

Some empirical estimates of the H₂ formation rate in photon-dominated regions

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Abstract. We combine recent ISO observations of the vibrational ground state lines of H₂ towards Photon-Dominated Regions (PDRs) with observations of vibrationally excited states made with ground-based telescopes in order to constrain the formation rate of H₂ on grain surfaces under the physical conditions in the layers responsible for H₂ emission. We briefly review the data available for five nearby PDRs. We use steady state PDR models in order to examine the sensitivity of different H₂ line ratios to the H₂ formation rate R_f . We show that the ratio of the 0–0 S(3) to the 1–0 S(1) line increases with R_f but that one requires independent estimates of the radiation field incident upon the PDR and the density in order to infer R_f from the H₂ line data. We confirm earlier work by Habart et al. (2003) on the Oph W PDR which showed that an H₂ formation rate higher than the standard value of $3 \times 10^{-17} \text{ cm}^3 \text{ s}^{-1}$ inferred from UV observations of diffuse clouds is needed to explain the observed H₂ excitation. From comparison of the ISO and ground-based data, we find that moderately excited PDRs such as Oph W, S140 and IC 63 require an H₂ formation rate of about five times the standard value whereas the data for PDRs with a higher incident radiation field such as NGC 2023 and the Orion Bar can be explained with the standard value of R_f . We compare also the H₂ 1–0 S(1) line intensities with the emission in PAH features and find a rough scaling of the ratio of these quantities with the ratio of local density to radiation field. This suggests but does not prove that formation of H₂ on PAHs is important in PDRs. We also consider some empirical models of the H₂ formation process with the aim of explaining these results. Here we consider both formation on classical grains of size roughly $0.1 \mu\text{m}$ and on very small ($\sim 10 \text{ \AA}$) grains by either direct recombination from the gas phase (Eley–Rideal mechanism) or recombination of physisorbed H atoms with atoms in a chemisorbed site. We conclude that indirect chemisorption where a physisorbed H-atom scans the grain surface before recombining with a chemisorbed H-atom is most promising in PDRs. Moreover small grains which dominate the total grain surface and spend most of their time at relatively low (below 30 K for $\chi \leq 3000$) temperatures may be the most promising surface for forming H₂ in PDRs.

Key words. ISM: clouds – ISM: dust, extinction – atomic processes – molecular processes – radiative transfer

1. Introduction

The formation of molecular hydrogen is a key process affecting the thermal and density structure and the chemical evolution of the interstellar medium (see, for example, Combes & Pineau des Forêts 2000). Although there is a consensus that H₂ forms on the surface of dust grains (Gould & Salpeter 1963; Hollenbach & Salpeter 1971; Jura 1975; Duley & Williams 1984), the mechanism is not yet understood. This is partly due to our ignorance concerning interstellar grain composition, form, structure and physico-chemical state. It is also caused by our lack of understanding of surface reactions in the interstellar context.

Numerous theoretical and experimental studies have thus been dedicated to the study of the H₂ formation process (Sandford & Allamandola 1993; Duley 1996; Parneix & Brechignac 1998; Pirronello et al. 1997, 1999; Takahashi et al. 1999; Katz et al. 1999; Williams et al. 2000; Sidis et al. 2000;

Biham et al. 2001; Joblin et al. 2001; Cazaux & Tielens 2002, 2003). Another approach to this issue is to examine the H₂ formation rate in different regions of the ISM in order to see how it depends upon the local physical parameters. One can for example study the correlation of H₂-related quantities (abundance, rotational excitation, vibrational excitation) with the local dust properties. ISO observations of H₂ lines and small carbonaceous grains emission in several PDRs, and new H₂ UV absorption observations by FUSE of diffuse clouds, open new perspectives on our understanding of the H₂ formation process. In particular, the confrontation between observations and theoretical predictions provides strong constraints upon the H₂ formation rate (Habart et al. 2003; Gry et al. 2002; Tumulinson et al. 2002).

In this paper, we consider PDRs and investigate the H₂ formation process using observations of H₂ emission obtained by ISO and ground-based telescopes. PDRs, where stellar radiation plays a dominant role in determining the chemical and thermal state of the gas (for a recent review see Hollenbach & Tielens 1999), are privileged objects for the study of physical

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and chemical processes of the interstellar medium. In Sect. 2, we review the data available for five nearby PDRs and summarize their physical conditions. In Sect. 3, we estimate for each PDR of our sample the H₂ formation rate using the H₂ line intensity ratios as a diagnostic. Also, in order to probe the influence of PAHs on the H₂ formation, we compare in Sect. 4 the intensities of emission measured in H₂ fluorescent lines with those in the aromatic bands. Then, with the aim of explaining these results, we consider in Sect. 5 empirical models of the H₂ formation mechanism by recombination of an H atom in a bound site with a second H atom which is either in the gas phase or on a neighbouring physisorbed site. In Sect. 6, we compare the observational constraints on the H₂ formation rate with different model predictions. Our conclusions are summarized in Sect. 7.

2. Sample of PDRs observed by ISO

Recently, the Short Wavelength Spectrometer (SWS, Kessler et al. 1996) on board ISO has observed a series of pure H₂ rotational lines towards a variety of nearby PDRs. In the ISO data base, we have selected five nearby PDRs which sample well the range of excitation conditions covered by the SWS observations. At the low excitation end, we have the Oph W and the S140 PDRs. Then, with radiation field higher by a factor of 3–10, we have the PDR IC 63 and the reflection nebula NGC 2023 (where we focus on the filament at 60'' south of the central star). Finally, at the high excitation end, we have the Orion Bar at the position of the peak of the fluorescent H₂ emission. These PDRs close to the Sun ($d \sim 100\text{--}500$ pc) are ideal targets to discuss the formation of H₂ in hot regions of the ISM.

In Table 1, we summarize the physical conditions prevailing in each region as determined from the literature. The thermal and chemical structure of the PDR depends on two parameters, namely, the intensity of the incident far-ultraviolet (FUV, $6 < h\nu < 13.6$ eV) radiation field and the gas density. We adopt the radiation field of Draine (1978) and we characterize its intensity with a scaling factor χ ($\chi = 1$ corresponds to the standard FUV interstellar radiation field of 2.6×10^{-3} erg s⁻¹ cm⁻²). This factor is determined from the expected FUV luminosity of the exciting star and assuming that the distance of the exciting star to the PDR is equal to the distance projected onto the sky. This in principle is an upper limit and hence we also report in Table 1 estimations of χ based on observations of the fine structure lines of C⁺ or O⁰. In general, we note that χ is uncertain by a factor of about 2 to 5.

The proton gas density n_{H} has been derived from a variety of observational constraints: (1) for Oph W, $n_{\text{H}} \sim 10^4$ cm⁻³ is estimated from the brightness profile of the aromatic dust emission (Habart et al. 2003), while observations in the C⁰ and CO lines suggest $n_{\text{H}} \sim 6 \times 10^4$ cm⁻³ for the inner part of the PDR (Habart 2001); (2) for S140, using [C⁺] 158 μm and C⁰ radio recombination line, Wyrowski et al. (1997b) derive a density about $n_{\text{H}} \sim 5 \times 10^4$ cm⁻³ comparable to the gas density expected for pressure balance with the HII region $\sim 10^4$ cm⁻³ (Timmermann et al. 1996); (3) measurements of CO, HCO⁺, HCN or CS line ratios from the PDR IC 63 suggest $n_{\text{H}} \sim 5 \times 10^4\text{--}10^5$ cm⁻³ (Jansen et al. 1994, 1995);

(4) for the bright southern emission bar of NGC 2023, the inferred densities are in the range $\sim 10^4\text{--}10^5$ cm⁻³ using H₂ fluorescent line emission (Black & van Dishoeck 1987; Draine & Bertoldi 1996; Field et al. 1998; Draine & Bertoldi 2000) and $\sim 10^5$ cm⁻³ from [C⁺] 158 μm and C radio recombination line intensity (Wyrowski et al. 1997b, 2000); (5) finally, for the Orion Bar the gas density has been estimated to be about $\sim 5 \times 10^4$ cm⁻³ from the observed stratification of different tracers of PDRs (Tielens et al. 1993) and $\geq 10^5$ cm⁻³ from observations of fine-structure line emission (Herrmann et al. 1997), as well as C radio recombination lines (Wyrowski et al. 1997a) and CN, CS observations (Simon et al. 1997). The gas density inferred from various atomic/molecular species shows a relatively large dispersion (typically from 10^4 to 10^5 cm⁻³). This dispersion could result from systematic density gradients from the H₂ emitting layer to the molecular cold layer (see, for example, Walmsley et al. 2000; Habart et al. 2003). What is needed for our study is the density in the H₂ emitting region while mainly the density tracers reflect the density of the cold gas in the cloud.

We report also in Table 1 the observed intensities for the H₂ 0–0 S(3) and 1–0 S(1) lines obtained respectively with ISO-SWS and from ground based observations. High spatial resolution observations ($\sim 1''$) of the 1–0 S(1) line emission have been smoothed to the $\sim 20''$ beam of SWS. For measurements made with beams larger than the SWS observations, we have scaled the flux according to the beam ratio. For each region, we also give the excitation temperature of the H₂ pure rotational levels with $J \leq 7$, the H₂ column density inferred from H₂ rotational lines intensity, and the 1–0 S(1)/2–1 S(1) line ratio. In the case of NGC 2023 and the Orion Bar, the 1–0 S(1)/2–1 S(1) line ratio has been taken respectively at 18''S 11''W (Burton et al. 1998) and 50''N 30''E (Walmsley et al. 2000) of the SWS pointings. Finally, based on ISOCAM observations¹, we give the aromatic dust emission smoothed to the SWS beam. In the following, aromatic dust particles will be hereafter referred to as PAHs (Polycyclic Aromatic Hydrocarbons). This is a generic term which encompasses large aromatic molecules and tiny carbonaceous dust grains containing up to a few 1000 atoms and with radii of a few Å to a few tens of Å.

3. Estimates of the H₂ formation rate

In this section, we show how the H₂ formation rate can be derived from the analysis of the H₂ emission line using PDR models.

For several PDRs observed by ISO, the H₂ line intensities and the gas temperature as probed by the populations of the low rotational levels of H₂ were found to be higher than predicted by current models (Bertoldi 1997; Draine & Bertoldi 1999; Thi et al. 1999; Habart et al. 2003; Li et al. 2002). The cause of this

¹ From the brightness in the LW2 filter (5–8.5 μm), which is dominated by the aromatic dust emission (Boulanger et al. 1998), we can estimate the aromatic dust emission using the following relationship: $I_{\text{PAH}}(2\text{--}15 \mu\text{m}) \simeq 2 \times \nu I_{\nu}(5\text{--}8.5 \mu\text{m})$ based on ISOCAM-CVF spectrum (corrected from the dust continuum emission) taken in PDRs.

Table 1. Sample of PDRs observed by ISO.

	Oph W	S140	IC 63	NGC 2023	Orion Bar
χ^a	250	100–250	650	500–3000	5000– 2.4×10^4
Ref.	(1a)	(2a)–(2b)	(3a)	(4a)–(4b)	(5a)–(5a, b)
n_{H}^b (cm ⁻³)	10 ⁴	10 ⁴ – 5×10^4	5×10^4 –10 ⁵	10 ⁴ –10 ⁵	5×10^4 – 3×10^5
Ref.	(1a)	(2b)–(2a)	(3a)	(4c)–(4a, b, d)	(5b, c, e)–(5e, f, g)
A_V^c (mag)	10	≥ 10	7	≥ 10	≥ 10
Ref.	(1b)	(2c)	(3a)	(4a)	(5h)

^a Incident FUV radiation field expressed in units χ of the Draine (1978) average interstellar radiation field.

^b Proton gas density $n_{\text{H}} \equiv n_{\text{H}^0} + 2 n_{\text{H}_2}$.

^c Visual extinction within the PDR inferred from sub-mm dust emission or CO observations.

References: (1a) Habart et al. (2003); (1b) Motte et al. (1998); (2a) Wyrowski et al. (1997b); (2b) Timmermann et al. (1996); (2c) Minchin et al. (1993); (3a) Jansen et al. (1994, 1995); (4a) Wyrowski et al. (1997b, 2000); (4b) Draine & Bertoldi (1996, 2000); (4c) Black & van Dishoeck (1987); (4d) Field et al. (1998); (5a) Marconi et al. (1998); (5b) Tielens & Hollenbach (1985); (5c) Tielens et al. (1993); (5d) Tauber et al. (1994); (5e) Wyrowski et al. (1997a); (5f) Herrmann et al. (1997); (5g) Simon et al. (1997); (5h) Hogerheijde et al. (1995).

	Oph W	S140	IC 63	NGC 2023	Orion Bar
H ₂ 0–0 S(3) ^a 9.66 μm (SWS, 20'')	13.7[8]	16.8[30]	10[29]	16.5[13.5]	59.7[11]
T_{rot}^b (K)	330 \pm 15	500 \pm 40	620 \pm 45	330 \pm 15	390 \pm 20
$N_{\text{H}_2}^c$ (10 ²¹ cm ⁻²)	0.6	0.2	5	0.7	1
Ref.	(1)	(2)	(3a)	(4a)	(5a)
H ₂ 1–0 S(1) ^a 2.12 μm Beam	3.1[16] 1''	–	1.84[13] 74''	7[20] 1''	13[10] 1.5''
1–0 S(1)/2–1 S(1)	–	–	2.2[23]	2.8[18]	2.3[7]
Ref.	(1)	–	(3b)	(4b, c)	(5b, c)
PAH (2–15 μm)/10 ³ (ISOCAM, 6'')	3.6	–	0.8	11	62
Ref.	(1)	–	(3c)	(4d)	(5d)

^a Intensities (in 10⁻⁵ erg s⁻¹ cm⁻² sr⁻¹) with relative uncertainty in % (in between brackets). H₂ line intensities have not been corrected for dust attenuation. The 1–0 S(1) line intensity has been smoothed to the $\sim 20''$ beam of SWS or multiplied by a beam factor.

^b Excitation temperature of H₂ pure rotational levels with $J \leq 7$.

^c H₂ column density inferred from the intensity of H₂ rotational lines and assuming that the population distribution of low H₂ rotational levels is essentially in LTE.

References: (1) Data corresponding to the peak of the H₂ emission in Habart et al. (2003); (2) Timmermann et al. (1996); (3a) Thi et al. (1999) (note that the observations cannot be fitted by a single excitation temperature but two components at ~ 100 K and ~ 620 K are needed); (3b) Luhman et al. (1997); (3c) data from Cesarsky, priv. com.; (4a) Moutou et al. (1999); (4b) Field et al. (1998); (4c) Burton et al. (1998); (4d) Abergel et al. (2002); (5a) data from Bertoldi, priv. com.; (5b) van der Werf et al. (1996); (5c) Walmsley et al. (2000); (5d) Cesarsky et al. (2000).

discrepancy is that, in the models, the gas is not hot enough or alternatively that the column density of H₂ is too low in the zones where the gas is warm. One explanation of this discrepancy is that the H₂ formation rate is larger at high gas temperatures, moving the H⁰/H₂ transition zone closer to the edge of the PDR. Habart et al. (2003) have shown that the observed H₂ excitation from the moderately excited Oph W PDR can be accounted for by increasing the H₂ formation rate by a factor about 5 (compared to the standard H₂ formation rate derived in the diffuse ISM by Jura 1975) to $\sim 2 \times 10^{-16}$ cm³ s⁻¹ at $T_{\text{gas}} \approx 330$ K. In this study, we extend our study of the H₂ formation in

PDRs (described in Sect. 2) spanning a wide range of excitation conditions.

3.1. PDR model

In order to analyse the H₂ emission observations from the PDRs, we use an updated version of the stationary PDR model described in Le Bourlot et al. (1993). In this model, a PDR is represented by a semi-infinite plane-parallel slab with an incident radiation field. The input parameters are (i) the incident FUV field χ , and (ii) the proton gas density n_{H} . We will

consider constant density models with $n_{\text{H}} = 10^4 - 10^5 \text{ cm}^{-3}$ and $\chi = 10^2 - 10^5$ in the range of values prevailing in our PDR sample (see Table 1). With the inputs χ and n_{H} , the model solves the chemical and thermal balance starting from the slab edge at each A_v -step in the cloud. The H₂ abundance results from a balance between the formation of H₂ on dust grains and the photodissociation of H₂ by FUV flux, which is attenuated by dust extinction and self-shielding in the H₂ lines. At equilibrium, the density of atomic (n_{H^0}) and molecular hydrogen (n_{H_2}) are given by

$$R_{\text{f}} n_{\text{H}} n_{\text{H}^0} = R_{\text{d}}(0) \times \chi e^{-\tau_{\text{d}}} \times f_{\text{s}}(N(\text{H}_2)) \times n_{\text{H}_2} \quad (1)$$

with R_{f} ($\text{cm}^3 \text{ s}^{-1}$) the H₂ formation rate, $R_{\text{d}}(0) \sim 5 \times 10^{-11} \text{ s}^{-1}$ the unshielded photodissociation rate per H₂ for $\chi = 1$, $N(\text{H}_2)$ the column density of H₂ and $e^{-\tau_{\text{d}}}$ and $f_{\text{s}}(N(\text{H}_2))$ respectively the dust extinction and the H₂ self-shielding factors. In this study, we adopt R_{f} constant throughout the PDRs. The standard value inferred from observations of H₂ UV absorption lines in interstellar diffuse clouds is $R_{\text{f}}^0 \sim 3 \times 10^{-17} \text{ cm}^3 \text{ s}^{-1}$ (Jura 1975). We assume that the energy released by the nascent molecule (4.5 eV) is equally distributed between the kinetic energy of H₂ (E_{k}), the internal energy of H₂ (E_{int}) and the internal energy of the grain (E_{grain}). Moreover, we assume that the internal energy of the nascent H₂ is distributed in Boltzmann distribution through the energy levels. The energy used for the heating per H₂ formation is $E_{\text{k}} + E_{\text{int}} \times f$ with $E_{\text{k}} \sim 1.5 \text{ eV}$ and $E_{\text{int}} \times f \sim 0.7 \text{ eV}$ where f is the fraction of the internal energy of the nascent H₂ contributing to the heating. For the collisional excitation and de-excitation of H₂, we adopt the H⁰-H₂ inelastic rates of Martin & Mandy (1995) extrapolated to low temperatures. The heating rate due to the photoelectric effect on small dust grains is derived from the formalism of Bakes & Tielens (1994). For the physical conditions prevailing in our PDRs, the heating is mainly due to the photoelectric effect. Nevertheless, for high R_{f} ($\sim 10 \times R_{\text{f}}^0$) the heating rate per H₂ formation becomes comparable (factor of ~ 2 lower) to the photoelectric heating rate.

3.2. H₂ line intensity ratios as diagnostic of the H₂ formation rate

The (v , J) excited states of H₂ can be populated by inelastic collisions with gas phase species, UV pumping and by the formation process. The population distribution of H₂ levels is a function of the gas density, the gas temperature and the UV flux. Hence, the H₂ line intensity ratios – which depend on the physical conditions in the photodissociation front where atomic hydrogen becomes molecular – should probe the H₂ formation rate which controls the location of the H⁰/H₂ transition zone in PDRs. In the following, we study the dependence of several H₂ line ratios as a function of R_{f} (predicted by model calculations).

In Fig. 1, we show the model predictions (face-on) for the intensity of the 1–0 S(1) line as well as for several commonly observed line intensity ratios as a function of the molecular hydrogen formation rate. First, we discuss the dependence of the 1–0 S(1) line intensity on R_{f} . At equilibrium (Eq. (1)), the intensity of the 1–0 S(1) line $I_{\text{H}_2}^{\text{f}}$ is proportional to $R_{\text{f}} n_{\text{H}} N(\text{H}^0)$

where $N(\text{H}^0)$ is the column density of atomic H atoms. For high values of χ/n_{H} (≥ 0.01), the H⁰/H₂ transition is driven by the dust opacity and $N(\text{H}^0)$ is a constant equal to a few 10^{21} cm^{-2} . We thus have $I_{\text{H}_2}^{\text{f}} \propto R_{\text{f}} n_{\text{H}}$ (see Fig. 1a). Conversely, when $\chi/n_{\text{H}} \lesssim 0.01$, molecular hydrogen self shields sufficiently that the gas goes molecular before the dust gets optically thick. In this case, using the approximation $f_{\text{s}}(N(\text{H}_2)) = (N(\text{H}_2)/N_0)^{-3/4}$ with $N_0 = 10^{14} \text{ cm}^{-2}$ (Draine & Bertoldi 1996) for $N(\text{H}_2) \lesssim 10^{21} \text{ cm}^{-2}$, we find $R_{\text{f}} n_{\text{H}} N(\text{H}^0) = 4R_{\text{d}}(0) \times \chi \times N(\text{H}_2)^{1/4} N_0^{3/4}$ (Hollenbach & Tielens 1999). At the H⁰/H₂ transition, we have $N(\text{H}_2) = N(\text{H})/2$ with $N(\text{H})$ the proton column density from the edge of the PDR to the H⁰/H₂ transition zone. Finally, $I_{\text{H}_2}^{\text{f}} \propto \chi \times N(\text{H})^{1/4}$ (see Fig. 1a).

The low- J rotational $v = 0-0$ H₂ lines have a somewhat different dependence upon R_{f} because at densities above 10^4 cm^{-3} of interest to us, their population distribution is essentially in LTE and the line intensities depend mainly on the temperature in the photodissociation front where hydrogen becomes molecular. In the range of χ and n_{H} studied here, the gas temperature profiles as a function of depth in the PDR are fairly insensitive to the fraction of molecular hydrogen (heating is mainly due to photoelectric emission from dust grains and cooling to fine structure line emission of O⁰ and C⁺) but higher H₂ formation rates cause the photodissociation front to shift closer to the surface where the temperature is higher. We show in Figs. 1b and d the dependence of the 0–0 S(1)/0–0 S(3) and 0–0 S(3)/1–0 S(1) line ratios as functions of R_{f} . The ratio of the two 0–0 lines is essentially a measure of temperature and thus decreases as R_{f} increases as a consequence of the temperature increase in the dissociation front. This effect also causes a sharper increase in 0–0 S(3) than in 1–0 S(1) and thus the ratio 0–0 S(3)/1–0 S(1) increases with increasing R_{f} .

We also show in Fig. 1c the dependence of the 2–1 S(1)/1–0 S(1) line predicted by the models as a function of $R_{\text{f}}/R_{\text{f}}^0$. This commonly observed line ratio is known in PDRs to vary between values of ~ 2 typical of pure fluorescence to values of $\sim 3-5$ at high densities (above 10^5 cm^{-3}) when collisional deexcitation of higher vibrational levels becomes competitive with radiative decay (Black & van Dishoeck 1987; Draine & Bertoldi 1996). One sees from Fig. 1c that the model predicted line ratio for $\chi \leq 10^3$ and $n_{\text{H}} \leq 10^5 \text{ cm}^{-3}$ is independent of R_{f} (as well as of χ and n_{H}) and equal to ~ 2 . This is due to the fact that the densities and radiation fields of interest to us (and consequently assumed in the models) are in the range for which the population of excited vibrational levels of H₂ are controlled by purely radiative cascade process.

In summary, we find that the 0–0 S(3)/1–0 S(1) line intensity ratio depends considerably on the H₂ formation rate via the variation of both the gas temperature and the UV flux in the H⁰/H₂ transition zone. However, the changes in this ratio can also be due to changes in the radiation field and density. Thus, by comparing this H₂ line intensity ratio predicted by the model (essentially independent of the geometry and of the total column density) with observations from PDRs where χ and n_{H} have been determined from other observations, we can expect to probe the H₂ formation rate in PDRs.

In Fig. 2, we show the H₂ 0–0 S(3)/1–0 S(1) line intensity ratio as predicted by the model for an edge-on geometry

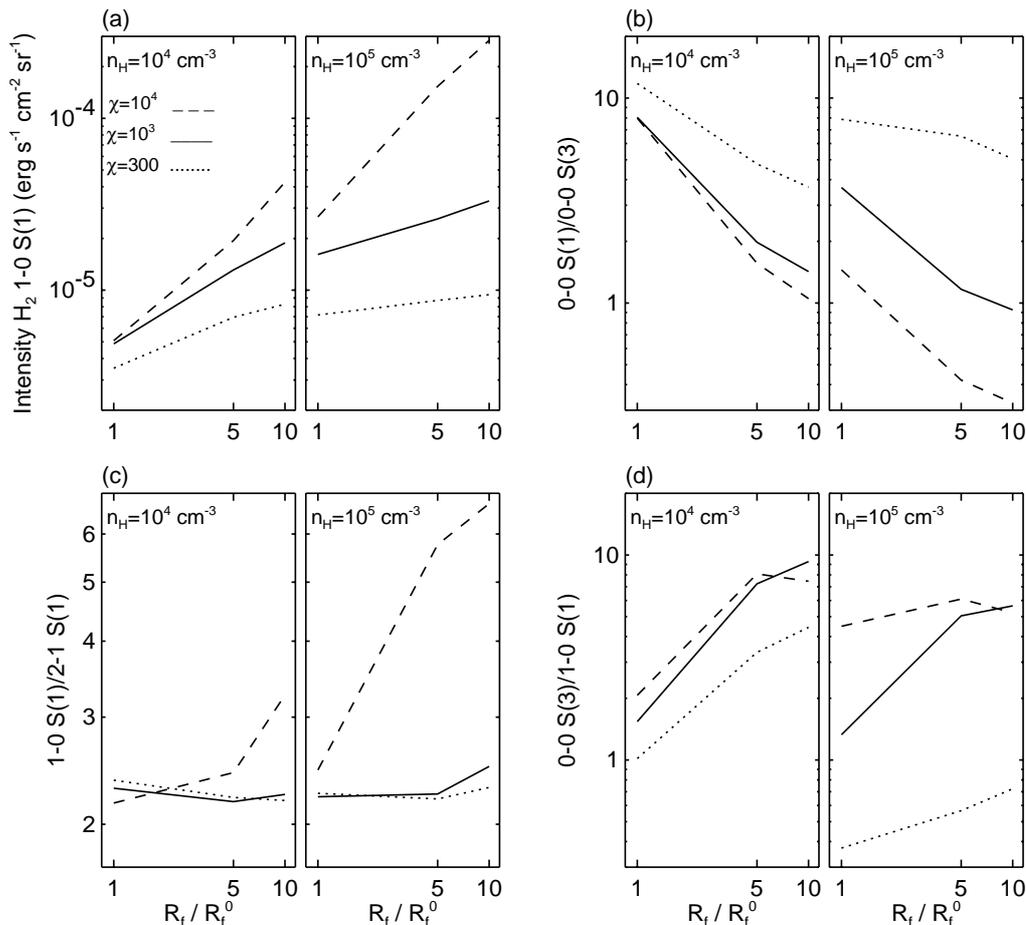


Fig. 1. Panel **a**): Intensity of the H₂ 1-0 S(1) line emission predicted by models (face-on) for two gas densities and different incident radiation fields – $\chi = 300$ (dotted lines), $\chi = 10^3$ (solid lines) and $\chi = 10^4$ (dashed lines) – as a function of the value of H₂ formation rate divided by R_f^0 corresponding to the formation rate based upon Copernicus data (Jura 1975). Panels **b**), **c**) and **d**): several H₂ line intensity ratios for the same models.

(as most of our PDRs are, see references in Table 1) in the H₂ emission region as a function of χ and for different H₂ formation rates. We compare these predicted line intensity ratios with observational data for our PDRs sample described in Sect. 2. The data has been corrected for dust attenuation applying a correction factor $\tau/(1 - e^{-\tau})$. Here, we use the extinction curve of Draine (1989) and the visual extinction within the PDR reported in Table 1 derived from sub-mm dust emission or CO observations. This assumes that our PDRs are exactly planar and edge-on and that densities are similar in the H₂ emission layer and in the cold molecular layer which is questionable because the column density inferred from the molecular hydrogen rotational transitions is generally an order of magnitude lower than the value derived from sub-mm dust emission or CO observations. The explanation of this difference is not clear. It could occur in an edge-on geometry due to beam dilution effects (i.e., H₂ emission region not resolved by ISO-SWS) or because of density gradients. For reasons of simplicity, we have adopted in Fig. 2 the estimate inferred from sub-mm dust emission or CO observations. The error involved here is small since using the column density derived from the molecular hydrogen rotational transitions, the H₂ 0-0 S(3)/1-0 S(1) line intensity ratio would diminish by $\sim 30\%$ which is comparable to the error bars.

In the following, we discuss for each PDR of our sample the value of R_f required to account for the observed H₂ excitation. For Oph W ($\chi \sim 250$, $n_H \sim 10^4 \text{ cm}^{-3}$) and IC 63 ($\chi \sim 650$, $n_H \sim 5 \times 10^4 - 10^5 \text{ cm}^{-3}$), we find that models with a high H₂ formation rate (i.e., $R_f \gtrsim 5 \times R_f^0$) roughly reproduce the 0-0 S(3)/1-0 S(1) line ratio observed. For the standard H₂ formation rate, the 0-0 S(3)/1-0 S(1) line ratio is underestimated by a factor about 4. For the more highly excited PDRs, i.e., NGC 2023 ($\chi \sim 500 - 3000$, $n_H \sim 10^4 - 10^5 \text{ cm}^{-3}$) and the Orion Bar ($\chi \sim 0.5 - 2.5 \times 10^4$, $n_H \sim 5 \times 10^4 - 3 \times 10^5 \text{ cm}^{-3}$), we find on the contrary that models with the standard H₂ formation rate roughly match the data. In the case of S140, where we have no measurement of the intensity for the 1-0 S(1) line, we use ISO observations of the 1-0 Q(3) line from Draine & Bertoldi (1999) to determine the H₂ rotational to rovibrational line intensity ratio. For the physical conditions of interest to us, the models predict that the 1-0 S(1)/1-0 Q(3) line intensity ratio is about a factor of 1.4. Applying this factor, we find that the 0-0 S(3)/1-0 S(1) line intensity ratio (corrected for dust attenuation) is about 3. Then, one sees from Fig. 2 that for S140 ($\chi \sim 100 - 250$, $n_H \sim 10^4 - 5 \times 10^4 \text{ cm}^{-3}$) models with a high H₂ formation rate are – as for the moderately excited PDR Oph W and IC 63 – required to explain the observed H₂ line intensity ratio. In Table 3, we give for each region the values

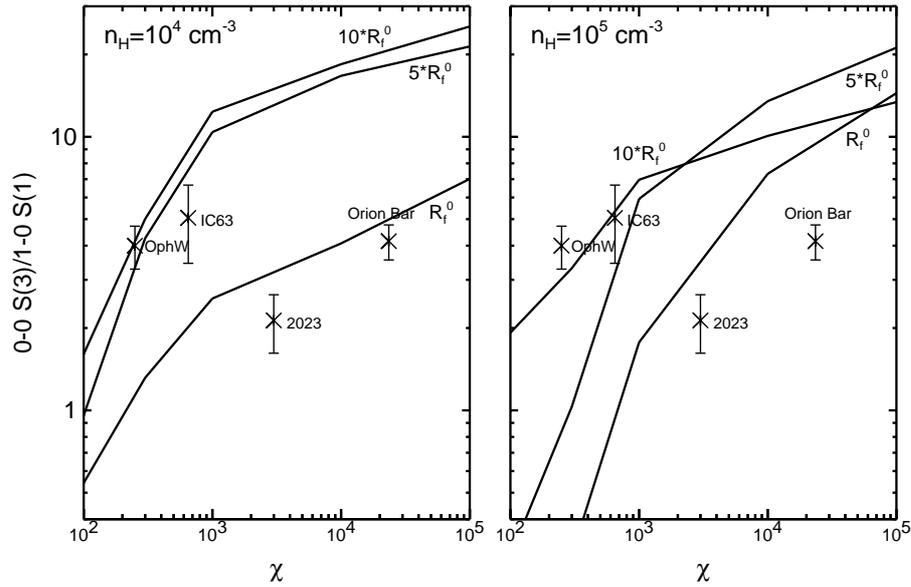


Fig. 2. H₂ 0–0 S(3)/1–0 S(1) line intensity ratio, as predicted by models (edge-on) and as observed for our PDR sample (crosses with error bars), as a function of χ the FUV incident radiation field. Predicted line intensity ratios (taken in the H₂ emitting zone) are presented for two gas densities and shown for three different H₂ formation rates (R_f^0 , $5 \times R_f^0$, $10 \times R_f^0$). Observed line intensity ratios have been corrected for dust attenuation (see text). For each PDR of our sample, χ has been derived from the expected FUV luminosity of the exciting star and assuming that the distance of the exciting star to the PDR is equal to the distance projected onto the sky (see Sect. 2). For S140, where we have no measurement of the intensity for the 1–0 S(1) line, we use observations of the 1–0 Q(3) line to determine the H₂ line intensity ratio (see text).

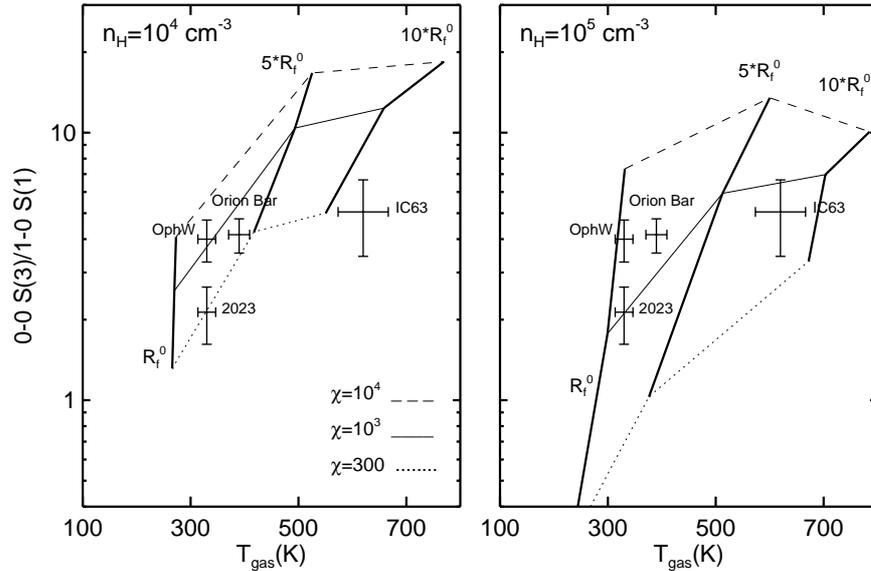


Fig. 3. H₂ 0–0 S(3)/1–0 S(1) line intensity ratio as predicted by the same models shown in Fig. 2 and as observed for our PDR sample (crosses with error bars) as a function of T_{gas} the gas temperature in the H₂ emitting region. For the observations, we use the excitation temperature of the H₂ pure rotational levels (see text). For IC 63, the observed H₂ pure rotational lines intensity cannot be fitted by a single excitation temperature but two components at ~ 100 K and ~ 600 K are needed.

of the H₂ formation rate derived using Fig. 2 and assuming that the gas density in the H₂ emission region is about 10^4 cm^{-3} for all sources. Considering that the gas density is about 10^5 cm^{-3} , R_f required to explain the data would be (by a factor of ~ 2) higher and lower for respectively the moderately and the highly excited PDRs. We emphasize that our determination of R_f from the H₂ line intensity ratios depends on the treatment in the model of the thermal balances and the chemistry. In particular, the calculation of the grain photoelectric heating which mainly determines T_{gas} in the PDR modelling (see Sect. 3.1) could

affect the excitation of the lowest rotational levels ($J \leq 5$) of H₂. For example, Habart et al. (2003) have shown that, throughout the Oph W PDR, increasing the photoelectric heating rate by $\sim 50\%$, which leads to higher T_{gas} in the H⁰/H₂ transition, the 0–0 S(3) line intensity is enhanced (by a factor ~ 2) and R_f required to explain the data would be reduced by a factor ~ 1.5 (see Fig. 2). However, even if we cannot precisely determine the uncertainties on our estimates of R_f , the values of R_f derived here should be at most uncertain by a factor of about 2.

One check of our estimates of R_f is to see if the predicted T_{gas} values in the H₂ emitting region are consistent with the observed rotational temperatures reported in Table 1. In Fig. 3, we show the 0–0 S(3)/1–0 S(1) line intensity ratio predicted by the same models shown in Fig. 2 as a function of the gas temperature in the H₂ emitting region and compared with observational data. For observations, we use the excitation temperature of H₂ pure rotational levels (with $J \leq 7$) which in principle is an upper limit as UV pumping could contribute to the excitation of H₂ even for low energy levels. In the case of IC 63 where the measured pure H₂ rotational lines show two excitation temperatures (at ~ 100 K and ~ 600 K, Thi et al. 1999) there is direct evidence for such contamination. Using Fig. 3, we favour (as previously) for the moderately excited PDRs models with high H₂ formation rate which can in fact explain the observed rotation temperatures. Models with a standard H₂ formation rate predict in fact a gas temperature (≤ 300 K) lower than observed (~ 300 – 600 K). For the Orion Bar and NGC 2023, we find on the contrary that models with standard H₂ formation rate predict temperatures consistent with the data (~ 300 – 400 K). Finally, we have checked that these models reproduce the observed absolute intensities of the 0–0 S(3) and 1–0 S(1) H₂ lines. Taking into account the inclinations of the PDRs of our sample, which are seen edge-on except for IC 63, we find an agreement within $\leq 50\%$.

It must be emphasized that these results are based on two fundamental assumptions. Firstly, we assume a uniform homogeneous gas density while PDRs may have a density gradient and could be clumpy. Nevertheless, because the modelling of the H₂ excitation mainly depends upon the average gas density in the H₂ emission zone, density structure effects are probably minor. In fact, the detailed study of Habart et al. (2003) of the H₂ excitation toward Oph W taking into account the gas density profile reaches the same estimation of R_f deduced here.

Secondly, we assumed a static, equilibrium PDR. In reality, the propagation of the ionization and photodissociation fronts will bring fresh H₂ into the zone emitting line radiation. Note that a non-equilibrium ortho-to-para H₂ ratio has been observed in ISO-SWS observations towards Oph W (Habart et al. 2003), NGC 2023 (Moutou et al. 1999) and NGC 7023 (Fuente et al. 1999). Nevertheless, the model of non-equilibrium PDRs of Störzer & Hollenbach (1998) predicts that, for the physical conditions prevailing in the Orion Bar and for an advection velocity of the order of 1 km s^{-1} , the H₂ 0–0 S(3)/1–0 S(1) line intensity ratio varies by a factor less than ~ 2 relative to the steady state value.

In the next section, we review other observational constraints on the H₂ formation rate based on H₂ UV absorption measurements.

3.3. Other observational constraints on the H₂ formation rate

UV absorption measurements of H₂ have been often used to study H₂ formation, destruction, and excitation in the diffuse ISM. With the numerous new H₂ UV absorption line

observations obtained recently by FUSE (Snow et al. 2000; Shull et al. 2000; Rachford et al. 2001, 2002; Tumlinson et al. 2002; Sonnentrucker et al. 2002), the H₂ formation in the diffuse ISM has been re-considered. In particular, Gry et al. (2002) have determined the H₂ formation rates over three lines of sight in the Chamaeleon clouds. They find a rate roughly constant and equal to about $4 \times 10^{-17} \text{ cm}^3 \text{ s}^{-1}$ (with an uncertainty of about a factor of 2) for $n_{\text{H}} \sim 30$ – 50 cm^{-3} and $T_{\text{gas}} \sim 60$ K, in agreement with the rate inferred by Jura (1975). Moreover, due to the high FUSE sensitivity, fainter stars with higher extinctions could be observed with far-UV instruments (Moos et al. 2000), thus allowing the study of translucent clouds. Rachford et al. (2002), studying correlations of the H₂-related quantities with the column densities of other molecules and dust extinction properties for lines of sight with $A_v \gtrsim 1$, investigate the dependence of the H₂ formation rate with the composition and physical state of the gas and grains. Furthermore, the FUSE observations in the lower metallicity environments of the Small and Large Magellanic Clouds allow us to probe H₂ formation and destruction in physical and chemical environments different from the Galaxy. Tumlinson et al. (2002) find that to reproduce the reduced molecular fraction and enhanced rotational excitation in the SMC and LMC, a low H₂ formation rate ($R_f \sim 3 \times 10^{-18} \text{ cm}^3 \text{ s}^{-1}$) and a high UV field relative to diffuse Galactic medium are required.

Combining the FUSE results in the diffuse Chamaeleon clouds and the ISO observations discussed above, we find that for a wide range of physical conditions – $1 \lesssim \chi \lesssim 10^4$, $100 \text{ cm}^{-3} \lesssim n_{\text{H}} \lesssim 10^5 \text{ cm}^{-3}$, $50 \text{ K} \lesssim T_{\text{gas}} \lesssim 600 \text{ K}$, $10 \text{ K} \lesssim T_{\text{dust}} \lesssim 100 \text{ K}$ (see Tables 1 and 3) – H₂ forms efficiently ($R_f \sim 4 \times 10^{-17}$ – $1.5 \times 10^{-16} \text{ cm}^3 \text{ s}^{-1}$). This result raises questions about our understanding of the H₂ formation process. In Sect. 5, we re-examine models of H₂ formation with this in mind and compare in Sect. 6 the observational constraints on the H₂ formation rate with model predictions.

4. Influence of aromatic dust on the H₂ formation process in PDRs

In PDRs, small dust grains are intimately coupled to the evolution of the gas. In fact, recent theoretical (Bakes & Tielens 1994; Weingartner & Draine 2001) and observational (Habart et al. 2001) work has shown that small grains (radius $\leq 100 \text{ \AA}$) dominate the photoelectric heating. Furthermore, given that small grains make a dominant contribution to the total grain surface (see Sect. 6), it is plausible that they play a dominant role in H₂ formation. Therefore, if H₂ forms on small grains, we can expect that both the grain photoelectric heating rate and the H₂ formation rate will scale with their abundance. In particular, increasing their abundance would lead to higher gas temperature and would bring the H⁰/H₂ transition closer to the edge: this could significantly enhance the rotational and fluorescent emission of H₂. Habart et al. (2003) have shown that, assuming that R_f scales with the PAH abundance, the enhancement in R_f required to account for the observed H₂ emission from Oph W may result from an increased PAH abundance. Based on this, we investigate what we can predict concerning the influence of PAHs on the H₂ formation process.

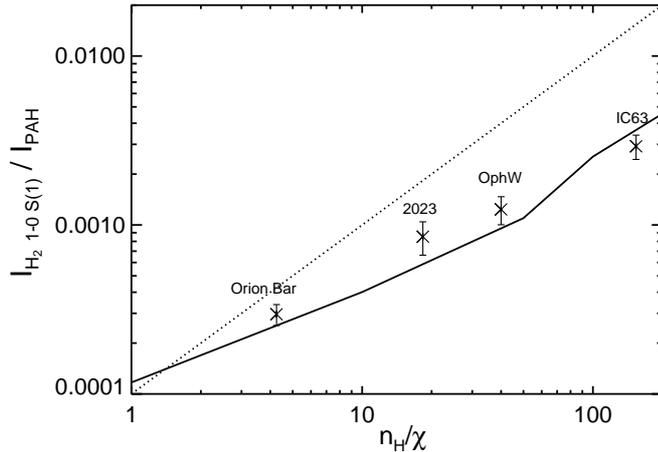


Fig. 4. Ratio between the H₂ 1–0 S(1) line and PAH emission as predicted by edge-on model (solid line) and as observed (crosses with error bars) as a function of n_{H}/χ . The dotted straight lines shows the linear dependence of the emission ratio with n_{H}/χ expected from Eq. (2) when $\chi/n_{\text{H}} \gtrsim 0.01$. For the PDRs of our sample, n_{H}/χ has been taken equal to the ratio between the average value of the n_{H} determinations given in Table 1 and χ determined from the expected FUV luminosity of the exciting star and assuming that the distance of the exciting star to the PDR is equal to the distance projected onto the sky (see Sect. 2).

To free oneself of the influence of the PAHs on the thermal balance, we study here the ratio between the H₂ 1–0 S(1) line (whose intensity does not depend on T_{gas} , see Sect. 3.2) and the PAH emission. We first express analytically the H₂ fluorescent to PAH emission ratio $I_{\text{H}_2}^f/I_{\text{PAH}}$ as a function of the H₂ formation rate and the PAH abundance, as well as the physical conditions (n_{H}, χ), in order to examine qualitatively the dependence of this ratio with these parameters. In Sect. 3.2, we have seen that the H₂ 1–0 S(1) line emission $I_{\text{H}_2}^f$ goes roughly as (i) $R_{\text{f}}n_{\text{H}}$ for high χ/n_{H} and as (ii) χ for low χ/n_{H} . The emission of aromatic dust scales with the intensity of the FUV radiation field (Puget et al. 1985; Sellgren et al. 1985) and we have $I_{\text{PAH}} \propto \chi e^{-\tau_{\text{d}}} \times N_{\text{H}} [\text{C}/\text{H}]_{\text{PAH}}$ with $[\text{C}/\text{H}]_{\text{PAH}}$ the abundance of carbon locked up in PAHs. As the column density over which PAHs emits is a few 10^{21} cm^{-2} (where dust is optically thin), I_{PAH} goes as $\chi \times [\text{C}/\text{H}]_{\text{PAH}}$. From these considerations, we find

$$\frac{I_{\text{H}_2}^f}{I_{\text{PAH}}} \propto \begin{cases} \frac{R_{\text{f}}}{[\text{C}/\text{H}]_{\text{PAH}}} \times \frac{n_{\text{H}}}{\chi} & : \chi/n_{\text{H}} \gtrsim 0.01 \\ \frac{1}{[\text{C}/\text{H}]_{\text{PAH}}} & : \chi/n_{\text{H}} \lesssim 0.01. \end{cases} \quad (2)$$

Thus, by studying the observed H₂ fluorescent to PAH emission ratio from PDRs covering a wide range of n_{H}/χ ratio, we should be able to probe the H₂ formation on PAH: if H₂ forms on PAHs, we expect that the $I_{\text{H}_2}^f/I_{\text{PAH}}$ ratio scales with n_{H}/χ . In other words, the $R_{\text{f}}/[\text{C}/\text{H}]_{\text{PAH}}$ ratio is constant and does not vary from one region to another.

We now compare the ratio between the H₂ 1–0 S(1) line and PAH emission observed from the PDRs of our sample to model results. For the models, we consider $\chi = 10^2\text{--}10^4$ and $n_{\text{H}} = 10^4\text{--}10^5 \text{ cm}^{-3}$ which corresponds to the range of values prevailing in our PDR sample (see Table 1). We adopt a constant $R_{\text{f}}/[\text{C}/\text{H}]_{\text{PAH}}$ ratio corresponding to the values derived in the Oph W PDR, i.e., $R_{\text{f}} \approx 5 \times R_{\text{f}}^0$ and $[\text{C}/\text{H}]_{\text{PAH}} \approx 0.5 \times 10^{-4}$ (Habart et al. 2003). The power emitted by PAHs has been

derived from the PAH absorption cross-section of Verstraete & Léger (1992) and the size distribution described in Sect. 6. In Fig. 4, we show the H₂ 1–0 S(1)/PAH emission ratio predicted by the model in the H₂ emission zone as a function of the n_{H}/χ ratio. As expected from the Eq. (2), for $\chi/n_{\text{H}} \gtrsim 0.01$ the H₂ 1–0 S(1)/PAH emission ratio increases proportionally with n_{H}/χ .

The observational ratios for our PDR sample are compared to these predictions. The observed points roughly fall on the model curve. From one PDR to another, the change of the emission ratio seems to result mainly from the physical conditions (i.e., n_{H}/χ) variations. We deduce from this that the $R_{\text{f}}/[\text{C}/\text{H}]_{\text{PAH}}$ ratio is roughly constant which suggests that formation of H₂ on PAHs should be important. However, the correlation between R_{f} and $[\text{C}/\text{H}]_{\text{PAH}}$ found in our PDR sample is observed not to apply to the main PDR in the 30 Dor star forming region in the Large Magellanic Cloud where for $n_{\text{H}}/\chi \sim 1$ the H₂ 1–0 S(1) line to PAH emission ratio is measured to be ~ 0.001 (Boulanger et al. 2003). In future work, this comparison should be extended so as to include all small grains, i.e., not only the band carriers but also the very small grains emitting at longer wavelengths.

5. H₂ formation mechanisms on grain surfaces

In this section, with the aim of explaining our observational constraints on the H₂ formation, we examine models of H₂ formation mechanism. Two general mechanisms for forming H₂ on grain surfaces have generally been proposed:

1. formation by physisorbed H atoms (Langmuir-Hinshelwood) whereby two adsorbed and mobile physisorbed H atoms (bound simply via van der Waals interaction with binding energies of the order of 0.05 eV or 500 K, Katz et al. 1999) interact to recombine and desorb as H₂ and
2. formation by the interaction of an H atom from the gas phase with a chemisorbed H atom (with binding energy roughly 1 eV equivalent to $\sim 10000 \text{ K}$, Fromherz et al. 1993) forming desorbed H₂ (the Eley–Rideal mechanism).

In the following discussion, we describe these processes mainly focusing on the version of the Langmuir-Hinshelwood mechanism whereby one of the adsorbed H-atoms is originally in a chemisorbed site (Hollenbach & Salpeter 1971; Cazaux & Tielens 2002, 2003). This approach will be called in the following the indirect chemisorption approach as opposed to the direct chemisorption or Eley–Rideal mechanism. We make simple empirical estimates of rates for these processes as a function of the physical conditions and grain characteristics. We consider small grains (SGs), dust particles with radii of a few Å to 100 Å (i.e., PAHs and Very Small Grains, VSGs) which fluctuate in temperature in the radiation field, and big grains (BGs), larger grains of radii $>0.01 \mu\text{m}$ in thermal equilibrium with the radiation field (Désert et al. 1990).

5.1. The Langmuir-Hinshelwood mechanism

In the formation from physisorbed atoms (pure Langmuir-Hinshelwood), an H atom is already physisorbed on the grain surface. A second H atom from the gas sticks to the grain and diffuses to finally recombine with the first H atom to form H₂. The rate depends upon the competition between the mobility of the H atom on the grain surface and its thermal evaporation rate. In the laboratory, this process is observed to be efficient on grains with $7 \lesssim T_{\text{dust}} \lesssim 20$ K (Pirronello et al. 1997, 1999).

Amongst the dust grain populations described above, only BGs could carry a large fraction of physisorbed H atoms. Indeed, after a UV photon is absorbed by SGs, the physisorbed H atoms should evaporate. Further, for the physical conditions typical of the PDRs, the rate of thermal fluctuations τ_{abs}^{-1} ($\sim 1.6 \times 10^{-9} \times N(\text{C}) \times \chi \text{ s}^{-1}$ with $N(\text{C})$ the number of carbon atom in the grain, Verstraete et al. 2001) is comparable to or larger than the accretion rate of H atoms τ_{acc}^{-1} : for a grain with a radius of 1.5 nm ($N(\text{C}) \simeq 1600$), we find $\tau_{\text{abs}}^{-1}/\tau_{\text{acc}}^{-1} \sim 1000 \times (100 \text{ K}/T_{\text{gas}})^{0.5} \times \chi/n_{\text{H}}$. Thus for χ/n_{H} larger than 0.001 (true in general for the objects in Table 1), UV radiation in PDRs will keep SG surfaces clean.

Since this mechanism will only be efficient on BGs and in interstellar regions of low excitation (in PDRs we find typically $T_{\text{BGs}} \geq 30$ K, see Table 3), we neglect it in what follows.

5.2. Formation involving a chemisorbed H atom

We now consider the case where the first H atom is bound to the surface in a chemisorbed site. The second H atom from the gas phase reaches this site directly (*direct* chemisorption or Eley-Rideal, Duley 1996; Parneix & Brechignac 1998) or after diffusion on the grain surface (*indirect* chemisorption, Hollenbach & Salpeter 1971; Cazaux & Tielens 2002, 2003). The incident H atom crosses the activation barrier E_a (typically about ~ 500 – 1500 K, Fromherz et al. 1993; Parneix & Brechignac 1998; Sidis et al. 2000; Cazaux & Tielens 2003) by either thermal hopping or tunneling and recombines to finally form H₂. This process involving strongly bound H atoms will be efficient at higher dust surface temperatures than the pure Langmuir-Hinshelwood mechanism.

We first consider the direct Eley-Rideal mechanism. This involves reaction of the incoming H atom with an chemisorbed H on the grain surface without any requirement for adsorption and thermal accommodation. The formation probability P_{H_2} can be written as:

$$P_{\text{H}_2} = f \times \eta \quad (3)$$

with f the probability that the incident H atom reaches the chemisorbed H and recombines to form H₂ and η the probability to eject the molecular hydrogen formed. The incident H atom from the gas phase must hit the grain with enough thermal energy to cross the activation barrier (E_a) by thermal hopping. f is given by:

$$f = \frac{N_c}{N} \times \exp\left(-\frac{E_a}{kT_{\text{gas}}}\right) \quad (4)$$

with N_c the total number of chemisorbed H atoms on the grain surface and N the total number of physisorbed and

chemisorbed sites. The fraction of chemisorbed H atoms (N_c/N) is critical for this process. This fraction will be significant when T_{gas} is sufficiently high to carry an appreciable fraction of chemisorbed sites occupied. In PDRs (where $T_{\text{gas}} \geq 300$ K) we expect N_c/N to be relatively high while in cold interstellar clouds N_c/N should be low.

An alternative to the above is the case where the incident H atom initially sticks to a physisorbed site and then scans the surface until it “finds” the chemisorbed H atom. Here, the formation probability P_{H_2} can be written as:

$$P_{\text{H}_2} = S \times f \times \eta \quad (5)$$

with S the sticking probability.

The probability f that the physisorbed H atom diffuses over the grain surface (until it reaches a neighbouring site to a chemisorbed H atom) and recombines before it is evaporated, can be given by $f = \frac{\tau_{\text{p}}^{-1}}{\tau_{\text{p}}^{-1} + \tau_{\text{ev}}^{-1}}$ where τ_{p}^{-1} is the inverse time scale for diffusing and recombining and τ_{ev}^{-1} the evaporation rate of physisorbed H. In the appendix we estimate the time scales τ_{p} and τ_{ev} . This leads to the expression:

$$f = \frac{1}{1 + \left(\frac{N}{4N_c}\right)^2 \times \exp\left(\frac{E_p - E_d}{kT_{\text{dust}}}\right) + \left(\frac{N}{4N_c}\right) \times k_{\text{rec}}} \quad (6)$$

with E_d the desorption energy of a physisorbed H atom and E_p the activation barrier energy for the diffusion of a physisorbed H (see Table 2). Considering that the physisorbed H atom crosses the activation barrier to recombine with a neighbouring chemisorbed atom by either (i) thermal diffusion or by (ii) tunnelling, we find (see appendix) that $k_{\text{rec}} = \exp\left(\frac{E_a - E_d}{kT_{\text{dust}}}\right)$ at high dust temperatures (above ~ 40 K) when thermal diffusion dominates whereas at low temperatures (below ~ 30 K) when tunneling is more important $k_{\text{rec}} = \exp\left(E_d \left(\frac{1}{kT_{\text{cr}}} - \frac{1}{kT_{\text{dust}}}\right)\right)$ with $kT_{\text{cr}} = 80 E_{\text{d}3}/(E_{\text{a}3}^{0.5} \times \Delta x(\text{\AA}))$ where $E_{\text{a}3} = E_a/(1000 \text{ K})$, $E_{\text{d}3} = E_d/(1000 \text{ K})$ and Δx is the width of the barrier typically of the order of ~ 1 – 3 \AA (Buch 1989; Fromherz et al. 1993; Sidis et al. 2000).

The activation barrier energies for physisorbed H atom diffusion (E_p) and for recombination with a neighbouring chemisorbed atom (E_a) are critical for this process. For E_a high (≥ 1000 K), the recombination term will dominate and f will be high only where tunneling dominates (see Fig. 5). For E_a low (~ 600 K), the diffusion term will be critical and f will depend much on E_p . In this case, f will be high for $E_p \lesssim E_d$ (if E_p is too large the atoms evaporate before they find a neighbouring chemisorbed site) and for $E_p \sim 500$ K we find that the fraction of chemisorbed H (N_c/N) needs to be at least about 0.1 (see Sect. 6).

We note that formation by chemisorption can happen on the surface of big or small grains. In fact, the thermal fluctuations undergone by SGs after absorbing a UV photon are not sufficient to evaporate chemisorbed H atoms (binding energy around $10\,000$ K). Moreover, we estimate that the timescale for a physisorbed H to find a chemisorbed H is much less than the timescale of thermal fluctuations (see Sect. 5.1).

Since SGs make a dominant contribution to the total grain surface (see Sect. 6) and also because they may have numerous chemically bonded hydrogen atoms (because of their small

Table 2. Parameters for carbonaceous dust surface.

Parameter	Value	Ref.
E_d (K)	600	(1)
E_p (K)	500	(1)
E_a (K)	600–1000	(2)–(3, 4)
Δx (Å)	~2	(2)

E_d is the desorption energy of a physisorbed H atom; E_p is the activation barrier energy for physisorbed H diffusion; E_a and Δx are respectively the energy and the width of the activation barrier for recombination with a neighbouring chemisorbed H. Here, we assume that the barrier E_a for recombination to form H₂ is the same between a physisorbed and a chemisorbed site as for direct recombination from the gas phase.

References. (1) Katz et al. (1999); (2) Cazaux & Tielens (2003); (3) Fromherz et al. (1993); (4) Parneix & Brechignac (1998).

size they are more disordered), it is plausible that they play a dominant role in H₂ formation by chemisorption. However, if small grains contribute efficiently to H₂ formation, they must be continuously rehydrogenated : this could be the case for larger PAHs and VSGs for which the adsorbed H atoms should evaporate less after UV photon absorption because of the lower temperature fluctuations (see, e.g., Verstraete et al. 2001).

In the next section, we compare the H₂ formation rates as predicted by the different mechanisms discussed here and as derived from observations.

6. Comparison between the H₂ formation rate as predicted and as derived from observations

In this section, we see how the observational values of H₂ formation rate in PDRs fit and constrain H₂ formation mechanisms on grain surfaces.

First, based on the empirical formation probabilities given above, we estimate the rate of formation through chemisorption on small and big carbonaceous grains. The formation rate R_f (in cm³ s⁻¹) can be written as:

$$R_f = \frac{1}{2} \sigma v_H \times P_{H_2} \quad (7)$$

where σv_H is the collision frequency between H atoms (with mean velocity v_H) and grains and P_{H_2} the probability of formation (see Eqs. (3) and (5)). The mean cross section for collisions between grains and H atoms, σ (cm²), is given by $\langle \frac{n_{\text{grain}}(a)}{n_H} \pi a^2 \rangle$ with $n_{\text{grain}}(a)$ the grain density with radius between a and $a+da$. We assume a MRN size distribution with $\alpha = 3.5$ while the lower and upper limits of the grain radius are respectively $a_{\text{min}} = 4$ and $a_{\text{max}} = 100$ Å for SGs and $a_{\text{min}} = 0.01$ and $a_{\text{max}} = 0.1$ μm for BGs. Adopting uniform mass density $\rho = 2.25$ g cm⁻³ (typical value for graphite grains) and an grain/gas mass ratio G about 0.001² for SGs and 0.01 for BGs,

² The carbon locked up in SGs has an abundance of [C/H] ~ 10⁻⁴ inferred from comparison between observations of dust galactic emission and extinction with model calculations (Désert et al. 1990; Li & Draine 2001).

we estimate³: (i) for SGs, $\sigma v_H \sim 6 \times 10^{-16} \left(\frac{T_{\text{gas}}}{100 \text{ K}} \right)^{0.5}$ cm³ s⁻¹; (ii) for BGs, $\sigma v_H \sim 3 \times 10^{-16} \left(\frac{T_{\text{gas}}}{100 \text{ K}} \right)^{0.5}$ cm³ s⁻¹. Under these assumptions, we find that the collisions cross section is ~2 higher for SGs than for BGs and that there is enough grain area with SGs to make R_f larger than the standard H₂ formation rate. We assume the small dust abundance to be constant from one region to another although variations are expected. However, this assumption should not be critical for our approach which attempts with simple empirical models to see what type of H₂ formation processes are to a first order relevant in PDRs.

To calculate P_{H_2} , we adopt the following assumptions. Firstly, for the indirect chemisorption, the formation efficiency will depend on the sticking coefficient S which remains uncertain. Studies of the sticking of H on grain surfaces generally predicts that S is about 1 at low temperatures and decreases with increasing temperature to about 0.4–0.1 at $T_{\text{gas}} \sim 300$ K (Hollenbach & McKee 1979; Burke & Hollenbach 1983; Leitch-Devlin & Williams 1985; Buch & Zhang 1991). Here, we approximate S by $1/(1 + T_{\text{gas}}/400 \text{ K} + (T_{\text{gas}}/400 \text{ K})^2)$ from Burke & Hollenbach (1983) and Bertoldi (1997). Secondly, for the parameters of the physisorbed and chemisorbed sites, we assume typical values for carbonaceous grains which are summarized in Table 2. We treat the surface coverage of chemisorbed H atoms (N_c/N) as a free parameter. Further, we take N_c/N for SGs and BGs to be equal and constant although this fraction is likely to depend upon grain characteristics and physical conditions. This is not completely satisfactory but it gives some insight into this parameter which more detailed theories of these processes should attempt to fit. We find that $N_c/N \sim 0.1$ (see below) gives a reasonable fit to our PDR data. Finally, we take the probability to eject H₂, η , to be unity. This is based simply on the fact that ejecting the newly formed H₂ molecule (the desorption energy is ~0.05 eV, Katz et al. 1999; Cazaux & Tielens 2003) requires a small fraction of the available formation energy deposited in the grain (1.5 eV). Note that if we do not assume spontaneous desorption, the H₂ formed would stay on the surface for really low temperatures (below 10 K) since the temperature is not high enough to allow evaporation (see Cazaux & Tielens 2002, 2003).

For the purpose of comparison with the formation rates determined using PDR models (Sect. 3), we need to estimate dust temperatures in the PDRs of interest to us. In Table 3, we give the temperatures of SGs and BGs expected in the H⁰/H₂ transition zone, where the radiation field is given by $\chi \exp(-\tau)$ with τ the FUV dust opacity in the transition zone equal to about unity. For the big grains at thermal equilibrium, we have adopted the analytic expression of Hollenbach et al. (1991). For the small grains subject to thermal fluctuations, we list in Table 3 the temperatures for a graphite grain of radius 1.5 nm ($N(C) \approx 1600$). We have computed for each value of the radiation field the full temperature histogram and the values in Table 3 correspond to the median value of the time

³ We calculate σv_H with $v_H = \left(\frac{8kT_{\text{gas}}}{\pi m_H} \right)^{1/2}$ and $\sigma = \int_{a_{\text{min}}}^{a_{\text{max}}} \pi a^2 a^{-\alpha} da \times \frac{V_{\text{grain/gas}}}{\int_{a_{\text{min}}}^{a_{\text{max}}} \frac{4}{3} \pi a^3 a^{-\alpha} da}$ with $V_{\text{grain/gas}} = 1.4 m_H G/\rho$ the volume of grain per hydrogen nuclei.

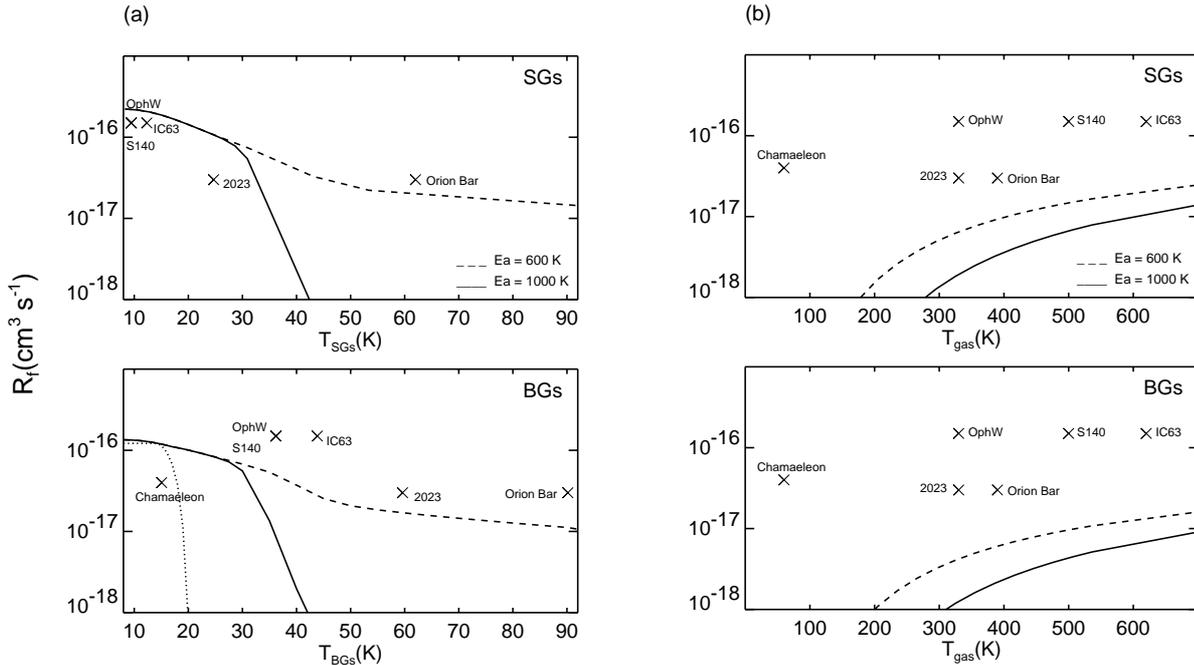


Fig. 5. Panel **a**): H₂ formation rate as predicted for the indirect chemisorption mechanism (solid and dashed lines) and for the pure Langmuir–Hinshelwood mechanism (dotted lines) and as observed (crosses, see Table 3) as a function of the dust temperature. The dust temperatures for Oph W and S140 derived are similar (see Table 3). The upper and lower panels show the rates predicted respectively for formation on small and big grains. The solid and dashed lines correspond respectively to E_a equal to 1000 and 600 K. Panel **b**): H₂ formation rate as predicted for the H₂ formation by direct chemisorption (solid and dashed lines) and as observed (crosses) as a function of the gas temperature. The “observed” gas temperatures are inferred from the distribution of low H₂ pure rotational levels reported in Table 1; for the Chamaeleon see Gry et al. (2002).

Table 3. Temperatures of dust and gas and H₂ formation rates.

Region	T_{SGs}^a (K)	T_{BGs}^a (K)	T_{gas}^b (K)	R_f^c (cm ³ s ⁻¹)
Chamaeleon	>2.7	15	60	4×10^{-17}
Oph W	10	36	330	1.5×10^{-16}
S140	10	36	500	1.5×10^{-16}
IC 63	12	44	620	1.5×10^{-16}
NGC 2023	25	60	330	3×10^{-17}
Orion Bar	62	90	390	3×10^{-17}

^a Temperature of the small grains (SGs) and big grains (BGs) expected in the H⁰/H₂ transition zone (see text in Sect. 6).

^b Gas temperature inferred from the distribution of low H₂ pure rotational levels (see Table 1). For the Chamaeleon see Gry et al. (2002).

^c H₂ formation rates derived from observations (see Sect. 3).

dependent temperature (i.e., the grain spends half of the time at temperature higher and lower than this value). The median temperature of small grains is unlike that of big grains not constrained by their emission spectrum. In these calculations, we used the absorption and emission cross section of bulk graphite from Draine & Lee (1984); the heat capacity is also of graphite given by Guhathakurta & Draine (1989). We have thus ignored quantum effects which might significantly change properties of these particles. This estimate of the small grain temperature is only indicative. Ideally, one should take into account the time dependence of the temperature as a function of the grain size.

Further, their emission properties might not allow then to cool down to the cosmic 2.7 K background temperature. Moreover, for very low temperatures (≤ 10 K), the heating due to the collisions between the grains and warm gas ($T_{gas} \geq 100$ K) or due to the formation of H₂ ($\sim 1/3$ of the formation energy is deposited in the grain) would increase the grain temperature. However, in the following we will use the SG temperatures reported in Table 3 in order to see if small grains are relevant for forming H₂. We find that the median temperatures of small grains are significantly lower than those of big grains. Indeed, SGs spend most of their time at low temperature (Guhathakurta & Draine 1989).

With the above formalism, we compute the formation rate R_f for the various processes outlined above on both SGs and BGs. The results are presented in Fig. 5, where we compare the H₂ formation rate predicted for indirect and direct chemisorption with the rates derived from observations. For completeness, we also show the results for the case of the pure Langmuir–Hinshelwood mechanism upon BGs using the model of Katz et al. (1999) based on experimental results for graphite surfaces (Pirronello et al. 1999).

First, we see from Fig. 5a that indirect chemisorption may explain the data for all sources if the activation barrier energy for recombination is $E_a \lesssim 1000$ K and if the fraction of chemisorbed H atoms is as large we have assumed, $N_c/N \sim 0.1$. This result is broadly consistent with the recent theoretical model of Cazaux & Tielens (2002, 2003), which accounts properly for the population of chemisorbed and physisorbed sites on

the surface. Thus, our estimate of the fraction of chemisorbed H atoms may be reasonable. However, the value of the activation barrier energy is uncertain and critically influences our estimate for R_f and the temperature range for which formation via indirect chemisorption is important. We find in fact that for $E_a \sim 1000$ K this process will be efficient until $T_{\text{dust}} \sim 30$ K (i.e., important in PDRs of relatively moderate excitation, $\chi < 5000$); for $T_{\text{dust}} > 30$ K the physisorbed H atoms evaporate before recombining. Conversely, for $E_a \sim 600$ K the formation via indirect chemisorption will be still efficient at $T_{\text{dust}} \sim 100$ K (i.e., important even in highly excited PDRs). In this last case, where the diffusion term dominates (see Sect. 5.2), the decreasing of R_f from moderate to highly excited PDRs is due to the competition between evaporation and finding the chemisorbed H atoms over the surface.

Secondly, we find that small grains which dominate the total grain area and spend most of their time at low temperature (< 30 K for $\chi \leq 3000$, see Table 3) may be the most promising surface for forming H₂ via indirect chemisorption. The H₂ formation on SGs can be effective even in highly excited PDRs where the equilibrium temperature of BGs can be too high to form H₂. In the case of SGs, we note that in most objects, the observed H₂ formation rates can be explained with a high value of E_a (~ 1000 K). For BGs, conversely a low value of E_a ($\lesssim 600$ K) is required. However, our description of the temperature of SGs is crude (median value of the temperature distribution for a single size of grain). As a consequence, we cannot quantitatively constrain the parameters (E_a , E_p , ...) of the H₂ formation process.

The direct or Eley–Rideal mechanism fails to explain the observations by a factor of a few (see Fig. 5b) although a higher N_c/N combined with a slightly lower E_a would suffice to explain some of the data. We cannot therefore exclude this mechanism but find that our present data suggest that the indirect chemisorption on SGs is more probable.

There are several complications which we have neglected in the above treatment. One is the possible presence of interstitial sites as suggested by Duley (1996) which can increase the efficiency of direct chemisorption. Another perhaps is H₂ formation through a reaction between two chemisorbed H atoms as suggested by Cazaux & Tielens (2002, 2003). This mechanism would be efficient at high dust temperatures ($\gtrsim 100$ K) and could be a possibility to explain the formation of H₂ in Orion.

In summary, we conclude that in order to explain the H₂ formation efficiency in PDRs, the indirect chemisorption mechanism upon small grains is the most promising. This requires an activation barrier energy between a physisorbed H atom and a neighbouring chemisorbed H atom $E_a \lesssim 1000$ K (or $\lesssim 0.1$ eV) and a fraction of occupied chemisorbed sites of around ten percent. This conclusion is consistent with our finding of a correlation between the H₂ and PAH emission which suggests that R_f scales with the PAH abundance (see Sect. 4). However, a better knowledge of the SGs properties (temperature, coverage of absorbed H atom, abundance ...) and of the mobilities of H atoms on realistic grain surfaces are critical.

7. Conclusion

The main aim of this study has been to provide estimates of the molecular hydrogen formation rate in a sample of nearby PDRs using results from both ISO and ground-based telescopes. The physical conditions in the PDR layers from which H₂ emission is observed ($n_{\text{H}} \approx 10^3\text{--}10^5$ cm⁻³, $T_{\text{gas}} \geq 300$ K) differ considerably from those in the diffuse clouds where one can observe the UV lines of H₂ ($n_{\text{H}} \approx 100\text{--}1000$ cm⁻³, $T_{\text{gas}} \approx 50\text{--}100$ K) and upon which most estimates of the molecular hydrogen formation rate have been based. Thus the results from PDRs allow important constraints to be placed upon the mechanisms for forming molecular hydrogen on grain surfaces. We confirm the earlier result of Habart et al. (2003) that the H₂ formation rate in regions of moderate excitation ($\chi \leq 1000$) such as Oph W, S140 and IC 63 is a factor of ~ 5 times larger than the standard rate estimated by Jura for diffuse clouds (and confirmed by recent FUSE data). On the other hand, towards regions of higher radiation field such as the Orion Bar and NGC 2023, we derive H₂ formation rates consistent with the standard value. Thus, the higher grain and gas temperatures in PDRs do not seem to impede the formation of H₂.

We have attempted to interpret these results with simple empirical models of the formation of H₂ on grain surfaces. From these, we conclude that an “indirect chemisorption” model analogous to that discussed by Cazaux & Tielens (2002, 2003) is capable of explaining the data. This result requires an activation barrier energy against the recombination of a physisorbed H atom and a neighbouring chemisorbed H atom $E_a \lesssim 0.1$ eV. Another condition appears to be that one needs an appreciable fraction of surface sites occupied (few percent at least) with a binding energy of order 1 eV relative to the total number of surface binding sites (presumably mainly physisorbed with binding energies of order 0.05 eV). Moreover, we suggest that small (size < 100 Å) grains may be the most promising surface for forming H₂ in PDRs. There is in fact enough grain surface in small grains to allow the formation rate to be larger than the standard H₂ formation rate and small grains spend most of their time at low temperature (Guhathakurta & Draine 1989). H₂ formation by indirect chemisorption upon small grains should be effective even in highly excited regions where large grains are quite warm.

Our results show that formation of molecular hydrogen in PDRs is likely to take place with a different mechanism than in the diffuse interstellar medium where the formation by physisorbed H atoms (Langmuir–Hinshelwood) probably dominates. In fact, in cold diffuse clouds the surface density of strongly bound H atoms should be low and consequently the formation by chemisorption would not be efficient.

There are several fundamental uncertainties in our present estimates of the H₂ formation rates in PDRs which future work should try to eliminate. One is due to the fact that we have used steady-state PDR models. This assumption can cause appreciable errors and it would be useful to calculate the expected H₂ line intensities for models with lower H₂ formation rates but where advection has been taken into account. However, Störzer & Hollenbach (1998) have modelled PDR structure assuming an ionization front moving into the PDR and found that

non-equilibrium effects are probably minor in objects similar to the Orion Bar.

Other uncertainties are of an observational nature. It would be useful to have reliable estimates of the inclination and density distribution in the PDRs of interest in order to better constrain the models. There are indications in the Orion Bar for instance (Walmsley et al. 2000) that the column density is higher in the molecular layers of the PDR than in the region (discussed in this paper) where the H₂ lines are formed. Density gradients perpendicular to the PDR photodissociation front clearly need to be taken into account when considering the spatial distribution of the various H₂ lines.

The theoretical models of H₂ formation discussed here are clearly very preliminary. More detailed models need to explicitly consider the degree of occupation of chemisorbed sites by H-atoms as well as the mobility of H atoms on various types of grain surfaces. Our results however do suggest that more detailed consideration of H₂ formation on the surface of small grains would be worthwhile. In this case, one should ideally follow the thermal fluctuations of these small particles and take into account the dependence on grain size in order to examine properly their contribution to H₂ formation. Clearly also our present estimates for processes such as tunneling are very crude.

Additional information on the H₂ formation process could probably be obtained using high quality data for H₂ in excited vibrational states which gives constraints on the excitation state of the newly formed H₂. It also would be useful to obtain estimates of the H₂ formation rate under a variety of different conditions. One such condition might be in the Magellanic clouds where the different metallicity, extinction curve, and radiation field potentially may influence both the available grain surface area and the efficiency of H₂ formation. Another is in the thin high excitation clouds such as that found by Meyer et al. (2001) towards the exciting star of NGC 2023. It is clear that given our uncertainty about grain compositions and size distributions in different ISM locations, one is forced to some extent to use the astrophysical data to guide our estimates of processes such as H₂ formation. This is perhaps philosophically not as satisfactory as the traditional approach of employing experimentally determined or theoretically calculated rates but it is likely that nature does not give us the choice.

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Appendix: Probability for the diffusion and recombination of a physisorbed H atom with a chemisorbed H atom

To calculate the probability $f = \frac{\tau_p^{-1}}{\tau_p^{-1} + \tau_{ev}^{-1}}$ (Eq. (6), see Sect. 5.2), we estimate the timescale τ_p for diffusion over the grain surface

followed by recombination and the timescale τ_{ev} for evaporation of the physisorbed H. The latter time scale is given by

$$\tau_{ev} = \nu_0^{-1} \exp\left(\frac{E_d}{kT_{dust}}\right) \quad (8)$$

with E_d the desorption energy of a physisorbed H and ν_0 the vibrational frequency of H in a physisorbed site typically of the order of 10^{12} s^{-1} . τ_p can be given by the sum of the time to find a neighboring site to a chemisorption site bearing a H atom, τ_m and of the time to recombine and form H₂, τ_{rec} . We assume that diffusion from one physisorbed site to another occurs by thermal hopping (Katz et al. 1999). The time to hop from one physisorbed site to the next is thus given by $\nu_0^{-1} \exp\left(\frac{E_p}{kT_{dust}}\right)$ with E_p the activation barrier energy for physisorbed H atom diffusion. The mobility is a random walk and considering that there are 4 neighboring sites for each chemisorbed site, we find that one needs approximately $(N/4N_c)^2$ steps to be adjacent to a filled chemisorbed site. Thus:

$$\tau_m = \left(\frac{N}{4N_c}\right)^2 \times \nu_0^{-1} \exp\left(\frac{E_p}{kT_{dust}}\right). \quad (9)$$

The physisorbed H atom must cross the activation barrier to recombine with the nearest chemisorbed H atom by either (i) thermal diffusion with a probability $f_{th} = \exp\left(-\frac{E_a}{kT_{dust}}\right)$ or by (ii) tunnelling with a probability $f_{tun} = \exp\left(-\frac{2\Delta x}{\hbar} (2m_H E_a)^{0.5}\right)$ (Messiah 1972) with Δx the width of the barrier. The recombination time scale can be approximated by

$$\tau_{rec} = \left(\frac{N}{4N_c}\right) \times \nu_0^{-1} \frac{1}{(f_{th} + f_{tun})}. \quad (10)$$

At high dust temperatures (above ~40 K) thermal diffusion dominates whereas at low temperature (below ~30 K) tunneling is more important.

There are many caveats to the above procedure. In particular, we note that considering the probability $\exp\left(-\frac{2\Delta x}{\hbar} (2m_H E_a)^{0.5}\right)$ for tunneling transmission through a single barrier is incorrect for relevant astrophysical surfaces which are not regular and need therefore to be modeled by a set of barriers as many as there are atoms. The tunneling probability we adopt is thus an upper limit. However, for the purpose of comparison with observationally determined rates, our approach allows us to see which of the H₂ formation processes considered in this study will dominate.

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