Cosmological constraints from Archeops


1 Centre de Recherche sur les Très Basses Températures, BP 166, 38042 Grenoble Cedex 9, France
2 Cardiff University, Physics Department, PO Box 913, 5, The Parade, Cardiff, CF24 3YB, UK
3 Physique Cosmique et Cosmologie, Collège de France, 11 Pl. M. Berthelot, 75231 Paris Cedex 5, France
4 Laboratoire de l’Accélérateur Linéaire, BP 34, Campus Orsay, 91898 Orsay Cedex, France
5 CEA-CE Saclay, DAPNIA, Service de Physique des Particules, Bât. 141, 91191 Gif-sur-Yvette Cedex, France
6 Laboratoire d’Astrophysique de l’Obs. Midi-Pyrénées, 14 avenue E. Belin, 31400 Toulouse, France
7 Institut d’Astrophysique Spatiale, Bât. 121, Université Paris XI, 91405 Orsay Cedex, France
8 California Institute of Technology, 105-24 Caltech, 1201 East California Blvd, Pasadena CA 91125, USA
9 Jet Propulsion Laboratory, 4800 Oak Grove Drive, Pasadena, California 91109, USA
10 IROE–CNR, Via Panciatichi, 64, 50127 Firenze, Italy
11 Institut d’Astrophysique de Paris, 98bis boulevard Arago, 75014 Paris, France
12 Gruppo di Cosmologia Sperimentale, Dipart. di Fisica, Univ. “La Sapienza”, P. A. Moro, 2, 00185 Roma, Italy
13 Laboratoire d’Astrophysique, Obs. de Grenoble, BP 53, 38041 Grenoble Cedex 9, France
14 Nuclear and Astrophysics Laboratory, Keble Road, Oxford, OX1 3RH, UK
15 CSNSM–IN2P3, Bât. 108, Campus Orsay, 91405 Orsay Cedex, France
16 Centre d’Étude Spatiale des Rayonnements, BP 4346, 31028 Toulouse Cedex 4, France
17 Institut des Sciences Nucléaires, 53 avenue des Martyrs, 38026 Grenoble Cedex, France
18 Infrared Processing and Analysis Center, Caltech, 770 South Wilson Avenue, Pasadena CA 91125, USA
19 School of Physics and Astronomy, 116 Church St. S.E., University of Minnesota, Minneapolis MN 55455, USA
20 Experimental Physics, National University of Ireland, Maynooth, Ireland
21 Landau Institute for Theoretical Physics, 119334 Moscow, Russia
22 Space Research Institute, Profsoyuznaya St. 84/32, Moscow, Russia
23 CEA-CE Saclay, DAPNIA, Service d’Astrophysique, Bât. 709, 91191 Gif-sur-Yvette Cedex, France
24 Fédération de Recherche APC, Université Paris 7, Paris, France
25 LERMA, Observatoire de Paris, 61 Av. de l’Observatoire, 75014 Paris, France

Received 16 October 2002 / Accepted 22 November 2002

Abstract. We analyze the cosmological constraints that Archeops (Benoît et al. 2003) places on adiabatic cold dark matter models with passive power-law initial fluctuations. Because its angular power spectrum has small bins in \( \ell \) and large \( \ell \) coverage down to COBE scales, Archeops provides a precise determination of the first acoustic peak in terms of position at multipole \( \ell_{\text{peak}} = 220 \pm 6 \), height and width. An analysis of Archeops data in combination with other CMB datasets constrains the baryon content of the Universe, \( \Omega_b h^2 = 0.022_{-0.003}^{+0.003} \), compatible with Big-Bang nucleosynthesis and with a similar accuracy. Using cosmological priors obtained from recent non–CMB data leads to yet tighter constraints on the total density, e.g. \( \Omega_m h^2 = 1.00_{-0.02}^{+0.03} \) using the HST determination of the Hubble constant. An excellent absolute calibration consistency is found between Archeops and other CMB experiments, as well as with the previously quoted best fit model. The spectral index \( n_s \) is measured to be \( 0.94_{-0.03}^{+0.03} \) when the optical depth to reionization, \( \tau \), is allowed to vary as a free parameter, and \( 0.96_{-0.04}^{+0.04} \) when \( \tau \) is fixed to zero, both in good agreement with inflation.

Key words. cosmic microwave background – cosmological parameters – early Universe – large–scale structure of the Universe

1. Introduction

A determination of the amplitude of the fluctuations of the cosmic microwave background (CMB) is one of the most
promising techniques to overcome a long standing problem in cosmology – setting constraints on the values of the cosmological parameters. Early detection of a peak in the region of the so-called first acoustic peak ($\ell \approx 200$) by the Saskatoon experiment (Netterfield et al. 1997), as well as the availability of fast codes to compute theoretical amplitudes (Seljak et al. 1996) has provided a first constraint on the geometry of the Universe (Lineweaver et al. 1997; Hancock et al. 1998). The spectacular results of Boomerang and Maxima have firmly established the fact that the geometry of the Universe is very close to flat (de Bernardis et al. 2000; Hanany et al. 2000; Lange et al. 2001; Balbi et al. 2000). Tight constraints on most cosmological parameters are anticipated from the Map (Bennett et al. 1997) and Planck (Tauber et al. 2000) satellite experiments. Although experiments have already provided accurate measurements over a wide range of $\ell$, degeneracies prevent a precise determination of some parameters using CMB data alone. For example, the matter content $\Omega_m$ cannot be obtained independently of the Hubble constant. Therefore, combinations with other cosmological measurements (such as supernovae, Hubble constant, and light element fractions) are used to break these degeneracies. Multiple constraints can be obtained on any given parameter by combining CMB data with anyone of these other measurements. It is also of interest to check the consistency between these multiple constraints. In this letter, we derive constraints on a number of cosmological parameters using the measurement of CMB anisotropy by the Archeops experiment (Benoît et al. 2003). This measurement provides the most accurate determination presently available of the angular power spectrum at angular scales of the first acoustic peak and larger.

2. Archeops angular power spectrum

The first results of the February 2002 flight of Archeops are detailed in Benoît et al. (2003). The band powers used in this analysis are plotted in Fig. 1 together with those of other experiments (CBDMVC for COBE, Boomerang, Dasi, Maxima, VSA, and CBI; Tegmark et al. 1996; Netterfield et al. 2002; Halverson et al. 2002; Lee et al. 2001; Scott et al. 2002; Pearson et al. 2002). Also plotted is a $\Lambda$CDM model (computed using CAMB, 2000), with the following parameters:

- $(\Omega_m, \Omega_{\Lambda}) = (0.3, 0.7)$
- $H_0 = 70$ km/s/Mpc
- $\Omega_b = 0.04$
- $\sigma_8 = 0.9$
- $n_s = 0.97$
- $\tau = 0.1$
- $\ln(10^{10}A_s) = 3.05$

The model is overplotted and appears to be in good agreement with all the data.
cosmological parameters: $\Theta = (\Omega_0, \Omega_m, \Omega_b h^2, h, n, Q, \tau)$ = (1.00, 0.7, 0.02, 0.70, 1.00, 18 $\mu K$, 0.), where the parameters are the total energy density, the energy density of a cosmological constant, the baryon density, the normalized Hubble constant ($H_0 = 100 h$ km s$^{-1}$ Mpc$^{-1}$), the spectral index of the scalar primordial fluctuations, the normalization of the power spectrum and the optical depth to reionization, respectively. The predictions of inflationary motivated adiabatic fluctuations, a plateau in the power spectrum at large angular scales followed by a first acoustic peak, are in agreement with the results from Archeops and from the other experiments. Moreover, the data from Archeops alone provides a detailed description of the power spectrum around the first peak. The parameters of the peak can be studied without a cosmological prejudice (Knox et al. 2000; Douspis & Ferreira 2002) by fitting a constant term, (error bars are smaller than the calibration uncertainty from Archeops only, because COBE amplitude is used for the constant term in the fit). This is the best determination of the parameters of the first peak to date, yet still compatible with other CMB experiments.

### 3. Model grid and likelihood method

To constrain cosmological models we constructed a $4.5 \times 10^5 C_\ell$ database. Only inflationary motivated models with adiabatic fluctuations are being used. The ratio of tensor to scalar modes is also set to zero. As the hot dark matter component modifies mostly large $\ell$ values of the power spectrum, this effect is neglected in the following. Table 1 describes the corresponding gridding used for the database. The models including reionization have been computed with an analytical approximation (Griffiths et al. 1999).

Cosmological parameter estimation relies upon the knowledge of the likelihood function $L$ of each band power estimate. Current Monte Carlo methods for the extraction of the $C_\ell$ naturally provide the distribution function $D$ of these power estimates. The analytical approach described in Douspis et al. (2003) and Bartlett et al. (2000) allows to construct the needed $L$ in an analytical form from $D$. Using such an approach was proven to be equivalent to performing a full likelihood analysis on the maps. Furthermore, this leads to unbiased estimates of the cosmological parameters (Wandelt et al. 2001; Bond et al. 2000; Douspis et al. 2001a), unlike other commonly used $\chi^2$ methods. In these methods, $L$ is also assumed to be Gaussian. However, this hypothesis is not valid, especially for the smaller modes covered by Archeops. The difference between our well-motivated shape and the Gaussian approximation induces a 10% error in width for large-scale bins. The parameters of the analytical form of the band power likelihoods $L$ have been computed from the distribution functions of the band powers listed in Table 1 of Benoît et al. (2003). Using $L$, we calculate the likelihood of any of the cosmological models in the database and maximize the likelihood over the 7% calibration uncertainty. We include the calibration uncertainty of each experiment as extra parameters in our analysis. The prior on these parameters are taken as Gaussians centered on unity, with a standard deviation corresponding to the quoted calibration uncertainty of each dataset. The effect of Archeops beam width uncertainty, which leads to less than 5% uncertainty on the $C_\ell$'s at $\ell \lesssim 350$, is neglected.

A numerical compilation of all the results is given in Table 2. Some of the results are also presented as 2D contour plots, showing in shades of blue the regions where the likelihood function for a combination of any two parameters drops to 68%, 95%, and 99% of its initial value. These levels are computed from the minimum of the negative of the log likelihood plus $\Lambda = 2.3, 6.17$ and 11.8. They would correspond to 1, 2, 3 $\sigma$ respectively if the likelihood function was Gaussian. Black contours mark the limits to be projected if confidence intervals are sought for any one of the parameters. To calculate either 1– or 2–D confidence intervals, the likelihood function is maximized over the remaining parameters. All single parameter confidence intervals that are quoted in the text are 1 $\sigma$ unless otherwise stated, and we use the notation $\chi^2_{\text{gen}} = m/n$ to mean that the generalized $\chi^2$ has a value $m$ with $n$ degrees of freedom. In all cases described below we find models that do fit the data and therefore confidence levels have a well defined statistical interpretation. Douspis et al. (2003) describes how to evaluate the goodness of fit and Table 2 gives the various $\chi^2$ values. When we use external non–CMB priors on some of the cosmological parameters, the analysis is done by multiplying our CMB likelihood hypercube by Gaussian shaped priors with mean and width according to the published values.

### 4. Cosmological parameter constraints

#### 4.1. Archeops

We first find constraints on the cosmological parameters using the Archeops data alone. The cosmological model that presents the best fit to the data has a $\chi^2_{\text{gen}} = 6/9$. Figure 3 gives confidence intervals on different pairs of parameters. The Archeops data constrain the total mass and energy density of the Universe ($\Omega_{\text{tot}}$) to be greater than 0.90, but it does not provide strong limits on closed Universe models. Figure 3 also shows that $\Omega_{\text{tot}}$ and $h$ are highly correlated (Douspis et al. 2001b). Adding the HST constraint for the Hubble constant, $H_0 = 72 \pm 8$ km s$^{-1}$ Mpc$^{-1}$ (68% CL, Freedman et al. 2001), leads to the tight constraint $\Omega_{\text{tot}} = 0.96^{+0.09}_{-0.04}$ (full line in Fig. 3), indicating that the Universe is flat.

Using Archeops data alone we can set significant constraints neither on the spectral index $n$ nor on the baryon content $\Omega_b h^2$ because of lack of information on fluctuations at small angular scales.
4.2. COBE, Archeops, CBI

We first combine only COBE/DMR, CBI and Archeops so as to include information over a broad range of angular scales, \(2 \leq \ell \leq 1500\), with a minimal number of experiments. The results are shown in Fig. 4, with a best model \(\chi^2_{\text{gen}} = 9/20\). The constraint on open models is stronger than previously, with a total density \(\Omega_{\text{tot}} = 1.0 \pm 0.2\) at 68% CL and \(\Omega_{\text{tot}} > 0.90\) at 95% CL. The inclusion of information about small scale fluctuations provides a constraint on the baryon content, \(\Omega_b h^2 = 0.019^{+0.008}_{-0.007}\) in good agreement with the results from BBN (O’Meara et al. 2001: \(\Omega_b h^2 = 0.0205 \pm 0.0018\)). The spectral index \(n = 1.06^{+0.11}_{-0.14}\) is compatible with a scale invariant Harrison–Zel’dovich power spectrum.

\footnote{For CBI data, we used only the joint mosaic band powers and restrict ourselves to \(\ell \leq 1500\).}

4.3. Archeops and other CMB experiments

By adding the experiments listed in Fig. 1 we now provide the best current estimate of the cosmological parameters using CMB data only. The constraints are shown in Figs. 5 and 6 (left). The combination of all CMB experiments provides...
Table 2. Cosmological parameter constraints from combined datasets. Upper and lower limits are given for 68% CL. See text for details on priors. The central values are given by the mean of the likelihood. The quoted error bars are at times smaller than the parameter grid spacing, and are thus in fact determined by an interpolation of the likelihood function between adjacent grid points.

<table>
<thead>
<tr>
<th>Data</th>
<th>Ωtot</th>
<th>n_s</th>
<th>Ω_bh²</th>
<th>h</th>
<th>Ω_L</th>
<th>τ</th>
<th>χ²_res/d.o.f.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Archeops</td>
<td>0.90</td>
<td>1.15</td>
<td>0.24</td>
<td>0.11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Archeops + COBE + CBI</td>
<td>1.16</td>
<td>0.11</td>
<td>0.02</td>
<td>0.11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>CMB</td>
<td>1.18</td>
<td>0.12</td>
<td>0.02</td>
<td>0.11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Archeops + CMB</td>
<td>1.16</td>
<td>0.11</td>
<td>0.02</td>
<td>0.11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Archeops + CMB + τ = 0</td>
<td>1.13</td>
<td>0.12</td>
<td>0.02</td>
<td>0.11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Archeops + CMB + Ω_tot = 1</td>
<td>1.00</td>
<td>0.11</td>
<td>0.02</td>
<td>0.11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Archeops + CMB + HST</td>
<td>1.00</td>
<td>0.11</td>
<td>0.02</td>
<td>0.11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Archeops + CMB + HST + τ = 0</td>
<td>1.00</td>
<td>0.11</td>
<td>0.02</td>
<td>0.11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Archeops + CMB + SN1a</td>
<td>1.04</td>
<td>0.11</td>
<td>0.02</td>
<td>0.11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Archeops + CMB + BBN</td>
<td>1.12</td>
<td>0.13</td>
<td>0.02</td>
<td>0.11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Archeops + CMB + BF(H)</td>
<td>1.11</td>
<td>0.13</td>
<td>0.02</td>
<td>0.11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Archeops + CMB + BF(L)</td>
<td>1.22</td>
<td>0.13</td>
<td>0.02</td>
<td>0.11</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

~10% errors on the total density, the spectral index and the baryon content respectively: Ωtot = 1.15^{+0.12}_{-0.17}, n = 1.04^{+0.10}_{-0.14} and Ω_bh² = 0.023^{+0.002}_{-0.003}. These results are in good agreement with recent analyses performed by other teams (Netterfield et al. 2002; Pryke et al. 2002; Rubino-Martin et al. 2002; Sievers et al. 2002; Wang et al. 2002). One can also note that the parameters of the ΛCDM model shown in Fig. 1 are included in the 68% CL contours of Fig. 6 (right).

As shown in Fig. 5, the spectral index and the optical depth are degenerate. Fixing the latter to its best fit value, τ = 0, leads to stronger constraints on both n and Ω_bh². With this constraint, the preferred value of n becomes slightly lower than 1, n = 0.96^{+0.03}_{-0.04}, and the constraint on Ω_bh² from CMB alone is not only in perfect agreement with BBN determination but also has similar error bars, Ω_bh²(CMB) = 0.021^{+0.002}_{-0.003}. It is important to note that many inflationary models (and most of the simplest of them) predict a value for n that is slightly less than unity (see, e.g., Linde 1990; Lyth & Riotto 1999 for a recent review).

4.4. Adding non-CMB priors

In order to break some degeneracies in the determination of cosmological parameters with CMB data alone, priors coming from other cosmological observations are now added. First we consider priors based on stellar candles like HST determination of the Hubble constant (Freedman et al. 2001) and supernovae determination of Ω_m and Λ (Perlmutter et al. 1999). We also consider non stellar cosmological priors like BBN determination of the baryon content, (O’Meara et al. 2001), and baryon fraction determination from X-ray clusters (Roussel et al. 2000; Sadat & Blanchard 2001). For the baryon fraction we use a low value, BF(L), f_b = 0.031h^{-3/2} ± 0.012 (±10%), and a high value, BF(H), f_b = 0.048h^{-3/2} ± 0.014 (±10%) (Douspis et al. 2001b and references therein). The results with the HST prior are shown in Fig. 6 (right). Considering the particular combination Archeops + CBDMVC + HST, the best fit model, with the Table 1 gridding, is (Ω_m, Ω_bh², h, n, Q, τ) = (1.00, 0.7, 0.02, 0.665, 0.945, 19.2K, 0.) with a χ²_res = 41/68.

The model is shown in Fig. 7 with the data scaled by their best-fit calibration factors which were simultaneously computed in the likelihood fitting process. The constraints on h break the degeneracy between the total matter content of the Universe and the amount of dark energy as discussed in Sect. 4.1. The constraints are then tighter as shown in Fig. 6 (right), leading to a value of Ω_L = 0.73 ±0.07 for the dark energy content, in agreement with supernovae measurements if a flat Universe is assumed. Table 2 also shows that Archeops + CBDMVC cosmological parameter determinations assuming either Ω_tot = 1 or the HST prior on h are equivalent at the 68% CL.

5. Conclusion

Constraints on various cosmological parameters have been derived by using the Archeops data alone and in combination with other measurements. The measured power at low ℓ is in agreement with the COBE data, providing for the first time a direct link between the Sachs–Wolfe plateau and the first acoustic peak. The Archeops data give a high signal-to-noise ratio determination of the parameters of the first acoustic peak and of the power spectrum down to COBE scales (ℓ = 15), because of the large sky coverage that greatly reduces the sample variance. The measured spectrum is in good agreement with that predicted by simple inflation models of scale–free adiabatic perturbations. Archeops on its own also sets a constraint on open models, Ω_m > 0.90 (68% CL). In combination with CBDMVC experiments, tight constraints are shown on cosmological parameters like the total density, the spectral index and the baryon content, with values of Ω_m = 1.13^{+0.12}_{-0.15} n = 0.96^{+0.03}_{-0.04} and Ω_bh² = 0.021^{+0.002}_{-0.003} respectively, all at 68% CL and assuming τ = 0. These results lend support to the inflationary paradigm. The addition of non-CMB constraints removes degeneracies between different parameters and allows to achieve a 10% precision on Ω_bh² and Ω_L and better than 5% precision on Ω_tot.
and $n$. Flatness of the Universe is confirmed with a high degree of precision: $\Omega_{\text{tot}} = 1.00^{+0.03}_{-0.02}$ (Archeops + CMB + HST).

Acknowledgements. The authors would like to thank the following institutes for funding and balloon launching capabilities: CNES (French space agency), PNC (French Cosmology Program), ASI (Italian Space Agency), PPARC, NASA, the University of Minnesota, the American Astronomical Society and a CMBNet Research Fellowship from the European Commission.

References