
<td>3.5</td>
<td>4.4</td>
<td>2.2</td>
<td>5.4</td>
</tr>
<tr>
<td>rms [m/s]</td>
<td>5.7</td>
<td>5.3</td>
<td>10</td>
<td>3.8</td>
<td>6.2</td>
</tr>
<tr>
<td>( V_0 [\text{m/s}] )</td>
<td>4.93</td>
<td>3.59</td>
<td>4.07</td>
<td>2.97</td>
<td>2.82</td>
</tr>
</tbody>
</table>
and $V_0 = 9.64$ m/s. Note the much larger eccentricity of the outer planet than in the fit by Gregory (2005a), $e_c \approx 0.2$. The 1σ scatter of the derived solutions around the best-fit (Fig. 1) provides the error estimate of the orbital elements. In general, the parameters of the inner planet are well fixed, while the elements of the outer body have much larger formal uncertainties. The errors of $K_c, P_c, e_c$ are about 100 d, 0.3, and 10 m/s, respectively.

Next, we explored the inner space to the ∼130 d orbit, assuming $2 < P_c < 130$. Surprisingly, we found an even better fit, given in Table 1, with $\chi^2_{\nu}^{1/2}\approx 0.581$ and an rms ≈ 2.82 m/s. The orbital elements of the best-fit solutions found in the entire search are projected onto the parameter planes and illustrated in Fig. 2. Note a small scatter of the elements of the outer planet and two sharp minima in $P_c$. The best-fit has $P_c \approx 14.5$ d and $e_c \approx 0.42$. Such large eccentricity may

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**Fig. 1.** The parameters of the best-fit solutions to the 2-planet model of the HD 208487 RV data projected onto the ($P, e$) - and ($P, K$) -plane. In this search, a more distant companion to the formerly known Jupiter-like body in ∼130 d orbit is assumed. Upper plots are for the inner planet, lower plots for the outer companion. The values of $\chi^2_{\nu}^{1/2}$ of the best-fit solutions are marked by the size of symbols. The largest circle is for $\chi^2_{\nu}^{1/2}$ equal to 0.619; smaller symbols are for 1σ solutions with $\chi^2_{\nu}^{1/2} \in [0.619, 0.710]$, 2σ solutions with $\chi^2_{\nu}^{1/2} \in [0.710, 0.841]$, and 3σ solutions with $\chi^2_{\nu}^{1/2} \in [0.841, 1.0]$ (smallest, filled circles), respectively.

**Fig. 2.** The parameters of the best-fit solutions to the 2-planet model of the HD 208487 RV data projected onto the ($P, e$) - and ($P, K$) -plane. In this search, an inner companion to the formerly known Jupiter-like body in ∼130 d orbit is assumed. Upper plots are for the outer planet, lower plots for the inner companion. The values of $\chi^2_{\nu}^{1/2}$ of the best-fit solutions are marked by the size of symbols. The largest circle is for $\chi^2_{\nu}^{1/2} = 0.581$ (the best-fit solution, Table 1); smaller symbols are for solutions within 1σ interval of the best-fit with $\chi^2_{\nu}^{1/2} \in [0.581, 0.677]$, 2σ solutions with $\chi^2_{\nu}^{1/2} \in [0.677, 0.813]$, and 3σ solutions with $\chi^2_{\nu}^{1/2} \in [0.813, 0.98]$ (smallest, filled circles), respectively.
Fig. 3. Stability analysis of the orbital fit with putative Neptune-like body in the HD 208487 system. The upper panel is for the eccentricities, the lower panel for MEGNO computed for $3 \times 10^5$ orbital periods of the outer companion.

contradict the requirement of a tidally circularized orbit. However, the orbital evolution of the whole system reveals large-amplitude variations of $e_c$ (Fig. 3), which are forced by the mutual interactions between companions. We also face another problem with a small periastron-apoastron distance of the two putative planets $\sim 0.2$ AU. Nevertheless, the system appears to be dynamically stable. The evolution of the MEGNO indicator (Goździewski et al. 2001) computed over $3 \times 10^5 P_b$ is illustrated in the lower panel of Fig. 3. Its oscillations of about 2 mean a quasi-periodic configuration and strictly confirm apparently regular behavior of $e_{b,c}$.

For a reference, we computed the Lomb-Scargle periodogram (Fig. 4) of the residuals of the dominant 1-planet signal having a period of 130 d. The largest peaks of about 28 d and 998 d (the period of a hypothetic long-period planet) most possibly are aliasing with the best-fit period $=14.5$ d. However, this period is favored by the smallest $\sqrt{\chi^2_{\nu}}$. The aliasing of the two dominant periods is illustrated in Fig. 5. This figure shows the synthetic RV signals of the putative configurations with the short- and long-period companions of planet b. Curiously, the orbital periods of the two planets in the model with the short-period orbit are very close to the 9:1 ratio. This again could be an effect of aliasing; the best-fit solution for single planet with $P_b$ about 14.5 d has much larger rms $\sim 9.7$ m/s than in the best 2-planet solution.

Some more interesting results provides the test of scrambled residuals, Fig. 6. It appears that the real residual signal lies far from the maximum of the Gaussian-like distribution, and it is unlikely that the residuals are only a white noise ($p_H \approx 3 \times 10^{-5}$). Also $K_b \approx 10.5$ m/s is much larger than the joint uncertainty of the measurements. Because HD 208487 is a very old and quiet G-dwarf with low chromospheric activity (Tinney et al. 2005), the hypothesis of a hot sub-Neptune planet in this extrasolar system seems very appealing.

Fig. 6. A histogram of $\sqrt{\chi^2}$ for Keplerian fits to 33 000 sets of scrambled RV residuals of the synthetic signal of the Jupiter-like planet in $\sim 130$ d orbit (HD 208487, see Table 1). The position of the best fit to the real data is marked with an arrow.
system could be its proximity to the 9:1 mean motion resonance of its companions.

2.2. Test case II: HD 190360

In a recent paper, Vogt et al. (2005) published the precision RV data for HD 190360. The variability of the RV is explained by the existence of two planetary companions: a Jupiter-like planet in long-period orbit, \( P_b \sim 3000 \) d, and a Neptune-like body in \( \sim 17.1 \) d orbit. The authors conclude that the existence of the smaller planet is the best explanation for the residual signal of the single-planet solution. Its contribution has small semi-amplitude \( K \approx 4.6 \) m/s. Yet the orbital period is about a half of the rotational period of the star, 36–44 d, and the RV variability may be an effect of spot complexes on the stellar surface (Vogt et al. 2005).
Fig. 10. The parameters of the best-fit solutions to the 2-planet model of the RV data of HD 190360 limited to the first 38 measurements, projected onto the \((P,e)-(P,K)\)-plane. Upper plots are for the outer planet, lower plots for the inner companion. The values of \((\chi^2/\nu)_{1/2}\) of the best-fit solutions are marked by the size of symbols. The largest circle is for \((\chi^2/\nu)_{1/2} \approx 0.733\); smaller symbols are for 1\(\sigma\) solutions with \((\chi^2/\nu)_{1/2} \in [0.733,0.793]\), 2\(\sigma\) solutions with \((\chi^2/\nu)_{1/2} \in [0.793,0.89]\), and 3\(\sigma\) solutions with \((\chi^2/\nu)_{1/2} \in [0.89,1.00]\) (smallest, filled circles), respectively. Vertical and horizontal lines mark the best-fit obtained for the full data (see Fig. 7 and Table 1).

Fig. 11. Lomb-Scargle periodogram of the residuals of the long-period signal in HD 190360 when only 38 first measurements are analyzed. Compare with Fig. 8 for the full data set.

The elements of a few hundred fits gathered by the hybrid search are illustrated in Fig. 7 (the elements of the best-fit are given in Table 1). The period of the inner planet corresponds to a single, very deep minimum of \((\chi^2/\nu)_{1/2}\). It is clear that \(e_c\) has a large error \(\approx 0.15\). Our fit is slightly better than the one quoted by Vogt et al. (2005), but \(e_c \approx 0.2\) is also different, and we have got slightly larger \(K_c \approx 5.2\) m/s. Note that we obtain similar uncertainties of 100 d for \(K_b\) and of 0.05 for \(e_b\).

The Lomb-Scargle periodogram (Fig. 8) of the residuals of the long-period orbit reveals a strong, dominant peak at 17.1 d. This an excellent confirmation of the results of the hybrid search. The test of scrambled residuals reveals that the residual signal is hardly random. The maximum of \((\chi^2/\nu)_{1/2}\) for scrambled data is shifted by \(\approx 0.4\) from the value of \((\chi^2/\nu)_{1/2}\) for the real data.
Fig. 13. The best-fit solutions to the RV data published by Marcy et al. (2005b) for HD 188015. a) The 1-Kepler model with a linear trend that is apparently present in the data. b) The 2-Kepler model is consistent with the measurement error, \( \chi^2_{\nu}^{1/2} \approx 1.02 \), rms \( \approx 4.9 \) m/s. c) Period-phased RV signal of the inner companion. d) A close-up of the synthetic signal of the best-fit 2-planet configuration (see Table 1).

Fig. 14. The elements of the best-fit solutions to the 2-planet model of the HD 188015 RV data projected onto the \((P, e)\)- and \((P, K)\)-plane. Upper plots are for the outer planet, lower plots for the inner companion. The \( \chi^2_{\nu}^{1/2} \) of the best-fit solutions are marked by the size of symbols. The largest circle is for \( \chi^2_{\nu}^{1/2} = 1.021 \) (the best-fit solution, Table 1); smaller symbols are for 1\( \sigma \) solutions with \( \chi^2_{\nu}^{1/2} \in [1.02, 1.07] \), 2\( \sigma \) solutions with \( \chi^2_{\nu}^{1/2} \in [1.07, 1.14] \), and 3\( \sigma \) solutions with \( \chi^2_{\nu}^{1/2} \in [1.14, 1.25] \) (smallest, filled circles), respectively.

Now, with such a clear picture, we analyze a smaller sample of measurements. To perform this test, we selected 38 first measurements spanning \( \sim 2200 \) d. The number of data points and their time-coverage are similar to other cases studied in this work. The procedure described above was repeated on such a synthetic data set.
3. HD 188015

Recently, Marcy et al. (2005b) published the precision RV of HD 188015. The variability of the RV is explained by the presence of a planetary companion with minimal mass 1.26 $m_\oplus$ and orbital period $\sim$ 1.25 yr. Our attention has been drawn to the relatively large rms of this 1-planet solution, $\sim$8.6 m/s. The mean error of the RV data is about 4.1 m/s and expected stellar jitter is $\sim$4 m/s (Marcy et al. 2005b). The mean measurement error added in quadrature to the jitter is about 5 m/s, still much smaller than the rms of 1-planet solution. However, this can be partially explained by a linear trend apparently present in the RV signal. If one adds such a trend to the fit model, the rms goes down by 1 m/s (Marcy et al. 2005b, also our Fig. 13a). The trends in the RV data frequently indicate a distant body (e.g., Marcy et al. 2005a; Jones et al. 2002; Goździewski et al. 2003). Nevertheless, we assumed that the second putative body is not a distant companion, but rather a planet closer to the star than the already detected companion b.

The elements of the best-fit solution found in the entire hybrid search are illustrated in Fig. 13 (panels b, c, d) and its elements given in Table 1. The synthetic Doppler signal is plotted over the data points in Fig. 13b. Surprisingly, the apparent slope of the RV data can only be an artifact related to a specific time-distribution of measurements. The value of $(\chi^2)^{1/2}$ $\sim$ 1.021 indicates a statistically good solution. Its rms is about 5 m/s, consistent with the adopted estimate of the mean uncertainty. The semi-amplitude of the inner planet signal is about 0.07 $m_\oplus$, and the mass of the host star $M_\ast$ is about 1.08 $M_\odot$ (Marcy et al. 2005b), we derived its minimal mass as about 0.07 $m_\oplus$ and the semi-major axis of about 0.08 AU. Thus, the new putative object can be classified as a hot-Neptune planet.

According to the 1σ-level of $(\chi^2)^{1/2}$, it is clear that the eccentricity of the inner companion (also its argument of periastron – not shown here) cannot be fixed well. A local minimum at $P_\text{c}$ $\approx$ 15.37 d that also models the observations (at the 1σ confidence interval of the best-fit solution) well, may correspond to an alias of the best-fit period 8.386 d. It could also be an alias for the rotational period $\sim$ 30 d of the star, assuming that it is smaller than the 36 d estimate by Marcy et al. (2005b). Indeed, there is a minimum of $(\chi^2)^{1/2}$ at the 1σ-level of the best-fit about 30 d and $e_\text{c}$ $\approx$ 0.3, see Fig. 14.

The results of the hybrid search agree perfectly with the Lomb-Scargle periodogram (Fig. 15) of the signal after removal of the contribution from the outer planet. All the relevant periods can be found in the periodogram, too. This assures us that the GAs search is robust in locating the best-fit solution even in the case when $(\chi^2)^{1/2}$ has several equally deep local minima. Additionally, we did an independent gradient-based scan over $P_\text{c}$, which test also confirmed the excellent performance of the GAs.

The test of scrambled velocities illustrated in Fig. 16 helps us to explain the difficulty of finding a clear, secondly
dominant short-period in the data. The histogram of \((\chi^2)^{1/2}\) has its maximum at about 1.1, and \((\chi^2)^{1/2} \approx 0.93\) of the real residuals is not separated well from this maximum. The estimated \(p_H \approx 0.03\) is significant and indicates that the residual signal is rather noisy, yet the best 2-planet fit improves the 1-planet solution substantially.

We were warned by the referee (and we quote her/him again here) that the jitter estimate by Marcy et al. (2005b) comes...
Similar to most of the stars monitored in precision RV surveys, the HD 114729 is a Sun-like star of G3V spectral type (GOV by Hipparcos). Its RV data indicate a Jupiter-like companion with minimal mass 0.84 $M_J$, orbital period =3.1 yr, and eccentricity =0.32 (Butler et al. 2003). An rms of the single Keplerian fit to the data is 5.34 m/s. It is larger than the mean of internal errors, =3.6 m/s. The expected jitter is 4 m/s (Butler et al. 2003). The mean measurement error scaled in quadrature with the jitter variance is comparable to the rms. Nevertheless, having in mind a significant scatter of the measurements around some parts of the synthetic 1-planet RV curve (see Fig. 17a), and the presence of the distant giant planet, we assumed (as in the previous case) that one more planet exists in the system with a short-period orbit of [2,136] d. To test this hypothesis, we make the same analysis of the RV data as described in previous sections. The results are illustrated in Figs. 17a–d, which is the graphical illustration of the best fit parameters. Figure 18 is for the Lomb-Scargle periodogram of the residual signal of the long-period companion, while Fig. 19 illustrates the shape of $(\chi^2)^{1/2}$ for the best-fit and the distribution of the best fits obtained in the hybrid search. The orbital parameters of the best fit are given in Table 1. Clearly, the results of the hybrid search agree perfectly with the Lomb-Scargle periodogram – the dominant peak of about 7 d is clearly visible in the $(P_e, e)$-plane as the deepest minimum of $(\chi^2)^{1/2}$ in the region of short periods. The best-fit eccentricity of the inner planet is found close to the assumed limit of 0.3. However, in a few tests with smaller jitter (~3 m/s) we obtained a better bounded minimum of $(\chi^2)^{1/2}$ and smaller best-fit $e_c = 0.2$, so this element is barely constrained by the RV data. An inspection of the Lomb-Scargle periodogram shows some other relatively strong peaks, for instance of about 180 d, which most likely are aliasing with a period of 13.844 d. The histogram of $(\chi^2)^{1/2}$ (Fig. 20) is obtained for scrambled residuals of the outer planet signal. The probability that the residual signal of the outer companion has a random origin is very small, $p_H \approx 0.003$. The $(\chi^2)^{1/2}$ for the best fit solution has a well defined minimum of about 0.71. Its rms of ~3.6 m/s is very close to the mean of the internal errors. Assuming that the mass of the host star is equal to 0.93 $M_\odot$, the derived minimal mass of the inner planet is about 0.065 $M_J$ and its semi-major axis =0.11 AU. Thus it would correspond to a hot Neptune-like planet.

5. HD 147513

The last example that we examine is HD 147513. This star was observed by Mayor et al. (2004), who published 30 measurements covering 1690 d. In this case, an rms of 5.7 m/s of the 1-planet fit is comparable to the mean of measurement errors; nevertheless, our attention is drawn to an irregular scatter of the measurements around the synthetic RV curve (see Fig. 22a). The discovery team announced a Jupiter-like planet of minimal mass 1.21 $M_J$ in a =528 d orbit. The host star is very active ($\log R'_{\text{HK}} = -4.4$). Following Wright (2005) we estimate its jitter as ~9 m/s.
Fig. 21. The projections of best-fit parameters to the 2-planet model of the HD 147513 RV data onto the $(P,e)$- and $(P,K)$-plane. Upper plots are for the outer planet, lower ones are for the inner companion. The values of $(\chi^2_\nu)^{1/2}$ for the best-fit solutions are marked by the size of symbols. The largest circle is for $(\chi^2_\nu)^{1/2} \approx 0.505$ (the best-fit solution, Table 1); smaller symbols are for $1\sigma$ solutions with $(\chi^2_\nu)^{1/2} \in [0.505, 0.619]$, $2\sigma$ solutions with $(\chi^2_\nu)^{1/2} \in [0.62, 0.773]$, and $3\sigma$ solutions with $(\chi^2_\nu)^{1/2} \in [0.773, 0.95]$ (smallest, filled circles), respectively.

Fig. 22. The best-fit solutions to the RV data published in (Mayor et al. 2004) for HD 147513. a) 1-planet model. The thick line is for the fit found with GA, assuming $\sigma_j = 9$ m/s; its parameters $(K, P, e, T_p - T_0)$ are: $(28.40\text{ m/s}, 520, 49\text{ d}, 0.346, 288.57, 3125.302\text{ d}), T_0 = \text{JD 2450000}, (\chi^2_\nu)^{1/2} = 0.737$, an rms $= 6.83$ m/s. The thin line is for the fit without accounting for the jitter; its parameters are almost the same as in Mayor et al. (2004): $(29.312\text{ m/s}, 528.112\text{ d}, 0.260, 282.453, 2214.94\text{ d}), (\chi^2_\nu)^{1/2} = 1.60$, an rms $= 7.26$ m/s. b) The 2-Kepler model is consistent with the measurement errors, $(\chi^2_\nu)^{1/2} \approx 0.505$, an rms $\approx 4.1$ m/s. c) Period-phased RV signal of the inner companion. d) A close-up of the synthetic signal of the best-fit 2-planet configuration, Table 1.
\(\chi^2\) for Keplerian fits to 30,000 sets of scrambled residuals. The residual signal has a planetary origin is always very risky. To confirm the existence of the putative hot-Neptune candidates, a deep astrophysical analysis is necessary (Mayor & Queloz 1995; Santos et al. 2003; Butler et al. 2004), far beyond our technical abilities. That includes many additional spectroscopic and photometric observations. Nevertheless, the dynamical environment of the putative new planetary companions, several recent discoveries of Neptune-like planets, and cosmogonic theories supporting their origin, all permit us to state and investigate a hypothesis of the planetary nature of the RV variability.

Our results may be useful in some aspects. Even if the residual periodicities are of pure stellar origin, accounting for them may improve the single planet fits, because it makes it possible to remove a contribution of a non-random RV signal from the data. When we deal with a small number of measurements, the short-term contribution of jitter does not average out, and it alters the long-period solution. Yet the stellar variations may have an origin in planetary-induced activity. This effect has been analyzed by Santos et al. (2000, 2003). An elimination of the planetary hypothesis also requires additional observations and analysis.

Basically, we used an independent, FFT-free method for the global analysis of the RV data and early detection of plausible planets. It can be used for checking the results of 1-dim periodogram-based analysis, extending it into the multidimensional space of the orbital elements. If some of our results are confirmed, a similar approach can be used to detect smaller bodies in short-period orbits in the other, already discovered extrasolar systems. Such studies can be useful for planning future observing sessions.

We did a similar but very preliminary analysis of the RV observations of a few other stars hosting single Jupiter-like planets. For instance, we found a short-term variability of the RV, about 7 d in the HD 19994 system (Mayor et al. 2004). The second companion would have \(K \sim 9\) m/s, larger than the mean uncertainty of measurements, about 6.6 m/s. In the same paper, we found the RV data of HD 121504 and a curious RV variability that may be well modeled by a new 2-planet system close to the 6:1 mean motion resonance. Probably, the data collected and published by Doppler planet searches already conceal many interesting and unusual planetary configurations.

Fig. 23. Lomb-Scargle periodogram of the residuals of the long-period signal visible in the RV data of HD 147513.

Fig. 24. A histogram of \((\chi^2)^{1/2}\) for Keplerian fits to 30,000 sets of scrambled RV residuals of the synthetic signal of the outer planet in the HD 147513 planetary system (Table 1). The position of the best-fit to the real data is marked with an arrow.

We searched for the second planet in a short-period orbit of \([2,136]\) d. The results of the hybrid search obtained for 2-planet fits are illustrated in Fig. 21 for the statistics of the gathered best-fits and in Figs. 22a–d for the graphical illustration of the best-fit solution. These results remind us of the HD 190360 case. The \((\chi^2)^{1/2}\) of the best-fit has a well defined minimum at \(P_c \approx 7.894\) d. Its rms \(\approx 4.1\) m/s means a significant improvement in the single-planet fit. This is seen in Figs. 22b,d; apparently the synthetic RV curve is ideally close to the measurements. A relatively large \(K_e \sim 11\) m/s and mass of the host star \(1.11 M_\odot\) imply that the minimal mass of the inner planet is \(0.115 m_\oplus\) and the semi-major axis about \(0.08\) AU.

The Lomb-Scargle periodogram, Fig. 23, reveals features that recall the first system examined in this paper, around HD 208487. The short period of \(\approx 7.9\) d seems to be aliased with a much longer period of \(810.8\) d. Figure 24 shows the histogram of \((\chi^2)^{1/2}\) computed for the scrambled residuals. The probability of a random character for the residual signal is negligible. At this time, such a characteristic is almost the same as for the HD 190360 system; in that case the 2-planet solution also produces very small rms, which is less than the joint measurement uncertainty.

Mostly due to the activity of the star, the periodicity of the RV variations can still be explained by jitter. According to Mayor et al. (2004), HD 147513 is a young G3/5V dwarf, only 0.3 Gyr old. Its spectrum reveals a strong emission in the Ca II H line. Although the estimated short rotation period of the host star, about 4.7 d (Mayor et al. 2004), differs from the secondary period visible in the RV signal (about 7.9 d), it is suspiciously close to this approximation. However, such coincidence of periods still does not exclude a planetary explanation (Santos et al. 2000, 2003), because the activity can be induced or amplified by a relatively massive and close planetary companion.

6. Conclusions

It is extremely difficult to interpret the RV measurements when their number is limited and their time coverage is poor. We are looking for signals that have an amplitude that is comparable to noise. Although it is already possible to pick up some promising extrasolar systems in which one planet is clearly visible and another putative body is at the detection limit, a claim that the residual signal has a planetary origin is always very risky. To confirm the existence of the putative hot-Neptune candidates, a deep astrophysical analysis is necessary (Mayor & Queloz 1995; Santos et al. 2003; Butler et al. 2004), far beyond our technical abilities. That includes many additional spectroscopic and photometric observations. Nevertheless, the dynamical environment of the putative new planetary companions, several recent discoveries of Neptune-like planets, and cosmogonic theories supporting their origin, all permit us to state and investigate a hypothesis of the planetary nature of the RV variability.

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